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Vector-vector scattering at the LHC with two charged leptons and two neutrinos in the final state

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ABSTRACT: A complete parton level analysis of $2\ell 2\nu 2j$ and $4\ell 2j$, $\ell = \mu, e$ production at the LHC is presented, including all processes at order $\mathcal{O}(\alpha_{\text{EM}}^6)$, $\mathcal{O}(\alpha_{\text{EM}}^4 \alpha_{\text{S}}^2)$. The infinite Higgs mass scenario, which is considered as a benchmark for strong scattering theories and is the limiting case for composite Higgs models, and one example of Strongly Interacting Light Higgs models are confronted with the Standard Model light Higgs predictions. This analysis is combined with the results in the $\ell\nu + \text{four jets}$, the $\ell^-\ell^+ + \text{four jets}$ and the $3\ell\nu + \text{two jets}$ channels presented in previous papers, in order to determine whether these alternative Higgs frameworks can be detected as an excess of events in boson-boson scattering.

KEYWORDS: Beyond Standard Model, Standard Model

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1 Introduction

Whether or not the search for a light Higgs boson at the LHC will be successful, vector boson scattering processes will require careful analysis. In fact, the corresponding amplitudes involving only vector bosons grow with energy when the bosons are longitudinally polarized and violate perturbative unitarity at about one TeV, requiring either the Higgs or some new physics in the energy range accessible to the LHC in order to tame this unphysical behaviour.¹

The Standard Model (SM) describes Electroweak Symmetry Breaking (EWSB) through a single complex Higgs doublet. Many alternative mechanisms of EWSB however have been explored. We will not try to summarize the different models and simply refer to the literature. We will only remark that it is conceivable that composite states are responsible for EWSB [9–18]. These theories typically predict the presence of new states which, if light enough, could be observed at the LHC.

The effective field theory approach [18–24] is a powerful method for treating the low energy dynamics of systems with broken symmetries. It provides a systematic expansion of the full unknown Lagrangian in terms of the fields which are relevant at scales much lower than the symmetry breaking scale.

In ref. [18] it has been pointed out that, if EWSB is triggered by a light composite Higgs which is a pseudo-Goldstone boson related to some large scale strongly interacting

¹Detailed reviews and extensive bibliographies can be found in refs. [1–8].

dynamics, the growth with energy of the vector boson scattering amplitudes typical of Higgsless models might not be completely canceled by Higgs exchange diagrams but only slowed down. This kind of models have been called Strongly Interacting Light Higgs (SILH) models. Examples which fall into this class are for instance the Holographic Higgs [16], the Little Higgs of ref. [17] and the Littlest Higgs [11].

In SILH models the leading low energy effects are described by two parameters (one responsible for a universal modification of all Higgs couplings, and the other one for a universal modification of Higgs couplings to fermions) characterized by the ratio $v^2/f^2 = \xi$, where v is the Higgs vacuum expectation value and f is the σ -model scale. The natural range of the ξ parameter is between $\xi = 0$ and $\xi = 1$ which correspond respectively to the limiting cases of the Standard Model and of technicolor theories. Because of the modified Higgs couplings, longitudinal gauge-boson scattering amplitudes violate unitarity at high energy, even in the presence of a light Higgs [18].

Scattering processes among vector bosons have been scrutinized since a long time [25–42]. In ref. [43, 44] an analysis of $\ell\nu + \text{four jets}$ and $\ell^+\ell^- + \text{four jets}$ production at the LHC has been presented, with the limitation of taking into account only purely electroweak processes. Preliminary results concerning the inclusion of the $\mathcal{O}(\alpha_{\text{EM}}^4\alpha_{\text{S}}^2)$ background, which include $VV + 2j$ and top-antitop production have appeared in ref. [45]. A preliminary analysis in the Equivalent Vector Boson Approximation of the observability of partial unitarization of longitudinal vector boson scattering in SILH models at the LHC can be found in ref. [46]. In the last few years QCD corrections to boson-boson production via vector boson fusion [47–50] at the LHC have been computed and turn out to be below 10%. Recently, VBFNLO [51] a Monte Carlo program for vector boson fusion, double and triple vector boson production at NLO QCD accuracy, limited to the leptonic decays of vector bosons, has been released. Recently, the first results for the NLO corrections to $W + 4j$ production have appeared [52]. New techniques which exploit the angular distribution of vector boson decay products to determine the ratio of longitudinal and transverse polarization have been proposed in [53].

In ref. [54] a complete parton level analysis of $\ell\nu + \text{four jets}$ production at the LHC, including all processes at order $\mathcal{O}(\alpha_{\text{EM}}^6)$, $\mathcal{O}(\alpha_{\text{EM}}^4\alpha_{\text{S}}^2)$ and $\mathcal{O}(\alpha_{\text{EM}}^2\alpha_{\text{S}}^4)$ has been presented, comparing a typical SM light Higgs scenario with the Higgsless case. It was noted that the $\mathcal{O}(\alpha_{\text{EM}}^2\alpha_{\text{S}}^4) W + 4j$ background is so large that the usual approach of comparing the number of events in the two scenarios at large invariant masses is useless. It was argued that the invariant mass distribution of the two central jets in the vector-vector scattering signal presents a peak corresponding to the decays of vector bosons while the background produced by $\mathcal{O}(\alpha_{\text{EM}}^2\alpha_{\text{S}}^4) W + 4j$ processes is rather flat and therefore can be measured from the sidebands and subtracted, drastically decreasing the theoretical uncertainties.

In ref. [55] the processes $pp \rightarrow \ell^+\ell^- + 4j$ and $pp \rightarrow 3\ell\nu + 2j$ have been studied along the lines introduced in ref. [54]. The infinite mass Higgs scenario and the instance of SILH models described above have been compared with the light Higgs SM framework.

In this paper we concentrate on the boson boson scattering reactions which produce a $2\ell 2\nu 2j$ final state. Because of the presence of two neutrinos the mass of the final state boson pair cannot be reconstructed. For completeness sake in the end we also discuss the

$2j4\ell$ channel in which the vector pair mass can obviously be measured with high accuracy but which has been left out of our previous papers because of its small cross section. These processes have been studied already in ref. [56, 57] where they have been described as gold-plated. A potentially large background to these channels is the copious yield of high p_T , isolated leptons in B-hadron production [58, 59] which mimic the signature of the leptonic decays of W bosons. A detailed experimental analysis of two same sign W 's has however shown that when standard isolation criteria are applied isolated leptons from B-hadrons can be efficiently eliminated [60]. Therefore, we have reanalyzed the $2\ell 2\nu 2j$ channels using complete $\mathcal{O}(\alpha_{\text{EM}}^6)$ and $\mathcal{O}(\alpha_{\text{EM}}^4\alpha_{\text{S}}^2)$ samples.

We have estimated the probability that, assuming that either the Higgsless scenario or the instance of SILH model we have considered is realized in Nature, the results of the measurements at the LHC yield results which are incompatible with the SM. We have first combined separately the three channels, $2j\ell^\pm\ell^\pm\nu\nu$, $2jZZ \rightarrow 2j\ell\nu\ell\nu$, $2jWW \rightarrow 2j\ell\nu\ell\nu$ in which the invariant mass of the final state cannot be directly measured and the four channel, $2j4\ell$, $4j\ell\nu$, $4j\ell\ell$ and $2j3\ell\nu$ in which it can instead be reconstructed. Finally we have combined all channels.

2 Calculation

Two perturbative orders contribute to the $2\ell 2\nu 2j$ and $4\ell 2j$ signals at the LHC. The purely electroweak set of diagrams at $\mathcal{O}(\alpha_{\text{EM}}^6)$ is the one which includes boson boson scattering as a subprocess. In the second set of diagrams at $\mathcal{O}(\alpha_{\text{EM}}^4\alpha_{\text{S}}^2)$ no such scattering takes place: either two fermion lines exchange a gluon or a single fermion line and two external gluons are present. In contrast with the processes examined in ref. [54, 55] where the dominating background is due to $V+4j$ $\mathcal{O}(\alpha_{\text{EM}}^2\alpha_{\text{S}}^4)$ processes in which only one vector boson is produced, in the present case the final states from both perturbative orders contain two vector bosons and are essentially impossible to separate. In ref. [61, 62] it has been pointed out that $t\bar{t}+n$ -jets production, $n = 1, 2$ can provide a significant background to vector boson scattering. Indeed, the additional jets which are present in the former processes can go undetected and mimic the signature of boson boson reactions.

