

# ACCURACY OF THE RELAXED EDDY-ACCUMULATION TECHNIQUE, EVALUATED USING CO<sub>2</sub> FLUX MEASUREMENTS\*

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**Abstract.** A system capable of measuring the fluxes of trace gases was developed. It is based on a simpler version of the eddy-accumulation technique (EA), known as the relaxed eddy-accumulation technique (REA). It accumulates air samples associated with updrafts and downdrafts at a constant flow rate in two containers for later analysis of the trace gas mean concentration. The flux integration is based on the durations of updraft and downdraft events, rather than on the vertical wind velocity ( $W$ ) as is the case for EA and eddy-correlation (EC) techniques. The flux, calculated by the REA technique, is equal to the difference in the mean concentration of the trace gas of interest between the upward and downward moving eddies, multiplied by the standard deviation of the vertical wind velocity and an empirical coefficient. CO<sub>2</sub> fluxes measured for 162 half-hour periods over a soybean field by both EC and REA techniques showed excellent agreement (coefficient of determination,  $R^2 = 0.92$ ). The slope (0.985) and the intercept ( $-0.042 \text{ mg m}^{-2} \text{ s}^{-1}$ ) were not significantly different from 1 and 0, respectively, at the 5% level; and the standard error of estimate was  $0.074 \text{ mg m}^{-2} \text{ s}^{-1}$ . It is also shown that the empirical coefficient can be calculated from either latent or sensible heat fluxes. A model describing the effect on this empirical coefficient of not sampling around  $W$  equal to zero is proposed.

## 1. Introduction

The global atmospheric concentration of trace gases is steadily increasing and the contribution from various sources is uncertain due to the lack of accurate field measurements of trace gas exchange. Such information is needed to develop process-based models and to obtain regional and global flux estimates (Stewart *et al.*, 1989).

The most direct approach to flux measurement is the eddy-correlation technique (EC). This technique is based on the mean product of the fluctuations of vertical wind velocity ( $W$ ) and concentration of the gas of interest ( $S$ ). This requires fast-response vertical wind velocity and trace gas sensors. However, for several gases, fast-response sensors are not readily available (Anderson *et al.*, 1989); hence other measuring techniques are needed.

The eddy-accumulation technique (EA) proposed by Desjardins (1972) overcomes the need for fast-response gas sensors without adding other uncertainties, since it is based on the same physical principle as EC. EA relies on the conditional sampling of air in proportion to the vertical wind velocity (positive or negative).

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Gas samples can be analyzed after each sampling period with a slow-response sensor; however, EA requires fast-response proportional sampling valves. A version of these valves developed by Buckley *et al.* (1988) has recently been improved.

Businger and Oncley (1990) modified the EA method by collecting air at a constant rate for updrafts and downdrafts. This approach, called the relaxed eddy-accumulation technique (REA), expresses the covariance of  $W$  with a scalar,  $S$  ( $\overline{W'S'}$ ), as the product of an empirical coefficient ( $A$ ), the standard deviation of  $W$  ( $s_w$ ) and the difference in the mean concentration of the scalar associated with updrafts ( $\overline{S^+}$ ) and downdrafts ( $\overline{S^-}$ ):

$$F_S = \overline{W'S'} = A s_w (\overline{S^+} - \overline{S^-}), \quad (1)$$

where  $F_S$  is the flux of  $S$ , primes indicate deviations from the mean and overbars denote the mean values over the sampling period. The coefficient “ $A$ ” was found to be about 0.6 in simulations of the REA method (Businger and Oncley, 1990; MacPherson and Desjardins, 1991).

Only a few field experiments have been carried out on EA and REA techniques (Speer *et al.*, 1985; MacPherson and Desjardins, 1991; Baker *et al.*, 1992; Majewski *et al.*, 1993) due to technical difficulties. The absence of a bias in  $W$  during conditional sampling is essential, since biased flux measurements cannot be corrected by later data manipulation. In addition, the analysis of the gas concentration requires high accuracy because differences in concentration associated with updrafts and downdrafts are generally small (Hicks and McMillen, 1984; Businger, 1986; Businger and Delany, 1990). For most gases, this high accuracy can only be obtained under laboratory conditions; hence air samples must be stored in containers for subsequent analysis.

In this study, field measurements of  $\text{CO}_2$  fluxes obtained with a REA system are compared to fluxes measured with the EC technique to test the feasibility of measuring trace gas fluxes by the REA technique.

## 2. Materials and Methods

The measurements were carried out over a 40-ha soybean (*Glycine max* [L.] Merrill) field at the Greenbelt farm of Agriculture Canada (Ottawa, Canada). The instruments were mounted on a tower at a height of 3.2 m above the crop. Observations were made on 13 days during the 1992 growing season from calendar day 197 to 238. Fluxes were calculated on a 30-min basis. Measurements were taken mainly under unstable atmospheric conditions; that is, 84% of the observations had a  $z/L$  parameter ranging from  $-0.5$  to  $-0.05$ .

### 2.1. EDDY-CORRELATION MEASUREMENTS

Wind velocities and temperature fluctuations were measured with a three-dimensional ultrasonic anemometer/thermometer (DAT-310, Kaijo Denki Ltd., Tokyo, Japan) and the  $\text{CO}_2$  and  $\text{H}_2\text{O}$  density fluctuations by an open-path fast-response

infrared gas analyzer (IRGA) developed at Agriculture Canada (Chahuneau *et al.*, 1989; Desjardins, 1991). The CO<sub>2</sub> fluxes were corrected for the IRGA sensitivity to water vapour and for air density fluctuations, using sensible and latent heat fluxes (Webb *et al.*, 1980). The vertical wind velocity signal was high-pass filtered at 0.001 Hz with a digital filter. No rotation of axes correction (Chahuneau *et al.*, 1989) was applied to the fluxes in order to compare them with fluxes computed by the REA technique. All signals were recorded at a sampling frequency of 20 Hz with an A/D converter (Labmaster card DMA TM-40, Scientific Solutions, Solon, Ohio) connected to a microcomputer.

