# Calculation of O<sub>2</sub> Saturation and of the Oxyhemoglobin Dissociation Curve for Different Species, Using a New Programmable Pocket Calculator\*

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Summary. The degree of O<sub>2</sub> saturation and different data of acid-base status are determined from  $pO_2$ , pH, and  $pCO_2$  values by a programmable pocket calculator. Since the operating program should be usable for different species and also in the range of very low O<sub>2</sub> saturations, obviously the usual Hill equation for calculating the oxygen dissociation curve of hemoglobin is not applicable; the same is true in some cases for the Adair equation. Thus a 3-fold subdivision of the dissociation curve was undertaken and programmed. Suitable programs for several species could be established despite the limited number of program steps in the new calculator, giving systematic deviations in calculated  $O_2$  saturations of  $\leq \pm 0.9$ saturation percent over the full range of dissociation curves. A reverse procedure for calculation of  $pO_2$  from saturation is added. In situations where  $pCO_2$  or base excess are not known or only estimated, limits of the arising error are stated. In the acid-base program 7 parameters are evaluated partially using empirical formulae derived from nomograms. The programmable pocket calculator offers advantages of small size, economy, and independence of line voltage compared to much more spacious units and a precision equal or superior to nomograms.

Key words: Computer Programs — Bohr Effect — Acid-Base Status — Base Excess —  $pO_2$  — Oxyhemoglobin Dissociation Curve.

With the development of programmable pocket calculators difficult calculations can be carried out at relatively low cost and immediately at the site where measurements are taken. In addition, the further evaluation and elaboration of experimental results can be done at almost any place. It was our purpose to calculate the oxygen saturation from measured  $pO_2$ , pH, and partially  $pCO_2$  values for different species, considering largely the present knowledge of mutual influence of various factors. In spite of the limited number of programmable steps in the described calculators one can achieve an accuracy which could not be guaranteed by the use of even very exact and consequently very extensive nomograms. The following study elaborates on the programming and the degree of accuracy that can be obtained from evaluation of dissociation curves of different species as described by several authors.

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## Methods

Using a special experimental arrangement (Lutz et al., 1974), the following values were determined from blood flowing with constant velocity through a temperature-regulated electrode assembly:  $pO_2$  (Pt-electrode of Clark type, according to Lübbers and Windisch, 1963; produced by Eschweiler, Kiel), pH (microelectrodes Ingold KG Frankfurt), and in extension of the experimental procedure  $pCO_2$  (electrode according to Gleichmann and Lübbers, 1960; produced by Eschweiler, Kiel). For the determination of the O<sub>2</sub> consumption and its variations in organ circulations the oxygen saturation  $(SO_2)$  should be detected down to very low values. For this a new programmable pocket calculator HP-65 (Hewlett-Packard) was used. This may be easily moved to every measuring location as it has dimensions of only  $15 \times 8 \times 3.5$  cm and 312 g weight. For the programming 100 single steps are available. Calculating the oxygen saturation from the values of blood was done in the following manner. First the oxygen tension was converted to standard conditions (pH = 7.4,  $pCO_2 = 40 \text{ mm Hg}$ , BE = 0 mval/l, respectively). Then the resulting standardized pO2 value was inserted in equations describing the S-shaped dissociation curve and the appropriate oxygen saturation was determined. A correction for different temperature values is given in three of the programs; however, in order to obtain a good reproduction and calibration a constant temperature of 37°C in the electrode units is usual in most species. Various arithmetical methods were applied and specially checked in regard to their applicability for different animal species. The exclusive use of Hill's equation was abandoned already in preliminary tests, since it causes greater deviations; the same was true for the Adair equation in some species other than man. Furthermore the reverse procedure, calculation of  $pO_2$  from saturation, would require a multistep iteration by this equation.

