

# Direct CP violation in Cabibbo-favored charmed meson decays and $\epsilon'/\epsilon$ in $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ model

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**ABSTRACT:** Since the standard model contribution is virtually absent, any observation of direct CP violation in the Cabibbo-favored charmed meson decays would be evidence of new physics. In this paper, we conduct a quantitative study on direct CP violation in  $D^0 \rightarrow K^- \pi^+$ ,  $D_s^+ \rightarrow \eta \pi^+$  and  $D_s^+ \rightarrow \eta' \pi^+$  decays in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  gauge extension of the standard model. In the model, direct CP violation arises mainly from the interference between the decay amplitude coming from the SM left-left current operators and that from the right-right current operators induced by  $W_R^+$  gauge boson exchange. Interestingly, the strong phase between the two amplitudes is evaluable, since it stems from difference in QCD corrections to the left-left and right-right current operators, which is a short-distance QCD effect given by  $\sim (\alpha_s(M_{W_L}^2)/4\pi) \log(M_{W_R}^2/M_{W_L}^2)$ . We assess the maximal direct CP violation in the above decays in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model. Additionally, we present a correlation between direct CP violation in these modes and one in  $K \rightarrow \pi\pi$  decay parametrized by  $\epsilon'$ , since  $W_R^+$  gauge boson has a sizable impact on the latter.

**KEYWORDS:** CP violation, Heavy Quark Physics, Beyond Standard Model

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**1 Introduction**

In the standard model (SM), direct CP violation in the Cabibbo-favored charmed meson decays is highly suppressed at the level of  $\mathcal{O}(10^{-10})$  [1] because no multiple tree and/or penguin diagrams with different CP phases can interfere. Hence, if discovered, direct CP violation in these modes would immediately be a sign of new physics. This is in contrast to the singly-Cabibbo-suppressed decays, where tree and penguin diagrams in the SM interfere to yield direct CP violation, and also  $c \rightarrow s\bar{s}u$  and  $c \rightarrow d\bar{d}u$  processes interfere through long-distance effects and may lead to sizable direct CP violation in the SM [2]. In this paper, we conduct a quantitative study on direct CP violation in Cabibbo-favored charmed meson decays with no final-state  $K^0$ , namely,  $D^0 \rightarrow K^-\pi^+$ ,  $D_s^+ \rightarrow \eta\pi^+$  and  $D_s^+ \rightarrow \eta'\pi^+$  decays, in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  gauge extension of the SM. Here, the absence of final-state  $K^0$  ensures that Cabibbo-favored decay amplitudes do not interfere with doubly-Cabibbo-suppressed decay amplitudes via  $K^0$ - $\bar{K}^0$  mixing to induce SM contributions to direct CP violation [3, 4].

In the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model, the right-right current operators,  $(\bar{s}c)_{V+A}(\bar{u}d)_{V+A}$ , coming from  $W_R^+$  gauge boson exchange and the left-right current operators,  $(\bar{s}c)_{V\pm A}(\bar{u}d)_{V\mp A}$ , induced by  $W_L^+$ - $W_R^+$  mixing both contribute to the Cabibbo-favored decays. However, the Wilson coefficients for the latter are suppressed by  $\sim 2m_b/m_t \simeq 1/20$  compared to the former if the model naturally accommodates the bottom and top quark Yukawa couplings. Therefore, we assume throughout this paper that the contribution of the right-right current operators dominates over that of the left-right ones. As a support

for this assumption, we comment that the dominance of the right-right current contribution has been observed in the study [5] of direct CP violation in  $K \rightarrow \pi\pi$  decay in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model, where we have found that the right-right current contribution is larger by factor 5 than the left-right one, which indicates that although the hadronic matrix elements of the left-right operators are enhanced, this is insufficient to overcome the suppression of  $2m_b/m_t \simeq 1/20$  on their Wilson coefficients.

The hadronic matrix elements of the right-right current operators are simply the minus of those of the left-left current operators, due to parity symmetry of QCD. Nevertheless, the decay amplitude from the right-right current operators and that from the left-left ones acquire a non-trivial relative strong phase from difference in QCD corrections to the right-right and left-left current operators, which manifests itself as a difference between the ratio of the Wilson coefficients for  $(\bar{s}_\alpha c_\alpha)_{V+A}(\bar{u}_\beta d_\beta)_{V+A}$  and  $(\bar{s}_\alpha c_\beta)_{V+A}(\bar{u}_\beta d_\alpha)_{V+A}$  operators and the ratio of those for  $(\bar{s}_\alpha c_\alpha)_{V-A}(\bar{u}_\beta d_\beta)_{V-A}$  and  $(\bar{s}_\alpha c_\beta)_{V-A}(\bar{u}_\beta d_\alpha)_{V-A}$  operators ( $\alpha, \beta$  denote color indices) at a given renormalization scale. Ultimately, this difference is because the quark-gluon-quark- $W_L^+(W_R^+)$  box diagram in the fundamental theory contains terms proportional to  $\log M_{W_L}^2$  ( $\log M_{W_R}^2$ ), and hence the amount of QCD corrections to  $W_L^+$  and  $W_R^+$  gauge boson exchange diagrams differ by  $\sim (\alpha_s(M_{W_L}^2)/4\pi) \log(M_{W_R}^2/M_{W_L}^2)$ . Interestingly, this fact allows us to evaluate the relative strong phase, since the difference in QCD corrections at scales between  $\mu \sim M_{W_R}$  and  $\mu \sim M_{W_L}$  is a short-distance effect. Also, the scale-and-scheme-independent combinations [6] of Wilson coefficients and hadronic matrix elements for  $(\bar{s}_\alpha c_\alpha)_{V-A}(\bar{u}_\beta d_\beta)_{V-A}$  and  $(\bar{s}_\alpha c_\beta)_{V-A}(\bar{u}_\beta d_\alpha)_{V-A}$  operators can be estimated reliably with the diagrammatic approach with SU(3) flavor symmetry [7–11], which works successfully on the Cabibbo-favored charmed meson decays into two pseudoscalars [12, 18].<sup>1</sup>

Combining the strong phase thus evaluated and new CP-violating phases in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model, we assess the maximal direct CP violation in  $D^0 \rightarrow K^-\pi^+$ ,  $D_s^+ \rightarrow \eta\pi^+$  and  $D_s^+ \rightarrow \eta'\pi^+$  decays. Additionally, we investigate a correlation between direct CP violation in the above modes and one in  $K \rightarrow \pi\pi$  decay parametrized by  $\epsilon'$ . Previously, the authors have found [5] that  $W_R^+$  gauge boson in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model with ‘charge symmetry’ [19] has a sizable impact on  $\epsilon'/\epsilon$  because  $W_R^+$  exchange contributes to it at tree level. It has been further revealed that the model with  $\mathcal{O}(10)$  TeV  $W_R^+$  boson mass can account for the incompatibility between the experimental data on  $\epsilon'/\epsilon$  [20–22] and the upper bound on  $\epsilon'/\epsilon$  [23, 24] obtained with dual QCD approach and supported by lattice-based evaluations [25–30].<sup>2</sup> Therefore, it is of particular interest how  $\epsilon'/\epsilon$  and direct CP violation in Cabibbo-favored charmed meson decays are correlated in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model, and how the former constrains or predicts the latter.

This paper is organized as follows: In section 2, we briefly review the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  gauge extension of the SM. In section 3, we give the effective Hamiltonian for the Cabibbo-favored charmed meson decays. Section 4 presents our new results, where the diagrammatic amplitudes are reorganized in such a way that the decay amplitude coming from

<sup>1</sup>Earlier studies on the application of the diagrammatic approach with SU(3) flavor symmetry to charmed meson decays into two pseudoscalars are found in refs. [13, 14] and in refs. [15–17].

<sup>2</sup>For other works on new physics contributions to  $\epsilon'/\epsilon$ , see refs. [31–43].