## 2.2. SIMULATION

Raw signals of vertical wind velocity ( $W$ ), air temperature ( $T$ ), horizontal wind velocity ( $U$ ), water vapour ( $\rho_v$ ) and CO<sub>2</sub> ( $\rho_c$ ) densities were simultaneously recorded at 20 Hz. These data files were processed to compute fluxes by EC and REA techniques. The data analysis program permitted the following: (1) simulation of different intervals of suppressed sampling (deadbands) centred around  $W$  equal to zero, (2) high-pass filtering of the  $W$  signal, (3) introduction of various time lags between  $W$  and the other channels and (4) quantification of the effect of a bias on  $\overline{W}$ .

## 2.3. RELAXED EDDY-ACCUMULATION MEASUREMENTS

The REA system is illustrated in Figure 1. It consists of an inlet Teflon tube of 0.11 m length, connected to a diaphragm pump (micropump KNF, type NMP 08L, Neuberg Inc., Princeton, New Jersey) that pushes air through two fast-response 3-way valves (TFE 1-30-900 solenoid 3-way valve, General Valve Corp., Fairfield, New Jersey). This small assembly was mounted at the top of the tower, 0.15 m behind the sonic anemometer. The tubing between the inlet and the valves was kept small (1 mm inner diameter) and short (0.18 m). This limited the delay between the  $W$  signal and the effective conditional sampling to 14 ms for each reversal of  $W$ . The response time of the solenoid valves was 20 ms, leading to a total time lag of 34 ms per reversal of  $W$ , for the sampling device. The REA system is designed to have a continuous flow rate (0.600 L min<sup>-1</sup>) through the pump. Needle valves on the vent outlets (F3 and F4 in Figure 1) were used to balance the flow rates (0.400 L min<sup>-1</sup>) through the sampling tubing (F1 and F2 in Figure 1) in order to keep the time lag identical on both sides.

The  $W$  signal recorded for the EC method also controlled the two 3-way valves operating the conditional sampling (Figure 1). An assembler language routine was used to high-pass filter the  $W$  signal at a 0.001 Hz cutoff frequency in order to remove any bias on  $\overline{W}$  and to activate the valves via a control port of the data acquisition system. This setup reduces the delay between  $W$  and the control of the valves to less than 1 ms. The sampling frequency of 20 Hz generated a time lag ranging from 0 to 50 ms. This variable time lag corresponds to the period between the effective change of the sign of  $W$  and its measurement. Air samples

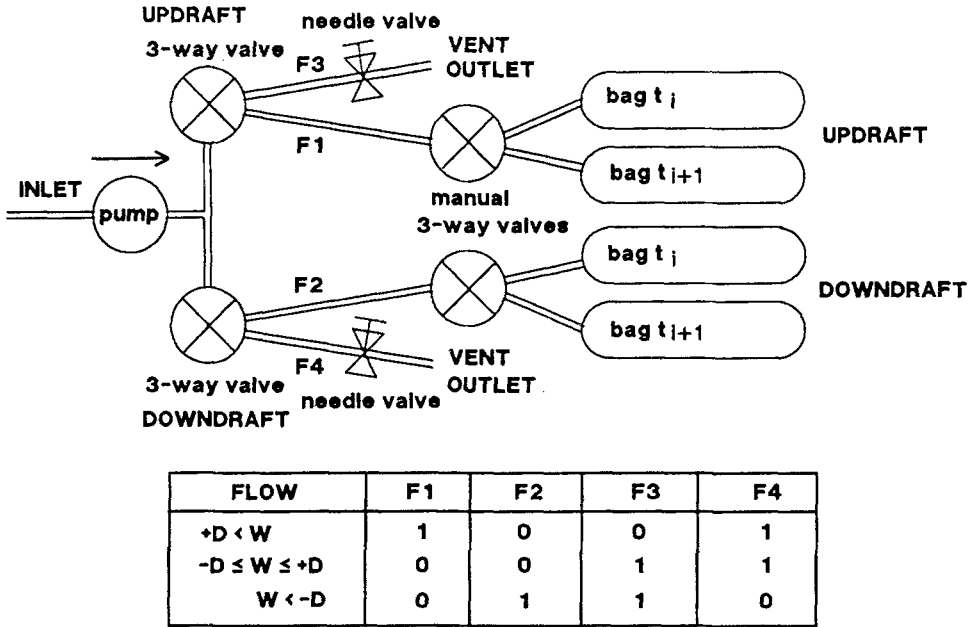


Fig. 1. Schematic of a relaxed eddy-accumulation device to measure trace gas fluxes. The status of flows F1 to F4 indicates if there is a flow (1: yes, 0: no) through the tubing depending on the vertical wind velocity ( $W$ ) compared to the negative and positive value of the deadband ( $\pm D$ ). Air is collected in bags that are changed from one period ( $t_i$ ) to another ( $t_{i+1}$ ).

associated with updrafts and downdrafts were accumulated in 6.5-L bags made of Curlam 9003 (Curwood Inc., New London, Wisconsin) equipped with double-end shutoff quick connectors to avoid contamination when connecting and disconnecting the bags. To allow continuous sampling from one half-hour period to another ( $t_i$  and  $t_{i+1}$  in Figure 1), two bags can be connected on each side (i.e., downdraft and updraft) of the sampling system (Figure 1). The bags were flushed with dry air having a  $\text{CO}_2$  concentration of  $360 \mu\text{mol mol}^{-1}$ , before use in order to avoid any contamination of the air samples.