Both the $\mathcal{O}(\alpha_{\text{EM}}^6)$ and the $\mathcal{O}(\alpha_{\text{EM}}^4\alpha_{\text{S}}^2)$ samples have been generated with PHANTOM, a dedicated tree level Monte Carlo generator which is documented in ref. [63] while additional material can be found in refs. [64–66]. The $t\bar{t}+n$ -jets processes have been simulated with MADEVENT [67–70] in the Narrow Width Approximation. Both programs generate events in the Les Houches Accord File Format [71]. For the LHC we have assumed the design energy of 14 TeV. For each perturbative order we have generated a sample of five hundred thousand unweighted events. In some cases additional event samples have been generated in order to increase the final statistics of particular phase space regions.

All samples have been generated using CTEQ5L [72] parton distribution functions. The QCD scale has been taken as

$$\Lambda^2 = M_W^2 + \frac{1}{6} \sum_{i=1}^6 p_{Ti}^2 \tag{2.1}$$

in all cases but for the reaction in which a triplet of final state particles with flavours compatible with deriving from the decay of a top or antitop quark could be found. In this case the scale has been taken as

$$\Lambda^2 = M_{\text{top}}^2 + p_{T_{\text{top}}}^2. \quad (2.2)$$

The analysis has been performed at parton level with no showering and hadronization.

The effective Lagrangian approach to SILH models of ref. [18] is valid for small values of ξ , while larger values demand a more detailed description of the particular model at hand. Such a Lagrangian leads to a modification of the Higgs couplings by a factor $1/\sqrt{1+c_H\xi}$, which can be reabsorbed in a Higgs propagator modification by a factor $1/(1+c_H\xi)$ in boson boson scattering studies. c_H is a pure number of order unity [11, 16–18]. For the present study we have selected the value $c_H\xi = 1$ which we intend as a possible upper limit for the model independent lagrangian description of ref. [18]. Both for the SM scenario and for the SILH model the Higgs mass has been fixed at 200 GeV. Since we are interested in large invariant mass vector vector scattering processes the actual value of the Higgs mass is irrelevant, provided it is appreciably smaller than the invariant mass of the vector pair.

For very large Higgs masses, all Born diagrams with Higgs propagators become completely negligible in the Unitary Gauge we work in. Therefore the no-Higgs model results for all processes coincide with those in the $M_H \rightarrow \infty$ limit. This framework therefore can be considered as an upper limit to SILH models and also as representative of all models in which resonances which unitarize vector vector scattering are present but too heavy to be directly detected. The no-Higgs case is also extremely useful to determine the phase space regions in which weak and strong interacting vector boson models differ the most. It is obvious that the Standard Model with an infinite mass Higgs is unphysical because of the violations of perturbative unitarity at about one TeV. This corresponds in our complete calculation to an invariant mass of the two vector bosons of the same magnitude. These events are present at the LHC but they are highly suppressed by the effective parton luminosities, as can be clearly extracted from the plots in ref. [54, 55] and in the following. We have studied the behaviour of unitarized models, and in particular we have compared the basic no-Higgs case with a model in which the no-Higgs amplitudes are unitarized using the K-matrix method and with some models which contain resonances. Typically the number of expected events in the presence of resonances is much larger than for the no-Higgs framework. What is perhaps more important, it turns out that, after cuts comparable to the ones adopted in this paper, the expected number of events in the unitarized no-Higgs model is only a few percent smaller than in the non-unitarized case. Therefore we consider the possibility of distinguishing the no-Higgs case from the SM at the LHC a quite solid benchmark for the observability of unitarized models. The details of our studies of unitarized models are given in ref. [73, 74].

The selection of events with jets widely separated in pseudorapidity is a well established technique for enhancing the scattering contributions at the LHC [25–42]. As shown in ref. [54] a powerful tool to increase the separation between the SM predictions and those of the Higgsless scenario is provided, at large invariant masses, by the request that the vector bosons and their decay products are in the central part of the detector since the

vector bosons in the Higgsless case have smaller rapidities and larger momenta than in the presence of a light Higgs.

The cuts in table 1 have been applied either at generation level or as a preliminary step to any further analysis. They require containment within the active region of the detectors and minimum transverse momentum for all observed partons; a minimum mass separation is imposed for all same-family opposite-sign charged leptons and all jet pairs. Furthermore, the two jets are required to be separated by at least three ($2j2\ell2\nu$) or four ($2j4\ell$) units in rapidity and their combined mass is forced to be outside the electroweak vector boson mass window in order to exclude three vector boson production.

We have considered two different ranges for the mass of the lepton pair in the $2j\ell^+\ell^-\nu\bar{\nu}$ channel. On one hand we have selected same flavour charged leptons with a mass in the interval $76\text{ GeV} < M(\ell^+\ell^-) < 106\text{ GeV}$. In this case we have considered the lepton pair to be produced in the decay of a Z boson. Requiring further a large missing transverse momentum we have produced an event sample corresponding to the $2jZZ \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ channel which will be discussed in section 4. When the mass of the lepton pair is outside the quoted range or the two oppositely charged leptons belong to different families we consider the event a candidate for the $2jWW$ channel. Since we are interested into high invariant mass W pairs, we have required $M(\ell^+\ell^-) > 250\text{ GeV}$ for this kind of events which will be analyzed in section 5. The mass of the WW system corresponds to the scale of boson boson scattering and large masses help in discriminating between the SM and other scenarios.

For both the Higgsless and SILH cases and for each channel we have computed the probability that, assuming a specific Beyond Standard Model (BSM) correctly describes nature, the result of an experimental outcome for a given luminosity has a chance of less than 5% in the SM (PBSM@95%CL).

For the combination of channels discussed in section 7 we have also computed the 99.7% exclusion limit (PBSM@99.7%CL).

All limits presented in the following, unless explicitly mentioned, have been computed summing over all possible combinations of first and second generation leptons, assuming an integrated luminosity of $L = 200\text{ fb}^{-1}$, which we intend as corresponding to one year of high luminosity combining CMS and ATLAS results.

We proceed as follows. We define the signal S as the sum of the events for all $\mathcal{O}(\alpha_{EM}^6)$ and $\mathcal{O}(\alpha_{EM}^4\alpha_S^2)$ processes after all selection cuts. It might be feasible to further decrease the $\mathcal{O}(\alpha_{EM}^4\alpha_S^2)$ contribution with a central jet veto, but this possibility is beyond the scope of this paper. For the $2jWW \rightarrow 2j\ell\nu\ell\nu$ channel we take as background B the expected yield of the $t\bar{t} + jets$. B and S are considered as random variables representing the number of background and signal events for a possible experimental outcome. \bar{B} and \bar{S} are the corresponding average values which will be taken equal to the predictions of our simulation. We take into account the statistical uncertainty of S assuming a standard Poisson distribution with average \bar{S} . The predicted signal cross section is also affected by theoretical uncertainties, so the parameter \bar{S} is itself subject to fluctuations. The theoretical error is modeled by a flat distribution in the window $\bar{S} \pm 30\%$ which, in our opinion, is a reasonable choice to account for both pdf's and scale uncertainties for the signal. The processes we are

$p_T(\ell^\pm) > 20 \text{ GeV}$
$ \eta(\ell^\pm) < 3.0$
$M(\ell^+\ell^-) > 20 \text{ GeV}$
$M(\ell^+\ell^-) > 250 \text{ GeV} \quad (2jW^+W^-)$
$76 \text{ GeV} < M(\ell^+\ell^-) < 106 \text{ GeV} \quad (2jZZ)$
$p_T(j) > 30 \text{ GeV}$
$ \eta(j) < 6.5$
$M(jj) > 60 \text{ GeV}$
$M(jj) < 70 \text{ GeV}; M(jj) > 100 \text{ GeV}$
$ \Delta\eta(jj) > 3.0 \quad (2j2\ell2\nu)$
$ \Delta\eta(jj) > 4.0 \quad (2j4\ell)$

Table 1. Acceptance cuts.

interested in require center of mass energies of the order of the TeV and therefore involve quarks with rather large longitudinal momentum fraction x , $x \approx 10^{-1} \div 10^{-2}$ at a typical scale Λ of about 100 GeV. In this region the uncertainty due to the parton distribution functions is of the order of 5% [75, 76]. As already stated, QCD corrections are in the range of 10% and, as a consequence theoretical uncertainties are expected to be well within this order of magnitude.

Only statistical fluctuations have been taken into consideration in the case of B . This is motivated by the fact that the $t\bar{t} + jets$ background is likely to be well measured experimentally in final states in which more than two jets are detected and then extrapolated via Monte Carlo to the region of interest in this paper, so that the theoretical error on B is not expected to be an issue at the time when real data analysis will be performed. In section 7 we will also discuss how our results would be affected if $t\bar{t} + jets$ were not measured.

