

The dark side of flipped trinification

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ABSTRACT: We propose a model which unifies the Left-Right symmetry with the $SU(3)_L$ gauge group, called flipped trinification, and based on the $SU(3)_C \otimes SU(3)_L \otimes SU(3)_R \otimes U(1)_X$ gauge group. The model inherits the interesting features of both symmetries while elegantly explaining the origin of the matter parity, $W_P = (-1)^{3(B-L)+2s}$, and dark matter stability. We develop the details of the spontaneous symmetry breaking mechanism in the model, determining the relevant mass eigenstates, and showing how neutrino masses are easily generated via the seesaw mechanism. Moreover, we introduce viable dark matter candidates, encompassing a fermion, scalar and possibly vector fields, leading to a potentially novel dark matter phenomenology.

KEYWORDS: Cosmology of Theories beyond the SM, Discrete Symmetries, Gauge Symmetry

ARXIV EPRINT: [1710.06951](https://arxiv.org/abs/1710.06951)

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1 Introduction

The mystery of Dark Matter (DM) is one of the biggest open questions in science [1–4]. Despite the fact that its existence has been ascertained at several distance scales of our universe, its nature has not yet been resolved and the Standard Model (SM) fails to account for it. The need to extend the SM goes beyond the DM problem, due to the existence of

important open questions connected to neutrino masses, the cosmological baryon-number asymmetry, inflation and reheating. Besides, from the theoretical side, the SM fails to explain the existence of (just) three fermion families as well as the origin of the observed parity violation of the weak interaction. The purpose of this paper is to study how an extension of the SM addressing these two issues, while hosting a viable DM candidate.

The minimal left-right symmetric model based on the $SU(3)_C \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$ gauge group, completed by a Z_2 symmetry that interchanges the left and right, is one of the most attractive extensions of the SM [5–10]. It gives a manifest understanding for the origin of parity violation in the weak interaction, neutrino mass generation as well as a framework for dark matter [11–15].

By the same token, models based on the $SU(3)_C \otimes SU(3)_L \otimes U(1)_N$ gauge group, for short 3-3-1, offer plausible explanations for the number of generations and a hospitable scenario for neutrino mass generation as well as implementing a viable dark sector [16–20, 20–24]. Hence it is theoretically well motivated to build a model where both groups are described in a unified way.

Indeed, models have been proposed in the context of the $SU(3)_C \otimes SU(3)_L \otimes SU(3)_R$ gauge group [25–42]. Since they are based on a three copies of the $SU(3)$ non-Abelian group, it has been coined the term trinification. The motivation for trinification lies in the unified description of both strong and electroweak interactions using the same non-Abelian gauge group, while incorporating nice features of both left-right and 3-3-1 gauge groups. Fully realistic models unifying left-right and 331 electroweak symmetries have, in fact, been recently proposed using a flipped trinification scenario with an extra $U(1)_X$ factor [40, 41].

In this paper we focus on an interesting question, namely, can we build a model preserving the nice features of the left-right and 3-3-1 symmetries while naturally explaining the origin of the matter parity and dark matter? We argue that, using the gauge principle to extend the trinification framework, there is a compelling and minimal solution incorporating dark matter and realistic fermion masses. Such a flipped trinification setup is better motivated because inherits the good features of both left-right and $SU(3)_L \otimes U(1)_N$ symmetries and, in addition, elegantly addresses the origin of matter parity and dark matter stability in the context of 3-3-1 type models [43–55], while generating fermion masses with a minimal scalar sector. Indeed, it suffices to have one triplet (χ_L), one bitriplet (ϕ), one sextet (σ_R) to generate realistic fermion masses, as opposed to earlier versions where another bitriplet was necessary [39, 40]. In order to ensure left-right symmetry further copies of the scalar multiplets are required. Thus, a minimal version of trinification with exact left-right symmetry requires one bitriplet (ϕ), two sextets (σ_L and σ_R) and two triplets (χ_L and χ_R).

The rest of this paper is organized as follows: in section 2, we introduce the model with the gauge symmetry and particle content, focusing on the particles with unusual $B - L$ charges. We find the viable patterns of symmetry breaking and show that W -parity is a residual gauge symmetry which protects the dark matter stability. In section 3, we identify the physical fields and the corresponding masses. In section 4, we discuss the dark matter phenomenology. Finally, we summarize the results and conclude this work in section 5.

2 A flipped trinification setup

2.1 Gauge symmetry

Trinification is a theory of unified interactions based on the gauge symmetry $SU(3)_C \otimes SU(3)_L \otimes SU(3)_R$, the maximal subgroup of E_6 [25–27]. When multiplied by an Abelian group factor, $U(1)_X$, we have the flipped trinification [40, 41],

$$SU(3)_C \otimes SU(3)_L \otimes SU(3)_R \otimes U(1)_X. \quad (2.1)$$

This symmetry can be obtained by left-right symmetrizing the 3-3-1 model in order to account for weak parity violation and close both $B - L$ and 3-3-1 algebras (cf. [56]). An alternative motivation is that it can be achieved from the minimal left-right symmetric model by enlarging the left and right weak isospin groups in order to resolve the number of fermion generations and accommodate dark matter (cf. [39]).

The electric charge operator is generally given by

$$Q = T_{3L} + T_{3R} + \beta(T_{8L} + T_{8R}) + X, \quad (2.2)$$

which reflects the left-right symmetry, where $T_{nL,R}$ ($n = 1, 2, 3, \dots, 8$) and X are the $SU(3)_{L,R}$ and $U(1)_X$ generators, respectively. Note that β is an arbitrary coefficient whose values dictate the electric charge of the new fermions present in the model.

As usual, the baryon minus lepton number is embedded as $Q = T_{3L} + T_{3R} + \frac{1}{2}(B - L)$, which implies that

$$B - L = 2[\beta(T_{8L} + T_{8R}) + X] \quad (2.3)$$

is a residual gauge symmetry of $SU(3)_L \otimes SU(3)_R \otimes U(1)_X$. Let us note that $B - L$ and $SU(3)_L$ neither commute nor close algebraically. Therefore, the present framework, along the 3-3-1-1 gauge theory, constitute a class of models with a fully consistent formulation of gauged $B - L$ symmetry in 3-3-1 extensions of the Standard Model [45, 51, 55–57].

2.2 Fermion sector

The fermion content in this model results simply from the left-right symmetrization the left-handed fermion sector of the 3-3-1 model, so as to produce the right-handed fermion sector. The fermion sector is given as

$$\psi_{aL} = \begin{pmatrix} \nu_{aL} \\ e_{aL} \\ N_{aL}^q \end{pmatrix} \sim \left(1, 3, 1, \frac{q-1}{3}\right), \quad \psi_{aR} = \begin{pmatrix} \nu_{aR} \\ e_{aR} \\ N_{aR}^q \end{pmatrix} \sim \left(1, 1, 3, \frac{q-1}{3}\right), \quad (2.4)$$

$$Q_{\alpha L} = \begin{pmatrix} d_{\alpha L} \\ -u_{\alpha L} \\ J_{\alpha L}^{-q-\frac{1}{3}} \end{pmatrix} \sim \left(3, 3^*, 1, -\frac{q}{3}\right), \quad Q_{\alpha R} = \begin{pmatrix} d_{\alpha R} \\ -u_{\alpha R} \\ J_{\alpha R}^{-q-\frac{1}{3}} \end{pmatrix} \sim \left(3, 1, 3^*, -\frac{q}{3}\right), \quad (2.5)$$

$$Q_{3L} = \begin{pmatrix} u_{3L} \\ d_{3L} \\ J_{3L}^{q+\frac{2}{3}} \end{pmatrix} \sim \left(3, 3, 1, \frac{q+1}{3}\right), \quad Q_{3R} = \begin{pmatrix} u_{3R} \\ d_{3R} \\ J_{3R}^{q+\frac{2}{3}} \end{pmatrix} \sim \left(3, 1, 3, \frac{q+1}{3}\right), \quad (2.6)$$

where $a = 1, 2, 3$ and $\alpha = 1, 2$ are generation indices, and $q \equiv -(1 + \sqrt{3}\beta)/2$.

The new fields N_a and J_a above are new leptons and quarks predicted by the model. It can be easily shown that all triangle anomalies vanish, since both $SU(3)_L$ or $SU(3)_R$ groups match the number of fermion generations to be that of fundamental colors, in agreement with the current observations [58]. This choice of fermion representations is the minimal for a flipped trinification [25–27].

2.3 Scalar sector

To break the gauge symmetry and generate the masses properly, we need introduce the scalar multiplets as follows,

$$\phi = \begin{pmatrix} \phi_{11}^0 & \phi_{12}^+ & \phi_{13}^{-q} \\ \phi_{21}^- & \phi_{22}^0 & \phi_{23}^{-1-q} \\ \phi_{31}^q & \phi_{32}^{1+q} & \phi_{33}^0 \end{pmatrix} \sim (1, 3, 3^*, 0), \quad (2.7)$$

$$\chi_L = \begin{pmatrix} \chi_1^{-q} \\ \chi_2^{-q-1} \\ \chi_3^0 \end{pmatrix}_L \sim \left(1, 3, 1, -\frac{2q+1}{3}\right), \quad (2.8)$$

$$\chi_R = \begin{pmatrix} \chi_1^{-q} \\ \chi_2^{-q-1} \\ \chi_3^0 \end{pmatrix}_R \sim \left(1, 1, 3, -\frac{2q+1}{3}\right), \quad (2.9)$$

$$\sigma_L = \begin{pmatrix} \sigma_{11}^0 & \frac{\sigma_{12}^-}{\sqrt{2}} & \frac{\sigma_{13}^q}{\sqrt{2}} \\ \frac{\sigma_{12}^-}{\sqrt{2}} & \sigma_{22}^{--} & \frac{\sigma_{23}^{q-1}}{\sqrt{2}} \\ \frac{\sigma_{13}^q}{\sqrt{2}} & \frac{\sigma_{23}^{q-1}}{\sqrt{2}} & \sigma_{33}^{2q} \end{pmatrix}_L \sim \left(1, 6, 1, \frac{2(q-1)}{3}\right), \quad (2.10)$$

$$\sigma_R = \begin{pmatrix} \sigma_{11}^0 & \frac{\sigma_{12}^-}{\sqrt{2}} & \frac{\sigma_{13}^q}{\sqrt{2}} \\ \frac{\sigma_{12}^-}{\sqrt{2}} & \sigma_{22}^{--} & \frac{\sigma_{23}^{q-1}}{\sqrt{2}} \\ \frac{\sigma_{13}^q}{\sqrt{2}} & \frac{\sigma_{23}^{q-1}}{\sqrt{2}} & \sigma_{33}^{2q} \end{pmatrix}_R \sim \left(1, 1, 6, \frac{2(q-1)}{3}\right), \quad (2.11)$$

with the corresponding VEVs,

$$\langle \phi \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} u & 0 & 0 \\ 0 & u' & 0 \\ 0 & 0 & w \end{pmatrix}, \quad \langle \chi_R \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ w' \end{pmatrix}, \quad \langle \sigma_R \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} \Lambda & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}. \quad (2.12)$$

Note that the scalars transform as $\phi \rightarrow U_L \phi U_R^\dagger$, $\chi_R \rightarrow U_R \chi_R$, and $\sigma_R \rightarrow U_R \sigma_R U_R^T$ under $SU(3)_L \otimes SU(3)_R$. We emphasize that these three scalar multiplets are sufficient to generate all fermion masses. The scalar multiplets χ_L and σ_L have been added to ensure the left-right symmetry, but they do not play any role in our phenomenology because the VEV of these fields are negligible hence contributing neither to gauge boson masses nor to the spontaneous symmetry breaking pattern.¹ Therefore, for simplicity hereafter we ignore the VEVs of σ_L, χ_L , keeping only the VEVs of σ_R, χ_R , denoted omitting the subscript “R”. We now discuss what types of spontaneous symmetry breaking patterns one may have in our model.

¹They only contribute to the tiny neutrino masses.

2.4 Spontaneous symmetry breaking

We now address the issue of which types of symmetry breaking patterns can be achieved within our model.

2.4.1 Case 1: $w, w' \gg \Lambda \gg u, u'$

In this scenario, we assume $w, w' \gg \Lambda \gg u, u'$, leading to the following breaking pattern,

$$\begin{aligned}
 & \text{SU}(3)_C \otimes \text{SU}(3)_L \otimes \text{SU}(3)_R \otimes \text{U}(1)_X \\
 & \quad \downarrow w, w' \\
 & \text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{SU}(2)_R \otimes \text{U}(1)_{B-L} \\
 & \quad \downarrow \Lambda \\
 & \text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{U}(1)_Y \otimes W_P \\
 & \quad \downarrow u, u' \\
 & \text{SU}(3)_C \otimes \text{U}(1)_Q \otimes W_P.
 \end{aligned}$$

Notice that spontaneous symmetry breaking leaves the residual discrete gauge symmetry, W_P , conserved along with the electric and color charges. Let us now identify what symmetry is that. The VEV of σ_{11}^0 , Λ , breaks $B - L$ since $[B - L]\langle\sigma_{11}^0\rangle = \sqrt{2}\Lambda \neq 0$, where σ_{11}^0 has $B - L = 2$. The $\text{U}(1)_{B-L}$ transformation that preserves the vacuum is $\langle\sigma_{11}^0\rangle \rightarrow e^{i\omega(B-L)}\langle\sigma_{11}^0\rangle = e^{i2\omega}\langle\sigma_{11}^0\rangle = \langle\sigma_{11}^0\rangle$, with ω as a transformation parameter.