The difference in  $\text{CO}_2$  concentrations between the bags was incorporated in the equation described by Pattey *et al.* (1992) that corrects the flux for density fluctuations:

$$F_C = \left[ \frac{P - \bar{e}}{\bar{T}} \right] A s_w \frac{M_C}{R} \left[ (\bar{C}_m^+ - \bar{C}_m^-) \left( 1 + \frac{\bar{e}}{P} \right) + (\bar{C}_m - \alpha) \left( \frac{e^+ - e^-}{P} \right) \right] 10^{-3}, \tag{2}$$

where  $F_C$  is the flux of  $\text{CO}_2$  ( $\text{mg m}^{-2} \text{s}^{-1}$ ) corrected for the density fluctuations and for the sensitivity of the  $\text{CO}_2$  analyzer to water vapour;  $T$  (K) is the absolute

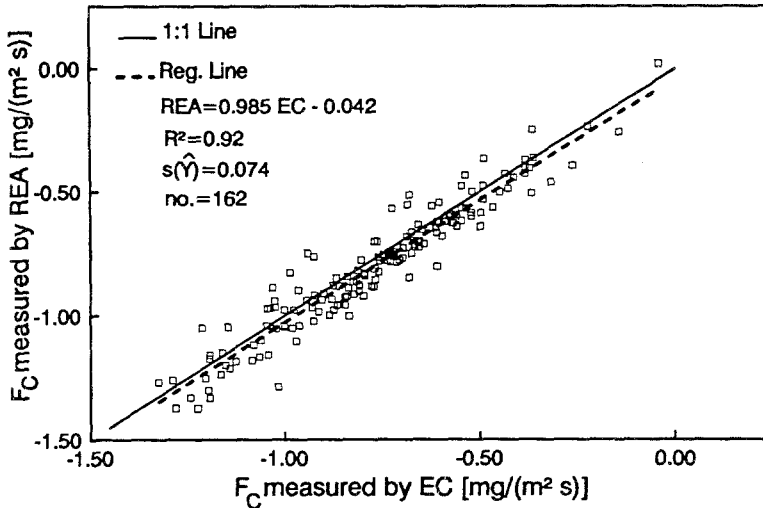


Fig. 2. Comparison between Relaxed Eddy-Accumulation (REA) and Eddy-Correlation (EC) techniques based on 30-min  $\text{CO}_2$  flux ( $F_C$ ) measurements carried out over a soybean field ( $s(\hat{Y})$ : standard error of the estimates;  $R^2$ : coefficient of determination).

air temperature;  $P$  (Pa) and  $e$  (Pa) are the atmospheric and water vapour pressures, respectively;  $C_m$  ( $\mu\text{mol CO}_2 \text{ mol}^{-1} \text{ air}$ ) is the measured molar fraction of  $\text{CO}_2$  and  $M_C$  ( $\text{g mol}^{-1}$ ) the  $\text{CO}_2$  molar mass;  $R$  ( $\text{J mol}^{-1} \text{ K}^{-1}$ ) is the gas constant and  $\alpha$  ( $\mu\text{mol}^{-1} \text{ CO}_2 \text{ mol}^{-1} \text{ H}_2\text{O}$ ) is the sensitivity coefficient to water vapour of the  $\text{CO}_2$  analyzer. Sensitivities to water vapour were  $270 \mu\text{mol CO}_2 \text{ mol}^{-1} \text{ H}_2\text{O}$  for the slow-response  $\text{CO}_2$  analyzer (ADC-MK3) and  $289 \mu\text{mol CO}_2 \text{ mol}^{-1} \text{ H}_2\text{O}$  for the open-path analyzer. Measurements from the ADC-MK3  $\text{CO}_2$  analyzer are considered insensitive to air temperature fluctuations because the density of gas accumulated in bags had time to equilibrate before analysis. The empirical coefficient "A" was computed from Equation (1) for each run using the signals of the fast-response sensors. The empirical coefficient was calculated for air temperature ( $A_T$ ), water vapour ( $A_V$ ),  $\text{CO}_2$  ( $A_C$ ) and vertical wind velocity ( $A_W$ ). " $A_C$ " was used in Equation (2) for the comparison illustrated in Figures 2 and 3, because it accounts for several factors that affect the conditional sampling such as the use of a deadband, the time lag due to sampling frequency and the high-pass filtering of  $W$ . The only effect that is not accounted for by the real-time computation of "A" is the impact of the time lag due to valve opening and closing and of the air mixing in front of the valves. These potential problems were minimized by the design of the system. The time lag due to the system hardware design (34 ms) is equivalent to less than one sampling period (50 ms). Based on eight 30-min simulations of a 50-ms lag between  $W$  and  $\text{CO}_2$  signals, the flux reduction was small, about 3%, and was considered negligible for our REA device.

