

# The *yuga* of the *Yavanajātaka*: David Pingree's text and translation reviewed \*

# Introduction

The Yavanajātaka written by Sphujidhvaja Yavaneśvara in the third century AD was edited and translated into English by Prof. David Pingree in 1978. The last chapter (Ch. 79) of this work is called *Horāvidhi* and deals with luni-solar astronomy on the basis of a period of 165 years called *yuga* and the synodic motion of the planets. The text is marred by faulty editing, the incorrect readings being adopted and the correct ones given in the apparatus criticus, with the result that the translation is incorrect at places and the meaning really intended by the author is lost.

The object of the present paper is to study this chapter so as to bring out the meaning really intended by the author. The paper will be confined to the study of the yuga of the  $Yavanaj\bar{a}taka$  and its various constituents. In the process the relevant passages and their translation as given by Prof. Pingree will be reviewed and modified.

### 1 Time-measures

Verses 28–29 of Ch. 79 of the  $Yavanaj\bar{a}taka$  give a table of time-measures. Pingree's text and translation run thus:

त्रयः पलाः स्युः कुडवोऽष्टमश्च तन्नाडिकाख्यं विदुरेकषष्टिम् । ताः षष्टिलिप्तापि च नाडिकाख्या भवन्ति षष्टिर्द्युनिशा क्रमेण ॥२८॥ कला निमेषाष्टशता दशोना विदुः कलास्त्रिंश [च] नाडिका तु । द्विनाडिकस्तु प्रथितो मुहूर्तो मानप्रमाणादिविधिप्रसिद्धौ ॥२९॥

trayah palāh syuh kudavo'stamaśca tannādikākhyam vidurekasastim |

\* K. S. Shukla, Indian Journal of History of Science, Vol. 24, No. 4 (1989), pp. 211–223.

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tāh şasţiliptāpi ca nādikākhyā bhavanti şasţirdyuniśā krameņa ||28|| kalā nimesāstašatā dašonā viduh kalāstrimša |ca| nādikā tu | dvinādikastu prathito muhūrto mānapramānādividhiprasiddhau ||29||

A kuḍava is  $3\frac{1}{8}$  palas, and 61 kuḍavas equal 1  $n\bar{a}\dot{q}ik\bar{a}$ . The  $n\bar{a}\dot{q}ik\bar{a}s$  are also each divided into 60 *liptās* ("minutes"); there are 60  $n\bar{a}\dot{q}ik\bar{a}s$  in a nychthemeron. One kalā equals 790 (?) nimeṣas, one  $n\bar{a}\dot{q}ik\bar{a}$  30 kalās, and one muhūrta 2  $n\bar{a}\dot{q}ik\bar{a}s$  in the accomplishment of the rules relating to measures and standards.

#### Remarks

(1) We find that according to this translation one  $n\bar{a}\dot{d}ik\bar{a}$  is equal to 30  $kal\bar{a}s$ , whereas in the formulation of the rules stated in vss. 11, 12, and 13 one  $muh\bar{u}rta$  ("a period of 2  $n\bar{a}\dot{d}ik\bar{a}s$ ") is taken equal to 20  $kal\bar{a}s$ , and in verse 31 also one  $kal\bar{a}$  has been used in the sense of  $\frac{1}{10}$  of a  $n\bar{a}\dot{d}ik\bar{a}$  or  $\frac{1}{20}$  of a  $muh\bar{u}rta$ . This discrepancy is due to adoption of the incorrect reading " $kal\bar{a}strimsa |ca|$ " (in vs. 29b) in place of the correct reading " $kal\bar{a}st\bar{a} dasa$ " which has been given in the apparatus criticus. Restoring the correct reading in place of the incorrect one, we find that the text gives the following table:

$3\frac{1}{8}$ palas	=	1 kuḍava
61 kuḍavas	=	$1 n \bar{a} \dot{d} i k \bar{a}$
$60 \ lipt\bar{as}$	=	$1 \ n \bar{a} \dot{d} i k \bar{a}$
$60 \ n \bar{a} \dot{d} i k \bar{a} s$	=	1 nychthemeron
790 nimeṣas	=	$1 \ kal\bar{a}$
$10 \ kal\bar{a}s$	=	$1 \ n \bar{a} \dot{d} i k \bar{a}$
$2 n \bar{a} dik \bar{a} s$	=	1 muhūrta (or kṣaṇa).

