A Self-determined Evaluation Method for Science Popularization Based on IOWA Operator and Particle Swarm Optimization

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Abstract. With the increase of science popularization, evaluation of science popularization has become an urgent demand. Considering science popularization bases as independent agents, a self-determined evaluation approach for science popularization using induced ordered weighted averaging (IOWA) operator and particle swarm optimization (PSO) is proposed in this paper. Firstly, six factors including science popularization personnel, space, fund, media, activity and influence are selected to construct an index system for science popularization evaluation. On this basis, the absolute dominance and relative dominance of evaluation indexes are used as induced components, and the prior order of the evaluation indexes is determined. Besides, the optimization model of index weighted vectors is established by IOWA operator, index weighted vectors and evaluation value vectors are obtain. Finally, the optimal evaluation vectors and evaluation results are given according to the Perron-Frobenius decision eigenvalve theorem .

Keywords: Science popularization · Self-determined evaluation · Induced Ordered Weighted Averaging operator · Particle swarm optimization · Perron-Frobenius decision eigenvalve theorem

1 Introduction

With the rapid development of science and technology, the industry deeply aware that to promote the marketization process of the science and technology, they need to further strengthen the science popularization work and improve public response speed for new technology products. With the increasing of the popularization, it has become an urgent demand to carry out evaluation work to measure the effect and to promote the quality of the science popularization work. The evaluation method for science popularization has gradually become one of the research hotspots in social computing.

In the world, the study on science popularization evaluation is mostly a summary of the practice method. The evaluation indexes mainly consider the universal surface, influence on the attitude and behavior of the public. Information collection is the first step, which mainly include the field interviews, questionnaires survey and Internet feedbacks [1-3]. In China, science popularization evaluation has made some achievements.

Li Zhaohui et al. evaluated the science popularization infrastructure development from the scale, structure, and effect 3 aspects, employed the Delphi method to determine the weights of the index [4]. Ren Rongrong et al. established the evaluation index system of regional science popularization ability in 5 aspects including investment, facilities, personnel, creation and activity organization. They also combined the entropy weight method with GEM to determine the index weight [5]. Zuo Qingfu et al. established the effect evaluation index system of the project on science popularization benefiting peasants and prospering the rural, employed analytic hierarchy process method to calculate index weight [6]. Wu Huagang established the evaluation index system of science popularization resources construction, employed the global principal component analysis method to evaluate the science popularization resource construction level in 31 provinces / autonomous regions / municipalities in China [7].

It can be seen from the research status on science popularization evaluation that the existing science popularization evaluation methods are all considered evaluation target as passive "evaluation object", which has no "discourse right" in the evaluation. While the views of the evaluation target should be adopted comprehensively in the actual evaluation, carry out self-determined evaluation with "fair competition" concept [8]. In view of this, this paper give full independence to the science popularization base and introduce the Induced Ordered Weighted Averaging (IOWA) operator into the science popularization level evaluation to construct the self-determined evaluation model. The model is solved by particle swarm optimization algorithm, and then the self-determined evaluation results of science popularization are given.

2 The Evaluation Index System of Science Popularization

The primary task of science popularization evaluation is to establish a scientific evaluation index system. This paper refer to science popularization statistic survey which made by the Ministry of Science and Technology in the People's Republic of China. The science popularization personnel, space, fund, media, activity and influence six first level indexes are selected, and be subdivided into twenty-two second level indexes, establishing a science popularization evaluation index system, as shown in Table 1.

