Published for SISSA by 🖄 Springer

RECEIVED: April 29, 2024 REVISED: July 26, 2024 ACCEPTED: September 2, 2024 PUBLISHED: September 18, 2024

# Exploring interference effects between two ALP effective operators at the LHC

Kingman Cheung<sup>(D)</sup>,<sup>*a,b,c*</sup> Chih-Ting Lu<sup>(D)</sup>,<sup>*d*</sup> C.J. Ouseph<sup>(D)</sup>,<sup>*b*</sup> and Priyanka Sarmah<sup>(D)</sup>,<sup>*b*</sup>

- <sup>a</sup>Department of Physics, National Tsing Hua University, Hsinchu 30013, Taiwan
- <sup>b</sup>Center for Theory and Computation, National Tsing Hua University, Hsinchu 30013, Taiwan
- <sup>c</sup>Division of Quantum Phases and Devices, School of Physics, Konkuk University, Seoul 143-701, Republic of Korea
- <sup>d</sup>Department of Physics and Institute of Theoretical Physics, Nanjing Normal University, Nanjing, 210023, P.R. China

*E-mail:* cheung@phys.nthu.edu.tw, ctlu@njnu.edu.cn, ouseph444@gmail.com, sarmahpriyanka@gapp.nthu.edu.tw

ABSTRACT: We observe that most studies of axion-like particle (ALP) production channels at the Large Hadron Collider (LHC) focus on a single type of ALP operator for each process in the effective field theory framework. In this work, we propose an alternative approach that considers two or more types of relevant ALP effective operators together in some specific ALP production channels and study their interference effects. Using the  $pp \rightarrow tja$  process with  $a \rightarrow \gamma \gamma$  as an example, we show that this approach allows us to constrain the ALP interactions with both the W boson and the top quark, as well as their interference in a single process. For the final state with two isolated photons and a top quark decaying semi-leptonically, we predict that the future bounds on the ALP decay constant can reach around  $f_a \sim 10$  (20) TeV for 25 GeV  $< M_a < 100$  GeV at the LHC with 300 (3000) fb<sup>-1</sup> luminosity.

KEYWORDS: Axions and ALPs, New Gauge Interactions

ARXIV EPRINT: 2404.14833



# Contents

1	Introduction	]
<b>2</b>	Theoretical setup	2
3	Production and interference effects in $pp \rightarrow taX$ processes	3
4	Experimental setup and simulations	6
	4.1 Signal and relevant SM background processes	6
	4.2 Event selections	7
5	Numerical results	ç
6	Conclusions	12

#### 1 Introduction

Axion-like particles (ALPs) are hypothetical particles that arise in several extensions of the Standard Model (SM) of particle physics as pseudo-Goldstone bosons with a shift symmetry [1–10]. They are characterized by a low mass and a weak coupling to ordinary matter, which makes them difficult to detect. However, their existence is predicted by various theories that attempt to solve some of the outstanding problems in physics, such as the strong CP problem [11–17], the nature of dark matter [18, 19] and experimental anomalies [20–23].

In the effective field theory (EFT) framework [24], possible interaction operators of ALP(s) and SM particles start at dimension-five [25] and continue to higher order ones [26]. We can explore the effect of each term separately or some of them collectively. On the other hand, the ALP mass range in the general EFT extends from almost massless to the electroweak scale or above. Therefore, there are various search strategies for different ALP interactions and masses including laboratory-based [27], beam-dump [28, 29], Higgs factories [30, 31], and high energy collider [26, 30] experiments, as well as cosmological and astrophysical observations [32] (for a recent summary please see ref. [33]).

Among various kinds of ALP searches, the collider experiments are sensitive to probe the GeV to TeV scale ALPs. Although there were already a number of studies to explore the properties of ALPs at the Large Hadron Collider(LHC) [30, 34–40] and other future colliders [26, 39, 41–46], we find that most of the previous studies of ALP production channels at the LHC only focus on a single ALP effective operator in each process. However, people often overlook the potential for interference effects among different ALP operators except for the global analysis [40]. An interesting example in the SM is the associated production of the Higgs boson with a single top quark [47–54], in which the *HWW* coupling interferes non-trivially with the top-Yukawa coupling and experimentally it can be disentangled. With the same spirit, we propose an alternative approach that takes into account two or more relevant ALP effective operators simultaneously in a single production process and explore their interference effects. In particular, we study the ALP- $W^+W^-$  and the ALP- $t\bar{t}$  couplings in the process  $pp \rightarrow tja$  at the LHC.

The process  $pp \to tja$  as well as  $pp \to j\gamma a$  and  $pp \to t\bar{t}a$  have been considered in ref. [36]. However, interference effects among different ALP effective operators for these processes are not explored in that work. The process  $pp \to j\gamma a$  involves the ALP-quark pair, ALP-gluon pair, ALP-ZZ, and ALP-Z $\gamma$  couplings. Similarly, the process  $pp \to t\bar{t}a$  involves both ALP- $t\bar{t}$ and ALP-gluon pair couplings. Moreover, ref. [36] focuses only on  $M_a < 100$  MeV, where the ALPs become invisible particles at the LHC. Therefore, further study on interference effects and heavy ALPs with prompt decays to SM particles is essential and complementary to exploring the properties of ALPs at the LHC.

In this work, we focus on the process  $pp \to tja$  with  $a \to \gamma\gamma$ , in which only the ALP- $W^+W^-$  and ALP- $t\bar{t}$  couplings are involved. Especially, the final state with two isolated photons and a top quark decaying semi-leptonically is considered for 25 GeV  $< M_a < 100$  GeV. Although this process is similar to the associated production of the Higgs boson with a single top quark, the relevant ALP coupling types are different from the Higgs boson ones. Therefore, the process  $pp \to tja$  can generate quite distinct predictions. Our proposed approach allows us to explore novel ALP production processes that involve multiple ALP operators and investigate their interference effects.

The organization of this paper is as follows. In the next section, we describe the ALP interactions relevant to this study in the EFT framework. In section 3, we explore the interference effects between the ALP- $W^+W^-$  and ALP- $t\bar{t}$  couplings in  $pp \rightarrow taX$  processes where "X" is the possible SM particles. In section 4, we describe the experimental setup for discriminating the signal from the related SM backgrounds. We give the numerical results and sensitivity reach of the ALP couplings in section 5. Finally, we conclude in section 6.