Likewise

20	$kal\bar{a}s$	=	$1 muh\bar{u}rta$
30	$muh\bar{u}rtas$	=	1 nychthemeron

It is these two relations that have been used in verses 11, 12, and 13. The same relations were given by Suśruta<sup>1</sup> and Parāśara.<sup>2</sup>

<sup>&</sup>lt;sup>1</sup>See Suśruta-saṃhitā; Sutrasthāna, ch. vi. 4.

 $<sup>^2 {\</sup>rm See}~Brhat-samhit\bar{a}$  with Bhattotpala's commentary, Sudhakara Dvivedi's edition, p. 24, lines 3–5.

(2) It is noteworthy that according to the  $Ved\bar{a}\dot{n}ga$ - $jyautisa^3$  too,

$$3\frac{1}{8} \ palas = 1 \ kudava,$$
  
and 61 kudavas = 1  $n\bar{a}dik\bar{a}.$ 

But there

$$1 \ n\bar{a}\dot{d}ik\bar{a} = 10\frac{1}{20} \ kal\bar{a}s$$

It seems that Sphujidhvaja Yavaneśvara has taken

$$1 n \bar{a} dik \bar{a} = 10 ka l \bar{a} s$$

to avoid fractions, or he has followed Suśruta or Parāśara.

### 2 Tithis in the yuga

Verse 6 gives the number of tithis in the yuga ("a period of 165 years"). Pingree's text and translation run thus:

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क्रमेण चन्द्रः क्षयवृद्धिलक्ष्य-
स्तिथिश्चतुर्मानविधानबीजः ।
षद्वञ्चकाग्रे द्विशते सहस्रं
तेषां युगे बिन्दुयुतानि षट् च ॥६॥
krameṇa\ candrah\ kṣayavrddhilakṣya-
stithiścaturmānavidhānabījah |
saṭpañcakāgre\ dviśate\ sahasram
teṣām\ yuge\ binduyutāni\ ṣat\ ca\ ||6||
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The Moon is to be characterised by waning and waxing in order. The *tithi* possesses the seed of the principles of the four (systems of time-) measurement. There are 60,265 (days) in a *yuga*.

#### Remarks

The last sentence of this translation is wrong. The number 60,265 as well as its designation as "days" both are incorrect. The word *satpañcaka* means  $6 \times 5$  i.e. 30, not 65; and the word "*teṣām*" refers to *tithis*, not to civil days. Moreover, the number of civil days in a *yuga* is 60,272, not 60,265. See below.

The second half of the text really gives the number of *tithis* in the *yuga*, not the number of civil days in the *yuga* as supposed by Pingree. The error is due to faulty editing of the text. The adoption of the incorrect readings " $k\bar{a}gre\ dvisate$ " and "*bindu*" in place of the correct readings " $k\bar{a}gr\bar{a}\ dvisat\bar{a}$ "

<sup>&</sup>lt;sup>3</sup>See Yājuṣa-jyautiṣa, vs. 24.

and "*viddhya*", respectively has spoiled the text. It is noteworthy that the correct readings are given in the apparatus.