We define the test statistics $D = S + B - \bar{B}$ which reduces to S in the absence of background. Having computed the probability distributions $P(D|SM)$ and $P(D|BSM)$ of D in the Standard Model and in the Beyond the Standard Model under consideration, the 95%CL region for the SM can be defined from the probability ratio

$$Q(D) = \frac{P(D|BSM)}{P(D|SM)} \tag{2.3}$$

determining a number α such that

$$\int dD P(D|SM) \theta(\alpha - Q) = 95\%. \tag{2.4}$$

The probability for the BSM to yield a result outside this 95%CL region for the SM is then

$$P_{BSM@95\%CL} = \int dD P(D|BSM) \theta(Q - \alpha). \tag{2.5}$$

A number of comments, which apply to all channels discussed in this paper, should be made. We have performed a simple cut based study, which can undoubtedly be improved

M_{cut} (GeV)	no Higgs	SILH	$M_H = 200$ GeV
	$\sigma(\text{fb})$	$\sigma(\text{fb})$	$\sigma(\text{fb})$
200	3.11(2.39)	2.87(2.15)	2.73(2.01)
300	1.73(1.23)	1.55(1.06)	1.46(.967)
400	1.01(.682)	.892(.560)	.839(.507)
500	.630(.407)	.538(.315)	.505(.283)
600	.400(.253)	.334(.187)	.311(.163)
700	.262(.162)	.214(.114)	.198(.0975)
800	.177(.108)	.142(.0728)	.130(.0613)

Table 2. Total cross section for the $\ell^\pm \ell^\pm \nu\nu + 2j$ channel after generation cuts, table 1. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample.

upon with a more sophisticated multivariate analysis. On the other hand we have not taken into account experimental efficiencies and all issues related to additional hadronic activity due to showering and the underlying event. The selection cuts discussed below have been chosen in order to maximize the separation of the light Higgs case from the no-Higgs one.

In the following we will present cross sections as a function of appropriate minimum invariant masses M_{cut} , typically extracted from lepton momenta. The best discrimination between the SM and the BSM schemes are generally obtained for M_{cut} values which yield production rates which are uncomfortably small, particularly because of neglected experimental uncertainties. It should however be noticed that at smaller values of M_{cut} the rate is usually much larger with a modest decrease of discriminating power.

3 The $2j\ell^\pm\ell'^\pm\nu\nu$ channel: two same-sign leptons in the final state

This channel, which is characterized by two same sign charged leptons, possibly of different flavour, in the final state, has low EW and QCD background, for no external gluons contribute to this final state. We remark that the production of two same-sign W 's has been extensively discussed in the context of Multiple Particle Interactions (MPI) [77–79], since it has the peculiarity that it can be realized in MPI at a lower perturbative order than in ordinary two parton collisions where at least two additional partons must appear in the final state. However, if two jets in the final state are required, the MPI contribution is small and concentrated in the region of small total visible energy and therefore has been neglected.

The presence of two neutrinos in the final state makes it impossible to reconstruct the invariant mass of the di-boson system which corresponds to the center of mass energy of the WW scattering. For M_{cut} we have resorted to a correlated observable, the di-lepton mass $M(\ell\ell)$.

The total cross section for the $2j\ell^\pm\ell'^\pm\nu\nu$ channel with the acceptance cuts in table 1 is presented in table 2 as a function of the minimum $\ell\ell$ invariant mass M_{cut} . In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ processes. Table 2 shows that the cross section for the $\mathcal{O}(\alpha_{\text{EM}}^4\alpha_s^2)$ processes is only about 25% to 40% of the total cross section in the Higgsless scenario

$\Delta\eta(jj) > 4.5$
$\max \eta(j) > 2.5$
$ \eta(j) > 1.$
$ \eta(\ell) < 2.5$
$p_T(\ell) > 50 \text{ GeV}$
$\min p_T(j) < 120 \text{ GeV}$
$\Delta R(\ell j) > 1.5$
$ \vec{p}_T(\ell_1) - \vec{p}_T(\ell_2) > 150 \text{ GeV}$
$\cos(\delta\phi_{\ell\ell}) < -0.6$

Table 3. Additional selection cuts for channel $2j\ell^\pm\ell^\pm\nu\nu$.

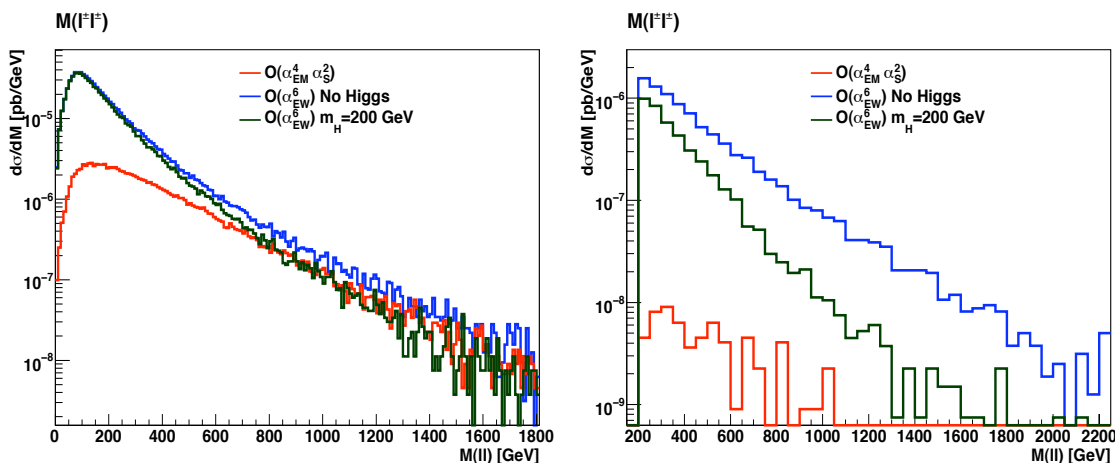


Figure 1. $M(\ell\ell)$ distribution with acceptance cuts only, table 1 (left) and after all additional selection cuts, table 3 (right).

already at this level. The distribution of the lepton pair mass, with acceptance cuts only, is presented on the left hand side of figure 1. The $\mathcal{O}(\alpha_{EM}^4\alpha_S^2)$ background is negligible at small di-lepton mass, while it becomes of the same order of magnitude of the $\mathcal{O}(\alpha_{EM}^6)$ contribution for $M_{cut} > 500 \text{ GeV}$.

In the following, as already mentioned, we will consider the full sample as our signal. It is possible to improve the discriminating power of the analysis increasing the fraction of $\mathcal{O}(\alpha_{EM}^6)$ events in the event sample since only those are sensitive to the mechanism of EWSB. Therefore, on the generated samples we have applied the additional selection cuts shown in table 3. These cuts force the two tag jets to be well separated and not central. One of the two leading jets is forbidden from having a very large transverse momentum. The two charged leptons are required to be rather central and well separated from the jets. They are required to be well separated in the transverse plane and to have large transverse momentum. Finally, the vector difference between the lepton momenta is required to be large.

M_{cut} (GeV)	no Higgs		SILH		$M_H = 200$ GeV
	$\sigma(\text{fb})$	PBSM	$\sigma(\text{fb})$	PBSM	$\sigma(\text{fb})$
200	.435(.431)	94.9%	.276 (.273)	39.1%	.206(.203)
300	.290(.288)	98.2%	.166 (.164)	42.3%	.114(.111)
400	.191(.189)	98.7%	.0977(.0958)	41.2%	.0629(.0609)
500	.129(.128)	98.7%	.0604(.0588)	34.4%	.0351(.0336)
600	.0886(.0876)	97.5%	.0385(.0375)	37.1%	.0194(.0183)
700	.0614(.0607)	96.6%	.0262(.0254)	42.3%	.0112(.0105)
800	.0438(.0432)	91.1%	.0184(.0178)	31.2%	.00701(.00640)

Table 4. Total cross section for the $\ell^\pm\ell^\pm\nu\nu + 2j$ channel in femtobarns, with the full set of cuts in table 1 and table 3, as a function of the minimum dilepton invariant mass M_{cut} for the $\ell^\pm\ell^\pm$ system. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample. We also show the PBSM probabilities. The result for $M_{\text{cut}} = 400$ GeV which provides the best discrimination between the Higgsless and light Higgs scenario is highlighted.

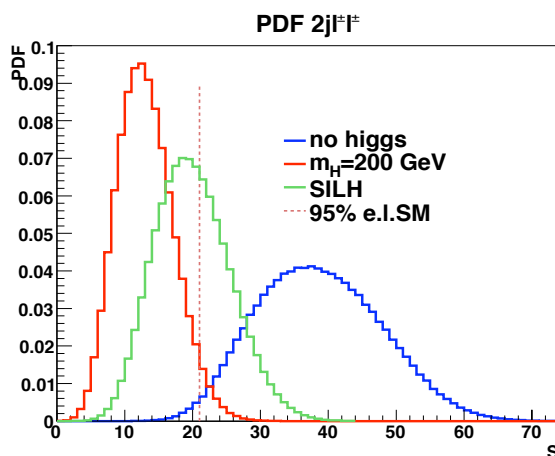


Figure 2. Probability distribution for no-Higgs, SILH and SM cases for the $2j\ell^\pm\ell^\pm\nu\nu$ channel. The vertical line indicates the 95%CL for the SM. $M_{\text{cut}} = 400$ GeV.