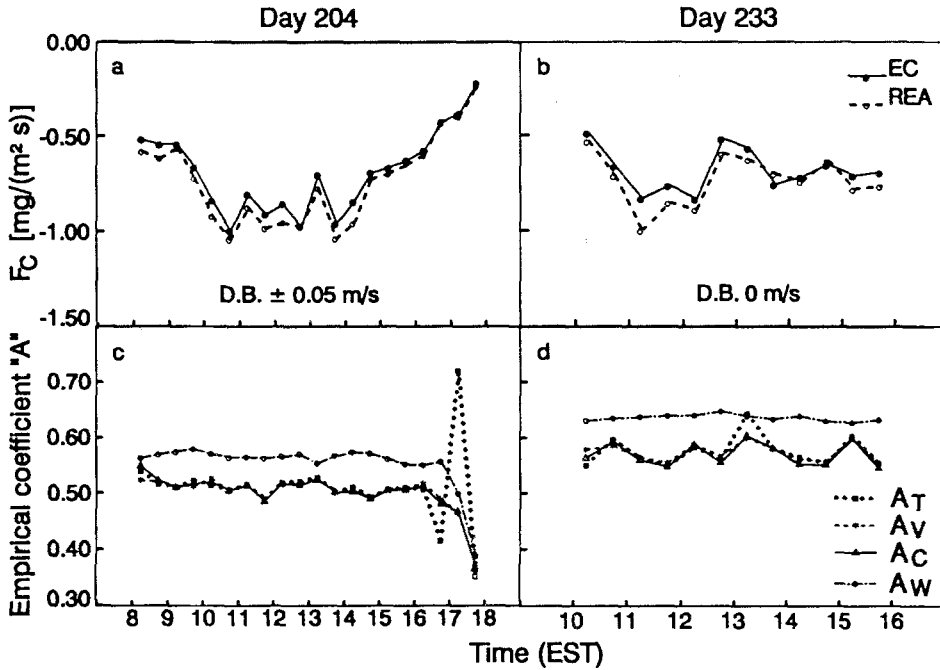


Fig. 3. (a, b) Temporal variations of  $\text{CO}_2$  flux ( $F_C$ ) measured using REA and EC techniques, (c, d) of empirical coefficient "A" for temperature ( $A_T$ ), water vapour ( $A_V$ ),  $\text{CO}_2$  ( $A_C$ ) and vertical wind velocity ( $A_W$ ), illustrated for two days, with and without deadband (D.B.).

#### 2.4. ANALYSIS OF THE DIFFERENCE IN $\text{CO}_2$ CONCENTRATION ( $\Delta C$ )

Air collected in bags during the conditional sampling was analyzed using an infrared gas analyzer in differential mode ( $\Delta C = \overline{C^F} - \overline{C^-}$ ). The  $\text{CO}_2$  analyzer (ADC 225 MK3, Analytical Development Co. Ltd, Hoddesdon, UK) was kept in the laboratory to minimize vibration and temperature changes during measurements. A zero adjustment was made at the beginning and at the end of a series of  $\Delta C$  measurements. Span adjustments were performed at the beginning and end of each  $\Delta C$  analysis to account for the drift of the instrument. Dry air with a  $\text{CO}_2$  concentration of  $360 \mu\text{mol mol}^{-1}$  was used as a calibration gas. In this range, a change of  $10 \mu\text{mol mol}^{-1}$  of the background concentration caused a sensitivity change of 1.6%. This effect was neglected in our calculations. The output of the  $\text{CO}_2$  analyzer was sampled at 5 Hz for 20 s to compute the mean and standard deviation of each measurement. To analyze  $\Delta C$ , a four-way valve connected at the inlet of the two cells was used to interchange the flow from the bags to the cells, permitting the determination of an implicit zero value without disconnecting the bags. The switching was done twice to account for the drift during each measuring period of  $\Delta C$ . The equation used to compute  $\Delta C$  is as follows:

$$\Delta C = K \frac{(V_1 + V_3 - 2V_2)}{(4V_S - V_1 - V_3 - 2V_2)}, \quad (3)$$

where  $K$  is the difference in  $\text{CO}_2$  concentration used for span adjustment ( $18 \mu\text{mol mol}^{-1}$  in our experiment);  $V_S$  (V) is the mean of the two span readings before and after  $\Delta C$  determination;  $V_1, V_2, V_3$  (V) are the three consecutive steady-state readings of the  $\Delta C$  between a pair of bags corresponding to each time that the air samples to the analyzer cells were interchanged.

Several tests were carried out to evaluate the overall precision of the  $\text{CO}_2$  analysis with this experimental setup. The precision was about  $0.03 \mu\text{mol mol}^{-1}$ , which corresponds to a  $\text{CO}_2$  flux of  $0.015 \text{ mg m}^{-2} \text{ s}^{-1}$ , under typical conditions.

### 3. Results and Discussion

#### 3.1. COMPARISON OF $\text{CO}_2$ FLUX MEASUREMENTS

A linear regression curve was performed on the 162 observations of  $\text{CO}_2$  flux measured by REA (Equation 2) using calculated  $A_C$  against those measured by EC (Figure 2). Excellent agreement was found between the techniques ( $R^2 = 0.92$ ), giving a slope and an intercept, which were not significantly different from 1 and 0, respectively, at the 5% level. The standard error of the estimates was  $0.074 \text{ mg m}^{-2} \text{ s}^{-1}$ , indicating small dispersion. The limited scattering, which is random, can be caused by errors associated with measuring  $\Delta C$  by the bag-analyzer assembly, and imprecisions in sensible heat flux measurement used to correct EC estimates of  $\text{CO}_2$  fluxes for density fluctuations.

REA is not as exact as EC or EA. However, the good agreement between REA and EC suggests that integrating the sampled air by the duration of updraft or downdraft events as is the case for the REA technique is a good approximation to a flux integration based on the vertical wind velocity as is the case for EA and EC techniques.

Fluxes measured by REA and EC had a very similar pattern of temporal variation as illustrated for two typical days in Figures 3a and 3b. These flux values were based on  $A_C$  values calculated for each run. This did not improve the agreement in the temporal flux pattern variation because  $A_C$  was relatively constant during most of the day. It will normally not be possible to calculate  $A_C$  but it is not serious because calculated values of  $A_T, A_V$  and  $A_C$  were identical except for one case at the end of day 204 (Figure 3c). It should be noted that the  $A_W$  values were considerably larger.

