

Simplified R-symmetry breaking and low-scale gauge mediation

Jason L. Evans,^a Masahiro Ibe,^{a,b} Matthew Sudano^a and Tsutomu T. Yanagida^a

^a*Institute for the Physics and Mathematics of the Universe, University of Tokyo,
Chiba 277-8583, Japan*

^b*Institute for Cosmic Ray Research, University of Tokyo,
Chiba 277-8582, Japan*

E-mail: jason.evans@ipmu.jp, ibe@icrr.u-tokyo.ac.jp,
matthew.sudano@ipmu.jp, tsutomu.tyanagida@ipmu.jp

ABSTRACT: We argue that some of the difficulties in constructing realistic models of low-scale gauge mediation are artifacts of the narrow set of models that have been studied. In particular, much attention has been paid to the scenario in which the Goldstino superfield in an O’Raifeartaigh model is responsible for both supersymmetry breaking and R-symmetry breaking. In such models, the competing problems of generating sufficiently massive gauginos while preserving an acceptably light gravitino can be quite challenging. We show that by sharing the burdens of breaking supersymmetry and R-symmetry with a second field, these problems are easily solved even within the O’Raifeartaigh framework. We present explicit models realizing minimal gauge mediation with a gravitino mass in the eV range that are both calculable and falsifiable.

KEYWORDS: Supersymmetry Breaking, Beyond Standard Model

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1 Introduction

Much of the research on gauge mediation [1–8] has had little need for more than an effective description of the high-scale dynamics. With the introduction of General Gauge Mediation [9] and associated works,¹ the low-scale parameterization of this class of models is quite robust. Attempts at dynamically generating such effective descriptions, however, have had largely discouraging results. Without explicit models the plausibility of these scenarios can be called into question. And, of course, if evidence consistent with gauge mediation is found at the LHC, we will have ample motivation to go beyond a spurion analysis. It is in that spirit that we revisit the problem of constructing a fully consistent Minimal Gauge Mediation.

Since the relevant interactions in SUSY phenomenology are essentially fixed and have been thoroughly studied, SUSY model building has effectively been reduced to the problem of obtaining a spectrum within known bounds. Let’s discuss the players in turn.

- *Scalars* — Scalar masses are famously easy to generate. Indeed, one of the primary motivations for low-scale SUSY breaking is to keep a scalar (the Higgs) light. To get

¹For some extensions and restrictions see, for example [10–17].

sufficiently large scalar masses, we simply need to break supersymmetry at a sufficiently high scale.² In minimal gauge mediation, the scalars of the supersymmetric Standard Model first get masses at two-loops by coupling through gauge interactions to messenger fields. These masses are schematically given by

$$m_0^2 \sim \left(\frac{g^2}{16\pi}\right)^2 \left|\frac{F}{M}\right|^2 + \mathcal{O}(|F^4/M^6|), \quad (1.1)$$

where g is a Standard Model gauge coupling and F gives the splitting of the messenger mass from its supersymmetric value, M .

Applying the experimental lower bounds on sparticle masses, we learn that $|F/M| \gtrsim 10-100$ TeV. This is not strictly sufficient, however, because there are also constraints on relative magnitudes of sfermion masses from flavor changing neutral current data. The flavor universality of gauge interactions gives adequate flavor degeneracy in gauge mediation to evade these constraints. One must be mindful, however, of gravity-mediated effects that can reintroduce a flavor problem if the SUSY breaking scale is too high.

- *Gravitino* — In gauge mediation, though gravitational effects are otherwise decoupled, the gravitino plays a prominent role. Since its mass is set by the reduced Planck scale, M_{PL} , rather than the messenger scale,

$$m_{3/2} \sim \frac{F}{M_{PL}} \quad (1.2)$$

it is generically the LSP and thus, assuming R-parity, it is stable. Its stability affords it a conspicuous role in cosmology. It is automatically a dark matter candidate, and interestingly, the thermal relic abundance for $m_{3/2} \simeq 100$ eV is consistent with the observed dark matter density. Unfortunately, however, such a light gravitino is not cold dark matter but corresponds to hot dark matter and conflicts with structure formation data [20]. The thermal relic density of the heavier gravitino which can be cold dark matter is, on the other hand, much higher than the observed density of dark matter. If we allow an additional source of dark matter, however, a very light gravitino, $m_{3/2} \lesssim 16$ eV, evades all constraints [20]. Lowering the scale of SUSY breaking to this degree, however, is not easy. We will discuss model building implications of such a light gravitino in section 2.

- *Gauginos* — In minimal gauge mediation, the gauginos present no difficulties as one finds schematically

$$m_{1/2} \sim m_0 \sim \frac{g^2}{16\pi} \frac{F}{M} + \mathcal{O}(|F^2/M^3|). \quad (1.3)$$

Realizing such gaugino masses, however, is a notorious problem in explicit models of gauge mediation. The problem begins with the R-symmetry conflict: An unbroken

²The Higgs, of course, is a special case. We won't discuss the Higgs sector in detail in this work, but the models we will discuss can be extended to include a μ_H and B_μ generating sector as in [18, 19].

R-symmetry, forbids gaugino masses; without the presence of such a symmetry, however, SUSY breaking is somewhat difficult [21]. Of course, we can have it both ways. In theories with a spontaneously broken R-symmetry, SUSY breaking is generic and gaugino masses are generated, but two problems have been encountered. First, breaking the R-symmetry is not trivial in practice [22]. Second, even when the symmetry is broken, many have found that the gaugino masses vanish to leading order in SUSY breaking [23–25]. We will discuss these issues further in section 3.

- *R-axion* — As for any global symmetry, the spontaneous breaking of an R-symmetry results in a massless particle. It is, however, assumed that this symmetry is not present in a gravitational theory. One may further introduce explicit and small breaking of the R-symmetry in the low-energy effective theory. This is tantamount to accepting the metastability of our vacuum [25–27]. By the explicit R-symmetry breaking effects in the supergravity, this axion can be made heavy enough in some models [28], but its existence remains an imminently falsifiable prediction in many scenarios including those to be discussed here. In section 5 we will elaborate on these points.

In the remainder of this paper we will present a framework in which each of the above challenges is met. The low-energy effective action will be minimal gauge mediation after integrating out a SUSY-breaking sector along the lines of cascade gauge mediation (to be reviewed in section 2). The key to addressing the gravitino problems, and the novelty in our approach, is that our messenger masses are generated at one-loop, so we can have a truly low-scale gauge mediation and a light gravitino. The classic problems with breaking R-symmetry and generating gaugino masses simply aren't present in this framework. As we will discuss in detail in the section 3, R-symmetry breaking is loop-induced and not strictly along the Goldstino pseudomodulus direction, so the analyses of [22, 25] do not apply. This method of SUSY and R-symmetry breaking is applied to an explicit class of models in section 4, where we discuss a dynamical embedding of the models. This is needed to avoid a Landau pole problem. In section 5 we show that our R-axion decay constant is bounded on both sides and that future experiments should fully explore the currently allowed region. The composition of the dark matter is not predicted. Prospective candidates are discussed in section 6 with our concluding remarks. In appendices we show that our mechanism of R-symmetry breaking can be sourced by D-term SUSY breaking, and we prove that in the F-term breaking case, we must have a field with R-charge other than 0 or 2.

2 Attempts at models with a light gravitino

The fundamental SUSY breaking scale can be expressed in terms of the gravitino mass as follows.

$$\sqrt{F} \simeq (\sqrt{3}m_{3/2}M_{PL})^{1/2} \simeq 65 \text{ TeV} \times \left(\frac{m_{3/2}}{1 \text{ eV}}\right)^{1/2}. \quad (2.1)$$

In minimal gauge mediation, the soft supersymmetry breaking masses of the superparticles in the SSM are roughly given by,

$$m_{\text{soft}} \simeq 10^{-2} \frac{F_S}{M} \gtrsim \mathcal{O}(10^{2-3}) \text{ GeV}. \quad (2.2)$$

Here, M is the messenger scale and F_S is the mass splitting of the messenger multiplets. These mass scales satisfy $F_S < M^2$ and $F_S < F$, where the first condition ensures that our messengers are non-tachyonic and the second one says that the mass splitting is smaller than the total size of supersymmetry breaking. By combining these conditions with (2.1) and (2.2), we find that having an eV scale gravitino while having sufficiently heavy superpartner requires

$$M \sim \sqrt{F_S} \sim \sqrt{F} \sim \mathcal{O}(10 - 100) \text{ TeV}. \quad (2.3)$$

For the SUSY breaking mass splitting in the messenger sector to be comparable to the fundamental SUSY breaking scale, i.e. $F_S/F = \mathcal{O}(1)$, we need to have the fundamental SUSY breaking sector and the messenger sector couple via interactions that are not too suppressed. As we briefly discuss below, this fact makes building a model with a very light gravitino rather difficult.

