# **Mechanical Modeling and Analysis Based on Fine Drill**



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**Abstract** The main purpose of this paper is to study the change law of the contact condition between the fine drilling tool and the workpiece surface during cutting. Firstly, the structure of the drill tip of the fine drilling tool is analyzed, and the contact force of the drill tip is effectively decomposed. Then, on the basis of considering the cutting edge radius, the cutting mechanics model of each part of the drill tip was established according to the theory of slip line field. Finally, drilling experiments under different cutting conditions were carried out to solve the contact coefficient between the tool and the workpiece surface. The research shows that the high feed leads to greater ploughing effect in cutting, resulting in sharp change of contact force, which provides a research direction for tool tip design.

**Keywords** Fine drill · Main cutting edge · Chisel edge · Slip line field · Ploughing

# **1 Introduction**

As an important part of aerospace engine, the injection plate is distributed with thousands of small holes. The size range of these holes belongs to the mesoscopic scale [\[1\]](#page-9-0), and their geometric parameters play an important role in propellant injection performance and combustion stability in rocket engines. Therefore, it is of great

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significance to establish the mechanical model and analyze its mechanical characteristics in the process of fine-hole cutting to improve the machining quality of injection plate and reduce the engine failure.

Fine drilling is essentially similar to conventional drilling and has many similarities in mechanical properties of cutting. However, the natural difference in the size magnitude also causes the mechanical properties to be different, which will be affected by the size effect  $[2]$ , cutting edge radius  $[3]$ , minimum cutting thickness [\[4\]](#page-9-3) and other factors.

Abouridouane et al. [\[5\]](#page-9-4) analyzed the scale effect in the cutting process of twist drill and established a three-dimensional FEM of ferrite-pearlite based C45 steel to study the influence law of cutting edge radius on chip shape. Lucca et al. [\[6\]](#page-9-5) studied the relationship between plastic deformed layer, cutting edge radius and minimum cutting thickness in micro cutting, and found that the surface morphology of plastic deformed layer was independent of the minimum cutting thickness and only affected by the cutting edge radius. Malekian et al. [\[7\]](#page-9-6) established the minimum chip thickness model based on the principle of minimum energy consumption and the infinite shear strain method, and then concluded that the cutting radius of the tool was positively correlated with the minimum chip thickness. Son et al. [\[8\]](#page-9-7) established an ultra-precision cutting model and believed that the cutting edge radius and the friction coefficient should be considered to control the minimum chip thickness. Based on FEM, Vogler et al. [\[9\]](#page-9-8) predicted that the minimum cutting thickness of pearlite and ferrite materials was 0.2 and 0.3 times of the radius of the blunt circle of the cutting edge, respectively. It can be seen that the cutting edge radius and the minimum cutting thickness are the important factors to determine the cutting quality of fine drill, and there is a close relationship between them. However, the cutting edge radius is dynamically changed under the action of force at all times in the cutting process. We need to carry on the mechanical analysis to the whole process of fine drilling cutting, in order to effectively monitor the tool state and predict the problems that will arise in fine drilling.

This paper focuses on the interaction between drill tip and borehole surface and its effect on material properties. In this paper, a mechanical model of fine drill based on time is established to analyze the contact force of each part of the drill tip, especially the change of the drilling force at the cutting edge when the cutting tool is worn. Through the analysis of the experimental data, the contact coefficient of the cutting deformation zone was solved, and the relationship between the tool wear and the contact force was evaluated.

## **2 Experimental Setup**

The cutting force of the tool in the drilling process was measured experimentally to verify the mechanical model of fine drilling in this study. Figure [1](#page-2-0) show the schematic diagram of the experimental device. We Prepared a 1Cr18Ni9Ti stainless steel sample, the size is  $\varnothing$  100  $\times$  4 mm, placed it in the table of the Kistler 9275



<span id="page-2-0"></span>**Fig. 1** Diagram of cutting experimental

#### <span id="page-2-1"></span>**Table 1** Parameters of tool



dynamometer in desktop on the dynamometer. The material of drill is carbide, its parameters are shown in Table [1.](#page-2-1)

# <span id="page-2-2"></span>**3 Cutting Process Analysis**

In the fine drilling process, the cutting part of the drill tip is composed of two parts, namely the main cutting edge and the chisel edge (Fig. [2\)](#page-3-0). The main cutting edge is the intersecting line of the spiral groove and the flank, which is used for oblique cutting of the workpiece. The chisel edge is the intersection line between the rake face and the flank face, showing a slightly curved S-shape. Therefore, the cutting process of fine drilling is divided into five stages  $[10]$ . The 0–t<sub>1</sub> stage: The chisel cutting edge orthogonal cutting workpiece; The  $t_1-t_2$  stage: The main cutting edge oblique cutting material; The  $t_2$ – $t_3$  stage: The drill tip is drilled into the workpiece completely, and the workpiece is acted on by two parts of cutting force. The  $t_3-t_4$ stage: Part of the chisel edge drill through the workpiece; The  $t_4$ – $t_5$  stage: The chisel edge and part of the main cutting edge drill through the workpiece, and the workpiece