Thus, we obtain $e^{i2\omega} = 1$, or $\omega = m\pi$ for $m = 0, \pm 1, \pm 2, \dots$, and the surviving transformation is $M_P = e^{im\pi(B-L)} = (-1)^{m(B-L)}$. Since the spin parity $(-1)^{2s}$ is always conserved due to Lorentz symmetry, the residual discrete symmetry preserved after spontaneous symmetry breaking is $W_P = M_P \times (-1)^{2s}$, which is actually a whole class of symmetries parameterized by m . Among such conserving transformations, we focus on the one with $m = 3$,

$$W_P = (-1)^{3(B-L)+2s}, \quad (2.13)$$

which we call the matter parity.² We stress that in our model, it emerges as a residual gauge symmetry,

$$W_P = (-1)^{6[\beta(T_{8L}+T_{8R})+X]+2s}, \quad (2.14)$$

and it acts nontrivially on the fields with unusual (wrong) $B - L$ numbers. For details, see table 1. W -parity, W_P , is thus named following the ‘‘wrong’’ item as in previous studies.

2.4.2 Case 2: $\Lambda \gg w, w' \gg u, u'$

For $\Lambda \gg w, w'$, the gauge symmetry is broken following a different path,

$$\begin{aligned}
 & \text{SU}(3)_C \otimes \text{SU}(3)_L \otimes \text{SU}(3)_R \otimes \text{U}(1)_X \\
 & \quad \downarrow \Lambda \\
 & \text{SU}(3)_C \otimes \text{SU}(3)_L \otimes \text{SU}(2)_{R'} \otimes \text{U}(1)_{X'} \otimes W'_P \\
 & \quad \downarrow w, w' \\
 & \text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{U}(1)_Y \otimes W_P \\
 & \quad \downarrow u, u' \\
 & \text{SU}(3)_C \otimes \text{U}(1)_Q \otimes W_P.
 \end{aligned}$$

²We note that the matter parity present in our model coincides with R -parity in supersymmetry.

The $SU(2)_{R'}$ symmetry is generated by $\{T_{6R}, T_{7R}, \frac{1}{2}(\sqrt{3}T_{8R} - T_{3R})\}$, meaning that the left-right symmetry is initially broken in this case. The $U(1)_{X'}$ charge is $X' = \frac{\sqrt{3+\beta}}{4}(T_{8R} + \sqrt{3}T_{3R}) + X$, with $\beta = -(1 + 2q)/\sqrt{3}$. The discrete symmetry W'_P takes a form, $W'_P = (-1)^{m(\beta T_{8R} + X)}$, which is a residual symmetry of a broken $U(1)$ group, with $U(\omega) = e^{i\omega 2(\beta T_{8R} + X)}$ transformation. The second stage of the symmetry breaking is driven by ϕ_{33}^0, χ_3^0 fields. The VEV of χ_3^0 breaks the symmetry $SU(2)_{R'} \otimes U(1)_{X'}$, while the VEV of ϕ_{33}^0 breaks not only that symmetry but also W'_P and a $U(1)$ group, with $U(\omega') = e^{i\omega' 2\beta T_{8L}}$ transformation, as a $SU(3)_L$ subgroup. However, the VEV of ϕ_{33}^0 leaves W_P unbroken. Indeed, ϕ_{33}^0 transforms under $U(1)_{2\beta T_{8L}} \otimes W'_P$ as,

$$\phi_{33}^0 \rightarrow \phi_{33}^{0'} = e^{i\frac{2}{3}(\omega' - m\pi)(1+2q)} \phi_{33}^0, \tag{2.15}$$

which is invariant if $\omega' = \pi(m + \frac{3k}{1+2q})$ with $k = 0, \pm 1, \pm 2 \dots$. Choosing $k = 0$, the residual symmetry coincides with W_P after spin parity is included and taking $m = 3$. Lastly, note that the hypercharge is

$$Y = \beta T_{8L} + \frac{\sqrt{3}\beta - 1}{4}(\sqrt{3}T_{8R} - T_{3R}) + X', \tag{2.16}$$

and the electric charge is $Q = T_{3L} + Y$, all of which have the usual form.

2.4.3 Case 3: $w, w' \sim \Lambda$

Another possible breaking pattern takes place when assuming that the symmetry breaking of the left-right and $SU(3)_L$ symmetry occurs at the same scale, i.e. $w, w' \sim \Lambda$. Therefore, we have only one new physics scale and the gauge symmetry is directly broken down to that of the SM as,

$$\begin{aligned} &SU(3)_C \otimes SU(3)_L \otimes SU(3)_R \otimes U(1)_X \\ &\quad \downarrow \Lambda, w, w' \\ &SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes W_P \\ &\quad \downarrow u, u' \\ &SU(3)_C \otimes U(1)_Q \otimes W_P. \end{aligned}$$

Here, W_P is the residual discrete gauge symmetry preserved by all VEVs and has the form obtained above.

In summary, regardless of symmetry breaking scheme adopted, they all lead to the residual conserved W -parity, $W_P = (-1)^{3(B-L)+2s}$, with $B - L = 2[\beta(T_{8L} + T_{8R}) + X]$. In this way, the matter parity is a direct consequence of the gauge group and as we shall see, it naturally leads to the existence of stable dark matter particles.

The transformation properties of the particles of the model under $B - L$ number and W -parity are collected in table 1. Notice that the $B - L$ charge for the new particles depends on their electric charge, i.e. on the basic electric charge parameter q , with W -parity values $P^\pm \equiv (-1)^{\pm(6q+1)}$. When the new particles have ordinary electric charges $q = m/3$ for m integer, they are W -odd, $P^\pm = -1$, analogously to superparticles in supersymmetry. Generally, assuming that $q \neq (2m - 1)/6$, W -parity is nontrivial, with $P^\pm \neq 1$ and $(P^+)^\dagger = P^-$. Such new particles, denoted as W -particles in what follows,

Particle	ν_a	e_a	N_a	u_a	d_a	J_α	J_3	ϕ_{11}^0	ϕ_{12}^+	ϕ_{13}^{-q}	ϕ_{21}^-
$B-L$	-1	-1	$2q$	$\frac{1}{3}$	$\frac{1}{3}$	$-\frac{2(1+3q)}{3}$	$\frac{2(2+3q)}{3}$	0	0	$-(1+2q)$	0
W_P	1	1	P^+	1	1	P^-	P^+	1	1	P^-	1
Particle	ϕ_{31}^q	ϕ_{32}^{1+q}	ϕ_{33}^0	ϕ_{22}^0	ϕ_{23}^{-1-q}	$\chi_1^{(-q)}$	$\chi_2^{-(q+1)}$	χ_3^0	σ_{11}^0	σ_{12}^-	σ_{13}^q
$B-L$	$(1+2q)$	$(1+2q)$	0	0	$-(1+2q)$	$-(1+2q)$	$-(1+2q)$	0	-2	-2	$-1+2q$
W_P	P^+	P^+	1	1	P^-	P^-	P^-	1	1	1	P^+
Particle	σ_{22}^{--}	σ_{23}^{q-1}	σ_{33}^{2q}	A	$Z_{L,R}$	$Z'_{L,R}$	$W_{L,R}^\pm$	$X_{L,R}^q$	$X_{L,R}^{-q}$	$Y_{L,R}^{q+1}$	$Y_{L,R}^{-(q+1)}$
$B-L$	-2	$-1+2q$	$4q$	0	0	0	0	$1+2q$	$-(1+2q)$	$1+2q$	$-(1+2q)$
W_P	1	P^+	P^+	1	1	1	1	P^+	P^-	P^+	P^-

Table 1. The $B-L$ number and W -parity of the model particles, with $P^\pm \equiv (-1)^{\pm(6q+1)}$.

have different $B-L$ numbers than those of the standard model. Recall that W -parity is only trivial for $q = (2m-1)/6 = \pm 1/6, \pm 1/2, \pm 5/6, \pm 7/6, \dots$, values not studied in this work as they require fractional charges for the new leptons.

Since the W -charged and SM particles are unified within the gauge multiplets, W -parity separates them into two classes,

- Normal particles with $W_P = 1$: consist on all SM particles plus extra new fields. Explicitly, the particles belonging to this class are the fermions, ν_a, e_a, u_a, d_a , the scalars, $\phi_{11}^0, \phi_{12}^\pm, \phi_{21}^\pm, \phi_{22}^0, \phi_{33}^0, \chi_3^0, \sigma_{11}^0, \sigma_{12}^\pm, \sigma_{22}^\pm, \sigma_{33}^\pm$, the gauge bosons, $A, Z_{L,R}, Z'_{L,R}$, and the gluon.
- W -particles with $W_P = P^+$ or P^- : includes the new leptons and quarks, N_a, J_a , the new scalars, $\phi_{13}^\pm, \phi_{23}^{\pm(1+q)}, \phi_{31}^\pm, \phi_{32}^{\pm(1+q)}, \chi_1^\pm, \chi_2^{\pm(q+1)}, \sigma_{13}^\pm, \sigma_{23}^{\pm(q-1)}$, and the new non-Hermitian gauge bosons, $X_{L,R}^\pm, Y_{L,R}^{\pm(q+1)}$.

It can be easily shown that W -particles always appear in pairs in interactions, similarly to superparticles in supersymmetry. Indeed, consider an interaction that includes x P^+ -fields and y P^- -fields. The W -parity conservation implies $(-1)^{(6q+1)(x-y)} = 1$ for arbitrary q which is satisfied only if $x = y$. Hence, the fields P^+ and P^- are always coupled in pairs. The lightest W -particle (often called LWP) cannot decay due to the W -parity conservation. Thus, if the lightest W -particle carries no electrical and color charges, it can be identified as a dark matter candidate.

From table 1, the colorless W -particles have electrical charges $\pm q, \pm(1+q), \pm(q-1)$, and therefore three dark matter models can be built, corresponding to $q = 0, \pm 1$.³ The model $q = 0$ includes three dark matter candidates, namely, a lepton as the lightest mixture of N_a^0 , a scalar as the combination of $\phi_{13}^0, \phi_{31}^0, \chi_1^0, \sigma_{13}^0$, and a gauge boson from the mixing of $X_{L,R}^0$. The model $q = -1$ contains two dark matter candidates: a scalar composed of $\phi_{23}^0, \phi_{32}^0, \chi_2^0$ and a gauge boson from the lightest mixture of $Y_{L,R}^0$. Lastly, the model $q = 1$ has only one dark matter candidate: the scalar field σ_{23}^0 .

³The $q = 1$ case might be ruled out in the manifest left-right model [38].

Before closing this section, it is important to notice that the fundamental field σ_{33}^{2q} , carrying W -parity $(P^+)^2$, leads to self-interactions among three W -fields, if it transforms nontrivially under this parity. However, its presence does not alter the results and conclusions given below. See [39] for a proof.

3 Identifying physical states and masses

The Lagrangian of the model takes the form, $\mathcal{L} = \mathcal{L}_{\text{gauge}} + \mathcal{L}_{\text{Yukawa}} - V$, where the first term contains all kinetic terms plus gauge interactions. The second term includes Yukawa interactions, obtained by

$$\begin{aligned} \mathcal{L}_{\text{Yukawa}} = & x_{ab} \bar{\psi}_{aR}^c \sigma_R^\dagger \psi_{bR} + x'_{ab} \bar{\psi}_{aL}^c \sigma_L^\dagger \psi_{bL} + y_{ab} \bar{\psi}_{aL} \phi \psi_{bR} + z_{33} \bar{Q}_{3L} \phi Q_{3R} + z_{\alpha\beta} \bar{Q}_{\alpha L} \phi^* Q_{\beta R} \\ & + \frac{t_{3\alpha}}{M} \bar{Q}_{3L} \phi \chi^* Q_{\alpha R} + \frac{t_{\alpha 3}}{M} \bar{Q}_{\alpha L} \phi^* \chi Q_{3R} + H.c., \end{aligned} \quad (3.1)$$

where M is a new physics scale that defines the effective interactions required to generate a consistent CKM matrix. The scalar potential is $V = V_\phi + V_\chi + V_\sigma + V_{\text{mix}}$, where

$$V_\phi = \mu_\phi^2 \text{Tr}(\phi^\dagger \phi) + \lambda_1 [\text{Tr}(\phi^\dagger \phi)]^2 + \lambda_2 \text{Tr}[(\phi^\dagger \phi)^2], \quad (3.2)$$

$$V_\chi = \mu_\chi^2 \chi^\dagger \chi + \lambda (\chi^\dagger \chi)^2, \quad (3.3)$$

$$V_\sigma = \mu_\sigma^2 \text{Tr}(\sigma^\dagger \sigma) + \kappa_1 [\text{Tr}(\sigma^\dagger \sigma)]^2 + \kappa_2 \text{Tr}[(\sigma^\dagger \sigma)^2], \quad (3.4)$$

$$\begin{aligned} V_{\text{mix}} = & \zeta_1 \chi^\dagger \chi \text{Tr}(\phi^\dagger \phi) + \zeta_2 \text{Tr}(\phi^\dagger \phi) \text{Tr}(\sigma^\dagger \sigma) + \zeta_3 \text{Tr}(\phi^\dagger \phi \sigma \sigma^\dagger) + \zeta_4 \chi^\dagger \chi \text{Tr}(\sigma^\dagger \sigma) \\ & + \zeta_5 \chi^\dagger \sigma \sigma^\dagger \chi + \zeta_6 \chi^\dagger \phi^\dagger \phi \chi + (f \epsilon^{ijk} \epsilon_{\alpha\beta\gamma} \phi_i^\alpha \phi_j^\beta \phi_k^\gamma + H.c.). \end{aligned} \quad (3.5)$$

We see that ϕ has trilinear couplings. An $SU(2)_L$ doublet contained in ϕ can be made heavy by taking f at the new physics scale. The remaining Higgs doublet in ϕ is light and lies in the weak scale, as shown below. If another bi-fundamental field ρ is introduced in this minimal framework, coupling the third quark generation to the first two, there are no such soft-terms for arbitrary values of the β parameter, since its X -charge is nonzero. Thus, both the Higgs doublets contained in ρ would be light as their VEVs are in the weak scale. In order to avoid light scalars, the triplet χ is included in this work instead of ρ in order to generate viable quark masses and mixings.