Tree-level interactions. The simplest idea for realizing models with $F_S \sim F$ is to connect the messenger and the SUSY breaking sectors by tree-level interactions in the superpotential with coupling constants of order one. For example, if we require that the SUSY breaking vacuum is the absolute minimum of the model, the model can be realized by an O’Raifeartaigh model with the superpotential,

$$W = \mu^2 S + (m_{ij} + \lambda_{ij} S) \bar{\psi}_i \psi_j. \quad (2.4)$$

Here, S represents a SUSY breaking field, $\psi, \bar{\psi}$ are messenger fields, μ and m_{ij} are mass parameters, and the λ_{ij} are coupling constants. In this class of models, the SUSY breaking vacuum is the absolute minimum when the model possesses an R-symmetry under which S has charge 2 for $\det m \neq 0$ [25] and $\lambda m^{-1} \lambda = 0$ [29].³

In this class of models [24] (and a broader class, as shown in [25]), the leading contribution to the gaugino masses appears only at order F_S^3 (first calculated in [24]). This is opposed to the naive expectation in (2.2),⁴

$$m_{\text{gaugino}} \sim \frac{\alpha}{4\pi} \frac{F_S}{M} \left| \frac{F_S}{M^2} \right|^2. \quad (2.5)$$

For the parameters satisfying (2.3), the factor $|F_S/M^2|^2$ may appear to be of order unity. Detailed numerical analysis, however, has shown that the predicted gaugino masses are rather suppressed and have been almost excluded by Tevatron constraints on the neutralino/chargino masses for $m_{3/2} \lesssim 16 \text{ eV}$ [29–31].

Larger gaugino masses are possible in models based on tree-level interactions by allowing an instability. For example, naively we expect gaugino masses like those in (2.2) are generated by the superpotential

$$W = \mu^2 S + (m + \lambda S) \bar{\psi} \psi, \quad (2.6)$$

³Notice that the R-symmetry is also a necessary condition for the models not to have SUSY vacua when the superpotential is generic under the symmetries [21]. If the models are restricted to have renormalizable interactions, the necessary condition can be relaxed to a discrete R-symmetry.

⁴We are assuming that the R-symmetry is spontaneously broken by the expectation value of the SUSY breaking field, i.e. $\langle S \rangle = O(M)$, which is the optimal choice for generating large gaugino masses.

which breaks R-symmetry explicitly. The model has a SUSY preserving vacuum at $\langle \bar{\psi}\psi \rangle = -\mu^2/\lambda$. In this class of models, to ensure sufficiently long lifetime of the SUSY breaking vacuum one must increase the messenger mass m , which suppresses superparticle masses for a given gravitino mass. For $m_{3/2} \lesssim 16$ eV, the numerical analysis has shown that the upper bound on the gluino/squark masses is about 1 TeV [32]. Besides, this class of models requires some justification for the SUSY breaking vacuum to be chosen in the evolution of the universe, regardless of its higher energy compared with the energies of the nearby supersymmetric vacua.

Direct/indirect gauge mediation. Another approach that may give $F_S \sim F$ is to assume that the messenger fields are charged under the gauge symmetry which is responsible for dynamical SUSY breaking (DSB). Such models are often called direct or semi-direct gauge mediation models. In direct mediation models, the messengers play a role in SUSY breaking dynamics, while they do not in semi-direct mediation models. (A precise definition of direct gauge mediation is given, for example, in [33, 34].) In these classes of models, since messengers strongly couple to the SUSY breaking fields, the size of the messenger mass splittings are expected to be comparable to the fundamental SUSY breaking scale.

In the direct mediation models, however, the need for a large flavor symmetry in the DSB sector usually implies that the DSB gauge group is rather large. Thus, to avoid Landau poles of the Standard Model gauge interactions below the GUT scale, both the messenger and SUSY breaking scales are pushed up, which precludes the possibility of having a light gravitino.⁵

The messenger and SUSY breaking scales can be much lower in semi-direct gauge mediation models [35–39] (see also [40, 41] for earlier attempts), where the gauge group for the DSB can be smaller. In this class of models, however, the leading contribution to the gaugino mass as in (2.2) is again vanishing (see [42–44] for details). Therefore, both direct and semi-direct gauge mediation models have difficulty producing a gravitino mass in the eV range.

Cascade gauge mediation. In [46], a class of models termed cascade gauge mediation was proposed with the following features.

- Gravitino mass in the eV range
- Sufficiently large gaugino masses
- A SUSY-breaking vacuum with a long enough lifetime
- Perturbativity up to the GUT scale

Since our construction will mirror that of cascade gauge mediation in some ways, we will describe it in some detail.

The mechanism employs some of the tools proposed in previous gauge mediation models [47–49]. Namely two SUSY-breaking fields are introduced, one of which is an ordinary

⁵The Landau pole problems may be ameliorated if the messenger fields receive large positive anomalous dimensions under the renormalization group evolution between the GUT and the messenger scales [35–37].

tree-level SUSY-breaking field. The other field is the one that couples to the messengers in the superpotential and it only breaks SUSY and only couples to the “fundamental” SUSY-breaking field through radiative corrections to the Kähler potential.

The simplest such model is described by the following Kähler potential and superpotential.

$$\begin{aligned} K &= |Z|^2 + |S|^2 + \frac{c}{\Lambda^2}|Z|^2|S|^2 + \dots, \\ W &= \mu^2 Z + kS\tilde{\Phi}\Phi + \frac{h}{3}S^3, \end{aligned} \tag{2.7}$$

where μ and Λ are dimensionful parameters, and k, h are dimensionless coupling constants.⁶ Here, Z is the fundamental SUSY-breaking field, while S now represents the secondary SUSY breaking field. Note that the messenger sector possesses a supersymmetric vacuum in the limit $c \rightarrow 0$.

Once the primary sector breaks SUSY, i.e. $|F_Z| = \mu^2$, the linking term in the Kähler potential induces a SUSY breaking soft mass for S , and the scalar potential of the secondary SUSY-breaking field is given by,

$$V(S) \simeq m_S^2 |S|^2 + |hS^2|^2, \quad m_S^2 = -c \frac{|F_Z|^2}{\Lambda^2}. \tag{2.8}$$

For $m_S^2 < 0$, the secondary SUSY-breaking field obtains a non-vanishing expectation value,⁷

$$\langle S \rangle \simeq \frac{|m_S|}{\sqrt{2}h}. \tag{2.9}$$

which breaks SUSY by,

$$F_S = h \langle S \rangle^{*2} \simeq \frac{|m_S^2|}{2h}. \tag{2.10}$$

Thus, in this model, secondary SUSY breaking is initiated by spontaneous R-symmetry breaking which is, in turn, triggered by fundamental SUSY breaking.

Since the structure of the messenger and the secondary fields coupling is nothing but that of minimal gauge mediation, the gaugino masses are given by

$$m_a = \frac{\alpha_a F_S}{4\pi \langle S \rangle} = \frac{\alpha_a}{4\pi} h \langle S \rangle \simeq \frac{\alpha_a |m_S|}{4\pi \sqrt{2}}. \tag{2.11}$$

Thus, for models with $m_S \sim \sqrt{F_Z}$ which corresponds to $\Lambda \sim \sqrt{F_Z}$ and $c = O(1)$, the conditions in (2.3) for a very light gravitino are satisfied while having heavy gauginos.⁸

⁶The phases of h and k can be rotated at will by field redefinitions, so we will not keep track of them in what follows.