The total cross section in femtobarns for the $2j\ell^\pm\ell^\pm\nu\nu$ channel, with the full set of cuts in table 1 and table 3, as a function of the minimum invariant mass M_{cut} is shown in table 4. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ contribution, which dominate the cross section, are reported. The distribution of $M(\ell\ell)$ is presented on the right hand side of figure 1 which clearly demonstrates the good separation between the two scenarios obtained through the additional cuts. As expected the separation increases with increasing di-lepton invariant mass.

In table 4 we also give the PBSM@95%CL for the two BSM scenarios. The corresponding normalized frequency for the three scenarios, as a function of the number of events, is reported in figure 2 for $M_{\text{cut}} = 400$ GeV. The red curve refers to the probability distribution for a Higgs of 200 GeV while the green one refers to the SILH model and the blue one to the no-Higgs case. The dotted vertical line in the plot marks the 95% exclusion limit for the SM predictions.

M_{cut} (GeV)	no Higgs	SILH	$M_H = 200$ GeV
	$\sigma(\text{fb})$	$\sigma(\text{fb})$	$\sigma(\text{fb})$
300	1.84 (.607)	1.73 (.494)	1.70(.464)
400	.675 (.319)	.578 (.222)	.544(.187)
500	.363 (.197)	.288 (.122)	.262(.0962)
600	.223 (.134)	.161 (.0727)	.140(.0515)
700	.143 (.0952)	.0947(.0466)	.0781(.0300)
800	.0926(.0686)	.0553(.0313)	.0426(.0186)
900	.0646(.0515)	.0341(.0210)	.0251(.0120)

Table 5. Total cross section for the $(ZZ)\ell^+\ell^-\nu\nu + 2j$ channel after generation cuts, table 1. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample.

The probability of an experiment to find a result incompatible with the SM at 95%CL, assuming that the Higgsless model is realized in Nature, is of the order of 99% for $M_{\text{cut}} = 400$ GeV and decreases to about 90% for $M_{\text{cut}} = 800$ GeV. Because of the absence of large backgrounds this channel has a discriminating power which is in fact quite high. The corresponding probabilities for the SILH model vary between 30% and 40%.

About 40(20) events are predicted for the Higgsless(SILH) scenario assuming our standard luminosity of $L = 200 \text{ fb}^{-1}$ and $M_{\text{cut}} = 400$ GeV, which provides the best discrimination between the Higgsless scenario and the SM.

4 The $2jZZ \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ channel: two opposite-sign same-flavour leptons in the final state

This channel has been separated from the $2jWW \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ case using the di-lepton mass. If $|M(\ell\ell) - M_Z| < 15$ GeV, the event is considered as produced by a ZZ intermediate state. Since the mass of the final state ZZ system cannot be fully reconstructed we estimate the center of mass energy of the vector boson scattering from the transverse mass:

$$M_T^2(ZZ) = [\sqrt{M_Z^2 + p_T^2(\ell\ell)} + \sqrt{M_Z^2 + p_{T\text{miss}}^2}]^2 - |\vec{p}_T(\ell\ell) + \vec{p}_{T\text{miss}}|^2 \quad (4.1)$$

The total cross section for the $2jZZ \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ channel with the acceptance cuts in table 1 is presented in table 5 as a function of the minimum $M_{\text{cut}} = M_T(ZZ)$. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ processes.

The $M_T(ZZ)$ distribution, with acceptance cuts only, is presented on the left hand side of figure 3. The QCD background is much larger than in the channels discussed in section 3. The contribution from top pair production is large, particularly at small transverse masses, even though we are requiring a lepton pair with an invariant mass in the neighborhood of the Z mass. This contribution rapidly fades at large $M_T(ZZ)$ where the QCD processes without top are dominating. Moreover, since no requirement of large missing transverse momentum has been imposed, additional backgrounds at small transverse masses are generated by $2jZ \rightarrow 2j\ell^+\ell^-$ production. We have not included this

$\Delta\eta(jj) > 4.5$
$M(jj) > 800 \text{ GeV}$
$\Delta\eta(\ell j) > 1.3$
$p_{T\text{miss}} > 120 \text{ GeV}$
$ \vec{p}_T(\ell^+\ell^-) - \vec{p}_T^{\text{miss}} > 290 \text{ GeV}$
$p_T(\ell^+\ell^-) > 120 \text{ GeV}$
$ \eta(j) > 1.9$

Table 6. Selection cuts for channel $(ZZ)\ell^+\ell^-\nu\nu + 2j$.

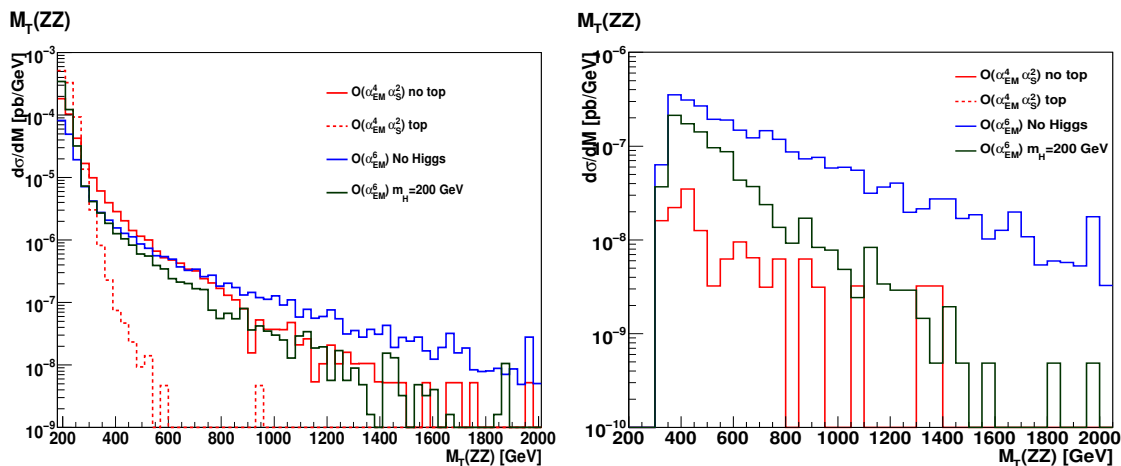


Figure 3. ZZ transverse mass distribution with initial cuts, table 1 (left) and adding extra cuts, table 6 (right).

background contribution in our study since large $p_{T\text{miss}}$ is demanded in our final analysis and this additional contribution is completely eliminated.

In order to sharpen the separation between the Standard Model results and those from alternative symmetry breaking scenarios we impose the additional cuts in table 6.

The total cross section in femtobarns for the $2jZZ \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ channel, with the full set of cuts in table 1 and table 6, as a function of the minimum ZZ transverse mass M_{cut} is shown in table 7. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ contribution. The PBSM probabilities are also given.

The $M_T(ZZ)$ distribution, with the full set of cuts, is presented on the right hand side of figure 3. The $\mathcal{O}(\alpha_{\text{EM}}^4 \alpha_S^2)$ background has been sharply reduced while increasing the separation between the Higgsless and light Higgs scenarios. The top related background has been totally suppressed.

The probability distribution for the three scenarios is reported in figure 4 for $M_T(ZZ)_{\text{cut}} = 600 \text{ GeV}$. The red curve refers to a Higgs of 200 GeV while the green one refers to the SILH model and the blue one to the no-Higgs case. The dotted vertical line in the plot marks the 95% exclusion limit for the SM predictions. The probability of an experiment to find a result incompatible with the SM at 95%CL, assuming that the

M_{cut} (GeV)	no Higgs		SILH		$M_H = 200$ GeV
	$\sigma(\text{fb})$	PBSM	$\sigma(\text{fb})$	PBSM	$\sigma(\text{fb})$
300	.143(.136)	94.6%	.0770(.0700)	31.5%	.0540(.0470)
400	.120(.115)	96.1%	.0614(.0564)	36.2%	.0396(.0345)
500	.0887(.0860)	97.5%	.0396(.0369)	39.8%	.0214(.0187)
600	.0691(.0668)	98.4%	.0268(.0246)	44.3%	.0118(.00957)
700	.0547(.0533)	97.0%	.0186(.0171)	32.0%	.00697(.00555)
800	.0410(.0401)	94.6%	.0145(.0136)	33.2%	.00463(.00368)
900	.0327(.0321)	94.3%	.00991(.00927)	31.9%	.00300(.00236)

Table 7. Total cross section for the $(ZZ)\ell^+\ell^-\nu\nu + 2j$ channel in femtobarns, with the full set of cuts in table 1 and table 6, as a function of the minimum transverse mass $M_T(ZZ)_{\text{cut}}$. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample. The PBSM@95%CL are also shown.

