

# Enhancement of Oscillatory Stability of a Grid Integrated Microgrid by Optimized Governor Damping Action



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**Abstract** An optimized mechanical damping torque is proposed in the present work provided by the synchronous generator governor to improve oscillatory stability for a grid integrated micro grid. Small signal modelling of micro grid with grid has been considered here with uncertain variations in solar and wind power generations. The gains of the governor are optimized by the Random Walk Grey wolf optimizer (RWGO) in contrast to PSO and GWO algorithms. Pertained to uncertain variations in solar and wind variations, time and frequency analysis have been conducted to observe effective damping by governor action. It has been found that intermittency in solar and wind generation variations create a challenge for oscillatory instability and the governor can impart adequate damping torque if its gains are properly set by an efficient control law. The excitation system of the generator is kept fixed at an initial operating condition by RWGO. The ITAE criterion is selected for the minimization problem for which a step change of 10percent of input mechanical power is executed. The aggravation of oscillations due to variations in renewable penetration can be damped and compensated by the phase lead provided by tuned governor action.

**Keywords** Governor · Wind source · SPV · Random walk GWO · Oscillatory stability

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## 1 Introduction

Microgrid (MG) plays a vital role for reliable and economic operation of a power system. The reliability includes stabilising voltage and frequency. When a MG is connected to a grid, there are several challenges for a system operator out of which an important issue is the dynamical interaction of low inertia MG with the conventional grid. The MG may be of AC, DC or hybrid type and may include synchronous generation, induction generation or generation based on different power electronics converters. For the dynamic stability study of MG a linearized model of MG along with other power system components is needed. The linear modelling of various power systems has been reported by different researchers [1–3]. The low frequency Heffron Phillips modelling of the power system has been employed in many research studies for linear modelling [4–7]. In [8], a generalised modelling of MG has been reported and in [9] KVL and KCL have been employed for MG modelling. But estimating the MG and control action parameters are reported [10, 11]. The equivalent model of MG has been reported in many research studies including black box theory as in [12–14] or using mathematical modelling as in [15]. A linear equivalent model of MG connected to the grid has been presented in [16] which has been considered in this work with optimal tuning of the governor parameters for the synchronous generator of MG. An important issue is selection of proper gains for creating an effective damping torque and for which a suitable algorithm can be applied. In [5] a modification of the GWO algorithm called random walk GWO is proposed as a challenging technique in contrast to prevailing algorithms. This algorithm is proposed here to tune governor gains and has been compared with PSO and GWO algorithms for justification of tuning efficacy.

## 2 Low Frequency Model of Micro Grid

### 2.1 Synchronous Generator-Based MG Modelling

The low frequency MG model considered here is based on modification of the small signal Heffron Phillips model [5] including the governor and excitation system. Figure 1 represents the single line diagram of MG connected to an infinite bus. Figure 2 shows the IEEE ST6B excitation system considered in this work and Fig. 3 depicts the equivalent turbine governor model. Equations describing the MG are presented by [16]

$$\frac{dw}{dt} = \frac{1}{2H}(T_m - T_e - T_D)$$

$$\frac{d\delta}{dt} = \omega_b(\omega - 1)$$

$$\frac{de'_q}{dt} = \frac{1}{T'_{d0}} [E_{fd} - e'_q - (X_d - X'_d)i_d] \quad (1)$$