⁷For generic models of cascade gauge mediation, the secondary sector breaks supersymmetry even for $m_S^2 > 0$ [46].

⁸Models with cascade gauge mediation break supersymmetry and R-symmetry via the higher-dimensional Kähler potential term in (2.7), which connects the primary and secondary supersymmetry breaking sectors. In [25] a canonical Kähler potential is assumed for the SUSY breaking field in showing that their gauginos cannot obtain leading order masses unless the vacuum is metastable, so the argument does not apply to this class of models.

To realize models with $\Lambda \sim \sqrt{F_Z}$ and $c = O(1)$ is, however, not an easy task. In previous cascade gauge mediation models [47–49], for example, the connecting term in (2.7) is generated at three loops, which leads to $\Lambda \gg \sqrt{F_Z}$ and/or $|c| \ll 1$.

In the model given in [46], the connection term is also generated at higher-loop level. In that model, however, all the interactions are expected to be very strong, so that the conditions in (2.3) are realized, and hence, the model allows the gravitino mass to be in the eV range. The drawback of the model in [46] is that the model cannot predict the sign of the sfermion masses squared due to the non-calculable contribution of the strong interactions.

Therefore, the framework of cascade gauge mediation is a promising way for realizing a gravitino mass in the eV range. However, it is desirable to construct models where $m_{\tilde{g}}^2$ is generated at one-loop, so that the conditions in (2.3) can be satisfied in a perturbative framework.

3 Non-Goldstino R-symmetry breaking at one-loop

In this section, we discuss the mechanism of R-symmetry breaking that we utilize in our models.

In [22], the problem of R-symmetry breaking was considered in the set of O’Raifeartaigh models defined by the superpotential

$$W = fX + \frac{1}{2}(M^{ij} + XN^{ij})\phi_i\phi_j + \dots, \quad \langle \phi_i \rangle = 0. \quad (3.1)$$

It was shown that one-loop spontaneous R-symmetry breaking is only possible when some fields are assigned R-charge other than 0, 2. The proof made use of an expression for the one-loop mass of the charge-two pseudomodulus, X , in terms of a positive semi-definite and a negative semi-definite contribution. It was shown that the latter contribution vanishes if every field can be assigned an R-charge of 0 or 2. This illuminated the observed absence of R-symmetry breaking in ungauged O’Raifeartaigh models.

One limitation of this analysis is that only models with a single pseudo-modulus (the superpartner of the Goldstino) are allowed. The important difference in our approach is that we allow a second pseudo-modulus and look for R-symmetry breaking in a direction other than the Goldstino pseudo-modulus direction. Although these models are not included in (3.1) we still find that a field with R-charge other than 0 or 2 is required (see appendix A).

R-symmetry breaking in O’Raifeartaigh models. Here, we discuss models with calculable R-symmetry breaking that is radiatively induced by SUSY breaking. We restrict ourselves to models where the R-charge of our non-Goldstino pseudomodulus is undetermined. We will also restrict ourselves to models with a global SUSY breaking minimum. A broad class⁹ of models with these features is

$$W = Z(\mu^2 + g_{ij}B_iB_j) + M_{ij}B_iC_j + M'_{ij}B_iD_j + \lambda_{ij}SD_iE_j + M''_{ij}X_iY_j. \quad (3.2)$$

⁹This class has been chosen to have a strictly negative $m_{\tilde{g}}^2$. More general models with positive contributions that are subdominant to the the negative ones are not difficult to construct. Adding interactions of the form, SB_iB_j , can generate a tachyonic mass for S , however, they tend to require fine tuning.

where the X_i and Y_i may be any fields other than S , Z , or the C_i . In any model of this form, S will have a tachyonic mass at one loop. This can be seen by tracing the effects of SUSY breaking. S is chosen to be massless at tree-level, so the one-loop mass must vanish in the limit of unbroken supersymmetry by the perturbative non-renormalization of the superpotential. When SUSY is broken, the masses of the bosons are split, but the fermion masses stay the same. This means that at one loop, the only negative contributions to m_S^2 that are affected by SUSY breaking are the boson loops coming from the trilinear interactions,

$$\mathcal{L} = M'_{ij} B_j \lambda_{ik}^* S^* E_k^* + h.c. \tag{3.3}$$

In the above model, the only fields that get split masses at tree level are the B_i . Since these fields only interact with S through trilinears, only the negative contribution to m_S^2 is enhanced by SUSY breaking. Naturally, m_S^2 is negative.

Another important feature of this class of models is that the SUSY breaking minimum is a global minimum as long as $\det M \neq 0$. In this case, the only solution to

$$-F_{C_i}^* = M_{ij} B_j = 0 \tag{3.4}$$

is $B_i = 0$. If $B_i = 0$ for all i then $|F_Z| = \mu^2$ at the global minimum of the potential and SUSY is broken.¹⁰

Now that we have found a class of models with $m_S^2 < 0$, we will consider the simplest case,

$$W = Z(\mu^2 - gB^2) + m(BC + BD) + \lambda SDE + m'(EF + GD). \tag{3.5}$$

We have kept two mass scales m and m' for later use. This model has an R-symmetry (under which $R[S] = -R[E] = R[F] - 2$ is undetermined), and a Z_2 symmetry under which all the superfields are odd except for Z and S . Under these symmetries, the terms

$$GC, \quad SCE, \tag{3.6}$$

are allowed. Including them would introduce unwanted supersymmetric vacua. Those problematic terms, however, can be naturally suppressed by assuming that there is an additional U(1) symmetry which has been spontaneously broken at around the Planck scale only by a positively charged suprior field ϕ_+ (charge +1). By assuming that G and E have charge +1, D and F have charge -1, and the other fields have charge 0, the terms in (3.6) are suppressed under the broken symmetries with the help of the holomorphic nature of the superpotential, while the terms appearing in (3.5) are not suppressed as long as $\langle \phi_+ \rangle = O(M_{PL})$. In this sense, the model in (3.5) is generic under the (broken) symmetries.

Of course, the term $hS^3/3$ is also allowed. We will include this term when we consider cascade gauge mediation. The cubic term of S has no effect on the one-loop mass, but it fixes $R[S] = 2/3$, making the vev of this field R-symmetry breaking.

The one-loop squared mass of S in this model is quite complicated but takes the form

$$m_S^2 = \frac{g^2 \lambda^2}{16\pi^2} \frac{\mu^4}{m^2} g(x, y), \tag{3.7}$$

¹⁰Depending on the mass parameters, $F_Z = \mu^2$ may not be the global minimum. However, the global minimum of these models is always a SUSY breaking minimum.

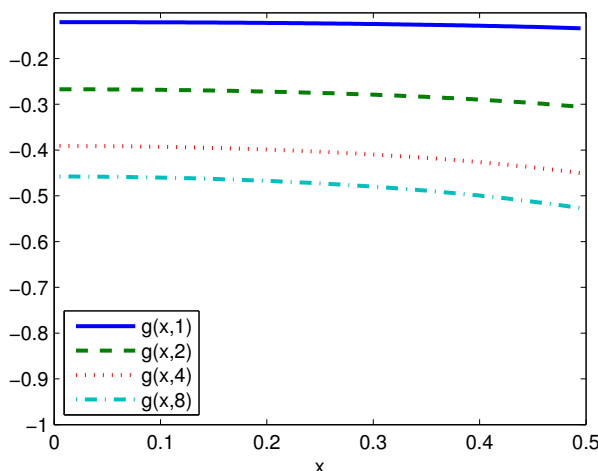


Figure 1. The function $g(x, y)$ ($x = g\mu^2/m^2, y = m'/m$) given in (3.7). The figure shows that the mass squared of S is always negative in these models, which leads to spontaneous R-symmetry breaking. $g(x, y)$ is cut off at $x = 1/2$ because of the emergence of a tachyonic mass.