Field	Lorentz SO(1, 3)	SU(3) <sub>C</sub>	SU(2) <sub>L</sub>	SU(2) <sub>R</sub>	U(1) <sub>B-L</sub>
$Q_L^i$	(2, 1)	<b>3</b>	<b>2</b>	<b>1</b>	1/3
$Q_R^{ci}$	(2, 1)	$\bar{\mathbf{3}}$	<b>1</b>	<b>2</b>	-1/3
$L_L^i$	(2, 1)	<b>1</b>	<b>2</b>	<b>1</b>	-1
$L_R^{ci}$	(2, 1)	<b>1</b>	<b>1</b>	<b>2</b>	1
$\Phi$	<b>1</b>	<b>1</b>	<b>2</b>	<b>2</b>	0
$\Delta_L$	<b>1</b>	<b>1</b>	<b>3</b>	<b>1</b>	2
$\Delta_R$	<b>1</b>	<b>1</b>	<b>1</b>	<b>3</b>	-2

**Table 1.** Matter content and charge assignments with  $i$  being generation indices.

the right-right current operators are expressed in terms of the ratio of the Wilson coefficients that is calculable in short-distance QCD, and the diagrammatic amplitudes. In section 5, we show the results of our analysis on direct CP violation in  $D^0 \rightarrow K^-\pi^+$ ,  $D_s^+ \rightarrow \eta\pi^+$  and  $D_s^+ \rightarrow \eta'\pi^+$  decays, including its correlation with  $\epsilon'/\epsilon$ . Section 6 summarizes the paper.

## 2 SU(2)<sub>L</sub> × SU(2)<sub>R</sub> × U(1)<sub>B-L</sub> model

We briefly describe the SU(2)<sub>L</sub> × SU(2)<sub>R</sub> × U(1)<sub>B-L</sub> gauge extension of the SM. Remind that charge symmetry [19] is not imposed, unlike ref. [5]. We summarize the matter content in table 1. SU(2)<sub>L</sub> × SU(2)<sub>R</sub> × U(1)<sub>B-L</sub> gauge interactions and Yukawa interactions of quarks are described as

$$\begin{aligned}
 -\mathcal{L} \supset & Q_L^{i\dagger} \bar{\sigma}_\mu \left( \frac{1}{2} g_L \sigma^a W_L^{a\mu} + \frac{1}{3} g_X X^\mu \right) Q_L^i + Q_R^{ci\dagger} \bar{\sigma}_\mu \left( -\frac{1}{2} g_R (\sigma^a)^T W_R^{a\mu} - \frac{1}{3} g_X X^\mu \right) Q_R^{ci} \\
 & + (Y_q)_{ij} Q_L^{i\dagger} \Phi \epsilon_s (Q_R^{cj})^* + (\tilde{Y}_q)_{ij} Q_L^{i\dagger} (\epsilon_g^T \Phi^* \epsilon_g) \epsilon_s (Q_R^{cj})^* + \text{H.c.}
 \end{aligned} \tag{2.1}$$

$\Delta_R$  acquires a VEV,  $v_R$ , to break SU(2)<sub>R</sub> × U(1)<sub>B-L</sub> → U(1)<sub>Y</sub>, and  $\Phi$  further gains a VEV,  $\langle \Phi \rangle = \text{diag}(v \sin \beta, v \cos \beta e^{i\alpha})$  with  $v \simeq 246$  GeV, to trigger the electroweak symmetry breaking. As a result, the charged SU(2)<sub>L</sub> gauge boson,  $W_L^+$ , and the charged SU(2)<sub>R</sub> gauge boson,  $W_R^+$ , mix and form two mass eigenstates  $W^+$ ,  $W'^+$  as

$$-\mathcal{L} \supset M_W^2 W^+ W^- + M_{W'}^2 W'^+ W'^-, \quad \begin{pmatrix} W_L^+ \\ W_R^+ \end{pmatrix} = \begin{pmatrix} \cos \zeta & -e^{-i\alpha} \sin \zeta \\ e^{i\alpha} \sin \zeta & \cos \zeta \end{pmatrix} \begin{pmatrix} W^+ \\ W'^+ \end{pmatrix}, \tag{2.2}$$

$$\sin \zeta \simeq \frac{g_R}{g_L} \frac{M_W^2}{M_{W'}^2} \sin(2\beta) \quad \text{for } M_{W'}^2 \gg M_W^2. \tag{2.3}$$

The up-type quark mass matrix,  $M_u$ , and the down-type one,  $M_d$ , are given by<sup>3</sup>

$$M_u = \frac{v}{\sqrt{2}} \left( \sin \beta Y_q + \cos \beta e^{-i\alpha} \tilde{Y}_q \right), \quad M_d = \frac{v}{\sqrt{2}} \left( \cos \beta e^{i\alpha} Y_q + \sin \beta \tilde{Y}_q \right), \tag{2.4}$$

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<sup>3</sup> $U_R^i \equiv \epsilon_s (U_R^{ci})^*$ ,  $D_R^i \equiv \epsilon_s (D_R^{ci})^*$ .

which are diagonalized as  $M_u = V_{uL}^\dagger \text{diag}(m_u, m_c, m_t) V_{uR}$  and  $M_d = V_{dL}^\dagger \text{diag}(m_d, m_s, m_b) V_{dR}$  with unitary matrices  $V_{uL}, V_{uR}, V_{dL}, V_{dR}$ . Then, we obtain the SM Cabibbo-Kobayashi-Maskawa matrix as  $V_L = V_{uL} V_{dL}^\dagger$ , and the corresponding flavor mixing matrix for right-handed quarks as  $V_R = V_{uR} V_{dR}^\dagger$ . From eq. (2.2), we find that the charged-current interactions are described by the following term in the unitary gauge:

$$\begin{aligned}
 -\mathcal{L} \supset & \frac{1}{\sqrt{2}} \bar{U}^i W^{+\mu} \gamma_\mu \{g_L(V_L)_{ij} \cos \zeta P_L + g_R(V_R)_{ij} e^{i\alpha} \sin \zeta P_R\} D^j \\
 & + \frac{1}{\sqrt{2}} \bar{U}^i W'^{+\mu} \gamma_\mu \{-g_L(V_L)_{ij} e^{-i\alpha} \sin \zeta P_L + g_R(V_R)_{ij} \cos \zeta P_R\} D^j + \text{H.c.} \quad (2.5)
 \end{aligned}$$

From eq. (2.4), it is clear that the top and bottom Yukawa couplings are derived without fine-tuning only when  $\tan \beta \simeq m_b/m_t$  holds, which, combined with eq. (2.3), gives  $\sin \zeta \simeq (2m_b/m_t)(g_R/g_L)(M_W^2/M_{W'}^2)$ . Then, one finds from eq. (2.5) that the Wilson coefficients for the left-right currents obtained by integrating out  $W^+$  are suppressed by  $2m_b/m_t$  compared to those for the right-right currents obtained by integrating out  $W'^+$ .

### 3 Effective Hamiltonian for Cabibbo-favored $\Delta C = 1$ process

The effective Hamiltonian for Cabibbo-favored  $\Delta C = 1$  process reads,

$$\mathcal{H}_{\text{eff}}^{\Delta C=1} = \sum_{i=1}^2 (C_i^{\text{LL}} Q_i^{\text{LL}} + C_i^{\text{RR}} Q_i^{\text{RR}}). \quad (3.1)$$

The operators above are defined as

$$\begin{aligned}
 Q_1^{\text{LL}} &= (\bar{s}_\alpha c_\beta)_{V-A} (\bar{u}_\beta d_\alpha)_{V-A}, & Q_2^{\text{LL}} &= (\bar{s}_\alpha c_\alpha)_{V-A} (\bar{u}_\beta d_\beta)_{V-A}, \\
 Q_1^{\text{RR}} &= (\bar{s}_\alpha c_\beta)_{V+A} (\bar{u}_\beta d_\alpha)_{V+A}, & Q_2^{\text{RR}} &= (\bar{s}_\alpha c_\alpha)_{V+A} (\bar{u}_\beta d_\beta)_{V+A}, \quad (3.2)
 \end{aligned}$$

where  $(\bar{q}q')_{V-A}$  and  $(\bar{q}q')_{V+A}$  stand for  $\bar{q}\gamma_\mu(1-\gamma_5)q'$  and  $\bar{q}\gamma_\mu(1+\gamma_5)q'$ , respectively, and  $\alpha, \beta$  denote QCD color indices.  $C_i^{\text{LL}} (i = 1, 2)$  in eq. (3.1) represents the SM contribution, while  $C_i^{\text{RR}}$  arises from  $W_R^+$  gauge boson exchange. In this paper, we neglect the left-right current operators  $(\bar{s}c)_{V\pm A} (\bar{u}d)_{V\mp A}$  induced by  $W_L^+ - W_R^+$  mixing, because the corresponding Wilson coefficients are suppressed by  $2m_b/m_t \simeq 1/20$  compared to  $C_i^{\text{RR}}$  if there is no fine-tuning in deriving the bottom quark Yukawa coupling.

