



# A S-Max-Log-MPA Multiuser Detection Algorithm Based on Serial in SCMA System

Guanghua Zhang<sup>1</sup>(✉), Zonglin Gu<sup>1</sup>, Weidang Lu<sup>2</sup>, and Shuai Han<sup>3</sup>

<sup>1</sup> Northeast Petroleum University, Daqing, China  
dqzgh@nepu.edu.cn

<sup>2</sup> Zhejiang University of Technology, Hangzhou, China

<sup>3</sup> Harbin Institute of Technology, Harbin, China

**Abstract.** Sparse code multiple access (SCMA) has become one of the most promising key technologies for 5G communication in the future. In the multi-user detection algorithm of SCMA system, the message passing algorithm (MPA) has high complexity because of the exponential (EXP) operation. Because the maximum and approximate algorithms are used in the maximum logarithm message passing algorithm (Max-log-MPA), it will cause some information loss, resulting in poor accuracy of system transmission information. The serial message passing algorithm (S-MPA) combines the user node message update with the resource node message update, which will also cause some information loss, resulting in poor bit error rate of the system. Therefore, a maximum logarithm message passing algorithm based on serial (S-Max-log-MPA) is proposed in the paper, which first converts the exponential operation to the sum of the maximum values and then integrates the user node message update into the resource node message update. In the iterative process, the user node information is updated and then transferred to the next node to update the information of the resource node, which can greatly reduce the information loss and the space occupied by the intermediate variables, and effectively improve the accuracy of the system transmission information. Simulation results show that the bit error ratio (BER) performance of the system is better with the increase of iterations.

**Keywords:** SCMA · BER · Serial · Message passing algorithm · Max-log-MPA

## 1 Introduction

With the development of the Internet of things and mobile communication system, the demand for larger capacity, higher transmission rate, ultra-high-density throughput and large-scale application scenarios has also increased dramatically [1]. The research of the fifth-generation (5G) mobile communication technology has become an inevitable trend [2]. The development trend of 5G technology includes continuous wide area coverage, low delay and high reliability, hot spot and high capacity coverage, low power consumption and large connection [3, 4]. Therefore, 5G can solve many problems of

network demand of mobile devices at this stage. Sparse code multiple access (SCMA) is a non-orthogonal multiplexing technology proposed by Huawei in 2014. It is one of the key technologies of 5G. SCMA is evolved from low-density spread spectrum multiple access (LDS-MA) [5], which has good flexibility and strain capacity, and can obtain additional SNR gain.

The SCMA system integrates quadrature amplitude modulation (QAM) and sparse spread spectrum [6], which can directly map binary data stream to multi-dimensional code word in complex domain, so it can solve the overload caused by large-scale connection [7]. The sender of SCMA system uses message passing algorithm (MPA) to detect multiple users. Multiple data layers from users are orthogonally superposed in the same time-frequency resource block for transmission [8]. The receiver separates multiple data layers of the same time-frequency resource block through the MPA decoder. In reference [9], a message delivery algorithm based on logarithmic domain is proposed. In reference [10], an uplink scheme SCMA system based on serial message passing algorithm (S-MPA) is proposed. In reference [11], an improved maximum logarithm message passing algorithm (Max-log-MPA) multiuser detection algorithm is proposed. Compared with the original MPA algorithm, the above algorithm has improved the bit error ratio, but the SCMA system still has a high bit error ratio.

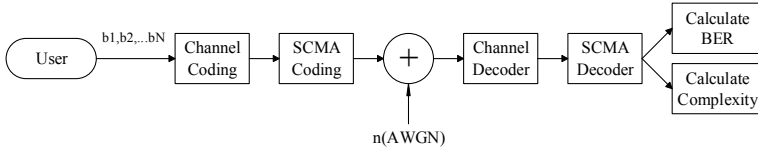
In order to solve the problem of user data loss caused by logarithm operation in Max-log-MPA algorithm and part of information loss caused by the combination of user node message update and resource node update in S-MPA, a maximum logarithm message passing algorithm based on serial (S-Max-log-MPA) is proposed in the paper. The algorithm transforms the exponential (EXP) operation in the original MPA into the multiplication operation and the maximum operation in the log domain and then integrates the user node message update into the resource node message update. During the iterative update process, the information of user node is updated and transferred to the next node immediately, and then the information of resource node is updated immediately. In this way, this can reduce the storage of intermediate variables in the transmission process and also reduce the loss of user information, so improve the bit error ratio (BER) performance of the system.