3 A Self-determined Evaluation Model for Science Popularization Based on IOWA

3.1 Formation of Decision Matrix for Science Popularization Evaluation

The *n* science popularization base to be evaluated is $E_i(i = 1, 2, \dots, n \in N)$, where the *j*-th evaluation index is $x_j(j = 1, 2, \dots, m \in M)$, then the indexes set of science popularization base is $I_i = \{x_{i1}, x_{i2}, \dots, x_{ij}, \dots, x_{im}\}$, where x_{ij} represents the value of the *j*-th evaluation index for the *i*-th science popularization base. All x_{ij} consist of the evaluation index matrix.

| First-level index | Second-level index | | | |
|---------------------------------|---|--|--|--|
| Science popularization | Full-time personnel <i>I</i> ₁ | | | |
| personnel | Part-time personnel I ₂ | | | |
| | Volunteers I ₃ | | | |
| Science popularization | Area of exhibition hall I_4 | | | |
| space | The number of exhibits I_5 | | | |
| | Equipment I ₆ | | | |
| Science popularization | Annual funds raised I ₇ | | | |
| fund | Annual amount used I ₈ | | | |
| | Special funds I ₉ | | | |
| Science popularization | Annual number of science popularization books published I_{10} | | | |
| media | Annual number of science popularization periodicals published I_{11} | | | |
| | Annual total page view of science popularization website I_{12} | | | |
| | Other science popularization readings I_{13} | | | |
| Science popularization activity | Person-time of participants in science popularization lectures and training I_{14} | | | |
| | Person-time of visitors for science popularization exhibitions I_{15} | | | |
| | Person-time of participants in science popularization competitions I_{16} | | | |
| | Person-time of participants in international communication of science popularization I_{17} | | | |
| | Person-time of young participants in science popularization I_{18} | | | |
| | Person-time of participants in science and technology activity week I_{19} | | | |
| Science popularization | Affirmation and naming I_{20} | | | |
| influence | Science popularization award I_{21} | | | |
| | Media coverage I_{22} | | | |

Table 1. Evaluation index system for science popularization

$$\mathbf{X} = (x_{ij})_{n \times m} = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1j} & \cdots & x_{1m} \\ x_{21} & x_{22} & & x_{2j} & \cdots & x_{2m} \\ \vdots & \vdots & \ddots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nj} & \cdots & x_{nm} \end{bmatrix}.$$
 (1)

Since the dimension of the evaluation index is not consistent, X should be normalized before the evaluation, and the normalized matrix is called the evaluation decision matrix $X' = (x'_{ij})_{n \times m}$. Because all the evaluation indexes selected in this paper are the benefit indexes, so they can be standardized as follows:

$$x_{ij}^{'} = \frac{x_{ij} - \min_{i} \{x_{ij}\}}{\max_{i} \{x_{ij}\} - \min_{i} \{x_{ij}\}}.$$
(2)

-

3.2 Absolute and Relative Dominance Calculation of Evaluation Index

In the self-determined evaluation, the competition field of the evaluation subject should be determined at first. For science popularization base E_i , the determination method of its competition field as follows:

- (1) For $\forall j \in M$, if $x_{ij} \ge x_{kj} (k \in N, k \ne i)$, then science popularization base E_i is better than E_k , not form a competitive relationship.
- (2) For $\forall j \in M$, if $x_{ij} \le x_{kj} (k \in N, k \ne i)$, then science popularization base E_i is worse than E_k , not form a competitive relationship.
- (3) For $\forall j \in M$, if both $x_{ij} \ge x_{kj}$ and $x_{ij} \le x_{kj} (k \in N, k \ne i)$ existing, then science popularization base E_i and E_k form a competitive relationship.

For science popularization base E_i , the set of the science popularization bases which form the competitive relationship with it is called competition field of E_i , as $H_i = \left\{ E_1^{(i)}, E_2^{(i)}, \dots, E_{n_i}^{(i)} \right\}$, where n_i represents the number of the science popularization bases which form the competitive relationship with E_i .