#### 1. Equation of Adair

Although the value of the equation of Adair (1925) today is to be seen more as a formal than as a causal description (Hutten, 1968; Yoder *et al.*, 1973), it permits a sufficiently exact description of the human oxyhemoglobin dissociation curve. The most appropriate form for the computing process is found by the following equations (SO<sub>2</sub> in  $^{0}/_{0}$  saturation):

$$SO_2 = 25 \frac{A_1 p O_2 + 2A_2 p O_2^2 + 3A_3 p O_3^2 + 4A_4 p O_2^4}{1 + A_1 p O_2 + A_2 p O_2^2 + A_3 p O_2^3 + A_4 p O_2^4} \quad \text{after Adair} \quad (1)$$

further by differential calculus:

$$SO_{2} = 25 pO_{2} \frac{d}{dpO_{2}} \left\{ \ln \left(1 + A_{1}pO_{2} + A_{2}pO_{2}^{2} + A_{3}pO_{2}^{3} + A_{4}pO_{2}^{4}\right) \right\}$$
(2)

continued:

$$SO_{2} = 125 \ pO_{2} \cdot \\ \ln \left\{ \frac{1 + A_{1}(pO_{2} + 0.1) + A_{2}(pO_{2} + 0.1)^{2} + A^{3}(pO_{2} + 0.1)^{3} + A_{4}(pO_{2} + 0.1)^{4}}{1 + A_{1}(pO_{2} - 0.1) + A_{2}(pO_{2} - 0.1)^{2} + A_{3}(pO_{2} - 0.1)^{3} + A_{4}(pO_{2} - 0.1)^{4}} \right\}$$
(3)

| LBL | R/S | 7        | R/S            | ST03     | EEX  | CHS             |               | +      | ÷        |
|-----|-----|----------|----------------|----------|------|-----------------|---------------|--------|----------|
| A   | •   |          | x              | •        | CHS  |                 | +             | RCL2   | f        |
| 7   | 0   | •        | ST01           | <b>2</b> |      | -               | RCL2          | x      | $\ln$    |
| •   | 0   | 0        | •              | CHS      | RCL2 | RCL2            | x             | 1      | 1        |
| 4   | 1   | 3        | 3              | STO      | x    | x               | <sup>2)</sup> | +      | <b>2</b> |
| -   | 3   | 1        | +              | +        | 4)   | <sup>3)</sup> 🗌 |               | RCL3   | 5        |
| •   | x   | x        | ST02           | <b>2</b> |      |                 |               | gx≓y   | Х        |
| 1)  |     | -        | CLX            | 5)       |      |                 | EEX           | gx > y | RCL1     |
|     | R/S | $f^{-1}$ | $\mathbf{LBL}$ |          |      | EEX             | CHS           | ĞTO    | x        |
| x   | 3   | log      | 8              |          | EEX  | CHS             |               | 8      | RTN      |

Program 1 (Adair)

The sign  $\Box$  is used for digits and exponents of constants to be set in: Man<sup>a</sup>: 1) B = 0.48; 2) A<sub>1</sub> = 257 EEX CHS4; 3) A<sub>2</sub> = 780 EEX CHS6; 4) A<sub>3</sub> =

4440 EEX CHS9; 5)  $A_4 = 255$  EEX CHS8.

(Maximal deviation from listed values:  $\Delta S = \pm 1.2 \text{ S}^{0}/_{0}$ , compare with Fig.1). Man (own calculation<sup>b</sup>): 1) B = 0.48; 2) A<sub>1</sub> = 972 EEX CHS5; 3) A<sub>2</sub> = 177 EEX CHS5; 4) A<sub>8</sub> = 210 CHS EEX CHS7; 5) A<sub>4</sub> = 259 EEX CHS8.

(Maximal deviation from listed values:  $\Delta S = \pm 0.7 S^0/_0$ ).

Rat<sup>c</sup>: 1) B = 0.47; 2) A<sub>1</sub> = 310 EEX CHS4; 3) A<sub>2</sub> = 190 EEX CHS6; 4) A<sub>3</sub> = 5200 EEX CHS9; 5) A<sub>4</sub> = 077 EEX CHS8.

