Chapter 4 Monolayer PtSe₂

Abstract Single-layer transition-metal dichalcogenides (TMDs) attract considerable attention due to their interesting physical properties and potential applications. Here, we demonstrate the epitaxial growth of high-quality monolayer platinum diselenide ($PtSe₂$), a new member of the layered TMDs family, by a single step of direct selenization of a Pt(111) substrate. A combination of atomic-resolution experimental characterizations and first-principles theoretic calculations reveals the atomic structure of the monolayer $PtSe₂/Pt(111)$. Angle-resolved photoemission spectroscopy measurements confirm for the first time the semiconducting electronic structure of monolayer PtSe₂ (in contrast to its semimetallic bulk counterpart). The photocatalytic activity of monolayer PtSe₂ film is evaluated by a methylene-blue photodegradation experiment, demonstrating its practical application as a promising photocatalyst. Moreover, circular polarization calculations predict that monolayer $PtSe₂$ also has potential applications in valleytronics.

Keywords PtSe₂ · Transition metal dichalcogenides · Atomic structure · Electronic property · Photocatalysis · Valleytronics

4.1 Background

As discussed in Chap. 1, layered transition-metal dichalcogenides (TMDs) with the general formula MX_2 , where M represents a transition metal from groups $4-10$ and X is a chalcogen (S, Se, or Te), received significant attention in the last dozen years due to their intriguing physical properties for both fundamental research and potential applications in electronics, optoelectronics, spintronics, catalysis, and so on. Depending on the coordination environment and oxidization state of the transition metal, layered TMDs can be metals, semiconductors, and insulators and thus show various physical properties. Recent investigations of MX_2 have resulted in discoveries of dramatically different electronic structures at the monolayer limit compared to the bulk materials due to quantum confinement effects. For example, while pushing from bulk to monolayer, $MoS₂$ and $MoSe₂$ show an indirect-to-direct bandgap transition [\[1–](#page-8-0)[4\]](#page-8-1). With these exciting findings, experimental research efforts so far have been mainly focused on prototypical semiconducting MX_2 with group VIB transition

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Fig. 4.1 Summary of about 40 different layered MX₂ compounds, which are highlighted. Partial highlights for Co, Rh, Ir and Ni indicate that only some of the dichalcogenides form layered structures. Reprinted with permission from Ref. [\[6\]](#page-9-0), © 2013 Springer Nature

metals ($M = Mo$, W). Note, however, that about 40 different MX_2 compounds can form stable, 2D single-layer TMDs structures $[5, 6]$ $[5, 6]$ $[5, 6]$, as summarized in Fig. [4.1.](#page-1-0) In the large family of layered TMDs, many other promising single-layer TMDs and related quantum defined properties remain to be explored experimentally. For example, IrTe₂ and $1T-TaS₂$ exhibit novel low-temperature phenomena including superconductivity and charge density wave $[7, 8]$ $[7, 8]$ $[7, 8]$; bulk ReS_2 shows monolayer behavior due to electronic and vibrational decoupling [\[9\]](#page-9-4). These interesting properties motivate considerable interest in exploring other promising TMDs materials, such as group 10 TMDs, which have rarely been reported.

Reliable preparation of ultra-thin 2D TMDs is the essential step for exploring their properties and applications. Among various production methods, chemical vapor deposition (CVD) and CVD analogs are the most important approaches of bottomup synthesis. As described in Sect. $1.3.4.2$, MX_2 growth using CVD-related methods usually involves two components containing M and X as precursors, which increases experimental steps and complexities.

4.2 Growth and Atomic Structure

In this chapter, we report epitaxial growth of monolayer $PtSe₂$ - a heretoforeunexplored member of the single-layer TMDs family—on a Pt substrate by direct "selenization" [\[10\]](#page-9-5), an analog of direct oxidation. In contrast to conventional fabrication methods of $MX₂$ by exfoliation or chemical vapor deposition, the present route toward a monolayer dichalcogenide is very straightforward: only one element, Se, is deposited on a Pt(111) substrate, and then the sample is annealed to ~200 $^{\circ}$ C to obtain epitaxial PtSe $_2$ films, as illustrated in Fig. [4.2a](#page-2-0).