$$i = i_d + ji_q$$

$$v_t = v_d + jv_q$$

$$V_{pcc} = v_{pcc}(\sin \delta + j \cos \delta)$$

$$Z = R + jX \quad Y = G + jB$$

$$C_1 + jC_2 = 1 + ZY$$

$$R_1 = R - C_2X'_d, \quad R_2 = R - C_2X_q$$

$$X_1 = X + C_1X_q, \quad R_2 = R - C_2X_q$$

$$X_1 = X + C_1X_q, \quad X_2 = X - C_1X'_d$$

$$Z_e^2 = R_1R_2 + X_1X_2$$

$$Y_d = (C_1X_1 - C_2R_2)/Z_e^2$$

$$Y_q = (C_1R_1 - C_2X_2)/Z_e^2 \quad (2)$$

$$v_{d0} = P_0v_{t0} [P_0^2 + (Q_0^2 + v_{t0}^2/X_q)^2]^{-1/2}$$

$$V_{q0} = (V_{t0}^2 - V_d^2)^{1/2}$$

$$i_{q0} = \frac{vd0}{X_q} i_{d0} = (P_0 - i_{q0}v_{q0})/v_{d0}$$

$$e'_{q0} = v_{q0} + X'_d i_{d0}$$

$$v_{pccd0} = C_1 v_{d0} - C_2 v_{q0} - R i_{d0} + X i_{q0}$$

$$v_{pccq0} = C_2 v_{d0} + C_1 v_{q0} - X i_{d0} - R i_{q0}$$

$$\delta_0 = \tan^{-1} \left( \frac{v_{pccd0}}{v_{pccq0}} \right)$$

$$i_{Ld0} = G v_{d0} - B v_{q0} \quad i_{Lq0} = G v_{q0} + B v_{d0}$$

$$i_{Lined0} = i_{d0} - i_{Ld0} \quad i_{Lineq0} = i_{q0} - i_{Lq0} \tag{3}$$

By Kirchoff's voltage law the parameters are presented as:

$$Zi = (1 + ZY)v_t - v_{pcc}$$

$$\begin{bmatrix} R & -X \\ X & R \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} = \begin{bmatrix} C_1 & -C_2 \\ C_2 & C_1 \end{bmatrix} \begin{bmatrix} v_d \\ v_q \end{bmatrix} - v_{pcc} \begin{bmatrix} \sin \delta \\ \cos \delta \end{bmatrix} \tag{4}$$

**Wind power generation**

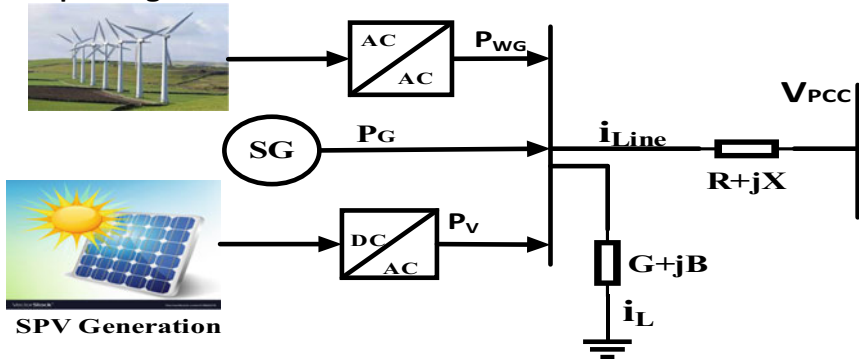


Fig. 1 SG with SPV and wind source connected to infinite bus

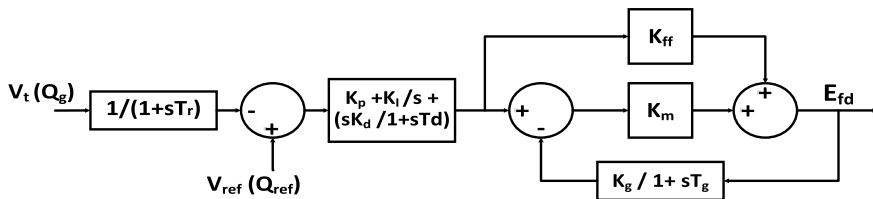


Fig. 2 IEEE-ST6B excitation system

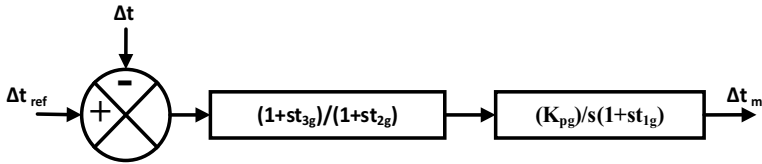


Fig. 3 Equivalent turbine governor modelling

As per the voltage and currents in d and q axis are stated as:

$$\begin{bmatrix} v_d \\ v_q \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} e'_q - \begin{bmatrix} 0 & -X_q \\ X'_d & 0 \end{bmatrix} \begin{bmatrix} i_d \\ i_q \end{bmatrix} \tag{5}$$