The correct reading of the text is:

# क्रमेण चन्द्रक्षयवृद्धिलक्ष्य-स्तिथिश्चतुर्मानविधानबीजः । षद्वञ्चकाग्रा द्विशती सहस्रं तेषां युगे विद्ध्ययुतानि षट् च ॥६॥

krameņa candrakṣayavṛddhilaksyastithiścaturmānavidhānabījaḥ | ṣaṭpañcakāgrā dviśatī sahasraṃ teṣāṃ yuge viddhyayutāni ṣaṭ ca ||6||

The *tithi*, which is the indicator of the gradual waning or waxing of the Moon, is the seed of the principles of the four (systems of time-) measurement. Know that there are 60000 plus 1000 plus 200 and  $6 \times 5$  (i.e. 61,230) of them (in a *yuga*).

That is,

one 
$$yuga = 61230$$
 tithis,

or 2041 synodic months, as stated in vss. 9 and 20 c–d.

# 3 Civil days in the yuga

Verse 7 gives the number of civil days in the yuga. Pingree's text and translation run thus:

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त्रिंशन्मुहूर्तं दिनरात्रमुक्तं
सूर्योदयात् कालबुधास्तदाहुः ।
तेषां शते द्वे <u>त्रिशदेकका</u>ग्रे
षट् खायुतान्यर्कयुगं वदन्ति ॥७॥
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trimśanmuhūrtam dinarātramuktam sūryodayāt kālabudhāstadāhuḥ | teṣām śate dve triśadekakāgre ṣaṭ khāyutānyarkayugaṃ vadanti ||7||

A nychthemeron is said to consist of 30  $muh\bar{u}rtas$ ; experts on time say that it beings with sunrise. They say that a *yuga* of the Sun consists of 61,230 (*tithis*).

#### Remarks

The second sentence of this translation, though mathematically correct, is not the correct translation of the second half of the text. The number 61330 and

its designation as "tithis" both are wrong. The word "triśat" means 300, not 30; and it is difficult to interpret " $ekak\bar{a}gre$  sat  $kh\bar{a}yutani$ " as meaning 61000. Also, the word " $tes\bar{a}m$ " refers to nychthemera or civil days, not to tithis.

The second half of the verse really gives the number of civil days in a *yuga*, not the number of *tithis* in a *yuga* as supposed by Pingree. The error is due to the faulty editing of the text. The adoption of the incorrect readings "*triśadekakāgre*" and "*şaṭ khā*°" in place of the correct readings "*trikṛdaṣṭakā-gre*" and "*şaṭkā*°" respectively has marred the text. It is noteworthy that the correct readings are given in the apparatus.

The correct reading of the text is:

त्रिंशन्मुहूर्तं दिनरात्रमुक्तं सूर्योदयात् कालबुधास्तदाहुः । तेषां शते द्वे त्रिकृदष्टकाग्रे षद्भायुतान्यर्कयुगं वदन्ति ॥७॥

trimšanmuhūrtam dinarātramuktam sūryodayāt kālabudhāstadāhuh | tesām šate dve trikŗdastakāgre satkāyutānyarkayugam vadanti ||7||

A nychthemeron (civil day) is said to consist of 30 muh $\bar{u}rtas$ ; experts on time say that it begins with sunrise. They say that a *yuga* of the Sun consists of 60000 plus 200 plus  $3^2 \times 8$  (i.e. 60,272) of them (i.e. civil days).

That is,

one 
$$yuga = 60272$$
 civil days.

The word "trikrt" means  $3^2$  i.e. 9, and the word "trikrdastaka"  $3^2 \times 8$  i.e. 72.

#### Further remarks on vss. 6 and 7

Pingree is aware of the fact that the second half of vs. 6 should contain the number of *tithis* in a *yuga* and the second half of vs. 7 the number of *civil* days in a *yuga*, but his text has landed him in trouble and he remarks: "A more logical order might be achieved by interchanging 6 c–d with 7 c–d." He also complains about Sphujidhvaja Yavaneśvara's way of expressing numbers in verse: "The extreme clumsiness with which Sphujidhvaja expresses numbers is a reflection of the fact that a satisfactory and consistent method of versifying them had not yet been devised in the late third century." But these remarks are uncalled for, as it is all due to the faulty edited text.