The similarity between the coefficients calculated from temperature, water vapour and  $\text{CO}_2$  data was examined for the entire data set (Figure 4). Values of  $A_T, A_V$  and  $A_C$  agreed closely, within the limitations of the large scatter for  $A_T$  and one value of  $A_V$ . These cases occurred when the flux of the scalar was small and when the rate of convergence towards zero of  $\overline{W'S'}$  was different from that of

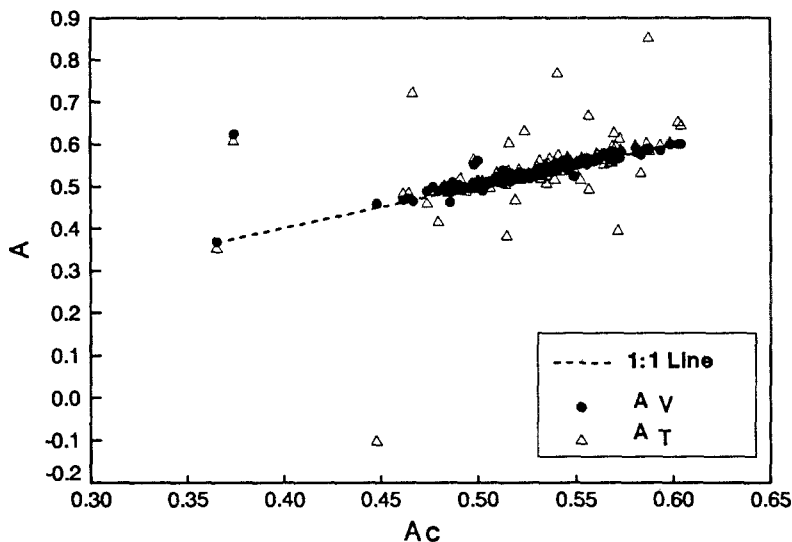


Fig. 4. Similarity between the empirical coefficients for  $\text{CO}_2$  ( $A_C$ ), water vapour ( $A_V$ ) and temperature ( $A_T$ ) for the entire data set. The range of values reflects the effect of a deadband of  $\pm 0.05 \text{ m s}^{-1}$  used for 67% of the observations.

( $\overline{S^+} - \overline{S^-}$ ). This situation is illustrated (Figure 5) by the increased dispersion of  $A_T$  when  $F_T$  was between 1 and  $-25 \text{ W m}^{-2}$ . Most of the difference between  $A_C$  and  $A_T$  (Figures 3c, 4) is related to the change in the sign of  $F_T$  that occurred earlier in the afternoon, rather than the change in sign of  $F_C$ .  $A_C$ ,  $A_T$  and  $A_V$  appear to be interchangeable except when the scalar used to calculate the coefficient has a flux tending towards zero. The  $\text{CO}_2$  fluxes were therefore calculated again using  $A_T$  instead of  $A_C$  in Equation (2) and were compared to EC fluxes (Figure 6). If we exclude the 20 runs when  $-25 \leq F_T \leq 1 \text{ W m}^{-2}$ , the same regression coefficients and statistics were found. The standard error of estimate is also of the same magnitude, i.e.,  $0.078 \text{ mg m}^{-2} \text{ s}^{-1}$ .  $A_T$  can therefore be used for most cases to characterize the empirical coefficient for a specific experimental setup. For the case of  $\text{CO}_2$ ,  $A_V$  gave even better results than  $A_T$  but the ease of obtaining  $A_T$  justifies its use.

For observations that were taken without deadband (42 obs.),  $A_C$  averaged 0.57, which agrees with previous estimates (Businger and Oncley, 1990; MacPherson and Desjardins, 1991; Baker *et al.*, 1992). The coefficient of variation was 5%, indicating that the empirical coefficient is relatively constant between runs.

The similarity between the empirical coefficients does not extend to  $A_W$ . The values of  $A_W$  were higher than those of  $A_C$  by an average of 13% (Figure 7). This difference can be explained by the fact that the derivation of  $A_W$  (MacPherson and Desjardins, 1991) relies on the  $W$  frequency distribution only, while the other coefficients are calculated by accounting for the characteristics of the joint



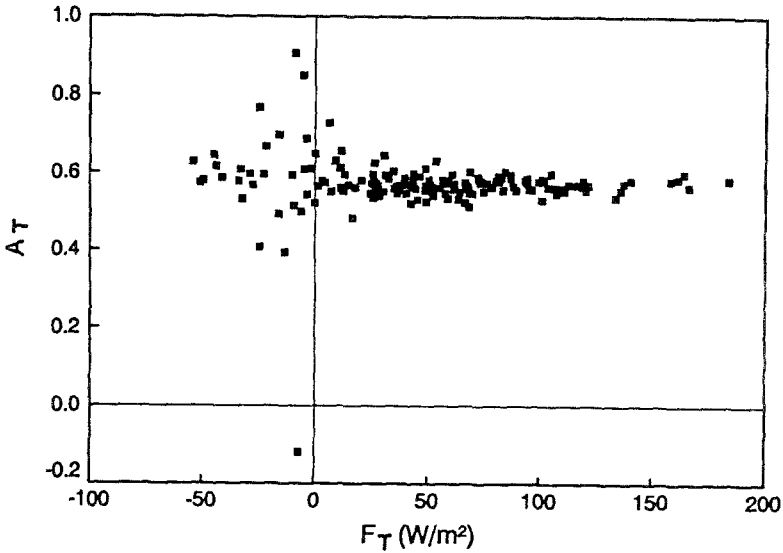


Fig. 5. Variations of the empirical coefficient for temperature ( $A_T$ ), corrected for the deadband effect using Equation (5), with respect to the sensible heat flux ( $F_T$ ), for 162 observations.