By combining Eqs. (4) and (5) the equations are presented as

$$\begin{bmatrix} i_d \\ i_q \end{bmatrix} = \begin{bmatrix} Y_d \\ Y_q \end{bmatrix} e'_q - \frac{v_{pcc}}{Z_e^2} \begin{bmatrix} R_2 & X_1 \\ -X_2 & R_1 \end{bmatrix} \begin{bmatrix} \sin \delta \\ \cos \delta \end{bmatrix} \tag{6}$$

And which can be linearized as

$$\begin{bmatrix} \Delta i_d \\ \Delta i_q \end{bmatrix} = \begin{bmatrix} Y_d \\ Y_q \end{bmatrix} \Delta e'_q + \begin{bmatrix} F_d \\ F_q \end{bmatrix} \Delta \delta \tag{7}$$

For which

$$\begin{bmatrix} F_d \\ F_q \end{bmatrix} = \frac{v_{pcc}}{Z_e^2} \begin{bmatrix} -R_2 & X_1 \\ X_2 & R_1 \end{bmatrix} \begin{bmatrix} \cos \delta_0 \\ \sin \delta_0 \end{bmatrix} \Delta e'_q \tag{8}$$

In the Heffron–Phillips model, the input signals have relations with the variables by the K-constants. So the torque and real powers are presented as:

$$T_e = p = i_d v_d + i_q v_q$$

$$\Delta T_e = K_1 \Delta \delta + K_2 \Delta e'_q$$

$$\begin{bmatrix} K_1 \\ K_2 \end{bmatrix} = \begin{bmatrix} 0 \\ i_{q0} \end{bmatrix} + \begin{bmatrix} F_d & F_q \\ Y_d & Y_q \end{bmatrix} \begin{bmatrix} (X_q - X_d) i_{q0} \\ e'_{q0} + (X_q - X'_d) i_{d0} \end{bmatrix} \tag{9}$$

The equation of internal voltage in Eq. (1) is linearized as

$$(1 + sT'_{d0}) \Delta e'_q = \Delta E_{fd} - (X_d - X'_d) \Delta i_d \tag{10}$$

And using Eq. (7) we can write Eq. (11) as:

$$(1 + sT'_{d0})\Delta e'_q = K_3[\Delta E_{fd} - K_4\Delta\delta]$$

$$K_3 = 1/[1 + (X_d - X'_d)Y_d]$$

$$K_4 = (X_d - X'_d)F_d \tag{11}$$

The state variables can be linked with output reactive power as Eq. (12).

$$Q = i_d v_q - i_q v_d$$

$$\Delta Q = K_5\Delta\delta Z + K_6\Delta e'_q$$

$$\begin{bmatrix} K_5 \\ K_6 \end{bmatrix} = \begin{bmatrix} 0 \\ i_{d0} \end{bmatrix} + \begin{bmatrix} F_d & F_q \\ Y_d & Y_q \end{bmatrix} \begin{bmatrix} e'_{q0} - 2X_d i_{d0} \\ -2X_q i_{q0} \end{bmatrix} \tag{12}$$

$K_1$  to  $K_5$  are constants for small signal model of the generator. The equivalent model of grid integrated MG can be formed by Eqs. (9), (11) and (12). The small signal model of MG is presented in Fig. 4 where the governor parameters are to be set optimally to provide adequate damping torque. Here the SPV and wind sources are integrated.  $K_v, T_v$  are gain and time constants for the SPV system,  $K_{wg}, T_{wg}$  are gain and time constants for the wind energy conversion system.