3.1 Fermion sector

After spontaneous symmetry breaking, the fermions receive their masses via the Yukawa Lagrangian (3.1). For the up-type quarks and down-type quarks, the corresponding mass matrices are given by

$$M_u = -\frac{1}{\sqrt{2}} \begin{pmatrix} z_{11} u' & z_{12} u' & -\frac{t_{13} u' w'}{\sqrt{2M}} \\ z_{21} u' & z_{22} u' & -\frac{t_{23} u' w'}{\sqrt{2M}} \\ \frac{t_{31} u w'}{\sqrt{2M}} & \frac{t_{32} u w'}{\sqrt{2M}} & z_{33} u \end{pmatrix}, \quad M_d = -\frac{1}{\sqrt{2}} \begin{pmatrix} z_{11} u & z_{12} u & -\frac{t_{13} u w'}{\sqrt{2M}} \\ z_{21} u & z_{22} u & -\frac{t_{23} u w'}{\sqrt{2M}} \\ \frac{t_{31} u' w'}{\sqrt{2M}} & \frac{t_{32} u' w'}{\sqrt{2M}} & z_{33} u' \end{pmatrix}. \quad (3.6)$$

The ordinary quarks obtain consistent masses at the weak scale, u, u' . The new physics or cut-off scale can be taken as at the largest breaking scale, $M \sim w'$. The scale M

characterizing the non-renormalizable interaction is responsible for generating V_{ub} , V_{cb} , as well as quark CP violation, as required.

The exotic quark, J_3 , is a physical field by itself, with mass, $m_{J_3} = -\frac{z_{33}w}{\sqrt{2}}$, which is heavy, lying at the new physics regime. The two remaining exotic quarks, J_α ($\alpha = 1, 2$), mix via a mass matrix,

$$M_{J_\alpha} = -\frac{1}{\sqrt{2}} \begin{pmatrix} z_{11}w & z_{12}w \\ z_{21}w & z_{22}w \end{pmatrix}, \quad (3.7)$$

and are both heavy, at the new physics regime too.

The mass matrix elements for the charged leptons,

$$[M_e]_{ab} = -\frac{1}{\sqrt{2}} y_{ab} u', \quad (3.8)$$

belong to the weak regime as usual. In contrast, the new leptons, N_a , have large masses dictated by the mass matrix

$$[M_N]_{ab} = -\frac{1}{\sqrt{2}} y_{ab} w. \quad (3.9)$$

Neutrinos have both Dirac and Majorana masses. The mass matrix in the $(\nu_L \nu_R^c)$ basis can be written as

$$M_\nu = \begin{pmatrix} M_L & M_D \\ M_D^T & M_R \end{pmatrix}, \quad (3.10)$$

where M_L, M_D, M_R are 3×3 mass matrices, given by

$$[M_D]_{ab} = -\frac{1}{\sqrt{2}} y_{ab} u, \quad [M_L]_{ab} = -\sqrt{2} x'_{ab} v_L, \quad [M_R]_{ab} = -\sqrt{2} x_{ab} \Lambda, \quad (3.11)$$

with $\langle \sigma_{L11}^0 \rangle = v_L/\sqrt{2}$. As $v_L \ll u \ll \Lambda$, the mass matrix (3.11) provides a realization of the full seesaw mechanism, producing small masses for the light neutrinos $\sim \nu_L$,

$$m_\nu = M_L - M_D M_R^{-1} M_D^T \sim u^2/\Lambda - v_L, \quad (3.12)$$

and large masses for the mostly right-handed neutrinos $\sim \nu_R$, of order M_R .

3.2 Scalar sector

Since W -parity is conserved, only the neutral fields carrying $W_P = 1$ can develop the VEVs given in (2.12). We expand the fields around their VEVs as

$$\begin{aligned} \sigma &= \begin{pmatrix} \frac{\Lambda+S_1+iA_1}{\sqrt{2}} & \frac{\sigma_{12}^-}{\sqrt{2}} & \frac{\sigma_{13}^q}{\sqrt{2}} \\ \frac{\sigma_{12}^-}{\sqrt{2}} & \sigma_{22}^{--} & \frac{\sigma_{23}^{q-1}}{\sqrt{2}} \\ \frac{\sigma_{13}^q}{\sqrt{2}} & \frac{\sigma_{23}^{q-1}}{\sqrt{2}} & \sigma_{33}^{2q} \end{pmatrix}, \\ \phi &= \begin{pmatrix} \frac{u+S_2+iA_2}{\sqrt{2}} & \phi_{12}^+ & \phi_{13}^{-q} \\ \phi_{21}^- & \frac{u'+S_3+iA_3}{\sqrt{2}} & \phi_{23}^{-(q+1)} \\ \phi_{31}^q & \phi_{32}^{q+1} & \frac{w+S_4+iA_4}{\sqrt{2}} \end{pmatrix}, \\ \chi &= \begin{pmatrix} \chi_1^{-q} \\ \chi_2^{-(q+1)} \\ \frac{w'+S_5+iA_5}{\sqrt{2}} \end{pmatrix}. \end{aligned} \quad (3.13)$$

The scalar potential can be written as $V = V_{\min} + V_{\text{linear}} + V_{\text{mass}} + V_{\text{int}}$, where V_{\min} is independent of the fields, and all interactions are grouped into V_{int} . V_{linear} contains all the terms that depend linearly on the fields, and the gauge invariance requires,

$$\begin{aligned}
2\mu_\sigma^2 + (u'^2 + w^2)\zeta_2 + u'^2(\zeta_2 + \zeta_3) + w'^2\zeta_4 + 2(\kappa_1 + \kappa_2)\Lambda^2 &= 0, \\
2\mu_\phi^2 + 6\sqrt{2}f\frac{u'}{u}w + 2\lambda_1(u^2 + u'^2 + w^2) + (2\lambda_2u^2 + \zeta_1w'^2 + (\zeta_2 + \zeta_3)\Lambda^2) &= 0, \\
2\mu_\phi^2 + 6\sqrt{2}f\frac{u}{u'}w + 2(\lambda_1 + \lambda_2)u'^2 + (2\lambda_1(u'^2 + w^2) + \zeta_1w'^2 + \zeta_2\Lambda^2) &= 0, \\
2\mu_\phi^2 + 6\sqrt{2}f\frac{uu'}{w} + 2\lambda_1(u^2 + u'^2) + 2(\lambda_1 + \lambda_2)w^2 + (\zeta_1 + \zeta_6)w'^2 + \zeta_2\Lambda^2 &= 0, \\
2\mu_\chi^2 + 2\lambda w'^2 + \zeta_1(u^2 + u'^2 + w^2) + \zeta_6w^2 + \zeta_4\Lambda^2 &= 0. \tag{3.14}
\end{aligned}$$

V_{mass} consists of the terms that quadratically depend on the fields, and can be further decomposed as $V_{\text{mass}} = V_{\text{mass}}^A + V_{\text{mass}}^S + V_{\text{mass}}^{\text{singly-charged}} + V_{\text{mass}}^{\text{doubly-charged}} + V_{\text{mass}}^{q\text{-charged}} + V_{\text{mass}}^{(q+1)\text{-charged}} + V_{\text{mass}}^{(q-1)\text{-charged}} + V_{\text{mass}}^{2q\text{-charged}}$, which are listed in appendix A.

The first mass term includes all pseudo-scalars A_1, A_2, A_3, A_4, A_5 . From appendix A, we see that A_1, A_5 are massless and can be identified to the Goldstone bosons of the right-handed neutral gauge bosons, $\mathcal{Z}_R, \mathcal{Z}'_R$, respectively. The remaining fields A_2, A_3, A_4 mix, but their mass matrix produces only one physical pseudo-scalar field with mass

$$\begin{aligned}
\mathcal{A} &= \frac{1}{\sqrt{u^2w^2 + u'^2w^2 + u^2u'^2}} [u'wA_2 + uwA_3 + u'uA_4], \\
m_{\mathcal{A}}^2 &= \frac{[u'^2w^2 + u^2(u'^2 + w^2)][2\lambda_2(u'^2 - w^2) - \zeta_6w'^2]}{2u^2(w^2 - u'^2)}, \tag{3.15}
\end{aligned}$$

which is heavy, at the w, w' scale. The remaining fields are massless and orthogonal to \mathcal{A}

$$\begin{aligned}
G_{\mathcal{Z}_L} &= \sqrt{\frac{u^2(w^2 + u'^2)}{w^2u'^2 + u^2(w^2 + u'^2)}} \left\{ -A_2 + \frac{u'w^2}{u(w^2 + u'^2)}A_3 + \frac{u'^2w}{u(w^2 + u'^2)}A_4 \right\}, \\
G_{\mathcal{Z}'_L} &= \frac{u'}{\sqrt{w^2 + u'^2}}A_3 - \frac{w}{\sqrt{w^2 + u'^2}}A_4, \tag{3.16}
\end{aligned}$$

and can be identified with the Goldstone bosons of the neutral boson \mathcal{Z}_L , analogous to the SM Z boson, and the new neutral gauge boson \mathcal{Z}'_L .

The V_{mass}^S term contains all the mass terms of the scalar fields, S_1, S_2, S_3, S_4, S_5 , as shown in appendix A. The five scalars mix through a 5×5 matrix. In general, it is not easy to find the eigenstates. However, using the fact that $u, v \ll w', w, \Lambda$, one can diagonalize the mass matrix perturbatively. At leading order, this matrix yields one massless scalar field, $H_1 = \frac{1}{\sqrt{u^2 + u'^2}}(uS_2 + u'S_3)$, and a massive scalar field, $H_2 = \frac{1}{\sqrt{u^2 + u'^2}}(u'S_2 - uS_3)$, with $m_{H_2}^2 = -\frac{u^2 + u'^2}{2u^2}(\zeta_6w'^2 + 2\lambda_2w^2)$. The H_1 field obtains a mass at next-to-leading order, $m_{H_1} \simeq O(u, u')$, and is identified with the standard model Higgs boson. The remaining fields, (S_1, S_4, S_5) , are heavy and mixed among themselves via a 3×3 matrix. In the limit,

$\Lambda \gg w, w'$, the corresponding physical fields have masses given by

$$H_3 = S_1, \quad m_{H_3}^2 = \frac{1}{2}(\kappa_1 + \kappa_2)\Lambda^2, \quad (3.17)$$

$$H_4 = c_H S_4 - s_H S_5, \quad (3.18)$$

$$m_{H_4}^2 = \frac{1}{2} \left\{ (\lambda_1 + \lambda_2)w^2 + \lambda w'^2 - \frac{(\zeta_2^2 w^2 + \zeta_4^2 w'^2)}{4(\kappa_1 + \kappa_2)} \right. \\ \left. + \sqrt{\left[(\lambda_1 + \lambda_2)w^2 - \lambda w'^2 + \frac{\zeta_4^2 w'^2 - \zeta_2^2 w^2}{4(\kappa_1 + \kappa_2)} \right]^2 + \frac{1}{4} w^2 w'^2 \left(\frac{\zeta_2 \zeta_4}{\kappa_1 + \kappa_2} - 2(\zeta_1 + \zeta_6) \right)^2} \right\}, \quad (3.19)$$

$$H_5 = s_H S_4 + c_H S_5, \quad (3.19)$$

$$m_{H_5}^2 = \frac{1}{2} \left\{ (\lambda_1 + \lambda_2)w^2 + \lambda w'^2 - \frac{(\zeta_2^2 w^2 + \zeta_4^2 w'^2)}{4(\kappa_1 + \kappa_2)} \right. \\ \left. - \sqrt{\left[(\lambda_1 + \lambda_2)w^2 - \lambda w'^2 + \frac{\zeta_4^2 w'^2 - \zeta_2^2 w^2}{4(\kappa_1 + \kappa_2)} \right]^2 + \frac{1}{4} w^2 w'^2 \left(\frac{\zeta_2 \zeta_4}{\kappa_1 + \kappa_2} - 2(\zeta_1 + \zeta_6) \right)^2} \right\},$$

where the mixing angle θ_H is defined by the relation

$$t_{2\theta_H} = \frac{ww' \left\{ -\frac{\zeta_2 \zeta_4}{\kappa_1 + \kappa_2} + 2(\zeta_1 + \zeta_6) \right\}}{2 \left\{ -(\lambda_1 + \lambda_2)w^2 + \lambda w'^2 + \frac{\zeta_2^2 w^2 - \zeta_4^2 w'^2}{4(\kappa_1 + \kappa_2)} \right\}}. \quad (3.20)$$