where $x = \mu^2/m^2$ and $y = m/m'$.¹¹ Since $g(x, y)$ is only weakly dependent on x , we only need its leading order contribution

$$g(x, y) \simeq g(0, y) = \frac{12y^6(1+2y^2)}{(1+4y^4)^{5/2}} \left[\ln \left(\frac{1+2y^2+\sqrt{1+4y^4}}{1+2y^2-\sqrt{1+4y^4}} \right) - \frac{\sqrt{1+4y^4}(1+12y^2+4y^4)}{6y^2(1+2y^2)} \right]. \quad (3.8)$$

To supplement our approximation, we show the x dependence of $g(x, y)$ for a few values of y in figure 1. From the figure it is apparent that $g(x, y)$ is negative for all values of x, y and is typically in the range $g(x, y) \simeq -(0.2 - 0.5)$. Clearly we find that R symmetry is successfully broken at one loop and

$$\langle S \rangle \simeq \frac{g\lambda}{4\pi h} \frac{\mu^2}{m}. \quad (3.9)$$

4 Gravitino mass in the eV range

Now let us apply the models in section 3 to cascade gauge mediation, and examine whether the models allow a gravitino mass in the eV range. For that purpose, we add the cubic term of S and messenger coupling to the model in (3.5);

$$W = Z(\mu^2 - gB^2) + m(BC + BD) + \lambda SDE + \tilde{m}(EF + GD) + \frac{h}{3}S^3 + kS\psi\bar{\psi}. \quad (4.1)$$

By integrating out everything except for S and the messengers, this model is reduced to cascade gauge mediation,

$$W = \frac{h}{3}S^3 + kS\psi\bar{\psi}, \quad (4.2)$$

¹¹In terms of the effective Kähler potential in (2.7) the negative squared mass corresponds to $c/\Lambda^2 = -g^2\lambda^2g(x, y)/(16\pi^2 m^2)$.

and

$$V_{\text{soft}} \simeq m_S^2 |S|^2, \tag{4.3}$$

where $m_S^2 < 0$ is given in (3.7).

In order to have the largest possible gaugino masses for $\mu \lesssim 260$ TeV (i.e. $m_{3/2} < 16$ eV, see (2.1)), the coupling constants g and λ should be as large as possible and m should be as small as possible. From our numerical analysis, however, we found that to avoid tachyonic modes, we must have

$$g\mu^2 \lesssim 0.5 m^2, \tag{4.4}$$

for $k = \mathcal{O}(1)$.

With this constraint, the soft mass of S , is bounded from above,

$$|m_S| \simeq \left(\frac{g^2 \lambda^2 \mu^4}{16\pi^2 m^2} |g(x, y)| \right)^{1/2} \lesssim \frac{g^{1/2} \lambda}{8\pi} \mu, \tag{4.5}$$

where we have used $g(x, y) \simeq -0.5$ in the final expression. In cascade gauge mediation, the bound on m_S^2 results in a bound on the gaugino masses. For example, we obtain,

$$m_{\text{gluino}} \lesssim 50 \text{ GeV} \times N_{\text{mess}} g^{1/2} \lambda \left(\frac{\mu}{260 \text{ TeV}} \right), \tag{4.6}$$

where $N_{\text{mess}} \leq 5$ is the number of messengers (see (2.11)).¹² Therefore, the gluino mass does not satisfy the current lower limit placed by the ATLAS collaboration [50]¹³ $m_{\text{gluino}} \gtrsim 700$ GeV as long as $g^{1/2} \lambda \lesssim 1$ even for $N_{\text{mess}} = 5$.

Notice that we cannot freely take large values of g and λ . For example, if we require that both g and λ are perturbative up to some high energy scale (such as the GUT scale), they are expected to be at most below 1 or so.¹⁴ Therefore, to have an acceptably heavy gluino, we need to allow g or λ to blow up below the GUT scale, which in turn requires some other description of the model, i.e. a UV completion.¹⁵

Fortunately, we find that the model in (4.1) can be embedded into a dynamical SUSY breaking model based on a vector-like SU(2) gauge theory developed in [53, 54]. There, the coupling constant g in the effective description in (4.1) of the dynamical SUSY breaking model can be rather large, and the predicted gluino mass can be above the current experimental limit. In the rest of this section, we discuss how the above model in (4.1) is embedded in this dynamical SUSY breaking model.

¹²Here, we have approximated that the pole mass of the gluino is roughly μ enhanced by 25% from the value of m_3 at the weak scale. For the model with a large hierarchy between the gaugino masses and sfermion masses, the pole mass enhancement can be slightly larger. Even with such an enhancement, it is unlikely that the gluino mass exceeds the lower mass bound at the LHC experiment.

¹³See also the result from the CMS collaboration [51].

¹⁴By assuming that h is much smaller than λ and g , the renormalization group equations are solved by

$$\lambda^2(\mu_R) \simeq \frac{\lambda^2(M_{\text{GUT}})}{1 - \frac{3\lambda^2(M_{\text{GUT}})}{8\pi^2} \ln(\mu_R/M_{\text{GUT}})}, \quad g^2(\mu_R) \simeq \frac{g^2(M_{\text{GUT}})}{1 - \frac{10g^2(M_{\text{GUT}})}{8\pi^2} \ln(\mu_R/M_{\text{GUT}})}, \tag{4.7}$$

which give $\lambda(10^5 \text{ GeV}) \simeq 1$ and $g(10^5 \text{ GeV}) \simeq 0.6$ for $\lambda(M_{\text{GUT}}) = g(M_{\text{GUT}}) \simeq 4\pi$.

¹⁵Alternate solutions for such Landau pole problems have been proposed. See, for example, [52].

4.1 Embedding in dynamical SUSY breaking model

Now let us begin with a brief review of the dynamical SUSY breaking model based on SU(2) gauge theory [53, 54]. The model consists of four fundamentals $Q_i (i = 1 \cdots 4)$ and six singlets, $Z_{ij} = -Z_{ji} (i, j = 1 \cdots 4)$. The Q 's and Z 's couple in the classical superpotential,

$$\begin{aligned}
 W &= g_{ij}^{kl} Z_{ij} Q_k Q_l, \quad (i < j), \\
 &= g_0 Z_0 (QQ)_0 + g' Z_a (QQ)_a, \quad (a = 1 \cdots 5),
 \end{aligned}
 \tag{4.8}$$

where the g 's are coupling constants. The maximal global symmetry this model may have is $SU(4) \simeq SO(6)$ symmetry which requires $g_{ij}^{kl} = g$. For simplicity, in the second expression we have rearranged the fields and coupling constants assuming there exist an $SO(5) \subset SO(6)$ global symmetry. The subscript $a = 1 \cdots 5$ corresponds to a fundamental representation of $SO(5)$. In this model, SUSY is broken dynamically due to the tension between the F -term conditions of Z 's and the quantum modified constraint [55] $\text{Pf}(Q_i Q_j) = \Lambda_{\text{dyn}}^2$.

Below the dynamical scale Λ_{dyn} , the light degrees of freedom are the composite operators $M_A = (QQ)_A$ and $Z_A, (A = 0, 1 \cdots 5)$. In terms of the composite operators, the quantum moduli constraint is given by,

$$M_A M_A = \Lambda_{\text{dyn}}^2. \tag{4.9}$$

Here, we have assumed that the effective composite operators M_A are canonically normalized.