## 2 SCMA System

In the SCMA uplink system, assuming that  $J$  user information shares  $K$  ( $J > K$ ) time-frequency resource blocks, the system overload rate is:  $\lambda = J/K$ , and the communication model is shown in Fig. 1. After source coding and channel coding, user information  $u_j(u_1, u_2, \dots, u_J)$  obtains binary bit data stream  $b_j(b_1, b_2, \dots, b_J)$ , which is then mapped to  $n$ -dimensional codeword  $x = f(b_j)$  in codebook by SCMA encoder. Because of the sparsity of SCMA, the mapping process of SCMA can be defined as:  $f : B^{\log_2 M} \rightarrow \chi$ , where  $M$  is the codebook size,  $B$  is the set of binary numbers, and  $\chi$  is the user codebook.

If  $y_j = [y_1, y_2, \dots, y_K]^T$  is the signal received on  $K$  resource blocks, then

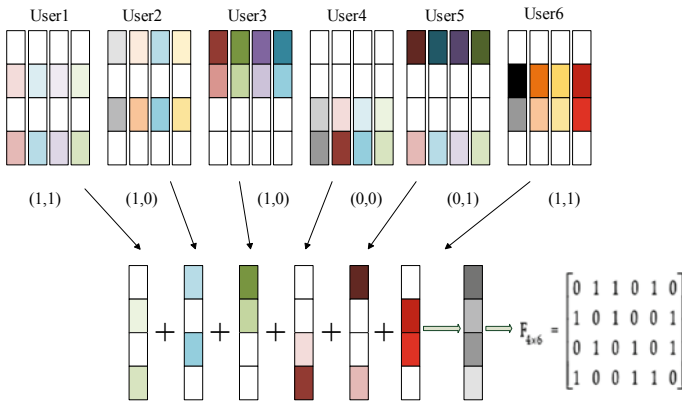
$$y = \sum_{j=1}^J \text{diag}(h_j)x_j + n \quad (1)$$



**Fig. 1** Uplink SCMA communication system model

Because the channels of each layer of the upper link are different, the channel factor is  $h_j(h_1, h_2, \dots, h_J)$ ,  $x_j = [x_{1,j}, x_{2,j}, \dots, x_{K,j}]^T$  represents the  $k$ -dimension SCMA codeword of the  $j$ -th user, and  $n_j = [n_1, n_2, \dots, n_K]^T$  is the white Gaussian noise vector added to the channel with distribution  $N(0, \sigma^2 I)$ .

Assuming that six users share four time-frequency resource blocks, the system overload rate is 150%. The user information is mapped to the codewords on the SCMA codebook. Each user has a unique codebook, as shown in Fig. 2.



**Fig. 2** SCMA coding principle

### 3 S-MPA Algorithm

S-MPA algorithm is based on the original MPA algorithm, which uses the serial resource node update, and integrates the user node message update with the resource node message update in each iteration. The updated information can be delivered in time, which reduces the storage space of intermediate variables and improves the convergence speed of messages. The updating process of S-MPA algorithm can be divided into three steps.

Step 1: initialize the conditional probability of the S-MPA algorithm.

$$I_{c_k \rightarrow u_j}^0(x_j) = \frac{1}{M}, j = 1, 2, \dots, J \tag{2}$$

where  $c_k$  represents the function node, and  $I_{c_k \rightarrow u_j}^0(x_j)$  represents the information of variable node  $u_j$  sent by function node  $c_k$  during the initial iteration.