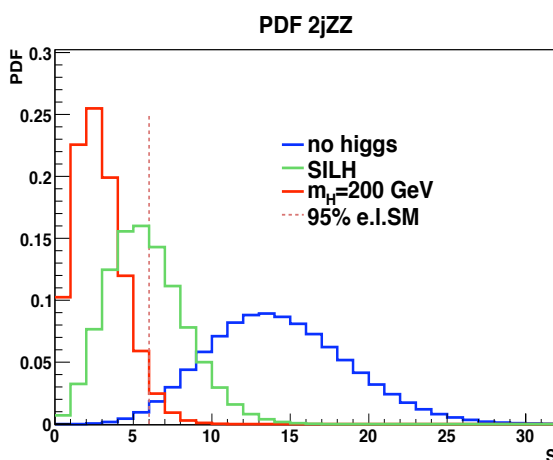


Figure 4. Probability distribution for the no-Higgs, SILH and SM cases for the $2jZZ \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ channel. The vertical line indicates the 95%CL for the SM. $M_{\text{cut}} = 600$ GeV.

Higgsless model is realized in Nature, is of the order of 98% for $M_{\text{cut}} = 600$ GeV and does not vary significantly over the range considered in table 7. The corresponding probabilities for the SILH model vary between 30% and 45%.

5 The $2jW^+W^- \rightarrow 2j\ell^+\ell'^-\nu\bar{\nu}$ channel: two opposite-sign leptons in the final state

The total cross section for the $2jW^+W^- \rightarrow 2j\ell^+\ell'^-\nu\bar{\nu}$ channel, with the acceptance cuts in table 1, is shown in table 8 as a function of the minimum $\ell\ell$ invariant mass. As usual, in parentheses we show the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ processes. The cross sections for $t\bar{t}j$ and $t\bar{t}jj$ production are presented separately. We have required exactly two jets in the acceptance region. This however is not sufficient to guarantee a well defined cross section because two b quarks are produced in the leptonic decay of the tops. Therefore we have further required that one b for $t\bar{t}j$ events and both b 's for $t\bar{t}jj$ ones remain undetected. We

M_{cut} (GeV)	no Higgs	SILH	$M_H = 200$ GeV	$t\bar{t}j$	$t\bar{t}jj$
	$\sigma(\text{fb})$	$\sigma(\text{fb})$	$\sigma(\text{fb})$	$\sigma(\text{fb})$	$\sigma(\text{fb})$
300	70.0(4.65)	69.7(4.42)	69.7(4.35)	39.7	2.59
400	29.7(2.32)	29.5(2.11)	29.5(2.12)	16.4	1.22
500	13.5(1.24)	13.4(1.14)	13.4(1.13)	7.21	.516
600	6.69(.713)	6.62(.643)	6.60(.627)	3.13	.237
700	3.55(.440)	3.49(.376)	3.47(.362)	1.45	.139
800	1.92(.274)	1.88(.236)	1.87(.225)	.849	.0737

Table 8. Total cross section for the $(W^+W^-)\ell^+\ell^-\nu\nu + 2j$ channel after initial cuts, table 1 in function of the minimum $\ell\ell$ invariant mass, $M(\ell\ell)$. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample.

consider a b -quark detected if $|\eta_b| < 5$ and $p_{Tb} > 30$ GeV. As a consequence the partons produced in association with the $t\bar{t}$ pair are forced to be visible and the corresponding cross section is finite. The phase space regions which are excluded by these constraints are eliminated by the cut on the mass of all lepton-jet pairs discussed below.

This process has the largest production rate among all channels considered in this paper, however the QCD background is much larger than the electroweak part.

The $M(\ell\ell)$ distribution, with acceptance cuts only, is presented on the left hand side of figure 5. $t\bar{t}$ production is very important at this level, and the usual way to suppress it, by requiring $M(Wj)$ out of the top nominal mass window, is not applicable because of the impossibility to reconstruct the W mass. Instead we require the mass of all lepton-jet pairs to be larger than the top mass.

The relatively high signal rate and the large background allow and require harder cuts than in all previous cases. The additional selection requirements are shown in table 9. The constraint on the lepton-jet mass is quite effective in reducing the background due to top pair production. The $t\bar{t}$ and $t\bar{t}j$ contributions are essentially eliminated and the two light partons in $t\bar{t}jj$ production are forced to be tagged. However this cut reduces significantly the boson scattering signal and furthermore it increases the relative contribution of $t\bar{t}jj$.

The total cross section in femtobarns for the $(W^+W^-)\ell^+\ell^-\nu\nu + 2j$ channel, with the full set of cuts in table 1 and table 9, as a function of the minimum di-lepton invariant mass M_{cut} is shown in table 10. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ contribution. The PBSM probabilities are also presented. As mentioned in section 2 only the statistical uncertainty has been taken into account for the $t\bar{t}jj$ background. The requirement that both b -quarks have a transverse momentum smaller than 30 GeV or a rapidity in modulus larger than 5 units is quite stringent, in fact the cross section for $t\bar{t}jj$ requiring both b 's to produce visible jets, not necessarily identified as b -jets, is at least an order of magnitude larger than the results presented in table 10. Therefore, we believe the $t\bar{t}jj$ will be measured in the complementary region and extrapolated to the signal domain with small uncertainty. In any case, since the hadronic activity is expected to be much higher in $t\bar{t}$ +jets events than in boson boson scattering ones, a more accurate assessment of this background would require complete showering and hadronization.

$M(jj) > 1000 \text{ GeV}$
$\Delta\eta(jj) > 4.8$
$ \eta(\ell) < 2.00$
$p_T(\ell) > 40 \text{ GeV}$
$\max \eta(j) > 2.5$
$ \eta(j) > 1.3$
$E(j) > 180 \text{ GeV}$
$\Delta\eta(\ell j) > 0.8$ (and $\Delta R(\ell j) > 1$)
$M(\ell j) > 180 \text{ GeV}$
$ \vec{p}_T(\ell^+) - \vec{p}_T(\ell^-) > 220 \text{ GeV}$
$\cos(\delta\phi_{\ell\ell}) < -0.6$

Table 9. Additional selection cuts for the $2jW^+W^- \rightarrow 2j\ell^+\ell^-\nu\nu$ channel.

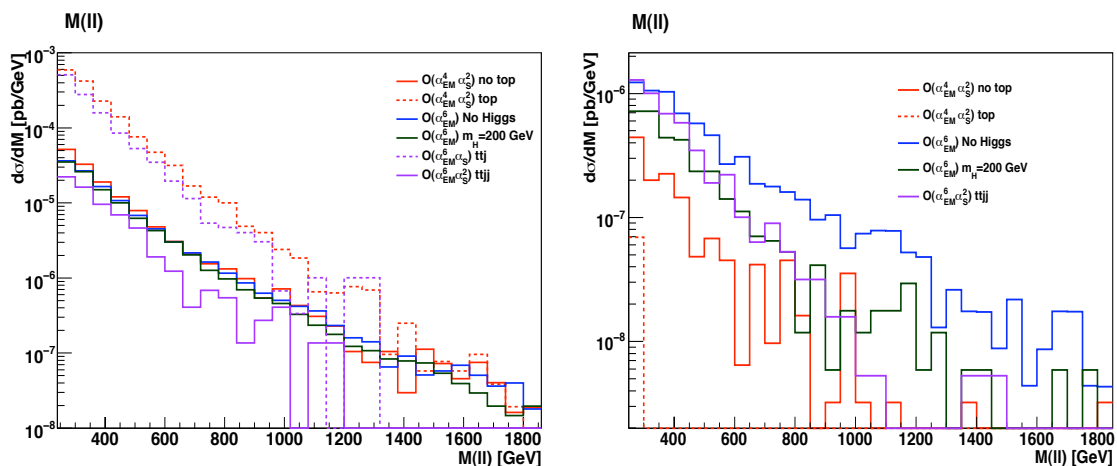


Figure 5. Di-lepton mass distribution with initial cuts, table 1 (left) and adding extra cuts, table 9 (right).

We will come back to the impact on our results in case the $t\bar{t}jj$ could not be measured in section 7. For the time being we only report that the PBSM@95%CL reported in table 10 for $M_{\text{cut}} = 600 \text{ GeV}$ would change from 85% to 78% for the no Higgs case and from 27% to 22% for the SILH model.

