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Testing the custodial symmetry in the Higgs sector of the Georgi-Machacek model

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Abstract: We study how the custodial symmetry in the Higgs sector of the Georgi-Machacek (GM) model can be tested at the LHC. As the minimal extension of the Higgs triplet model, in which tiny neutrino masses are generated via the Type-II Seesaw Mechanism, the GM model keeps the electroweak ρ parameter at unity at tree level. In the GM model, there are 5-plet (H_5) , 3-plet (H_3) and singlet (H_1) Higgs bosons under the classification of the custodial $SU(2)_V$ symmetry, in addition to the standard model-like Higgs boson (h) . These new Higgs bosons have the following characteristic features at the tree level: (1) the masses of the Higgs bosons belonging to the same $SU(2)_V$ multiplet are degenerate; and (2) H_5 and H_1 couple to the electroweak gauge bosons but not SM quarks, whereas H_3 couples to the quarks but not the gauge bosons. We find that the H_5 production from the weak vector boson fusion process and the Drell-Yan process associated with H_3 are useful in testing the custodial symmetry of the Higgs sector at the LHC. In addition, these processes can also be used to discriminate from other models that contain singly-charged Higgs bosons and extra neutral Higgs bosons. We also investigate a possible enhancement in the $h \to \gamma\gamma$ as well as $h \to Z\gamma$ decays.

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1 Introduction

Recently, a new particle of mass about 125 GeV has been discovered at the CERN Large Hadron Collider (LHC) with a total production rate consistent with that of the standard model (SM) Higgs boson [\[1,](#page-33-0) [2\]](#page-33-1). Confirming this Higgs-like particle as the one responsible for the electroweak symmetry breaking is of paramount importance in particle physics because, for one thing, it explains the origin of mass for elementary particles. While further detailed examinations are required, the current LHC data show some deviations in the pattern of its decay branching ratios from the SM expectation. This leads to the speculation that the Higgs sector may not as simple as the one in SM.

In certain new physics models such as supersymmetry, the Higgs sector has to be extended with additional nontrivial isospin $SU(2)_L$ scalar multiplets for consistency or to explain new phenomena. Such an extension also holds the capacity to provide additional CP-violating sources for low-energy phenomena as well as baryon asymmetry of the Universe. For example, the two-Higgs doublet model (2HDM) [\[3\]](#page-33-2) is an extensively studied

prototype in which an additional scalar doublet is introduced. $SU(2)_L$ triplet Higgs fields also occur in some new physics models, such as the left-right symmetric model [\[4](#page-33-3)[–6](#page-33-4)] and little Higgs models [\[7](#page-33-5), [8](#page-33-6)]. By introducing a complex triplet Higgs field, it is possible to have an effective dimension-5 operator for generating tiny Majorana mass for neutrinos. Therefore, it is important to determine the true Higgs sector in order to exactly know what kind of new physics models exist at the TeV or higher energy scales. In this paper, we want to focus on the phenomenology of the extended Higgs sector in the model proposed by Georgi and Machacek (GM) [\[9](#page-33-7)] in mid-80s. We investigate how one can distinguish it from the other Higgs-extended models at the LHC.

The GM model contains a Higgs doublet field Φ and a triplet field Δ , with the latter containing a hypercharge $Y = 1$ component and a $Y = 0$ component. The model is of great interest because it can provide tiny mass to neutrinos à la the Seesaw Mechanism, dubbed the Type-II Seesaw $[10-14]$. Moreover, it has been shown that the Higgs potential in this model can be constructed to maintain a custodial $SU(2)_V$ symmetry at the tree level [\[15\]](#page-34-2), keeping the electroweak ρ parameter at unity to be consistent with the experimental constraint. In the model, there are 5-plet Higgs bosons $H_5 = (H_5^{\pm \pm}, H_5^{\pm}, H_5^0)$, 3-plet Higgs bosons H_3 ($=$ H_3^{\pm} , H_3^0) and singlet Higgs boson H_1^0 under the classification of the SU(2)_V symmetry. The masses of the Higgs bosons belonging to the same $SU(2)_V$ multiplet are the same at the tree level as the consequence of custodial symmetry.

The doubly-charged Higgs boson $H_5^{\pm\pm}$, for example, is an important but not unique feature of the model. Finding particles in one Higgs multiplet and checking their (near) mass degeneracy would better verify the model. Strategies of discovering such Higgs bosons, however, depend largely on the vacuum expectation value (VEV) of the Higgs triplet field, v_Λ .

In the minimal Higgs triplet model (HTM) where only one additional complex Higgs triplet is introduced, the doubly-charged Higgs bosons couples dominantly to a pair of likesign leptons when $v_{\Delta} \lesssim 10^{-4} \text{ GeV}$. The collider phenomenology of this scenario has been extensively studied recently [\[16](#page-34-3)[–21\]](#page-34-4). The doubly-charged Higgs boson has been searched for at the Tevatron $[22-25]$ and the LHC $[26, 27]$ $[26, 27]$ $[26, 27]$ by looking for like-sign lepton pairs with the same or different flavors. A lower mass bound of about 400 GeV has been obtained for most scenarios. On the other hand, the doubly-charged Higgs bosons couples dominantly to a pair of like-sign W bosons when $v_{\Delta} \gtrsim 10^{-4} \text{ GeV}$ $v_{\Delta} \gtrsim 10^{-4} \text{ GeV}$ $v_{\Delta} \gtrsim 10^{-4} \text{ GeV}$.¹ This possibility is less explored experimentally. Besides, the triplet VEV in the HTM is constrained by the ρ parameter to be less than a few GeV, limiting significantly the discovery reach at the LHC.

In the GM model, a larger triplet VEV is allowed due to the custodial symmetry. It is therefore interesting to consider signatures of the like-sign gauge boson decays. In ref. [\[28\]](#page-35-1), collider phenomenology of the GM model has been discussed in the case of light triplet-like Higgs bosons, e.g., less than 100 GeV. A recent study by one of the authors and collaborators [\[29](#page-35-2)] finds that with $v_{\Delta} = 55 \,\text{GeV}$ and appropriate cuts, the current LHC can reach up to 450 GeV for the doubly-charged Higgs mass. In this work, we further explore

¹When there is a non-zero mass splitting among the scalar bosons in the triplet Higgs field and the doubly-charged Higgs boson mass is the heaviest, the cascade decays of the doubly-charged Higgs boson become dominant. Phenomenology of this scenario has been discussed in refs. [\[30](#page-35-3)[–32\]](#page-35-4).

consequences of the custodial symmetry in the Higgs sector of the GM model and study the phenomenology of its entire Higgs sector at the LHC. We find that the single production of $H₅$ via the weak vector boson fusion process is useful to test the mass degeneracy among the H_5 bosons. We also find that the Drell-Yan process, where H_5 and H_3 are simultaneously produced can be used to check the mass degeneracy among H_3 .

The structure of this paper is organized as follows. We review the GM model in section [2.](#page-3-0) The Higgs bosons are first classified according to their group representations under the custodial symmetry. We then consider possible mixings between the two triplets and between the two singlets, and work out their masses. A mass relation among the Higgs bosons of different representations is obtained in the decoupling limit when the triplet VEV vanishes. Finally, we show the Yukawa couplings between SM fermions and the physical Higgs bosons. In section [3,](#page-9-0) we consider both theoretical constraints of perturbative unitarity and vacuum stability and the experimental constraint from the Z-pole data of $Z \rightarrow b\bar{b}$ decay at one-loop level. In particular, they impose bounds on the triplet VEV and the Higgs triplet mass. In section [4,](#page-11-1) we discuss in detail how the Higgs bosons decay in scenarios with or without hierarchy in the masses of the physical Higgs singlet, 3-plet, and 5-plet. The collider phenomenology of the model can be drastically different in different regions of the v_∆- Δm (Δm is the mass difference between H_5 H_5 and H_3) space. section 5 discusses how the Higgs bosons can be searched for at the LHC. Finally, we compute the decay rates of $h \to \gamma\gamma$ and $Z\gamma$ in the model in section [6.](#page-27-0) Our findings are summarized in section [7.](#page-28-0)

2 The model

In the GM model, the Higgs sector is composed of the SM isospin doublet Higgs field ϕ with hypercharge $Y = 1/2$ and two isospin triplet Higgs fields χ with $Y = 1$ and ξ with $Y = 0$. These fields can be expressed in the form:

$$
\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ \phi^- & \phi^0 \end{pmatrix}, \quad \Delta = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \chi^+ \\ \chi^{--} & \xi^- & \chi^0 \end{pmatrix}, \tag{2.1}
$$

where Φ and Δ are transformed under $SU(2)_L \times SU(2)_R$ as $\Phi \to U_L \Phi U_R^{\dagger}$ and $\Delta \to U_L \Delta U_R^{\dagger}$ with $U_{L,R} = \exp(i\theta_{L,R}^a T^a)$ and T^a being the SU(2) generators. The neutral components in eq. [\(2.1\)](#page-3-1) can be parametrized as

$$
\phi^0 = \frac{1}{\sqrt{2}}(\phi_r + v_\phi + i\phi_i), \quad \chi^0 = \frac{1}{\sqrt{2}}(\chi_r + i\chi_i) + v_\chi, \quad \xi^0 = \xi_r + v_\xi,
$$
 (2.2)

where v_{ϕ} , v_{χ} and v_{ξ} are the VEV's for ϕ^0 , χ^0 and ξ^0 , respectively. When the two triplet VEV's v_χ and v_ξ are taken to be the same, i.e., $v_\chi = v_\xi \equiv v_\Delta$, the SU(2)_L × SU(2)_R symmetry is reduced to the custodial $SU(2)_V$ symmetry. The phase convention for the component scalar fields are chosen to be $\chi^{--} = (\chi^{++})^*, \ \phi^- = -(\phi^+)^*, \ \chi^- = -(\chi^+)^*,$ $\xi^- = -(\xi^+)^*$ and $\xi^0 = (\xi^0)^*.$

The relevant Lagrangian involving the Higgs fields can be written as

$$
\mathcal{L}_{GM} = \mathcal{L}_{kin} + \mathcal{L}_Y + \mathcal{L}_{\nu} - V_H, \qquad (2.3)
$$

where \mathcal{L}_{kin} , \mathcal{L}_Y , \mathcal{L}_ν and V_H are the kinetic term, the Yukawa interaction between ϕ and the fermions, the neutrino Yukawa interaction between χ and the lepton doublets, and the Higgs potential, respectively.

The most general Higgs potential invariant under the $SU(2)_L \times SU(2)_R \times U(1)_Y$ symmetry in terms of the fields defined in eq. [\(2.1\)](#page-3-1) is

$$
V_H = m_1^2 \text{tr}(\Phi^\dagger \Phi) + m_2^2 \text{tr}(\Delta^\dagger \Delta) + \lambda_1 \text{tr}(\Phi^\dagger \Phi)^2 + \lambda_2 [\text{tr}(\Delta^\dagger \Delta)]^2 + \lambda_3 \text{tr}[(\Delta^\dagger \Delta)^2]
$$

+ $\lambda_4 \text{tr}(\Phi^\dagger \Phi) \text{tr}(\Delta^\dagger \Delta) + \lambda_5 \text{tr}\left(\Phi^\dagger \frac{\tau^a}{2} \Phi \frac{\tau^b}{2}\right) \text{tr}(\Delta^\dagger t^a \Delta t^b)$
+ $\mu_1 \text{tr}\left(\Phi^\dagger \frac{\tau^a}{2} \Phi \frac{\tau^b}{2}\right) (P^\dagger \Delta P)^{ab} + \mu_2 \text{tr}\left(\Delta^\dagger t^a \Delta t^b\right) (P^\dagger \Delta P)^{ab},$ (2.4)

where τ^a are the Pauli matrices, t^a are the 3×3 matrix representation of the SU(2) generators given by

$$
t_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \quad t_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & -i & 0 \\ i & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad t_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}, \tag{2.5}
$$

and the matrix P is defined as

$$
P = \begin{pmatrix} -1/\sqrt{2} \ i/\sqrt{2} \ 0 \\ 0 & 0 \ 1 \\ 1/\sqrt{2} \ i/\sqrt{2} \ 0 \end{pmatrix} . \tag{2.6}
$$

As in the HTM, the SM electroweak symmetry breaking can induce the triplet field to develop a VEV v_{Δ} through the μ_1 term in the Higgs potential. To our knowledge, most of the previous analyses ignore both μ_1 and μ_2 interactions in their phenomenology studies. We will keep these terms in this work.

