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High-scale leptogenesis with three-loop neutrino mass generation and dark matter

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ABSTRACT: We demonstrate a common origin for high-scale leptogenesis and three-loop neutrino mass generation. Specifically we extend the standard model by two real singlet scalars, two singly charged scalars carrying different quantum numbers under certain global symmetry and two or more singlet fermions with Majorana masses. This global symmetry is only allowed to be softly or spontaneously broken. Our model also respects an exactly conserved Z_2 discrete symmetry. Through the real scalar decays and then the charged scalar decays, we can obtain a lepton asymmetry stored in the standard model leptons. This lepton asymmetry can be partially converted to a baryon asymmetry by the sphaleron processes. The interactions for this leptogenesis can also result in a three-loop diagram to generate the neutrino masses. The lightest singlet fermion can keep stable to serve as a dark matter particle.

KEYWORDS: Beyond Standard Model, Cosmology of Theories beyond the SM, Neutrino Physics

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Contents

1	Introduction	1
2	The model	2
3	Neutrino masses and dark matter	3
4	Leptogenesis	4
5	Summary	7

1 Introduction

The phenomena of neutrino oscillations have been established by the atmospheric, solar, accelerator and reactor neutrino experiments. This means the existence of three flavors of massive and mixing neutrinos which are beyond the standard model (SM) [1]. Meanwhile, the cosmological observations stringently constrain the neutrino masses should be in the sub-eV region [1]. Currently the most popular scheme for the neutrino mass generation is the famous seesaw [2–13] mechanism which can highly suppress the neutrino masses by a small ratio of the electroweak scale over a newly high scale. The seesaw scale can be lowered if we do some fine tuning on the related couplings. In the usual seesaw models, the lepton-number-violating interactions for the neutrino mass generation can also accommodate a leptogenesis [14–27] mechanism to generate the baryon asymmetry in the universe. In this scenario the seesaw and the leptogenesis are realized at a same scale.

Alternatively, some TeV-scale fields can help us to obtain the small neutrino masses at loop level [28–39]. In this scenario, the neutrino masses may be suppressed by the chirality besides the loop factors. For example, Krauss, Nasri and Trodden (KNT) ever proposed an interesting model with two TeV-scale singly charged scalars and one Majorana singlet fermion to give the neutrino masses at three-loop level [32]. The Majorana singlet fermion can keep stable to serve as a dark matter particle. In order to fulfill the neutrino oscillation data which require at least two nonzero neutrino mass eigenvalues, the KNT model should contain two or more Majorana singlet fermions [33]. Although the KNT model has an advantage of testability at colliders, it cannot explain the cosmic baryon asymmetry.

In this work we will slightly extend the KNT model by two real singlet scalars in order to demonstrate an interesting scenario that a high-scale leptogenesis can be consistent with a testable neutrino mass generation. Specifically, the real singlet scalars are very heavy so that their decays can be responsible for the leptogenesis. Meanwhile, we can obtain the KNT model by integrating out these real singlet scalars.

2 The model

We denote the non-SM fields by

$$N_R(1, 1, 0)(0), \quad \delta(1, 1, +1)(-2), \quad \xi(1, 1, +1)(-1), \quad \sigma(1, 1, 0)(0). \quad (2.1)$$

Here and thereafter the first brackets following the fields describe the transformations under the $SU(3)_c \times SU(2)_L \times U(1)_Y$ gauge groups, while the second brackets are the lepton numbers. We assume the lepton number can be softly broken. Furthermore, our model respects a Z_2 discrete symmetry under which the fields transform as

$$(\text{SM}, \delta) \xrightarrow{Z_2} (\text{SM}, \delta), \quad (N_R, \xi, \sigma) \xrightarrow{Z_2} -(N_R, \xi, \sigma). \quad (2.2)$$

The Z_2 symmetry will not be broken at any scales. This means the real singlet scalars σ will not be allowed to obtain any non-zero vacuum expectation values.