(No listed values available, deviation therefore not to be calculated).

| Running | program | : |
|---------|---------|---|
|         | 1 0     |   |

| Input        | Units  | Key                     | Output | Units |  |
|--------------|--------|-------------------------|--------|-------|--|
| pH           |        | Α                       |        |       |  |
| BE (or zero) | mval/l | R/S                     |        |       |  |
| т            | °C     | $\mathbf{R}'$           |        |       |  |
| $pO_2$       | mm Hg  | $\mathbf{R}/\mathbf{S}$ | $SO_2$ | Sº/0  |  |

The first 33 steps are used for standardizing the  $pO_2$  according to Eq. (2), steps 34-100 to Eq. (1).

<sup>a</sup>  $A_1 - A_4$  after Roughton and Severinghaus (1973).

<sup>b</sup> Executed after the method of smallest squared deviations on a Telefunken TR 440 computer (Rechenzentrum der Universität Würzburg).

<sup>c</sup> B after Turek et al. (1972); A<sub>1</sub>-A<sub>4</sub> after Turek et al. (1973).

The 4 determined coefficients  $A_{1-4}$  were ascertained from a recent article (Roughton and Severinghaus, 1973) and are given in Program 1. In this Program 1 the conversion of  $pO_2$  to  $SO_2$  requires 67 program steps (including the insertion of the constants); there remain 33 steps for determining the standardized  $pO_2$  in the beginning of the program, so that it was calculated with a constant Bohr factor B and an inserted base excess (BE), which can be obtained from the values of the acid-base status according to Program 4<sup>1</sup>. In the relationship between  $SO_2$  and

<sup>&</sup>lt;sup>1</sup> Equations for the standardization of the  $pO_2$ , in which  $pCO_2$  enters directly instead of BE, were not used, because there are no data available concerning the resulting much lower Bohr factor in other species (man: B = -0.40).

 $pO_2$ , a variable Bohr factor for different species can be used. The appropriate standardization corresponds to the equation specified by Severinghaus (1966):

$$\Delta (\log pO_2) = B \cdot (pH - 7.4) + 0.0013 BE - 0.031 (T - 37);$$
  
[BE in mval, T in °C]. (4)

The maximal systematic deviations of oxygen saturation appearing from the use of Program 1 are for man  $\pm 1.2$  % saturation (S<sup>0</sup>/<sub>0</sub>) compared with the original values. If the BE is determined only by sample taking at random or is unknown entirely, the following deviations of the calculated saturations arise additionally:

A deviation of the real BE from the keyed BE (or from a BE = 0) called  $\triangle$  BE leads to the following differences in per cent saturation  $\triangle$  SO<sub>2</sub>:

| ⊿BE  | $\leq$              | 5  mval/l  | leads to $\Delta SO_2 \leq$ | ≤ :      | $\pm 1.5$ S°/o                          |
|------|---------------------|------------|-----------------------------|----------|---|
| 5.1  | $\mathbf{to}$       | 10  mval/l | leads to $\Delta SO_2 \leq$ | $\leq$   | $\pm 2.0$ S <sup>0</sup> / <sub>0</sub> |
| 10.1 | $\operatorname{to}$ | 15 mval/l  | leads to $\Delta SO_2 \leq$ | $\leq$   | $\pm 3.0  { m S}^{0}/_{0}$              |
| 15.1 | $\mathbf{to}$       | 20  mval/l | leads to $\Delta SO_2 \leq$ | $\leq$ : | $\pm 4.0  {\rm S}^{0}/_{0}$             |

[The deviations were calculated according to Mengden *et al.* (1969) and Thews (1971)]. Therefore it is necessary to decide in each individual case, how much of an expected deviation of BE may be tolerated.