Set the competition intensity of the *j*-th evaluation index x_i of popularization science base E_i relative to E_k in the competition field [8].

$$d_{ik}^{(j)} = x_{ij} - x_{kj} (i, k \in N; j \in M).$$
(3)

For science popularization base E_i , the absolute dominance and relative dominance of the evaluation indexes are:

$$\lambda_i^{(j)} = \frac{\sum_{m=1}^{P_i} d_{im}^{(j)}}{\sum_{m=1}^{n_i} \left| d_{ik}^{(j)} \right|}.$$
(4)

$$\lambda_i^{\prime(j)} = \frac{\exp(\sum_{k=1}^{n_i} d_{ik}^{(j)})}{\sum_{j=1}^{m} \exp(\sum_{k=1}^{n_j} d_{ik}^{(j)})}.$$
(5)

Where, P_i is the number of the non-negative value of the competition strength of science popularization base E_i relative to all the science popularization bases in the competition field.

3.3 Determination of Position Weight Vector

For science popularization base E_i , the position weight vector of the evaluation index is $\boldsymbol{w} = (w_1, w_2, \dots, w_j, \dots, w_m)^T$, where

$$w_{j} = \frac{\frac{\sum_{l=1}^{j} \eta_{l}}{\sum_{j=1}^{m} q_{l-1}^{j} \eta_{l}}}{\sum_{j=1}^{m} q_{l-1}^{j} \eta_{l}}.$$
(6)

In Eq. (6), $\eta_1 = 1 - (\alpha \lambda_i^{(l)} + \beta \lambda_i^{\prime(l)}), (l \in M), 0 < q < 1, \alpha \lambda_i^{(l)} + \beta \lambda_i^{\prime(l)}$, is the overall competitive advantage of the *l*-th index, α and β are the preference of the absolute and relative dominance of the evaluation expert respectively, $\alpha + \beta = 1, \alpha, \beta \in [0, 1]$, this paper set $\alpha = \beta = 0.5$.

Take the absolute and relative preference dominance as the induced components, the evaluation value of the science popularization base E_k with E_i as the evaluation subject is [9]

$$Y_{k}[(\lambda_{1}^{(1)},\lambda_{1}^{'(1)},x_{1m}),(\lambda_{2}^{(2)},\lambda_{2}^{'(2)},x_{2m}),\cdots,(\lambda_{i}^{(k)},\lambda_{i}^{'(k)},x_{km})]$$

$$=\sum_{j=1}^{m}w_{j}a_{kj}(k\in N).$$
(7)

Where, a_{kj} is the value of the *j*-th ranked evaluation index of the science popularization base E_k .

According to the ordered weight averaging operator, the following optimization model can be used to solve the position weight vector:

$$\max \quad orness(w) = \frac{1}{m-1} \sum_{j=1}^{m} [(m-j)w_j]$$

s.t.
$$\begin{cases} w_j = \frac{\sum_{l=1}^{j} \eta_l}{\sum_{j=1}^{m} q_{l-1}^{l-j} \eta_l}, j \in M \\ \sum_{j=1}^{m} q_{l-1}^{j-j} \eta_l \\ 0 < q < 1, 0 < w_1 \le 0.5. \end{cases}$$
(8)

3.4 Aggregation of Self-determined Evaluation Values

If science popularization base E_i is the evaluation subject, whose given evaluation values of all the science popularization bases are $y^{(i)} = \left(y_1^{(i)}, y_2^{(i)}, \cdots, y_n^{(i)}\right)^T$, the evaluation value vector of all the science popularization bases is recorded as $\boldsymbol{Y} = (y^{(1)}, y^{(2)}, \cdots, y^{(n)})$. The sum of the angle between the optimal self-determined evaluation vector $\boldsymbol{y}^* = (y_1^*, y_2^*, \cdots, y_n^*)^T$ and the vector $y_1^{(i)}, y_2^{(i)}, \cdots, y_n^{(i)}$ should be the smallest, so that \boldsymbol{y}^* can be obtained according to the Perron-Frobenius decision eigenvalve theorem [10].

Theorem 1. For $\forall y \in \mathbb{R}^n, \max_{\|y\|_2} \sum_{i=1}^n (y^T, y^{(i)})^2 = \sum_{i=1}^n ((y^*)^T, y^{(i)})^2 = \lambda_{\max}$, where λ_{\max} is the largest eigenvalue of $YY^T, Y = (y^{(1)}, y^{(2)}, \dots, y^{(n)})$ is the positive eigenvectors of λ_{\max} correspond to YY^T , and $\|y^*\|_2 = 1$.