By assuming that g_0 's are perturbative and $g_0 < g'$, we may parametrize the deformed moduli space by,

$$M_0 = \sqrt{\Lambda_{\text{dyn}}^2 - M_a M_a}. \tag{4.10}$$

By plugging it into the effective superpotential in (4.8), we obtain the effective O'Raifeartaigh model,

$$W_{\text{eff}} \simeq g_0 \Lambda_{\text{dyn}}^2 Z_0 - \frac{g_0}{2} Z_0 M_a M_a + g' \Lambda_{\text{dyn}} Z_a M_a + O(M_a^4). \tag{4.11}$$

In this effective description, SUSY is broken by,

$$F_{Z_0} = g_0 \Lambda_{\text{dyn}}^2. \tag{4.12}$$

Now we can relate the dynamical SUSY breaking model to the model discussed in the previous section by matching the fields and parameters;¹⁶

$$\begin{aligned}
 Z_0 &\rightarrow Z, & M_a &\rightarrow B_a, & Z_a &\rightarrow D_a, \\
 g_0 \Lambda_{\text{dyn}}^2 &\rightarrow \mu^2, & g' \Lambda_{\text{dyn}} &\rightarrow m, & g_0 &\rightarrow 2g.
 \end{aligned}
 \tag{4.13}$$

With this dictionary, the above effective O'Raifeartaigh model is rewritten as

$$W_{\text{eff}} \simeq Z (\mu^2 - g B_a B_a) + m B_a D_a, \tag{4.14}$$

¹⁶In these matching conditions, we have ambiguities of $O(1)$ due to non-perturbative effects.

where we have neglected the higher dimension operators. Finally, let us introduce four SO(5)-vector superfields, C_a, E_a, F_a and G_a , a singlet field S and pairs of messengers.

$$W_{\text{eff}} \simeq Z(\mu^2 - gB_a^2) + mB_a(D_a + C_a) + \tilde{m}(F_aE_a + G_aD_a) + \lambda SD_aE_a + \frac{h}{3}S^3 + kS\bar{\psi}\psi, \quad (4.15)$$

where SO(5) indices are contracted. In this way, we can embed the previous R-symmetry breaking model into a dynamical SUSY breaking model.

The important feature of this embedding is that the superfields S, D_a, E_a are not the composite but elementary fields. Thus, the trilinear couplings SDE and S^3 are not suppressed in the UV theory. That is, in the UV theory, the model in (4.15) is realized by,

$$W_{\text{tree}} \simeq g_0Z_0(QQ)_0 + g'D_a(QQ)_a + g'C_a(QQ)_a + \tilde{m}(F_aE_a + G_aD_a) + \lambda SD_aE_a + \frac{h}{3}S^3 + kS\bar{\psi}\psi, \quad (4.16)$$

which shows that λ, h and k are unsuppressed.¹⁷

The advantage of this embedding is that the effective coupling g , which is related to g_0 in the UV theory, is not directly constrained by the Landau pole problem. In particular, the coupling g (or g_0) is expected to become very large around the dynamical scale Λ_{dym} due to the renormalization group effects of the SU(2) gauge interactions, which enhance the coupling g (or g_0) in the lower energy. Of course, we should preserve perturbativity, $\frac{g}{4\pi} < 1$, to suppress corrections to (3.7), but we are not nearly as constrained as we were without the dynamical embedding. Besides, since we have SO(5) vectors, the one-loop contribution to $m_{\tilde{g}}^2$ is enhanced by a factor of 5. With these two effects, the gluino mass upper bound is enhanced to

$$m_{\text{gluino}} \lesssim 2 \text{ TeV} \times \lambda \left(\frac{N_{\text{mess}}}{5} \right) \left(\frac{g}{4\pi} \right)^{1/2} \left(\frac{\mu}{260 \text{ TeV}} \right). \quad (4.17)$$

We have put in 4π as the reference value for g . We should remain somewhat below this value to take our analysis seriously quantitatively, but we have no reason to expect an R-symmetry-restoring phase transition even as g becomes strong. So, while 2TeV may be an optimistic upper bound on the gluino mass, and non-perturbativity prevents us from determining the precise upper bound, we can certainly obtain an experimentally consistent spectrum.¹⁸ Therefore, by considering the dynamical SUSY breaking model behind the R-breaking model, we find that the models with O(eV) gravitino mass can be constructed with a heavy enough gluino, a stable vacuum, and perturbative unification. Furthermore, the predicted upper bound is well within the reach of the LHC experiment, and hence, the class of models with the gravitino mass in the eV range based on R-symmetry breaking at one loop will be ruled out or supported by data in near future.

¹⁷By adding $\lambda'S'D_aJ_a + m_JJ_aK_a + \alpha'S'^3 + k'S'H\bar{H}$ to the above superpotential, a μ_H/B_μ term can be generated. If $\lambda' \ll \lambda$ and/or $m_J \gg m$, μ_H/B_μ will have the same size as the soft masses.

¹⁸Here, again, we have assumed that the pole mass of the gluino is roughly enhanced by 25% compared with the value of m_3 at the weak scale.

5 R-axion properties

Before concluding this paper, let us discuss the important properties of the R-axion in this class of models. The R-axion is the pseudo-Nambu-Goldstone boson resulting from spontaneous R-symmetry breaking [21]. The R-axion would be a true Nambu-Goldstone field if the R-symmetry were exact, but this is not the case. It is at least explicitly broken by the cosmological constant in supergravity, which yields a mass for the R-axion [28].

To see how the axion mass is generated, let us first study a simple example. Consider the superpotential terms

$$W \supset \mu^2 Z + m_{3/2} M_{PL}^2, \quad (5.1)$$

and assume that the R-charge-two field, Z , gets an expectation value providing the sole source of R-symmetry breaking in the limit $m_{3/2} \rightarrow 0$.

$$Z = \langle Z \rangle e^{2ia/f_R}, \quad f_R = 2\sqrt{2} \langle Z \rangle. \quad (5.2)$$

This defines the R-axion, a . We can then compute the potential and see that the explicit R-symmetry breaking constant term provides a mass for a .

$$V_{\text{R-breaking}} = -2m_{3/2}\mu^2 Z + h.c. \quad (5.3)$$

Using $\mu^2 \simeq \sqrt{3}m_{3/2}M_{PL}$, we find

$$m_R^2 \simeq \frac{8}{\sqrt{2}} \frac{m_{3/2}\mu^2}{f_a} \simeq 8\sqrt{\frac{3}{2}} \frac{M_{PL}}{f_R} m_{3/2}^2. \quad (5.4)$$

In the models discussed in the previous section, the mechanism is somewhat different. There the source of spontaneous R-symmetry breaking is the vev of S , which couples to other fields through dimensionless interactions at tree level (see (4.1)). In this case, the explicit R-symmetry breaking term analogous to the one in (5.3) is induced from the higher-dimensional operators in the Kähler potential, which can be expressed as the anomaly-mediated A-term [57, 58],

$$\begin{aligned} \mathcal{L} &= \frac{h}{3} A_h S^3 + h.c. \\ A_h &= \dot{h} \gamma_S \times m_{3/2}, \\ \gamma_S &= 2h^2 + 5N_{\text{mess}} k^2 + 5\lambda^2. \end{aligned} \quad (5.5)$$

The first contribution to the anomalous dimension of S , γ_S , comes from the S^3 interactions, the second one is from the $S\bar{\psi}\psi$ interactions, and the third one from the contributions of $SD^a E_a$ interactions. The induced explicit R-breaking term is then given by,

$$V_{\text{R-breaking}} \simeq -\frac{1}{16\pi^2} \frac{h}{3} (2h^2 + 5k^2 N_{\text{mess}} + 5\lambda^2) m_{3/2} S^3 + h.c. \quad (5.6)$$

Thus, the R-axion defined by,

$$\begin{aligned} S &= \langle S \rangle e^{\frac{2ia}{3f_R}}, \quad (f_R = 2\sqrt{2} \langle S \rangle / 3), \\ F_S &= \langle F_S \rangle e^{\frac{-4ia}{3f_R}}, \end{aligned} \quad (5.7)$$

obtains the mass,

$$m_R^2 \simeq \frac{9}{16\sqrt{2}\pi^2} (4h^2 + 5k^2 N_{\text{mess}} + 5\lambda^2) m_{3/2} |m_S|. \quad (5.8)$$

In the final expression, we have used (2.9), and (2.10). For $k = O(1)$, the contribution from the messenger loop dominates the R-axion mass and gives,

$$m_R \lesssim 40 \text{ MeV} \times k\lambda^{1/2} \left(\frac{N_{\text{mess}}}{5}\right)^{1/2} \left(\frac{g}{4\pi}\right)^{1/4} \left(\frac{m_{3/2}}{16 \text{ eV}}\right)^{3/4}, \quad (5.9)$$

where we have used the upper bound on m_S in (4.5).¹⁹ We should note that the fact that our R-symmetry is anomaly free — even in our dynamical completion — is important. As noted in [56] there is an enhancement to the R-axion mass when the R-symmetry is anomalous.