An attempt to express the oxyhemoglobin dissociation curve for various animal species by the Adair equation by means of calculated factors  $A_1 - A_4$  partially resulted in greater systematic deviations. Kelman (1966) used an analogous equation with 7 coefficients which, however, becomes inexact in the range of lower saturations. A later paper of Thomas (1972) avoids this shortcoming, but it is very difficult or impossible to calculate the given coefficients with a comparable accuracy in some species. The same holds for an Fortran subroutine of Aberman et al. (1973) with 8 constants. A method of approximation according to Heise and Schmidt (1973) involves considerable requirements to the computer and must be performed each time for a special species with supporting points. Relationships used by Maas et al. (1972) in the course of a determination of acid-base parameters trace back to Hill's equation and involve the restrictions mentioned above. However, it appeared that deviations of  $\pm 0.9$  S<sup>0</sup>/<sub>0</sub> may be obtained with a much less extensive method, additionally making possible a reverse procedure to calculate  $pO_2$  from saturation values (Program 3). The method is described in the following section.

# **II. 3-Segment Equations**

The oxyhemoglobin dissociation curve may be described by 3 segments, whereby the curve is approximated by a parabola in the first segment (low saturations;  $SO_2$  in  $^0/_0$  saturation):

$$SO_2 = K_1 p O_2^2 + K_2 p O_2.$$
 (5)

This equation is valid in different species up to a  $SO_2$  of  $19-51 S^0/_0$  ("a"). In the following segment the curve is reproduced by the equation of a straight line:

$$\mathrm{SO}_2 = \mathrm{K}_3 p \mathrm{O}_2 - \mathrm{K}_4. \tag{6}$$

In the last segment, beginning in different species at  $41-80 \text{ S}^{0/_{0}}$  ("b") the dissociation curve is approximated by the equation:

$$SO_2 = \frac{100}{\left(\frac{K_5}{pO_2}\right)^{K_s} + 1}$$
 (7)

The equivalent programming (Program 2) requires 62 steps with 2 logical decisions for the limits a and b, so that 38 steps remain for the

|               |     |                   |                         | -               |               |             |      |             |                |
|---------------|-----|-------------------|-------------------------|-----------------|---------------|-------------|------|-------------|----------------|
| LBL           | R/S | 7                 | $\mathbf{R}/\mathbf{S}$ | RCL1            | gx≤y          |             | 6)   |             | x              |
| A             | •   |                   | x                       | <sup>3)</sup> 🗌 | GTO           | •           |      | g           | $\mathbf{RTN}$ |
| 7             | 0   | •                 | ST01                    |                 | 8             |             | •    | $\lambda_x$ | LBL            |
| •             | 0   | 0                 | ↑                       |                 | <sup>4)</sup> | —           |      | 1           | 8              |
| 4             | 1   | 3                 | x                       |                 | •             | р           |      | +           | RTN            |
|               | 3   | 1                 | 2).                     | x               |               |             | RCL1 | g           |                |
| 1).           | x   | x                 |                         | +               |               | gx⇔y        | ÷    | 1/x         |                |
|               | +   |                   |                         | a 📋             | RCL1          | $gx \leq y$ | 7) 🗌 | 1           |                |
|               | R/S | f1                |                         |                 | x             | GTO         | •    | 0           |                |
| x             | 3   | log               | x                       | gx⇒y            | 5)            | 8           |      | 0           |                |
| Input         |     | $\mathbf{U}$ nits |                         | Keys            |               | Outpu       | t    | Units       |                |
| $_{\rm pH}$   |     |                   |                         | A               |               |             |      |             |                |
| $\mathbf{BE}$ |     | mval/l            |                         | R/S             |               |             |      |             |                |
| т             |     | °C                |                         | R/S             |               |             |      |             |                |
| $pO_2$        |     | mm Hg             | i                       | R/S             |               | $SO_2$      |      | Sº/0        |                |

Program 2 (3 segments)