The renormalization group equation (RGE) of the Wilson coefficients is divided into two pieces for chirality-flipped sectors. At leading order, it reads

$$\mu \frac{d}{d\mu} \vec{C}_{\text{LL}} = \gamma^{\text{T}} \vec{C}_{\text{LL}}, \quad \mu \frac{d}{d\mu} \vec{C}_{\text{RR}} = \gamma^{\text{T}} \vec{C}_{\text{RR}}, \quad \gamma = \begin{pmatrix} -2 & 6 \\ 6 & -2 \end{pmatrix} \frac{\alpha_s}{4\pi}, \quad (3.3)$$

where  $\vec{C}_{\text{LL}} = (C_1^{\text{LL}}, C_2^{\text{LL}})^T$ ,  $\vec{C}_{\text{RR}} = (C_1^{\text{RR}}, C_2^{\text{RR}})^T$ , and the anomalous dimension matrix  $\gamma$  is common for LL and RR sectors. The initial conditions for the RGE at leading order are

$$C_1^{\text{LL}}(\mu_W) = 0, \tag{3.4}$$

$$C_2^{\text{LL}}(\mu_W) = \frac{G_F}{\sqrt{2}} V_{cs}^{L*} V_{ud}^L, \tag{3.5}$$

$$C_1^{\text{RR}}(\mu_{W'}) = 0, \tag{3.6}$$

$$C_2^{\text{RR}}(\mu_{W'}) = \frac{G_F}{\sqrt{2}} V_{cs}^{R*} V_{ud}^R \left( \frac{g_R}{g_L} \frac{M_W}{M_{W'}} \right)^2, \tag{3.7}$$

with  $\mu_W \sim M_W, \mu_{W'} \sim M_{W'}$ . The RGE (3.3) is diagonalized in the basis of  $C_{\pm}^{\text{LL}} = C_1^{\text{LL}} \pm C_2^{\text{LL}}$  and  $C_{\pm}^{\text{RR}} = C_1^{\text{RR}} \pm C_2^{\text{RR}}$  so that the RG evolution is simply described without operator mixing.

#### 4 Decay amplitudes from right-right current operators

Hereafter, we exclusively work under the assumption of SU(3) flavor symmetry of  $u, d, s$  quarks. The amplitudes of charmed meson decays to two pseudoscalars ( $D \rightarrow PP$ ) can be categorized by diagrammatic topologies [12–18]. For the Cabibbo-favored  $D \rightarrow PP$  decays, the diagrammatic amplitudes consist of  $T$ (tree),  $C$ (color-suppressed tree),  $A$ (annihilation) and  $E$ (exchange) diagrams. In addition, ref. [6] has clarified the correspondence between the diagrammatic amplitudes and the scale-and-scheme-independent combinations of Wilson coefficients and operators.

For the left-left and right-right current contributions, the diagrammatic amplitudes are rewritten as

$$\begin{aligned} T_{\text{LL}} &= C_1^{\text{LL}}(\mu) \langle Q_1(\mu) \rangle_{\text{CE}} + C_2^{\text{LL}}(\mu) \langle Q_2(\mu) \rangle_{\text{DE}}, \\ T_{\text{RR}} &= -C_1^{\text{RR}}(\mu) \langle Q_1(\mu) \rangle_{\text{CE}} - C_2^{\text{RR}}(\mu) \langle Q_2(\mu) \rangle_{\text{DE}}, \end{aligned} \tag{4.1}$$

$$\begin{aligned} C_{\text{LL}} &= C_1^{\text{LL}}(\mu) \langle Q_1(\mu) \rangle_{\text{DE}} + C_2^{\text{LL}}(\mu) \langle Q_2(\mu) \rangle_{\text{CE}}, \\ C_{\text{RR}} &= -C_1^{\text{RR}}(\mu) \langle Q_1(\mu) \rangle_{\text{DE}} - C_2^{\text{RR}}(\mu) \langle Q_2(\mu) \rangle_{\text{CE}}, \end{aligned} \tag{4.2}$$

$$\begin{aligned} A_{\text{LL}} &= C_1^{\text{LL}}(\mu) \langle Q_1(\mu) \rangle_{\text{CA}} + C_2^{\text{LL}}(\mu) \langle Q_2(\mu) \rangle_{\text{DA}}, \\ A_{\text{RR}} &= -C_1^{\text{RR}}(\mu) \langle Q_1(\mu) \rangle_{\text{CA}} - C_2^{\text{RR}}(\mu) \langle Q_2(\mu) \rangle_{\text{DA}}, \end{aligned} \tag{4.3}$$

$$\begin{aligned} E_{\text{LL}} &= C_1^{\text{LL}}(\mu) \langle Q_1(\mu) \rangle_{\text{DA}} + C_2^{\text{LL}}(\mu) \langle Q_2(\mu) \rangle_{\text{CA}}, \\ E_{\text{RR}} &= -C_1^{\text{RR}}(\mu) \langle Q_1(\mu) \rangle_{\text{DA}} - C_2^{\text{RR}}(\mu) \langle Q_2(\mu) \rangle_{\text{CA}}, \end{aligned} \tag{4.4}$$

where  $\mu$  denotes a common renormalization scale for the Wilson coefficients and operators of both left-left and right-right currents.  $\langle Q_i(\mu) \rangle$  denotes a hadronic matrix element defined by  $\langle Q_i(\mu) \rangle = \langle PP | Q_i^{\text{LL}}(\mu) | D \rangle$ , whose subscript represents the connected emission (CE), the disconnected emission (DE), the connected annihilation (CA) and the disconnected annihilation (DA), respectively [6]. We have used  $\langle PP | Q_i^{\text{LL}}(\mu) | D \rangle = -\langle PP | Q_i^{\text{RR}}(\mu) | D \rangle$  ( $i = 1, 2$ ) that follows from parity conservation of QCD. We emphasize that each of  $T_{\text{LL}}, T_{\text{RR}}, C_{\text{LL}}, C_{\text{RR}}, A_{\text{LL}}, A_{\text{RR}}, E_{\text{LL}}, E_{\text{RR}}$  is independent of renormalization scale and scheme [6].

By rewriting  $Q_1^{\text{LL}}$  as  $(\bar{s}_\alpha d_\alpha)_{V-A}(\bar{u}_\beta c_\beta)_{V-A}$  through the Fierz rearrangement, we obtain the following relations based on SU(3) flavor symmetry of  $u, d, s$  quarks:

$$\langle Q_1(\mu) \rangle_{\text{CE}} = \langle Q_2(\mu) \rangle_{\text{CE}}, \quad (4.5)$$

$$\langle Q_1(\mu) \rangle_{\text{DE}} = \langle Q_2(\mu) \rangle_{\text{DE}}, \quad (4.6)$$

$$\langle Q_1(\mu) \rangle_{\text{CA}} = \langle Q_2(\mu) \rangle_{\text{CA}}, \quad (4.7)$$

$$\langle Q_1(\mu) \rangle_{\text{DA}} = \langle Q_2(\mu) \rangle_{\text{DA}}. \quad (4.8)$$