# 2 Theoretical setup

In this study, the relevant ALP operators include the ALP-gauge boson pair and the ALP-top quark pair couplings, which start at dimension-five. The CP-odd couplings of the ALP to the electroweak gauge boson fields are given by

$$\mathcal{L}_{\rm EW} \supset -\frac{a}{f_a} \left( C_{WW} W^i_{\mu\nu} \tilde{W}^{i\mu\nu} + C_{BB} B_{\mu\nu} \tilde{B}^{\mu\nu} \right), \tag{2.1}$$

where i = 1, 2, 3 represents the SU(2) index, and  $\tilde{W}^{i\mu\nu}$  and  $\tilde{B}^{\mu\nu}$  are the dual field strength tensors. Here the ALP field and its decay constant are represented by a and  $f_a$ , respectively. After transforming  $W^i$  and B to the physical fields  $\gamma, Z, W^{\pm}$ , the interactions in eq. (2.1) can be written as

$$\mathcal{L}_{\rm EW} \supset -\frac{1}{4}a \left( g_{a\gamma\gamma} F_{\mu\nu} \tilde{F}^{\mu\nu} + g_{a\gamma Z} F_{\mu\nu} \tilde{Z}^{\mu\nu} + g_{aZZ} Z_{\mu\nu} \tilde{Z}^{\mu\nu} + g_{aWW} W_{\mu\nu} \tilde{W}^{\mu\nu} \right) , \qquad (2.2)$$

where  $F_{\mu\nu}$ ,  $W_{\mu\nu}$ , and  $Z_{\mu\nu}$  are the field strength tensors of the photon,  $W^{\pm}$ , and Z bosons, respectively. Thus, the dimensionful couplings of the photon and the electroweak gauge



**Figure 1.** Two key contributing Feynman diagrams for the process  $pp \rightarrow tja$  at the LHC.

bosons to the ALP can be written in terms of  $C_{WW}$  and  $C_{BB}$  [25, 31, 35, 38, 46],

$$g_{a\gamma\gamma} = \frac{4}{f_a} (C_{BB} c_w^2 + C_{WW} s_w^2), \qquad (2.3)$$

$$g_{aWW} = \frac{4}{f_a} C_{WW},\tag{2.4}$$

$$g_{aZZ} = \frac{4}{f_a} (C_{BB} s_w^2 + C_{WW} c_w^2), \qquad (2.5)$$

$$g_{aZ\gamma} = \frac{8}{f_a} s_w c_w (C_{WW} - C_{BB}), \qquad (2.6)$$

where  $c_w$  and  $s_w$  are cosine and sine of the Weinberg angle that is related to the rotation between the electroweak fields and the physical fields as in

$$W^3_{\mu} = c_w Z_{\mu} + s_w A_{\mu}, \quad B_{\mu} = -s_w Z_{\mu} + c_w A_{\mu}.$$

On the other hand, the ALP-top quark pair interaction is given by [55]

$$\mathcal{L}_{at\bar{t}} = C_{a\phi} \frac{\partial_{\mu}a}{2f_a} (\bar{t}\gamma^{\mu}\gamma^5 t).$$
(2.7)

After applying the equation of motion, the above Lagrangian, eq. (2.7), can be written as

$$\mathcal{L}_{at\bar{t}} = -iC_{a\phi}\frac{m_t a}{f_a}(\bar{t}\gamma^5 t).$$
(2.8)

where  $m_t$  is the top quark mass. As we can see, the ALP-quark pair coupling is proportional to the mass of the quark. Therefore, for the similar size of  $C_{a\phi}/f_a$ , the  $at\bar{t}$  coupling can provide stronger interaction than other  $aq\bar{q}$  couplings. Equipped ourselves with these theoretical setups, we are now ready to discuss the interference effects between the  $aW^+W^-$  and the  $at\bar{t}$  couplings in the process  $pp \to tja$ .

# 3 Production and interference effects in $pp \rightarrow taX$ processes

In this section, our focus is on investigating the interference effects between the  $aW^+W^$ and the  $at\bar{t}$  operators in the process  $pp \to taX$  where "X" is the possible SM particles at the



Figure 2. Production cross sections for the signal process  $pp \rightarrow j t a$  with  $a \rightarrow \gamma \gamma$  and  $t \rightarrow bW$ ,  $W \rightarrow l\nu_l$  at the LHC ( $\sqrt{s} = 14$  TeV) for  $M_a = 25, 50, 100$  GeV. We fix the  $aW^+W^-$  coupling by setting  $C_{WW} = C_{BB} = 1$  and  $f_a = 10$  TeV. The  $at\bar{t}$  coupling  $C_{a\phi}$  varies from -10 to +10.



**Figure 3.** Two key contributing Feynman diagrams for the process  $pp \rightarrow tjba$  at the LHC.

LHC with  $\sqrt{s} = 14$  TeV. Firstly, two key contributing Feynman diagrams for  $pp \rightarrow tja$  are shown in figure 1. The ALP can bremsstrahlung off a W propagator and also off a top-quark leg.<sup>1</sup> Thus, these two sets of diagrams can interfere.

We apply MadGraph5\_aMC@NLO [56] with the 5-flavor scheme (u, d, s, c, b) to calculate the production cross sections for the process  $pp \to tja$  fixing the parameters:  $C_{WW} = C_{BB} = 1$ and  $f_a = 10$  TeV, and vary the  $at\bar{t}$  coupling labeled by  $C_{a\phi}$  from -10 to 10. We show in figure 2 the production cross sections for  $M_a = 25, 50, 100$  GeV at the LHC ( $\sqrt{s} = 14$  TeV), including the branching ratios for  $a \to \gamma\gamma$  and  $t \to bW$ ,  $W \to l\nu_l$  ( $l = e, \mu$ ).

<sup>&</sup>lt;sup>1</sup>Here we do not involve the Feynman diagrams in which the ALP attached to the *b* quark or light quarks since their contributions are much smaller than that from the  $at\bar{t}$  coupling with the same  $C_{a\phi}/f_a$  value.



**Figure 4.** Two key contributing Feynman diagrams for the process  $pp \rightarrow tWa$  at the LHC.



**Figure 5.** Two key contributing Feynman diagrams for the process  $pp \rightarrow tba$  at the LHC.

It is not difficult to see the interference effects when we look at the cross-section curves at both ends (-10 and +10), although the effects are moderate at only about 10% difference. Moreover, we have observed that the contribution from the  $at\bar{t}$  interaction with  $C_{a\phi} \sim 1$ is smaller than that from the  $aW^+W^-$  interaction with  $C_{WW} = C_{BB} = 1$  in this process. Meanwhile, the constraints for the  $aW^+W^-$  coupling are much stronger than that for the  $at\bar{t}$  coupling as shown in refs. [37, 55, 57].