Under the softly broken lepton number and the exactly conserved Z_2 discrete symmetry, the Lagrangian should include

$$\begin{aligned} \mathcal{L} \supset & -\frac{1}{2}M_{\sigma_i}^2\sigma_i^2 - \left(\mu_\delta^2 + \lambda_{\delta\phi}\phi^\dagger\phi\right)\delta^\dagger\delta \\ & - \left(\mu_\xi^2 + \lambda_{\xi\phi}\phi^\dagger\phi\right)\xi^\dagger\xi - \frac{1}{2}M_{N_i}(\bar{N}_{Ri}N_{Ri}^c + \text{H.c.}) \\ & - \left[\rho_i\sigma_i\xi^\dagger\delta + \frac{1}{2}(f_\delta)_{\alpha\beta}\delta\bar{l}_{L\alpha}^c i\tau_2 l_{L\beta} + (f_\xi)_{\alpha i}\xi\bar{e}_{R\alpha}^c N_{Ri} + \text{H.c.}\right] \\ & - y_\alpha(\bar{l}_{L\alpha}\phi e_{R\alpha} + \text{H.c.}). \end{aligned} \quad (2.3)$$

Here ϕ denotes the SM Higgs scalar while l_L and e_R are the SM leptons,

$$\begin{aligned} \phi\left(1, 2, +\frac{1}{2}\right)(0) &= \begin{bmatrix} \phi^+ \\ \phi^0 \end{bmatrix}, \\ l_{L\alpha}\left(1, 2, -\frac{1}{2}\right)(+1) &= \begin{bmatrix} \nu_{L\alpha} \\ e_{L\alpha} \end{bmatrix}, \\ e_{R\alpha}(1, 1, -1)(+1) & \quad (\alpha = e, \mu, \tau). \end{aligned} \quad (2.4)$$

Obviously, the singlet fermions N_{Ri} can form the Majorana fermions as follows,

$$N_i = N_{Ri} + N_{Ri}^c = N_i^c. \quad (2.5)$$

In addition, the two cubic parameters $\rho_{1,2}$ are always allowed to have a relative phase. As we will show later this phase provides the necessary CP violation for the leptogenesis.

So far we have assumed that the cubic terms among the non-SM scalars, i.e. the ρ_i -terms in eq. (2.3), are the unique source for the lepton number violation. Alternatively, we can consider the lepton number assignment in the KNT model where the Majorana mass term of the singlet fermions N_R is the unique source of the lepton number violation. In this case, the present lepton number assignment in eq. (2.1) should be understood as

an additionally global symmetry under which the SM leptons carry a quantum number as same as their lepton number. Clearly, such soft lepton number breaking or other soft symmetry breaking can be induced by a spontaneous symmetry breaking. In this case, we need introduce a complex singlet scalar,

$$\omega(1, 1, 0)(+1), \tag{2.6}$$

and then replace the ρ_i -terms in eq. (2.3) by the following quartic terms,

$$\mathcal{L} \supset -\lambda_i \sigma_i \xi^\dagger \delta \omega + \text{H.c.} . \tag{2.7}$$

After the spontaneous symmetry breaking, we have

$$\rho_i = \lambda_i \langle \omega \rangle, \tag{2.8}$$

with $\langle \omega \rangle$ being the related vacuum expectation value.

The above symmetry breaking will result in a massless Goldstone boson which couples to the δ and ξ scalars as well as the SM leptons. However, these couplings are suppressed by the symmetry breaking scale $\langle \omega \rangle$. For a large symmetry breaking scale $\langle \omega \rangle \gg \langle \phi \rangle \simeq 174 \text{ GeV}$, the Goldstone will decouple at a very high temperature $T_{\langle \omega \rangle} \gg \langle \phi \rangle$ at which the relativistic degrees of freedom should be about $g_* = 112.5$ (the SM fields plus the charged scalars δ and ξ as well as the singlet fermion N_R). The temperature of the Goldstone at the BBN epoch $T \sim 1 \text{ MeV}$ thus should be [41]

$$\left(\frac{T_{\langle \omega \rangle}}{T} \right)^4 \simeq \left(\frac{10.75}{112.5} \right)^{\frac{4}{3}} \simeq 0.044. \tag{2.9}$$

Therefore, the Goldstone will give a negligible contribution to the effective number of additional light neutrinos [41], i.e.

$$\Delta N_\nu = \frac{4}{7} \left(\frac{T_{\langle \omega \rangle}}{T} \right)^4 \simeq 0.025. \tag{2.10}$$

3 Neutrino masses and dark matter

As shown in figure 1, the non-SM scalars and fermions can mediate a three-loop diagram in association with the Yukawa couplings for generating the SM lepton masses. Clearly, after the electroweak symmetry breaking, this three-loop diagram will contribute a Majorana mass term of the left-handed neutrinos. Since the real singlet scalars σ are very heavy, they can be integrated out from eq. (2.3). The resulting Lagrangian then can contain a sizable quartic coupling between the singly charged scalars δ and ξ , i.e.

$$\mathcal{L} \supset -\kappa (\delta^\dagger \xi)^2 + \text{H.c.} \quad \text{with} \quad \kappa = \sum_i \frac{\rho_i^2}{M_{\sigma_i}^2}. \tag{3.1}$$

We hence obtain the KNT model where the lightest one of the Majorana fermions N_i can be a stable dark matter particle. For simplicity, we will not repeat the details of the neutrino masses and the dark matter [32, 33, 40].