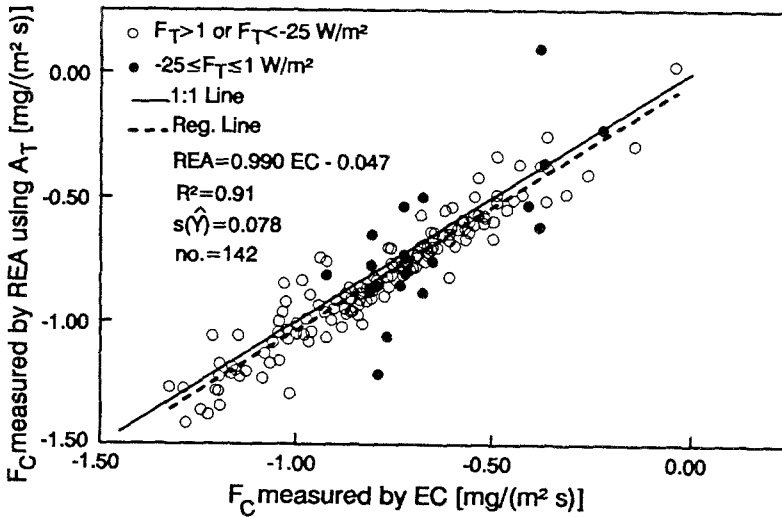


Fig. 6. Comparison between  $\text{CO}_2$  flux ( $F_C$ ) measured by Relaxed Eddy-Accumulation (REA) using the empirical coefficient for air temperature ( $A_T$ ) and Eddy-Correlation (EC) techniques based on 30-min measurements. The linear regression applies to 142 observations. It excludes  $A_T$  values associated with  $-25 \leq F_T \leq 1 \text{ W m}^{-2}$ .

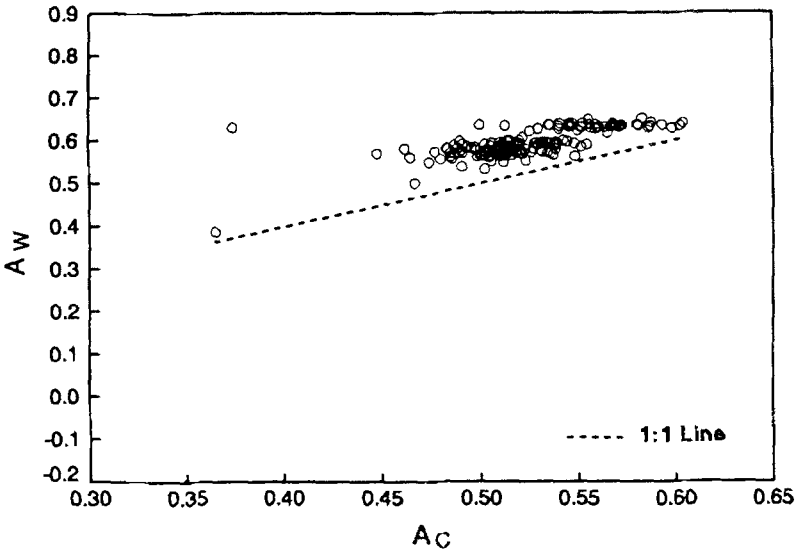


Fig. 7. Comparison between the empirical coefficients for CO<sub>2</sub> ( $A_C$ ), and vertical wind velocity ( $A_w$ ) for the entire data set. The range of values reflects the effect of a deadband of  $\pm 0.05 \text{ m s}^{-1}$  used for 67% of the observations.

probability distribution of  $W$  with the scalar. Therefore, the derivation of the empirical coefficient cannot be based only on the frequency distribution characteristics of  $W$ .

### 3.2. SIMULATION STUDIES

#### 3.2.1. Deadband Effect

A deadband is an interval defined on the  $W$  signal, centred at  $W = 0$ , in which no air sampling takes place. It can be used to prolong the life of the valves driven by the conditional sampling system and to increase the difference in trace gas concentration between updrafts and downdrafts ( $\overline{S}^+ - \overline{S}^-$ ). However, using a deadband can bias the sampling towards larger eddies as it first removes air samples having a concentration close to the mean. The increase of the differences in concentration is then compensated by the decrease of  $A_S$ . This effect is illustrated in Figure 3, when lower coefficients  $A_C$  were computed on day 204 (Figure 3c), for which a deadband of  $\pm 0.05 \text{ m s}^{-1}$  was used, than on day 233 when no deadband was used (Figure 3d). In addition, the deadband removed many more observations (20 to 50%) during light horizontal wind conditions (at 17:00), leading to a strong reduction of “ $A$ ” values, than during normal daytime conditions ( $\sim 5\%$  of the observations) (Figure 3c). In Figure 4, the range of  $A_C$  values (0.36 to 0.60) reflects the effect of a fixed deadband from run to run. A deadband of  $\pm 0.05 \text{ m s}^{-1}$

TABLE I

Values of the coefficients ( $b_0, b_1$ ) for the nonlinear model describing the effect of a deadband normalized with  $s_w$  ( $\beta_S(D/s_w)$ ) applied on the filtered signal of  $W$  (high-pass filter of 0.001 Hz), for the relaxed eddy-accumulation coefficients for temperature ( $T$ ), CO<sub>2</sub> ( $\rho_C$ ) and water vapour ( $\rho_V$ ). The coefficient of determination ( $R^2$ ) applies to the linear regression between the predicted and observed data, and  $s(\hat{Y})$  represents the standard error of the estimates. The model is:

$$\beta_S(D/s_w) = 1 - b_0[1 - e^{(-b_1 D/s_w)}]$$

	$\beta_S(D/s_w)$		
	$T$	$\rho_C$	$\rho_V$
$b_0$	0.437	0.412	0.432
$b_1$	1.958	2.125	1.947
$R^2$	0.985	0.981	0.988
$s(\hat{Y})$	0.012	0.013	0.011

was used for 67% of the data set while no deadband was used for the remaining runs.