The growth of PtSe₂ thin films was monitored by in situ X-ray photoelectron spectroscopy (XPS). Figure [4.2b](#page-2-0) shows the XPS spectra of the Se 3d core level during

Fig. 4.2 a Schematic illustration of synthesizing PtSe₂ monolayer by a single step of direct selenization of a Pt(111) substrate. The Pt spheres with different colors and sizes are used just to differentiate the Pt atoms in the Pt (111) substrate and in the PtSe₂ sublayer. **b** XPS measurements for the binding energies of Se during PtSe₂ growth demonstrating the formation of PtSe₂ at 270 °C. The blue arrows indicate the peak positions (55.19 and 54.39 eV) corresponding to the binding energy of Se^{2−}. The Se⁰ peaks (at 55.68 and 54.80 eV) are dominant at 25 °C, whereas at 200 °C the peaks in the curve indicate the coexistence of Se⁰ and Se^{2−}. Reprinted with permission from Ref. [\[10\]](#page-9-5), © 2015 ACS

PtSe₂ growth. When Se-deposited Pt(111) substrate is annealed to 200 °C, two new peaks appear at binding energies of 55.19 and 54.39 eV (labeled by the blue arrows), which can be explained by a change in the chemical state of Se from Se^{0} to Se^{2-} , corresponding to the selenization process of the sample. Further annealing of the sample to 270 °C results in the disappearance of Se⁰ peaks (at 55.68 and 54.80 eV) and the dominance of Se^{2-} peaks, indicating full crystallization and complete formation of PtSe₂ films.

To obtain the structural information on the as-grown epitaxial films, we observed the samples by LEED. Figure [4.3a](#page-3-0) shows a LEED pattern. Hexagonal diffraction spots from PtSe₂ (red circles) are observed to have the same orientation as those from the Pt(111) substrate (blue circles), suggesting a rotational-domain-free growth. A (3×3) diffraction pattern of the epitaxial PtSe₂ film is clearly identified, which corresponds to a well-defined moiré superstructure arising from the lattice mismatch between the PtSe₂ film and Pt(111) substrate. Furthermore, identical LEED patterns were observed on the entire sample surface $(4 \text{ mm} \times 4 \text{ mm} \text{ in size})$, indicating the growth of a large-area, homogeneous, and high-quality film.

To investigate the atomic structure of the $PtSe₂$ film, we performed STM studies. Figure [4.3b](#page-3-0) is a large-scale STM image with a well-ordered moiré pattern of $PtSe₂$ thin film on Pt(111). The periodicity of this moiré pattern is about 11.1 Å, four times the lattice constant of Pt(111). Figure [4.3c](#page-3-0) shows an atomic-resolution image of the area indicated by the white square in Fig. [4.3b](#page-3-0), revealing hexagonally arranged protrusions with an average lattice constant of $a_1 = 3.7 \text{ Å}$, which agrees perfectly

Fig. 4.3 a LEED pattern of PtSe₂ films formed on the Pt substrate. The blue, red, white circles indicate the diffraction spots from the Pt(111) lattice, PtSe₂ thin film, and (3 \times 3) superstructure with respect to PtSe₂, respectively. **b** Large-scale STM image ($U = -1.9$ V, I = 0.12 nA) shows the moiré pattern of PtSe₂ thin film on Pt(111). The white rectangle marks the size of the close-up image in (c). **c** Atomic-resolution STM image ($U = -1.0$ V, $I = 0.12$ nA) of single-layer PtSe₂ showing the hexagonal lattice of Se atoms in the topmost sublayer of the PtSe₂ sandwich-type structure. A (3×3) moiré superstructure is visible. The red and white rhombi denote the unit cell of the PtSe₂ lattice and (3×3) superlattice, respectively. The inset displays the FFT pattern corresponding to PtSe₂ and the superstructure. Adapted with permission from Ref. $[10]$, \odot 2015 ACS