Furthermore, we would like to discuss some other associated ALP production with a single top quark processes. The first one is  $pp \to t \ j \ b \ a$  (figure 3), which can be regarded as a higher-order correction from  $pp \to t \ j \ a$  when the *b*-quark is not tagged in the final state. To identify this process from  $pp \to t \ j \ a$  and avoid the collinear divergence, the following cuts are applied to the *b* and *j* in the final state (note that the  $P_{T_j}$  and  $|\eta_j|$  cuts used in the signal-background analysis in the next section are different):

$$P_{T_b} > 25 \text{ GeV}, \quad |\eta_b| < 2.5, \quad P_{T_i} > 10 \text{ GeV}, \quad |\eta_i| < 5.$$
 (3.1)

The second and the third ones are  $pp \to t \ W \ a$  (figure 4) and  $pp \to t \ b \ a$  (figure 5) processes, respectively. In order to fairly compare the production cross-sections of these processes, we do not impose any cuts for them here, except for  $pp \to t \ j \ b \ a$  with the cuts in eq. (3.1) to avoid the double-counting. The production cross-sections for the processes  $pp \to t \ j \ a$ ,  $pp \to t \ j \ b \ a$ ,  $pp \to t \ W \ a$ , and  $pp \to t \ b \ a$  at the LHC ( $\sqrt{s} = 14 \ \text{TeV}$ ) for  $M_a = 50 \ \text{GeV}$  are shown in figure 6. We fix the ALP-gauge boson pair coupling by setting  $C_{WW} = C_{BB} = 1$ and  $f_a = 10 \ \text{TeV}$  and vary the  $at\bar{t}$  coupling  $C_{a\phi}$  from -10 to +10. Firstly, the shape of  $pp \to t \ j \ b \ a$  is similar to  $pp \to t \ j \ a$ , but the cross-section is smaller as we expect it to be a



**Figure 6.** Production cross sections for the signal processes  $pp \to t \ j \ a, pp \to t \ j \ b \ a, pp \to t \ W \ a$ , and  $pp \to t \ b \ a$  at the LHC ( $\sqrt{s} = 14 \text{ TeV}$ ) for  $M_a = 50 \text{ GeV}$ . We fix the ALP-gauge boson pair coupling by setting  $C_{WW} = C_{BB} = 1$  and  $f_a = 10 \text{ TeV}$ . The  $at\bar{t}$  coupling  $C_{a\phi}$  varies from -10 to +10.

higher-order correction. Secondly,  $pp \to t \ W \ a$  is also a promising process which can show obvious interference effects. However, its cross-section is less sensitive to the variation of  $C_{a\phi}$ than the one from  $pp \to t \ j \ a$  and the decay modes of W should be taken into account. Note that for the processes  $pp \to tjba$  and  $pp \to tWa$ , the agg coupling can also be included to study the interference effects among the  $aW^+W^-$ ,  $at\bar{t}$ , and agg couplings simultaneously. Finally,  $pp \to t \ b \ a$  displays sizable interference effects as well, but its cross-section is much smaller than the other three processes. Therefore, we will stick with the process  $pp \to t \ j \ a$ for the analysis in this study.

#### 4 Experimental setup and simulations

In this section, we describe the calculation and experimental setup for discriminating the signal from dominant SM backgrounds. We show the event rates for the center-of-mass energy  $\sqrt{s} = 14$  TeV and integrated luminosities of 300 fb<sup>-1</sup> (current run) and 3000 fb<sup>-1</sup> (High-Luminosity LHC) [58].

# 4.1 Signal and relevant SM background processes

The Monte Carlo simulations of signal and relevant SM background events are calculated utilizing MadGraph5\_aMC@NLO. The UFO model file of the ALP EFT framework (eqs. (2.2) and (2.8)) is employed for the signal event simulation [24].<sup>2</sup> In our simulation,  $10^4$  events are generated for the signal process and  $10^5$  events for each SM background process. The subsequent steps involve parton showering and hadronization using Pythia8 [59], and

<sup>&</sup>lt;sup>2</sup>This UFO model file is publicly accessible for download at https://feynrules.irmp.ucl.ac.be/wiki/ALPsEFT.

detection simulations conducted with Delphes3 [60], incorporating the ATLAS\_card.dat for accuracy and consistency. Here a jet cone size R = 0.4 is employed for clustering jets using FastJet [61] with the *anti*- $k_T$  algorithm [62]. The output root files from Delphes3 are passed to the Python-based tool uproot [63] for further analysis.

In order to investigate the final-state signature of two isolated photons, we focus on the ALP within a mass range spanning from 25 GeV to 100 GeV.<sup>3</sup> In this simulation, some specific benchmark values are assigned to the model parameters:  $f_a = 10$  TeV,  $C_{WW} = C_{BB} = 1$ , and a scan of  $C_{a\phi}$  from -10 to 10. A nonzero  $C_{a\phi}$  together with  $C_{WW} = 1$  initiates ALP production from top bremsstralung, alongside with ALP production from W-boson fusion. In contrast, the choice of  $C_{a\phi} = 0$  prohibits the top bremsstralung into ALP. The variation  $C_{a\phi}$  offers additional insights into the interference effects among these ALP operators. We have already shown the interference effects in figure 2 in the last section.

The signal final state consists of the decay of the ALP and the top quark, as well as a hadronic jet. The dominant decay mode of the ALP is into a pair of isolated photons for the ALP mass range from 25 - 100 GeV for the setting  $C_{WW} = C_{BB} = 1$ . We choose the semi-leptonic decay of the top quark:  $t \to Wb$ ,  $W \to l\nu_l$  in this study. For such a final state, we consider two main SM backgrounds: (i)  $p \ p \to t \ j \ \gamma \ \gamma$  (labeled as BG1) and (ii)  $p \ p \to W \ j \ j \ \gamma \ \gamma$  (labeled as BG2). Note that BG1 emerges as the predominant background in comparison to BG2. In order to estimate the sensitivity reach of the ALP coupling, we evaluate the total number of signal and background events at the LHC with a center-of-mass energy of  $\sqrt{s} = 14$  TeV. The total number of events is defined as:

$$N_s, N_b = \sigma_{s,b} \times \frac{N_{\text{selected}}}{N_{\text{sim}}} \times \mathcal{L} \times \eta_{b-\text{tag}} , \qquad (4.1)$$

where  $\sigma_b$  and  $\sigma_s$  denote the cross-sections of background and signal events, respectively. The ratio  $\frac{N_{\text{selected}}}{N_{\text{sim}}}$  represents the selection rate, and  $\mathcal{L}$  is the integrated luminosity. The factor  $\eta_{b-\text{tag}}$  represents the *b*-quark tagging efficiency or *b*-mistag probability according to *b* or *j* in the context.