The active and reactive powers at PCC are given by Eqs. (13) and (14):

$$P_{pcc} = v_{pcc}i_{Lined} + v_{pccq}i_{Lineq}$$

$$Q_{pcc} = v_{pcc}i_{Lined} - v_{pccd}i_{Lineq} \tag{13}$$

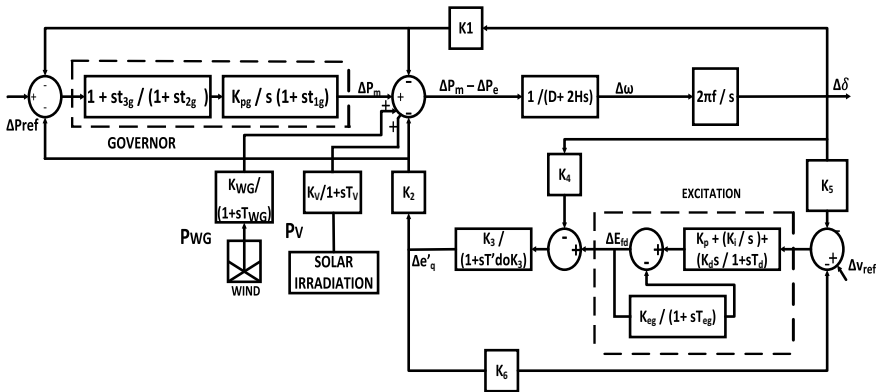


Fig. 4 Small signal MG modelling

$$\Delta P_{pcc} = \Delta v_{pcc} i_{Lined0} + v_{pccd0} \Delta i_{Lined} + \Delta v_{pccq} i_{Lined} + v_{pccq0} \Delta i_{Lineq}$$

$$\Delta Q_{pcc} = \Delta v_{pccq} i_{Lined0} + v_{pccq0} \Delta i_{Lined} - \Delta v_{pccd} i_{Lineq0} - v_{pccd0} \Delta i_{Lineq} \quad (14)$$

### 3 Governor Control Action and Objective Function

In the small signal model of Fig. 4, the governor parameters are  $K_g$ ,  $t_{1g}$ ,  $t_{2g}$ ,  $t_{3g}$  and  $t_{4g}$  that represent the governor control action and these parameters are to be tuned by the RWGO algorithm. The flow chart of the proposed control scheme is presented in Fig. 5. The objective of the present work is to damp out the electromechanical oscillations followed by disturbances. So, an ITAE based objective function is chosen here.

$$J = \int_0^{tsim} t |\Delta \omega| dt \quad (15)$$

Subject to constraint

$$K_{pg}^{\min} \leq K_{pg} \leq K_{pg}^{\max},$$

$$t_{1g}^{\min} \leq t_{1g} \leq t_{1g}^{\max}, \quad t_{2g}^{\min} \leq t_{2g} \leq t_{2g}^{\max}$$

$$t_{3g}^{\min} \leq t_{3g} \leq t_{3g}^{\max}$$

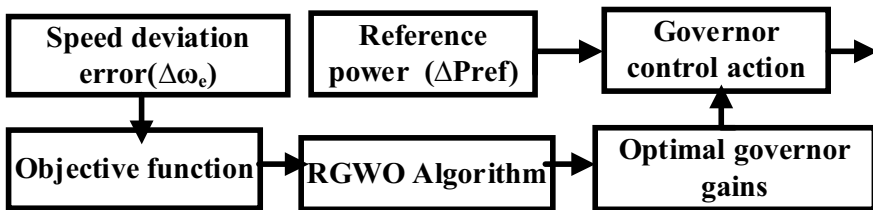


Fig. 5 Flow chart of proposed control scheme

## 4 Random Grey Wolf Optimiser Algorithm

GWO has been implemented by many researchers in different areas of applications which involve around 5–11 wolves in a group which are divided as per their participation in the hunting process. There are certain merits and demerits of GWO. The demerit is that the decision regarding the group which will guide the positions of the alpha group because this group dominates the wolf pack and also the problem is whether the alpha group takes the guidance of the guidance of the lower group or not. Due to this, for each iteration in the GWO, the position of different individual wolf packs needs updation, hence premature convergence may occur in GWO. To avoid this, certain changes may be implemented in the leader pack of GWO. Also, to avoid stagnation in local optimum, in [5] the leaders explore the searching space by random walk known as Random path Grey Wolf Optimisation (RGWO) followed by finally omega wolves being presented as:

$$W_N = \sum_{i=1}^N S_i \quad (16)$$

$S_i$  being a random step can be obtained by random distributions.

