

# Effect of Substrate Inclination on Post-impact Dynamics of Droplets



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## *Nomenclature*

$v$  Velocity of droplet (m/s)  
 $d$  Diameter of droplet (m)  
 $t$  Time

## *Greek Symbols*

$\rho$  Density (dimensionless)  
 $\beta$  Elongation factor (dimensionless)  
 $\phi$  Tilted angle

## *Subscripts*

$i$  Pre-impact  
 $l$  Liquid

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## 1 Introduction

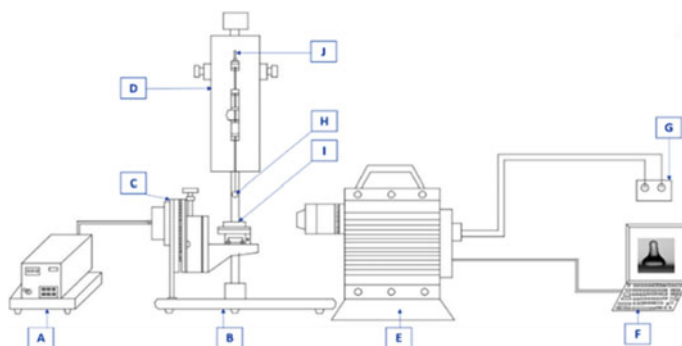
Drop impact dynamics on surfaces is a complex phenomenon due to interplay of fluid mechanics, surface physics, and interfacial chemistry. This impact process exhibits a diverse set of intriguing behavior depending upon the wettability of the solid surface with respect to the fluid [1, 2] and the fluid properties [3–6]. Oblique impact studies may be useful in applications like spraying of pesticides at random angles and impact of supercooled water drops on airplane leading to frost formation [7–9]. In IC engines too, fuel injection system sprays fuel obliquely toward the combustion zone [10]. In addition, typical applications such as spray coating, painting, cooling, or inkjet printing are more likely to occur at oblique angles instead of normal impact. Sikalo et al. [11] reported asymmetry in the spreading factor, i.e., the differences in the deformation at the front and back of the droplet after impact. Chiarot et al. [12] and Zheng et al. [13] studied grazing impact of high velocity continuous drop streams on inclined SH surfaces and observed that the shape and structure of the rebounding stream are influenced by the frequency of the drop ejection and velocity. Yeong et al. [14] investigated the dependence of drop dynamics on Weber number. Antonini et al. [15] distinguished six distinct impact regimes at wide range of  $We$  for drop impact on tilted hydrophobic and superhydrophobic (SH) substrates. LeClerc et al. [16] observed the transition from the superhydrophobic Cassie–Baxter regime to the fully wetted Wenzel regime while studying the impact of water drops on inclined textured SH surfaces.

While a lot of attention has been paid to the spreading dynamics on SH surfaces, the dynamics of lift off of the drops upon inclined surfaces are rarely studied. Therefore, the present study highlights the role of non-dimensional numbers like Reynolds number ( $Re$ ) and Weber number ( $We$ ) and surface inclination upon impact of droplets. Experiments have been carried out with different fluids to observe the post-impact elongation characteristics of droplets and the dynamics vis-à-vis physical properties.

## 2 Methodology

### 2.1 Experimental Details

The experimental setup consists of a drop dispenser controller (Holmarc Opto-Mechantronics Pvt. Ltd., India) that maintains constant volume of droplet discharged from a syringe pump as shown in Fig. 1. The drop impact images were recorded using a high speed camera (Photron FASTCAM SA4) mounted with a G-type AF-S macrolens of focal length 105 mm (Nikkor, Nikon). The images were taken at  $1024 \times 1024$  pixels resolution at 3600 frame per second. Experiments were performed at ambient conditions ( $25^\circ\text{C}$ ) on SH surfaces. For impact study, sterile glass slides were thoroughly cleaned with acetone and DI water and then dried in hot air oven. The SH surfaces were created on similar glass substrates using superhydrophobic spray



**Fig. 1** Schematic of the experimental setup [17] (A) drop dispenser controller (B) base (C) substrate inclination apparatus with backlight arrangement (D) syringe pump (E) high-speed camera (F) laptop (G) power source (H) drop (I) target surface (J) syringe