Using the tadpole conditions,

$$
\left. \frac{\partial V_H}{\partial \phi_r} \right|_0 = 0, \quad \left. \frac{\partial V_H}{\partial \xi_r} \right|_0 = 0, \quad \left. \frac{\partial V_H}{\partial \chi_r} \right|_0 = 0, \tag{2.7}
$$

the parameters m_1^2 and m_2^2 can be eliminated as

$$
m_1^2 = -v^2 \left(2c_H^2 \lambda_1 + \frac{3}{8}s_H^2 \lambda_4 + \frac{3}{16}s_H^2 \lambda_5 \right) + \frac{3}{8}s_H^2 M_1^2,
$$
\n(2.8a)

$$
m_2^2 = -v^2 \left(\frac{3}{4}s_H^2 \lambda_2 + \frac{1}{4}s_H^2 \lambda_3 + c_H^2 \lambda_4 + \frac{1}{2}c_H^2 \lambda_5\right) + \frac{1}{2}c_H^2 M_1^2 + \frac{1}{4}M_2^2,
$$
 (2.8b)

where $v^2 = v_\phi^2 + 8v_\Delta^2 = 1/(\sqrt{2}G_F)$ and $\tan \theta_H = 2\sqrt{2}v_\Delta/v_\phi$ with $s_H = \sin \theta_H$ and $c_H =$ $\cos \theta_H$. In eq. [\(2.8\)](#page-4-0), we introduce M_1^2 and M_2^2 as

$$
M_1^2 = -\frac{v}{\sqrt{2}s_H}\mu_1, \quad M_2^2 = -3\sqrt{2}s_Hv\mu_2.
$$
 (2.9)

The second and third conditions in eq. (2.7) give the same constraint in eq. $(2.8b)$ as long as $v_{\chi} = v_{\xi}$.

Before we discuss the mass matrices and the mass eigenstates for the Higgs bosons, it is convenient to classify the Higgs boson states according to the custodial $SU(2)_V$ symmetry. The triplet field Δ , which can be understood as a 3 ⊗ 3 representation of the SU(2)_V multiplet, can be decomposed into the irreducible representations $\mathbf{5} \oplus \mathbf{3} \oplus \mathbf{1}$. Likewise, the doublet field Φ being the $2\otimes 2$ representation of the SU(2)_V multiplet, can be decomposed into $3 \oplus 1$. The 3 representation of Φ can be identified as the Nambu-Goldstone (NG) bosons of the SM as long as there is no mixing between the 3 representations of Δ and Φ . The 5-plet $(H_5^{\pm \pm}, H_5^{\pm}$ and H_5^0), the 3-plet $(H_3^{\pm}$ and $H_3^0)$ and the singlet (H_1^0) originating from Δ can be related to the original component fields as

$$
H_5^{\pm \pm} = \chi^{\pm \pm}, \qquad H_5^{\pm} = \frac{1}{\sqrt{2}} (\chi^{\pm} - \xi^{\pm}), \qquad H_5^0 = \frac{1}{\sqrt{3}} (\chi_r - \sqrt{2}\xi_r),
$$

$$
\tilde{H}_3^{\pm} = \frac{1}{\sqrt{2}} (\chi^{\pm} + \xi^{\pm}), \qquad \tilde{H}_3^0 = \chi_i,
$$

$$
\tilde{H}_1^0 = \frac{1}{\sqrt{3}} (\xi_r + \sqrt{2}\chi_r).
$$
 (2.10)

It is seen that H_5^0 and H_1 are CP-even states, whereas \tilde{H}_3^0 is a CP-odd state. In eq. [\(2.10\)](#page-5-0), the scalar fields with a tilde are not mass eigenstates in general. They can in principle mix with the corresponding scalar fields from the Higgs doublet field.

The mass of the doubly-charged Higgs boson $H_5^{\pm\pm}$ is

$$
m_{H_5^{++}}^2 = \left(s_H^2 \lambda_3 - \frac{3}{2} c_H^2 \lambda_5\right) v^2 + c_H^2 M_1^2 + M_2^2. \tag{2.11}
$$

The mass matrix for the CP-odd Higgs states in the basis of (ϕ_i, H_3^0) and that for the singly-charged states in the basis of $(\phi^+, \tilde{H}_3^+, H_5^+)$ are given by

$$
(M^{2})_{\text{CP-odd}} = -\left(\frac{1}{2}\lambda_{5}v^{2} - M_{1}^{2}\right)\left(\begin{array}{cc} s_{H}^{2} & -c_{H}s_{H} \\ -c_{H}s_{H} & c_{H}^{2} \end{array}\right), (M^{2})_{\pm} = \left(\begin{array}{cc} (M^{2})_{\text{CP-odd}} & 0 \\ 0 & 0 \ m_{H_{5}^{++}}^{2} \end{array}\right).
$$

The mass matrix for the CP-even Higgs states in the basis of $(\phi_r, \tilde{H}_1^0, \tilde{H}_5^0)$ is

$$
(M^2)_{\text{CP-even}} = \begin{pmatrix} (M^2)_{11} & (M^2)_{12} & 0 \\ (M^2)_{12} & (M^2)_{22} & 0 \\ 0 & 0 & m_{H_5^+}^2 \end{pmatrix},
$$

where the elements of the 2×2 submatrix are

$$
(M2)11 = 8cH2 \lambda_1 v2,
$$
\n(2.12a)

$$
(M2)22 = sH2 (3\lambda2 + \lambda3)v2 + cH2M12 - \frac{1}{2}M22,
$$
\n(2.12b)

$$
(M2)12 = \sqrt{\frac{3}{2}} s_{H} c_{H} [(2\lambda_{4} + \lambda_{5})v^{2} - M_{1}^{2}].
$$
 (2.12c)

The mass eigenstates are related to the above-mentioned states via the following unitary transformations

$$
\begin{pmatrix}\n\phi_i \\
\tilde{H}_3^0\n\end{pmatrix} = U_{\rm CP-odd} \begin{pmatrix} G^0 \\
H_3^0 \end{pmatrix}, \quad\n\begin{pmatrix}\n\phi^{\pm} \\
\tilde{H}_3^{\pm} \\
H_5^{\pm} \end{pmatrix} = U_{\pm} \begin{pmatrix} G^{\pm} \\
H_3^{\pm} \\
H_5^{\pm} \end{pmatrix}, \quad\n\begin{pmatrix}\n\phi_r \\
\tilde{H}_1^0 \\
H_5^0 \end{pmatrix} = U_{\rm CP-even} \begin{pmatrix}\nh \\
H_1^0 \\
H_5^0 \end{pmatrix},
$$
\n(2.13)

where G^{\pm} and G^{0} are the NG bosons for the longitudinal components of the W^{\pm} and Z bosons. The explicit forms of the unitary matrices are

$$
U_{\rm CP-odd} = \begin{pmatrix} c_H & -s_H \\ s_H & c_H \end{pmatrix}, \ U_{\pm} = \begin{pmatrix} 0 \\ U_{\rm CP-odd} \\ 0 \\ 0 \end{pmatrix}, \ U_{\rm CP-even} = \begin{pmatrix} c_{\alpha} & -s_{\alpha} & 0 \\ s_{\alpha} & c_{\alpha} & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad (2.14)
$$

where $c_{\alpha} = \cos \alpha$, $s_{\alpha} = \sin \alpha$ and the mixing angle α is defined by

$$
\tan 2\alpha = \frac{2(M^2)_{12}}{(M^2)_{11} - (M^2)_{22}}.\tag{2.15}
$$

The masses of the singly-charged Higgs bosons $(H_5^{\pm}$ and H_3^{\pm}), the CP-odd Higgs boson (H_3^0) and the CP-even Higgs bosons $(H_5^0, H_1^0$ and $h)$ are then

$$
m_{H_5^+}^2 = m_{H_5^0}^2 = m_{H_5^{++}}^2,
$$

\n
$$
m_{H_3^+}^2 = m_{H_3^0}^2 = -\frac{1}{2}\lambda_5 v^2 + M_1^2,
$$

\n
$$
m_h^2 = (M^2)_{11} c_\alpha^2 + (M^2)_{22} s_\alpha^2 + 2(M^2)_{12} s_\alpha c_\alpha,
$$

\n
$$
m_{H_1^0}^2 = (M^2)_{11} s_\alpha^2 + (M^2)_{22} c_\alpha^2 - 2(M^2)_{12} s_\alpha c_\alpha.
$$
\n(2.16)

It is observed that $H_5^{\pm \pm}$, H_5^{\pm} and H_5^0 are degenerate in mass and so are H_3^{\pm} and H_3^0 because of the custodial invariance in the Higgs potential. Therefore, the Higgs boson masses can be conveniently written as

$$
m_{H_5}^2 \equiv m_{H_5^{++}}^2 = m_{H_5^{+}}^2 = m_{H_5^{0}}^2, \quad m_{H_3}^2 \equiv m_{H_3^{+}}^2 = m_{H_3^{0}}^2, \quad m_{H_1}^2 \equiv m_{H_1^{0}}^2. \tag{2.17}
$$

The five dimensionless couplings in the potential, $\lambda_1, \ldots, \lambda_5$, can be substituted by the five physical parameters m_{H_5} , m_{H_3} , m_{H_1} , m_h and α as follows:

$$
\lambda_1 = \frac{1}{8v^2c_H^2} (m_h^2c_\alpha^2 + m_{H_1}^2s_\alpha^2),
$$

\n
$$
\lambda_2 = \frac{1}{6v^2s_H^2} \left[2m_{H_1}^2c_\alpha^2 + 2m_h^2s_\alpha^2 + 3M_2^2 - 2m_{H_5}^2 + 6c_H^2(m_{H_3}^2 - M_1^2) \right],
$$

\n
$$
\lambda_3 = \frac{1}{v^2s_H^2} \left[c_H^2(2M_1^2 - 3m_{H_3}^2) + m_{H_5}^2 - M_2^2 \right],
$$

\n
$$
\lambda_4 = \frac{1}{6v^2s_Hc_H} \left[\frac{\sqrt{6}}{2}s_{2\alpha}(m_h^2 - m_{H_1}^2) + 3s_Hc_H(2m_{H_3}^2 - M_1^2) \right],
$$

\n
$$
\lambda_5 = \frac{2}{v^2}(M_1^2 - m_{H_3}^2).
$$
\n(2.18)

The decoupling limit of this model can be obtained when we take the $v_{\Delta} \to 0$ limit (or equivalently $s_H \to 0$). In this limit, the mass formulae of the Higgs bosons reduce to

$$
m_{H_5}^2 = -\frac{3}{2}\lambda_5 v^2 + M_1^2 + M_2^2, \ m_{H_3}^2 = -\frac{1}{2}\lambda_5 v^2 + M_1^2, \ m_{H_1}^2 = M_1^2 - \frac{1}{2}M_2^2, \ m_h^2 = 8\lambda_1 v^2. \tag{2.19}
$$

Notice that M_2^2 is proportional to $s_H\mu_2$, and thus it becomes zero in this limit for a fixed value of μ_2 . If one wants to fix M_2^2 at a finite value, μ_2 has to be taken to infinity to compensate $s_H \rightarrow 0$ and eventually violates perturbativity in this model. Therefore, $M_2^2 = 0$ is the natural choice in this limit. On the other hand, M_1^2 is proportional to μ_1/s_H . Even in the $s_H \to 0$ limit, we can take a finite value for M_1^2 as long as $\mu_1 \to 0$ at the same rate as s_H . Consequently, the triplet-like Higgs bosons decouple when $M_1^2 \gg v^2$, and only h remains at the electroweak scale and acts like the SM Higgs boson. In addition, in the decoupling region $v_\Delta \simeq 0$, we find a simple mass relation for the triplet-like Higgs bosons:

$$
m_{H_1}^2 = \frac{3}{2}m_{H_3}^2 - \frac{1}{2}m_{H_5}^2.
$$
\n(2.20)

For the convenience in discussing interactions between leptons and the Higgs triplet field, we reorganize the Higgs fields as follows:

$$
\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}, \quad \chi = \begin{pmatrix} \frac{\chi^+}{\sqrt{2}} - \chi^{++} \\ \chi^0 & -\frac{\chi^+}{\sqrt{2}} \end{pmatrix}, \quad \xi = \begin{pmatrix} \frac{\xi^0}{\sqrt{2}} - \xi^+ \\ \xi^- & -\frac{\xi^0}{\sqrt{2}} \end{pmatrix}.
$$
 (2.21)

The relationship between the two representations in eqs. [\(2.1\)](#page-3-1) and [\(2.21\)](#page-7-0) are given in appendix A. With the introduction of the χ field above, the Yukawa interactions between the lepton doublets and the Higgs triplet are

$$
\mathcal{L}_{\nu} = h_{ij} \overline{L_L^{ic}} i \tau_2 \chi L_L^j + \text{h.c.}
$$
\n(2.22)

If we assign two units of lepton number to χ , then the λ_5 and μ_1 terms in the Higgs potential violate the lepton number. If we then take $\lambda_5 = \mu_1 = 0$, H_3^0 becomes massless and corresponds to the NG boson for the spontaneous breakdown of the global U(1) lepton number symmetry. In fact, H_3^{\pm} are also massless in that case because of the custodial symmetry.