The decay constant f_R of the R-axion with a mass of tens of MeV is constrained by the contribution to the invisible decay mode of the K -meson, $K^+ \rightarrow \pi^+ + a$, which requires $f_R \gtrsim 2 \times 10^5 \text{ GeV}$. The decay constant is also constrained by the supernova SN 1987a, which requires $f_R \lesssim 10^6 \text{ GeV}$. Thus, by remembering that $|m_S| \lesssim 10^5 \text{ GeV}$ for $m_{3/2} \lesssim 16 \text{ eV}$, we find that the coupling constant h needs to satisfy $h \lesssim 0.1$, so that f_R is in between these constraints. Furthermore, future neutrino experiments are expected to discover the R-axion in this range or close the gap between these constraints [59].

6 Conclusions and unresolved issues

In this paper, we have discussed challenges in building explicit realistic models of gauge mediation. Focussing on the very light gravitino scenario, we found that in the framework of cascade gauge mediation we can construct viable models. The key was a one-loop breaking of R-symmetry that was not aligned with the goldstino.

As is well known, it is quite challenging to find perturbative models with a very light gravitino, sufficiently heavy gaugino masses, and a stable SUSY-breaking vacuum. Examining models based on one-loop R-symmetry breaking, we found that it is possible to construct models that satisfy all of these conditions by considering a UV complete theory. We also found that the predicted upper bound on the gluino mass is within the reach of the LHC. Therefore, models with a gravitino mass in the eV range based on one-loop R-symmetry breaking are expected to be supported or disproved in the near future.

Several final remarks are in order. A gravitino with a mass in the eV range cannot be the dominant component of the dark matter and these models require other dark matter candidates. In models with gauge mediation, we have several places to look for a dark matter candidate. Dark matter candidates could possibly be found in the messenger or SUSY breaking sectors. In fact, these sectors could provide stable particles with masses in the hundreds of TeV that could be interesting candidates for dark matter, since the dark matter density can be consistent with observations if the annihilation cross sections of the dark matter candidates saturate the unitarity bound.

¹⁹We multiply the upper bound by $5^{1/2}$ with the embedding into the dynamical model in mind.

For example, the messengers can be good candidates for dark matter if they are confined into a composite state by strong dynamics and are neutral under the SSM gauge groups. In cascade gauge mediation, those composite states are expected to have mass around 100 TeV, since the messenger scale is in that range. The annihilation cross section of the composite neutral state is expected to saturate the unitarity limit due to the strong dynamics responsible for their compositeness. As discussed in [60, 61], models with composite messenger dark matter can be realized for $N_{\text{mess}} = 5$ where the $SU(N_{\text{mess}})$ symmetry is identified with the strongly coupled gauge theory which is responsible for creating the composite states out of the messengers. The model with $N_{\text{mess}} = 5$ also has the feature of a relatively heavy gluino mass (see (4.17)).

Another possibility is that the primary SUSY breaking sector may provide dark matter candidates with masses in the TeV range in the form of pseudo-Nambu-Goldstone bosons. As discussed in [62, 63], a consistent dark matter density is achieved through a Breit-Wigner enhancement [64] of the dark matter annihilation cross section.

In our argument, we have assumed that the secondary field, S , couples to $SU(3)$ -triplet and $SU(2)$ -doublet messengers universally. If we introduce two secondary fields, $S_{d,\ell}$, which couple to the triplet and doublet messengers separately, the usual mass spectrum for SUSY particles in minimal gauge mediation could be changed. In such a case, however, one may worry about introduction of new CP-phases. As discussed in [18], however, there is no CP-problem even in this extension.

Finally, we note that the cascade gauge mediation model based on the R-symmetry breaking models in this paper can also be used to construct models with much heavier gravitinos. One important application of such a possibility is to models in which a gravitino of mass 1-10 keV can be the dominant dark matter component.²⁰ Gravitino dark matter with mass in this range draws attention as a possible solution to the seeming discrepancies between the observation and the simulated results of galaxy formation based on the cold dark matter model.²¹ The thermally produced gravitino density, however, exceeds the current observed dark matter density. Thus, we need to dilute the dark matter density by entropy production, for example, from the long lived particles in the primary SUSY breaking sector [73].

Another interesting feature of the cascade gauge mediation for a heavier gravitino mass is the direct R-axion search at the LHC. As we discussed in section 5, the mass of the R-axion increases with the gravitino mass. The R-axion decay constant, which governs the R-axion interactions, however, remains around $10^5/h$ GeV even for a heavier gravitino. As discussed in [74], the R-axion with a mass of hundreds of MeV can dominantly decay into a pair of muons. At the LHC, an R-axion with a decay constant $f_R = 10^{4-5}$ GeV can be copiously produced, and hence, it is possible to detect the R-axion at the LHC by searching for the displaced vertex of the R-axion decay from which a muon pair with low invariant mass is produced.

²⁰A gravitino mass in the one to ten keV range is still difficult to realize in the conventional cascade gauge mediation models, where more than one loop is used to generate m_S^2 as in [47–49].

²¹For recent developments on the effects on the galaxy formation in the warm dark matter scenario see, for example, [65–72] and references therein.

Acknowledgments

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A Necessary condition for R-symmetry breaking at one loop

In this appendix, we show the need for fields with R-charge other than 0 or 2 to achieve spontaneous R-breaking in O’Raifeartaigh models at one loop and at leading order in SUSY breaking. In our discussion we assume that R-symmetry is broken by the vev of an R-charged superfield S , which is not necessarily identified with the SUSY breaking field Z that obtains $\langle F_Z \rangle \neq 0$. We also assume that the R-breaking field has no mass term in the superpotential, which is the natural assumption since we are seeking models with R-symmetry breaking at one loop.

At leading order in SUSY breaking, the soft mass of S is given by,

$$m_S^2 = \frac{c}{m^2} |F_Z|^2, \tag{A.1}$$

where c is the one-loop coefficient and m is the mass scale of the fields that are integrated out. For $m_S^2 < 0$, the scalar component of S is repelled from its origin, and hence, R-symmetry is spontaneously broken.

To be specific let us assume that S and Z couple to some other superfields X_i in the O’Raifeartaigh model²² via the superpotential terms,

$$y_{ij} S X_i X_j, \quad g_{ij} Z X_i X_j. \tag{A.2}$$

Here we assume that the X_i have diagonalized mass terms at $S = Z = 0$. The leading soft mass squared in (A.1) is generated by inserting F_Z and F_Z^* into the one-loop self-energy diagram of S in which only scalars are circulating (see figure 2).

From the figure, we see that there are two ways to insert $|F_Z|^2$ into the self-energy diagram. One way is to insert F_Z and F_Z^* into the upper half of the loop, (i.e. the scalar line, see figure 3). The contribution to m_S^2 is

$$m_{S,\phi}^2 = \frac{1}{16\pi^2} \sum_{i,j,k,l} \int \frac{d^4 \ell_E}{(2\pi)^4} y_{ji} \frac{1}{m_{X_i}^2 + \ell_E^2} g_{ik}^* \frac{1}{m_{X_k}^2 + \ell_E^2} g_{kl} \frac{1}{m_{X_l}^2 + \ell_E^2} y_{lj}^* \frac{1}{m_{X_j}^2 + \ell_E^2} \ell_E^2, \tag{A.3}$$

where we have rotated the loop momentum to the Euclidian momentum. Now, let us define,

$$\begin{aligned} X_{jk} &= \sum_i \frac{1}{\sqrt{m_{X_j}^2 + \ell_E^2}} y_{ji} \frac{1}{m_{X_i}^2 + \ell_E^2} g_{ik}^* \frac{1}{\sqrt{m_{X_k}^2 + \ell_E^2}}, \\ X'_{km} &= \sum_l \frac{1}{\sqrt{m_{X_k}^2 + \ell_E^2}} g_{kl} \frac{1}{m_{X_l}^2 + \ell_E^2} y_{lm}^* \frac{1}{\sqrt{m_{X_m}^2 + \ell_E^2}} = X_{mk}^*, \end{aligned} \tag{A.4}$$

²²The X_i may include S or Z as long as the stability of the SUSY breaking vacuum is intact.