with the interatomic spacing of Se atoms in the (0001) basal plane of bulk PtSe. Therefore, we interpret the hexagonal protrusions in Fig. [4.3c](#page-3-0) to be the Se atoms in the topmost Se plane of a PtSe₂ film. A regular (3×3) moiré superstructure with respect to the PtSe₂ lattice is then established, with a periodicity of $b_1 = 3a_1 \approx 11.1 \text{ Å}$ (labeled by the white rhombus). The orientation of the moiré pattern is aligned with that of the PtSe₂ lattice. This is in agreement with the LEED observation (Fig. [4.3a](#page-3-0)), where the diffraction spots of the (3×3) superlattice are in line with those of the PtSe₂ lattice. Based on LEED and STM measurements, the moiré pattern can be explained as the (3 \times 3) PtSe₂ supercells located on the (4 \times 4) Pt(111) atoms.

To gain further insight into interfacial features of the $PtSe₂/Pt(111)$ sample, we performed a cross-section high-angle annular-dark-field (HAADF) STEM study. A Z-contrast image of the $PtSe₂/Pt(111)$ interface is shown in Fig. [4.4a](#page-4-0). One bright layer combined with two dark layers observed on the topmost surface suggests a Se–Pt–Se sandwich configuration (as indicated by a model diagram superimposed in Fig. [4.4a](#page-4-0)). The atomically resolved bulk Pt substrate lattice with an experimentally measured interlayer spacing of 2.28 Å served as a reference for calibrating other spacing measurements. After the calibration, the spacing between the Se sublayers in the Se–Pt–Se sandwich is found to be 2.53 Å, which is in agreement with the calculated value in single-layer PtSe $_2$, as displayed in Fig. [4.4b](#page-4-0). These atomic-scale cross-section data obtained by STEM further verify that the fabricated structure is indeed a single-layer PtSe₂ film on the Pt (111) substrate.

The combination of LEED, STM, and STEM studies indicates a (3×3) singlelayer PtSe₂ on a (4 \times 4) Pt(111) structure. We then carried out DFT calculations based on this structure. The simulated STM image is shown in Fig. [4.4c](#page-4-0), in which the overall features of the experimental STM image (Fig. [4.3c](#page-3-0)) are well reproduced.

Fig. 4.4 a Atomic-resolution STEM Z-contrast image of the PtSe₂/Pt(111) interface along the $[110]$ zone axis. A PtSe₂ single layer over the Pt (111) substrate is resolved at atomic scale with a model diagram overlaid for clarity. **b** The relaxed model. The blue and orange spheres represent Pt atoms and Se atoms, respectively. **c** Simulated STM image ($U = -1.0$ V) based on the calculated atomic structure in (**b**) is consistent with the experimental observation in Fig. [4.3c](#page-3-0). Adapted with permission from Ref. [\[10\]](#page-9-5), © 2015 ACS

Only the hexagonally arranged Se atoms in the topmost sublayer of monolayer $PtSe₂$ are imaged. The remarkable agreement between the STM simulation and experimental STM observation strongly supports our conclusions and thus demonstrates the successful growth of a highly crystalline PtSe₂ monolayer.

4.3 Electronic Structure

Having grown highly crystalline single-layer $PtSe₂$, we investigated its electronic energy band structure by ARPES. Figure [4.5a](#page-5-0) shows ARPES data measured along the high symmetry direction $K-\Gamma$ -M-K in the hexagonal Brillouin zone at a photon energy of 21.2 eV. Data taken at other photon energies show the same dispersion, confirming the 2D character of the monolayer PtSe₂. Second-derivative spectra of raw experimental band structures (Fig. [4.5a](#page-5-0)) are depicted in Fig. [4.5b](#page-5-0) to enhance the visibility of the bands. Here, the top of the valence band is observed to be at $-$ 1.2 eV at the Γ point and the conduction band is above the Fermi level, indicating that monolayer $PtSe_2$ is a semiconductor. It is quite different from the bulk $PtSe_2$, which-according to calculations-is a semimetal. A direct comparison between the ARPES spectrum (Fig. [4.5b](#page-5-0)) and the calculated band structure (green dotted lines in Fig. [4.5b](#page-5-0)) shows excellent quantitative agreement. Combining the ARPES spectra with DFT calculations, we confirm that we have synthesized a single-layer $PtSe₂$ and that the epitaxial $PtSe₂$ essentially has the same electronic properties as the freestanding single-layer PtSe₂. For the first time, the band structure of monolayer PtSe₂ films has been determined experimentally.