Henceforth, the subscripts of the operators are omitted. Using eqs. (4.5)–(4.8), we can re-express the diagrammatic amplitudes in terms of  $C_\pm^{\text{LL}} = C_1^{\text{LL}} \pm C_2^{\text{LL}}$  as

$$T_{\text{LL}} = C_+^{\text{LL}} \frac{\langle Q \rangle_{\text{CE}} + \langle Q \rangle_{\text{DE}}}{2} + C_-^{\text{LL}} \frac{\langle Q \rangle_{\text{CE}} - \langle Q \rangle_{\text{DE}}}{2}, \quad (4.9)$$

$$C_{\text{LL}} = C_+^{\text{LL}} \frac{\langle Q \rangle_{\text{CE}} + \langle Q \rangle_{\text{DE}}}{2} - C_-^{\text{LL}} \frac{\langle Q \rangle_{\text{CE}} - \langle Q \rangle_{\text{DE}}}{2}, \quad (4.10)$$

$$A_{\text{LL}} = C_+^{\text{LL}} \frac{\langle Q \rangle_{\text{CA}} + \langle Q \rangle_{\text{DA}}}{2} + C_-^{\text{LL}} \frac{\langle Q \rangle_{\text{CA}} - \langle Q \rangle_{\text{DA}}}{2}, \quad (4.11)$$

$$E_{\text{LL}} = C_+^{\text{LL}} \frac{\langle Q \rangle_{\text{CA}} + \langle Q \rangle_{\text{DA}}}{2} - C_-^{\text{LL}} \frac{\langle Q \rangle_{\text{CA}} - \langle Q \rangle_{\text{DA}}}{2}. \quad (4.12)$$

It follows that the right-right current contributions can be rewritten as

$$T_{\text{RR}} = -\frac{C_+^{\text{RR}}}{C_+^{\text{LL}}} \frac{T_{\text{LL}} + C_{\text{LL}}}{2} - \frac{C_-^{\text{RR}}}{C_-^{\text{LL}}} \frac{T_{\text{LL}} - C_{\text{LL}}}{2}, \quad (4.13)$$

$$C_{\text{RR}} = -\frac{C_+^{\text{RR}}}{C_+^{\text{LL}}} \frac{T_{\text{LL}} + C_{\text{LL}}}{2} + \frac{C_-^{\text{RR}}}{C_-^{\text{LL}}} \frac{T_{\text{LL}} - C_{\text{LL}}}{2}, \quad (4.14)$$

$$A_{\text{RR}} = -\frac{C_+^{\text{RR}}}{C_+^{\text{LL}}} \frac{A_{\text{LL}} + E_{\text{LL}}}{2} - \frac{C_-^{\text{RR}}}{C_-^{\text{LL}}} \frac{A_{\text{LL}} - E_{\text{LL}}}{2}, \quad (4.15)$$

$$E_{\text{RR}} = -\frac{C_+^{\text{RR}}}{C_+^{\text{LL}}} \frac{A_{\text{LL}} + E_{\text{LL}}}{2} + \frac{C_-^{\text{RR}}}{C_-^{\text{LL}}} \frac{A_{\text{LL}} - E_{\text{LL}}}{2}. \quad (4.16)$$

The ratio of the Wilson coefficients,  $C_\pm^{\text{RR}}/C_\pm^{\text{LL}}$ , in eqs. (4.13)–(4.16) is independent of renormalization scale and scheme. As a reference, we find, at the leading order,

$$\frac{C_\pm^{\text{RR}}(\mu)}{C_\pm^{\text{LL}}(\mu)} = (\eta_{\mu_{W'}}^{\mu_W})^{-\frac{\lambda_{0\pm}}{2\beta_0}} \left( \frac{g_R}{g_L} \frac{M_W}{M_{W'}} \right)^2 \frac{V_{cs}^{\text{R}*} V_{ud}^{\text{R}}}{V_{cs}^{\text{L}*} V_{ud}^{\text{L}}}, \quad (4.17)$$

where  $\lambda_{0+} = 4$ ,  $\lambda_{0-} = -8$ , and  $\beta_0 = 11 - 2n_f/3$  with  $n_f = 6$ , and we have defined the QCD correction factor as  $\eta_{\mu_2}^{\mu_1} = \alpha_s(\mu_1)/\alpha_s(\mu_2)$ . The next-leading order (NLO) QCD corrections to eq. (4.17) are found in eq. (A.1).

The diagrammatic amplitudes have been determined through a phenomenological fitting of  $D \rightarrow PP$  decay partial widths in ref. [12] (see also ref. [18]). In that study, an important assumption is that OZI-suppressed diagrams for  $D^0 \rightarrow \bar{K}^0 \eta$ ,  $D^0 \rightarrow \bar{K}^0 \eta'$ ,  $D_s^+ \rightarrow \pi^+ \eta$ ,  $D_s^+ \rightarrow \pi^+ \eta'$  decays are negligible in the partial widths. Also, the SU(3) flavor symmetry is assumed. These assumptions are justified for the Cabibbo-favored decays, since a good fit with  $\chi^2 = 1.79$  for 1 degree of freedom for fixed  $\eta - \eta'$  mixing angle is obtained in

that study.<sup>4</sup> In this paper, we employ the result of ref. [12] by fixing the  $\eta - \eta'$  mixing angle at  $19.5^\circ$ . Assuming that the contributions of the right-right current operators to the partial widths are negligible, one finds [12] (in  $10^{-6}$  GeV unit),  $T_{LL} = 2.927 \pm 0.022$ ,  $C_{LL} = (2.337 \pm 0.027) \exp[i(-151.66 \pm 0.63)^\circ]$ ,  $A_{LL} = (0.33 \pm 0.14) \exp[i(70.47 \pm 10.90)^\circ]$  and  $E_{LL} = (1.573 \pm 0.032) \exp[i(120.56 \pm 1.03)^\circ]$ .

## 5 Numerical analysis on direct CP violation

In the SM, direct CP violation in the Cabibbo-favored decays is generated via the interference between the tree diagram and the box and di-penguin diagrams [1]. CP asymmetry in  $D^0 \rightarrow K^- \pi^+$  decay rate is estimated to be  $1.4 \times 10^{-10}$  in ref. [1]. We infer that direct CP violation is suppressed similarly in all Cabibbo-favored modes, and therefore neglect the SM contribution in all modes. Provided the contribution of the right-right current is small, CP asymmetry in the decay rates can be expanded as

$$A_{CP}^{D \rightarrow f} = \frac{\Gamma[D \rightarrow f] - \Gamma[\bar{D} \rightarrow \bar{f}]}{\Gamma[D \rightarrow f] + \Gamma[\bar{D} \rightarrow \bar{f}]} \simeq \text{Re} \left[ \frac{(\mathcal{A}_f)_{RR}}{(\mathcal{A}_f)_{LL}} - \frac{(\bar{\mathcal{A}}_{\bar{f}})_{RR}}{(\bar{\mathcal{A}}_{\bar{f}})_{LL}} \right]. \quad (5.1)$$

The diagrammatic amplitude of each Cabibbo-favored decay is given in table 2. By using the relations eqs. (4.13)–(4.16) and the leading order expression for the Wilson coefficient ratio eq. (4.17), we find that the asymmetry takes a simple form,

$$A_{CP}^{D \rightarrow f} = F_{CP}^{D \rightarrow f} \left[ \left( \eta_{\mu_{W'}}^{\mu_W} \right)^{-\frac{2}{7}} - \left( \eta_{\mu_{W'}}^{\mu_W} \right)^{\frac{4}{7}} \right] \left( \frac{g_R}{g_L} \frac{M_W}{M_{W'}} \right)^2 \text{Im} \left( \frac{V_{cs}^{R*} V_{ud}^R}{V_{cs}^{L*} V_{ud}^L} \right), \quad (5.2)$$

where  $F_{CP}^{D \rightarrow f}$  is a process-dependent factor, which is summarized in table 2. The QCD correction factor and CP phase dependence in eq. (5.2) are common for all Cabibbo-favored modes. Note that  $A_{CP}^{D^0 \rightarrow \bar{K}^0 \pi^+}$  vanishes because  $T_{RR} + C_{RR}$  and  $T_{LL} + C_{LL}$  have an identical strong phase. In appendix A, NLO QCD corrections with the appropriate threshold corrections at the matching scales  $\mu_W$  and  $\mu_{W'}$ , which we use in the numerical analysis, are given.