On the other hand, if one assumes that instead the hierarchy $w, w' > \Lambda$ holds, the masses and mixing of the heavy states, (H_4, H_5) change accordingly to

$$t_{2\theta_H} = \frac{ww'(\zeta_1 + \zeta_6)}{\lambda w'^2 - (\lambda_1 + \lambda_2)w^2}, \\ m_{H_4}^2 = \frac{1}{2} \left\{ (\lambda_1 + \lambda_2)w^2 + \lambda w'^2 + \sqrt{[(\lambda_1 + \lambda_2)w^2 - \lambda w'^2]^2 + w^2 w'^2 (\zeta_1 + \zeta_6)^2} \right\}, \\ m_{H_5}^2 = \frac{1}{2} \left\{ (\lambda_1 + \lambda_2)w^2 + \lambda w'^2 - \sqrt{[(\lambda_1 + \lambda_2)w^2 - \lambda w'^2]^2 + w^2 w'^2 (\zeta_1 + \zeta_6)^2} \right\}. \quad (3.21)$$

Turning now to the singly-charged Higgs fields, we have three fields plus their conjugates. The mass matrix extracted from (A.3) yields four massless fields, which can be identified to the Goldstone bosons of the $W_{L,R}^\pm$ gauge bosons,

$$G_{W_L}^\pm = \frac{1}{\sqrt{u^2 + u'^2}} \{u' \phi_{12}^\pm - u \phi_{21}^\pm\}, \\ G_{W_R}^\pm = \frac{1}{\sqrt{1 + \frac{u'^2}{u^2} + \frac{2(u^2 + u'^2)^2 \Lambda^2}{u^2(u^2 - u'^2)^2}}} \left\{ \frac{\sqrt{2}(u^2 + u'^2)\Lambda}{u(u^2 - u'^2)} \sigma_{12}^\pm + \phi_{12}^\pm + \frac{u'}{u} \phi_{21}^\pm \right\}, \quad (3.22)$$

and two singly-charged massive Higgs fields with corresponding masses

$$H^\pm = \frac{\sqrt{2}u\Lambda}{\sqrt{(u^2 - u'^2)^2 + 2\Lambda^2(u^2 + u'^2)}} \left\{ \frac{u'^2 - u^2}{\sqrt{2}u\Lambda} \sigma_{12}^\pm + \phi_{12}^\pm + \frac{u'}{u} \phi_{21}^\pm \right\}, \\ m_{H^\pm}^2 = \frac{\{2\lambda_2(u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w'^2\} \{(u^2 - u'^2)^2 + 2(u^2 + u'^2)\Lambda^2\}}{4u^2(u'^2 - w^2)\Lambda^2}. \quad (3.23)$$

There is only one doubly-charged Higgs field, $\sigma_{22}^{\pm\pm}$, and is physical by itself, with mass

$$m_{\sigma_{22}}^2 = \frac{(u^2 - u'^2)^2 [2\lambda_2(u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w'^2] + 2\kappa_2 u^2 (w^2 - u'^2) \Lambda^4}{2u^2 \Lambda^2 (u'^2 - w^2)}. \quad (3.24)$$

For q -charged scalars, $V_{\text{mass}}^{q\text{-charged}}$ contains the fields, $\phi_{13}^{\pm q}, \phi_{31}^{\pm q}, \sigma_{13}^{\pm q}, \chi_1^{\pm q}$, as shown in appendix A. The spectrum in this sector includes four massless Goldstone bosons of the new gauge bosons $X_{L,R}^{\pm q}$,

$$G_{X_L}^{\pm q} = \frac{1}{\sqrt{u^4 + w^4 + u^2(w'^2 + 2\Lambda^2 - 2w^2)}} \left\{ (w^2 - u^2) \phi_{13}^{\pm q} - \sqrt{2} u \Lambda \sigma_{13}^{\pm q} + u w' \chi_1^{\pm q} \right\}, \quad (3.25)$$

$$G_{X_R}^{\pm q} = \frac{1}{\sqrt{(u^4 + w^4 + u^2(w'^2 + 2\Lambda^2 - 2w^2))(u^4 + u^2(w'^2 + 2\Lambda^2 - 2w^2) + w^2(w^2 + w'^2 + 2\Lambda^2))}} \\ \times \left\{ u w (w'^2 + 2\Lambda^2) \phi_{13}^{\pm q} + (-u^4 - w^4 + u^2(2w^2 - 2\Lambda^2 - w'^2)) \phi_{31}^{\pm q} + \sqrt{2} w \Lambda (w^2 - u^2) \sigma_{13}^{\pm q} \right. \\ \left. + (u^2 - w^2) w' \chi_1^{\pm q} \right\}. \quad (3.26)$$

The remaining fields are massive. In the limit, $\Lambda, w, w' \gg u, u'$, their physical states are

$$\mathcal{H}_1^{\pm q} \simeq \frac{c_{\theta_q}}{\sqrt{w'^2 + 2\Lambda^2}} \left\{ w' \sigma_{13}^{\pm q} + \sqrt{2} \Lambda \chi_1^{\pm q} \right\} \\ - \frac{s_{\theta_q}}{\sqrt{(w^2 + 2\Lambda^2)(w^2 + w'^2 + 2\Lambda^2)}} \left\{ (w'^2 + 2\Lambda^2) \phi_{31}^{\pm q} + \sqrt{2} w \Lambda \sigma_{13}^{\pm q} - w w' \chi_1^{\pm q} \right\}, \quad (3.27)$$

$$\mathcal{H}_2^{\pm q} \simeq \frac{s_{\theta_q}}{\sqrt{w'^2 + 2\Lambda^2}} \left\{ w' \sigma_{13}^{\pm q} + \sqrt{2} \Lambda \chi_1^{\pm q} \right\} \\ + \frac{c_{\theta_q}}{\sqrt{(w^2 + 2\Lambda^2)(w^2 + w'^2 + 2\Lambda^2)}} \left\{ (w'^2 + 2\Lambda^2) \phi_{31}^{\pm q} + \sqrt{2} w \Lambda \sigma_{13}^{\pm q} - w w' \chi_1^{\pm q} \right\}, \quad (3.28)$$

with masses

$$m_{\mathcal{H}_1}^2 = \frac{1}{4\Lambda^2} \left\{ w'^2 (\zeta_5 - 2t_u^2 \zeta_6) \Lambda^2 + 2\zeta_5 \Lambda^4 + \zeta_6 w^2 (w'^2 - t_u^2 w'^2 - 2\Lambda^2) - 2\lambda_2 (t_u^2 - 1) w^2 (w^2 + 2\Lambda^2) \right\} \\ + \frac{1}{2\Lambda (w'^2 + 2\Lambda^2)} \sqrt{2w^2 w'^2 (w^2 + w'^2 + 2\Lambda^2) [(t_u^2 - 1)(2\lambda_2 w^2 + \zeta_6 w'^2) - 2\zeta_6 \Lambda^2]^2 + \epsilon_{H^{\pm q}}}, \quad (3.29)$$

$$m_{\mathcal{H}_2}^2 = \frac{1}{4\Lambda^2} \left\{ w'^2 (\zeta_5 - 2t_u^2 \zeta_6) \Lambda^2 + 2\zeta_5 \Lambda^4 + \zeta_6 w^2 (w'^2 - t_u^2 w'^2 - 2\Lambda^2) - 2\lambda_2 (t_u^2 - 1) w^2 (w^2 + 2\Lambda^2) \right\} \\ - \frac{1}{2\Lambda (w'^2 + 2\Lambda^2)} \sqrt{2w^2 w'^2 (w^2 + w'^2 + 2\Lambda^2) [(t_u^2 - 1)(2\lambda_2 w^2 + \zeta_6 w'^2) - 2\zeta_6 \Lambda^2]^2 + \epsilon_{H^{\pm q}}}, \quad (3.30)$$

where

$$t_{\theta_q} = \frac{2\sqrt{2} w w' \Lambda (w'^2 + 2\Lambda^2) \sqrt{w^2 + w'^2 + 2\Lambda^2} \{ 2\lambda_2 (t_u^2 - 1) w^2 + \zeta_6 ((t_u^2 - 1) w'^2 - 2\Lambda^2) \}}{\epsilon_{H^{\pm q}}}, \\ \epsilon_{H^{\pm q}} = (w'^2 + 2\Lambda^2) \left[\Lambda^2 (w'^2 + 2\Lambda^2) (w'^2 (\zeta_5 + 2t_u^2 \zeta_6) + 2\zeta_5 \Lambda^2) \right. \\ \left. + \zeta_6 w^2 (w'^4 (1 - t_u^2) + 2t_u^2 w'^2 \Lambda^2 - 4\Lambda^4) \right. \\ \left. - 2\lambda_2 (t_u^2 - 1) w^2 (w^2 w'^2 - 2(w^2 + w'^2) \Lambda^2 - 4\Lambda^4) \right]. \quad (3.31)$$

$V_{\text{mass}}^{(q+1)\text{-charged}}$ contains the mixing terms of $\phi_{23}^{\pm(q+1)}$, $\phi_{32}^{\pm(q+1)}$, $\chi_2^{\pm(q+1)}$. The mass matrix extracted from (A.5) yields four massless fields, identified with the Goldstone bosons of the new gauge bosons $Y_{L,R}^{\pm(q+1)}$, and defined by

$$\begin{aligned} G_{Y_L}^{\pm(q+1)} &= \frac{1}{\sqrt{u'^2 w^2 w'^4 + (u'^2 - w^2)^4 + (u'^6 - 3u'^2 w^4 + 2w^6)w'^2 + w^4 w'^4}} \times \\ &\quad \left\{ [-(u'^2 - w^2)^2 - w^2 w'^2] \phi_{23}^{\pm(q+1)} + u' w w'^2 \phi_{32}^{\pm(q+1)} + u' w' (u'^2 - w^2) \chi_2^{\pm(q+1)} \right\}, \\ G_{Y_R}^{\pm(q+1)} &= \frac{1}{\sqrt{(u'^2 - w^2)^2 + w^2 w'^2}} \left\{ (w^2 - u'^2) \phi_{32}^{\pm(q+1)} + w w' \chi_2^{\pm(q+1)} \right\}. \end{aligned} \quad (3.32)$$

The other physical fields are massive with corresponding masses,

$$\begin{aligned} \mathcal{H}_Y^{\pm(q+1)} &= \frac{1}{\sqrt{w'^2 (w^2 + u'^2) + (u'^2 - w^2)^2}} \left\{ w' u' \phi_{23}^{\pm(q+1)} + w w' \phi_{32}^{\pm(q+1)} + (u'^2 - w^2) \chi_2^{\pm(q+1)} \right\}, \\ m_{\mathcal{H}_Y}^2 &= \frac{\zeta_6}{2(u'^2 - w^2)} \left\{ u'^4 + u'^2 (w'^2 - 2w^2) + w^2 (w^2 + w'^2) \right\}. \end{aligned} \quad (3.33)$$

For $(q-1)$ and $2q$ -charged scalars, $\sigma_{23}^{\pm(q-1)}$ and $\sigma_{33}^{\pm 2q}$ are already physical fields, with masses

$$\begin{aligned} m_{\sigma_{23}}^2 &= \frac{1}{4} \left\{ \zeta_5 w'^2 - 4\kappa_2 \Lambda^2 + \frac{(u^2 - u'^2)(2u^2 - u'^2 - w^2) [2\lambda_2 (u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w'^2]}{u^2 \Lambda^2 (u'^2 - w^2)} \right\}, \\ m_{\sigma_{33}}^2 &= \frac{1}{2} \left\{ \zeta_5 w'^2 - 2\kappa_2 \Lambda^2 + \frac{(u^2 - u'^2)(u^2 - w^2) [2\lambda_2 (u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w'^2]}{u^2 (u'^2 - w^2) \Lambda^2} \right\}. \end{aligned} \quad (3.34)$$

3.3 Gauge-boson sector

Let us now study the physical gauge boson states and their masses. In the non-Hermitian gauge boson sector, there are three kinds of left-right gauge bosons, $W_{L,R}^{\pm}$, $X_{L,R}^{\pm q}$, $Y_{L,R}^{\pm(q+1)}$. The fields $W_{L,R}^{\pm}$, which are defined as $W_L^{\pm} = \frac{1}{\sqrt{2}}(A_{1L} \mp iA_{2L})$ and $W_R^{\pm} = \frac{1}{\sqrt{2}}(A_{1R} \mp iA_{2R})$, mix through the mass matrix,

$$\frac{g_L^2}{4} \begin{pmatrix} u^2 + u'^2 & -2t_R u u' \\ -2t_R u u' & t_R^2 (u^2 + u'^2 + 2\Lambda^2) \end{pmatrix}. \quad (3.35)$$

Diagonalizing this matrix, the eigenstates and masses are given by

$$\begin{aligned} W_1 &= c_{\xi} W_L - s_{\xi} W_R, & m_{W_1}^2 &\simeq \frac{g_L^2}{4} \left\{ u^2 + u'^2 - \frac{4t_R^2 u^2 u'^2}{(t_R^2 - 1)(u^2 + u'^2) + 2t_R^2 \Lambda^2} \right\}, \\ W_2 &= s_{\xi} W_L + c_{\xi} W_R, & m_{W_2}^2 &\simeq \frac{g_R^2}{4} \left\{ u^2 + u'^2 + 2\Lambda^2 + \frac{4t_R^2 u^2 u'^2}{(t_R^2 - 1)(u^2 + u'^2) + 2t_R^2 \Lambda^2} \right\}, \end{aligned} \quad (3.36)$$

where $\Lambda \gg u, u'$ and $t_2 \xi = \frac{-4t_R u u'}{2t_R^2 \Lambda^2 + (t_R^2 - 1)(u^2 + u'^2)}$ and $t_R = \frac{g_R}{g_L}$. W_1 is identified as the SM W boson, which implies $u^2 + u'^2 \simeq (246 \text{ GeV})^2$. W_2 is a physical heavy state, with mass at the new physics scale.