The Majorana mass of neutrinos is derived as

$$
(m_{\nu})_{ij} = h_{ij}v_{\Delta} = \frac{h_{ij}}{2\sqrt{2}}vs_H.
$$
\n
$$
(2.23)
$$

This mass matrix can be diagonalized by the Pontecorvo-Maki-Nakagawa-Sakata matrix V_{PMNS} , and the Yukawa matrix h_{ij} can be rewritten as

$$
h_{ij} = 2\sqrt{2} \frac{V_{\text{PMNS}}^T m_{\nu}^{\text{diag}} V_{\text{PMNS}}}{v s_H}.
$$
\n(2.24)

The left-handed neutrino fields are then transformed as

$$
\nu_L = V_{\text{PMNS}}^{\dagger} \nu'_L. \tag{2.25}
$$

For simplicity, we hereafter assume that V_{PMNS} is the unit matrix and the mass eigenvalues of m_{ν}^{diag} are degenerate: $m_{\nu}^{\text{diag}} = \text{diag}(m_{\nu}, m_{\nu}, m_{\nu})$. In terms of the scalar mass eigenstates, the interaction terms are

$$
\mathcal{L}_{\nu} = \frac{2\sqrt{2}m_{\nu}}{s_{H}v} H_{5}^{++} \overline{e_{i}^{c}} P_{L} e_{i} - \frac{2\sqrt{2}m_{\nu}}{s_{H}v} \left(H_{5}^{+} + c_{H} H_{3}^{+} + s_{H} G^{+} \right) \overline{\nu_{i}^{c}} P_{L} e_{i} \Big] + \frac{2m_{\nu}}{s_{H}v} \left[\frac{1}{\sqrt{3}} (H_{5}^{0} + \sqrt{2}s_{\alpha}h + c_{\alpha}H_{1}^{0}) + i(G^{0}s_{H} + H_{3}^{0}c_{H}) \right] \overline{\nu_{i}^{c}} P_{L} \nu_{i} + \text{h.c.}
$$
 (2.26)

The Yukawa interaction between the fermions of one generation and the Higgs doublet ϕ is given by

$$
\mathcal{L}_Y = -Y_u \overline{Q_L} \tilde{\phi} u_R - Y_d \overline{Q_L} \phi d_R - Y_e \overline{L_L} \phi e_R + \text{h.c.},\tag{2.27}
$$

with $\tilde{\phi} = i\tau_2 \phi^*$. In terms of the fermion masses $m_f = \frac{vc_H}{\sqrt{2}} Y_f$ and the physical Higgs states, the interaction terms are expressed as

$$
\mathcal{L}_Y = -\sum_{f=u,d,e} \frac{m_f}{v} \left[\frac{c_\alpha}{c_H} \bar{f} f h - \frac{s_\alpha}{c_H} \bar{f} f H_1^0 + i \text{Sign}(f) \tan \theta_H \bar{f} \gamma_5 f H_3^0 \right] \n- \frac{\sqrt{2} V_{ud}}{v} \left[\tan \theta_H \bar{u} (m_u P_L - m_d P_R) d H_3^+ \right] + \frac{\sqrt{2} m_e}{v} \tan \theta_H \bar{\nu} P_R e H_3^+ + \text{h.c.}, \quad (2.28)
$$

where V_{ud} is one element of the Cabibbo-Kobayashi-Maskawa (CKM) matrix, Sign($f =$ u) = +1 and Sign($f = d, e$) = -1.

Finally, we discuss the kinetic terms for the Higgs fields

$$
\mathcal{L}_{\text{kin}} = \frac{1}{2} \text{tr}(D_{\mu} \Phi)^{\dagger} (D^{\mu} \Phi) + \frac{1}{2} \text{tr}(D_{\mu} \Delta)^{\dagger} (D^{\mu} \Delta), \tag{2.29}
$$

where the covariant derivatives are

$$
D_{\mu}\Phi = \partial_{\mu}\Phi + ig\frac{\tau^a}{2}W^a_{\mu}\Phi - ig'B_{\mu}\Phi\frac{\tau^3}{2},\tag{2.30}
$$

$$
D_{\mu}\Delta = \partial_{\mu}\Delta + ig t^{a} W^{a}_{\mu}\Delta - ig' B_{\mu}\Delta t^{3}.
$$
\n(2.31)

The masses of the gauge bosons are obtained under the condition of $v_\chi = v_\xi \equiv v_\Delta$ as

$$
m_W^2 = \frac{g^2}{4}v^2, \quad m_Z^2 = \frac{g^2}{4\cos^2\theta_W}v^2.
$$
 (2.32)

Thus, the electroweak rho parameter $\rho = m_W^2/(m_Z^2 \cos^2 \theta_W)$ is unity at the tree level. Oneloop corrections to ρ have been calculated in ref. [\[33\]](#page-35-5) for the GM model. The deviation of ρ from unity depends on the logarithm of the triplet-like Higgs boson masses and, therefore, the one-loop effect is not important in this model.

The Gauge-Gauge-Scalar (Gauge-Scalar-Scalar) vertices are listed in table [3](#page-32-1) (table [4\)](#page-32-2) in appendix B. We note that there is the $H_5^{\pm}W^{\mp}Z$ vertex at the tree level in the GM model (see table [3\)](#page-32-1). In the Higgs-extended models with $\rho = 1$ at the tree level and having singly-charged Higgs bosons (e.g., the 2HDM), the $H^{\pm}W^{\mp}Z$ vertex is absent at the tree level [\[34](#page-35-6)] and can only be induced at loop levels. Therefore, the magnitude of this vertex in such models is much smaller than that in the GM model. Thus, this vertex can be used to discriminate models with singly-charged Higgs bosons. The possibility of measuring the $H^{\pm}W^{\mp}Z$ vertex has been discussed in ref. [\[35\]](#page-35-7) for the LEPII, in ref. [\[36](#page-35-8)] for the Tevatron in refs. [\[37](#page-35-9)[–40\]](#page-35-10) for the LHC and in ref. [\[41](#page-35-11)] for future linear colliders.

3 Constraints

In this section, we discuss constraints on the parameter space of the GM model. First, we consider the theoretical constraints from perturbative unitarity and vacuum stability. Secondly, as experimental constraints, we consider the $Zb\bar{b}$ data and other B physics data.

3.1 Perturbative unitarity and vacuum stability bounds

The perturbative unitarity bound for the GM model has been studied in ref. [\[42](#page-35-12)] and can be directly applied to our analysis. Before doing so, we will make a change in the parameterization. This is because eqs. (2.18) suggest apparent divergences in $\lambda_{2,3,4}$ in the limit $v_{\Delta} \ll v$. However, this is only an artefact that can be avoided by reparameterization.

We therefore select the following parameterization

$$
m_{H_1}^2 = \frac{1}{2} \left(3m_{H_3}^2 - m_{H_5}^2 + 3s_H^2 \bar{M}^2 \right), \quad M_1^2 = \frac{1}{2} \left(3m_{H_3}^2 - m_{H_5}^2 + M^2 \right), \quad M_2^2 = M^2, \tag{3.1}
$$

in terms of which all the dimensionless couplings can be rewritten for $\sin \alpha = 0$ as

$$
\lambda_1 = \frac{m_h^2}{8v^2c_H^2}, \qquad \lambda_2 = \frac{m_{H_3}^2 - m_{H_5}^2 + M^2 + \bar{M}^2}{2v^2}, \qquad \lambda_3 = \frac{m_{H_5}^2 - M^2}{v^2},
$$
\n
$$
\lambda_4 = \frac{m_{H_3}^2 + m_{H_5}^2 - M^2}{4v^2}, \qquad \lambda_5 = \frac{m_{H_3}^2 - m_{H_5}^2 + M^2}{v^2}.
$$
\n(3.2)

It is seen that the v_{Δ} dependence drops out in $\lambda_{2,3,4}$ and no divergent λ 's appear even when $v_{\Delta} \ll v$.

For the vacuum stability condition, we require that the potential is bounded from below in any direction with large scalar fields. This condition imposes constraints on the dimensionless coupling constants $\lambda_1, \ldots, \lambda_5$. In the GM model, we then derive the following inequalities

$$
\lambda_1 > 0, \qquad \lambda_2 + \lambda_3 > 0, \qquad \lambda_2 + \frac{1}{2}\lambda_3 > 0, \qquad -|\lambda_4| + 2\sqrt{\lambda_1(\lambda_2 + \lambda_3)} > 0, \n\lambda_4 - \frac{1}{4}|\lambda_5| + \sqrt{2\lambda_1(2\lambda_2 + \lambda_3)} > 0.
$$
\n(3.3)

They have taken into account the positivity of all combinations of two non-zero scalar fields, as have been discussed in ref. [\[43\]](#page-35-13) for the HTM.

Figure [1](#page-10-0) shows the regions excluded by the unitarity and the vacuum stability constraints for the case of $m_{H_3} = 150 \,\text{GeV}$ and $v_{\Delta} = 1 \,\text{MeV}$. The left, center and right plots show the cases for $M=0$, 300, 350 GeV, respectively. For the unitarity bound, we consider the S-wave amplitudes for elastic scatterings of two scalar boson states and require their absolute values of the eigenvalues to be less than 1. It is observed that the allowed regions by the unitarity bound for larger M is smaller than those for smaller M . This is because the λ_2 coupling increases as \overline{M} becomes larger. In fact, the excluded regions are determined by the following unitarity condition [\[42\]](#page-35-12);

$$
\left| 12\lambda_1 + 22\lambda_2 + 14\lambda_3 \pm \sqrt{(12\lambda_1 - 22\lambda_2 - 14\lambda_3)^2 + 144\lambda_4^2} \right| < 16\pi. \tag{3.4}
$$

Figure 1. Constraints from the unitarity and vacuum stability in the $M-m_{H_5}$ plane. In all the plot, the uncolored regions are allowed, and the 3-plet Higgs mass is taken to be 150 GeV, $v_{\Delta} = 1 \,\text{MeV}$ and $\alpha = 0$. Blue, gray and pink shaded regions are respectively excluded by the vacuum stability bound, unitarity bound and a negative singlet Higgs mass $(m_H, < 0)$. The left, center and right plot show the case of $\overline{M} = 0$, 300 GeV and 350 GeV, respectively.

Figure 2. Constraints from the unitarity and vacuum stability in the $M-m_{H_5}$ plane. In all the plot, the uncolored regions are allowed, and the 3-plet Higgs mass is taken to be 300 GeV, $v_{\Delta} = 1 \,\text{MeV}$ and $\alpha = 0$. Blue and pink shaded regions are respectively excluded by the vacuum stability bound and the unitarity bound. The left, center and right plot show the case of $\overline{M} = 0$, 200 GeV and 230 GeV, respectively.

On the other hand, the vacuum stability bound becomes milder as \overline{M} is taken to be a larger value because of the increasing λ_2 coupling. For a fixed value of m_{H_5} and \overline{M} , a larger M value is allowed (excluded) by the unitarity (vacuum stability) bound.

Figure [2](#page-10-1) also shows the regions excluded by the unitarity and the vacuum stability conditions for the case of $m_{H_3} = 300 \,\text{GeV}$ and $v_{\Delta} = 1 \,\text{MeV}$. The allowed regions are much smaller than those in the case of $m_{H_3} = 150 \,\text{GeV}$. The excluded regions from the vacuum stability for smaller (larger) values of M are determined by the third (fourth) inequality in eq. [\(3.3\)](#page-9-2).

In the case of larger v_{Δ} values (e.g., $v_{\Delta} \geq 10 \,\text{GeV}$), the regions excluded by the unitarity (vacuum stability) condition are larger (smaller) compared to the small v_{Δ} case. This is because the λ_1 coupling becomes larger. In addition, the singlet Higgs boson mass gets a larger value, so that the regions excluded due to $m_{H_1} < 0$ are smaller in the larger v[∆] case.