Two consecutive random wolves are related as

$$W_N = \sum_{i=1}^N S_i = \sum_{i=1}^{N-1} S_i + X_N = W_{N-1} + S_N \quad (17)$$

Initiation point of wolf denoted as  $x_0$  & final as  $x_N$ , so the random wolves are represented as: -

$$x_n = x_0 + \alpha_1 S_1 + \alpha_2 S_2 + \dots + \alpha_N S_N = x_0 + \sum_{i=1}^N \alpha_i S_i \quad (18)$$

where  $\alpha_i > 0$  is a condition controlling step size  $S_i$ .

The algorithm RW-GWO step size is taken from Cauchy distribution. As the variance of Cauchy distribution is infinity, it might take longer jump sometimes which is very effective at the time of stagnation and very useful from the leader wolves exploring the search space for getting the prey and guiding other wolves. Pseudocode for RGWO is given in Table 1.

## 5 Result and Analysis

Different case studies have been conducted in the present work to justify the optimal governor actions for power oscillation damping. These case studies include sudden and discrete variations in solar and wind generations. RWGO has been implemented



**Table 1** Pseudo code of RGWO

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Initializing Populations of grey wolf  $x_i(i = 1,2,3,\dots,n)$ 
Initializing  $c, b$  &  $\mu$ 
Initializing  $l = 1$ , the ITER number
Evaluating separate wolves fitness
Selecting  $\alpha =$  fit wolf pack
 $\beta =$  best second wolf
 $\delta =$  best third wolf
While  $l <$  ITER of maximum number
Evaluating each wolf fitness
For individual wolf leader
To find new position of  $y_i$  of leader  $x_i$  by randomising wolf
if  $f(x_i) > f(y_i)$ 
leaders updatation
end
for individual wolf  $\omega$ 
updatation of position & apply greedy move in present and
updated position
end
    
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to set the governor parameters optimally. The initial stage of synchronous generators is set at 0.8 pu and 0.17 pu for real and reactive power generations, respectively. In case 1, solar generation is a step raised by 0.3 pu and the system response is presented in Fig. 6. Bode plot is presented in Fig. 7 with the RGWO algorithm. Also, in case-1 wind source is varied suddenly by 0.4 pu and eigen values depicted in Table 2. Table 3 depicts optimal governor parameters with fixed PID excitation gains. The performance of RWGO has been compared with PSO, GWO techniques. In case 2, the solar and wind powers are varied discretely as per the pattern shown in Fig. 8. The system response has been represented in Figs. 9 and 10. From the results obtained in discrete variations of solar and wind penetrations, it has been observed that the parameters of the governor when tuned by RGWO provide better damping efficacy as compared to PSO, and GWO. Also the capability of the governor can be significantly improved by properly tuning of its parameters.

## 6 Conclusion

In a micro-grid, the oscillations brought by uncertain solar and wind penetrations create challenge for maintaining oscillatory stability, which has been presented in this work. The variations in solar and wind sources are executed with step and random pattern for a micro-grid integrated with grid, and subject to this the governor gains are set optimally by the RWGO algorithm in contrast with PSO and GWO algorithms. A random walk being incorporated with GWO makes it more robust for the optimization problem and the additional lead compensation brought by governor action can provide a better damping torque to enhance oscillatory stability of the micro-grid system. System eigen analysis and frequency response plots are obtained