The mass matrix of the fields $X_L^{\pm q} = \frac{1}{\sqrt{2}}(A_{4L} \mp iA_{5L})$ and $X_R^{\pm q} = \frac{1}{\sqrt{2}}(A_{4R} \mp iA_{5R})$ is

$$\frac{g_L^2}{4} \begin{pmatrix} u^2 + w^2 & -2t_R u w \\ -2t_R u w & t_R^2(u^2 + w'^2 + w^2 + 2\Lambda^2) \end{pmatrix}, \quad (3.37)$$

and yields two physical heavy states with masses

$$X_1^{\pm q} \simeq c_{\xi_1} X_L^{\pm} - s_{\xi_1} X_R^{\pm q}, \quad (3.38)$$

$$m_{X_1}^2 \simeq \frac{g_L^2}{4} \left\{ u^2 + w^2 + \frac{4t_R^2 u^2 w^2}{u^2 + w^2 - t_R^2(u^2 + w'^2 + w^2 + 2\Lambda^2)} \right\}, \quad (3.39)$$

$$X_2^{\pm q} \simeq s_{\xi_1} X_L^{\pm} + c_{\xi_1} X_R^{\pm q}, \quad (3.40)$$

$$m_{X_2}^2 \simeq \frac{g_R^2}{4} \left\{ u^2 + w^2 + w'^2 + 2\Lambda^2 - \frac{4u^2 w^2}{u^2 + w^2 - t_R^2(u^2 + w'^2 + w^2 + 2\Lambda^2)} \right\}, \quad (3.41)$$

with $t_{2\xi_1} = \frac{4t_R u w}{u^2 + w^2 - t_R^2(u^2 + w'^2 + w^2 + 2\Lambda^2)}$.

The fields, $Y_L^{\pm(1+q)} = \frac{1}{\sqrt{2}}(A_{6L} \pm iA_{7L})$ and $Y_R^{\pm(1+q)} = \frac{1}{\sqrt{2}}(A_{6R} \pm iA_{7R})$, have the following mass matrix

$$\frac{g_L^2}{4} \begin{pmatrix} u'^2 + w^2 & -2t_R u' w \\ -2t_R u' w & t_R^2(u'^2 + w'^2 + w^2) \end{pmatrix}, \quad (3.42)$$

which provides physical heavy states with masses

$$Y_1^{\pm(1+q)} = c_{\xi_2} Y_L^{\pm(1+q)} - s_{\xi_2} Y_R^{\pm(1+q)}, \quad (3.43)$$

$$m_{Y_1}^2 \simeq \frac{g_L^2}{4} \left\{ u'^2 + w^2 + \frac{4t_R^2 u'^2 w^2}{u'^2 + w^2 - t_R^2(u'^2 + w'^2 + w^2)} \right\}, \quad (3.44)$$

$$Y_2^{\pm(1+q)} = s_{\xi_2} Y_L^{\pm(1+q)} + c_{\xi_2} Y_R^{\pm(1+q)}, \quad (3.45)$$

$$m_{Y_2}^2 \simeq \frac{g_R^2}{4} \left\{ u'^2 + w'^2 + w^2 - \frac{4u'^2 w^2}{u'^2 + w^2 - t_R^2(u'^2 + w'^2 + w^2)} \right\}, \quad (3.46)$$

where the mixing angle ξ_2 satisfies $t_{2\xi_2} = \frac{4t_R u' w}{u'^2 + w^2 - t_R^2(u'^2 + w'^2 + w^2)}$.

The neutral gauge bosons, $A_{3L}, A_{3R}, A_{8L}, A_{8R}, B$, mix via a 5×5 mass matrix. In order to find its eigenstates, we first work with a new basis

$$\begin{aligned} A &= s_W A_{3L} + c_W \left\{ \frac{t_W}{t_R} A_{3R} + \beta t_W A_{8L} + \beta \frac{t_W}{t_R} A_{8R} + \frac{t_W}{t_X} B \right\}, \\ Z_L &= c_W A_{3L} - s_W \left\{ \frac{t_W}{t_R} A_{3R} + \beta t_W A_{8L} + \beta \frac{t_W}{t_R} A_{8R} + \frac{t_W}{t_X} B \right\}, \\ Z'_L &= \varsigma_1 t_X t_W \beta A_{3R} - \frac{t_W}{\varsigma_1 t_X t_R} A_{8L} + \varsigma_1 t_X t_W \beta^2 A_{8R} + \varsigma_1 t_R t_W \beta B, \\ Z_R &= -\frac{\varsigma_1}{\varsigma} A_{3R} + \varsigma \varsigma_1 t_X^2 \beta A_{8R} + \varsigma \varsigma_1 t_X t_R B, \\ Z'_R &= \varsigma (t_R A_{8R} - t_X \beta B), \end{aligned} \quad (3.47)$$

where $t_X = \frac{g_X}{g_L}$, $\varsigma = \frac{1}{\sqrt{t_R^2 + \beta^2 t_X^2}}$, $\varsigma_1 = \frac{1}{\sqrt{t_R^2 + (1+\beta^2)t_X^2}}$, and $s_W = \frac{t_X t_R}{\sqrt{t_X^2(1+\beta^2) + t_R^2(1+t_X^2(1+\beta^2))}}$.

The gauge boson A is massless and decouples, therefore it is identified with the photon field. The remaining fields, Z_L, Z'_L, Z_R, Z'_R , mix among themselves through a 4×4 mass matrix. Given that $w, \Lambda \gg u, u'$, the mass matrix elements that connect Z_L to Z'_L, Z_R, Z'_R are very suppressed. The mass matrix can be diagonalized using the seesaw formula to separate the light state Z_L from the heavy ones Z'_L, Z_R, Z'_R . Thus, the SM Z boson is identified with Z_L whose mass is $m_Z^2 \simeq \frac{g_L^2}{4c_W^2} (u^2 + u'^2)$. For the heavy neutral gauge bosons, the mass matrix elements are proportional to the square of the w, w', Λ energy scales. In the general case, it is very difficult to find the physical heavy states. However, if there is a hierarchy between two energy scales w, w' and Λ , we can find them. In particular, in the limit $\Lambda \gg w, w'$, the physical heavy states are

$$Z'_L \simeq Z'_L, \quad m_{Z'_L}^2 \simeq \frac{g_L^2}{3} \frac{(1 + \varsigma_1^2 t_R^2 t_X^2 \beta^2)^2 t_W^2 w^2}{\varsigma_1^2 t_R^2 t_X^2}, \quad (3.48)$$

$$Z_R \simeq c_{\xi_3} Z_R - s_{\xi_3} Z'_R, \quad Z'_R \simeq s_{\xi_3} Z_R + c_{\xi_3} Z'_R, \quad (3.49)$$

$$m_{Z_R}^2 \simeq \frac{g_L^2}{3} \frac{3w'^2 [t_R^2 + t_X^2 (1 + \beta^2)]^2 + w^2 [3t_R^4 + 2t_R^2 t_X^2 (3 + \sqrt{3}\beta) + t_X^4 (3 + 2\sqrt{3}\beta + \beta^2)]}{\varsigma_1^{-2} [4 + (3 + 2\sqrt{3}\beta + \beta^2) (t_X^2 / t_R^2)]},$$

$$m_{Z'_R}^2 \simeq \frac{g_L^2}{3} \left\{ 4t_R^2 + t_X^2 (3 + 2\sqrt{3}\beta + \beta^2) \right\} \Lambda^2, \quad (3.50)$$

where the Z_R - Z'_R mixing angle is

$$t_{2\xi_3} = \frac{2t_R [\sqrt{3}t_R^2 + \beta(3 + \sqrt{3}\beta)t_X^2] \sqrt{t_R^2 + t_X^2 (1 + \beta^2)}}{2t_R^4 + t_R^2 t_X^2 (3 - 2\sqrt{3}\beta + \beta^2) - \beta^2 (3 + 2\sqrt{3}\beta + \beta^2) t_X^4}. \quad (3.51)$$

With the physical states properly identified, we list in appendix B the most important interactions between the gauge bosons and fermions in the model. Now we turn to the discussion of the dark matter phenomenology.

4 Dark matter

Despite the multitude of evidence for the existence of dark matter in our universe, its nature remains a mystery and it is one of the most exciting and important open questions in basic science [2]. In this work, we will investigate the possible dark matter candidates in our model and discuss the relevant observables, namely relic density and direct detection cross section. Indirect detection is not very relevant in our model because we will be discussing multi-TeV scale dark matter, a regime for which indirect dark matter detection cannot probe the thermal annihilation cross section [59]. In this section we will briefly address the possibility of scalar and fermion WIMP dark matter. First we note that, in some limiting cases, it is very similar to the one present in 3-3-1 models [43, 44, 47, 51, 60, 61]. As a result we opt for a more sketchy presentation here, primarily aimed at establishing the viability of the present scenario, rather than covering it in full generality. Our main goal in this section is to illustrate our reasoning concerning the origin of the dark matter stability in a unified framework involving 3-3-1 and left-right symmetries, by simply showing that we have do viable dark matter candidates.

That said, we have seen that the W -parity symmetry is exact and unbroken by the VEVs. Thus, the lightest neutral W -particle is stable and can be potentially responsible for the observed DM relic density. For concreteness we will study the model with $q = 0$, i.e. $\beta = -\frac{1}{\sqrt{3}}$. The neutral W -particles include a fermion N_a^0 , a vector gauge boson $X_{1,2}^0$, and a scalar $\mathcal{H}_{1,2}^0$.⁴

4.1 Scalar dark matter

4.1.1 Relic density

Suppose that \mathcal{H}_2^0 is the lightest W -particle (LWP). It cannot decay and can only be produced in pairs. The scalar dark matter has only s -wave contribution to the annihilation cross-section. Hence, the dark matter abundance can be approximated as

$$\Omega_{\mathcal{H}_2} h^2 \simeq \frac{0.1 \text{ pb}}{\langle \sigma v_{\text{rel}} \rangle}, \quad (4.1)$$

where $\langle \sigma v_{\text{rel}} \rangle$ is the thermally averaged cross-section times relative velocity. As our candidates are naturally heavy at the new physics scale, the SM Higgs portal is inaccessible. The main contribution to the cross-section times relative velocity is determined by the direct annihilation channel $\mathcal{H}_2^{0*} \mathcal{H}_2^0 \rightarrow H_1 H_1$ or mediated by new scalars. In the limit $\Lambda \gg w, w' \gg u, u'$, the interaction between \mathcal{H}_2^0 and H_1 is approximated as

$$\mathcal{L}_{\mathcal{H}_2^0-H_1} = \frac{[\lambda_2 u^2 + \lambda_1(u^2 + u'^2)] c_{\theta_q}^2}{u^2 + u'^2} \mathcal{H}_2^0 \mathcal{H}_2^0 H_1 H_1. \quad (4.2)$$

It can be shown that the new Higgs portal gives a contribution of the same magnitude as the one above. Therefore in our estimate it is enough to consider only the $\mathcal{H}_2^{0*} \mathcal{H}_2^0 \rightarrow H_1 H_1$ contact interaction. The average cross-section times relative velocity is

$$\langle \sigma v_{\text{rel}} \rangle = \frac{1}{16\pi m_{\mathcal{H}_2}^2} \left\{ \frac{[\lambda_2 u^2 + \lambda_1(u^2 + u'^2)] c_{\theta_q}^2}{u^2 + u'^2} \right\}^2 \left(1 - \frac{\langle v^2 \rangle}{2} - \frac{m_{H_1}^2}{m_{\mathcal{H}_2}^2} \right), \quad (4.3)$$

where the dark matter velocity v satisfies $\langle v^2 \rangle = \frac{3}{2x_F}$, with $x_F = m_{\mathcal{H}_2}/T_F \sim 20$ at the freezeout temperature [1]. Since $m_{\mathcal{H}_2}^2 \gg m_{H_1}^2$, we approximate

$$\langle \sigma v_{\text{rel}} \rangle = \left\{ \frac{\alpha}{150 \text{ GeV}} \right\}^2 \left\{ \frac{[\lambda_2 u^2 + \lambda_1(u^2 + u'^2)] c_{\theta_q}^2}{u^2 + u'^2} \right\}^2 \left\{ \frac{2.656 \text{ TeV}}{m_{\mathcal{H}_2}} \right\}^2. \quad (4.4)$$

Thus, the dark matter candidate \mathcal{H}_2^0 reproduces the correct relic density, $\Omega_{\mathcal{H}_2} h^2 \simeq 0.11$ [58], if $\langle \sigma v_{\text{rel}} \rangle \simeq 1$ pb, or

$$m_{\mathcal{H}_2} \simeq \frac{[\lambda_2 u^2 + \lambda_1(u^2 + u'^2)] c_{\theta_q}^2}{u^2 + u'^2} \times 2.656 \text{ TeV} \sim 2.5 \text{ TeV}, \quad (4.5)$$

for scalar couplings of $\mathcal{O}(1)$, and using the fact that $\alpha^2/(150 \text{ GeV})^2 \simeq 1$ pb. Furthermore, the above condition implies

$$m_{\mathcal{H}_2} < 2.66(\lambda_1 + \lambda_2) \text{ TeV} < 67 \text{ TeV}, \quad (4.6)$$

⁴The other two dark matter models with $q = \pm 1$ can be examined in a similar way.

where the upper limit comes from the perturbativity bound $\lambda_1, \lambda_2 < 4\pi$. Therefore, the dark matter mass may be in the range few TeVs to 67 TeV, depending on its interaction strength with the SM Higgs boson.