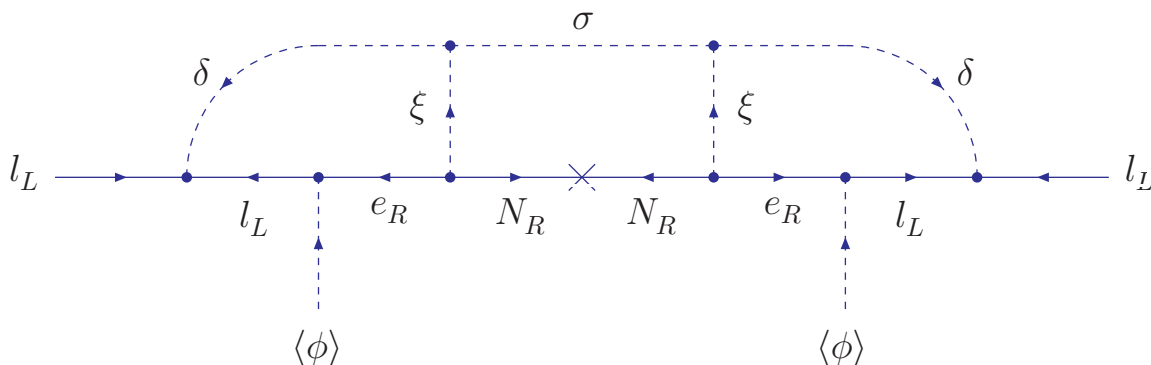


Figure 1. The three-loop diagram for neutrino mass generation.

4 Leptogenesis

Figure 2 shows the decays of the real singlet scalars σ_i as well as the decays of the singly charged scalar pairs (δ, δ^*) and (ξ, ξ^*) . According to the lepton number assignment (2.1), the real scalar decays can generate a lepton asymmetry stored in the charged scalars. Through the charged scalar decays, the SM leptons then can acquire a lepton asymmetry, which participates in the sphaleron processes so that it can be partially converted to a baryon asymmetry. We calculate the width in the real scalar decays at tree level,

$$\Gamma_{\sigma_i} = \Gamma(\sigma_i \rightarrow \delta^* + \xi) + \Gamma(\sigma_i \rightarrow \delta + \xi^*) = \frac{1}{8\pi} \frac{|\rho_i|^2}{M_{\sigma_i}}, \quad (4.1)$$

and the CP asymmetry at one-loop order,

$$\begin{aligned} \varepsilon_{\sigma_i} &= \frac{\Gamma(\sigma_i \rightarrow \delta^* + \xi) - \Gamma(\sigma_i \rightarrow \delta + \xi^*)}{\Gamma_{\sigma_i}} \\ &= \frac{1}{8\pi} \frac{\text{Im}(\rho_i^{*2} \rho_j^2)}{|\rho_i|^2} \frac{1}{M_{\sigma_j}^2 - M_{\sigma_i}^2} \\ &= \frac{\sin 2\alpha_{ji}}{8\pi} \frac{|\rho_j|^2}{M_{\sigma_j}^2 - M_{\sigma_i}^2} \quad \text{with} \quad \alpha_{ji} = \arg\left(\frac{\rho_j}{\rho_i}\right). \end{aligned} \quad (4.2)$$

As an example, we assume the real scalar σ_1 much lighter than the other one σ_2 . The final baryon asymmetry then should mainly come from the σ_1 decays. For a numerical estimation, we define

$$K = \frac{\Gamma_{\sigma_1}}{2H(T)} \Big|_{T=M_{\sigma_1}}, \quad (4.3)$$

where $H(T)$ is the Hubble constant,

$$H = \left(\frac{8\pi^3 g_*}{90}\right)^{\frac{1}{2}} \frac{T^2}{M_{\text{Pl}}}, \quad (4.4)$$

with g_* being the relativistic degrees of freedom during the leptogenesis epoch. In the strong washout region where