The probability  $Q^t(x_j)$  ( $t = 1, 2, 3, \dots, t_{\max}$ ) of codeword combination on time-frequency resource block  $K$  is:

$$Q^t(x_j) = \exp\left(-\frac{1}{N_{0,k}} \left\| y_k - \sum_{v \in \xi_k} h_{k,v} x_{k,v} \right\|^2\right) \quad (3)$$

where  $v \neq j, v \in \xi_k, j \in \xi_k, y_k (k = 1, 2, 3, \dots, K)$  represents the received signal,  $N_{0,k}$  represents the noise power on the time-frequency resource block  $K$ ,  $\xi_k$  represents the set of users allocated on the time-frequency resource block,  $h_{k,v}$  represents the channel coefficient of the  $v$ -th user on the  $k$ -th resource block, and  $x_{k,v}$  represents the codeword of the  $v$ -th user on the  $k$ -th resource block.

Step 2: the S-MPA algorithm first updates the resource nodes.

$$I_{c_k \rightarrow u_j}^t(x_j) = \sum_{\sim x_j} \left[ Q^t(x_j) \times \prod_{m \in \xi_k/j} I_{c_m \rightarrow u_k}^t(x_j) \times \prod_{m \in \xi_k/j} I_{c_m \rightarrow u_k}^{t-1}(x_j) \right] \quad (4)$$

Among them,  $\sim x_j$  represents the edge probability of symbol  $x_j$ , and  $\xi_k/j$  represents the set of all variable nodes except the  $j$ -th user connected with function node  $c_k$ .

Then, update the user variable node.

$$I_{c_k \rightarrow u_j}^t(x_j) = \text{normalize} \left[ ap_v(x_j) \times \prod_{m \in \xi_k/j} I_{c_m \rightarrow u_k}^{t-1}(x_j) \right] \quad (5)$$

Among them,  $ap_v(x_j)$  represents the prior probability of user  $J$  code word, and  $\text{normalize}(x_j)$  represents normalization processing.

Step 3: decision processing of S-MPA algorithm.

First, the probability of codeword  $x_{j,m}$  transmitted by user variable node  $j$  is estimated,  $m = 1, 2, \dots, M$ .

$$Q(x_{j,m}) = ap_v(x_{j,m}) \times \prod_{m \in \xi_k/j} I_{c_m \rightarrow u_k}(x_j) \quad (6)$$

where  $Q(x_{j,m})$  represents the probability of codeword;  $x_{j,m}$  transmitted by user variable node  $j$ .

Then, the log likelihood ratio (LLR) of each coding bit is calculated to determine the user:

$$\text{LLR}_{j,x} = \log \left[ \frac{P(b_i = 0)}{P(b_i = 1)} \right] = \log \left[ \frac{\sum_{m: b_{m,i}=0} Q(x_{j,m})}{\sum_{m: b_{m,i}=1} Q(x_{j,m})} \right] \quad (7)$$

where  $P(b_i = 0)$  represents the probability of the variable node to be decoded, and  $P(b_i = 1)$  represents the probability of the variable node to be decoded.

## 4 S-Max-Log-MPA Algorithm

Because of the large amount of operation of exponential operation (EXP) and the large space occupied in the process of message iterative updating, and the node message updating and resource node message updating are carried out respectively, the performance of multi-user checking algorithm is high. The Max-log-MPA algorithm will make part of the information lost, which leads to the poor bit error ratio performance. In this paper, the S-Max-log-MPA algorithm is based on the idea of adding the S-MPA algorithm to the max log MPA algorithm. Firstly, using the MPA algorithm of sum product operation [12], the index operation of the original MPA algorithm is reduced to the maximum value and addition operation, which greatly reduces the space occupied by the operation. In addition, the node message update and the resource node message update are combined. In each iteration, the updated message is immediately delivered to the next node, and the latter node immediately updates the resource node's message, which can reduce the loss of user information and the space occupied by intermediate variables. Therefore, the S-Max-log-MPA algorithm can effectively reduce the bit error ratio of the detection algorithm.