4.1.2 Direct detection

The detection through low energy nuclear recoils constitute a clear signature for dark matter particles. Since no signal has been observed thus far, stringent limits have been derived on the dark matter-nucleon scattering cross section [62–70].

In the scalar dark matter scenario, this scattering takes place through the t-channel exchange of a Z'_L and a heavy scalar \mathcal{H}_0^1 . This scenario is similar to the one studied in [50], where it has been shown that one can obey direct detection limits from the XENON1T experiment with 2 years of data for the dark matter masses above 3 TeV, while reproducing the correct relic density. We emphasize that our goal here was simply to show that we do have viable dark matter candidates, rather than investigating in detail their phenomenology. In fact, the latter is substantially more complex than found in previous 3-3-1 models. However it suffices to exemplify the viability of our dark matter candidates under certain assumptions.

4.2 Fermion dark matter

4.2.1 Relic density

Let us now assume that the LWP is one of the neutral fermions denoted by N . The model predicts that N is a Dirac fermion. The covariant derivative (i.e., gauge interactions) dictates the dark matter phenomenology. The dark matter might annihilate into SM particles via the well known Z' portal with predictive observables [53, 71]. The relic density is governed by s-channel annihilations into SM fermions, whose interactions are presented in appendix B. Assuming that the mixing between the gauge boson Z'_L and the other gauge bosons to be small, which can be achieved by taking $\Lambda \gg w, w' \gg u, u'$, one finds the relic density to be achieved either by annihilation into fermion pairs, or into $Z'_L Z'_L$. The role of Z_R is analogous to Z_N in the 3-3-1-1 model [51], which is not discussed further. In figure 1 we show the relic density curve in green.

4.2.2 Direct detection

The dark matter-nucleon scattering is mostly driven by the t-channel exchange of the Z'_L gauge boson. This scattering is very efficient since it is governed simply the couplings with up and down quarks without much freedom. Taking into account the current and projected sensitivities on the dark matter-nucleon scattering cross-section, one can conclude that the dark matter mass must lie in the few TeV scale, as already investigated in [61]. Notice that this conclusion holds for a Dirac fermion (the possibility of having a Majorana fermion has already been ruled out by direct detection data [61]). The Majorana dark matter case leads to an annihilation rate which is helicity suppressed and therefore the range of parameter space that yields the correct relic density is smaller compared to the Dirac fermion scenario, only Z'_L masses up to 2.5 TeV can reproduce the correct relic density in the Z'_L resonance regime.

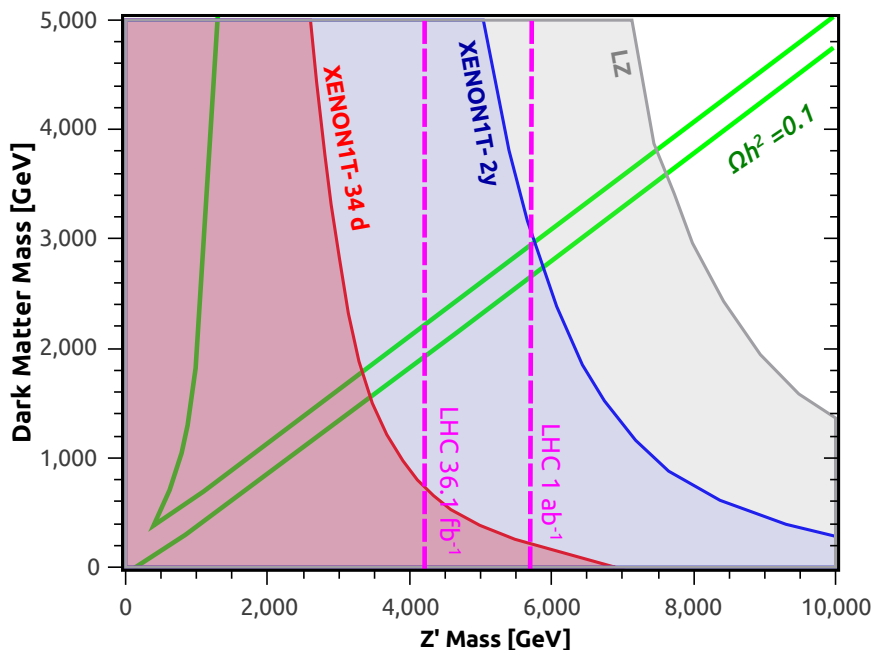


Figure 1. Summary plot for the fermion dark matter. Relic density curve (green), LHC (pink) and current direct detection limit from XENON1T-34 days (red) [67], projected from XENON1T-2 years (blue) [74] and LZ (gray) [75] are overlaid. See text for detail.

4.2.3 Collider

As for collider bounds, LHC results based on heavy dilepton resonance searches with $13.3 fb^{-1}$ of integrated luminosity exclude Z'_L masses below few 3.8 TeV [61]. This is very important because in light of this bound, the Majorana dark matter case has already been ruled out, since the entire parameter space which yields the correct relic density is within the LHC exclusion region.

In light of the importance of this collider bound we took the opportunity to do a rescaling with the luminosity to obtain current and projected limits on the Z'_L mass in our model for $36.1 fb^{-1}$ and $1000 fb^{-1}$ keeping the center-of-energy of 13 TeV, using the collider reach tool introduced in.⁵ The limits read $m_{Z'_L} > 4.2 \text{ TeV}$ and $m_{Z'_L} > 5.7 \text{ TeV}$, respectively. These bounds can be seen as vertical lines in figure 1. We emphasize that other limits stemming from electroweak precision or low energy physics are subdominant thus left out of the discussion [72, 73]. In summary, one can conclude that our model can successfully accommodate a Dirac fermion dark matter in agreement with existing and projected limits near the Z'_L resonance. Once again, our discussion clearly shows the present of a viable dark matter candidate. We stress that, in full generality, the phenomenology of our model is substantially more complex than presented in previous literature. Here we only consider simple benchmarks, for which a detailed study of the dark matter phenomenology has

⁵<http://collider-reach.web.cern.ch/?rts1=13&lumi1=3.2&rts2=13&lumi2=13.3&pdf=MSTW2008mlo68cl.LHgrid>.

already been performed earlier, hence we have not repeated it here. A complete study of the phenomenological implications of our model lies beyond the scope of this paper and will be taken up elsewhere. Nevertheless, our results suffice to establish the consistency of our dark matter candidates.

4.3 Gauge-boson dark matter

4.3.1 Relic density

Finally, let us give a comment on the possibility of vector gauge boson dark matter. In this case one assumes that the LWP is the gauge boson X_1^0 . It can annihilate into SM particles via following channels,

$$X_1^0 X_1^{0*} \rightarrow W_1^+ W_1^-, Z_L Z_L, H_1 H_1, \nu \nu^c, ll^c, qq^c, \tag{4.7}$$

where $\nu = \nu_e, \nu_\mu, \nu_\tau$, $l = e, \mu, \tau$, $q = u, d, c, s, t, b$. However, the dominant channels are $X_1^0 X_1^{0*} \rightarrow W_1^+ W_1^-, Z_L Z_L$. Our predicted result is similar to the one given in [45]. The dark matter relic abundance is approximately given as

$$\Omega_{X_1} h^2 \simeq 10^{-3} \frac{m_W^2}{m_{X_1}^2}. \tag{4.8}$$

Since the annihilation cross section is large and it is dictated by gauge interactions, the abundance of this vector dark matter is too small. In the context of thermal dark matter production, the vector dark matter in our model can contribute to only a tiny fraction of the dark matter abundance in our universe. A similar conclusion has been found in [43].

One way to circumvent the vector dark matter underabundance is by abdicating thermal production and tie its abundance to inflation, where the inflaton decay or the gravitational mechanism would generate the correct dark matter abundance [55]. Alternatively, we mention that vector DM could be just part of the overall cosmological dark matter within a multicomponent thermal dark matter scenario.

5 Conclusions

We have proposed a model of flipped trinification that encompasses the nice features of left-right and 3-3-1 models, while providing an elegant explanation for the origin of matter parity and dark matter stability, which follows as a remnant of the gauge symmetry. The model offers a natural framework for three types of dark matter particles, which is an uncommon feature in UV complete models. One can have a Dirac fermion, as well as a scalar dark matter particle, with masses at the few TeV scale. Both scenarios reproduce the correct relic density, while satisfying existing limits, in the context of thermal freeze-out. As for the vector case, thermal production leads to an under-abundant dark matter. We have also discussed other features of the model such as the symmetry breaking, driven by a minimal scalar content, but sufficient to account for realistic fermion masses. In summary, we have presented a viable theory of flipped trinification able to account naturally for the origin of matter parity and dark matter.

Acknowledgments

The authors thank Carlos Yaguna, Carlos Pires, Alex Dias. This research is funded by Vietnam National Foundation for Science and Technology Development (NAFOSTED) under grant numbers 103.01-2016.77 and 103.01-2017.05, and is supported by the Spanish grants FPA2014-58183-P and SEV-2014-0398 (MINECO), and PROMETEOII/2014/084 (Generalitat Valenciana). FSQ acknowledges support from MEC, UFRN and ICTP-SAIFR FAPESP grant 2016/01343-7. C.A.V-A. acknowledges financial support from Cátedras CONACYT, proyect 749.

A Relevant scalar mass terms

The scalar fields mix according to the class they belong, and their relevant corresponding mass terms are derived as

$$\begin{aligned}
 V_{\text{mass}}^A = & A_2^2 \left\{ \frac{w^2 u'^2 (2\lambda_2 (w^2 - u'^2) + \zeta_6 w'^2)}{4u^2 (u'^2 - w^2)} \right\} + A_2 A_3 \left\{ \frac{w^2 u' (2\lambda_2 (w^2 - u'^2) + \zeta_6 w'^2)}{2u (u'^2 - w^2)} \right\} \\
 & + A_2 A_4 \left\{ \frac{w u'^2 (2\lambda_2 (w^2 - u'^2) + \zeta_6 w'^2)}{2u (u'^2 - w^2)} \right\} + A_3^2 \left\{ \frac{w^2 (2\lambda_2 (w^2 - u'^2) + \zeta_6 w'^2)}{4(u'^2 - w^2)} \right\} \\
 & + A_3 A_4 \left\{ \frac{w u' (2\lambda_2 (w^2 - u'^2) + \zeta_6 w'^2)}{2(u'^2 - w^2)} \right\} + A_4^2 \left\{ \frac{u'^2 (2\lambda_2 (w^2 - u'^2) + \zeta_6 w'^2)}{4(u'^2 - w^2)} \right\}. \quad (\text{A.1})
 \end{aligned}$$

$$\begin{aligned}
 V_{\text{mass}}^S = & (\kappa_1 + \kappa_2) \Lambda^2 S_1^2 + \left\{ \frac{(u'^2 - u^2) [2\lambda_2 (u^2 - w^2) (u'^2 - w^2) + \zeta_6 w^2 w'^2]}{u (u'^2 - w^2) \Lambda} + \zeta_2 u \Lambda \right\} S_1 S_2 + \zeta_2 u' \Lambda S_1 S_3 \\
 & + \zeta_2 w \Lambda S_1 S_4 + \zeta_4 w' \Lambda S_1 S_5 + \frac{2(u'^2 - w^2) [2(\lambda_1 + \lambda_2) u^4 - \lambda_2 u'^2 w^2] + \zeta_6 u'^2 w^2 w'^2}{4u^2 (u'^2 - w^2)} S_2^2 \\
 & + \frac{u' [4\lambda_1 u^2 + w^2 (2\lambda_2 + \frac{\zeta_6 w'^2}{w^2 - u'^2})]}{2u} S_2 S_3 + \frac{w (4\lambda_1 u^2 + u'^2 [2\lambda_2 + \frac{\zeta_6 w'^2}{w^2 - u'^2}])}{2u} S_2 S_4 + \zeta_1 u w' S_2 S_5 \\
 & + \left\{ \lambda_1 u'^2 + \lambda_2 (u'^2 - \frac{w^2}{2}) - \frac{\zeta_6 w^2 w'^2}{4(w^2 - u'^2)} \right\} S_3^2 + \frac{w u'}{2} \left\{ 4\lambda_1 + 2\lambda_2 + \frac{\zeta_6 w'^2}{w^2 - u'^2} \right\} S_3 S_4 + \zeta_1 u' w' S_3 S_5 \\
 & + \left\{ \lambda_1 w^2 + \lambda_2 (w^2 - \frac{u'^2}{2}) - \frac{\zeta_6 u'^2 w'^2}{4(w^2 - u'^2)} \right\} S_4^2 + w w' (\zeta_1 + \zeta_6) S_4 S_5 + \lambda w'^2 S_5^2. \quad (\text{A.2})
 \end{aligned}$$