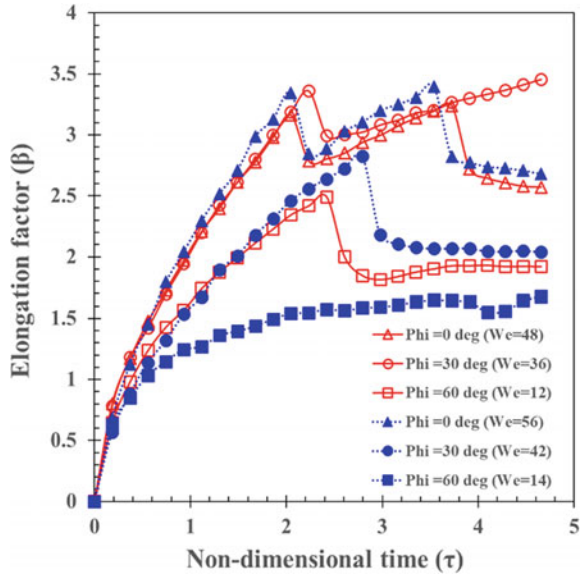
coating (Ultra Tech International Inc., USA). In the present study, three fluids such as DI water, SiO<sub>2</sub> water nanocolloids (2.5 and 5% wt.), and different concentrations of sodium dodecyl sulfate (SDS, Merck, India) dissolved in DI water (0.25 and 0.50% of the critical micelle concentration (CMC)) were used as test fluids.

### 3 Results and Discussions

The present study focuses on experiments with different test fluids, highlighting the role of surface inclination and Weber number ( $We$ ) and Reynolds number ( $Re$ ). The Weber number has been defined based on the initial velocity ( $v_i$ ), density ( $\rho_l$ ), diameter ( $d_i$ ), and fluid surface tension ( $\sigma_l$ ) (Subscripts  $i$ ,  $l$  stand for initial condition before impact and liquid, respectively). The Weber number ( $We$ ) was varied between 10 and 127 ( $We = 10-89$  for water,  $We = 12-127$  for sodium dodecyl sulfate (SDS) surfactant solutions (0.25 and 0.5 wt % of critical micelle concentration (CMC)), and  $We = 10-89$  for aqueous solutions of silica particles (2.5 and 5 wt %)). Similarly, the Reynolds number based on initial velocity is defined as  $Re = \frac{\rho_l v_i d_i}{\mu}$ .  $Re$  was varied from 28 to 4873, ( $Re = 1624-4873$  for water,  $Re = 28-1105$  for silica colloids and  $Re = 1411-4587$  for surfactant solutions). The initial diameter of droplets of DI water, 0.25 and 0.5 wt. % CMC are considered as 2.9, 2.71, and 2.52 mm, respectively. The initial diameters of 2.5 and 5 wt. % of silica colloidal solutions are almost similar to the initial diameters of water droplets. The measurement uncertainty of initial diameter of droplets for test fluids is within 5% error.

Figure 2 elucidates the elongation dynamics of post-impact drops on different inclination angles on SH surfaces. The elongation factor ( $\beta$ ) is expressed as the ratio of height of post-impact drop bouncing off from the target to initial drop diameter. The non-dimensional time ( $\tau$ ) is expressed as the ratio of the product of time ( $t$ ) at which post-impact image is considered and initial velocity ( $v_i$ ) to the initial droplet diameter

**Fig. 2** Variation of elongation factor with non-dimensional time on SH surface. The test fluids are surfactant solutions considering 0.25 and 0.5 CMC. Considering the surface inclination, the normal Weber number is defined as  $We_n = \rho_l v_i^2 d_i (\cos \Phi)^2 / \sigma_l$ , where  $\phi$  is the tilted angle. We represents normal Weber number in the plot



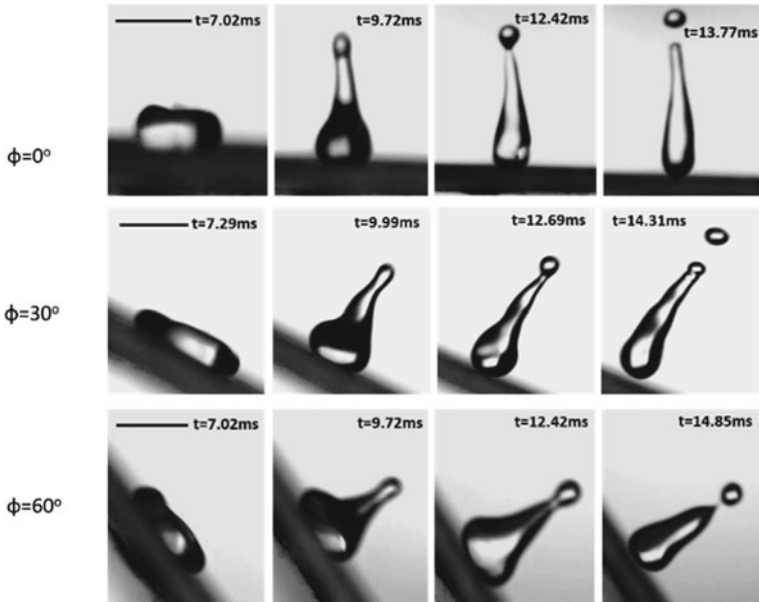
( $d_i$ ). It is observed that the elongation factor for droplets of 0.25 and 0.5 wt. % CMC solution increases up to certain time interval followed by a sharp decline. The sharp decline occurs due to emission of secondary droplets during vertical acceleration of the droplets after impact. The vertical momentum and reduction in interfacial energy promotes pinching off event (Fig. 3). At  $\phi = 0^\circ$ , for 0.25 CMC surfactant solution, formation of secondary droplet twice at time  $t = 13.77$  and  $18.63$  ms corresponds to twice decrease in  $\beta$  (Fig. 2).