$$1 \ll K \lesssim 10^6, \quad (4.5)$$

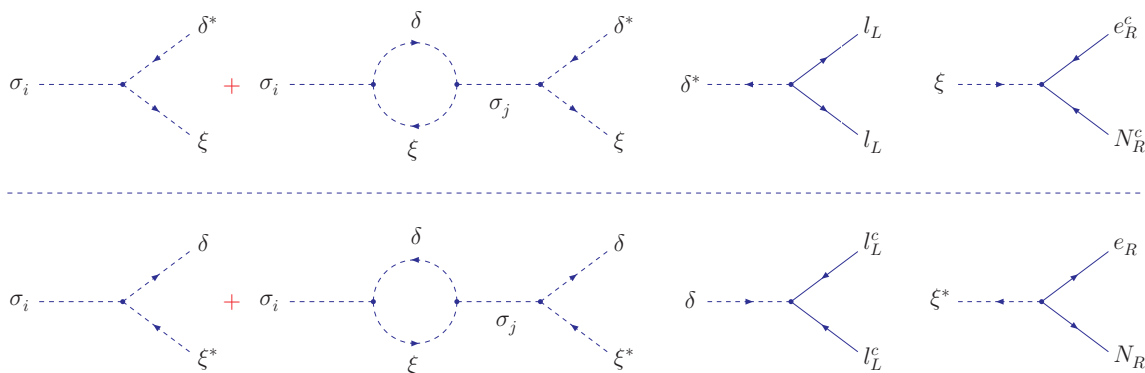


Figure 2. The real scalars σ_i decay into the charged scalars δ and ξ which subsequently decay into the SM leptons l_L and e_R as well as the fermion singlets N_R .

the final baryon asymmetry can be simply described by [41]

$$\eta_B = \frac{n_B}{s} \simeq -\frac{28}{79} \times \frac{\varepsilon_{\sigma_1}}{g_* K z_f}$$

with $z_f = \frac{M_{\sigma_1}}{T_f} \simeq 4.2(\ln K)^{0.6}$. (4.6)

Here n_B and s , respectively, are the baryon number density and the entropy density, while the factor $-\frac{28}{79}$ is the sphaleron lepton-to-baryon coefficient [42]. After fixing $g_* = 112.5$ (the SM fields plus two singly charged scalars as well as two singlet fermions) and inputting,

$$M_{\sigma_1} = |\rho_1| = 10^{14} \text{ GeV}, \quad M_{\sigma_2} = |\rho_2| = 10^{15} \text{ GeV}, \quad (4.7)$$

we read

$$K = 137, \quad z_f = 11, \quad T_f = 9 \times 10^{12} \text{ GeV}, \quad \varepsilon_{\sigma_1} = 5 \times 10^{-5} \left(\frac{\sin 2\alpha_{21}}{1.25 \times 10^{-3}} \right). \quad (4.8)$$

The baryon asymmetry then can arrive at an expected value,

$$\eta_B = 10^{-10} \left(\frac{\sin 2\alpha_{21}}{1.25 \times 10^{-3}} \right). \quad (4.9)$$

One may worry about the produced lepton asymmetry will be erased by some lepton-number-violating processes at low energies since figure 1 actually results in the dimension-5 Weinberg operators violating the lepton number by two units. Usually one estimates these processes will decouple at a very high temperature [43],

$$T = 10^{12} \text{ GeV} \left[\frac{0.04 \text{ eV}^2}{\text{Tr}(m_\nu^\dagger m_\nu)} \right], \quad (4.10)$$

with m_ν being the Majorana neutrino mass matrix. Therefore, no lepton asymmetry can survive above the temperature $T \sim 10^{12} \text{ GeV}$ if the neutrino masses arrive at an acceptable level. In our model, the effective dimension-5 operators are induced by integrating out the

scalars σ , δ and ξ as well as the fermions N_R . However, the fields δ , ξ and N_R are near the TeV scale, i.e. their masses are lighter than the crucial temperature $T \sim 10^{12}$ GeV. So, the estimation (4.10) is not consistent with the present scenario. Actually, in the above demonstration, the cubic terms among the scalars σ , δ and ξ are assumed to provide the unique source of the lepton number violation. After this lepton number violation is decoupled, no other lepton-number-violating processes can keep in equilibrium to wash out the produced lepton asymmetry.

If we take the lepton number assignment in the KNT model, the Majorana mass term of the singlet fermions N_R should be the unique source of the lepton number violation. In this case, the lepton asymmetry in the singly charged scalar ξ will get converted to a lepton asymmetry in the SM leptons e_R and an equal lepton asymmetry in the singlet fermions N_R . The $N_R - N_R^c$ oscillations will wash out the N_R asymmetry but will not affect the e_R asymmetry. So, the lepton asymmetry in the SM leptons e_R can survive for a successful leptogenesis. This SM lepton asymmetry definitely equals to that in the case with the lepton number assignment (2.1).