The effect of increasing the deadband on the estimate of flux was examined by simulation studies. Deadbands up to  $\pm 0.4 \text{ m s}^{-1}$  in steps of  $\pm 0.02 \text{ m s}^{-1}$  were simulated for 20 half-hour runs, in which the  $W$  signal was high-pass filtered. The observations correspond to horizontal wind speed values ranging from 2.6 to  $5.9 \text{ m s}^{-3}$  and  $s_w$  from 0.45 to  $0.84 \text{ m s}^{-1}$ . For a given run, the effect of the deadband on  $A_S$  was expressed by:

$$\beta_S(D) = \frac{[\overline{S^+(0)} - \overline{S^-(0)}]}{[\overline{S^+(D)} - \overline{S^-(D)}]} \tag{4}$$

with  $0 \leq \beta_S(D) \leq 1$  and where  $S(D)$  is the value of a scalar for a given deadband and  $S(0)$  its value without deadband. The magnitude of  $\beta_S(D)$  is expected to vary with the intensity of fluctuations in  $W$ . To compare the deadband effect on  $A_S$  between runs with different turbulence intensities, the deadband should be normalized with  $s_w$  as proposed by Businger and Oncley (1990). The following general model was used to describe the deadband effect normalized with  $s_w$  on  $A_S$ :

$$\beta_S(D/s_w) = 1 - b_0[1 - e^{(-b_1 D/s_w)}], \tag{5}$$

where  $D$  is the positive half-interval of the deadband ( $0 \leq D \leq 0.4 \text{ m s}^{-1}$ ) and  $b_0$  and  $b_1$  are nonlinear regression coefficients. The coefficients of the nonlinear model were fitted using the Marquardt iterative method (SAS, 1985) for air temperature, CO<sub>2</sub> and water vapour (Table I).

The general model for  $\beta_S$  (Equation 5) has been used to determine the maximum deadband that can be applied without invalidating the REA equation. The result-

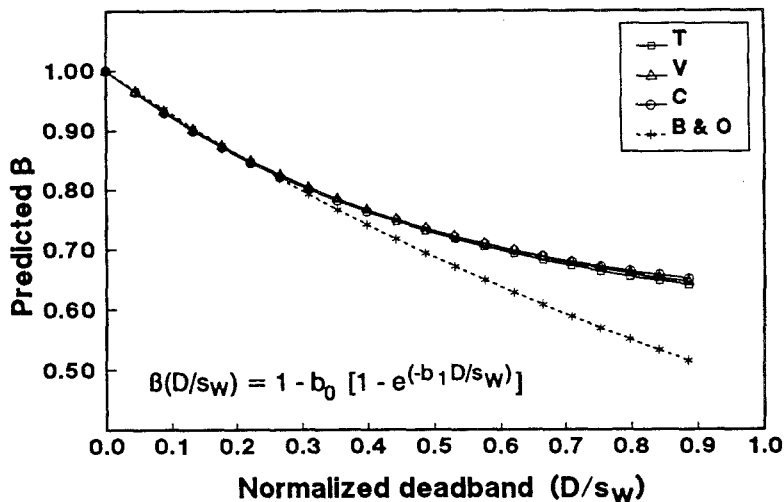


Fig. 8. Model describing the effect of the deadband ( $\beta$ ) on the empirical coefficient "A" for temperature ( $T$ ), water vapour ( $V$ ) and  $\text{CO}_2$  ( $C$ ) as a function of the deadband ( $D$ ) normalized using the standard deviation of the vertical wind velocity ( $s_w$ ). "B & O" is the model proposed by Businger and Oncley (1990).

ing fitted curves gave similar results for the three scalars (Figure 8). The ratio of  $\beta_T(D/s_w)$  over  $\beta_C(D/s_w)$  was equal to one ( $\pm 1\%$ ), based on the 20 half-hour runs, for  $D/s_w$  values up to 0.5. These results suggest that when run-specific  $A_T$  or  $A_V$  is calculated, they can be used to assess the deadband effect for other species, for normalized deadbands up to  $\pm 0.5$ . Moreover,  $\Delta S$  is increased by as much as 27% (Figure 8). The difference between estimated  $\beta_s$  values and the observed  $\beta_s$  from individual runs increases as the deadband increases (Figure 9), meaning that the effect of the deadband is less predictable for these larger intervals. The variability of  $\beta_s$  between runs is much larger than the variation of  $\beta_s$  between the scalars within a run. Equation (5) should therefore be used with caution for estimating the deadband effect on the conditional sampling, when a constant "A" is used in place of  $A_T$  or  $A_V$  calculated simultaneously with actual measurements. Based on the pattern of scattering in Figure 9, Equation (5) should not be used to correct "A" when  $\beta_s(D)$  is lower than 0.85 (Figure 9), or when expressed as normalized deadband, when  $D/s_w$  is greater than 0.2 (Figure 8). For  $D/s_w$  values lower than 0.2, Equation (5) and the model proposed by Businger and Oncley (1990) give similar estimates of  $\beta_s$ . However, the model of Businger and Oncley tends towards zero for large values of  $D/s_w$  while our model has an asymptotic value of " $1 - b_0$ ". We believe that the asymptotic value should be different from zero because if a large deadband is used, this is equivalent to sampling the large eddies only, for which the mean concentration difference is finite. By extending the simulations of  $\beta_C$  against  $D/s_w$  up to 2.5, we fitted values