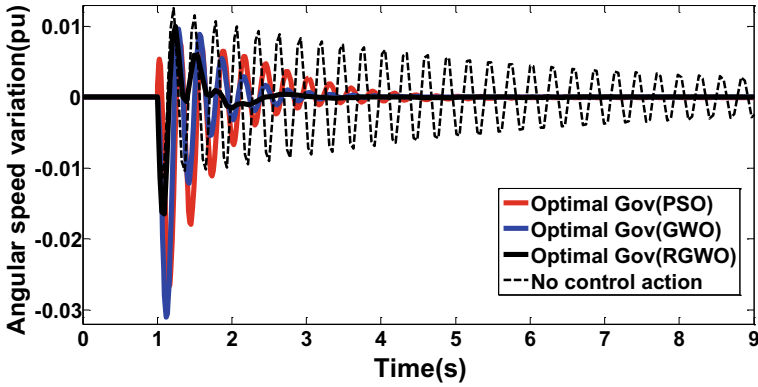


Fig. 6 Angular frequency variations

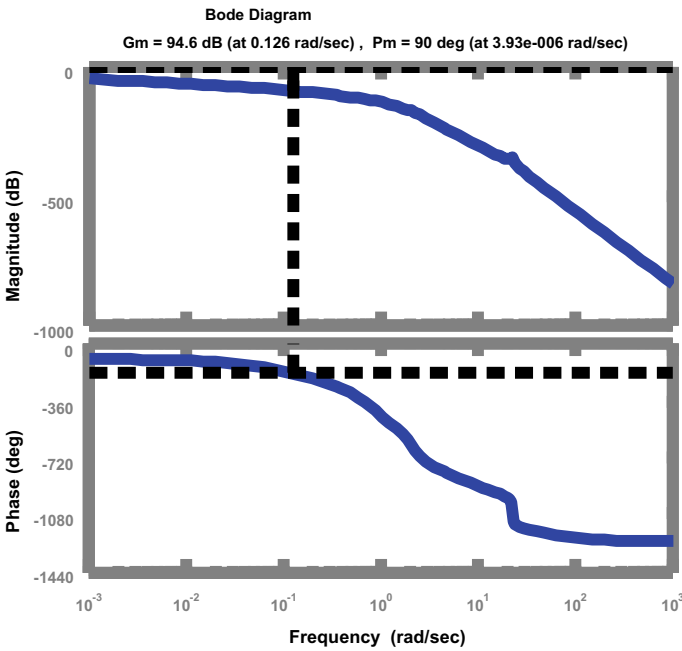


Fig. 7 Bode plot for case-1

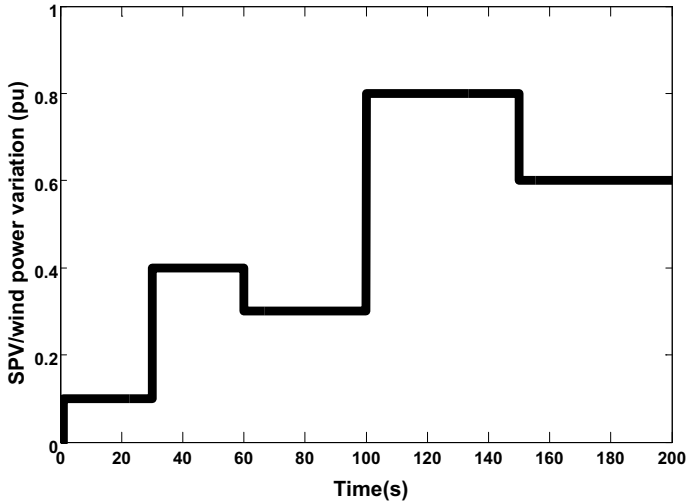
for sudden variations in solar and wind generations. It has been concluded that synchronous generator’s governor can improve oscillatory stability if its parameters are efficiently tuned by a suitable algorithm. This work was further extended with more renewable penetrations using the 33-bus micro-grid system.