The semimetal-to-semiconductor transition was revealed by DFT-LDA calculations. As shown in Fig. [4.5c](#page-5-0), the band structure and density of state (DOS) suggest

Fig. 4.5 ARPES spectra and valence bands of single-layer PtSe₂. **a** ARPES spectra obtained on the monolayer PtSe₂ on Pt(111). The high symmetry directions are shown in the inset. **b** Secondderivative spectra of the raw ARPES data in (**a**). The calculated valence bands, superimposed as green dashed lines, are in excellent agreement with the experimental data. The bands marked by white arrows are from the Pt substrate. **c**, **d** Theoretically calculated band structure and density of states of monolayer PtSe₂ and bulk PtSe₂, respectively. Reproduced with permission from Ref. [\[10\]](#page-9-5), © 2015 ACS

single-layer PtSe₂ is a semiconductor with an energy gap of 1.20 eV (2.10 eV bandgap is predicted from GW calculation [\[11\]](#page-9-6)). As a comparison, the band structure and DOS of bulk PtSe₂ are plotted in Fig. [4.5d](#page-5-0), which confirm that bulk PtSe₂ is semimetallic $[12, 13]$ $[12, 13]$ $[12, 13]$. Actually, bilayer PtSe₂ remains a semiconductor, but the energy gap decreases to 0.21 eV. Starting from a trilayer, $PtSe₂$ becomes semimetallic, as shown in Fig. [4.6.](#page-5-1) Therefore, only single-layer PtSe₂ is a semiconductor with a sizeable bandgap.

4.4 Photocatalytic Properties

The opening of a sizable bandgap within the range of visible light makes monolayer PtSe₂ potentially suitable for optoelectronics and photocatalysis. We explored the photocatalytic properties of monolayer $PtSe₂$ by the degradation of methylene blue (MB) aqueous solution, which serves as a typical indicator of photocatalytic reactivity [\[14,](#page-9-9) [15\]](#page-9-10).

4.4.1 Experimental Setups

Figure [4.7a](#page-6-0) displays the schematic diagram of photocatalytic experiments. The photocatalytic activity of as-prepared monolayer $PtSe₂$ films was tested by catalytic degradation of methylene blue serving as a standard model dye under visible-light irradiation at room temperature. The ultraviolet/visible-light source was a 150 W Xe lamp located at a distance of 15 cm above the solution. A set of appropriate cut-off filters was applied to determine illumination wavelength and ensured that the photocatalytic reaction took place just under visible light. The as-prepared monolayer PtSe₂ films were exfoliated from the Pt (111) substrate by ultra-sonication in aqueous solution. The $Pt(111)$ crystal was picked out from the solution to avoid its possible influence on the photocatalytic activity. Then MB molecules and ethanol (0.01 mL)

Fig. 4.7 Photocatalytic activity of a single-layer PtSe₂ film. **a** Schematic diagram of the photocatalytic degradation of methylene blue (MB) molecules. Electrons and holes are excited by visible-light irradiation of epitaxial PtSe₂ monolayer films. The MB degradation by photo-induced electrons demonstrates the photocatalytic activity of PtSe₂ monolayer films. **b** Time trace of the normalized concentration (C_t/C_0 , where C_t and C_0 are the MB concentrations at time t min and 0 min, respectively) of the absorbance at a wavelength of 667 nm, the main absorbance peak of MB. The inset shows the UV-vis absorption spectra of MB, recorded at time intervals of 4 min. Reproduced with permission from Ref. [\[10\]](#page-9-5), © 2015 ACS

were added to the solution containing peeled $PtSe₂$ monolayers. Before the photocatalytic reaction, the solution was kept in darkness for one hour in order to achieve an adsorption-desorption equilibrium between the $PtSe₂$ film and MB molecules. After that, the suspension was exposed to visible-light irradiation. At time intervals of 4 min, solution samples were collected and their absorbance was measured by a commercial ultraviolet-visible (UV-vis) spectrophotometer. Accordingly, the intensity changes of characteristic absorbance peaks of the MB molecules were recorded. The photocatalytic performance of $PtSe₂$ monolayers was thus evaluated by the time-dependent degradation rate C_t/C_0 , as exhibited in Fig. [4.7b](#page-6-0).