One may concern about the  $t\bar{t}$ -related backgrounds such as  $t\bar{t}$ ,  $t\bar{t}j$ , or even  $t\bar{t}\gamma j$  when j's are mis-tagged as photons. Since we have applied isolation cuts among the photons, the jet, the *b*-jet, and lepton shown in eq. (4.2), the mis-tag probability for  $P_{j\to\gamma} \simeq 5 \times 10^{-4}$  [64]. Therefore, with such a small factor we do not expect these  $t\bar{t}$  related backgrounds can affect significantly the sensitivity estimates.

## 4.2 Event selections

In an effort to reduce these two main SM background events, we scrutinize the kinematic characteristics between the signal and background events, aiming to determine a suitable threshold. As discussed in the preceding section, we explore ALP masses ranging from  $M_a = 25$  GeV to  $M_a = 100$  GeV. To illustrate interference effects, we select three benchmark values for the ALP mass, namely  $M_a = 10, 25$ , and 100 GeV, and keeping  $C_W = C_B = 1$  fixed. Additionally, we examine the cases with  $C_{a\phi} = -10, -5, 0, 5, 10$ . By observing variations in

<sup>&</sup>lt;sup>3</sup>Two photons from the ALP decay will become too collimated to pass the isolation criteria when  $M_a \lesssim$  20 GeV. In this situation, a photon-jet forms in the final state [38, 39, 45] instead of two isolated photons.



Figure 7. Kinematical distributions for the signal with  $M_a = 50 \text{ GeV}$  and two main SM backgrounds BG1 and BG2. Here  $f_a = 10 \text{ TeV}$  and  $C_{WW} = C_{BB} = 1$  are fixed. The "leading" in  $P_{T_{\gamma}}^{\text{leading}}$  and  $|\eta_{\gamma}^{\text{leading}}|$  refers to the photon with the highest transverse momentum.

the number of events (as already depicted in figure 2, where the event rate quantifies the interference effect) for couplings with the same magnitude but opposite signs, we can readily discern the interference effect. Finally, the results for the integrated luminosities  $300 \text{ fb}^{-1}$  (current run) and  $3000 \text{ fb}^{-1}$  (High-Luminosity LHC) will be shown in the next section.

Various kinematical distributions for the signal case of  $M_a = 50$  GeV along with two main SM backgrounds at detector level are shown in figure 7. The signal cases for  $M_a = 25$  GeV and 100 GeV show similar behavior. As an initial requirement for event selection, we applied a set of cuts on the transverse momentum  $P_T$  and rapidity  $|\eta|$  of the final-state particles. We refer to these cuts as "Basic Cuts". The Basic Cuts are given below in eq. (4.2):

#### **Basic Cuts:**

$$P_{T_b} > 25 \text{ GeV}, \quad |\eta_b| < 2.5, \quad P_{T_j}^{\text{lead}} > 25 \text{ GeV}, \quad |\eta_j^{\text{lead}}| < 2.5, P_{T_l} > 25 \text{ GeV}, \quad |\eta_l| < 2.5, \quad P_{T_{\gamma}}^{\text{lead}} \& P_{T_{\gamma}}^{\text{sub-lead}} > 20 \text{ GeV}, \quad |\eta_{\gamma}^{\text{lead}}| \& |\eta_{\gamma}^{\text{sub-lead}}| < 2.5, \Delta R_{ij} > 0.4 \text{ for } i, j = \gamma, l, j, b \text{ (except } \Delta R_{\gamma\gamma} > 0.3).$$

$$(4.2)$$

Here "lead" and "sub-lead" refer to the leading and sub-leading orders according to  $P_T$ . Additionally, the *b*-quark tagging efficiency and mistag probability are adopted from the ATLAS template in Delphes3.

We impose the following cuts for event selection:  $M_{bl} < 150$  GeV, ensuring the invariant mass of the system consisting of the b-jet and the charged lepton from the top-quark decay is less than  $150 \,\text{GeV}$ . This helps isolate events where the *b*-jet and charged lepton originate from the top-quark decay. The cut  $\Delta R_{bl} < 2.5$  ensures that the angular separation between the b-jet and the charged lepton (in  $\eta$ - $\phi$  space) is less than 2.5, ensuring the b-jet and charged lepton are sufficiently close, as expected from top-quark decays. We require  $P_{T_{\gamma}}^{\text{leading}} > 60$ GeV, ensuring the transverse momentum of the leading (highest  $p_T$ ) photon is greater than 60 GeV, to select high-energy photons from the ALP decay. The cut  $|\eta_{\gamma}^{\text{leading}}| < 1.7$  ensures the pseudorapidity of the leading photon is within 1.7, selecting photons within the central detector region where detection efficiency is higher. The cut on  $\Delta R_{l\gamma} > 2.0$  ensures the angular separation between the charged lepton and the photon (in  $\eta$ - $\phi$  space) is greater than 2.0, ensuring the charged lepton and photon are well separated, reducing the background from misidentified charged leptons and photons. Finally, we impose the invariant-mass window cut on the diphoton from the ALP decay:  $|M_{\gamma\gamma} - M_a| < 5 \,\text{GeV}$ . As shown in figure 7, the ALP mass window within 10 GeV is broad enough to encompass the major part of this resonance in the invariant diphoton mass distribution. Our cut on  $|M_{\gamma\gamma} - M_a| < 5 \,\text{GeV}$ could be further refined in a real experimental bump hunt analysis. Since the chosen ALP mass window reflects the energy measurement precision of the relevant detectors, such an analysis is beyond the scope of this study.

We summarize the above cuts for the signal and background event selections:

- **Basic Cuts** in eq. (4.2),
- $M_{bl} < 150 \text{ GeV},$
- $\Delta R_{bl} < 2.5$ ,
- $P_{T_{\gamma}}^{\text{leading}} > 60 \text{ GeV},$
- $|\eta_{\gamma}^{\text{leading}}| < 1.7,$
- $\Delta R_{l\gamma} > 2.0$ ,
- $|M_{\gamma\gamma} M_a| < 5 \,\text{GeV}.$

The cut-flow tables for  $M_a = 25, 50$ , and 100 GeV are given in tables 1, 2 3, respectively. We found that the ALP invariant-mass window cut is the strongest one to reduce events from both BG1 and BG2 but keep the signal events.