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| Species                  | 1. Bohr<br>factor | Cha<br>seg<br>men<br>[S <sup>0</sup> /<br>a | inge<br>-<br>nts<br>/ <sub>0</sub> ]<br>b | 2. K <sub>1</sub> | 3. K <sub>2</sub> | 4. K <sub>3</sub> | 5. $K_4$ | 6. K <sub>5</sub> | 7. K <sub>6</sub> | ⊿S<br>[S⁰/₀]    |
|--------------------------|-------------------|---|---|-------------------|-------------------|-------------------|----------|-------------------|-------------------|-----------------|
| Man <sup>1</sup>         | 0.481             | 40  | 56  | 0.062             | 0.351             | 2.50              | 16.9     | 27.00             | 2.80              | +0.6            |
| Horse <sup>2</sup>       | 0.482             | 19  | 46  | 0.075             | 0.244             | 2.86              | 22.1     | 25.18             | 2.87              | $\pm 0.0 + 0.3$ |
| Cow <sup>3</sup>         | 0.496             | 28  | 38  | 0.052             | 0.109             | 2.38              | 24.9     | 30.80             | 3.25              | +0.6            |
| Pig <sup>3</sup>         | $0.42^{6}$        | 22  | 41  | 0.041             | 0.331             | 2.56              | 27.7     | 30.60             | 2.79              | +0.5            |
| Sheep <sup>3</sup>       | 0.436             | 19  | 41  | 0.040             | 0.113             | 2.35              | 28.8     | 33.70             | 2.87              | +0.3            |
| Dog <sup>3</sup>         | 0.506             | <b>23</b>                                   | <b>46</b>                                 | 0.059             | 0.267             | 2.35              | 18.9     | 29.11             | 3.13              | +0.5            |
| Rabbit <sup>3</sup>      | $0.45^{6}$        | <b>29</b>                                   | <b>58</b>                                 | 0.022             | 0.806             | 2.53              | 27.7     | 30.70             | 3.28              | +0.6            |
| Cat <sup>3</sup>         | $0.54^{6}$        | <b>4</b> 0                                  | 66  | 0.035             | 0.192             | 1.87              | 18.4     | 38.80             | 4.10              | +0.9            |
| Guinea pig <sup>3</sup>  | $0.47^{6}$        | <b>4</b> 0                                  | 66  | 0.047             | 0.622             | 2.38              | 15.4     | 28.45             | 3.48              | +0.9            |
| Rat <sup>4</sup>         | 0.477             | 22  | <b>58</b>                                 | 0.020             | 0.535             | 1.91              | 20.8     | 36.71             | 2.70              | +0.5            |
| Golden                   | 0.415             | 51  | <b>64</b>                                 | 0.028             | 1.04              | 2.77              | 26.3     | 26.39             | 2.78              | +0.9            |
| Hamster <sup>5</sup>     |                   |   |   |                   |                   |                   |          |                   |                   |                 |
| White mouse <sup>5</sup> | $0.63^{5}$        | 25  | 80  | 0.021             | 0.975             | 1.65              | 05.3     | 40.69             | 5.70              | $\pm 0.9$       |

Program 2 (continuted)

<sup>2</sup> Baumann *et al.* (1963).
 <sup>3</sup> Bartels and Harms (1959).

<sup>6</sup> Hilpert *et al.* (1961).

<sup>7</sup> Turek et al. (1972).

<sup>4</sup> Turek et al. (1973).

initial standardization. Gaps at the transition of the segments lead to errors in the limits mentioned below the program. A fixed value for BE is to be keyed; this (just as for the first program) is evaluated besides other values of the acid-base status with a special program (nr. 4). A comparison of the systematic deviations between values of the human dissociation curve taken from Roughton and Severinghaus (1973) and those calculated after the Adair method and our 3-segment method is given in Fig. 1.

In a third program the reverse conversion of  $O_2$  saturation into standardized  $pO_2$  is made possible using the same 7 constants as in Program 2. Either an additional temperature correction or a correction for the actual pH value using the special Bohr factor can be made.

Programs for the calculation of the acid-base status by computers have been described to a different extent by Jalowaysky *et al.* (1968), Hardt (1972), Maas *et al.*, (1972). It could be shown, however, that already 7 important values may be determined with a limited number of steps to a great degree of accuracy by a selection of relationships—partly taken from nomograms empirically. The equations underlying these calculations are presented below Program 4.