3.2 $Zb\bar{b}$ data

The renormalized $Zb\bar{b}$ vertex is defined by [\[44\]](#page-36-0)

$$
\mathcal{L}_{Zb\bar{b}}=-\frac{e}{s_Wc_W}Z_\mu\bar{b}\gamma^\mu(\bar{g}_b^LP_L+\bar{g}_b^RP_R)b,
$$

where the renormalized coupling $\bar{g}_b^{L,R}$ $b^{L,R}$ can be expressed as

$$
\bar{g}_b^{L,R} = g_b^{L,R} + \delta g_b^{L,R} \, (\text{SM}) + \delta g_b^{L,R} \, (\text{GM}) \text{ with}
$$
\n
$$
g_b^L = I_b - s_W^2 Q_b, \quad g_b^R = -s_W^2 Q_b,
$$
\n(3.5)

where $\delta g_b^{L,R}$ (SM) $(\delta g_b^{L,R}$ (GM)) denote the one-loop corrections to the $Zb\bar{b}$ vertices from the SM (GM) contributions, where the W boson and the NG boson (H_3^{\pm}) are running in the loop, $I_f(Q_f)$ is the third component of the isospin (the electric charge) for the field f, and $s_W = \sin \theta_W$ and $c_W^2 = 1 - s_W^2$. The analytic formulas for $\delta g_b^{L,R}$ (SM) is given in ref. [\[45\]](#page-36-1), and their numerical values are calculated as [\[46](#page-36-2)]

$$
\delta g_b^L \,^{(SM)} = -0.4208, \quad \delta g_b^R \,^{(SM)} = 0.0774. \tag{3.6}
$$

The one-loop correction $\delta g_b^{L(\text{GM})}$ is given in terms of the Passarino-Veltman function [\[48\]](#page-36-3) by

$$
\delta g_b^{L(\text{GM})} = -\frac{e}{s_W c_W} \frac{2 \tan^2 \theta_H m_t^2}{v^2} \frac{1}{16\pi^2}
$$

$$
\times \left[c_{2W} C_{24}(m_b^2, m_Z^2, m_b^2, m_t, m_{H_3}, m_{H_3}) + 2s_W^2 Q_t C_{24}(m_b^2, m_Z^2, m_b^2, m_{H_3}, m_t, m_t) - \frac{1}{2} s_W^2 Q_t \right.
$$

+
$$
m_t^2 (I_t - s_W^2 Q_t) C_0(m_b^2, m_Z^2, m_b^2, m_{H_3}, m_t, m_t) - (I_b - s_W^2 Q_b) B_1(m_b^2, m_t, m_{H_3}) \right].
$$
 (3.7)

On the other hand, $\delta g_b^{R(\text{GM})}$ can be neglected because the corrections are proportional to the bottom quark mass [see eq. (2.28)]. We can also neglect the contributions from H_3^0 loop diagrams for the same reason. The renormalized couplings $\bar{g}_h^{L,R}$ $b^{L,R}$ can be compared to the experimental value of R_b^{exp} $_b^{\rm exp}\;[47]$ $_b^{\rm exp}\;[47]$ $_b^{\rm exp}\;[47]$

$$
R_b^{\text{exp}} = 0.21629 \pm 0.00066. \tag{3.8}
$$

In figure [3,](#page-12-0) we show the excluded parameter space in the m_{H_3} - v_{Δ} plane using the R_b data in eq. [\(3.8\)](#page-11-2). Basically, the upper bound on v_{Δ} increases monotonically with m_{H_3} . The 2σ bound is about 25 GeV more relaxed than the 1σ bound over the considered range. We note in passing that the constraint of the $b \to s\gamma$ data for the GM model is similar to that in the Type-I 2HDM [\[49,](#page-36-5) [50](#page-36-6)] and is milder than the R_b constraint.

4 Higgs decays

In this section, we discuss the decay of the triplet-like Higgs bosons, namely the 5-plet Higgs bosons H_5 (= $H_5^{\pm\pm}$, H_5^{\pm} or H_5^0), 3-plet Higgs bosons H_3 (= H_3^{\pm} or H_3^0) and the singlet Higgs boson H_1^0 . Decay branching ratios of the Higgs bosons depend on the mass

Figure 3. Constraint from the R_b data given in eq. [\(3.8\)](#page-11-2) on v_{Δ} as a function of m_{H_3} . The region above the black (red) line is excluded at 1σ (2σ) level.

parameters m_{H_5} , m_{H_3} and m_{H_1} , the VEV of the triplet field v_{Δ} , and the mixing angle α . The mass of the SM-like Higgs boson h is fixed at 125 GeV. Using the mass relation given in eq. [\(2.20\)](#page-7-1), we can treat m_{H_1} as an dependent parameter determined by m_{H_3} and m_{H_5} . Hereafter, we take $\Delta m \equiv m_{H_3} - m_{H_5}$, m_{H_3} and v_{Δ} as the input parameters, and assume $\alpha = 0$ for simplicity. Once we apply the mass relation, there are three different patterns of masses for the triplet-like Higgs bosons. In the case of $\Delta m = 0$, all the masses of the triplet-like Higgs bosons are degenerate: $m_{H_5} = m_{H_3} = m_{H_1}$, whereas in the case of $\Delta m > 0 \; (\Delta m < 0)$, the mass spectrum is then $m_{H_1} > m_{H_3} > m_{H_5} \; (m_{H_5} > m_{H_3} > m_{H_1})$.

First, we consider the decays of the 5-plet Higgs bosons. In the case of $\Delta m \geq 0$, the 5-plet Higgs bosons can decay into weak gauge boson pairs or lepton pairs depending on the magnitude of v_{Δ} . When $\Delta m < 0$, the 5-plet Higgs bosons can decay into a 3-plet Higgs boson and a gauge boson, such as $H_5^{++} \to W^+ H_3^+$ and $H_5^+ \to W^+ H_3^0$, in addition to the two decay modes allowed in the case of $\Delta m \geq 0$.

In figure [4,](#page-13-0) the decay branching ratios of H_5^{++} , H_5^+ and H_5^0 are shown as a function of v_{Δ} in the case of $m_{H_3} = 150 \,\text{GeV}$. When $\Delta m = 0$ (upper row), the main decay modes of H_5^{++} , H_5^+ and H_5^0 change from $\ell^+\ell^+$, $\ell^+\nu$, and $\nu\nu$ to W^+W^+ , W^+Z , and W^+W^- or ZZ at around $v_{\Delta} = 10^{-3} \text{ GeV}$, respectively. Here H_5^0 decays more dominantly into $W^+ W^$ than ZZ because of the mass threshold effect. When $\Delta m = -50$ GeV (lower row) and for the wide range of $10^{-8} \lesssim v_{\Delta} \lesssim 1 \,\text{GeV}$, the main decay mode of H_5^{++} is $H_3^+W^+$, those of H_5^+ are H_3^+Z and $H_3^0W^+$, and those of H_5^0 are $H_3^{\pm}W^{\mp}$ and H_3^0Z .

Figure [5](#page-13-1) shows the decay branching ratios of the 5-plet Higgs bosons for m_{H_3} = 300 GeV. The general behavior here is roughly the same as the case with $m_{H_3} = 150 \,\text{GeV}$. The crossing point for the main decay modes in each of the upper plots $(\Delta m = 0)$ slightly shifts to a smaller v_{Δ} ($\simeq 10^{-4} \,\text{GeV}$).

Figure [6](#page-14-0) shows the contour plots of the decay branching ratios of H_5^{++} , H_5^+ and H_5^0 on the v_∆- $|\Delta m|$ plane (with $\Delta m < 0$) for the cases with $m_{H_3} = 150 \,\text{GeV}$ (upper plots) and $m_{H_3} = 300 \,\text{GeV}$ (lower plots). There are always three distinct regions in this plane. In

Figure 4. The decay branching ratios of H_5^{++} (left), H_5^{+} (center) and H_5^{0} (right) as a function of v_{Δ} . We take $m_{H_3} = 150 \,\text{GeV}, m_h=125 \,\text{GeV}$ and $\alpha = 0$ in all the plots. The mass difference Δm is taken to be 0 for the upper three plots, and to be −50 GeV for the lower three plots.

Figure 5. Same as figure [4,](#page-13-0) but for $m_{H_3} = 300 \,\text{GeV}$.

Figure 6. Contour plots of the decay branching ratios of H_5^{++} (left column), H_5^{+} (center column) and H_5^0 (right column) on the v_∆- $|\Delta m|$ plane (with $\Delta m < 0$). We take m_h =125 GeV and $\alpha = 0$ in all the plots. The upper (lower) three plots show the case for $m_{H_3} = 150 \,\text{GeV}$ (300 GeV). Each solid (dashed) curve represents the branching ratio of 50% (90%) for the corresponding decay mode indicated by the arrow.

the region of small $|\Delta m|$ and small (large) v_{Δ} , the main decay modes of the 5-plet Higgs bosons are the a pair of leptons (weak bosons). In the region of large $|\Delta m|$, they are a 3-plet Higgs boson and a gauge boson, denoted by H_3V in the plots $(V = W^{\pm}$ or Z), where it is understood that all the possible channels of H_3V should be summed over.

Secondly, we consider the decays of the 3-plet Higgs bosons. The 3-plet Higgs bosons can decay into a pair of fermions through the Yukawa interactions given in eq. [\(2.28\)](#page-8-0) and a pair of leptons through the neutrino Yukawa interaction given in eq. [\(2.26\)](#page-8-1), depending on the value of v_{Δ} in the case of $\Delta m \simeq 0$. In the region dominated by fermionic decays, the main decay mode strongly depends on m_{H_3} . When m_{H_3} is smaller than the top quark mass, H_3^+ (H_3^0) mainly decays into $\tau^+\nu$ or $c\bar{s}$ ($b\bar{b}$), whereas in the case of $m_t < m_{H_3} < 2m_t$, H_3^+ (H_3^0) decays into $t\bar{b}$ ($b\bar{b}$). Furthermore, when m_{H_3} is larger than $2m_t$, H_3^0 decays dominantly into $t\bar{t}$, and H_3^+ still mainly into $t\bar{b}$. In addition, the 3-plet Higgs bosons can decay into the SM-like Higgs boson h and a gauge boson, e.g., $H_3^+ \rightarrow hW^+$ and $H_3^0 \rightarrow hZ$ if m_{H_3} is larger than m_h . When $\Delta m > 0$ ($\Delta m < 0$), the 3-plet Higgs bosons can decay into a gauge boson and a 5-plet (singlet) Higgs boson.

In figure [7,](#page-15-0) the decay branching ratios of H_3^+ and H_3^0 are shown as a function of v_{Δ} for $m_{H_3} = 150 \,\text{GeV}$. The mass difference Δm is taken to be 0, 50 GeV and -50 GeV in the top, middle and bottom plots, respectively. From the top two figures, it is seen that the dominant decay modes of H_3^+ (H_3^0) change from $\ell^+\nu$ ($\nu\nu$) to $\tau^+\nu$ or $c\bar{s}$ ($b\bar{b}$) at

Figure 7. Decay branching ratios of H_3^+ (left column) and H_3^0 (right column) as a function of v_{Δ} . We take $m_{H_3} = 150 \,\text{GeV}, m_h = 125 \,\text{GeV}$ and $\alpha = 0$ in all the plots. The mass difference Δm is fixed to 0 (top plots), 50 GeV (middle plots) and −50 GeV (bottom plots), respectively.

around $v_{\Delta} = 10^{-3}$ GeV. In the case of $\Delta m = 50$ GeV (middle plots) and for a wide range $10^{-8} \lesssim v_{\Delta} \lesssim 10 \,\text{GeV}$, the 3-plet Higgs bosons mainly decay into a 5-plet Higgs boson and a weak gauge boson, i.e., $H_3^+ \to H_5^{++}W^-$, $H_3^+ \to H_5^+Z$ and $H_3^+ \to H_5^0W^+$ for H_3^+ decays and $H_3^0 \rightarrow H_5^{\pm} W^{\mp}$ and $H_3^0 \rightarrow H_5^0 Z$ for H_3^0 decays. On the other hand, in the case of $\Delta m = -50 \,\text{GeV}$ (bottom plots), the main decay modes of H_3^+ (H_3^0) are $H_1^0 W^+$ ($H_1^0 Z$) in the range of $10^{-8} \lesssim v_{\Delta} \lesssim 10 \,\text{GeV}.$

Figure [8](#page-16-0) shows the decay branching ratios of H_3^+ and H_3^0 as a function of v_{Δ} for $m_{H_3} = 300 \,\text{GeV}$. The mass difference Δm is taken to be 0, 50 GeV and $-50 \,\text{GeV}$ in the

Figure 8. Same as figure [7,](#page-15-0) but for $m_{H_3} = 300 \,\text{GeV}$.

top, middle and bottom plots, respectively. When $\Delta m = 0$ (top plots), the main decay modes of H_3^+ (H_3^0) change from $\ell^+\nu$ ($\nu\nu$) to $t\bar{b}$ and hW^+ (hZ) at $v_{\Delta} \simeq 10^{-4}$ GeV. When $\Delta m = 50 \,\text{GeV}$ (middle plots) and $\Delta m = -50 \,\text{GeV}$ (bottom plots), the main decay modes are the same as in the case of $m_{H_3} = 150 \,\text{GeV}$ in the range of $10^{-7} \lesssim v_\Delta \lesssim 1 \,\text{GeV}$.