The di-lepton mass distribution, with the full set of cuts, is presented on the right hand side of figure 5. The $\mathcal{O}(\alpha_{\text{EM}}^4 \alpha_S^2)$ background is now very small while the separation between the Higgsless and light Higgs scenarios is clearly visible.

The probability distribution for the three scenarios is reported in figure 6 for $M(l)_{\text{cut}} = 600 \text{ GeV}$. The probability of an experiment to find a result incompatible with the SM at 95%CL, assuming that the Higgsless model is realized in Nature, is between 80 and 85% for $300 \text{ GeV} < M_{\text{cut}} < 700 \text{ GeV}$. For the SILH model the corresponding probabilities lie between 20 and 26%.

M_{cut} (GeV)	no Higgs		SILH		$M_H = 200$	$t\bar{t}jj$
	$\sigma(\text{fb})$	PBSM	$\sigma(\text{fb})$	PBSM	$\sigma(\text{fb})$	$\sigma(\text{fb})$
300	.337(.292)	79.58%	.224(.179)	22.69%	.179(.134)	.173
400	.212(.188)	80.74%	.131(.107)	20.89%	.100 (.0765)	.0890
500	.139(.125)	82.83%	.0841(.0700)	26.35%	.0577(.0435)	.0407
600	.0968(.0883)	85.03%	.0533(.0448)	26.56%	.0332(.0247)	.0215
700	.0696(.0635)	80.55%	.0353(.0292)	20.63%	.0217(.0156)	.0138

Table 10. Total cross section for the $2jW^+W^- \rightarrow 2j\ell^+\ell^-\nu\nu$ channel in femtobarns, with the full set of cuts in table 1 and table 9, as a function of the minimum di-lepton invariant mass $M(\ell\ell)_{\text{cut}}$. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample. The PBSM@95%CL are given in the third and fifth column.

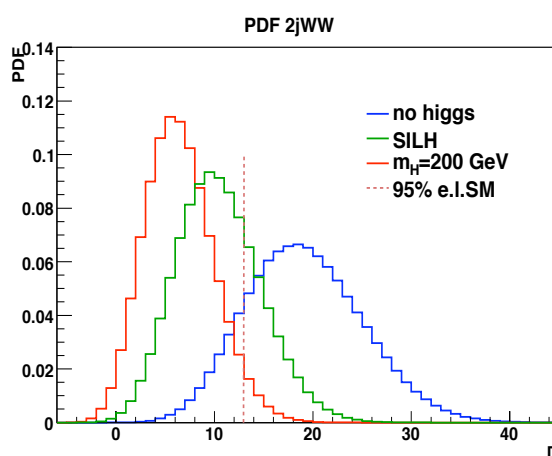


Figure 6. Probability distribution for the no-Higgs, SILH and SM cases for the $2jW^+W^- \rightarrow 2j\ell^+\ell^-\nu\bar{\nu}$ channel. The vertical line indicates the 95%CL for the SM. $M_{\text{cut}} = 600$ GeV.

$M(jj) > 800$ GeV
$p_T(Z) > 100$ GeV
$\Delta R(Zj) > 1$
$\cos(\delta\phi_{ZZ}) < -0.4$

Table 11. Additional selection cuts for the $2j4\ell$ channel.

6 The $2j4\ell$ channel

Contrary to all reaction discussed above, in the $2j4\ell$ channel the mass of the final state vector boson pair can be directly measured to a high precision. It is presented here for completeness despite its small rate and statistical discriminating power.

The QCD contribution is small already at generation level. However, for a luminosity of $L = 200 \text{ fb}^{-1}$ the difference between the number of events expected for an infinite mass Higgs and a light one is of the order the statistical uncertainty for the $\mathcal{O}(\alpha_{\text{EM}}^4 \alpha_s^2)$ contribution and no meaningful separation between the two cases can be obtained. Only

M_{cut} (GeV)	no Higgs		SILH		$M_H = 200$ GeV
	$\sigma(\text{ab})$	PBSM	$\sigma(\text{ab})$	PBSM	$\sigma(\text{ab})$
300	51.8(41.6)	35.6%	36.1(26.0)	8.4%	31.6(21.5)
400	44.7(36.7)	40.7%	30.1(22.1)	10.3%	25.5(17.5)
500	35.6(30.1)	41.8%	22.8(17.3)	10.5%	18.4(12.9)
600	28.2(24.2)	34.1%	17.2(13.2)	7.0%	13.5(9.45)
700	22.2(19.5)	29.3%	12.8(10.0)	5.3%	9.64(6.93)
800	17.8(15.8)	29.1%	9.79(7.82)	5.4%	7.09(5.12)
900	14.0(12.6)	31.0%	7.38(6.05)	6.7%	5.19(3.87)

Table 12. Total cross section for the $4\ell + 2j$ channel in attobarns, with the full set of cuts in table 1 and table 11, as a function of the minimum invariant mass M_{cut} for the 4ℓ system. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample. Also shown are the PBSM probabilities.

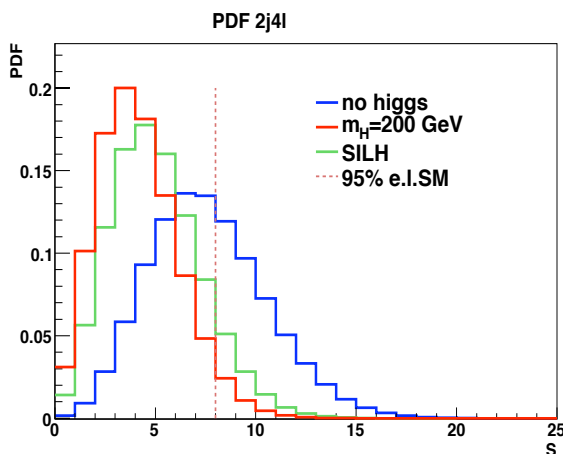


Figure 7. Probability distribution for the no-Higgs, SILH and SM cases for the $2j4\ell$ channel. The vertical line indicates the 95%CL for the SM. $M_{\text{cut}} = 500$ GeV.

a minimum set of additional cuts can be applied in order to have at least a handful of events for $L = 200 \text{ fb}^{-1}$. This channel could clearly profit from higher luminosities. The additional selection cuts are shown in table 11.

The cross section after these extra cuts is presented in table 12 as a function of the minimum ZZ mass. In parentheses the results for the $\mathcal{O}(\alpha_{\text{EM}}^6)$ sample. We also show the PBSM@95%CL for the standard $L = 200 \text{ fb}^{-1}$ luminosity.

The probability distribution of the discriminant S for the three scenarios is reported in figure 7 for $M_{\text{cut}} = 500$ GeV with the full set of cuts in table 1 and table 11.

As reported in table 12, the probability of an experiment to find a result incompatible with the SM at 95%CL, assuming that the Higgsless model is realized in Nature, is of the order of 42% for $M_{\text{cut}} = 500$ GeV and decreases to about 30% for $M_{\text{cut}} = 700$ GeV. For the SILH model the PBSM@95%CL is only about 10% at most, for $M_{\text{cut}} = 500$ GeV.

For $L = 200 \text{ fb}^{-1}$ and summing over all final states, the expected total rates are of the order of $4 \div 8$ events for the Higgsless case.

	S(noHiggs)	S(SILH)	S($m_H = 200$ GeV)	B $\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$	$t\bar{t}jj$
$4j\ell\nu$	473.6	281.6	210.4	1956.	92.6
$4j\ell^+\ell^-$	61.6	30.4	19.38	220.	—
$2j\ell^+\ell^-\ell'\nu$	10.8	5.4	3.4	—	—
$2j\ell^+\ell^-\ell^+\ell^-$	7.12	4.56	3.68	—	—

Table 13. Number of events expected for $L = 200fb^{-1}$ for the channels in which the VV mass can be reconstructed. The cuts for the first three reactions are described in [54] and [55]. The cuts for the $2j4\ell$ channel are discussed in section 6. M_{cut} is chosen in such a way that the best PBSM@95%CL for each channel is obtained.

	S(noHiggs)	S(SILH)	S($m_H = 200$ GeV)	$t\bar{t}jj$
$2j\ell^\pm\ell^\pm\nu\nu$	38.2	19.54	12.58	—
$2jZZ \rightarrow \ell^+\ell^-\nu\nu$	13.82	5.36	2.36	—
$2jW^+W^- \rightarrow \ell^+\ell^-\nu\nu$	19.36	10.66	6.64	4.3

Table 14. Number of events expected for $L = 200fb^{-1}$ for the channels in which the VV mass cannot be reconstructed. M_{cut} is chosen in such a way that the best PBSM@95%CL for each channel is obtained.