# 4 Civil days in a solar year

Verse 34 gives the number of civil days in a solar year. Pingree's text and translation run thus:

सपञ्चषष्टिं त्रिशतं दिनानां द्यूनं द्विभिन्नं तु दिनांशकानाम् । ज्यूनं शतार्धं दिनकृत्समा स्याद् यया भवर्गं सविता भुनक्ति ॥३४॥

sapañcaṣaṣṭiṃ triśataṃ dinānāṃ dyūnaṃ dvibhinnaṃ tu dināṃśakānām | tryunaṃ śatārdhaṃ dinakṛtsamā syād yayā bhavargaṃ savitā bhunakti ||34||

A year of the Sun consists of 365 days and 14; 47 sixtieths (*amśas*) of a day, in which the Sun traverses the signs.

#### Remarks

This translation is incorrect, because "14; 47 sixtieths" does not yield the value of the solar year according to Sphujidhvaja. For, according to this translation

one solar year = 6, 5; 14, 47 days,

whereas according to Sphujidhvaja

one solar year = 6, 5; 17, 5, 27, 16 days.

The error is due to the adoption of the incorrect reading " $dy\bar{u}nam dvibhinnam$ " in place of the correct reading " $yug\bar{a}dvibhinnam$ " given in the apparatus.

The correct reading of the text is:

सपञ्चषष्टिं त्रिशतं दिनानां युगाद्विभिन्नं तु दिनांशकानाम् । त्र्यूनं शतार्धं दिनकृत्समा स्याद् यया भवर्गं सविता भुनक्ति ॥३४॥

sapañcaṣaṣṭiṃ triśataṃ dinānāṃ yugādvibhinnaṃ tu dināṃśakānāṃ | tryūnaṃ śatārdhaṃ dinakṛtsamā syād yayā bhavargaṃ savitā bhunakti ||34||

A yuga of the Sun consists of 365 days and a fraction of a day equal to fifty minus three divided by (the number of years in) a yuga, in which the Sun traverses the signs.

That is,

one solar year = 
$$365 + \frac{50 - 3}{165}$$
 civil days  
=  $\frac{60272}{165}$  civil days.

This result confirms the statement of vs. 7 that there are 60,272 days in a yuga (consisting of 165 years).

### 5 Civil days in a solar month

Verse 11 defines a civil month and gives the number of civil days etc. in a solar month. Pingree's text and translation run thus:

त्रिंशद्दिनाः सावनमास आर्क-स्र्यग्रैर्विशिष्टा दशभिर्मुहूर्तैः । कलाचतुष्केण च पञ्चषद्वै-स्र्यग्र्यांशकेश्च द्विगुणेश्चतुर्भिः ॥१९॥

trimśaddināḥ sāvanamāsa ārkastryagrairvišisṭā daśabhirmuhūrtaiḥ | kalācatuṣkeṇa ca pañcaṣaṭkaistryagryāṃśakaiśca dviguṇaiscaturbhiḥ ||11||

A civil month equals 30 days, a solar month equals (a civil month) plus 13  $muh\bar{u}rtas$  and 4  $kal\bar{a}s$  and 56 thirds and 2 fourths.

#### Remarks

Here the text is correct<sup>4</sup> but the translation incorrect. For, "*pañcaṣatka*" means  $5 \times 6$  i.e. 30, not 56; also "*tryagryāmśaka*" does not mean third, nor "*catur*" fourth. Moreover, according to this translation,

one solar month = 30; 26, 9, 52, 4 days

whereas, according to Sphujidhvaja,

one solar month = 30; 26, 25, 27, 16 days.

The correct translation is:

A civil month equals 30 days, a solar month is greater (than that) by 10+3 muhūrtas, 4 kalās, and  $\frac{2\times 4}{5\times 6+3}$  of a kalā.

<sup>&</sup>lt;sup>4</sup>Read °*rviśisto* in place of °*rviśistā*.