4.4.2 Photocatalytic Characterizations

The MB molecules adsorbed on the PtSe₂ films are degraded by electrons that are excited by visible light. The time-dependent degradation of MB with a single layer PtSe₂ catalyst was monitored by checking the decrease in the intensities of characteristic absorbance peaks of the MB molecules. As we can see in Fig. [4.7b](#page-6-0), the photodegradation portion of MB molecules reached 38% after visible-light irradiation for 24 min. This rate is about four times faster than the rate obtained using $PtSe₂$ nanocrystals $[16, 17]$ $[16, 17]$ $[16, 17]$, putting single-layer PtSe₂ in the same class as nitrogen-doped $TiO₂$ nanoparticles for photocatalysis [\[18,](#page-9-13) [19\]](#page-9-14).

4.5 Valleytronics

With the existence of an energy gap in the single-layer $PtSe₂$, optical excitations can occur between the Γ point and the valley point along the Γ -M direction. This is reminiscent of the recently discovered valley-selective circular dichroism in $MoS₂$ by circularly polarized light [\[20](#page-9-15)[–22\]](#page-9-16). To explore this possibility, we calculated the degree of circular polarization of free-standing single-layer $PtSe₂$. The calculated circular polarization due to the direct interband transition between the top of the valence band (VB) to the bottom of the conduction band (CB) is shown in Fig. [4.8a](#page-8-2). It shows significant circular dichroism polarization along the M-K direction and near the Γ point. In view of the indirect energy gap, this process can be assisted by lattice vibrations. It is noteworthy that the circular dichroism polarization not only exists in the transition between the top of the VB and the bottom of the CB, it also exists in transitions to higher energy levels. Circular dichroism polarization due to transitions from the vicinity of the VB to the vicinity of the CB can be clearly seen in Figs. [4.8b](#page-8-2)–d. Due to this significant circular polarization, in the presence of a nonvanishing in-plane electric field, the anomalous charge current driven by the Berry curvature would flow to the opposite edges, leading to a valley polarized current and the resulting quantum valley Hall effect [\[23,](#page-9-17) [24\]](#page-9-18).

Fig. 4.8 Momentum dependence of circular polarization of single-layer PtSe₂. **a–d** represent the calculated circular polarization due to the direct interband transition from the top of the valence band (VB1) to the bottom of the conduction band (CB1), from VB1 to the higher conduction band (CB2), from the lower valence band (VB2) to CB1, and from VB2 to CB2, respectively. Significant circular dichroism polarization exists along the M-K direction and near the Γ point. Reproduced with permission from Ref. [\[10\]](#page-9-5), \odot 2015 ACS

4.6 Summary and Outlook

We have successfully fabricated high-quality, single-crystalline, monolayer $PtSe₂$ films, a new member of the TMDs family, through a single-step, direct selenization of a Pt(111) substrate at a relatively low temperature (∼270 °C).

- (1) Characterizations by LEED, STM, STEM, and DFT calculations elucidated both in-plane and vertical monolayer structures with atomic resolution.
- (2) The ARPES measurements and their agreement with calculations revealed the semiconducting electronic structure of the single-layer PtSe₂.
- (3) Together with the photocatalytic performance observed experimentally, monolayer PtSe₂ shows promise for potential applications in optoelectronics and photocatalysis.
- (4) The circular polarization of monolayer $PtSe₂$ in momentum space indicates a promising potential for valleytronic devices.
- (5) Our studies are a significant step forward in expanding the family of single-layer semiconducting TMDs and exploring the application potentials of ultra-thin TMDs in photoelectronic and energy-harvesting devices.

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