7 Combining all channels

In this section we derive the probability that, assuming that either the Higgsless scenario or the instance of SILH model we have considered is realized in Nature, the results of the measurements of the seven channels $2j\ell^\pm\ell^\pm\nu\nu$, $2jZZ \rightarrow 2j\ell\nu\ell\nu$, $2jWW \rightarrow 2j\ell\nu\ell\nu$, $2j4\ell$, $4j\ell\nu$, $4j\ell\ell$ and $2j3\ell\nu$ at the LHC yield results which are outside the 95% probability region for the SM.

Table 13 shows the number of expected events for the reactions in which the VV mass can be reconstructed. The data for $4j\ell\nu$ production are taken from ref. [54] while those for $4j\ell^+\ell^-$ and $2j\ell^+\ell^-\ell'\nu$ are from ref. [55] to which we refer for more details. Table 14 instead shows the number of expected events for the channels in which direct reconstruction of the vector boson pair mass is impossible. In both instances the assumed integrated luminosity is $200fb^{-1}$. In each case the prediction corresponds to the value of M_{cut} which gives the best PBSM@95%CL. These values are highlighted in tables 4, 7, 10 and 12 for the reactions described in detail in this paper. For the remaining channels M_{cut} has been set to 600 GeV.

For a given number of events for each channel k_1, k_2, \dots, k_n , with corresponding mean values $\lambda_1, \lambda_2, \dots, \lambda_n$, which we will refer to collectively as \vec{k} and $\vec{\lambda}$, the standard likelihood ratio in eq. (2.3) can be expressed as $Q(\vec{k}; \vec{\lambda}_{BSM}, \vec{\lambda}_{SM}) = P(\vec{k}, \vec{\lambda}_{BSM})/P(\vec{k}, \vec{\lambda}_{SM})$

The procedure we have employed so far and in ref. [55] to evaluate the PBSM becomes cumbersome when too many channels have to be considered and the dimensionality of the integrals in eqs. (2.4), (2.5) becomes large. Therefore for the combination of all results we have resorted to the variable $-2\ln Q$. From the one dimensional probability distribution of $-2\ln Q$ the 95%CL and 99.7%CL limits for the SM can be easily determined.

In the following we will first combine separately the first three channels, in which the

uncorrelated error				
	non-reconstructable		reconstructable	
	NOH	SILH	NOH	SILH
95%CL	>99.99 %	76.24 %	99.96%	52.81%
99.7%CL	99.98 %	40.34%	99.37%	18.61%

Table 15. Probability to exclude the SM with different confidence levels, for different strong alternative scenarios combining the three non-reconstructable channels ($2j\ell^\pm\ell^\pm\nu\nu$, $ZZ \rightarrow 2j\ell\nu\ell\nu$ and $WW \rightarrow 2j\ell\nu\ell\nu$), and the four reconstructable ones ($4j\ell\nu$, $4j\ell\ell$, $2j3\ell\nu$ and $2j4\ell$). Theoretical errors are assumed to be uncorrelated as in eq. (7.1).

strongly-correlated error				
	non-reconstructable		reconstructable	
	NOH	SILH	NOH	SILH
95%CL	99.99 %	66.05%	99.34%	44.07%
99.7%CL	99.66 %	34.33%	94.24%	16.07%

Table 16. Probability to exclude the SM with different confidence levels, for different strong alternative scenarios combining the three non-reconstructable channels ($2j\ell^\pm\ell^\pm\nu\nu$, $ZZ \rightarrow 2j\ell\nu\ell\nu$ and $WW \rightarrow 2j\ell\nu\ell\nu$), and the four reconstructable ones ($4j\ell\nu$, $4j\ell\ell$, $2j3\ell\nu$ and $2j4\ell$). Theoretical errors are assumed to be fully correlated as in eq. (7.3).

invariant mass of the VV pair cannot be reconstructed, and the last four, in which the VV mass can be directly measured. Later we will proceed to a full combination.

The probability $P(\vec{k}, \vec{\lambda})$ depends on the correlations between channels. In our simplified approach in which only statistical and theoretical errors are accounted for, only the uncertainties which are related to theory are correlated. Statistical errors in each channel are independent.

As a first step, we assume each channel to be subject to an independent theoretical error which is implemented by smearing the mean value for each channel separately and then combining the smeared channels. The corresponding probability, for the simple case in which the $\mathcal{O}(\alpha_{EM}^2 \alpha_S^4)$ background is absent, is given by:

$$P_U(\vec{k}; \vec{\lambda}) = \prod_i \int dx_i \rho(x_i) \mathcal{P}(k_i, (1+x_i)\lambda_i) \tag{7.1}$$

where $\mathcal{P}(k, \lambda)$ is the standard Poisson distribution with mean λ and

$$\rho(x) = \begin{cases} \frac{1}{2 \times 0.3} & \text{if } |x| < 0.3 \\ 0 & \text{otherwise} \end{cases} \tag{7.2}$$

models the (flat) theoretical uncertainty.

Combining separately the two set of channels we obtain the probabilities to exclude the SM at 95%CL and at 99.7%CL shown in table 15.

The hypothesis that the theoretical errors in each channel are independent may underestimate the actual uncertainty. The dominant production mechanisms are the same for all

total combination				
	NOH	SILH	NOH($L = 50 \text{ fb}^{-1}$)	SILH($L = 400 \text{ fb}^{-1}$)
95%CL	>99.99%	69.32%	96.31%	80.82%
99.7%CL	99.96%	41.67%	83.64%	57.16%

Table 17. Statistical combination of all seven channels. Also shown are the results using an integrated luminosity of $L = 50 \text{ fb}^{-1}$ for the no-Higgs and of $L = 400 \text{ fb}^{-1}$ for the SILH scenario. For the no-Higgs analysis we have used the lowest mass cut for each channel in order to increase the number of events at this luminosity.

channels and therefore it is likely that both pdf and scale uncertainties are fully correlated between channels. Assuming this to be the case for the total theoretical uncertainty, the average values of each channel which enter the combination must be shifted by a common factor and the corresponding probability P_C can be expressed as

$$P_C(\vec{k}; \vec{\lambda}) = \int dx \rho(x) \prod_i \mathcal{P}(k_i, (1+x)\lambda_i). \tag{7.3}$$

The PSM@95%CL and PSM@99.7%CL in case of complete correlation between theoretical errors are shown in table 16. Comparing table 16 with table 15, it is clear that dropping the hypothesis of independent theoretical errors degrades little the overall probability. Within the present theoretical framework it remains certain that the no-Higgs case would be distinguished from the SM case. In the SILH model the PSM@95%CL drops from 76% to 66% for the non-reconstructable channels and from 53% to 44% for the reconstructable ones.

The non-reconstructable channels presented here, independently of the detailed treatment of the theoretical uncertainty, provide a better discrimination between the SM and the BSM scenarios, despite their low rates, than those in which the invariant mass of the boson pair can be measured. This is clearly related to the absence of huge QCD backgrounds, which are instead present in the $V + 4j$ channels. The statistical uncertainties of these background are large and spoil the significance of the corresponding channels even when the backgrounds are assumed to be measured from the sidebands of the weak boson peak in the mass distribution of the two central jets and then subtracted as proposed in ref. [54, 55].

The distribution of $-2 \ln Q$, for the combination of all seven channels, in the Higgsless and SILH scenarios with our standard luminosity are shown in the top row of figure 8. In the bottom row of figure 8 we present the distributions for the Higgsless case with a luminosity of 50 fb^{-1} and for the SILH model with $L = 400 \text{ fb}^{-1}$. In all cases theoretical errors are treated as fully correlated. For the no-Higgs case at $L = 50 \text{ fb}^{-1}$ we have adopted the lowest invariant mass cut reported in tables 4, 7, 10 and 12 for the reactions discussed in this paper, in order to increase the number of events at this luminosity. Explicitly, $M_{\text{cut}} = 200, 300, 300, 300 \text{ GeV}$ for the $2j\ell^\pm\ell^\pm\nu\nu$, $ZZ \rightarrow 2j\ell\nu\ell\nu$, $WW \rightarrow 2j\ell\nu\ell\nu$ and $2j4\ell$ channel respectively. For the remaining channels M_{cut} has been kept at 600 GeV. The corresponding PSM@95%CL and PSM@99.7%CL are given in table 17. Assuming