Thus,

one solar month = 30 days + 13 
$$muh\bar{u}rtas + 4\frac{8}{33} kal\bar{a}s$$
  
=  $\frac{60272}{1980}$ civil days,

because 20  $kal\bar{a}s = 1 muh\bar{u}rta$  and 30  $muh\bar{u}rtas = 1$  civil day.

This result also confirms the statement of vs. 7 that there are 60272 civil days in a *yuga*.

### 6 Civil days in a synodic month

Verse 12 gives the number of civil days etc. in a synodic month. Pingree's text and translation run thus:

अह्रस्तु षद्वञ्चकमेकहीनं क्षणाष्टकौ द्वौ द्विकलाविहीनौ । कलालवाः सप्त <u>शतं विदिष्टः</u> समासभिन्नः शशिनः स मासः ॥१२॥

ahnastu şaţpañcakamekahīnam kşaņāsţakau dvau dvikalāvihīnau | kalālavāḥ sapta śatam vidisţaḥ samāsabhinnaḥ śaśinaḥ sa māsaḥ ||12||

A (synodic) month of the Moon, which ends with a conjunction, consists of 29 days and 32 ksanas minus 4  $kal\bar{a}s$  and 107 sixtieths of a  $kal\bar{a}$ .

#### Remarks

This translation is based on misinterpretation of the text and does not accord to the teaching of Sphujidhvaja. For, according to this translation,

one synodic month = 30; 3, 55, 34 days,

whereas according to Sphujidhvaja.

one synodic month = 29; 31, 50, 14, 24 days.

The error is really due to the adoption of the incorrect readings "ahnastu", "satam vidistah", and "samāsabhinnah" in place of the correct readings "ahnām tu", "satī dvisastā", and "svamāsabhinnā" respectively which are given in the apparatus.

Thus, the correct reading of the text is:

अह्नां तु षद्वञ्चकमेकहीनं क्षणाष्टकौ द्वौ द्विकलाविहीनौ । कलालवाः सप्तशती द्विषष्टा स्वमासभिन्ना शशिनः स मासः ॥१२॥

ahnām tu satpañcakamekahīnam ksaņāstakau dvau dvikalāvihīnau | kalālavāh saptašatī dvisastā svamāsabhinnā šašinah sa māsah ||12||

 $6 \times 5 - 1$  days,  $2 \times 8$  kṣaṇas (muhūrtas) minus 2 kalās, and a fraction of a kalā equal to 762 divided by (the number of) its own (i.e. synodic) months (in a yuga): this is (the length of) the (synodic) month of the Moon.

That is,

one synodic month = 29 days + (16  $muh\bar{u}rtas - 2 kal\bar{a}s) + \frac{762}{2041} kal\bar{a}$ ,

because there are 2041 synodic months in a yuga,  $=\frac{60272}{2041}$  civil days, because 20  $kal\bar{a}s = 1 \ muh\bar{u}rta$  and 30  $muh\bar{u}rtas = 1$  civil day.

This again confirms that there are 60272 civil days in a yuga.

# 7 Civil days in a sidereal month

Verse 13 gives the length of a sidereal month in terms of civil days, etc. Pingree's text and translation run thus:

आर्क्षस्तु कृत्त्रिर्द्विगुणस्तु कृच क्षणाः क्षणार्धं च कलाश्च तिस्रः । कलांशकानां च त्रिसप्तकाग्रं शतं विभक्तो दलितैः समासैः ॥१३॥

ārksastu krttrirdviguņastu krcca ksaņāḥ ksanārdhaṃ ca kalāśca tisraḥ | kalāṃśakānāṃ ca trisaptakāgraṃ śataṃ vibhakto dalitaiḥ samāsaiḥ ||13||

A sidereal month consists of 27 days plus  $8\frac{1}{2}$  ksanas and 3 kalās and 137 sixtieths of a kalā: it is separated by half-conjunctions(?).