4 Optimal Evaluation Value Solve Based on Particle Swarm Optimization Algorithm

4.1 Particle Swarm Optimization Algorithm

Particle swarm optimization algorithm is an intelligent iterative optimization algorithm based on group oriented search, which is easy to implement, and has good robustness and fast convergence speed [11–14]. In the previous iteration of the standard particle swarm optimization algorithm, the particle *i* is updated according to the velocity *v* and position *x*:

$$v_i^{k+1} = \omega v_i^k + c_1 r_1 (p_i^k - x_i^k) + c_2 r_2 (p_g^k - x_i^k).$$
(9)

$$x_i^{k+1} = x_i^k + v_i^{k+1}.$$
 (10)

Where, k is the number of iterations, p_g^k is the history optimal position of the *i*-th individual particle in the k-th iteration; p_g^k is the history optimal position of group in the k-th iteration; ω is inertial weight; c_1 and c_2 is the learning factor which controlling the maximum step size; r_1 and r_2 are the random number between [0,1]; to ensure the search efficiency of the particle, usually limited velocity $v_i = [-v_{\min}, v_{\max}]$.

4.2 Solving Process of Optimal Evaluation Value

For the optimization model of Eq. (8), the PSO algorithm is employed to solve the optimal position weight vector, the optimal evaluation value vector, and then obtain the evaluation result. The calculation flow is shown in Fig. 1.

5 Case Analysis

Through the issuance of science popularization survey, collected the operational data of annual Guangzhou new energy and renewable energy science popularization base, Beijing new energy automobile exhibition center, smart grid demonstration hall of Sichuan electric power company of state grid, Yancheng new energy automobile industrial park and the Xin'ao group energy innovation experience center 5 science popularization bases ($E_1 \sim E_5$), as shown in Table 2, where p-t means person-times.



Fig. 1. The calculation process of optimal evaluation value and evaluation result

| Index | E_1 | E_2 | E_3 | E_4 | E_5 |
|------------|--------------------|---------------------|--------------------|--------------------|--------------------|
| I_1 | 2 | 1 | 5 | 2 | 2 |
| I_2 | 16 | 15 | 7 | 45 | 0 |
| I_3 | 0 | 80 | 28 | 60 | 0 |
| I_4 | 450 m ² | 1100 m ² | 900 m ² | 600 m ² | 660 m ² |
| I_5 | 17 pcs. | 6 pcs. | 20 pcs. | 200 pcs. | 4 pcs. |
| I_6 | 10 sets | 51 sets | 20 sets | 15 sets | 30 sets |
| I_7 | 280000 | 215000 | 800000 | 200000 | 8000000 |
| I_8 | 260000 | 215000 | 500000 | 200000 | 8000000 |
| <i>I</i> 9 | 0 | 0 | 200000 | 100000 | 2000000 |

Table 2. Operation data from science popularization bases

(Continued)