Fig.1. Systematic deviations between 27 values of the oxyhemoglobin dissociation curve for humans according to Roughton and Severinghaus (1973) and their Adair approximation (dashed line) and the 3-segment approximation (solid line). In the latter in no case the deviation exceeds  $\pm 0.7 \text{ S}^{0}/_{0}$ . The dotted line stands for the gaps

## Discussion

The handiness of a pocket calculator opens ranges of application which hitherto were covered either exclusively by nomograms or by a system in which compiled data were fed into a much larger computer, frequently loaded with numerous other functions. As has been described, substantial information is available already from 100 program steps; for more extensive calculations additional programs may be attached. The lack of a printout of numerical values has to rank as a disadvantage; but it should be taken into consideration that the normal one-column printing of most desk calculators requires further tabulation; a multicolumn printing to tabulations is possible only with much larger computers.

The constants used for the programs can also be replaced by additional instructions later on. Thus studies have been presented for the influence of 2,3-diphosphoglycerate (Benesch and Benesch, 1967; Chanutin and Curnish, 1967; Sigaard-Andersen and Salling, 1961), for the variation of the Bohr factor in the range of extreme oxygen saturations (Glauser and Forster, 1967; Kernohan and Forster, 1967; Kernohan and Roughton, 1972), for large variations of pH (Karmann *et al.*, 1971; Roughton and Severinghaus, 1973), and for the different influence of fixed acids against  $pCO_2$  variations (Naeraa *et al.*, 1963; Kirschbaum, J. Lutz et al.

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|          | Program 3 (reverse program) |                |                      |                 |                |          |            |                |  |  |  |
|----------|-----------------------------|----------------|----------------------|-----------------|----------------|----------|------------|----------------|--|--|--|
| LBL      |                             | ÷              | 6)                   | RCL1            | ÷              | 2        | ,<br>↓     | ST05           |  |  |  |
| Α        | gx > y                      | 7)             |                      | <sup>5)</sup> 🗌 | ST05           | ÷        | RCL1       | $\mathbf{RTN}$ |  |  |  |
| ST01     | GTO                         | •              | •                    |                 | $\mathbf{RTN}$ | <b>†</b> | x          |                |  |  |  |
| a 🗌      | 1                           |                |                      | •               | $\mathbf{LBL}$ | ↑        | +          |                |  |  |  |
|          | 1                           |                |                      |                 | 2              | x        | f          |                |  |  |  |
| gx > y   | 0                           | $\mathbf{CHS}$ | x                    | +               | 3)             | 2).      | $\sqrt{-}$ |                |  |  |  |
| GTO      | 0                           | g              | STO5                 | 4) 🗌            |                |          | gx⇒y       |                |  |  |  |
| <b>2</b> | RCL1                        | 1/x            | $\operatorname{RTN}$ | ٠               |                |          |            |                |  |  |  |
| RCL1     |                             | g              | LBL                  |                 |                |          | RCL2       |                |  |  |  |
| рП       | RCL1                        | yx             | 1                    |                 | 1              | STO2     | ÷          |                |  |  |  |

Factors to be set in see below program 2.

Continued by

| LBL<br>B<br>3<br>7<br> | 1<br>x<br>f <sup>-1</sup><br>log<br>RCL5<br>x<br>RTN | LBL<br>B<br>7<br>4<br> | CHS<br>x<br>f-1<br>log<br>RCL5<br>x<br>RTN |
|------------------------|--|------------------------|--|
| 0                      |  | <br>1).                | RTN  |
| 3                      |  |                        |  |

temp. correction

pH correction

|                            | Input           | Units | Key | Output                             | Units                                 |
|----------------------------|-----------------|-------|-----|------------------------------------|---------------------------------------|
| $(O_2 \text{ saturation})$ | SO <sub>2</sub> | Sº/0  | A   | $p\mathrm{O}_{2\mathrm{St}}$       | mm Hg                                 |
| (temp. correction)         | т               | °C    | в   | $p\mathrm{O}_{2\ \mathrm{T-cor}}$  | ${ m mm}~{ m Hg}$                     |
| (pH correction)            | $\mathbf{pH}$   |       | В   | $p\mathrm{O}_{2\ \mathrm{pH-cor}}$ | $\operatorname{mm} \operatorname{Hg}$ |

1963; Garby et al., 1972), whereby decisive evaluations of the degree of their mutual influence are not yet possible. These studies mainly refer to the problem of the  $pO_2$  conversion to standard conditions, from which the oxygen saturation is determined as described with a fixed program. Even when several supplementary programs are needed the instant availability of a pocket calculator provides important advantages.