$$\begin{aligned}
 V_{\text{mass}}^{\text{singly-charged}} = & \frac{(u^2 - u'^2)^2 [2\lambda_2 (u'^2 - w^2) (u'^2 - w^2) + \zeta_6 w^2 w'^2]}{4u^2 (u'^2 - w^2) \Lambda^2} \sigma_{12}^- \sigma_{12}^+ \\
 & + \left\{ \lambda_2 (u^2 - w^2) + \frac{\zeta_6 w^2 w'^2}{2(u'^2 - w^2)} \right\} \phi_{12}^- \phi_{12}^+ + \left\{ \frac{\lambda_2 u'^2 (u^2 - w^2)}{u^2} + \frac{\zeta_6 w^2 w'^2 u'^2}{2u^2 (u'^2 - w^2)} \right\} \phi_{21}^+ \phi_{21}^- \\
 & + \left\{ \frac{(u'^2 - u^2) (2\lambda_2 (u^2 - w^2) (u'^2 - w^2) + \zeta_6 w^2 w'^2)}{2\sqrt{2} u (u'^2 - w^2) \Lambda} \left(\sigma_{12}^- \phi_{12}^+ + \frac{u'}{u} \sigma_{12}^- \phi_{21}^+ \right) \right. \\
 & \left. + \left(\frac{\lambda_2 u'^2 (u^2 - w^2)}{u^2} + \frac{\zeta_6 u'^2 w^2 w'^2}{2u^2 (u'^2 - w^2)} \right) \phi_{12}^- \phi_{21}^+ + H.c. \right\}. \quad (\text{A.3})
 \end{aligned}$$

$$\begin{aligned}
 V_{\text{mass}}^{q\text{-charged}} = & \left\{ \lambda_2(u^2 - u'^2) + \frac{\zeta_6 u'^2 w'^2}{2(u'^2 - w'^2)} \right\} \phi_{13}^{+q} \phi_{13}^{-q} + \left\{ \frac{\lambda_2 w^2 (u^2 - u'^2)}{u^2} + \frac{\zeta_6 u'^2 w'^2 w^2}{2u^2(u'^2 - w'^2)} \right\} \phi_{31}^{+q} \phi_{31}^{-q} \\
 & + \left\{ \frac{(u^2 - u'^2)(u^2 - w^2)(2\lambda_2(u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w' + \zeta_5(u'^2 - w^2)u^2 w'^2 \Lambda^2)}{4u^2 \Lambda^2 (u'^2 - w'^2)} \right\} \sigma_{13}^{+q} \sigma_{13}^{-q} \\
 & + \frac{1}{2} \left\{ \zeta_6(u^2 - w^2) + \zeta_5 \Lambda^2 \right\} \chi_1^{+q} \chi_1^{-q} + \left\{ \frac{\lambda_2 w (u^2 - u'^2)}{u} + \frac{\zeta_6 u'^2 w'^2 w}{2u(u'^2 - w'^2)} \right\} \phi_{13}^{+q} \phi_{31}^{-q} \\
 & + \frac{(u'^2 - u^2)(2\lambda_2(u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w'^2)}{2\sqrt{2}u(u'^2 - w'^2)\Lambda} \phi_{13}^{+q} \sigma_{13}^{-q} + \frac{\zeta_6 u w'}{2} \phi_{13}^{+q} \chi_1^{-q} + \frac{\zeta_5 w' \Lambda}{2\sqrt{2}} \sigma_{13}^{+q} \chi_1^{-q} \\
 & + \left. \frac{(u'^2 - u^2)w(2\lambda_2(u^2 - w^2)(u'^2 - w^2) + \zeta_6 w^2 w'^2)}{2\sqrt{2}u^2(u'^2 - w'^2)\Lambda} \phi_{31}^{+q} \sigma_{13}^{-q} + \frac{\zeta_6 w w'}{2} \phi_{31}^{+q} \chi_1^{-q} + H.c. \right\}. \tag{A.4}
 \end{aligned}$$

$$\begin{aligned}
 V_{\text{mass}}^{(q+1)\text{-charged}} = & \frac{\zeta_6 u'^2 w'^2}{2(u'^2 - w'^2)} \phi_{23}^{q+1} \phi_{23}^{-(q+1)} + \frac{\zeta_6 w^2 w'^2}{2(u'^2 - w'^2)} \phi_{32}^{q+1} \phi_{32}^{-(q+1)} + \frac{1}{2} \zeta_6 (u'^2 - w'^2) \chi_2^{(q+1)} \chi_2^{-(q+1)} \\
 & + \left\{ \frac{\zeta_6 u' w w'^2}{2(u'^2 - w'^2)} \phi_{23}^{q+1} \phi_{32}^{-(q+1)} + \frac{\zeta_6 u' w'}{2} \phi_{23}^{q+1} \chi_2^{-(q+1)} + \frac{\zeta_6 w w'}{2} \phi_{32}^{q+1} \chi_2^{-(q+1)} + H.c. \right\}. \tag{A.5}
 \end{aligned}$$

B Fermion gauge-boson interactions

The gauge interactions of fermions arise from,

$$\mathcal{L} \supset \bar{\Psi} i \gamma^\mu \partial_\mu \Psi - g_L \bar{\Psi}_L \gamma^\mu (P_{L\mu}^{CC} + P_{L\mu}^{NC}) \Psi_L - g_R \bar{\Psi}_R \gamma^\mu (P_{R\mu}^{CC} + P_{R\mu}^{NC}) \Psi_R, \tag{B.1}$$

where Ψ_L and Ψ_R run on all left-handed and right-handed fermion multiplets, respectively, and $P_{L,R}^{CC} = \sum_{n=1,2,4,5,6,7} T_{nL,R} A_{nL,R}$, $P_{L,R}^{NC} = T_{3L,R} A_{3L,R} + T_{8L,R} A_{8L,R} + \frac{g_X}{g_{L,R}} X_{\Psi_{L,R}} B$.

The interactions of the physical charged gauge bosons with fermions are

$$\mathcal{L}_{CC} = J_{1W}^{-\mu} W_{1\mu}^+ + J_{2W}^{-\mu} W_{2\mu}^+ + J_{1X}^{-q\mu} X_{1\mu}^q + J_{2X}^{-q\mu} X_{2\mu}^q + J_{1Y}^{-(q+1)\mu} Y_{1\mu}^{q+1} + J_{2Y}^{-(q+1)\mu} Y_{2\mu}^{q+1} + H.c.,$$

where the charged currents take the form,

$$\begin{aligned}
 J_{1W}^{-\mu} &= -\frac{g_L C \xi}{\sqrt{2}} (\bar{\nu}_{\alpha L} \gamma^\mu e_{\alpha L} + \bar{u}_{\alpha L} \gamma^\mu d_{\alpha L}) + \frac{g_R S \xi}{\sqrt{2}} (\bar{\nu}_{\alpha R} \gamma^\mu e_{\alpha R} + \bar{u}_{\alpha R} \gamma^\mu d_{\alpha R}), \\
 J_{2W}^{-\mu} &= -\frac{g_L S \xi}{\sqrt{2}} (\bar{\nu}_{\alpha L} \gamma^\mu e_{\alpha L} + \bar{u}_{\alpha L} \gamma^\mu d_{\alpha L}) - \frac{g_R C \xi}{\sqrt{2}} (\bar{\nu}_{\alpha R} \gamma^\mu e_{\alpha R} + \bar{u}_{\alpha R} \gamma^\mu d_{\alpha R}), \\
 J_{1X}^{-q\mu} &= -\frac{g_L C \xi_1}{\sqrt{2}} (\bar{N}_{\alpha L} \gamma^\mu \nu_{\alpha L} - \bar{d}_{\alpha L} \gamma^\mu J_{\alpha L} + \bar{J}_{3L} \gamma^\mu u_{3L}) + \frac{g_R S \xi_1}{\sqrt{2}} (\bar{N}_{\alpha R} \gamma^\mu \nu_{\alpha R} - \bar{d}_{\alpha R} \gamma^\mu J_{\alpha R} + \bar{J}_{3R} \gamma^\mu u_{3R}), \\
 J_{2X}^{-q\mu} &= -\frac{g_L S \xi_1}{\sqrt{2}} (\bar{N}_{\alpha L} \gamma^\mu \nu_{\alpha L} - \bar{d}_{\alpha L} \gamma^\mu J_{\alpha L} + \bar{J}_{3L} \gamma^\mu u_{3L}) - \frac{g_R C \xi_1}{\sqrt{2}} (\bar{N}_{\alpha R} \gamma^\mu \nu_{\alpha R} - \bar{d}_{\alpha R} \gamma^\mu J_{\alpha R} + \bar{J}_{3R} \gamma^\mu u_{3R}), \\
 J_{1Y}^{-(q+1)\mu} &= -\frac{g_L C \xi_2}{\sqrt{2}} (\bar{N}_{\alpha L} \gamma^\mu e_{\alpha L} + \bar{u}_{\alpha L} \gamma^\mu J_{\alpha L} + \bar{J}_{3L} \gamma^\mu d_{3L}) + \frac{g_R S \xi_2}{\sqrt{2}} (\bar{N}_{\alpha R} \gamma^\mu e_{\alpha R} + \bar{u}_{\alpha R} \gamma^\mu J_{\alpha R} + \bar{J}_{3R} \gamma^\mu d_{3R}), \\
 J_{2Y}^{-(q+1)\mu} &= -\frac{g_L S \xi_2}{\sqrt{2}} (\bar{N}_{\alpha L} \gamma^\mu e_{\alpha L} + \bar{u}_{\alpha L} \gamma^\mu J_{\alpha L} + \bar{J}_{3L} \gamma^\mu d_{3L}) - \frac{g_R C \xi_2}{\sqrt{2}} (\bar{N}_{\alpha R} \gamma^\mu e_{\alpha R} + \bar{u}_{\alpha R} \gamma^\mu J_{\alpha R} + \bar{J}_{3R} \gamma^\mu d_{3R}).
 \end{aligned}$$

The interactions of the physical neutral gauge bosons with fermions are obtained by

$$\begin{aligned}
 \mathcal{L}_{NC} &= -g_L \bar{\Psi}_L \gamma^\mu P_{L\mu}^{NC} \Psi_L - g_R \bar{\Psi}_R \gamma^\mu P_{R\mu}^{NC} \Psi_R \\
 &= -eQ(f) \bar{f} \gamma^\mu f A_\mu - \frac{g_L}{2c_W} \bar{f} \gamma^\mu [g_V^{Z_L}(f) - g_A^{Z_L}(f) \gamma_5] f Z_{L\mu} - \frac{g_L}{2c_W} \bar{f} \gamma^\mu [g_V^{Z'_L}(f) - g_A^{Z'_L}(f) \gamma_5] f Z'_{L\mu} \\
 &\quad - \frac{g_L}{2c_W} \bar{f} \gamma^\mu [g_V^{Z_R}(f) - g_A^{Z_R}(f) \gamma_5] f Z_{R\mu} - \frac{g_L}{2c_W} \bar{f} \gamma^\mu [g_V^{Z'_R}(f) - g_A^{Z'_R}(f) \gamma_5] f Z'_{R\mu}, \tag{B.2}
 \end{aligned}$$

f	$g_V^{Z_L}(f)$
$g_V^{Z_L}(\nu_a)$	$\frac{\{t_R^2[3+(1+t_R)t_X(3+\sqrt{3}\beta)]+t_X^2[3+3\beta^2+t_R^2(3\beta^2-3-2\sqrt{3}\beta)]\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(\nu_a)$	$\frac{\{t_R^2[3-(t_R-1)t_X(3+\sqrt{3}\beta)]+3(1+t_R^2)t_X^2(1+\beta^2)\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(e_a)$	$-\frac{\{t_R^2[3-(1+t_R)t_X(3+\sqrt{3}\beta)]+t_X^2[3+3\beta^2+t_R^2(-3+2\sqrt{3}\beta+3\beta^2)]\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(e_a)$	$-\frac{\{t_R^2[3+(t_R-1)t_X(3+\sqrt{3}\beta)]+3(t+t_R^2)t_X^2(1+\beta^2)\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(N_a)$	$\frac{t_X t_R^2 \{4\sqrt{3}\beta t_X + (1+t_R)(3+\sqrt{3}\beta)\} c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(N_a)$	$-\frac{(t_R-1)t_R^2 t_X (3+\sqrt{3}\beta) c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(u_\alpha)$	$-\frac{\{3t_R^2+(1+t_R)t_X t_R^2(1+\sqrt{3}\beta)+t_X^2[3+3\beta^2+t_R^2(3\beta^2+2\sqrt{3}\beta-3)]\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(u_\alpha)$	$-\frac{\{3t_R^2-(t_R-1)t_R^2 t_X (1+\sqrt{3}\beta)+3(1+t_R^2)t_X^2(1+\beta^2)\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(u_3)$	$\frac{\{3t_R^2+t_R^2(1+t_R)t_X(\sqrt{3}\beta-1)+t_X^2[3+3\beta^2+t_R^2(3\beta^2-3-2\sqrt{3}\beta)]\}c_W}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(u_3)$	$\frac{\{3t_R^2-(t_R-1)t_R^2 t_X (\sqrt{3}\beta-1)+3(1+t_R^2)t_X^2(1+\beta^2)\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(d_\alpha)$	$\frac{\{3t_R^2-t_R^2(1+t_R)t_X(1+\sqrt{3}\beta)+t_X^2[3+3\beta^2+t_R^2(3\beta^2-2\sqrt{3}\beta-3)]\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(d_\alpha)$	$\frac{\{3t_R^2+(t_R-1)t_R^2 t_X (1+\sqrt{3}\beta)+3(1+t_R^2)t_X^2(1+\beta^2)\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(d_3)$	$\frac{\{-3t_R^2+t_R^2(1+t_R)t_X(\sqrt{3}\beta-1)-t_X^2[3+3\beta^2+t_R^2(3\beta^2+2\sqrt{3}\beta-3)]\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)\beta^2 t_X^2]}$
$g_A^{Z_L}(d_3)$	$\frac{\{-3t_R^2+(1-t_R)t_R^2 t_X (\sqrt{3}\beta-1)-3t_X^2(1+t_R^2)(1+\beta^2)\}c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)\beta^2 t_X^2]}$
$g_V^{Z_L}(J_\alpha)$	$-\frac{t_X t_R^2 [1+t_R+\sqrt{3}t_R\beta+\sqrt{3}(1-4t_X)\beta] c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(J_\alpha)$	$\frac{(t_R-1)t_R^2 t_X (1+\sqrt{3}\beta) c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_V^{Z_L}(J_3)$	$\frac{t_R^2 t_X [4\sqrt{3}t_X\beta+(1+t_R)(\sqrt{3}\beta-1)] c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z_L}(J_3)$	$\frac{(t_R-1)t_R^2 t_X (\sqrt{3}\beta-1) c_W^2}{6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$