#### Remarks

The first line of the text is corrupt and the translation is arbitrary and wrong. "*Trisaptaka*" does not mean 37; it means  $3 \times 7$  or 21. It is difficult to understand how the first line has been interpreted in that way.

According to the above translation,

one sidereal month = 27; 17, 10, 34 days

whereas, according to Sphujidhvaja,

one sidereal month = 27; 19, 18, 39 days.

The correct text is:

आर्क्षस्त्रिकृत्त्रिर्द्यगणस्त्रिकृच क्षणाः क्षणार्धं च कलाश्च तिस्रः । कलांशकानां च त्रिसप्तकाग्रं शतं विभक्तं दलितैः स्वमासैः ॥१३॥

ārkṣastrikṛttrirdyugaṇastrikṛcca kṣaṇāḥ kṣaṇārdhaṃ ca kalāśca tisraḥ | kalāmśakānāṃ ca trisaptakāgram śataṃ vibhaktaṃ dalitaiḥ svamāsaiḥ ||13||

A sidereal month consists of  $3^2 \times 3$  days,  $3^2$  kṣaṇas (muhūrtas) plus half a kṣaṇa, 3 kalās plus a fraction of a kalā equal to 121 divided by half (the number) of its own (i.e. sidereal) months (in a yuga).

That is,

one sidereal month = 27 days + 
$$9\frac{1}{2}$$
 muh $\bar{u}$ rtas +  $3\frac{121}{1103}$  kal $\bar{a}$ s,

because there are 2206 sidereal months (or Moon's revolutions) in a yuga,

$$=\frac{60272}{2206}$$
 civil days,

because 20  $kal\bar{a}s = 1 muh\bar{u}rta$  and 30  $muh\bar{u}rtas = 1$  civil day.

This is true because there are 60272 civil days and 2206 sidereal months in a yuga.

### 8 Intercalary days in a solar year

Verse 19(a–c) gives the number of intercalary days in a solar year and the number of intercalary months in a given number of solar years. Pingree's text and translation run thus:

एकादशैकाद[श] भागयुत्त्वा युगाद्गताब्दान् विहतान् विभज्य । षद्वञ्चकेनाधिकमासकास्ते ... ... ॥୨९॥ ekādaśaikāda[śa] bhāgayuktyā yugādgatābdān vihatān vibhajya | ṣaṭpañcakenādhikamāsakāste ... ... ... ... ... ||19||

The number of years which have passed of the *yuga* is to be multiplied by 11; 11 and divided by 30: (the result is the number of lapsed) intercalary months.

#### Remarks

The text is correct with one exception that there should be "yutya" in place of "yuktyā" in the first line. But the translation is erroneous because the number 11; 11 (denoting  $11\frac{11}{60}$ ) is wrong. There are  $11\frac{1}{11}$  intercalary days in a solar year, not  $11\frac{11}{60}$ . The correct translation is:

The number of years which have passed of the *yuga*, multiplied by  $11\frac{1}{11}$  and divided by 30 gives the number of intercalary months (in that period).

This is true because there being 1980 solar months and 2041 synodic months in a *yuga*, there are 61 intercalary months in a *yuga*. Likewise there are  $\frac{61 \times 30}{165}$  or  $11\frac{1}{11}$  intercalary days in a year.

#### 9 Omitted tithis in a yuga

Verse 5 given length of a *tithi* in terms of civil days, the length of a civil day in terms of *tithis*, and the number of omitted *tithis* in a *yuga*, Pingree's text and translation run thus:

दिनं चतुः षष्टिलवोनमाहु-स्तिथिं प्रषष्ट्यन्त्यमहस्तु सर्वम् । <u>द्विषष्टिभागं नवतिः</u> सहस्रं युगे त्वृतुनामपशुद्धशतम् ॥५॥

dinam catuhṣaṣṭilavonamāhustithim praṣaṣṭyantyamahastu sarvam | dviṣaṣṭibhāgam navatih sahasram yuge tvṛtūnāmapaśuddhaśatam ||5||

They say that a *tithi* equals a day minus  $\frac{1}{64}$ th, but that every day equals a *tithi* plus  $\frac{1}{60}$ th. In a *yuga* there are 990 seasons (*rtu*), (each) consisting of 62 (*tithis*).