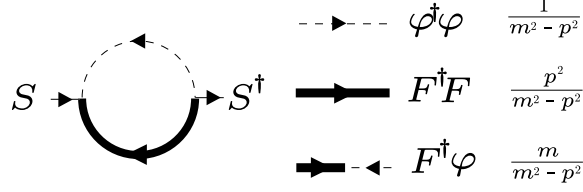


Figure 2. The diagram of the one-loop self energy of S to which $|F_Z|^2$ is inserted. Here, the dashed line denotes the scalar propagator, while the thick line denotes that of the F -component.

where we have used $y_{ij} = y_{ji}$ and $g_{ij} = g_{ji}$ to show that $X'_{km} = X^*_{mk}$. By using these matrices, the contribution to the mass is rewritten as

$$m_{S,\phi}^2 = \frac{1}{16\pi^2} \sum_{j,k} \int \frac{d^4\ell_E}{(2\pi)^4} X_{jk} X'_{kj} \ell_E^2 = \frac{1}{16\pi^2} \sum_{j,k} \int \frac{d^4\ell_E}{(2\pi)^4} |X_{jk}|^2 \ell_E^2 > 0. \quad (\text{A.5})$$

Therefore, the contribution from the $|F_Z|^2$ insertion into the scalar line is always positive, and hence, cannot cause R-symmetry breaking.

The other way to insert $|F_Z|^2$ is into the lower half of the loop (i.e. the F -line). The resultant contribution to m_S^2 is given by,

$$m_{S,F}^2 = -\frac{1}{16\pi^2} \sum_{i,j,k,l} \int \frac{d^4\ell_E}{(2\pi)^4} y_{ji} \frac{1}{m_{X_i}^2 + \ell_E^2} y_{il}^* \frac{1}{m_{X_l}^2 + \ell_E^2} g_{lk}^* \frac{1}{m_{X_k}^2 + \ell_E^2} g_{kj} \frac{1}{m_{X_j}^2 + \ell_E^2} m_j^* m_l. \quad (\text{A.6})$$

This can be rewritten by using

$$Y_{ik} = \sum_l \frac{1}{\sqrt{m_{X_i}^2 + \ell_E^2}} y_{il}^* \frac{m_l}{m_{X_l}^2 + \ell_E^2} g_{lk}^* \frac{1}{\sqrt{m_{X_k}^2 + \ell_E^2}},$$

$$Y'_{km} = \sum_j \frac{1}{\sqrt{m_{X_k}^2 + \ell_E^2}} g_{kj} \frac{m_j^*}{m_{X_j}^2 + \ell_E^2} y_{jm} \frac{1}{\sqrt{m_{X_m}^2 + \ell_E^2}} = Y_{mk}^*, \quad (\text{A.7})$$

to

$$m_{S,F}^2 = -\frac{1}{16\pi^2} \sum_{i,k} \int \frac{d^4\ell_E}{(2\pi)^4} |Y_{ik}|^2 < 0. \quad (\text{A.8})$$

Thus, the contribution from the insertion to the F -line gives a negative contribution to m_S^2 , which may lead to R-symmetry breaking.

From this argument, we see that the necessary condition to have negative $m_S^2 + m_{S,\phi}^2 + m_{S,F}^2$ at the leading order is that the model allows the insertion of $|F_Z|^2$ to the internal F -line. By cutting the diagram in between $|F_Z|^2$ on the F -line in figure 3, we see that the insertion to the F -line is possible when the effective term

$$\mathcal{L}_{\text{eff}} \propto F_Z S X_i X_k + h.c., \quad (\text{A.9})$$

is allowed by the symmetries of the model, which corresponds to the term in the superpotential,

$$W_{\text{eff}} \propto Z S X_i X_k. \quad (\text{A.10})$$

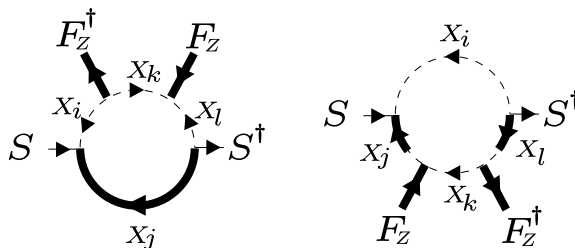


Figure 3. The diagrams with $|F_Z|^2$ insertion. $|F_Z|^2$ is inserted on the scalar line on the left diagram, while it is inserted on the F -term line.

Since we assume that the R-charge of Z is 2 and S has a non-vanishing R-charge, the above effective superpotential is allowed only when S or X_i or X_k have R-charges other than 0 or 2. This proves that R-symmetry breaking at one loop (and at leading order in $|F_Z|^2$) requires the superfields with R-charge other than 0 or 2.

B Renormalization group behavior of the dynamical model

In this appendix, we discuss the behavior of the coupling constants under the renormalization group evolution in subsection 4.1. Above the dynamical scale Λ_{dyn} of the SU(2) gauge interaction, the superpotential of the model is given by,

$$\begin{aligned}
 W = & \frac{ig_0}{\sqrt{2}}Z_0(Q_1Q_3 + Q_2Q_4) + \frac{g_1}{\sqrt{2}}Z_1(Q_2Q_3 + Q_1Q_4) + \frac{g_2}{\sqrt{2}}Z_2(Q_1Q_2 + Q_3Q_4) \\
 & - \frac{ig_3}{\sqrt{2}}Z_3(Q_1Q_2 - Q_3Q_4) + \frac{ig_4}{\sqrt{2}}Z_4(Q_2Q_3 - Q_1Q_4) + \frac{g_5}{\sqrt{2}}Z_5(Q_1Q_3 - Q_2Q_4). \quad (\text{B.1})
 \end{aligned}$$

Here, we have rearranged Z_{ij} in subsection 4.1 by the unitary transformation,

$$\begin{aligned}
 Z_{12} = \frac{1}{\sqrt{2}}(Z_2 - iZ_3), \quad Z_{13} = \frac{1}{\sqrt{2}}(Z_5 + iZ_0), \quad Z_{14} = \frac{1}{\sqrt{2}}(Z_1 - iZ_4), \\
 Z_{23} = \frac{1}{\sqrt{2}}(Z_1 + iZ_4), \quad Z_{24} = \frac{-1}{\sqrt{2}}(Z_5 - iZ_6), \quad Z_{34} = \frac{-1}{\sqrt{2}}(Z_2 + iZ_3), \quad (\text{B.2})
 \end{aligned}$$

and defined appropriate coupling constants g_A , ($A = 0, \dots, 5$).²³ In the following, we assume that the model possesses an SO(5) global symmetry and assume that $g_i = g' > g_0$, ($i = 1, \dots, 5$) for simplicity.

At an energy scale above Λ_{dyn} , the model can be well described by the Z_A and Q_i , and the beta functions of the SU(2) gauge coupling constant g_2 and the Yukawa coupling constants g_0 and g' are given by,

$$\begin{aligned}
 \frac{dg_2}{d \ln \mu} &= -\frac{g_2^3}{4\pi^2}, \\
 \frac{dg_0}{d \ln \mu} &= \frac{g_0}{16\pi^2}(3g_0^2 + 5g'^2 - 3g_2^2), \\
 \frac{dg'}{d \ln \mu} &= \frac{g'}{16\pi^2}(g_0^2 + 7g'^2 - 3g_2^2). \quad (\text{B.3})
 \end{aligned}$$

²³Below the scale of Λ_{dyn} , the meson fields M_A is defined so that we have $W = g_A Z_A M_A$.

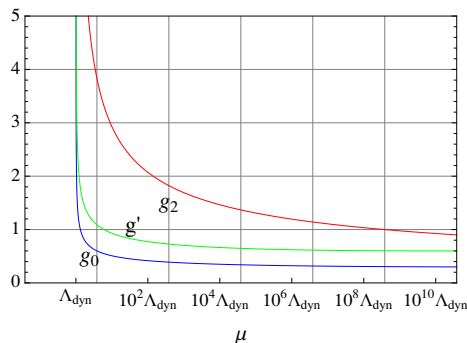


Figure 4. The running of the coupling constants under the renormalization group evolution. We have taken $g_2(M_{\text{GUT}}) = 0.9$ which leads to $\Lambda_{\text{dyn}} = O(10^2)$ TeV. We have also taken $g_0(M_{\text{GUT}}) = 0.3$ and $g'(M_{\text{GUT}}) = 0.6$. The figure shows that the Yukawa coupling constants become strong at the energy scale around Λ_{dyn} .