#### 5 Numerical results

After imposing the event selections provided in the last section, the number of signal events are comparable to, if not larger than, the background events. It is thus meaningful to calculate the significance of the signal and set limits on the cutoff scale  $f_a$ . The relation between the ALP signal events,  $N_s$ , and the ALP cutoff scale,  $f_a$ , is given as follows:

$$N_s \propto f_a^{-2} \,. \tag{5.1}$$

Cut	BG1	$\mathbf{BG2}$	Signal				
			$C_{a\phi} = -10$	$C_{a\phi} = -5$	$C_{a\phi} = 0$	$C_{a\phi} = 5$	$C_{a\phi} = 10$
Basic Cuts	404.35	8.95	4.25	1.64	0.35	1.85	4.67
$M_{bl} < 150 \text{ GeV}$	371.85	3.23	3.88	1.50	0.32	1.69	4.24
$\Delta R_{bl} < 2.5$	219.2	1.72	2.38	0.97	0.18	1.00	2.58
$P_{T_{\gamma}}^{\text{leading}} > 60 \text{ GeV}$	135.46	1.17	0.92	0.34	0.09	0.40	1.14
$ \eta_{\gamma}^{\rm leading}  < 1.7$	111.89	1.00	0.83	0.30	0.07	0.35	0.93
$\Delta R_{l\gamma} > 2.0$	87.47	0.66	0.69	0.23	0.05	0.29	0.82
$20~{\rm GeV} < {\rm M}_{\gamma\gamma} < 30~{\rm GeV}$	0.74	0.00	0.69	0.23	0.05	0.29	0.80

**Table 1.** Cutflow table for the SM backgrounds (BG1:  $p \ p \to t \ j \ \gamma \ \gamma$  and BG2:  $p \ p \to W \ j \ j \ \gamma \ \gamma$ ), and the signal:  $p \ p \to j \ t \ a$  with various  $C_{a\phi}$  couplings. Here we set  $M_a = 25$  GeV,  $f_a = 10$  TeV,  $C_{WW} = C_{BB} = 1$ , and  $C_{a\phi} = -10, -5, 0, 5, 10$  GeV. **Basic Cuts** in the first row denotes the total number of events passed the cuts coded in eq. (4.2). The number of events are calculated by eq. (4.1) and integrated luminosity is set to  $\mathcal{L} = 3000$  fb<sup>-1</sup>.

Cut	BG1	BG2	Signal				
			$C_{a\phi} = -10$	$C_{a\phi} = -5$	$C_{a\phi} = 0$	$C_{a\phi} = 5$	$C_{a\phi} = 10$
Basic Cuts	404.35	8.95	18.52	6.46	2.07	7.36	20.84
$M_{bl} < 150 \text{ GeV}$	371.85	3.23	16.09	5.72	1.88	6.59	18.26
$\Delta R_{bl} < 2.5$	219.2	1.72	11.81	4.11	1.26	4.42	12.35
$P_{T_{\gamma}}^{\text{leading}} > 60 \text{ GeV}$	135.46	1.17	9.86	3.54	1.17	3.81	10.51
$ \eta_{\gamma}^{\rm leading}  < 1.7$	111.89	1.0	8.84	3.18	0.98	3.36	9.4
$\Delta R_{l\gamma} > 2.0$	87.47	0.66	7.99	2.72	0.83	3.05	8.69
$45~{\rm GeV} < {\rm M}_{\gamma\gamma} < 55~{\rm GeV}$	3.2	0.02	7.91	2.68	0.82	3.01	8.62

**Table 2.** Cutflow table for the SM backgrounds (BG1:  $p \ p \to t \ j \ \gamma \ \gamma$  and BG2:  $p \ p \to W \ j \ j \ \gamma \ \gamma$ ), and the signal:  $p \ p \to j \ t \ a$  with various  $C_{a\phi}$  couplings. Here we set  $M_a = 50$  GeV,  $f_a = 10$  TeV,  $C_{WW} = C_{BB} = 1$ , and  $C_{a\phi} = -10, -5, 0, 5, 10$  GeV. **Basic Cuts** in the first row denotes the total number of events passed the cuts coded in eq. (4.2). The number of events are calculated by eq. (4.1) and integrated luminosity is set to  $\mathcal{L} = 3000$  fb<sup>-1</sup>.

Cut	BG1	$\mathbf{BG2}$	Signal				
			$C_{a\phi} = -10$	$C_{a\phi} = -5$	$C_{a\phi} = 0$	$C_{a\phi} = 5$	$C_{a\phi} = 10$
Basic Cuts	404.35	8.95	27.3	10.31	4.22	11.07	31.21
$M_{bl} < 150 \text{ GeV}$	371.85	3.23	23.67	8.91	3.75	9.58	27.16
$\Delta R_{bl} < 2.5$	219.2	1.72	17.92	6.75	2.73	7.04	20.63
$P_{T_{\gamma}}^{\text{leading}} > 60 \text{ GeV}$	135.46	1.17	17.29	6.49	2.7	6.83	19.84
$ \eta_{\gamma}^{ m leading}  < 1.7$	111.89	1.0	15.63	5.8	2.3	6.07	17.91
$\Delta R_{l\gamma} > 2.0$	87.47	0.66	13.98	5.1	1.92	5.49	16.77
$95 \text{ GeV} < M_{\gamma\gamma} < 105 \text{ GeV}$	5.96	0.04	13.93	5.05	1.9	5.46	16.7

**Table 3.** Cutflow table for the SM backgrounds (BG1:  $p p \rightarrow t j \gamma \gamma$  and BG2:  $p p \rightarrow W j j \gamma \gamma$ ), and the signal:  $p p \rightarrow j t a$  with various  $C_{a\phi}$  couplings. Here we set  $M_a = 100$  GeV,  $f_a = 10$  TeV,  $C_{WW} = C_{BB} = 1$ , and  $C_{a\phi} = -10, -5, 0, 5, 10$  GeV. **Basic Cuts** in the first row denotes the total number of events passed the cuts coded in eq. (4.2). The number of events are calculated by eq. (4.1) and integrated luminosity is set to  $\mathcal{L} = 3000$  fb<sup>-1</sup>.