In figure 1, maximal CP asymmetries in  $D^0 \rightarrow K^- \pi^+$ ,  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$  in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  are plotted by taking  $\text{Im} (V_{cs}^{R*} V_{ud}^R / V_{cs}^{L*} V_{ud}^L) = 1 / \cos^2 \theta_C$  ( $\theta_C$  denotes the SM Cabibbo angle). To estimate theoretical uncertainty, we have varied the matching scales  $\mu_W$  and  $\mu_{W'}$  in the range  $M_W/2 \leq \mu_W \leq 2M_W$  and  $M_{W'}/2 \leq \mu_{W'} \leq 2M_{W'}$ , respectively. Also, the  $1\sigma$  errors of the diagrammatic amplitudes in ref. [12] are considered as a source of uncertainty. We observe in figure 1 that the asymmetry is specially enhanced in  $D_s^+ \rightarrow \pi^+ \eta$  decay, due to the relatively large process-dependent factor. Note that we do not study the other Cabibbo-favored decays, because they include a final-state  $\bar{K}^0$  and are thus observed via  $K^0$ - $\bar{K}^0$  mixing. Hence, the amplitudes of Cabibbo-favored and doubly-Cabibbo-suppressed decays interfere to yield non-negligible CP asymmetry in the SM.

<sup>4</sup>A better fit has been found in ref. [48], where factorization-assisted topological-amplitude approach with the inclusion of SU(3) breaking effects is used.



In real experiments, one measures the difference of the CP asymmetries in two processes, to nullify asymmetry in the production cross sections at  $pp$  colliders or a slight asymmetry in the production kinematics at  $e^+e^-$  colliders (due to  $Z$ -photon interference), and asymmetry in the efficiency of charged meson detection. Consequently, most of the systematic uncertainties cancel. For the search for direct CP violation in Cabibbo-favored decays in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model, we suggest that one measure

$$A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}, \quad (5.3)$$

because the two asymmetries are predicted to have opposite signs in table 2 (note the signs of  $F_{\text{CP}}^{D \rightarrow f}$ ) and  $A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta}$  is sizable. Also, asymmetries in the  $D_s^\pm$  production and the  $\pi^\pm$  detection efficiency largely cancel between the two processes. In figure 2, we plot the maximal difference in the CP asymmetries in  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$  by again taking  $\text{Im}(V_{cs}^{\text{R}*} V_{ud}^{\text{R}} / V_{cs}^{\text{L}*} V_{ud}^{\text{L}}) = 1 / \cos^2 \theta_C$ . We comment that, as shown in appendix B, our prediction for the CP asymmetry difference eq. (5.3), which has been derived by assuming SU(3) flavor symmetry, is not much affected by SU(3) flavor symmetry breaking.

We make a crude estimate on the statistical uncertainty in a measurement of eq. (5.3) at Belle II with  $50 \text{ ab}^{-1}$  of data. Reference [44] reports that with  $791 \text{ fb}^{-1}$  of data at Belle, statistical uncertainty of the CP asymmetry in the number of reconstructed events  $(N_{\text{rec}}(D \rightarrow f) - N_{\text{rec}}(\bar{D} \rightarrow \bar{f})) / (N_{\text{rec}}(D \rightarrow f) + N_{\text{rec}}(\bar{D} \rightarrow \bar{f}))$  is 1.13% for  $D^+ \rightarrow \pi^+ \eta$  and 1.12% for  $D^+ \rightarrow \pi^+ \eta'$ . Assuming that the signal efficiencies (1.6%-1.7%) are the same for  $D^+ \rightarrow \pi^+ \eta(\prime)$  and  $D_s^+ \rightarrow \pi^+ \eta(\prime)$ , and using the branching ratios found in ref. [45], we estimate the statistical uncertainty at Belle II with  $50 \text{ ab}^{-1}$  of data to be  $\Delta(A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}) = 0.08\%$ . Next, we estimate the statistical uncertainty in a measurement of eq. (5.3) at LHCb with  $50 \text{ fb}^{-1}$  of data. Reference [46] reports that with  $1 \text{ fb}^{-1}$  of data at 7 TeV and  $2 \text{ fb}^{-1}$  of data at 8 TeV LHCb, the signal yield of  $D_s^\pm \rightarrow \pi^\pm \eta'$  processes is  $152 \times 10^3$ . Making a rough approximation that the signal yield with  $2 \text{ fb}^{-1}$  of data at 8 TeV is twice the yield with  $1 \text{ fb}^{-1}$  of data at 7 TeV, and performing a naïve rescaling of the number of events by  $\times 200$  based on ref. [47], the signal yield of  $D_s^\pm \rightarrow \pi^\pm \eta'$  processes with  $50 \text{ fb}^{-1}$  of data is estimated to be  $10^7$ . Further assuming that the signal efficiencies for  $D_s^\pm \rightarrow \pi^\pm \eta'$  and  $D_s^\pm \rightarrow \pi^\pm \eta$  are the same, the statistical uncertainty with  $50 \text{ fb}^{-1}$  of data is found to be  $\Delta(A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}) = 0.06\%$ . We find that if the  $SU(2)_R$  gauge coupling is enhanced as  $g_R = 2g_L$ , one may hope to discover direct CP violation in Cabibbo-favored decays even with  $M_{W'} = 4 \text{ TeV}$  (this parameter point is nearly consistent with the bound on  $Z'$  derived in refs. [49, 50]).

In figure 3, a correlated prediction for the CP asymmetry difference  $A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}$  and  $\text{Re}(\epsilon'/\epsilon)$  calculated in ref. [5] in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model is presented. Here, as with ref. [5], we impose ‘charge symmetry’ [19] on the model, which gives  $g_L = g_R$  and  $V_{ud}^{\text{R}} = (V_{ud}^{\text{L}})^* e^{-i\psi_d}$ ,  $V_{cs}^{\text{R}} = (V_{cs}^{\text{L}})^* e^{i(\phi_c - \psi_s)}$ ,  $V_{us}^{\text{R}} = (V_{us}^{\text{L}})^* e^{-i\psi_s}$  with  $\psi_d, \psi_s, \phi_c$  being arbitrary CP-violating phases. We thereby forbid ad hoc tuning of model parameters, rendering the model more predictive. In our calculation of  $\text{Re}(\epsilon'/\epsilon)$ , we have considered all contributions including those from the left-right current operators, unlike in our calculation of direct CP violation in  $D \rightarrow PP$  decays. In the plot,  $\psi_d, \psi_s, \phi_c$  and  $\alpha$

$D \rightarrow f$	$\mathcal{A}_f$	$F_{\text{CP}}^{D \rightarrow f}$	# of $F_{\text{CP}}^{D \rightarrow f}$
$D^+ \rightarrow \bar{K}^0 \pi^+$	$T + C$	0	0
$D^0 \rightarrow K^- \pi^+$	$T + E$	$\text{Im} \left[ \frac{C_{\text{LL}} + A_{\text{LL}}}{T_{\text{LL}} + E_{\text{LL}}} \right]$	$0.146 \pm 0.042$
$D^0 \rightarrow \bar{K}^0 \pi^0$	$(C - E)/\sqrt{2}$	$\text{Im} \left[ \frac{T_{\text{LL}} - A_{\text{LL}}}{C_{\text{LL}} - E_{\text{LL}}} \right]$	$0.958 \pm 0.030$
$D^0 \rightarrow \bar{K}^0 \eta$	$C/\sqrt{3}$	$\text{Im} \left[ \frac{T_{\text{LL}}}{C_{\text{LL}}} \right]$	$0.595 \pm 0.015$
$D^0 \rightarrow \bar{K}^0 \eta'$	$-(C + 3E)/\sqrt{6}$	$\text{Im} \left[ \frac{T_{\text{LL}} + 3A_{\text{LL}}}{C_{\text{LL}} + 3E_{\text{LL}}} \right]$	$-0.479 \pm 0.076$
$D_s^+ \rightarrow K^+ \bar{K}^0$	$C + A$	$\text{Im} \left[ \frac{T_{\text{LL}} + E_{\text{LL}}}{C_{\text{LL}} + A_{\text{LL}}} \right]$	$-0.213 \pm 0.072$
$D_s^+ \rightarrow \pi^+ \eta$	$(T - 2A)/\sqrt{3}$	$\text{Im} \left[ \frac{C_{\text{LL}} - 2E_{\text{LL}}}{T_{\text{LL}} - 2A_{\text{LL}}} \right]$	$-1.367 \pm 0.074$
$D_s^+ \rightarrow \pi^+ \eta'$	$2(T + A)/\sqrt{6}$	$\text{Im} \left[ \frac{C_{\text{LL}} + E_{\text{LL}}}{T_{\text{LL}} + A_{\text{LL}}} \right]$	$0.1726 \pm 0.039$