Thus, not only the gauge coupling constant g_2 but also the Yukawa couplings g_0 and g' are asymptotically free²⁴ in the region where g_2 is larger than g_0 and g' . That is, for example, if we assume that these coupling constants are perturbative at the GUT scale, g_2 becomes very strong at Λ_{dyn} which raise up g_0 and g' via the beta functions. Therefore, the rather large coupling constants at around Λ_{dyn} are a natural consequence and do not lead to Landau pole problems.

In figure 4, we show typical behaviors of the coupling constants under the renormalization group evolution. In the figure, we have fixed $g_2(M_{\text{GUT}}) = 0.9$ so that $\Lambda_{\text{dyn}} = M_{\text{GUT}} \times e^{-2\pi^2/g_2^2(M_{\text{GUT}})} = O(10^2)$ TeV. The figure shows that the Yukawa coupling constants g and g' become strong at the energy scale around Λ_{dyn} , while they are perturbative at the higher energy scale. Therefore, the rather large Yukawa coupling constants can be naturally realized due to the renormalization group effects in this model.

C D-term spontaneous R-symmetry breaking

Here we show that our desired one-loop R-symmetry breaking may be induced by D -term SUSY breaking. We will begin with a simple FI model with two flavors with charge of unit magnitude, $\phi_{\pm}, \tilde{\phi}_{\pm}$. Consider the superpotential

$$W = m(\phi_+ \tilde{\phi}_- + \tilde{\phi}_+ \phi_-) + \lambda S \phi_+ \phi_- + \dots, \tag{C.1}$$

where the ellipsis stands in for S -independent, higher dimension terms, which do not affect the result. With our normalization conventions, D takes the form

$$D = -\xi - g \left(|\phi_+|^2 - |\phi_-|^2 + |\tilde{\phi}_+|^2 - |\tilde{\phi}_-|^2 \right), \tag{C.2}$$

²⁴The asymptotic freedom g_0 and g' is only approximate with the landau pole occurring well after the GUT scale.

where g is the gauge coupling constant and ξ is the mass-dimension-two FI parameter. For this model, the one-loop mass for S is found to be

$$m_S^2 = \frac{\lambda^2}{16\pi^2} \left(\frac{g\xi}{m}\right)^2 h(x),$$

$$h(x) = \frac{(2+x)\ln(1+x) + (2-x)\ln(1-x)}{x^2}, \tag{C.3}$$

where we have taken $x = g\xi/m^2 < 1$.

As we see from figure 5, m_S^2 is negative for all x , and so R-symmetry breaking is achieved when S has non-zero R-charge. The disadvantage of this model is that the one-loop mass vanishes to leading order in x . This means that the scale of R-symmetry breaking is suppressed compared with the models discussed in the main text unless x is close to one.

The result is, in fact, singular in the limit $x \rightarrow 1$. This is an IR singularity that emerges when two of our fields become massless. The diagram responsible is the one built from the trilinear scalar couplings,

$$\lambda m^* \phi_- \tilde{\phi}_-^* S + h.c. \tag{C.4}$$

Notice that, in the parameter region near the singularity, the estimate of the vacuum expectation value of S in terms of m_S in (2.9) is no longer reliable. Instead we need to consider the full Coleman-Weinberg potential to determine the vacuum expectation value of S , where the IR singularity is automatically cutoff by the VEV of S . Thus, even in the parameter region where $|m_S|$ is highly enhanced by the IR singularity, it is not expected that the vacuum expectation value of S is highly enhanced from

$$\langle S \rangle \simeq \frac{\lambda^2}{16\sqrt{2}\pi^2 h} \left(\frac{g\xi}{m}\right)^2. \tag{C.5}$$

From this result, it follows that R-symmetry breaking of this sort occurs in a much broader class of models. For example, we can consider couplings of the form in (C.1), but add an arbitrary number of fields with arbitrary (non-anomalous) charge assignments. For our purposes, the model effectively decouples into a sum over sectors of like charge magnitude, q . Each has the form,

$$W_q = M_{ij} \phi_{+i} \phi_{-j} + \lambda_{ij} S \phi_{+i} \phi_{-j}. \tag{C.6}$$

We further impose the constraint that there be an R-symmetry under which S is charged.

$$M_{ij} \neq 0 \Rightarrow R(q_i) + R(\bar{q}_j) = 2, \quad \lambda_{ij} \neq 0 \Rightarrow R(q_i) + R(\bar{q}_j) = \alpha, \quad R(S) = 2 - \alpha \neq 0. \tag{C.7}$$

α is undetermined here.²⁵ As before, we also require $\langle \phi_{\pm i} \rangle = 0$. The matrix, M , may be diagonalized by a biunitary transformation leaving D invariant. It is then easy to see that the theory has a further effective decoupling. If we consider the contribution to the

²⁵Upon including the cubic term, $\Delta W \sim S^3$, it is fixed to $\alpha = 4/3$.

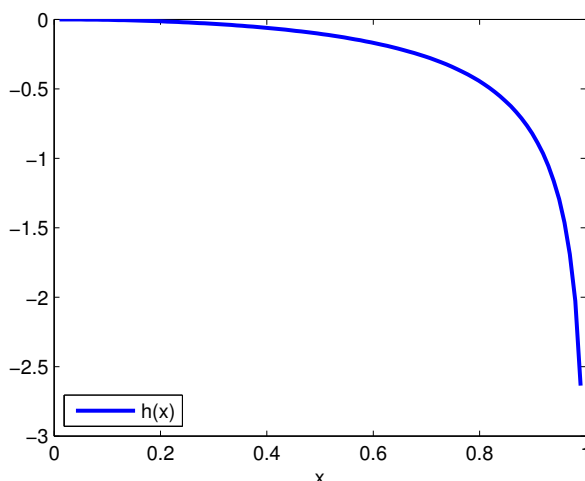


Figure 5. The function $h(x)$ ($x = ke/2m^2$) given in (C.3), which represents the size of the tachyonic mass in the model based on the D-term SUSY breaking. The value of $|h(x)|$ is highly enhanced in the region $x \rightarrow 1$, which corresponds to an IR singularities in the one-loop diagram.

mass of S from a particular coupling $\lambda_{\alpha\beta}$ (Greek indices will not be summed) the relevant terms involve just two flavors.

$$\begin{aligned} W &\supset m_\alpha \phi_{+\alpha} \phi_{-\alpha} + m_\beta \phi_{+\beta} \phi_{-\beta} + \lambda_{\alpha\beta} S \phi_{+\alpha} \phi_{-\beta} \quad (\text{no sum}), \\ D &\supset -\xi - qg(|\phi_{+\alpha}|^2 - |\phi_{-\alpha}|^2 + |\phi_{+\beta}|^2 - |\phi_{-\beta}|^2). \end{aligned} \tag{C.8}$$

This means that we may directly apply the previous result by rescaling the coupling and summing over charges.²⁶ The upshot is that, as before, S is tachyonic throughout the parameter space.

We may likewise extend this result to models with non-abelian D-term breaking [75–79]. We still take S to have no tree-level mass term, so it is not permitted to couple to the fields responsible for D-term breaking (and Higgsing). For our purposes, these fields only play a role by contributing to the masses of the fields that do couple to S :

$$V \supset \langle D^a \rangle \sum_r \phi_r^\dagger T_r^a \phi_r. \tag{C.9}$$

For example, in SUSY QCD, we may consider the analogous set of couplings to those in (C.6), but now with ϕ_+ a fundamental and ϕ_- an anti-fundamental under an $SU(N)$ gauge group. After a set of field transformations, one finds that the squared mass of S is given as a sum over colors of negative contributions, much like before.

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²⁶We previously considered the case with $m_\alpha = m_\beta$. However, the one-loop mass with $m_\alpha \neq m_\beta$ generically gives $m_S^2 < 0$ as well.

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