Step (4) of the message update process of S-Max-log-MPA algorithm can be modified as follows:

$$I_{c_k \rightarrow u_j}^t(x_j) = 2 \times \frac{1}{\sqrt{2\pi}\delta} \times \max_{\sim x_j} \left\{ -\frac{1}{2\delta^2} \left\| y_k - \sum_{v \in \xi_k} h_{k,v} x_{k,v} \right\|^2 + \prod_{m \in \xi_k/j} I_{c_m \rightarrow u_k}^t(x_j) + \prod_{m \in \xi_k/j} I_{c_m \rightarrow u_k}^{t-1}(x_j) \right\} \quad (8)$$

## 5 Analysis of BER Performance

The BER performance of the system is an important index to measure the accuracy of message transmission in communication system. Max-log-MPA algorithm uses sum product operation, which reduces the index operation of the original MPA algorithm to the maximum value and addition operation. But it will cause some information loss and poor performance of system bit error ratio. Because the S-MPA algorithm does not judge the stability of user information, some user information is wrongly transmitted. In this algorithm, the index operation is reduced to the maximum value and the addition operation, and then the user node information update is integrated into the resource node information update, which can reduce the loss of user information and improve the accuracy of user information transmission.

## 6 Analysis of Simulation Results

The simulation parameters are as follows: The number of multiple users is 6, the time-frequency resource block is 4, the nonzero element is 1000, the overload factor is 150%,

the channel is the Gaussian white noise (AWGN) channel, and the codebook is the four-dimensional codebook published by Huawei [13].

Figure 3 shows the average EBR performance comparison between the S-Max-log-MPA algorithm and the Max-log-MPA algorithm with the increase of SNR when the maximum number of iterations is  $t_{\max} = 3$ . It can be seen from Fig. 3 that the average BER of S-Max-log-MPA algorithm is better than that of Max-log-MPA algorithm, When  $E_b/N_o = 0$  dB, BER performance of S-Max-log-MPA algorithm is slightly higher than that of Max-log-MPA algorithm by 6.03%. When  $E_b/N_o = 14$  dB, BER performance of S-Max-log-MPA algorithm is slightly higher than that of Max-log-MPA algorithm by 0.967%.

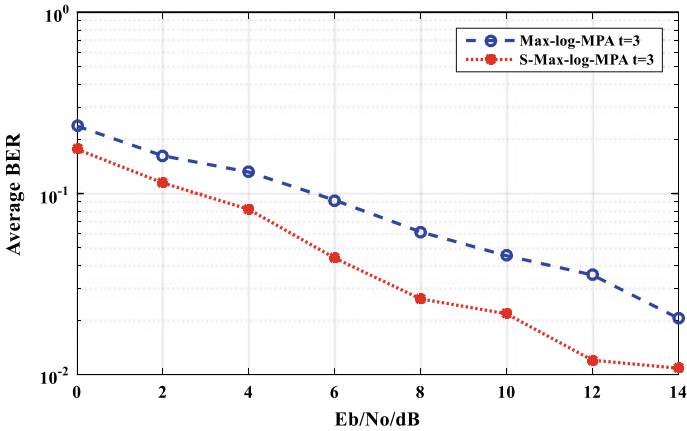
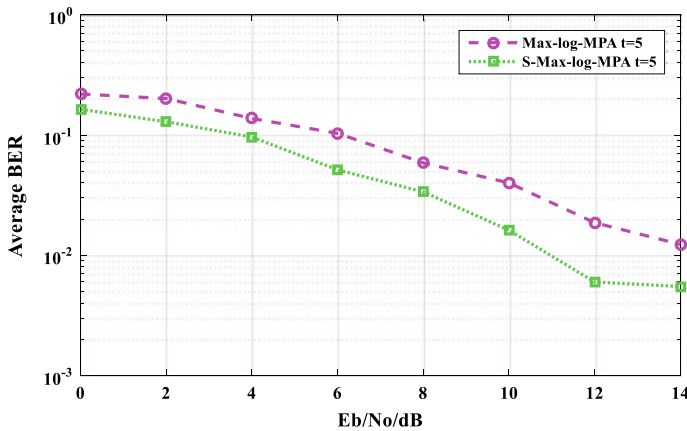


Fig. 3 Comparison of average BER performance of two algorithms when  $t_{\max} = 3$

Figure 4 shows the comparison of the average EBR performance of S-Max-log-MPA algorithm and Max-log-MPA algorithm with the increase of SNR when the maximum number of iterations is  $t_{\max} = 5$ . According to the comparison between Figs. 4 and 3, as the number of iterations increases, the closer the average bit error rate of the two algorithms is, the better. But in general, the average bit error rate of S-Max-log-MPA algorithm is still better than that of Max-log-MPA algorithm. When  $E_b/N_o = 0$  dB, BER performance of S-Max-log-MPA algorithm is slightly higher than that of Max-log-MPA algorithm by 5.56%. When  $E_b/N_o = 14$  dB, BER performance of S-Max-log-MPA algorithm is slightly higher than that of Max-log-MPA algorithm by 0.683%.