Figure 8. Exclusion regions at 95% confidence level (C.L.) for the ALP cutoff scale  $f_a$  derived from the process  $pp \rightarrow j t a$  followed by  $a \rightarrow \gamma \gamma$  and  $t \rightarrow b l \nu_l$  at the LHC with  $\sqrt{s} = 14$  TeV. This analysis is conducted with different choices of  $C_{a\phi} = 0$ , 10 and under two sets of integrated luminosities,  $\mathcal{L} = 300 \text{ fb}^{-1}$  and 3000 fb<sup>-1</sup>. Solid lines in the plot represent sensitivity curves with a 10% systematic uncertainty, while the dashed lines depict the curves without incorporating systematic uncertainty. The gray areas represent the existing limits from LEP [65, 66], CDF [67], and LHC [68, 69].

Therefore, we can rescale the factor  $f_a$  to match the expected signal events  $N_s$ . The significance of the signal is given by [31]

$$Z = \sqrt{2\left[ (N_s + N_b) \ln\left(\frac{(N_s + N_b)(N_b + \sigma_B^2)}{N_b^2 + (N_s + N_b)\sigma_B^2}\right) - \frac{N_b^2}{\sigma_B^2} \ln\left(1 + \frac{\sigma_B^2 N_s}{N_b(N_b + \sigma_B^2)}\right) \right]}, \quad (5.2)$$

where  $N_s$ ,  $N_b$  are the number of signal and background events, and  $\sigma_B$  is the systematic uncertainty in background estimation, which is taken to be zero and  $0.1N_b$  in the presentation. The 95% confidence level (C.L.) sensitivity curves for the ALP cutoff scale  $f_a$  to the ALP mass  $M_a$  are obtained by requiring the significance Z > 2.

In figure 8, we show 95% C.L. exclusion region for the ALP cutoff scale,  $f_a$ . This exclusion region is obtained through the process  $pp \to j t a$  with  $a \to \gamma\gamma$  and  $t \to bW$ ,  $W \to l\nu_l$  at the LHC with  $\sqrt{s} = 14$  TeV. In the figure, we fix  $C_{WW} = C_{BB} = 1$  and set  $C_{a\phi} = 0$  and  $C_{a\phi} = 10$ as two benchmark points. Two different sets of integrated luminosities,  $\mathcal{L} = 300$  fb<sup>-1</sup> and 3000 fb<sup>-1</sup> are plotted. In the plot, solid lines denote sensitivity curves accounting for a 10% systematic uncertainty, while dashed lines represent curves without incorporating systematic uncertainty. We can find that the systematic uncertainty only slightly changes the predictions of future bounds in this study. It indicates that our results are robust against possible uncertainties. The gray shaded areas correspond to the existing limits from LEP [65, 66], CDF [67], and LHC [68, 69]. The lines in figure 8 unmistakably demonstrate that sensitivity curves with non-zero values of  $C_{a\phi}$  can yield better limits on  $f_a$  than those with  $C_{a\phi} = 0$ . It can also be observed in figure 2 in which the minimal production cross section for the signal process appears at  $C_{a\phi} = 0$  and it enhances as the  $|C_{a\phi}|$  increases.

Specifically, the sensitivity reach corresponding to  $C_{a\phi} = 10$  and  $\mathcal{L} = 300 (3000)$  fb<sup>-1</sup> (depicted by the red (green) line) exhibits enhanced sensitivity compared to current constraints for  $M_a > 60$  GeV ( $M_a > 45$  GeV). Even in the absence of the  $C_{a\phi}$  coupling ( $C_{a\phi} = 0$ ), the HL-LHC ( $\mathcal{L} = 3000$  fb<sup>-1</sup>) can impose the sensitivity on  $f_a$  (indicated by the blue curve) for  $M_a > 80$  GeV.

## 6 Conclusions

In summary, we have presented a novel approach that considers simultaneous presence of two or more ALP interaction operators in a single process at the LHC. In particular, we demonstrated the interference effects of the ALP-gauge boson pair and the ALP-top quark pair couplings in the process  $pp \rightarrow tja$  as shown in figure 2. Through a detailed analysis of  $pp \rightarrow tja$ , followed by  $a \rightarrow \gamma\gamma$  and semi-leptonic decay of the top quark, as a case study, we demonstrated the efficacy of this approach in constraining ALP interactions as well as their interference within a single process.

Our findings indicate that the sensitivity of the ALP cutoff scale  $f_a$  could potentially reach down to the values around  $1/f_a \sim 5 \times 10^{-2} \text{ TeV}^{-1}$  for the ALP masses ranging from 25 GeV to 100 GeV at the HL-LHC as shown in figure 8. It indicates that some uncovered parameter space can be further explored from the process  $pp \rightarrow tja$  in the near future. Furthermore, once the absolute size of the ALP-gauge boson pair and the ALP-top quark pair couplings can be pinned down by other ALP production channels, this process can provide extra information about the relative sign (or phase) between two coefficients of ALP interaction operators. In our case, we observe a positive interference between the processes in figure 1 which is visible from the fact that the cross-section increases with  $C_{a\phi}$ .

#### Acknowledgments

The work of K.Cheung, P.Sarmah, and C.J. Ouseph is supported by the Taiwan NSTC with grant no. MoST-110-2112-M-007-017-MY3. The work of C.-T. Lu is supported by the Special funds for postdoctoral overseas recruitment, Ministry of Education of China (No. 164080H0262403).

**Open Access.** This article is distributed under the terms of the Creative Commons Attribution License (CC-BY4.0), which permits any use, distribution and reproduction in any medium, provided the original author(s) and source are credited.