In figure [9,](#page-17-0) we give the contour plots of the decay branching ratios of H_3^+ and H_3^0 for $m_{H_3} = 150 \,\text{GeV}$. The mass difference Δm is taken to be positive (negative) in the upper (lower) two figures. In this figure, $BR(H_3^+ \rightarrow H_5V)$ and $BR(H_3^0 \rightarrow H_5V)$ denote the sums of the decay branching ratios of the modes with a 5-plet Higgs boson and a gauge boson. BR($H_3^+ \to ff$) and BR($H_3^0 \to ff$) denote the sum of the decay branching ratios of $H_3^+ \to \tau^+\nu$ and $H_3^+ \to c\bar{s}$ and that of $H_3^0 \to b\bar{b}$ and $H_3^0 \to \tau^+\tau^-$, respectively. Similar

Figure 9. Contour plots of the decay branching ratios of H_3^+ (left column) and H_3^0 (right column) on the v_∆- Δm plane. We take $m_{H_3} = 150 \,\text{GeV}, m_h=125 \,\text{GeV}$ and $\alpha = 0$ in all the plots. The upper (lower) two plots show the case with $\Delta m > 0$ ($\Delta m < 0$). Each solid (dashed) curve represents the branching ratio of 50% (90%) for the corresponding decay mode indicated by the arrow.

to figure [6,](#page-14-0) it is seen that there are three distinct regions in this plane. In the small Δm and small (large) v_{Δ} region, the main decay modes are $\ell^+\nu$ ($\tau^+\nu$) for H_3^+ and $\nu\nu$ ($b\bar{b}$) for H_3^0 . On the other hand, in the large Δm region, the decay modes associated with a 5-plet (singlet) Higgs boson dominate in the case of $\Delta m > 0$ ($\Delta m < 0$). We notice that the regions where the H_5V decay is dominant are wider than the corresponding one where the H_1^0V decay is dominant. This is because of a larger number of decay modes in H_5V .

Figure [10](#page-18-0) shows the contour plots of the branching ratios of the 3-plet Higgs bosons for $m_{H_3} = 300 \,\text{GeV}$. In the plots of the left column, there is no dashed curve corresponding to the branching ratio of 90% for the $H_3^+ \to t\bar{b}$ decay mode. This is because the $H_3^+ \to hW^+$ decay mode is also kinematically allowed at the same time when the $H_3^+ \to t\bar{b}$ is open, and the former amounts to around 30%.

Figure 10. Same as figure [9,](#page-17-0) but for $m_{H_3} = 300 \,\text{GeV}$.

We here comment on the decays of the singlet Higgs boson H_1^0 . When we take $\alpha = 0$, the decay property of H_1^0 is similar to that of H_5^0 . In the case of $\Delta m \leq 0$, H_1^0 can decay into $\nu\nu$ (W⁺W⁻ or ZZ) for smaller (larger) values of v_{Δ} . When $\Delta m > 0$, H_1^0 can decay into a 3-plet Higgs boson and a weak gauge boson. If $\alpha \neq 0$, H_1^0 can mix with h and can thus decay into fermion pairs via the mixing in addition to the above-mentioned modes.

Throughout this section, the decay properties of the 5-plet Higgs bosons and the 3-plet Higgs bosons can be separately considered for four different regions in the v_Δ - Δm plane, as schematically shown in figure [11.](#page-19-1) In Region I, all the triplet-like Higgs bosons mainly decay leptonically:

$$
H_5^{++} \to \ell^+ \ell^+, \qquad H_5^+ \to \ell^+ \nu, \qquad H_3^0 \to \nu \nu, H_3^+ \to \ell^+ \nu, \qquad H_3^0 \to \nu \nu.
$$
 (4.1)

In this region, the mass of the 5-plet Higgs bosons is constrained to be $m_{H_5} \gtrsim 400 \,\text{GeV}$ by the search at the LHC for doubly-charged Higgs bosons decaying into same-sign dileptons [\[26](#page-34-7), [27](#page-35-0)]. In Region II, the 5-plet Higgs bosons mainly decay into the weak gauge boson

Figure 11. Four regions are schematically shown on the v_{Δ} - $|\Delta m|$ plane.

pairs, while the 3-plet Higgs bosons decay into the fermion pairs. When the mass of the 3-plet Higgs bosons is less than the top quark mass, the main decay modes are

$$
H_5^{++} \to W^+W^+, \qquad H_5^+ \to W^+Z, \qquad H_5^0 \to W^+W^-/ZZ, H_3^+ \to \tau^+\nu/c\bar{s}, \qquad H_3^0 \to b\bar{b}.
$$
 (4.2)

For Region III and Region IV, one has to separately consider the cases whether the sign of Δm is positive or negative. In the case of $\Delta m > 0$, the 5-plet Higgs bosons mainly decay into the lepton pairs (weak gauge boson pairs) in Region III (Region IV). The 3-plet Higgs bosons mainly decay into a 5-plet Higgs boson and a weak gauge boson:

$$
H_5^{++} \to \ell^+ \ell^+ (W^+ W^+), \qquad H_5^+ \to \ell^+ \nu (W^+ Z), \qquad H_5^0 \to \nu \nu (W^+ W^- / ZZ),
$$

\n
$$
H_3^+ \to H_5^{++} W^- / H_5^+ Z / H_5^0 W^+, \qquad H_3^0 \to H_5^{\pm} W^{\mp} / H_5^0 Z. \tag{4.3}
$$

In the case of $\Delta m < 0$, the main decay modes in both Region III and Region IV are

$$
H_5^{++} \to H_3^+W^+, \qquad H_5^+ \to H_3^+Z/H_3^0W^+, \qquad H_5^0 \to H_3^{\pm}W^{\mp}/H_3^0Z
$$

$$
H_3^+ \to H_1^0W^+, \qquad H_3^0 \to H_1^0Z.
$$
 (4.4)

5 Phenomenology at the LHC

In this section, we discuss how the custodial symmetry of the GM model can be tested at the LHC. There are characteristic features of the triplet-like Higgs bosons that mainly originate from the triplet field Δ of the model. (1) The masses of the Higgs bosons belonging to the same $SU(2)_V$ multiplet are the same. (2) The 5-plet and the singlet Higgs bosons have the Gauge-Gauge-Scalar type of couplings as listed in table [3,](#page-32-1) but not the Yukawa couplings given in eq. [\(2.28\)](#page-8-0), while the 3-plet Higgs bosons have the Yukawa couplings, but not the Gauge-Gauge-Scalar type of couplings. These features can be used to test the custodial symmetry of the GM model.

As is discussed in the previous section, it is important to study the decay pattern of the triplet-like Higgs bosons. In particular, feature (2) mentioned above can be most clearly tested in Region II because the 5-plet (3-plet) Higgs bosons mainly decay into weak gauge boson pairs (fermion pairs) in this region. In the following discussion, we focus on Region II and the detectability of the 5-plet and 3-plet Higgs bosons.

5.1 Production modes

There are several production modes for the 5-plet Higgs bosons H_5 and the 3-plet Higgs bosons H_3 , as listed below. Throughout this section, q, q', Q, Q' and those with bars denote light quarks and anti-quarks.

1. The Drell-Yan process

 H_5 and H_3 can be produced in pairs via γ and Z , e.g., $pp \rightarrow H_5H_5$ and $pp \rightarrow H_3H_3$. The cross section is determined by the gauge coupling as well as the Higgs masses m_{H_5} and m_{H_3} , independent of the value of v_{Δ} .

2. The mixed Drell-Yan (mDY) process

 H_5 and H_3 can be produced at the same time, e.g., $pp \rightarrow H_5H_3$, which we call the mixed Drell-Yan (mDY) process to be separated from the usual Drell-Yan process mentioned above. The cross section is proportional to c_H^2 , and is thus relatively suppressed in comparison with the Drell-Yan process, especially in the large v_{Δ} case.

3. The weak vector boson fusion (VBF) process

The single production of H_5 occurs via the $qQ \rightarrow H_5$ process. The cross section is proportional to v^2 , so that this mode can be important in the large v^2 case.

4. The weak vector boson associated process

In addition to the VBF process, H_5 can also be produced in association with a weak gauge boson, e.g., $q\bar{q}' \rightarrow H_5V$. The cross sections of such modes are proportional to v_{Δ}^2 as for the VBF production mode. Thus, this mode can also become important when the VBF process is important.

5. The Yukawa process

 H_3 can be produced through the Yukawa interactions given in eq. (2.28) as the gluon fusion process for the SM Higgs boson: $gg \to H_3^0$. There are t-channel H_3^{\pm} and H_3^0 production modes: $gb \to tH_3^-$ and $gb \to bH_3^0$. These production cross sections are proportional to $\tan^2 \theta_H$.

6. The top quark decay

When m_{H_3} is smaller than the top quark mass, H_3^{\pm} can be produced from the top quark decay. The decay rate of the $t \to bH_3^{\pm}$ depends on $\tan^2 \theta_H$.

Among these production processes, channels 3 and 4 can be useful to discriminate the GM model from the others with doubly-charged Higgs bosons and to test the mass degeneracy of H_5 . In the HTM, for example, the doubly-charged Higgs boson can in

Figure 12. Production cross sections of the 5-plet Higgs bosons in various processes as a function of m_{H_5} . The upper-left, upper-right, and bottom plots show the production cross sections for $H_5^{\pm\pm}$, H_5^{\pm} , and H_5^0 , respectively. In all the plots, we take $v_{\Delta} = 20 \,\text{GeV}$ and $\Delta m = 0$. The LHC collision energy is assumed to be 8 TeV (dashed curves) and 14 TeV (solid curves).

principle be produced via the VBF and the vector boson associated processes. However, these cross sections are much suppressed due to the tiny triplet VEV required by the electroweak rho parameter. In the GM model, v_{Δ} can be of order 10 GeV, so that these production processes become useful. The mDY process is also a unique feature of the GM model because the Higgs bosons H_5 and H_3 having different decay properties are produced at the same time. In particular, when Region II is realized, the main decay modes of these two Higgs bosons are distinctly different. Thus, this process can be useful not only to test the mass degeneracy of H_3 but also to distinguish the model from the others also having doubly-charged and/or singly-charged Higgs bosons.

In figure [12,](#page-21-0) production cross sections of the 5-plet Higgs bosons from channels 2, 3, and 4 are shown as a function of m_{H_5} for the LHC running at 8 and 14 TeV. We take $v_{\Delta} = 20 \,\text{GeV}$ and $\Delta m = 0$ as an example in all the plots. It is noted that the dominant production mechanism is the VBF process for a sufficiently large m_{H_5} .

5.2 Signal and background analysis

We will first discuss the VBF process and the vector boson associated process to study the mass degeneracy among $H_5^{\pm \pm}$, H_5^{\pm} and H_5^0 . Then we turn to the mDY process.

Let us consider the case with $m_{H_3} = 150 \,\text{GeV}$, $\Delta m = 10 \,\text{GeV}$ (i.e., $m_{H_5} = 140 \,\text{GeV}$) and $v_{\Delta} = 20 \,\text{GeV}$ as an example in Region II. In this case, the 5-plet Higgs bosons decay into gauge boson pairs almost 100% (the branching fractions of $H_5^0 \to W^+W^-$ and $H_5^0 \to ZZ$ being 67% and 33%, respectively). On the other hand, H_3^{\pm} decays to $\tau^{\pm} \nu$ at 66% and cs at 29%, and H_3^0 decays to $b\bar{b}$ at 89%. We note that the branching fraction of $t \to H_3^+ b$ here is around 0.4%. The upper limit of the top quark decay into a charged Higgs boson and the bottom quark is 2-3% in the case where the charged Higgs boson mass is between 80 and 160 GeV, under the assumption that the charged Higgs boson decays to $\tau\nu$ at 100% [\[51](#page-36-7)]. Thus, the selected parameter set is allowed by the constraint from the top quark decays. The signal events from the VBF production processes for the 5-plet Higgs bosons are given by

$$
qQ \to H_5^{\pm \pm} q'Q' \to W^{\pm}W^{\pm}jj,
$$

\n
$$
qQ \to H_5^{\pm} q'Q' \to W^{\pm} Zjj,
$$

\n
$$
qQ \to H_5^0 q'Q' \to W^{\pm}W^{\mp}jj/ZZjj.
$$
\n(5.1)

From the vector boson associated processes, we have the following events

$$
q\bar{q}' \to H_5^{\pm\pm}W^{\mp} \to W^{\pm}W^{\pm}jj
$$

\n
$$
q\bar{q} \to H_5^{\pm}W^{\mp} \to W^{\pm}Zjj, \qquad q\bar{q}' \to H_5^{\pm}Z \to W^{\pm}Zjj,
$$

\n
$$
q\bar{q} \to H_5^0Z \to W^+W^-jj/ZZjj, \qquad q\bar{q}' \to H_5^0W^{\pm} \to W^+W^-jj/ZZjj, \qquad (5.2)
$$

where the associated weak gauge bosons are assumed to decay hadronically so that they have the same final states as the VBF process. Moreover, we consider the case where the weak gauge bosons produced from the decay of $H₅$ decay leptonically. Then the final states of the signal events have same-sign (SS) dileptons plus dijets and missing transverse energy $(\ell^{\pm} \ell^{\pm} j j \mathcal{E}_T)$ for the $H_5^{\pm \pm}$ production mode, where ℓ^{\pm} denotes collectively the light leptons e^{\pm} and μ^{\pm} hereafter. The final state of the H_5^{\pm} production mode includes trileptons plus dijets and missing transverse energy $(\ell^{\pm} \ell^{\pm} \ell^{\mp} j j \not\!\! E_T)$, while that for the H_5^0 production mode has opposite-sign (OS) dileptons plus dijets and missing transverse energy $(\ell^{\pm} \ell^{\mp} j j \not\equiv_T)$. The corresponding background events for these signal events are from the $W^{\pm}W^{\pm}jj$ for the $H_5^{\pm\pm}$ production, $W^{\pm}Zjj$ for the H_5^{\pm} production, and $t\bar{t}$, $W^{\pm}W^{\mp}jj$ and $ZZjj$ for the H_5^0 production.