## 7 Conclusion

The S-Max-log-MPA algorithm in this paper is based on the idea of adding the S-MPA algorithm to the Max-log-MPA algorithm. It combines the advantages of the two algorithms and can effectively solve the problem of high bit error ratio caused by information loss caused by Max-log-MPA algorithm and S-MPA algorithm. From the simulation results, we can see that with the increase of the number of iterations, the BER performance of this algorithm is better.



**Fig. 4** Comparison of average BER performance of two algorithms when  $t_{\max} = 5$

**Funding.** This work was supported by the Youth Science Foundation of Northeast Petroleum University under Grant No. 2019QNL-34 and Graduate Innovative Research Work and the National Natural Science Foundation of China under Grant (61871348).

**Conflicts of Interest** The authors declare no conflict of interest.

## References

- Al-Falahy Naser, Alani Omar Y (2017) Technologies for 5G networks: challenges and Opportunities. *IEEE IT Prof* 19(1):12–20
- Yifei Yuan, Longming Zhu (2014) Application scenarios and enabling technologies of 5G. *IEEE China Commun* 11(11):69–79
- Zhang S, Xu X, Lu L, Wu Y, He G, Chen Y (2014) Sparse code multiple access: an energy efficient uplink approach for 5G wireless systems. In: *Proceedings of 2014 IEEE global communications conference*, pp 4782–4787. <https://doi.org/10.1109/glocom.2014.7037563>
- Agyapong PK, Iwamura M, Staehle D, Kiess W, Benjeb-bour A (2014) Design considerations for a 5G network architecture. *IEEE Commun Mag* 52(11):65–75
- Guo D, Shamai S, Verdu S (2005) Mutual information and minimum mean-square error in Gaussian channels. *IEEE Trans Inform Theory* 51(4):1261–1282
- Khalid SS, Abrar S (2015) Blind adaptive algorithm for sparse channel equalisation using projections onto  $\ell_p$ -ball. *Electron Lett* 51(18):1422–1424
- Nikopour H, Baligh H (2013) Sparse code multiple access. In: *2013 IEEE 24th international symposium on personal indoor and mobile radio communication (PIMRC)*, pp 332–336. <https://doi.org/10.1109/pimrc.2013.6666156>
- Nikopour H, Yi E, Bayesteh A, Au K, Hawryluck M, Baligh H, Ma J (2014) SCMA for downlink multiple access of 5G wireless networks. In: *2014 IEEE global communications conference*, pp 3940–3945. <https://doi.org/10.1109/glocom.2014.7037423>
- Zhang S, Xu X, Lu L, Wu Y, He G, Chen Y (2014) Sparse code multiple access: an energy efficient uplink approach for 5G wireless systems. In: *2014 IEEE global communications conference*, Austin, TX, USA, pp 4782–4787. <https://doi.org/10.1109/glocom.2014.7037563>

10. Yang D, Dong B, Chen Z, Fang J, Yang L (2016) Shuffled multiuser detection schemes for uplink sparse code multiple access systems. *IEEE Commun Lett* 20(6):1231–1234
11. Xiong W, Wenping G, Xuewan Z, Wenli D (2018) Improved MAX-Log MPA multiuser detection algorithm in SCMA system. *Appl Electron Tech* 44(5):111–123
12. Kschischang FR, Frey BJ, Loeliger H-A (2001) Factor graphs and the sum-product algorithm. *IEEE Trans Inf Theory* 47(2):498–519
13. Pokamestov DA, Demidov AY, Kryukov YV, Rogozhnikov EV (2017) Dynamically changing SCMA code- books. In: 2017 International Siberian conference on control and communications (SIBCON), conference location: Astana, Kazakhstan, pp 1–4. <https://doi.org/10.1109/SIBCON.2017.7998451>