#### References

- J. Preskill, M.B. Wise and F. Wilczek, Cosmology of the invisible axion, Phys. Lett. B 120 (1983) 127 [INSPIRE].
- [2] L.F. Abbott and P. Sikivie, A cosmological bound on the invisible axion, Phys. Lett. B 120 (1983) 133 [INSPIRE].
- [3] M. Dine and W. Fischler, The not so harmless axion, Phys. Lett. B 120 (1983) 137 [INSPIRE].
- [4] J. Bagger, E. Poppitz and L. Randall, The R axion from dynamical supersymmetry breaking, Nucl. Phys. B 426 (1994) 3 [hep-ph/9405345] [INSPIRE].
- [5] P. Svrcek and E. Witten, Axions in string theory, JHEP 06 (2006) 051 [hep-th/0605206]
   [INSPIRE].
- [6] A. Arvanitaki et al., String axiverse, Phys. Rev. D 81 (2010) 123530 [arXiv:0905.4720]
   [INSPIRE].
- [7] M. Cicoli, M. Goodsell and A. Ringwald, *The type IIB string axiverse and its low-energy* phenomenology, JHEP **10** (2012) 146 [arXiv:1206.0819] [INSPIRE].
- [8] L. Visinelli and S. Vagnozzi, Cosmological window onto the string axiverse and the supersymmetry breaking scale, Phys. Rev. D 99 (2019) 063517 [arXiv:1809.06382] [INSPIRE].
- S. Chang, S. Tazawa and M. Yamaguchi, Axion model in extra dimensions with TeV scale gravity, Phys. Rev. D 61 (2000) 084005 [hep-ph/9908515] [INSPIRE].
- M. Bastero-Gil, C. Beaufort and D. Santos, Solar axions in large extra dimensions, JCAP 10 (2021) 048 [arXiv:2107.13337] [INSPIRE].
- [11] R.D. Peccei and H.R. Quinn, CP conservation in the presence of instantons, Phys. Rev. Lett. 38 (1977) 1440 [INSPIRE].
- [12] R.D. Peccei and H.R. Quinn, Constraints imposed by CP conservation in the presence of instantons, Phys. Rev. D 16 (1977) 1791 [INSPIRE].
- [13] S. Weinberg, A new light boson?, Phys. Rev. Lett. 40 (1978) 223 [INSPIRE].
- [14] F. Wilczek, Problem of strong P and T invariance in the presence of instantons, Phys. Rev. Lett. 40 (1978) 279 [INSPIRE].
- [15] J.E. Kim, Weak interaction singlet and strong CP invariance, Phys. Rev. Lett. 43 (1979) 103 [INSPIRE].
- [16] M.A. Shifman, A.I. Vainshtein and V.I. Zakharov, Can confinement ensure natural CP invariance of strong interactions?, Nucl. Phys. B 166 (1980) 493 [INSPIRE].
- [17] M. Dine, W. Fischler and M. Srednicki, A simple solution to the strong CP problem with a harmless axion, Phys. Lett. B 104 (1981) 199 [INSPIRE].
- [18] L.D. Duffy and K. van Bibber, Axions as dark matter particles, New J. Phys. 11 (2009) 105008 [arXiv:0904.3346] [INSPIRE].
- [19] F. Chadha-Day, J. Ellis and D.J.E. Marsh, Axion dark matter: what is it and why now?, Sci. Adv. 8 (2022) abj3618 [arXiv:2105.01406] [INSPIRE].
- [20] C.-H.V. Chang, C.-R. Chen, S.-Y. Ho and S.-Y. Tseng, Explaining the MiniBooNE anomalous excess via a leptophilic ALP-sterile neutrino coupling, Phys. Rev. D 104 (2021) 015030 [arXiv:2102.05012] [INSPIRE].

- [21] G.-W. Yuan et al., Is the W-boson mass enhanced by the axion-like particle, dark photon, or chameleon dark energy?, Sci. China Phys. Mech. Astron. 65 (2022) 129512 [arXiv:2204.04183]
   [INSPIRE].
- [22] J. Liu, X. Ma, L.-T. Wang and X.-P. Wang, ALP explanation to the muon (g-2) and its test at future Tera-Z and Higgs factories, Phys. Rev. D 107 (2023) 095016 [arXiv:2210.09335] [INSPIRE].
- [23] K. Cheung and C.J. Ouseph, Interpretation of excess in  $H \to Z\gamma$  using a light axionlike particle, Phys. Rev. D 110 (2024) 055016 [arXiv:2402.05678] [INSPIRE].
- [24] I. Brivio et al., ALPs effective field theory and collider signatures, Eur. Phys. J. C 77 (2017) 572
   [arXiv:1701.05379] [INSPIRE].
- [25] H. Georgi, D.B. Kaplan and L. Randall, Manifesting the invisible axion at low-energies, Phys. Lett. B 169 (1986) 73 [INSPIRE].
- [26] M. Bauer, M. Heiles, M. Neubert and A. Thamm, Axion-like particles at future colliders, Eur. Phys. J. C 79 (2019) 74 [arXiv:1808.10323] [INSPIRE].
- [27] P. Sikivie, Experimental tests of the invisible axion, Phys. Rev. Lett. 51 (1983) 1415 [Erratum ibid. 52 (1984) 695] [INSPIRE].
- [28] E.M. Riordan et al., A search for short lived axions in an electron beam dump experiment, Phys. Rev. Lett. 59 (1987) 755 [INSPIRE].
- [29] B. Döbrich, J. Jaeckel and T. Spadaro, Light in the beam dump ALP production from decay photons in proton beam-dumps, JHEP 05 (2019) 213 [Erratum ibid. 10 (2020) 046]
   [arXiv:1904.02091] [INSPIRE].
- [30] M. Bauer, M. Neubert and A. Thamm, Collider probes of axion-like particles, JHEP 12 (2017) 044 [arXiv:1708.00443] [INSPIRE].
- [31] K. Cheung and C.J. Ouseph, Axionlike particle search at Higgs factories, Phys. Rev. D 108 (2023) 035003 [arXiv:2303.16514] [INSPIRE].
- [32] CAST collaboration, New CAST limit on the axion-photon interaction, Nature Phys. 13 (2017) 584 [arXiv:1705.02290] [INSPIRE].
- [33] C.A.J. O'Hare, Cosmology of axion dark matter, PoS COSMICWISPers (2024) 040 [arXiv:2403.17697] [INSPIRE].
- [34] J. Jaeckel and M. Spannowsky, Probing MeV to 90 GeV axion-like particles with LEP and LHC, Phys. Lett. B 753 (2016) 482 [arXiv:1509.00476] [INSPIRE].
- [35] I. Brivio et al., ALPs effective field theory and collider signatures, Eur. Phys. J. C 77 (2017) 572 [arXiv:1701.05379] [INSPIRE].
- [36] J. Ebadi, S. Khatibi and M. Mohammadi Najafabadi, New probes for axionlike particles at hadron colliders, Phys. Rev. D 100 (2019) 015016 [arXiv:1901.03061] [INSPIRE].
- [37] D. d'Enterria, Collider constraints on axion-like particles, in the proceedings of the Workshop on feebly interacting particles, (2021) [arXiv:2102.08971] [INSPIRE].
- [38] J. Ren et al., Detecting an axion-like particle with machine learning at the LHC, JHEP 11 (2021) 138 [arXiv:2106.07018] [INSPIRE].
- [39] K. Cheung, W. Hsiao, C.J. Ouseph and C. Wang, Probing the gauge-boson couplings of axion-like particle at the LHC and high-luminosity LHC, JHEP 05 (2024) 324 [arXiv:2402.10550] [INSPIRE].