**Fig. 2** Drill tip. **a** Entity, **b** structure

<span id="page-3-0"></span>is only subjected to part of the cutting force of the main cutting edge until the cutting force is completely eliminated at the time of  $t<sub>5</sub>$ . So the cutting force model of five stages can be established, as follows in Eq. [\(1\)](#page-3-1):

<span id="page-3-1"></span>
$$
F_c(t) = \begin{cases} \frac{t}{t_1} F_s, & 0 < t < t_1 \\ F_s + \frac{t - t_1}{t_2 - t_1} F_m, & t_1 < t < t_2 \\ F_s + F_m, & t_2 < t < t_3 \\ \frac{t_4 - t}{t_4 - t_3} F_s + F_m, & t_3 < t < t_4 \\ F_s + \frac{t_5 - t}{t_5 - t_4} F_m, & t_4 < t < t_5 \end{cases} \tag{1}
$$

where  $F_m$  and  $F_s$  are respectively the cutting forces of the main cutting edge and the chisel edge. Therefore, we can first establish the cutting force model of the two parts of the drill tip, and then solve the cutting force model based on time.

# *3.1 The Main Cutting Edge*

The cutting process of the main cutting edge is oblique cutting (Fig. [3\)](#page-4-0). The included Angle between the cutting direction and the chisel edge is the half peak angle  $\varphi$ , the thickness of the drilling core is  $r_w$ , and the distance between point *a* on the cutting



<span id="page-4-0"></span>**Fig. 3** The structure of main cutting edge

edge and the drilling shaft is  $r_i$ . The main cutting edge can be divided into several cutting units, and the cutting force of each cutting unit can be calculated according to the mechanical modeling method of Chandrasekharan et al. [\[11\]](#page-9-10). Then the cutting force acting on the workpiece is the superposition of the cutting force vectors of all the cutting units. Considering that the cutting thickness of fine drilling cutting is small, the cutting edge should be regarded as a circular arc. According to the slip line field theory, oblique cutting slip line field model [\[12\]](#page-9-11) of the main cutting edge is established, as shown in Fig. [4.](#page-4-1)



<span id="page-4-1"></span>**Fig. 4** Slip line field model of cutting element on main cutting edge

The model is divided into three plastic deformation zones [\[13\]](#page-9-12): the first shear plane region, ABCFGHIJK, the second deformation friction zone A'BC and the third deformation friction zone CSDEF. Surface CS and SD are edge contact surfaces, and their included angles with slip lines DE and CF are respectively  $\xi_1$  and  $\xi_2$ ; The central angles are respectively  $\theta_b$  and  $\theta_c$ ; The front Angle between AKJ and the horizontal plane is  $\delta$ ; The shearing Angle between curve AB and the horizontal plane is  $\phi_s$ ; The effective front Angle between CS and the vertical plane is  $\gamma_e$ ; The normal forward Angle between the rake face and the vertical plane is  $\gamma_n$ ; The radius of the drill tip is *rc*.

The contact length between drill tip and workpiece are given as

<span id="page-5-0"></span>
$$
\begin{cases}\n l_{CS} = 2r_c \sin(\frac{\pi}{4} + \frac{\gamma_n}{2} - \frac{\theta_c}{2}) \\
l_{SD} = 2r_c \sin \frac{\theta_c}{2}\n\end{cases}
$$
\n(2)

The feed is *f*, so the thickness of the undeformed chip is given by

<span id="page-5-1"></span>
$$
t_c = 0.5 f \sqrt{\frac{r_i^2 - r_w^2}{r_i^2 (1 + \cos^2 \varphi) - r_w^2}}
$$
(3)

The contact length between the rake face and the chip:

$$
l_{A'C} = \frac{t_c + \sqrt{2}(l_{CS}\cos\xi_2 + l_{SD}\sin\xi_1)\sin\delta - r_c(1 + \sin\gamma_e)}{\sin\phi_s}
$$
(4)

The cutting force perpendicular to the cutting edge plane on the cutting element is

$$
dF_m = k_s (k_{A'} l_{A'C} + k_C l_{CS} + k_S l_{SD})
$$
 (5)

where  $k_s$  is the shear flow stress;  $k_{A'}$ ,  $k_C$  and  $k_S$  are the contact coefficients between the tool and contact surface, respectively.

The axial cutting force  $F_m$  on the main cutting edge as follows:

<span id="page-5-2"></span>
$$
F_m = (D - D_c)dF_m \cos \varphi \tag{6}
$$

where *D* is the diameter of cutting tool;  $D_c$  is the diameter of chisel edge.