We simulate the signal and the background event rates by using MadGraph 5 [\[52](#page-36-8)] at the parton level for the cases where the LHC operates at the center-of-mass (CM) energy \sqrt{s} of 8 TeV and 14 TeV. We impose the following basic kinematic cuts

$$
p_T^j > 20 \text{ GeV}, \quad p_T^\ell > 10 \text{ GeV}, \quad |\eta^j| < 5, \quad |\eta^\ell| < 2.5, \quad \Delta R^{jj} > 0.4,\tag{5.3}
$$

where p_7^j $\frac{d}{dt}$ and p_T^{ℓ} are the transverse momenta of the jet and the lepton, respectively, η^j and η^{ℓ} are the pseudorapidities of the jet and the lepton, respectively, and ΔR^{jj} is the distance

	$\ell^{\pm} \ell^{\pm} j j \not\!{E}_T$			$\ell^{\pm} \ell^{\pm} \ell^{\mp} j j \not\!\!E_T$			$\ell^{\pm} \ell^{\mp} j j \not\!E_T$		
Cuts	$H_5^{\pm\pm}jj$	$W^{\pm}W^{\pm}jj$	$\mathcal{S}% _{CS}^{ab}(A)$	$H_5^{\pm}jj$	$W^{\pm} Z j j$	$\mathcal{S}% _{CS}^{ab}(A)$	H_5^0jj	$t\bar{t}/VVjj$	$\mathcal{S}% _{CS}^{ab}(A)$
Basic	3.71	3.48	13.8	0.61	45.9	0.89	1.15	4.39×10^{3}	0.17
	(8.72)	(8.13)	(21.2)	(1.60)	(1.39×10^{2})	(1.35)	(2.76)	(1.77×10^{4})	(0.21)
$\Delta \eta^{jj}$	1.82	0.20	12.8	0.33	4.42	1.51	0.51	30.7	0.91
	(5.68)	(0.65)	(22.6)	(0.98)	(15.6)	(2.41)	(1.42)	(1.99×10^{2})	(1.00)
M_T	1.80	0.05	13.2	0.33	0.07	5.22	0.48	11.4	1.39
	(5.58)	(0.12)	(23.4)	(0.98)	(0.46)	(8.17)	(1.36)	(67.4)	(1.64)
b -jet veto							0.48	1.82	3.16
							(1.36)	(10.8)	(3.90)

Table 1. Signal and background cross sections in units of fb after each kinematic cut, along with the significance S defined by eq. [\(5.4\)](#page-23-0) based on an integrated luminosity of 100 fb^{-1} . The numbers without (with) parentheses correspond to the case with a CM energy of 8 TeV (14 TeV). The signal cross section includes contributions from both the VBF production and the vactor boson associated production processes. For the $\ell^{\pm} \ell^{\mp} j j \not{\pounds}_{T}$ events, we further impose the requirement of the b-jet veto for each jet to reduce the background, where the b-tagging efficiency is take to be 0.6 [\[56\]](#page-36-9).

between the two jets. The cross sections for the signal and background events are listed in table [1,](#page-23-1) where the signal cross section includes contributions from the VBF production and the vector boson associated production. An integrated luminosity of 100 fb−¹ is assumed in the simulations. In this table, the signal significance is defined by

$$
S = S/\sqrt{S+B},\tag{5.4}
$$

where S and B are the numbers of the signal and background events, respectively. The significance of the $\ell^{\pm} \ell^{\pm} j j \not\llbracket_T$ event from the $H_5^{\pm \pm}$ production process exceeds 5 even using simply the basic cuts. However, the significances for the remaining two events from the H_5^{\pm} and H_5^0 production processes are less than 1. For the $\ell^{\pm}\ell^{\mp}jj\rlap{\,/}E_T$ event, in particular, the background is larger than the signal by 3 to 4 orders of the magnitude because of the huge $t\bar{t}$ background.

To improve the significance, we need to impose additional kinematic cuts. Figure [13](#page-24-0) shows the distributions of the pseudorapidity gap $\Delta \eta^{jj}$ for the dijet system and the trans-verse mass [\[53](#page-36-10)[–55](#page-36-11)] in the leptons plus missing transverse energy system for $\sqrt{s} = 8 \,\text{TeV}$ and the integrated luminosity of 100 fb^{-1} . Explicitly, these two kinematical quantities are defined by

$$
M_T^2 \equiv \left[\sqrt{M_{\rm vis}^2 + (\mathbf{p}_T^{\rm vis})^2} + |\mathbf{p}_T| \right]^2 - \left[\mathbf{p}_T^{\rm vis} + \mathbf{p}_T \right]^2, \tag{5.5}
$$

$$
\Delta \eta^{jj} \equiv |\eta^{j_1} - \eta^{j_2}|,\tag{5.6}
$$

where M_{vis} and \bm{p}_T^{vis} are the invariant mass and the vector sum of the transverse momenta of the charged leptons, respectively, and $p\llap/_T$ is the missing transverse momentum determined

Figure 13. $\Delta \eta^{jj}$ and M_T distributions for the signal and background events. The top, middle and bottom plots show these distributions for the $\ell^{\pm} \ell^{\pm} j j \cancel{E}_T$, $\ell^{\pm} \ell^{\pm} \ell^{\mp} j j \cancel{E}_T$ and $\ell^{\pm} \ell^{\mp} j j \cancel{E}_T$ events, respectively. The distributions for the signal events are divided into those from the VBF process and vector boson associated process (green dashed curve), the mDY process (blue dashed curve) and the sum of them (red solid curve). The bin size for the $\Delta \eta_{ij}$ (M_T) distribution is taken to be 0.2 (5 GeV). The integrated luminosity and the CM energy are assumed to be 100 fb−¹ and 8 TeV, respectively.

by the negative sum of visible momenta in the transverse direction. In figure [13,](#page-24-0) the distributions of $\Delta \eta^{jj}$ and M_T for the signal events from the VBF process plus vector boson associated process and the mDY process are separately indicated by dotted lines. The latter production mode will be discussed in details later. A significant feature of the VBF process is that the two external quark jets are almost along the beam direction and carry most of the energy of the collider protons. Therefore, they are mostly detected in the forward regions. This is seen in the $\Delta \eta^{jj}$ distribution of figure [13.](#page-24-0) The end point in the M_T distribution of signals rests at around 140 GeV, corresponding to the mass of the 5-plet Higgs boson.

According to the above-mentioned observations, we find the following additional kinematic cuts useful in further reducing the backgrounds:

$$
\Delta \eta^{jj} > 3.5 \ \ (>4.0 \ \text{for} \ \ \ell^{\pm} \ell^{\mp} j j \not{\!\! E}_T), \quad 50 < M_T < 150 \text{ GeV}. \tag{5.7}
$$

The cross sections for the signals and backgrounds in each step of the kinematic cuts are listed in table [1.](#page-23-1) After making the first two cuts, the significances of the events from $H_5^{\pm\pm}$ and H_5^{\pm} achieve 13.2 and 5.2, respectively. However, the significance of the events from H_5^0 is around 1.4. We further require that events with at least one b-jet are tagged and rejected in order to reduce the $t\bar{t}$ background. The b-tagging efficiency is taken to be 0.6 [\[56\]](#page-36-9). By using this cut, the $t\bar{t}$ background events with the final state of $b\bar{b}\ell^+\ell^-\rlap{\,/}E_T$ can be reduced to be 16%. Consequently, the signal significance for the $\ell^+ \ell^- j j \not\!\!E_T$ event can reach 3.16 (3.90) with $\sqrt{s} = 8 \,\text{TeV}$ (14 TeV) after all the cuts discussed above are imposed.

Next, we focus on the mDY production mode discussed in the previous subsection. In order to reconstruct the masses of H_3 Higgs bosons, we consider their hadronic decays, namely $H_3^{\pm} \rightarrow cs$ and $H_3^0 \rightarrow b\bar{b}$. The signal events are

$$
pp \to H_5^{\pm \pm} H_3^{\mp} \to W^{\pm} W^{\pm} cs,pp \to H_5^{\pm} H_3^{\mp} \to W^{\pm} Zcs, \qquad pp \to H_5^{\pm} H_3^0 \to W^{\pm} Zb\bar{b},pp \to H_5^0 H_3^{\pm} \to W^+ W^- cs/ZZcs, \qquad pp \to H_5^0 H_3^0 \to W^+ W^- b\bar{b}/ZZb\bar{b}, \qquad (5.8)
$$

where leptonic decays of the weak gauge bosons from the H_5 decays are also assumed in this analysis. Thus, the final states of the signal events from the mDY process are the same as those from the VBF process as well as the associated process. Its difference from the VBF process is observed in the $\Delta \eta^{jj}$ distribution of the dijet system. In the mDY process, the dijets in the final state come from the decay of the 3-plet Higgs boson, not the external quark jets. According to the plots in the left column of figure [13,](#page-24-0) the events from the mDY process concentrates in the $\Delta \eta^{jj} \lesssim 2.5$ region for all the three cases. On the other hand, the M_T distributions from the mDY process and the VBF plus associated process are almost the same. This is because the leptons plus missing transverse energy system come from the decays of H_5 in both processes. Therefore, we apply the same M_T cut given in eq. [\(5.7\)](#page-25-0) to this analysis, but not the $\Delta \eta^{jj}$ cut. In the analysis of the mDY process, the $\ell^{\pm}\ell^{\mp}jj\rlap{\,/}E_T$ signal events are overwhelmed by the huge background from the $t\bar{t}$ production.

	$\ell^{\pm} \ell^{\pm} j j E_T$		$\ell^{\pm} \ell^{\pm} \ell^{\mp} j j E_T$			
$ $ Cuts $ $	$H_5^{\pm \pm} j j \mid H_5^{\pm \pm} H_3^{\mp} W^{\pm} W^{\pm} j j $		$H_5^{\pm}jj$	$H_5^{\pm} H_3^{\mp,0}$	$W^{\pm}Zii$	
					$ \text{Basic} 3.71 (8.72) 0.72 (1.63) 3.48 (8.13) 15.8 (24.1) 0.61 (1.60) 0.53 (1.21) 45.9 (1.39 \times 10^2) 1.66 (2.36) $	
					M_T 3.65 (8.57) 0.71 (1.60) 1.02 (2.20) 18.8 (28.9) 0.61 (1.60) 0.53 (1.21) 1.16 (3.42)	7.52(11.3)

Table 2. Signal and background cross sections in units of fb after each kinematic cut, along with the significance based on an integrated luminosity of 100 fb^{-1} . The numbers without (with) parentheses correspond to the case with a CM energy of 8 TeV (14 TeV).

Figure 14. Invariant mass distribution for the dijets system. The bin size in this distribution is 5 GeV. The distributions for the signal events are divided into those from the VBF process and vector boson associated process (green dashed curve), the mDY process (blue dashed curve) and the sum of them (red solid curve). The integrated luminosity and the CM energy are assumed to be 100 fb^{-1} and 8 TeV , respectively.

Table [2](#page-26-0) lists the cross sections of the signal and the background events after imposing the basic cut and M_T cut. In addition, the signal significance is given by assuming an integrated luminosity of 100 fb^{-1} . We find that the significances exceed 5 in both cases after imposing the M_T cut.