#### Remarks

- 1. This translation is incorrect, because
  - (i) if one *tithi* consists of  $1 \frac{1}{64}$  civil day, a civil day cannot be equal to  $1 + \frac{1}{60}$  *tithis*; and
  - (ii) if there 990 seasons in a *yuga* and 62 *tithis* in a season, there must be  $990 \times 62$  or 61380 *tithis* in a *yuga*. but according to vs. 6 there are only 61230 *tithis* in a *yuga*.
- 2. The text given by Pingree is faulty, because he has adopted the incorrect reading "dvişaştibhāgam navatih" in place of the correct reading "trişaştibhāgam" and the incorrect reading "tvrtūnāmapaśuddhaśatam" in place of the correct reading "vamānāmapasaptaṣatkam". Partially correct readings occur in the apparatus.
- 3. The correct reading of the text is:

दिनं चतुः षष्टिलवोनमाहु-स्तिथिं प्रषष्ट्यन्त्यमहस्तु सर्वम् । त्रिषष्टिभागेन युतं सहस्रं युगेऽवमानामपसप्तषद्भम् ॥५॥

dinam catuḥṣaṣṭilavonamāhustithim praṣaṣṭyantyamahastu sarvam | triṣaṣṭībhāgena yutam sahasram yuge'vamānāmapasaptaṣaṭkam ||5||

They say that a *tithi* is equal to a day minus  $\frac{1}{64}$  of a day, correct up to the sixtieth of a sixtieth (of a day, i.e. up to *vighațīs*), and a day equals a whole *tithi* plus  $\frac{1}{63}$  of a *tithi*. The number of omitted *tithis* in a *yuga* is equal to 1000 minus 42 (i.e. 958).

This can be easily proved to be true. For, in a yuga

(i) no. of tithis = 61230, and no. of civil days = 60272. Therefore,

one 
$$tithi = \frac{60272}{61230} = 1 - \frac{1}{64}$$
 civil day.

and

one civil day 
$$=\frac{61230}{60272} = 1 + \frac{1}{63}$$
 tithis.

Both the results are correct up to vighatis.

(ii) no. of omitted tithis = tithis - civil days = 61230 - 60272 = 958.

# 10 Conclusion

From the above discussion, we conclude that the yuga defined in the Yavana- $j\bar{a}taka$  contains:

Solar years = 165Solar months =  $165 \times 12 = 1980$ Solar days =  $165 \times 360 = 59400$ Civil days = 60272Synodic months = 2041Intercalary months = synodic months - solar months = 2041 - 1980 = 61 (vide vs. 10) Synodic days or  $tithis = 2041 \times 30 = 61230$ Omitted tithis = tithis - civil days= 61230 - 60272 = 958Sidereal months (or Moon's revolutions) = synodic months - Sun's revolutions = 2041 - 165 = 2206Risings of asterisms (or Earth's rotations) = civil days + Sun's revolutions= 60272 + 165 = 60437Risings of the Sun = risings of asterisms – Sun's revolutions = 60437 - 165 = 60272 (vide vs. 8) Risings of the Moon = risings of asterisms -Moon's revs. = 60437 - 2206 = 58231 (vide vs. 8) Solar year = 6, 5; 17, 5, 27, 16 days Sun's mean daily motion = 0; 59, 7, 55, 28 degrees Synodic month = 29; 31, 50, 14, 24 days Sidereal month = 27; 19, 18, 39 days. According to Sūryasiddhānta:

> Solar year = 6, 5; 15, 31, 3 days Sun's mean daily motion = 0; 59, 8, 10, 10 degrees Synodic month = 29; 31, 50 days Sidereal month = 27; 19, 18 days.