**Table 2** Prominent system eigen values with SPV/wind variations

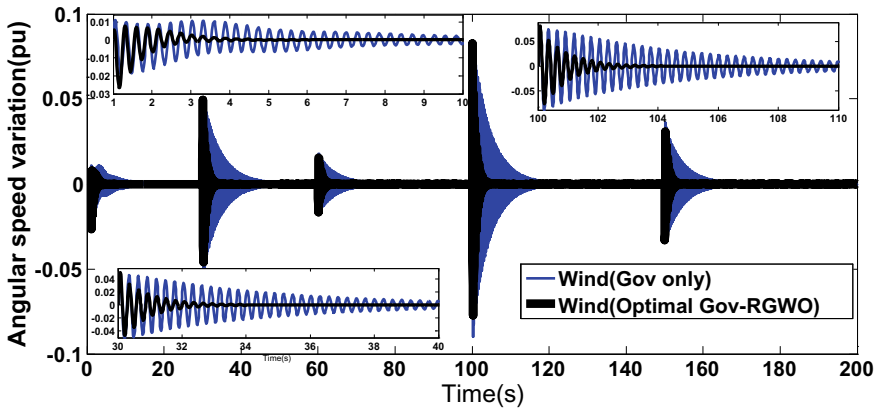
| $P_v = 0.3 pu$    | $P_w = 0.4 pu$    | $P_v = 0.3 pu$    | $P_w = 0.4 pu$    | $P_v = 0.3 pu$    | $P_w = 0.4 pu$    |
|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| PSO               |                   |                   |                   |                   |                   |
| -12.9729          | -12.4374          | -14.5330          | -14.3472          | -24.4627          | -12.7238          |
| -7.3532           | -4.1811           | -7.3470           | -3.4602           | -6.3470           | -3.4602           |
| -19.8917          | -1.2721 + 8.3590i | -20.3417          | -2.9923 + 8.1191i | -18.6417          | -3.2423 + 2.0793i |
| -13.3909          | -1.2721 - 8.3590i | -11.3209          | -2.9923 - 8.1191i | -10.4909          | -3.2423 - 2.0793i |
| -12.7067          | -16.5580          | -11.3206          | -12.4120          | -10.4406          | -11.7744          |
| -1.4711 + 3.7140i | -11.8351          | -2.8211 + 3.7220i | -10.3451          | -3.4801 + 2.2880i | -9.7851           |
| -1.4711 - 3.7140i | -2.4422           | -2.8211 - 3.7220i | -2.2289           | -3.4801 - 2.2880i | -1.2243           |
| -1.4244           | -2.1633           | -1.3666           | -2.4332           | -1.47667          | -2.6443           |
| -1.8883           | -0.4043           | -1.07661          | -0.4438           | -1.0798           | -0.4469           |
| -1.5419           | -0.4969           | -1.0762           | -0.2026           | -1.0766           | -0.2067           |
| -0.0959           | -1.1790           | -0.0723           | -1.2470           | -0.6799           | -1.2442           |
| 0.0000            | -0.0972           | 0.0000            | -0.0421           | 0.0000            | -0.0701           |
| -0.9252           | 0.0000            | -0.9529           | 0.0000            | -0.9912           | 0.0000            |
| RGWO              |                   |                   |                   |                   |                   |

**Table 3** Optimized parameters

| Gains    | Excitation parameters fixed at $Kp = 26.4988$ ,<br>$Kd = 2.5221$ , $Ki = 87.8001$ |        |        |
|----------|---|--------|--------|
|          | PSO   | GWO    | RGWO   |
| $K_{pg}$ | 1.8778  | 4.1277 | 7.2980 |
| $t_{1g}$ | 0.9987  | 0.6142 | 0.1581 |
| $t_{2g}$ | 0.1704  | 0.2788 | 0.6311 |
| $t_{3g}$ | 0.4099  | 0.6788 | 0.8278 |



**Fig. 8** SPV/wind power random variations



**Fig. 9** Angular speed variations for case-2 for varying wind source

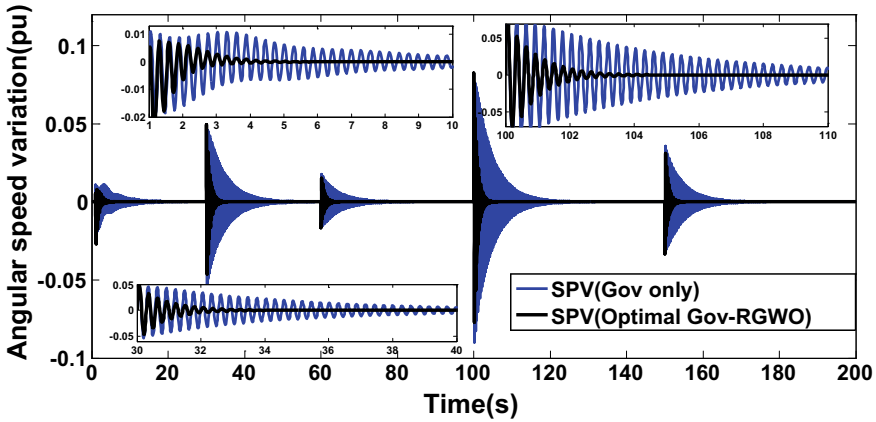


Fig. 10 Angular speed variations for case-2 for varying SPV source

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