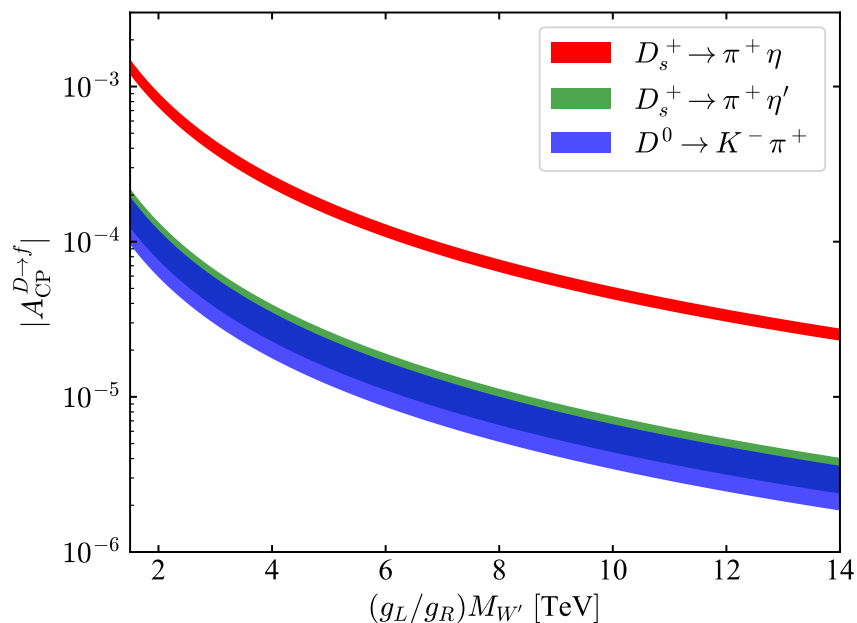
**Table 2.** Diagrammatic amplitudes [12], process-dependent factors for CP asymmetry, and their numerical values for Cabibbo-favored charmed meson decays. The uncertainty comes from the  $1\sigma$  errors of the diagrammatic amplitudes. Here, we fix the  $\eta - \eta'$  mixing angle at  $\arcsin(1/3)$ .

(which appears in eq. (2.2)) are randomly generated in the range  $[0, 2\pi]$ . We observe that when the experimental value of  $\text{Re}(\epsilon'/\epsilon)$  is naturally accounted for, the CP asymmetry difference is about  $10^{-6}$ . Conversely, to have  $A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}$  as large as  $10^{-4}$ , one must fine-tune the new CP-violating phases to satisfy the  $1\sigma$  range of  $\text{Re}(\epsilon'/\epsilon)$ .

We comment in passing that for  $W_R^+$  gauge boson in the  $\text{SU}(2)_L \times \text{SU}(2)_R \times \text{U}(1)_{B-L}$  model, the constraint from indirect CP violation in kaons,  $\text{Re}(\epsilon)$ , is mild compared to that from direct CP violation  $\text{Re}(\epsilon'/\epsilon)$ , because  $W_R^+$  gauge boson exchange contributes to the latter at tree level while it contributes to the former only at loop levels. However, it should be noted that unless the scalar potential is fine-tuned, the contribution from the heavy neutral scalar exchange to  $\text{Re}(\epsilon)$  is sizable, which is investigated in detail in refs. [51, 52].

## 6 Summary

We have studied the contribution of the right-right current operators in the  $\text{SU}(2)_L \times \text{SU}(2)_R \times \text{U}(1)_{B-L}$  model to direct CP violation in Cabibbo-favored charmed meson decays, for which the SM contribution is virtually absent. Interestingly, this contribution is evaluable, because it stems from difference in QCD corrections to the left-left current operators induced by  $W_L^+$  boson and the right-right ones induced by  $W_R^+$  boson, which is a short-distance effect  $\sim (\alpha_s(M_{W_L}^2)/4\pi) \log(M_{W_R}^2/M_{W_L}^2)$ . Combining a short-distance calculation of this difference with the result of the diagrammatic approach to the Cabibbo-favored decay amplitudes, we numerically evaluate the CP asymmetry in  $D^0 \rightarrow K^- \pi^+$ ,  $D_s^+ \rightarrow \pi^+ \eta$

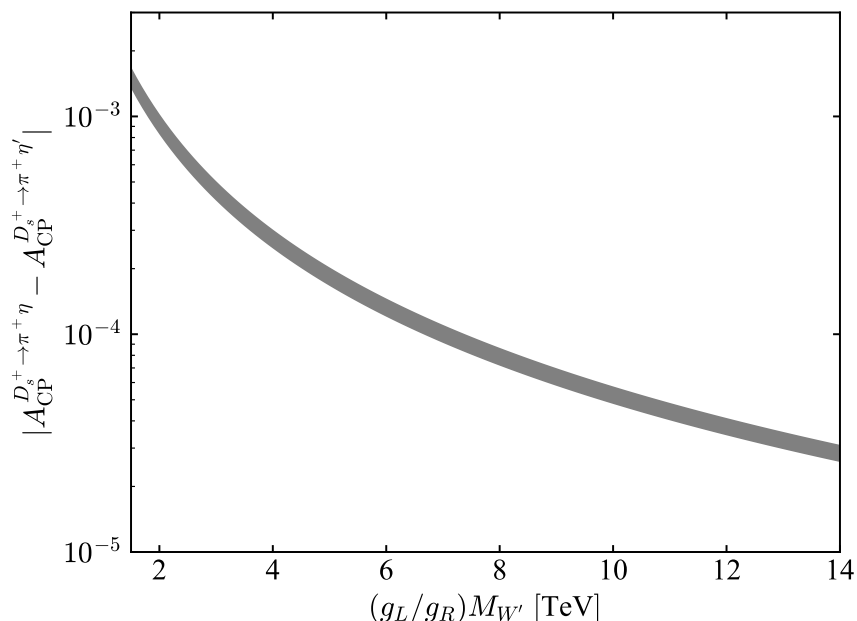


**Figure 1.** Absolute value of the maximal CP asymmetry of the partial width of Cabibbo-favored charmed meson decays in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model (without charge symmetry). The bands represent the combination of theoretical uncertainty evaluated by varying the matching scales as  $M_W/2 \leq \mu_W \leq 2M_W$  and  $M_{W'}/2 \leq \mu_{W'} \leq 2M_{W'}$ , and uncertainty from the  $1\sigma$  errors of the diagrammatic amplitudes.

and  $D_s^+ \rightarrow \pi^+ \eta'$  decay rates. We have found that the asymmetry in  $D_s^+ \rightarrow \pi^+ \eta$  is specially sizable, and further suggested the measurement of the difference in the CP asymmetries in  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$  decays. For  $M_{W'}$  (almost equal to  $M_{W_R}$ ) about 4 TeV and  $g_R = 2g_L$ , one may hope to observe this CP asymmetry difference at Belle II with  $50 \text{ ab}^{-1}$  of data or at LHCb with  $50 \text{ fb}^{-1}$  of data. Finally, we have presented a correlated prediction for the CP asymmetry difference in  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$  decays, and direct CP violation in  $K \rightarrow \pi\pi$  decay  $\text{Re}(\epsilon'/\epsilon)$ , under the assumption of ‘charge symmetry’ in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model. We have observed that if the experimental data on  $\text{Re}(\epsilon'/\epsilon)$  are naturally accounted for, the CP asymmetry difference in  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$  decays is as small as  $10^{-6}$ , and that a fine-tuning of the new CP-violating phases is mandatory to anticipate the discovery of direct CP violation in Cabibbo-favored charmed meson decays.

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**Figure 2.** Maximal difference in the CP asymmetry in  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$  in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model (without charge symmetry). The bands represent the combination of theoretical uncertainty evaluated by varying the matching scales as  $M_W/2 \leq \mu_W \leq 2M_W$  and  $M_{W'}/2 \leq \mu_{W'} \leq 2M_{W'}$ , and uncertainty from the  $1\sigma$  errors of the diagrammatic amplitudes.