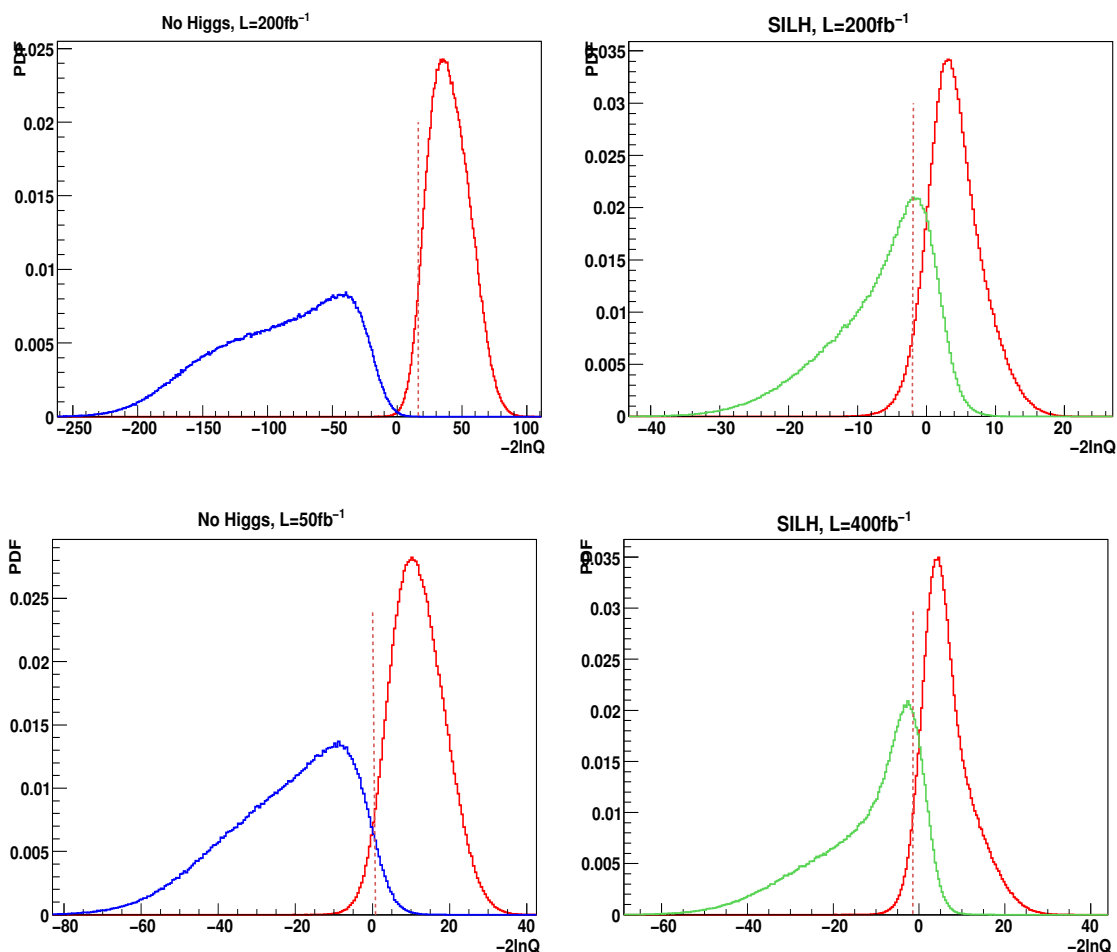


Figure 8. Combination of all the seven channels using $-2 \ln Q$ for the no-Higgs and SILH cases using strongly correlated theoretical errors. In the bottom plots an integrated luminosity of $L = 50 \text{ fb}^{-1}$ is assumed for the no-Higgs scenario and of $L = 400 \text{ fb}^{-1}$ for the SILH case. For the no-Higgs analysis at $L = 50 \text{ fb}^{-1}$ we have used the lowest mass cut for each channel in order to increase the number of events at this luminosity. Hence in this case $M_{\text{cut}} = 200, 300, 300, 300 \text{ GeV}$ for the $2j\ell^\pm\ell^\pm\nu\nu$, $ZZ \rightarrow 2j\ell\nu\ell\nu$, $WW \rightarrow 2j\ell\nu\ell\nu$ and $2j4\ell$ channel respectively. For the remaining channels M_{cut} has been kept at 600 GeV.

an integrated luminosity of 200 fb^{-1} the PSM@95%CL for the SILH case is about 69% which increases to 80% if the luminosity is doubled. The corresponding figures for the PSM@99.7%CL are 42% and 57% respectively. The probability to distinguish at 95%CL the no-Higgs case from the light Higgs picture with a reduced luminosity of $L = 50 \text{ fb}^{-1}$ remains above 95%.

Before stating our conclusions we return for completeness to the possible modification to our results if the $t\bar{t}jj$ turns out not to be measurable, even though as discussed previously we do not regard this prospect as probable. In this case the contribution from $t\bar{t}jj$ production should be considered as part of the signal S and therefore subject to theoretical uncertainties in addition to the statistical ones. For simplicity we have assumed the same range of variation for this process as for all others involved. We refer to this possibility as

Channel	no Higgs			SILH			SM	$t\bar{t}jj$	B
	$\sigma(\text{fb})$	$t\bar{t}jj \subset S$	$t\bar{t}jj = B$	$\sigma(\text{fb})$	$t\bar{t}jj \subset S$	$t\bar{t}jj = B$	$\sigma(\text{fb})$	$\sigma(\text{fb})$	$\sigma(\text{fb})$
$2j\ell\nu\nu$.0968	77.9%	85.0%	.0533	22.0%	26.6%	.0332	.0215	–
$4j\ell\nu$	2.36	90.1%	96.2%	1.41	30.9%	35.2%	1.05	.463	9.78

Table 18. PBSM@95%CL for 200 fb^{-1} with $t\bar{t}jj$ as as part of the signal ($t\bar{t}jj \subset S$) and $t\bar{t}jj$ as a background ($t\bar{t}jj = B$). We also give the total cross section for the $2jW^+W^- \rightarrow 2j\ell^+\ell^-\nu\nu$ and $4j\ell\nu$ channels with the full set of cuts and $M_{\text{cut}} = 600 \text{ GeV}$.

scenario	non-reconstructable		reconstructable		all channels	
	$t\bar{t}jj = B$	$t\bar{t}jj \subset S$	$t\bar{t}jj = B$	$t\bar{t}jj \subset S$	$t\bar{t}jj = B$	$t\bar{t}jj \subset S$
SILH	64.93%	63.25%	44.07%	40.46%	68.38%	67.47%
NOH	99.98%	99.97%	99.34%	98.27%	>99.99%	>99.99%

Table 19. PBSM@95%CL combining the non-reconstructable channels, the reconstructable ones and finally all channels with $t\bar{t}jj$ as as part of the signal ($t\bar{t}jj \subset S$) and $t\bar{t}jj$ as a background ($t\bar{t}jj = B$). For the $2jW^+W^- \rightarrow 2j\ell^+\ell^-\nu\nu$ process $M_{\text{cut}} = 500 \text{ GeV}$ has been used.

$t\bar{t}jj$ as signal ($t\bar{t}jj \subset S$) while the framework in which $t\bar{t}jj$ production is considered as a measured and extrapolated background is described as $t\bar{t}jj$ as background ($t\bar{t}jj = B$). In table 18 we present the cross sections and the PBSM@95%CL for the two channels which are affected by the $t\bar{t}jj$ background, namely $2jW^+W^-$ and $4jW$. In table 19 we compare the two results for the different combinations of channels. While there is a noticeable decrease of the PBSM for the individual reactions in table 18, the overall combinations are hardly affected.

These results suggest that the no-Higgs scenario can be disproved with a rather modest luminosity. This implies that any model which predicts vector vector scattering rates larger than those in the no-Higgs case can be disproved or verified with the same luminosity.

Our conclusions for the SILH framework are less optimistic. Clearly a substantial increase in luminosity and a combination of the results obtained by ATLAS and CMS are highly desirable. Furthermore, it should be recalled that the particular instance of SILH model we have discussed is a rather extreme case and that for smaller values of $c_H\xi$ results even closer to the SM ones are expected.

8 Conclusions

We have examined in detail at parton level the processes $2\ell 2\nu 2j$ and $4\ell 2j$, $\ell = \mu, e$ including all irreducible backgrounds contributing to these six parton final states. We have considered three scenarios: a light Higgs SM framework with $M_H = 200 \text{ GeV}$, one instance of the SILH models and an infinite mass Higgs scenario in order to determine whether the two BSM models can be distinguished from the SM at the LHC using boson-boson scattering. Because of the absence of large QCD backgrounds, the non-reconstructable channels presented here, provide a better discrimination between the SM and the BSM scenarios, despite their low rates, than those in which the invariant mass of the boson pair can be measured.

The results for the channels discussed above have been combined with those obtained in ref. [54] for $4j\ell\nu$ production and those obtained in ref. [55] for $4j\ell^+\ell^-$ and $2j3\ell\nu$. We have estimated the total probability, in the two BSM scenarios, of finding a result outside the 95% probability range in the Standard Model. This probability turns out to be essentially 100% for the Higgsless case and 69% for the SILH model. These probabilities correspond to an integrated luminosity of $L = 200 \text{ fb}^{-1}$ and to the sum of all electron and muon channels.

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