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| LBL  | •      | STO2     | 6        | 9        | 4    | ÷        | ST05 | 4      | •              |
|------|--------|----------|----------|----------|------|----------|------|--------|----------------|
| A    | 1      | R/S      | •        | _        | 1    | 1        | R/S  | +      | <b>2</b>       |
| .    |        | RCL1     | 8        | ST03     | •    |          | •    | ST06   | x              |
| 0    | f-1    | •        | 8        | R/S      | 7    | RCL8     | 0    | 6      | ST07           |
| 3    | $\log$ | 7        | x        | STO8     | +    | •        | 1    | •      | $\mathbf{RTN}$ |
| x    | RCL7   | 7        | +        | •        | ST04 | <b>2</b> | 4    | 1      |                |
| ST07 | x      | <b>5</b> | <b>2</b> | 4        | R/S  | x        | 5    |        |                |
| R/S  | ST01   | x        | 1        | <b>2</b> | 1    | x        | x    | f-1    |                |
| ST06 | RCL7   | RCL6     | 7        | x        | 0    | RCL3     | 7    | $\log$ |                |
| 6    | +      | 2        | •        | +        | 0    | +        | •    | 1      |                |

Program 4 (acid-base status)

| Input         | Units           | Key | Output        | Units  | Content<br>of register           | Register<br>number |
|---------------|-----------------|-----|---------------|--------|----------------------------------|--------------------|
| $pCO_2$       | mm Hg           | A   | $0.03 \ pCO2$ | mm Hg  | HCO3                             | 1                  |
| $\mathbf{pH}$ |                 | R/S | tot. $CO_2$   | mmol/l | tot. $CO_2$                      | <b>2</b>           |
| -             |                 | R/S | $BE_{ac}$     | mval/l | $BE_{ac}$                        | 3                  |
| Hb            | g/100 ml<br>bl. | R/S | BB            | mval/l | BB                               | 4                  |
| $SO_2$        | Sº/0            | R/S | $BE_{ox}$     | mval/l | BEox                             | 5                  |
|               |                 | R/S | HCO3s         | mval/l | $\mathrm{pH_s}$                  | 6                  |
|               |                 |     |               |        | $\mathrm{HCO}_{8}^{-}\mathrm{s}$ | 7                  |

 $\text{HCO}_{3} = 0.3 \text{ } p\text{CO}_{2} \cdot 10^{\text{(pH-6.1)}}$  (Henderson-Hasselbalch equation).

tot.  $CO_2 = HCO_3 + 0.03 pCO_2$ 

BE  $_{ae} = 0.775 \text{ HCO}_3 + 26.88 \text{ pH} - 217.9$  (empirical after Thews nomogram, 1971)

 $BE_{ox} = BE_{ac} + 0.2 \text{ Hb} \left( \frac{SO_2}{100} - 1 \right)$  (after Siggaard-Andersen and Salling, 1971)

 $BB = BE_{ac} + 41.7 + 0.42 \text{ Hb}$  (after Siggaard-Andersen, 1963).

 $pH_s = 0.0145 BE_{ox} + 7.4$  (empirical after Thews nomogram, 1971).

 $HCO_{3.5} = 1.2 \cdot 10 \ (pH_s^{-6.1})$  (Henderson-Hasselbalch equation).

 $Hb = hemoglobin; BE_{ac} = actual BE; BB = buffer base; BE_{ox} = BE for oxygenated blood; pH<sub>s</sub> = standard pH; HCO<sub>3</sub> = standard bicarbonate.$ 

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