## A NLO formulas

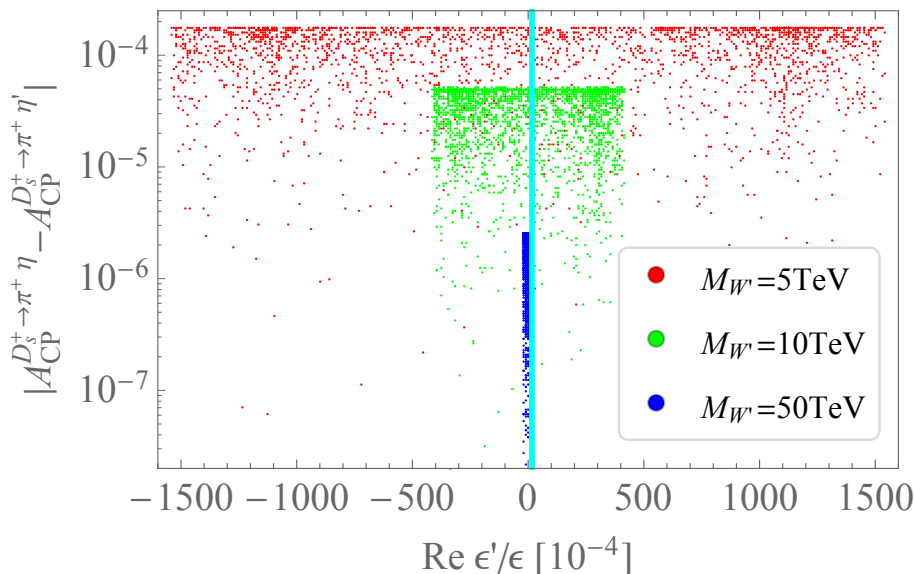
Here, we summarize NLO QCD corrections to the observables which are discussed in this paper. At NLO, the ratio of the Wilson coefficients in eq. (4.17) is modified to

$$\left. \frac{C_{\pm}^{LL}(\mu)}{C_{\pm}^{RR}(\mu)} \right|_{\text{NLO}} = U_{\pm}^{\text{NLO}} \left( \frac{g_R}{g_L} \frac{M_W}{M_{W'}} \right)^2 \frac{V_{cs}^{R*} V_{ud}^R}{V_{cs}^{L*} V_{ud}^L}, \quad (\text{A.1})$$

$$U_{\pm}^{\text{NLO}} = (\eta_{\mu_{W'}}^{\mu_W})^{-\frac{\lambda_{0\pm}}{2\beta_0}} \left[ 1 - \frac{\alpha_s(\mu_W)}{4\pi} \left( \frac{\beta_1 \lambda_{0\pm}}{2\beta_0^2} - \frac{\lambda_{1\pm}}{2\beta_0} + \frac{\lambda_{0\pm}}{2} \log \frac{M_W^2}{\mu_W^2} - B_{\pm} \right) \right] \\ \times \left[ 1 + \frac{\alpha_s(\mu_{W'})}{4\pi} \left( \frac{\beta_1 \lambda_{0\pm}}{2\beta_0^2} - \frac{\lambda_{1\pm}}{2\beta_0} + \frac{\lambda_{0\pm}}{2} \log \frac{M_{W'}^2}{\mu_{W'}^2} - B_{\pm} \right) \right], \quad (\text{A.2})$$

where  $\beta_1$  is the six-flavor NLO QCD  $\beta$  function coefficient,  $\lambda_{1\pm}$  are the NLO  $\gamma$  function coefficients for  $C_{\pm}^{LL}$  and  $C_{\pm}^{RR}$ , and  $B_{\pm}$  are constants (see, e.g., ref. [53]). Note that each of  $\lambda_{1\pm}$  and  $B_{\pm}$  is renormalization-scheme-dependent, but their scheme dependences cancel. Thus at NLO, the CP asymmetry in eq. (5.2) is

$$A_{\text{CP}}^{D \rightarrow f}|_{\text{NLO}} = F_{\text{CP}}^{D \rightarrow f} [U_+^{\text{NLO}} - U_-^{\text{NLO}}] \left( \frac{g_R}{g_L} \frac{M_W}{M_{W'}} \right)^2 \text{Im} \left( \frac{V_{cs}^{R*} V_{ud}^R}{V_{cs}^{L*} V_{ud}^L} \right). \quad (\text{A.3})$$



**Figure 3.** Correlated prediction for difference in the CP asymmetry in  $D_s^+ \rightarrow \pi^+ \eta$  and  $D_s^+ \rightarrow \pi^+ \eta'$ , and  $\text{Re}(\epsilon'/\epsilon)$ , in the  $SU(2)_L \times SU(2)_R \times U(1)_{B-L}$  model with charge symmetry. The red, green and blue dots represent the parameter points with randomly generated values of new CP violating phases for  $M_{W'} = 5 \text{ TeV}$ ,  $10 \text{ TeV}$  and  $50 \text{ TeV}$ , respectively. The cyan band stands for the  $1\sigma$  range of the experimental value of  $\text{Re}(\epsilon'/\epsilon)$  [45].

### B Effect of SU(3) flavor symmetry breaking

We study the effect of SU(3) flavor symmetry breaking on our prediction, which is not discussed in the main text. Our prediction of CP asymmetries depends crucially on V-spin symmetry (symmetry of  $u$  and  $s$ , which is part of SU(3) flavor symmetry), since our prediction is derived from eqs. (4.5)–(4.8), which are obtained by assuming V-spin. In particular, the isospin symmetry cannot lead to the above results. The effect of V-spin breaking on eqs. (4.5)–(4.8) is estimated to be simply  $f_K/f_\pi - 1 \simeq 0.2$ . This is in contrast to singly-Cabibbo-suppressed decays, where SU(3) breaking gives rise to corrections of order  $(f_K/f_\pi)^2 - 1 \simeq 0.4$  in factorized tree amplitudes, and also enhances penguin amplitudes (suppressed by  $V_{cb}V_{ub}^*$  in the SU(3) limit) leading to a further splitting of  $c \rightarrow d\bar{d}u$ -induced amplitudes and  $c \rightarrow s\bar{s}u$ -induced amplitudes [54]; all these effects are absent in the Cabibbo-favored decays.

Let us see how corrections of order  $f_K/f_\pi - 1 \simeq 0.2$  to eqs. (4.5)–(4.8) affect our prediction of CP asymmetries. First we concentrate on  $T$ (tree) and  $C$ (color-suppressed tree) diagrams. When eqs. (4.5), (4.6) are not valid,  $T_{LL}$  and  $C_{LL}$  are written as

$$T_{LL} = C_+^{LL} \frac{\langle Q_1 \rangle_{CE} + \langle Q_2 \rangle_{DE}}{2} + C_-^{LL} \frac{\langle Q_1 \rangle_{CE} - \langle Q_2 \rangle_{DE}}{2}, \tag{B.1}$$

$$C_{LL} = C_+^{LL} \frac{\langle Q_2 \rangle_{CE} + \langle Q_1 \rangle_{DE}}{2} - C_-^{LL} \frac{\langle Q_2 \rangle_{CE} - \langle Q_1 \rangle_{DE}}{2}. \tag{B.2}$$

The first and second terms on the right-hand side of eqs. (B.1), (B.2) are individually renormalization-scale-and-scheme independent. Therefore, we can parametrize the V-spin breaking effects in terms of renormalization-scale-and-scheme independent parameters  $\epsilon_{E+}$  and  $\epsilon_{E-}$  as

$$C_+^{\text{LL}} \frac{\langle Q_1 \rangle_{\text{CE}} + \langle Q_2 \rangle_{\text{DE}}}{2} = C_+^{\text{LL}} \frac{\langle Q_2 \rangle_{\text{CE}} + \langle Q_1 \rangle_{\text{DE}}}{2} (1 + \epsilon_{E+}), \quad (\text{B.3})$$

$$C_-^{\text{LL}} \frac{\langle Q_1 \rangle_{\text{CE}} - \langle Q_2 \rangle_{\text{DE}}}{2} = C_-^{\text{LL}} \frac{\langle Q_2 \rangle_{\text{CE}} - \langle Q_1 \rangle_{\text{DE}}}{2} (1 + \epsilon_{E-}), \quad (\text{B.4})$$

where we estimate the V-spin breaking parameters as  $|\epsilon_{E+}| \sim |\epsilon_{E-}| \sim f_K/f_\pi - 1 \simeq 0.2$ . In the leading order of  $\epsilon_{E+}, \epsilon_{E-}$ , we find

$$T_{\text{LL}} + (1 + \epsilon_{E-})C_{\text{LL}} = C_+^{\text{LL}} (\langle Q_2 \rangle_{\text{CE}} + \langle Q_1 \rangle_{\text{DE}}) (1 + \epsilon_{E-}/2 + \epsilon_{E+}/2), \quad (\text{B.5})$$

$$T_{\text{LL}} - (1 + \epsilon_{E+})C_{\text{LL}} = C_-^{\text{LL}} (\langle Q_2 \rangle_{\text{CE}} - \langle Q_1 \rangle_{\text{DE}}) (1 + \epsilon_{E-}/2 + \epsilon_{E+}/2). \quad (\text{B.6})$$