Table 2. The couplings of Z_L with fermions.

where f stands for every all the fermion fields, and $e = g_L s_W$. The vector and axial-vector couplings $g_{V,A}^{Z_L, Z'_L, Z_R, Z'_R}(f)$ are collected in tables 2, 3, 4, and 5. Note that at high energy $g_L = g_R$, i.e. $t_X = t_R$, due to the left-right symmetry. However, at the low energy, such relation does not hold anymore. Therefore, the couplings we provide are general, depending on both t_X and t_R .

$g_{V^L}^{Z'_L}(\nu_a)$	$\frac{\{-\sqrt{3}(t_R^2+t_X^2)-3\beta t_X t_R^2(1+t_R-t_X)-\sqrt{3}\beta^2 t_X(1+t_R)(t_R^2+t_X-t_R t_X)\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(\nu_a)$	$\frac{\{t_R^3 t_X \beta(3+\sqrt{3}\beta)-\sqrt{3}t_X^2(1+\beta^2)-t_R^2[\sqrt{3}+t_X(1+t_X)\beta(3+\sqrt{3}\beta)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(e_a)$	$\frac{\{-\sqrt{3}t_R^2-t_R^2(1+t_R)t_X\beta(3+\sqrt{3}\beta)+t_X^2[t_R^2\beta(-3+\sqrt{3}\beta)-\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(e_a)$	$\frac{\{-\sqrt{3}(t_R^2+t_X^2)+3\beta t_X t_R^2(-1+t_R+t_X)-\sqrt{3}\beta^2 t_X[t_X+t_R^2(1-t_R+t_X)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(N_a)$	$\frac{\{2\sqrt{3}t_R^2-\beta t_X t_R^2(1+t_R)(3+\sqrt{3}\beta)+2\sqrt{3}t_X^2[1-(t_R^2-1)\beta^2]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(N_a)$	$\frac{\{2\sqrt{3}t_R^2+\beta t_X t_R^2(t_R-1)(3+\sqrt{3}\beta)+2\sqrt{3}t_X^2[1+(1+t_R^2)\beta^2]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(u_\alpha)$	$\frac{\{-\sqrt{3}t_R^2+\beta t_X t_R^2(t_R+1)(\sqrt{3}\beta+1)+t_X^2[t_R^2\beta(-3+\sqrt{3}\beta)-\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(u_\alpha)$	$\frac{\{-\sqrt{3}t_R^2-\beta t_X t_R^2(t_R-1)(1+\sqrt{3}\beta)-t_X^2[\beta t_R^2(\sqrt{3}\beta-3)+\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(u_3)$	$\frac{\{-\sqrt{3}t_R^2-\beta t_X t_R^2(t_R+1)(\sqrt{3}\beta-1)+t_X^2[t_R^2\beta(3+\sqrt{3}\beta)-\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(u_3)$	$\frac{\{-\sqrt{3}(t_R^2+t_X^2)-\beta t_X t_R^2(t_R-1+3t_X)-\sqrt{3}t_X[t_X+t_R^2(1+t_X-t_R)]\beta^2\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(d_\alpha)$	$\frac{\{-\sqrt{3}t_R^2+\beta t_X t_R^2(t_R+1)(\sqrt{3}\beta+1)+t_X^2[t_R^2\beta(3+\sqrt{3}\beta)-\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(d_\alpha)$	$\frac{\{-\sqrt{3}t_R^2-\beta t_X t_R^2(t_R-1)(1+\sqrt{3}\beta)-t_X^2[\beta t_R^2(3+\sqrt{3}\beta)+\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(d_3)$	$\frac{\{-\sqrt{3}t_R^2-\beta t_X t_R^2(t_R+1)(\sqrt{3}\beta-1)+t_X^2[t_R^2\beta(-3+\sqrt{3}\beta)-\sqrt{3}(1+\beta^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(d_3)$	$\frac{\{-\sqrt{3}(t_R^2+t_X^2)+\beta t_X t_R^2(1-t_R+3t_X)-\sqrt{3}t_X[t_X+t_R^2(1+t_X-t_R)]\beta^2\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(J_\alpha)$	$\frac{\{2\sqrt{3}t_R^2+\beta t_X t_R^2(t_R+1)(\sqrt{3}\beta+1)+2\sqrt{3}t_X^2[1-(t_R^2-1)\beta^2]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(J_\alpha)$	$\frac{\{2\sqrt{3}t_R^2-\beta t_X t_R^2(t_R-1)(\sqrt{3}\beta+1)+2\sqrt{3}t_X^2[1+\beta^2(1+t_R^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_{V^L}^{Z'_L}(J_3)$	$\frac{\{2\sqrt{3}t_R^2-\beta t_X t_R^2(t_R+1)(\sqrt{3}\beta-1)+2\sqrt{3}t_X^2[1-(t_R^2-1)\beta^2]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$
$g_A^{Z'_L}(J_3)$	$\frac{\{2\sqrt{3}t_R^2+\beta t_X t_R^2(t_R-1)(\sqrt{3}\beta-1)+2\sqrt{3}t_X^2[1+\beta^2(1+t_R^2)]\}}{\zeta_1^{-1} t_R^{-1} t_X^{-1} c_W^{-1} t_W 6[t_R^2+t_X^2+(1+t_R^2)t_X^2\beta^2]}$

Table 3. The couplings of Z'_L with fermions.

f	$g_V^{\mathcal{Z}_R}(f)$
ν_a	$-\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}-\sqrt{3}\beta t_X^2+t_X(1+t_R)(3+\sqrt{3}\beta)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
e_a	$-\frac{\{c_{e_2}t_R\zeta_1^{-1}[-3\zeta^{-2}-\sqrt{3}\beta t_X^2+t_X(1+t_R)(3+\sqrt{3}\beta)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
N_a	$-\frac{\{c_{e_2}t_R t_X \zeta_1^{-1}[2\sqrt{3}t_X\beta+(t_R+1)(3+\sqrt{3}\beta)]+s_{e_2}\zeta_1^{-2}[-2\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_α	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_R(1+t_X)+\sqrt{3}\beta t_X(1+t_R+t_X)]+s_{e_2}\zeta_1^{-2}[-\sqrt{3}t_R^2+t_X\beta(1+\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_3	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[-3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}t_X(t_X-t_R-1)\beta]-s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_α	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[-3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}\beta t_X(t_X+t_R+1)]+s_{e_2}\zeta_1^{-2}[-\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_3	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}\beta t_X(t_X-t_R-1)]-s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_α	$\frac{\{c_{e_2}t_R t_X \zeta_1^{-1}[1+t_R+\sqrt{3}\beta(1+t_R-2t_X)]+s_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_3	$\frac{\{c_{e_2}t_R t_X \zeta_1^{-1}[1+t_R-\sqrt{3}t_R\beta-\sqrt{3}\beta(1+2t_X)]+s_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2+t_X\beta(1-\sqrt{3}\beta)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
f	$g_A^{\mathcal{Z}_R}(f)$
ν_a	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}-\sqrt{3}\beta t_X^2+t_X(t_R-1)(3+\sqrt{3}\beta)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
e_a	$\frac{\{-c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+\sqrt{3}\beta t_X^2+t_X(t_R-1)(3+\sqrt{3}\beta)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
N_a	$\frac{\{c_{e_2}t_R t_X \zeta_1^{-1}[2\sqrt{3}t_X\beta+(t_R-1)(3+\sqrt{3}\beta)]+s_{e_2}\zeta_1^{-2}[-2\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_α	$\frac{\{-c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R-1)+\sqrt{3}\beta t_X(-1+t_R+t_X)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(1+\sqrt{3}\beta)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_3	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R-1)(\sqrt{3}\beta-1)-\sqrt{3}\beta t_X^2]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_α	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(1-t_R)-\sqrt{3}\beta t_X(t_X+t_R-1)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_3	$\frac{\{-c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R-1)+\sqrt{3}\beta t_X(t_X-t_R+1)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(1-\sqrt{3}\beta)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_α	$\frac{\{c_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(1-t_R)-\sqrt{3}\beta(t_R+t_X-1)]+s_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_3	$\frac{\{c_{e_2}t_R t_X \zeta_1^{-1}[2\sqrt{3}t_X\beta+(t_R-1)(\sqrt{3}\beta-1)]+s_{e_2}\zeta_1^{-2}[-2\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$

Table 4. The couplings of \mathcal{Z}_R with fermions.

f	$g_V^{\mathcal{Z}'_R}(f)$
ν_a	$\frac{\{-s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}-\sqrt{3}\beta t_X^2+t_X(1+t_R)(3+\sqrt{3}\beta)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
e_a	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+\sqrt{3}\beta t_X^2-t_X(1+t_R)(3+\sqrt{3}\beta)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
N_a	$-\frac{\{s_{e_2}t_R t_X \zeta_1^{-1}[2\sqrt{3}t_X\beta+(t_R+1)(3+\sqrt{3}\beta)]+c_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2-t_X\beta(3+\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_α	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}\beta t_X(1+t_R+t_X)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2-t_X\beta(1+\sqrt{3}\beta)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_3	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[-3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}t_X(t_X-t_R-1)\beta]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_α	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[-3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}\beta t_X(t_X+t_R+1)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2-t_X\beta(\sqrt{3}\beta+1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_3	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R+1)+\sqrt{3}\beta t_X(t_X-t_R-1)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_α	$-\frac{\{-s_{e_2}t_R t_X \zeta_1^{-1}[1+t_R+\sqrt{3}\beta(1+t_R-2t_X)]+c_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_3	$-\frac{\{-s_{e_2}t_R t_X \zeta_1^{-1}[1+t_R-\sqrt{3}t_R\beta-\sqrt{3}\beta(1+2t_X)]+c_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2+t_X\beta(1-\sqrt{3}\beta)(t_R+1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
f	$g_A^{\mathcal{Z}'_R}(f)$
ν_a	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}-\sqrt{3}\beta t_X^2+t_X(t_R-1)(3+\sqrt{3}\beta)]-c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
e_a	$-\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+\sqrt{3}\beta t_X^2-t_X(t_R-1)(3+\sqrt{3}\beta)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
N_a	$\frac{\{s_{e_2}t_R t_X \zeta_1^{-1}[2\sqrt{3}t_X\beta+(t_R-1)(3+\sqrt{3}\beta)]+c_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2+t_X\beta(3+\sqrt{3}\beta)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_α	$-\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R-1)+\sqrt{3}\beta t_X(-1+t_R+t_X)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(1+\sqrt{3}\beta)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
u_3	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R-1)(\sqrt{3}\beta-1)-\sqrt{3}\beta t_X^2]-c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_α	$\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(1-t_R)-\sqrt{3}\beta t_X(t_X+t_R-1)]-c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(1-t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
d_3	$-\frac{\{s_{e_2}t_R\zeta_1^{-1}[3\zeta^{-2}+t_X(t_R-1)+\sqrt{3}\beta t_X(t_X-t_R+1)]+c_{e_2}\zeta_1^{-2}[\sqrt{3}t_R^2+t_X\beta(1-\sqrt{3}\beta)(1+t_R)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_α	$\frac{\{s_{e_2}t_R t_X \zeta_1^{-1}[(1-t_R)+\sqrt{3}\beta(1-t_R+2t_X)]+c_{e_2}\zeta_1^{-2}[2\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta+1)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$
J_3	$\frac{\{s_{e_2}t_R t_X \zeta_1^{-1}[2\sqrt{3}t_X\beta+(t_R-1)(\sqrt{3}\beta-1)]-c_{e_2}\zeta_1^{-2}[-2\sqrt{3}t_R^2+t_X\beta(\sqrt{3}\beta-1)(t_R-1)]\}c_W}{6\zeta^{-1}\zeta_1^{-2}}$

Table 5. The couplings of \mathcal{Z}'_R with fermions.

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