One can analyze the chemical potentials [42] to understand the leptogenesis in the present model. For this purpose, we denote $\mu_{q,d,u}$ for the chemical potentials of the SM quarks $q_L(3, 2, +\frac{1}{6})$, $d_R(3, 1, -\frac{1}{3})$ and $u_R(3, 1, +\frac{2}{3})$, while $\mu_{l,e,\phi,N,\delta,\xi}$ for the chemical potentials of the SM leptons and Higgs scalar l_L , e_R , ϕ as well as the non-SM fields N_R , δ , ξ . The singly charged scalars δ and ξ as well as the singlet fermions N_R are assumed near the TeV scale. Therefore, above the TeV scale, the SM Yukawa interactions yield [42],

$$\begin{aligned} -\mu_q + \mu_\phi + \mu_d &= 0, \\ -\mu_q - \mu_\phi + \mu_u &= 0, \\ -\mu_l + \mu_\phi + \mu_e &= 0, \end{aligned} \tag{4.11}$$

the sphalerons constrain [42],

$$3\mu_q + \mu_l = 0, \tag{4.12}$$

while the vanishing hypercharge in the universe require,

$$3 \left[\left(\frac{1}{6}\mu_q \times 2 - \frac{1}{3}\mu_d + \frac{2}{3}\mu_u \right) \times 3 + \left(-\frac{1}{2}\mu_l \times 2 - \mu_e \right) \right] + \left(\frac{1}{2}\mu_\phi \times 2 + \mu_\delta + \mu_\xi \right) \times 2 = 0. \tag{4.13}$$

Furthermore, from the non-SM Yukawa interactions and Majorana masses in eq. (2.3), we obtain,

$$\begin{aligned} \mu_\delta + 2\mu_l &= 0, \\ \mu_\xi + \mu_e + \mu_N &= 0, \\ -2\mu_N &= 0. \end{aligned} \tag{4.14}$$

Note in eqs. (4.11)–(4.14), we have identified the chemical potentials of the different-generation fermions because the Yukawa interactions establish an equilibrium between the different generations. By solving eqs. (4.11)–(4.14), we find

$$\begin{aligned} \mu_q &= -\frac{8}{3}\mu_e, & \mu_d &= -\frac{29}{3}\mu_e, & \mu_u &= \frac{13}{3}\mu_e, & \mu_l &= 8\mu_e, \\ \mu_\phi &= 7\mu_e, & \mu_\delta &= -16\mu_e, & \mu_\xi &= -\mu_e, & \mu_N &= 0. \end{aligned} \tag{4.15}$$

Clearly, the singlet fermions have a zero chemical potential because of their Majorana masses. However, the Majorana masses of the singlet fermions will not wash out the baryon/lepton asymmetry in the SM quarks/leptons as well as the lepton asymmetry in the singly charged scalars δ and ξ . Below the TeV scale, the non-relativistic δ and ξ have decayed so that the condition (4.13) for the zero hypercharge should be modified by [42],

$$3(\mu_q - \mu_d + 2\mu_u - \mu_l - \mu_e) + 2\mu_\phi = 0. \quad (4.16)$$

One then can solve eqs. (4.11), (4.12) and (4.16) to determine the chemical potentials as below [42],

$$\mu_q = -\frac{7}{9}\mu_e, \quad \mu_d = -\frac{19}{9}\mu_e, \quad \mu_u = \frac{5}{9}\mu_e, \quad \mu_l = \frac{7}{3}\mu_e, \quad \mu_\phi = \frac{4}{3}\mu_e. \quad (4.17)$$

The relation between the baryon and lepton numbers then should be [42]

$$B = \frac{28}{79}(B - L) \quad \text{with} \quad B = -\frac{28}{3}\mu_e, \quad L = \frac{51}{3}\mu_e. \quad (4.18)$$

5 Summary

In this paper we have simultaneously realized a high-scale leptogenesis and a low-scale neutrino mass generation. Specifically we have introduced two real singlet scalars to the KNT model which extended the SM by two singly charged scalars and two or more singlet fermions. The real scalar decays and then the charged scalar decays can produce a lepton asymmetry stored in the SM leptons. This lepton asymmetry can be partially converted to a baryon asymmetry by the sphaleron processes. At the low energy scales, we can integrate out the real scalars to derive the KNT model, where the neutrino masses are induced at three-loop level while the dark matter particle is given by the lightest singlet fermion. For the variant KNT models [36, 37], we can consider two real triplet or quintuplet scalars.

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