- [40] S. Bruggisser, L. Grabitz and S. Westhoff, Global analysis of the ALP effective theory, JHEP 01 (2024) 092 [arXiv:2308.11703] [INSPIRE].
- [41] Y. Bao, J.J. Fan and L. Li, Electroweak ALP searches at a muon collider, JHEP 08 (2022) 276 [arXiv:2203.04328] [INSPIRE].
- [42] H.-Y. Zhang, C.-X. Yue, Y.-C. Guo and S. Yang, Searching for axionlike particles at future electron-positron colliders, Phys. Rev. D 104 (2021) 096008 [arXiv:2103.05218] [INSPIRE].
- [43] Y. Liu and B. Yan, Searching for the axion-like particle at the EIC, Chin. Phys. C 47 (2023) 043113 [arXiv:2112.02477] [INSPIRE].
- [44] T. Han, T. Li and X. Wang, Axion-like particles at high energy muon colliders a white paper for Snowmass 2021, in the proceedings of the Snowmass 2021, (2022) [arXiv:2203.05484]
   [INSPIRE].
- [45] C.-T. Lu, Lighting electroweak-violating ALP-lepton interactions at e<sup>+</sup>e<sup>-</sup> and ep colliders, Phys. Rev. D 108 (2023) 115029 [arXiv:2210.15648] [INSPIRE].
- [46] C.-T. Lu, X. Luo and X. Wei, Exploring muonphilic ALPs at muon colliders, Chin. Phys. C 47 (2023) 103102 [arXiv:2303.03110] [INSPIRE].
- [47] V. Barger, M. McCaskey and G. Shaughnessy, Single top and Higgs associated production at the LHC, Phys. Rev. D 81 (2010) 034020 [arXiv:0911.1556] [INSPIRE].
- [48] S. Biswas, E. Gabrielli and B. Mele, Single top and Higgs associated production as a probe of the Htt coupling sign at the LHC, JHEP 01 (2013) 088 [arXiv:1211.0499] [INSPIRE].
- [49] S. Biswas, E. Gabrielli, F. Margaroli and B. Mele, Direct constraints on the top-Higgs coupling from the 8 TeV LHC data, JHEP 07 (2013) 073 [arXiv:1304.1822] [INSPIRE].
- [50] M. Farina et al., Lifting degeneracies in Higgs couplings using single top production in association with a Higgs boson, JHEP **05** (2013) 022 [arXiv:1211.3736] [INSPIRE].
- [51] P. Agrawal, S. Mitra and A. Shivaji, Effect of anomalous couplings on the associated production of a single top quark and a Higgs boson at the LHC, JHEP 12 (2013) 077 [arXiv:1211.4362] [INSPIRE].
- [52] J. Ellis, D.S. Hwang, K. Sakurai and M. Takeuchi, Disentangling Higgs-top couplings in associated production, JHEP 04 (2014) 004 [arXiv:1312.5736] [INSPIRE].
- [53] C. Englert and E. Re, Bounding the top Yukawa coupling with Higgs-associated single-top production, Phys. Rev. D 89 (2014) 073020 [arXiv:1402.0445] [INSPIRE].
- [54] J. Chang, K. Cheung, J.S. Lee and C.-T. Lu, Probing the top-Yukawa coupling in associated Higgs production with a single top quark, JHEP 05 (2014) 062 [arXiv:1403.2053] [INSPIRE].
- [55] F. Esser, M. Madigan, V. Sanz and M. Ubiali, On the coupling of axion-like particles to the top quark, JHEP 09 (2023) 063 [arXiv:2303.17634] [INSPIRE].
- [56] J. Alwall et al., MadGraph 5: going beyond, JHEP 06 (2011) 128 [arXiv:1106.0522] [INSPIRE].
- [57] G. Alonso-Álvarez, M.B. Gavela and P. Quilez, Axion couplings to electroweak gauge bosons, Eur. Phys. J. C 79 (2019) 223 [arXiv:1811.05466] [INSPIRE].
- [58] G. Apollinari et al., High-Luminosity Large Hadron Collider (HL-LHC): preliminary design report, CERN-2015-005, CERN, Geneva, Switzerland (2015) [D0I:10.5170/CERN-2015-005] [INSPIRE].
- [59] T. Sjostrand, S. Mrenna and P.Z. Skands, A brief introduction to PYTHIA 8.1, Comput. Phys. Commun. 178 (2008) 852 [arXiv:0710.3820] [INSPIRE].

- [60] DELPHES 3 collaboration, *DELPHES 3, a modular framework for fast simulation of a generic collider experiment*, *JHEP* **02** (2014) 057 [arXiv:1307.6346] [INSPIRE].
- [61] M. Cacciari, G.P. Salam and G. Soyez, FastJet user manual, Eur. Phys. J. C 72 (2012) 1896 [arXiv:1111.6097] [INSPIRE].
- [62] M. Cacciari, G.P. Salam and G. Soyez, The anti- $k_t$  jet clustering algorithm, JHEP 04 (2008) 063 [arXiv:0802.1189] [INSPIRE].
- [63] J. Pivarski et al., *uproot5: Root i/o in pure python and numpy*, https://github.com/scikit-hep/uproot5, (2024).
- [64] ATLAS collaboration, Study of the double Higgs production channel  $H(\rightarrow b\bar{b})H(\rightarrow \gamma\gamma)$  with the ATLAS experiment at the HL-LHC, ATL-PHYS-PUB-2017-001, CERN, Geneva, Switzerland (2017).
- [65] L3 collaboration, Search for anomalous  $Z \to \gamma\gamma\gamma$  events at LEP, Phys. Lett. B **345** (1995) 609 [INSPIRE].
- [66] OPAL collaboration, Multiphoton production in  $e^+e^-$  collisions at  $\sqrt{s} = 181 \text{ GeV}$  to 209 GeV, Eur. Phys. J. C 26 (2003) 331 [hep-ex/0210016] [INSPIRE].
- [67] CDF collaboration, First search for exotic Z boson decays into photons and neutral pions in hadron collisions, Phys. Rev. Lett. 112 (2014) 111803 [arXiv:1311.3282] [INSPIRE].
- [68] ATLAS collaboration, The ATLAS detector simulation, Nucl. Phys. B Proc. Suppl. 215 (2011) 85 [INSPIRE].
- [69] CMS collaboration, Search for supersymmetry with Higgs bosons in the final state, Nucl. Part. Phys. Proc. 273-275 (2016) 2378 [INSPIRE].