In case of water at initial impact velocity  $v_i = 1$  m/s, elongation factor follows the same trend as droplets of surfactant solutions (Fig. 4). The emission of secondary droplets occurs at  $\phi = 0^\circ$ , but this behavior is diminished with increasing surface inclinations. The reduction in normal momentum to the oblique plane inhibits the formation of secondary droplet formation while lifting off from the surface.

Figure 5 investigates the elongation dynamics of three test fluids such as water, silica colloid solutions and surfactant solutions at  $We = 40$  and  $\phi = 0^\circ$  for SH surfaces. It is found that the secondary droplet is formed earlier in case of surfactant solutions compared to water and  $\text{SiO}_2$  colloidal solution. This is obvious due to the fact that surfactants reduce the interfacial energy, thereby promoting the formation of secondary droplets.

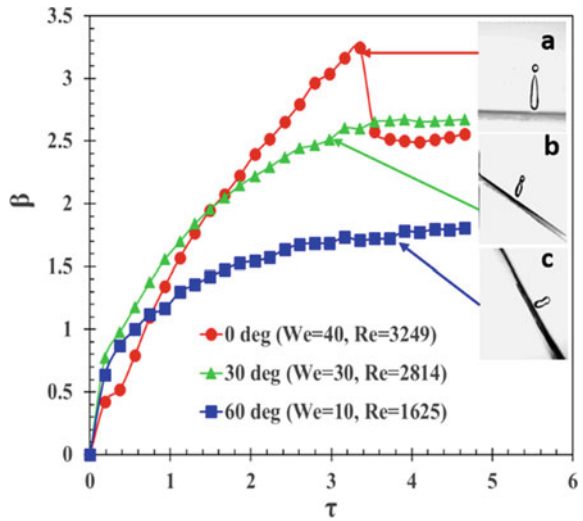
## 4 Conclusion

The present study investigates the temporal variation of elongation factor using different test fluids on tilted SH surfaces. It is observed that the elongation factor

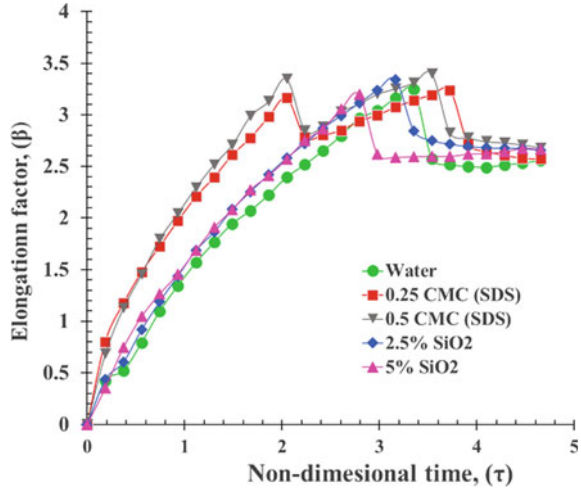


**Fig. 3** Post-impact droplet images of surfactant solution (0.25 CMC) at  $We = 40$  on SH surfaces. The magnitude of scale bar is equal to 2.71 mm for each figure

**Fig. 4** Variation of elongation factor with non-dimensional time on SH surface. The test fluid is water and  $We$  represents the normal Weber number. Inset (a-c) elongation dynamics of water drops post-impact on horizontal SH surface at  $t = 16.2$  ms



**Fig. 5** Elongation dynamics of different test fluids at  $\phi = 0^\circ$  and  $We = 40$  fo SH surface



decreases with increase in surface inclination. Again, the suppression of secondary droplet occurs with increase in substrate angle. The time at which secondary droplet departs from the original droplet depends upon the fluid properties. The reduction in normal momentum and interfacial energy are the two key parameters for the above events. This study enables to find the critical parameters for comprehensive study of elongation outcomes on SH surfaces.ables should be pasted within the text column as follows.

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