<span id="page-6-0"></span>



# *3.2 The Chisel Edge*

Similarly, the chisel edge is equally divided into multiple cutting elements, and the cutting force acting on the workpiece is the superposition of the cutting force vectors of all the cutting elements. The orthogonal cutting slip line field model of the chisel edge is shown in Fig. [5.](#page-6-0)

As in the model of the main cutting edge, the chisel edge is still divided into three plastic deformation zones. According to Eqs.  $(2)$ – $(4)$ , the contact length between the tool and the material is solved. Since the chisel edge is perpendicular to the cutting direction, the half peak Angle of the drill tip is  $\varphi = 90^\circ$ , and the thickness of unchipping  $t_c$  is 0.5*f*. So  $l_{A'C}$  is different. As the friction zone between the flank face and the workpiece have other zone-CFF1 and SEE1,  $\xi_1$  and  $\xi_2$  are reduced.

According to Eq. [\(5\)](#page-5-2), We could calculate the cutting force of the cutting unit, then the axial cutting force on the chisel edge of the fine drill as follows:

$$
F_s(t) = D_c dF_s \tag{7}
$$

# *3.3 Cutting Force Experiment*

The cutting heat generated by cutting will aggravate the tool wear and increase the radius of cutting edge, resulting in the undeformed chip thickness less than the minimum chip thickness and a large number of elastic deformation of the workpiece. The contact force is generated by ploughing and the tool contact coefficient will change at this time. Therefore, the cutting edge of the tool is actually dynamic, but in this example, it is assumed to be a constant value.



<span id="page-7-0"></span>**Fig. 6** The thrust value at low feed and high speed  $\mathbf{a} f = 5 \mu m/\text{rev}$  drilling in;  $\mathbf{b} f = 5 \mu m/\text{rev}$ drilling out;  $cf = 20 \mu$ m/rev drilling in;  $df = 20 \mu$ m/rev drilling out

In order to calculate the cutting force of the tool in the cutting process, the unknown indentation half Angle and the contact coefficients need to be determined by microdrilling experiments. We carried out cutting force experiments at constant rotational speed (n = [6](#page-7-0)000 rpm) and different feed rates (f =  $5-20 \mu$ m/rev). Figure 6 shows the thrust values for low and high feed cutting with an initial edge radius of  $3 \mu m$ . The chisel edge is drilled into the workpiece in a very short period of time, resulting in a very rapid increase in thrust, while the main cutting edge thrust increases slowly and remains stable after the bit is fully drilled. The thrust fluctuation value of the tool is large and the main cutting edge plays the leading role at low feed condition. It is related to the vibration in the cutting process. As the feed rate increases, the thrust value of the transverse cutting edge will become larger and larger, and even tends to exceed the main cutting edge, which is consistent with the description of Anish et al. [\[14\]](#page-9-13). It shows that with the increasing of tool temperature and wear, the contact conditions between the drill tip and the workpiece are changed, which affects the thrust measurement value.

Based on thrust measurements from fine drilling experiments under different conditions and the mechanical models of each area in Sect. [3,](#page-2-2) the contact coefficients



<span id="page-8-0"></span>**Fig. 7** Contact coefficient of tool-workpiece. **a** The main cutting edge, **b** the chisel edge

between the main cutting edge and the chisel edge of the drill tip and the contact surface can be determined by combining.

Figure [7](#page-8-0) shows that no matter the main cutting edge or the chisel edge, the contact coefficient is much higher than the other two contact coefficients at different feed, which indicates that the resistance of the tool mainly concentrates on the intersection of the rake face and the flank face—the material shear area. With the increase of feed, the contact coefficients of main cutting edge and chisel edge trend. However, the thrust of chisel edge rise rapidly in a very short time, gathered in the energy. So the center part have serious ploughing phenomenon, which makes the chip more difficult to form. It is why the contact coefficient of chisel edge increases significantly faster. In this case, the tool wear is serious; the cutting edge radius  $r_c$  is increased; and the contact force is further improved. It also confirms the chisel edge thrust growth faster than the main cutting edge.

Therefore, when we design the structure of fine drill, we should appropriately reduce the diameter of the chisel edge to prevent chip accumulation on the basis of maintaining the tool stiffness.

# **4 Conclusions**

(1) Based on the consideration of the cutting edge radius, this paper analyzes the mechanical problem of the drill tip in the dry drilling process of stainless steel 1Cr18Ni9Ti sample, and puts forward an instantaneous mechanical model to predict the change law of the cutler-workpiece contact force and contact coefficient with the feed amount. The results show that the high feed increases the complexity of the contact conditions between the tool and the workpiece surface.

(2) The contact coefficient at the intersection of the rake face and the flank face plays a leading role in the contact force of the whole tool. It is necessary to fully consider the local overheating caused by chip accumulation in the tool design, and reduce the width of chisel edge appropriately.

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