Consequently,  $T_{\text{RR}}$  and  $C_{\text{RR}}$  can be expressed in terms of  $T_{\text{LL}}, C_{\text{LL}}$  and the V-spin breaking parameters as

$$T_{\text{RR}} = -\frac{C_+^{\text{RR}} T_{\text{LL}} (1 + \epsilon_{E+}/2 - \epsilon_{E-}/2) + C_{\text{LL}} (1 + \epsilon_{E+}/2 + \epsilon_{E-}/2)}{C_+^{\text{LL}}} - \frac{C_-^{\text{RR}} T_{\text{LL}} (1 - \epsilon_{E+}/2 + \epsilon_{E-}/2) - C_{\text{LL}} (1 + \epsilon_{E+}/2 + \epsilon_{E-}/2)}{C_-^{\text{LL}}}, \quad (\text{B.7})$$

$$C_{\text{RR}} = -\frac{C_+^{\text{RR}} T_{\text{LL}} (1 - \epsilon_{E+}/2 - \epsilon_{E-}/2) + C_{\text{LL}} (1 - \epsilon_{E+}/2 + \epsilon_{E-}/2)}{C_+^{\text{LL}}} + \frac{C_-^{\text{RR}} T_{\text{LL}} (1 - \epsilon_{E+}/2 - \epsilon_{E-}/2) - C_{\text{LL}} (1 + \epsilon_{E+}/2 - \epsilon_{E-}/2)}{C_-^{\text{LL}}}. \quad (\text{B.8})$$

We obtain analogous expressions for  $A_{\text{RR}}$  and  $E_{\text{RR}}$ , with  $\epsilon_{E+}, \epsilon_{E-}$  replaced with different V-spin breaking parameters  $\epsilon_{A+}, \epsilon_{A-}$ . The above V-spin breaking corrections solely affect the factor  $F_{\text{CP}}^{D \rightarrow f}$  in the formula for CP asymmetry eq. (5.2). For the phenomenologically interesting modes  $D_s^+ \rightarrow \pi^+ \eta$ ,  $D_s^+ \rightarrow \pi^+ \eta'$  and  $D^0 \rightarrow K^- \pi^+$ , this factor is altered from table 2 to

$$F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} = \text{Im} \left[ \frac{C_{\text{LL}} - 2E_{\text{LL}}}{T_{\text{LL}} - 2A_{\text{LL}}} \right] + \text{Im} \left[ \frac{C_{\text{LL}} (\epsilon_{E+}/2 + \epsilon_{E-}/2) - 2E_{\text{LL}} (\epsilon_{A+}/2 + \epsilon_{A-}/2)}{T_{\text{LL}} - 2A_{\text{LL}}} \right] + \text{Im} \left[ \frac{T_{\text{LL}} (\epsilon_{E+}/2 - \epsilon_{E-}/2) - 2A_{\text{LL}} (\epsilon_{A+}/2 - \epsilon_{A-}/2)}{T_{\text{LL}} - 2A_{\text{LL}}} \right], \quad (\text{B.9})$$

$$F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'} = \text{Im} \left[ \frac{C_{\text{LL}} + E_{\text{LL}}}{T_{\text{LL}} + A_{\text{LL}}} \right] + \text{Im} \left[ \frac{C_{\text{LL}} (\epsilon_{E+}/2 + \epsilon_{E-}/2) + E_{\text{LL}} (\epsilon_{A+}/2 + \epsilon_{A-}/2)}{T_{\text{LL}} + A_{\text{LL}}} \right] + \text{Im} \left[ \frac{T_{\text{LL}} (\epsilon_{E+}/2 - \epsilon_{E-}/2) + A_{\text{LL}} (\epsilon_{A+}/2 - \epsilon_{A-}/2)}{T_{\text{LL}} + A_{\text{LL}}} \right], \quad (\text{B.10})$$

$$F_{\text{CP}}^{D^0 \rightarrow K^- \pi^+} = \text{Im} \left[ \frac{C_{\text{LL}} + A_{\text{LL}}}{T_{\text{LL}} + E_{\text{LL}}} \right] + \text{Im} \left[ \frac{C_{\text{LL}} (\epsilon_{E+}/2 + \epsilon_{E-}/2) + A_{\text{LL}} (-\epsilon_{A+}/2 - \epsilon_{A-}/2)}{T_{\text{LL}} + E_{\text{LL}}} \right] + \text{Im} \left[ \frac{T_{\text{LL}} (\epsilon_{E+}/2 - \epsilon_{E-}/2) + E_{\text{LL}} (-\epsilon_{A+}/2 + \epsilon_{A-}/2)}{T_{\text{LL}} + E_{\text{LL}}} \right]. \quad (\text{B.11})$$

Depending on the phases of V-spin breaking parameters  $\epsilon_{E+}, \epsilon_{E-}, \epsilon_{A+}, \epsilon_{A-}$ , the second and third terms of eqs. (B.9)–(B.11) can be enhanced far beyond  $f_K/f_\pi - 1 \simeq 0.2$ . However, as we will show below, the most promising observable,  $A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}$ , is not much affected by the V-spin breaking. To see this, note that this observable is proportional to  $F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}$ . Since  $|A_{\text{LL}}|$  is small, it can be approximated as

$$F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'} = \text{Im} \left[ \frac{C_{\text{LL}} - 2E_{\text{LL}}}{T_{\text{LL}} - 2A_{\text{LL}}} \right] - \text{Im} \left[ \frac{C_{\text{LL}} + E_{\text{LL}}}{T_{\text{LL}} + A_{\text{LL}}} \right] \quad (\text{B.12})$$

$$- 3 \text{Im} \left[ \frac{E_{\text{LL}}(\epsilon_{A+}/2 + \epsilon_{A-}/2)}{T_{\text{LL}}} \right] - 3 \text{Im} \left[ \frac{A_{\text{LL}}(\epsilon_{A+}/2 - \epsilon_{A-}/2)}{T_{\text{LL}}} \right]$$

$$= -1.54 - 3 \text{Im} \left[ \frac{E_{\text{LL}}(\epsilon_{A+}/2 + \epsilon_{A-}/2)}{T_{\text{LL}}} \right] - 3 \text{Im} \left[ \frac{A_{\text{LL}}(\epsilon_{A+}/2 - \epsilon_{A-}/2)}{T_{\text{LL}}} \right], \quad (\text{B.13})$$

where the first term  $-1.54$  is the prediction in the V-spin limit, while the second and third terms represent V-spin breaking effects. The second term is at most  $\pm 3|E_{\text{LL}}/T_{\text{LL}}|(f_K/f_\pi - 1) \simeq \pm 0.32$  and the third term is at most  $\pm 3|A_{\text{LL}}/T_{\text{LL}}|(f_K/f_\pi - 1) \simeq \pm 0.07$ . Thus, we conclude that the V-spin breaking corrections do not significantly change our prediction of  $F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - F_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}$  and hence of  $A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta} - A_{\text{CP}}^{D_s^+ \rightarrow \pi^+ \eta'}$ .

We note in passing that the fitted values of  $T_{\text{LL}}, C_{\text{LL}}, E_{\text{LL}}, A_{\text{LL}}$  in ref. [12], which we have adopted throughout the paper, are themselves obtained under the assumption of SU(3) flavor symmetry, but we expect that the SU(3) breaking effects are properly reflected in the errors of the fitted values.

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