Figure [14](#page-26-1) show the dijet invariant mass M_{ij} distributions of the signal and the background events. These distributions are plotted after imposing the M_T cut. We can see a peak at around 150 GeV, corresponding to the mass of the 3-plet Higgs bosons, in both the $\ell^{\pm} \ell^{\pm} j j \cancel{E}_T$ and $\ell^{\pm} \ell^{\pm} \ell^{\mp} j j \cancel{E}_T$ events. This suggests that the mass degeneracy between H_3^{\pm} and H_3^0 can be readily established from the mDY process. First, the $\ell^{\pm} \ell^{\pm} j j \not{\pounds}_T$ event comes from the $H_5^{\pm\pm}H_3^+$ production. Thus, the peak at around 150 GeV in the M_{jj} distribution gives the mass of H_3^{\pm} . Secondly, the $\ell^{\pm} \ell^{\pm} \ell^{\mp} j j \not\!{E}_T$ event comes from the $H_5^{\pm} H_3^{\mp}$ and $H_5^{\pm}H_3^0$ production processes. These two production cross sections are almost the same as shown in figure [12.](#page-21-0) Nevertheless, the decay branching fractions of $H_3^{\pm} \to cs$ and $H_3^0 \to b\bar{b}$ are about 30% and 90%, respectively. Thus, the $\ell^{\pm} \ell^{\pm} \ell^{\mp} j j \not\!\!E_{T}$ event mainly comes from the $H_5^{\pm}H_3^0$ production. Therefore, one can conclude that the peak at around 150 GeV in the M_{jj} distribution is the mass of H_3^0 .

6 Higgs to $\gamma\gamma$ and $Z\gamma$ decays

In this section, we discuss the decays of the SM-like Higgs boson h to diphotons and the photon plus Z boson, both of which are loop-mediated processes in the SM. The Higgs to diphoton decay is one of the most important modes in the Higgs boson search at the LHC. According to the current data, the signal strength, defined by (the observed cross section)/(the expected cross section in the SM), of the diphoton mode is 1.6 ± 0.4 at the CMS [\[1\]](#page-33-0) and 1.8 ± 0.5 at the ATLAS [\[2\]](#page-33-1). It is consistent with the SM prediction at the 2σ level. If the observed deviation persists, it may hint at contributions from new charged particles that can couple to the SM Higgs boson. The Higgs decay into the photon and Z boson is also important to determining the structure of the Higgs sector [\[59\]](#page-36-12). The decay rate of this mode is closely related to that of the Higgs to diphoton mode in the sense that particles contributing to the latter generally also contribute to the former. Yet the deviations do not follow the same pattern in general [\[57](#page-36-13)[–59\]](#page-36-12). In the GM model, the doubly-charged Higgs boson $H_5^{\pm\pm}$ as well as the singly-charged Higgs bosons H_5^{\pm} and H_3^{\pm} can contribute to these processes in addition to the W boson and the top quark at the one-loop level. The decay rates of these processes are calculated as

$$
\Gamma(h \to \gamma \gamma) = \frac{G_F \alpha_{em}^2 m_h^3}{128\sqrt{2}\pi^3} \Big| \sum_S Q_S^2 \lambda_{hSS^*} I_0(m_S) + \frac{c_\alpha}{c_H} \sum_f Q_f^2 N_c^f I_{1/2} + (c_\alpha c_H + \frac{2\sqrt{6}}{3} s_\alpha s_H) I_1 \Big|^2, \tag{6.1}
$$

$$
\Gamma(h \to Z\gamma) = \frac{\sqrt{2}G_F \alpha_{\rm em}^2 m_h^3}{128\pi^3} \left(1 - \frac{m_Z^2}{m_h^2}\right)^3
$$

$$
\times \left| \sum_S Q_S \lambda_{hSS^*} g_{ZSS^*} J_0(m_S) + \frac{c_\alpha}{c_H} \sum_f Q_f N_f^c J_{1/2} + (c_\alpha c_H + \frac{2\sqrt{6}}{3} s_\alpha s_H) J_1 \right|^2, \tag{6.2}
$$

where $N_c^f = 3$ (1) for $f = q$ (ℓ), and the loop functions $I_{0,1/2,1}$ for $h \to \gamma\gamma$ and $J_{0,1/2,1}$ for $h \to Z\gamma$ are given in appendix C. The summation over S includes H_5^{++} , H_5^+ , and H_3^+ . In eqs. [\(6.1\)](#page-27-1) and [\(6.2\)](#page-27-2), the couplings between h and the charged Higgs bosons λ_{hSS^*} are given by

$$
\lambda_{hH_{5}^{+}+H_{5}^{-}} = \frac{2}{v^{2}} \Biggl\{ c_{H} c_{\alpha} (3m_{H_{3}}^{2} - 2M_{1}^{2}) + \sqrt{\frac{2}{3}} \frac{s_{\alpha}}{s_{H}} \Bigl[2m_{H_{5}}^{2} + m_{h}^{2} - M_{2}^{2} + 3c_{H}^{2} (M_{1}^{2} - 2m_{H_{3}}^{2}) \Bigr] \Biggr\},\tag{6.3}
$$

$$
\lambda_{hH_{5}^{+}H_{5}^{-}} = -\lambda_{hH_{5}^{++}H_{5}^{--}} \tag{6.4}
$$

$$
\lambda_{hH_3^+H_3^-} = -\frac{1}{v^2} \left[\frac{c_\alpha}{c_H} \left(2c_H^2 m_{H_3}^2 + s_H^2 m_h^2 \right) + \frac{2\sqrt{6}}{3} \frac{s_\alpha}{s_H} \left(2s_H^2 m_{H_3}^2 + c_H^2 m_h^2 - M_1^2 \right) \right], \tag{6.5}
$$

and those between the Z boson and the charged Higgs bosons g_{ZSS^*} are given by

$$
g_{ZH_5^{++}H_5^{-}} = \frac{g}{c_W}(1 - 2s_W^2), \quad g_{ZH_5^+H_5^-} = g_{ZH_3^+H_3^-} = -\frac{1}{2}g_{ZH_5^{++}H_5^{-}}.\tag{6.6}
$$

To illustrate how the event rates of $h \to \gamma\gamma$ and $h \to Z\gamma$ deviate from the SM predictions, we define the following ratios:

$$
R_{\gamma\gamma} = \frac{\sigma(gg \to h)_{\text{GM}} \times BR(h \to \gamma\gamma)_{\text{GM}}}{\sigma(gg \to h)_{\text{SM}} \times BR(h \to \gamma\gamma)_{\text{SM}}}, \quad R_{Z\gamma} = \frac{\sigma(gg \to h)_{\text{GM}} \times BR(h \to Z\gamma)_{\text{GM}}}{\sigma(gg \to h)_{\text{SM}} \times BR(h \to Z\gamma)_{\text{SM}}},\tag{6.7}
$$

where $\sigma(gg \to h)_{\text{SM}}$ $[\sigma(gg \to h)_{\text{GM}}]$ is the gluon fusion production cross section in the SM (GM model), and $BR(h \to X)_{\text{SM}}$ $[BR(h \to X)_{\text{GM}}]$ is the branching fraction of the $h \to X$ decay mode in the SM (GM model) with $X = \gamma \gamma$ or $Z\gamma$. In fact, the ratio in the production cross sections, $\sigma(gg \to h)_{\text{GM}}/\sigma(gg \to h)_{\text{SM}}$, can be replaced by c_{α}^2/c_H^2 .

In the numerical calculation of $R_{\gamma\gamma}$ and $R_{Z\gamma}$, we use the parameterization given in eq. (3.1) . The mass of the singlet Higgs boson m_{H_1} does not directly affect the decay rates of $h \to \gamma\gamma$ and $h \to Z\gamma$. Nevertheless, it affects the parameter space as constrained by the vacuum stability and unitarity conditions. In this parameterization, the couplings given in eq. [\(6.5\)](#page-27-3) can be rewritten as

$$
\lambda_{hH_5^{++}H_5^{-}} = \frac{2}{v^2} (m_{H_5}^2 - M^2), \quad \lambda_{hH_3^{+}H_3^{-}} = -\frac{1}{c_H v^2} (2c_H^2 m_{H_3}^2 + s_H^2 m_h^2). \tag{6.8}
$$

Figure [15](#page-29-0) shows the contours of $R_{\gamma\gamma}$ (left plot) and $R_{Z\gamma}$ (right plot) on the M - m_{H_5} plane. Here we take $m_{H_3} = 150 \,\text{GeV}, \,\bar{M} = 300 \,\text{GeV}$ and $\alpha = 0$. The triplet VEV v_{Δ} is taken to be 20 GeV in the upper two plots and 60 GeV in the lower two plots. The blue, pink and gray shaded regions are excluded by the vacuum stability bound, unitarity bound and by having a negative value for m_{H_1} , respectively. For fixed values of m_{H_5} , both $R_{\gamma\gamma}$ and $R_{Z\gamma}$ increase with M. In other words, there is a correlation between the two ratios in this model. For the case with a larger v_{Δ} , $R_{\gamma\gamma}$ and $R_{Z\gamma}$ tend to have smaller values because the hW^+W^- coupling gets smaller. Using $m_{H_5} = 150 \,\text{GeV}$ as an example, the maximally allowed values of $R_{\gamma\gamma}$ and $R_{Z\gamma}$ are about 1.8 (1.0) and 1.2 (0.8) in the case of $v_{\Delta} = 20 \,\text{GeV}$ (60 GeV), respectively.

Figure [16](#page-30-0) also shows the corresponding contour plots for the case of $m_{H_3} = 300 \,\text{GeV}$, $\overline{M} = 200 \,\text{GeV}$ and $\alpha = 0$. The parameter space allowed by the unitarity and the vacuum stability constraints is much smaller than the previous case. Again, using $m_{H_5} = 150 \,\text{GeV}$, the maximally allowed values of $R_{\gamma\gamma}$ and $R_{Z\gamma}$ are almost the same as the case of $m_{H_3} =$ 150 GeV, but the minimum values of both $R_{\gamma\gamma}$ and $R_{Z\gamma}$ are around 1.0 in the case of $v_{\Delta} = 20 \,\text{GeV}.$

7 Conclusions

We have discussed how to test the custodial symmetry in the Higgs sector of the GM model at the LHC. This can be done by experimentally verifying three characteristic features. First, there are several Higgs bosons in addition to the SM-like Higgs boson h; namely, a pair of doubly-charged Higgs bosons, two pairs of singly-charged Higgs bosons, a CP-odd Higgs boson and three CP-even Higgs bosons. These Higgs bosons can be classified into the 5 plet Higgs bosons $(H_5^{\pm \pm}, H_5^{\pm}, H_5^0)$, the 3-plet Higgs bosons (H_3^{\pm}, H_3^0) , and the singlet Higgs

Figure 15. Contour plots of $R_{\gamma\gamma}$ (left) and $R_{Z\gamma}$ (right) on the M- m_{H_5} plane in the case of $m_{H_3} = 150 \,\text{GeV}, \,\overline{M} = 300 \,\text{GeV}$ and $\alpha = 0$. In the upper (lower) two plots, v_{Δ} is taken to be 20 GeV (60 GeV). The blue, pink and gray shaded regions are respectively excluded by the vacuum stability bound, unitarity bound and by having a negative mass for H_1 .

boson H_1^0 under the custodial $SU(2)_V$ symmetry. The Higgs bosons belonging to the same $SU(2)_V$ multiplet have the same mass, subject to small electromagnetic corrections at the order of a few hundred MeV. Secondly, the 5-plet and the singlet Higgs bosons can couple to weak gauge boson pairs, but not fermion pairs via the usual (not neutrino) Yukawa interaction at the tree level. On the other hand, the 3-plet Higgs bosons can couple to fermion pairs, but not weak gauge boson pairs. As discussed in the main text, such a feature leads to specific final states for detecting these Higgs bosons and measuring their masses. Thirdly, the VEV of the isospin triplet Higgs fields can be taken to be of order 10 GeV while keeping $\rho = 1$ at the tree level. This is not possible in models with triplet fields in general.

The decay properties of the triplet-like Higgs bosons have been discussed in details. They depend on the mass splitting Δm , defined by $m_{H_3} - m_{H_5}$, and the triplet VEV v_{Δ} . We find that the parameter space in the v_{Δ} - Δm plane can be divided into four regions, among which the main decay modes of the triplet-like Higgs bosons are quite distinct.

Figure 16. Contour plots of $R_{\gamma\gamma}$ (left) and $R_{Z\gamma}$ (right) on the M- m_{H_5} plane in the case of $m_{H_2} = 300 \,\text{GeV}, \,\overline{M} = 200 \,\text{GeV}$ and $\alpha = 0$. In the upper (lower) two plots, v_{Δ} is taken to be 20 GeV (60 GeV). The blue and pink shaded regions are respectively excluded by the vacuum stability bound and unitarity bound.

We have discussed the collider phenomenology of the GM model at the LHC in Region II where the 5-plet Higgs bosons mainly decay to weak gauge boson pairs, whereas the main decay modes of H_3^{\pm} are $\tau\nu$ and cs and that of H_3^0 is $b\bar{b}$ when the mass of the 3-plet Higgs bosons is less than m_t . We focus on the VBF, the vector boson associated and the mDY production processes in order to verify the custodial symmetric nature of the model. We find that $H_5^{\pm\pm}$ and H_5^{\pm} can be detected at more than 5σ level by using the forward jet tagging for the VBF process and the transverse mass cut on the charged leptons and missing transverse energy system if the center-of-mass energy and the luminosity are 8 TeV and 100 fb⁻¹, respectively. The significance of the H_5^0 Higgs boson can be reached at 3σ level by further imposing the b-jet veto.