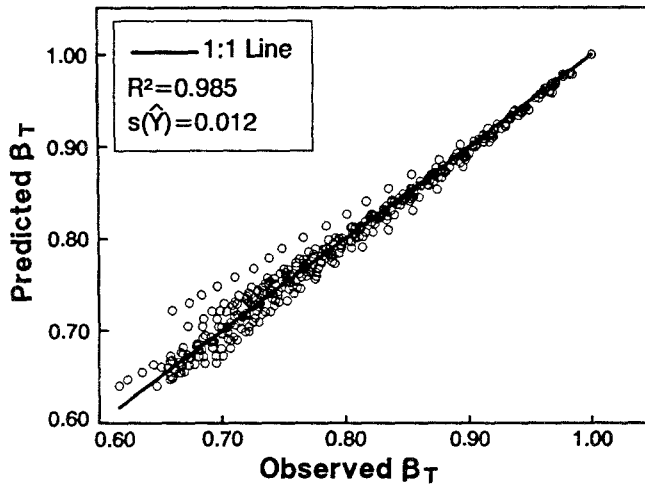


Fig. 9. Accuracy of the estimated effect of the deadband ( $\beta_T$ ) on the empirical coefficient for temperature, evaluated from 20 30-min runs.

of  $b_0$  and  $b_1$  on 12 individual runs. Asymptotic values ranging from 0.48 to 0.77 were found.

### 3.2.2. Effect of a Nonzero Mean $W$ on $F_C$

The conditional sampling could be biased if  $W$  is not filtered. A bias on  $W$  ( $W_b$ ) could be generated by nonlevel terrain, an electrical offset or improper levelling of the sonic anemometer. Simulations were done after high-pass filtering  $W$  at 0.001 Hz and then adding a bias on  $W$ , to quantify the effect of a nonzero mean  $W$  on the REA fluxes. Simulations of  $W_b$  values ranging from  $-0.20$  to  $0.20 \text{ m s}^{-1}$  by steps of  $0.05 \text{ m s}^{-1}$  were done on 12 runs for unstable conditions. Figure 10 illustrates the effect of a bias on  $W$  normalized with  $s_W$  on the estimate of the  $\text{CO}_2$  flux. The simulations confirm the result of Businger and Oncley (1990) that the effect of the bias is small for a normalized bias of  $\pm 0.1$ . A negative bias induced an overestimation while a positive bias generated a greater flux underestimation for the same absolute value of the bias. The asymmetry of the effect of  $W_b$  seems to be due to the skewed  $\text{CO}_2$  distribution, reflecting a difference in the shape of the  $C^-$  and  $C^+$  distributions. The variation from run to run increased with  $|W_b/s_W|$ .

## 4. Conclusion

Excellent agreement was found between  $\text{CO}_2$  fluxes measured by EC and REA techniques, under the experimental conditions that corresponded mostly to unstable atmospheric conditions. It confirms the potential of the REA technique, which was suggested by simulation studies (Businger and Oncley, 1990; MacPherson and Desjardins, 1991), and shows that operational REA systems can be

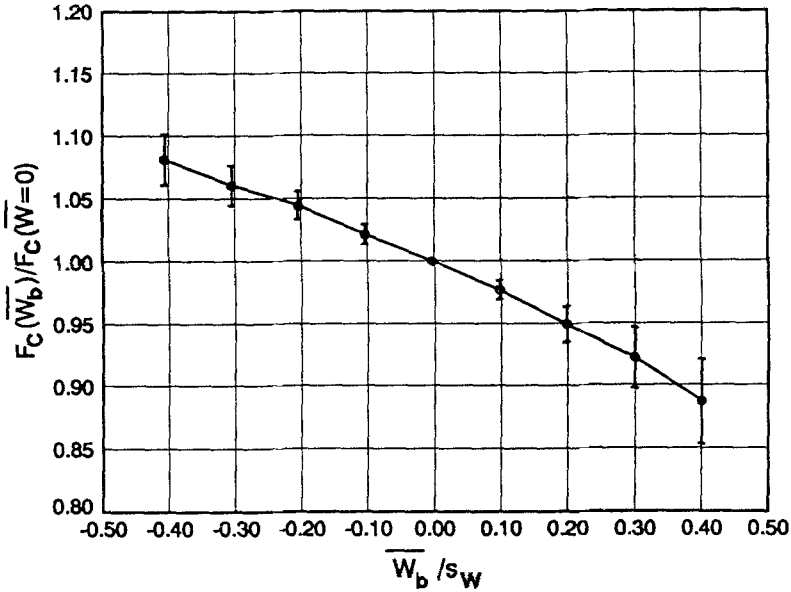


Fig. 10. Effect on the relative value of the CO<sub>2</sub> flux ( $F_C$ ) of a bias on the mean vertical wind velocity ( $\overline{W}_b$ ).  $\overline{W}_b$  is normalized with the standard deviation of the vertical wind velocity ( $s_w$ ). Intervals of confidence (95%) illustrated on the graph are based on 12 30-min runs.

developed whenever slow-response gas analyzers with adequate sensitivity are available (Desjardins *et al.*, 1993). It also shows that it is possible to minimize the effect of measurement errors such as: (1) the bias on the mean vertical wind velocity, (2) the time lag between the sign change of  $W$  and the effective conditional sampling of air, (3) the contamination of air samples collected in bags.

A model describing the effect of the deadband can be used to correct "A" for normalized deadband values not exceeding  $\pm 0.2$ . The effect of the deadband can also be compensated by calculating "A" with the simultaneous measurements of another scalar. Empirical coefficients calculated from CO<sub>2</sub>, water vapour and temperature data were interchangeable for  $D/s_w$  up to 0.5. On the other hand,  $A_w$  should not be used because it does not reflect the characteristics of the joint probability distribution between  $W$  and the scalar. When no deadband was used, the empirical coefficient averaged 0.57 with a coefficient of variation of 5% between the runs. Further research should be carried out to evaluate the accuracy of REA technique under stable atmospheric conditions.

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