We also find that the 3-plet Higgs bosons can be detected via the mDY production process. After the M_T cut, the masses of H_3^{\pm} and H_3^0 can be measured from the peak in the invariant mass distribution of the dijet system. Therefore, the respective mass degeneracy in the 5-plet Higgs bosons and the 3-plet Higgs bosons can be tested.

We have also investigated the $h \to \gamma\gamma$ and $h \to Z\gamma$ processes in the GM model. In this model, the $H_5^{\pm\pm}$, H_5^{\pm} and H_3^{\pm} bosons can contribute to these processes in addition to the SM top quark and the W boson at one-loop level. We find that in the parameter space consistent with the unitarity and the vacuum stability, the maximally allowed value of $R_{\gamma\gamma}$ is around 1.8 (1.0) for the parameter choice of $m_{H_3} = 150 \,\text{GeV}, m_{H_5} = 150 \,\text{GeV}$ and $v_{\Delta} = 20 \,\text{GeV}$ (60 GeV). Deviations in the rates of $h \to Z\gamma$ and $h \to \gamma\gamma$ processes from the SM predictions can be used to distinguish models with various extended Higgs sectors. In the GM model, the maximally allowed value of $R_{Z\gamma}$ is around 1.2 (0.8) for $m_{H_3} = 150 \,\text{GeV}, m_{H_5} = 150 \,\text{GeV}$ and $v_{\Delta} = 20 \,\text{GeV}$ (60 GeV). For the cases of larger m_{H_3} (e.g., $m_{H_3} = 300 \,\text{GeV}$), the maximally allowed values of $R_{\gamma\gamma}$ and $R_{Z\gamma}$ are not so different from the case of $m_{H_3} = 150 \,\text{GeV}$. But, the minimum values of both $R_{\gamma\gamma}$ and $R_{Z\gamma}$ are about 1.0 when $m_{H_5} = 150 \,\text{GeV}$ and $v_{\Delta} = 20 \,\text{GeV}$.

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A Relationships among different representations of the Higgs fields

The Higgs fields expressed in eqs. (2.1) and (2.21) are related as follows:

$$
\operatorname{tr}(\Phi^{\dagger}\Phi) = 2\phi^{\dagger}\phi,\tag{A.1}
$$

$$
tr(\Delta^{\dagger}\Delta) = 2tr(\chi^{\dagger}\chi + \xi^{\dagger}\xi), \tag{A.2}
$$

$$
\text{tr}[(\Delta^{\dagger}\Delta)^2] = 6[\text{tr}(\chi^{\dagger}\chi)]^2 - 4\text{tr}[(\chi^{\dagger}\chi)^2] + 2\text{tr}(\xi^4) + 4\text{tr}(\chi\xi)\text{tr}(\xi\chi^{\dagger}), \tag{A.3}
$$

$$
\operatorname{tr}\left(\Phi^{\dagger} \frac{\tau^{a}}{2} \Phi \frac{\tau^{b}}{2}\right) \operatorname{tr}(\Delta^{\dagger} t^{a} \Delta t^{b}) = \sqrt{2} [(\phi^{\dagger} \chi)(\xi \tilde{\phi}) + \text{h.c.}] + 2(\phi^{\dagger} \chi)(\chi^{\dagger} \phi) - (\phi^{\dagger} \phi) \operatorname{tr}(\chi^{\dagger} \chi), \quad \text{(A.4)}
$$

$$
\operatorname{tr}\left(\Phi^{\dagger} \frac{\tau^a}{2} \Phi \frac{\tau^b}{2}\right) (P^{\dagger} \Delta P)^{ab} = -\frac{1}{\sqrt{2}} \phi^{\dagger} \xi \phi + \frac{1}{2} (\phi^{\dagger} \chi \tilde{\phi} + \text{h.c.}),\tag{A.5}
$$

$$
\operatorname{tr}(\Delta^{\dagger}t^a \Delta t^b)(P^{\dagger} \Delta P)^{ab} = 6\sqrt{2} \operatorname{tr}(\chi^{\dagger} \chi \xi). \tag{A.6}
$$

B Coupling constants between the triplet-like Higgs bosons and the weak gauge bosons

The Gauge-Gauge-Scalar vertices and the corresponding coefficients are listed in table [3.](#page-32-1) The Gauge-Scalar-Scalar vertices are listed in table [4,](#page-32-2) where p_1 and p_2 are respectively the four-momenta of the first and second particles in the vertex column into the vertex.

Vertex	Coefficient	Vertex	Coefficient
$H_5^{\pm\pm}W_{\mu}^{\mp}W_{\nu}^{\mp}$	$\frac{g^2}{2\sqrt{2}}$ SHU $g_{\mu\nu}$	$H_1^0Z_{\mu}Z_{\nu}$	$-\frac{g_Z^2}{12}(3s_\alpha c_H - 2\sqrt{6}c_\alpha s_H)v g_{\mu\nu}$
$H_5^{\pm}W_\mu^{\mp}Z_\nu$	$\mp \frac{gg_Z}{2} s_H v g_{\mu\nu}$	$hW_u^+W_\nu^-$	$\frac{g^2}{6}(3c_{\alpha}c_H+2\sqrt{6}s_{\alpha}s_H)v g_{\mu\nu}$
$H_5^0 W^+_\mu W^-_\nu$	$-\frac{g^2}{2\sqrt{3}}s_Hv g_{\mu\nu}$	$hZ_{\mu}Z_{\nu}$	$\frac{g_Z^2}{12}(3c_{\alpha}c_H+2\sqrt{6}s_{\alpha}s_H)v g_{\mu\nu}$
$H_5^0Z_{\mu}Z_{\nu}$	$\frac{g_Z^2}{2\sqrt{3}}$ SHU $g_{\mu\nu}$	$G^{\pm}W_{\mu}^{\mp}A_{\nu}$	$\pm em_Wg_{\mu\nu}$
$H_1^0 W^+_\mu W^-_\nu$	$-\frac{g^2}{6}(3s_{\alpha}c_H-2\sqrt{6}c_{\alpha}s_H)v g_{\mu\nu}$	$G^{\pm}W_{\mu}^{\mp}Z_{\nu}$	$\mp es_Wm_Zg_{\mu\nu}$

Table 3. Gauge-Gauge-Scalar vertices and the associated coefficients.

Vertex	Coefficient	Vertex	Coefficient
$H_5^{++}H_5^{--}A_\mu$	$2e(p_1-p_2)_{\mu}$	$H_5^{\pm\pm} H_5^{\mp} W_{\mu}^{\mp}$	$-\frac{g}{\sqrt{2}}(p_1-p_2)_{\mu}$
$H_5^+H_5^-A_\mu$	$-e(p_1-p_2)_{\mu}$	$H_5^{\pm}H_5^0W_{\mu}^{\mp}$	$\frac{\sqrt{3}}{2}g(p_1-p_2)_{\mu}$
$H_3^+H_3^-A_\mu$	$-e(p_1-p_2)_{\mu}$	$H_5^{\pm\pm} H_3^{\mp} W_{\mu}^{\mp}$	$-\frac{g}{\sqrt{2}}c_H(p_1-p_2)_{\mu}$
$G^+G^-A_\mu$	$-e(p_1-p_2)_{\mu}$	$H_5^{\pm} H_3^0 W_{\mu}^{\mp}$	$\mp i \frac{g}{2} c_H (p_1 - p_2)_{\mu}$
$H_5^{++}H_5^{--}Z_{\mu}$	$\frac{g}{c_W}(1-2s_W^2)(p_1-p_2)_{\mu}$	$H_3^{\pm}H_5^0W_{\mu}^{\mp}$	$-\frac{\sqrt{3}}{6}gc_H(p_1-p_2)_{\mu}$
$H_5^+H_5^-Z_\mu$	$-\frac{g}{2c_W}(1-2s_W^2)(p_1-p_2)_{\mu}$	$H_3^{\pm}H_3^0W_{\mu}^{\mp}$	$\mp i \frac{g}{2}(p_1-p_2)_{\mu}$
$H_3^+H_3^-Z_\mu$	$-\frac{g}{2c_W}(1-2s_W^2)(p_1-p_2)_{\mu}$	$H_3^{\pm} H_1^0 W_{\mu}^{\mp}$	$\frac{g}{6}(2\sqrt{6}c_Hc_{\alpha}+3s_Hs_{\alpha})(p_1-p_2)_{\mu}$
$H_5^{\pm}H_3^{\mp}Z_{\mu}$	$\pm \frac{g_Z}{2} c_H (p_1 - p_2)_{\mu}$	$H_3^{\pm} h W_{\mu}^{\mp}$	$\frac{g}{6}(2\sqrt{6}c_Hs_{\alpha}-3s_Hc_{\alpha})(p_1-p_2)_{\mu}$
$H_5^0H_3^0Z_\mu$	$i\frac{g_Z}{\sqrt{3}}c_H(p_1-p_2)_{\mu}$	$G^{\pm}hW^{\mp}$	$\frac{g}{6}(3c_{\alpha}c_H+2\sqrt{6}s_{\alpha}s_H)$
$H_3^0H_1^0Z_{\mu}$	$-i\frac{g_Z}{6}(2\sqrt{6}c_Hc_{\alpha}+3s_Hs_{\alpha})(p_1-p_2)_{\mu}$	$H_3^0hZ_\mu$	$-i\frac{g_Z}{6}(2\sqrt{6}c_Hs_{\alpha}-3s_Hc_{\alpha})(p_1-p_2)_{\mu}$

Table 4. Gauge-Scalar-Scalar vertices and the associated coefficients.

C Loop functions in the $h \to \gamma\gamma$ and $Z\gamma$ decay rates

The loop functions appearing in the calculations of the SM-like Higgs boson decay to diphotons are given in terms of the Passarino-Veltman functions [\[48](#page-36-3)] as

$$
I_0(m) = \frac{2v^2}{m_h^2} [1 + 2m^2 C_0(0, 0, m_h^2, m, m, m)],
$$
\n(C.1)

$$
I_{1/2} = -4m_f^2 \left[\frac{2}{m_h^2} - \left(1 - \frac{4m_f^2}{m_h^2} \right) C_0(0, 0, m_h^2, m_f, m_f, m_f) \right],
$$
 (C.2)

$$
I_1 = 2m_W^2 \left[\frac{6}{m_h^2} + \frac{1}{m_W^2} + 6 \left(\frac{2m_W^2}{m_h^2} - 1 \right) C_0(0, 0, m_h^2, m_W, m_W, m_W) \right].
$$
 (C.3)

Those for the $h \to Z\gamma$ process are given by

$$
J_0(m) = \frac{2}{e(m_h^2 - m_Z^2)} \left[1 + 2m^2 C_0(0, m_Z^2, m_h^2, m, m, m) + \frac{m_Z^2}{m_h^2 - m_Z^2} \left(B_0(m_h^2, m, m) - B_0(m_Z^2, m, m) \right) \right],
$$
\n(C.4)

$$
J_{1/2} = -\frac{4m_f^2(\frac{1}{2}I_f - s_W^2Q_f)}{s_W c_W (m_h^2 - m_Z^2)} \left[2 + (4m_f^2 - m_h^2 + m_Z^2) C_0(0, m_Z^2, m_h^2, m_f, m_f, m_f) + \frac{2m_Z^2}{m_h^2 - m_Z^2} \left(B_0(m_h^2, m_f, m_f) - B_0(m_Z^2, m_f, m_f) \right) \right],
$$
 (C.5)

$$
J_{1} = \frac{2m_{W}^{2}}{s_{W}c_{W}(m_{h}^{2} - m_{Z}^{2})} \Biggl\{ \Biggl[c_{W}^{2} \Biggl(5 + \frac{m_{h}^{2}}{2m_{W}^{2}} \Biggr) - s_{W}^{2} \Biggl(1 + \frac{m_{h}^{2}}{2m_{W}^{2}} \Biggr) \Biggr] \times \Biggl[1 + 2m_{W}^{2}C_{0}(0, m_{Z}^{2}, m_{h}^{2}, m_{W}, m_{W}, m_{W}) + \frac{m_{Z}^{2}}{m_{h}^{2} - m_{W}^{2}} \Biggl(B_{0}(m_{h}^{2}, m_{W}, m_{W}) - B_{0}(m_{Z}^{2}, m_{W}, m_{W}) \Biggr) \Biggr] - 6c_{W}^{2}(m_{h}^{2} - m_{Z}^{2})C_{0}(0, m_{Z}^{2}, m_{h}^{2}, m_{W}, m_{W}, m_{W}) + 2s_{W}^{2}(m_{h}^{2} - m_{Z}^{2})C_{0}(0, m_{Z}^{2}, m_{h}^{2}, m_{W}, m_{W}, m_{W}) \Biggr\}.
$$
 (C.6)

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