| | | | - | |
|----------|---|--|---|---|
| E_1 | E_2 | E_3 | E_4 | E_5 |
| 0 | 0 | 600 | 0 | 10000 |
| 0 | 0 | 0 | 0 | 12000 |
| 8000 | 0 | 0 | 4000 | 0 |
| 1000 | 5847 | 500 | 5000 | 0 |
| 1000 p-t | 0 | 400 p-t | 200 p-t | 6000 p-t |
| 5000 p-t | 5847 p-t | 1200 p-t | 5000 p-t | 3099 p-t |
| 200 p-t | 0 | 0 | 0 | 300 p-t |
| 0 | 503 p-t | 0 | 20 p-t | 576 p-t |
| 2500 p-t | 1671 p-t | 400 p-t | 300 p-t | 500 p-t |
| 2000 p-t | 0 | 200 p-t | 100 p-t | 0 |
| 3 | 6 | 2 | 1 | 2 |
| 0 | 0 | 0 | 3 | 0 |
| 3 times | 23 times | 18 times | 27 times | 100 times |
| | $\begin{array}{c} E_1 \\ 0 \\ 0 \\ 8000 \\ 1000 \\ 1000 \\ p-t \\ 5000 \\ p-t \\ 200 \\ p-t \\ 200 \\ p-t \\ 2000 \\ p-t \\ 3 \\ 0 \\ 3 \\ times \end{array}$ | E_1 E_2 000080000100058471000 p-t05000 p-t5847 p-t200 p-t02500 p-t1671 p-t2000 p-t036003 times23 times | E_1 E_2 E_3 00600000800000100058475001000 p-t0400 p-t5000 p-t5847 p-t1200 p-t200 p-t000503 p-t02500 p-t1671 p-t400 p-t2000 p-t0200 p-t3620003 times23 times18 times | E_1 E_2 E_3 E_4 006000000080000040001000584750050001000 p-t0400 p-t200 p-t5000 p-t5847 p-t1200 p-t5000 p-t5000 p-t5847 p-t1200 p-t5000 p-t200 p-t0000503 p-t020 p-t2500 p-t1671 p-t400 p-t300 p-t2000 p-t0200 p-t100 p-t362100033 times23 times18 times27 times |

 Table 2. (Continued)

The evaluation process of this method is as follows:

STEP1. Form the science popularization evaluation decision matrix.

According to Table 2 and Eq. (2), normalized the index data of the science popularization evaluation, obtain the decision matrix X.

STEP2. Calculate the absolute and relative dominance of the index.

According to Eq. (3)-(5), ensure the evaluation index priority order of the 5 science popularization base, and calculate the absolute and relative dominance, as shown in Table 3.

STEP3. Solve evaluation value vector.

In this paper, the PSO algorithm is employed to solve the optimization model of position weight vector. In order to find a PSO algorithm which has more advantage for solving, the accuracy, speed and stability of the standard particle swarm optimization (SPSO) [11], modified particle swarm optimization (MPSO) [12], improved particle swarm optimization algorithm (IPSO) [13] and time-varying acceleration coefficients particle swarm optimization algorithm (TACPSO) [14] are tested respectively. The object E_5 is chosen as an example to be evaluated, set the number of particles 10, 20 and 50 respectively, statistical data of fitness values and convergence iteration numbers are given of the four PSO algorithms for the 20 times continuous operation. The results are shown in Tables 4 and 5; when the number of particles is 50 and the maximum iteration number is 100, the convergence curve of the average fitness changing with the iteration number is shown in Fig. 2.

It can be seen from the figure and tables, the accuracy of the four PSO algorithms are very high, and the convergence speeds are very fast. In general, the performance of the four algorithms ranked as: TACPSO>IPSO>MPSO>SPSO.

The optimal q value and the minimum fitness are obtained by particle swarm optimization, and the corresponding evaluation value vector $\mathbf{y}^{(i)}$ is shown in Table 6.

| | | Ta | ble 3. | The evaluat | ion index p | monty c | order and do | ominance o | t the sci | ence popula | rrization ba | se | | |
|------------|-------------------|-------------------------|-----------------------|-------------------|-------------------------|-----------------------|-------------------|-------------------------|------------------------|-------------------|--------------------|------------------------|-------------------|-------------------------|
| E_1 | | | E_2 | | | E_3 | | | E_4 | | | E_5 | | |
| x_{j} | $\lambda_1^{(j)}$ | $\lambda_1^{\prime(j)}$ | x_j | $\lambda_2^{(j)}$ | $\lambda_2^{\prime(j)}$ | x_{j} | $\lambda_3^{(j)}$ | $\lambda_3^{\prime(j)}$ | x_{j} | $\lambda_4^{(j)}$ | $\lambda_4'^{(j)}$ | x_{j} | $\lambda_5^{(j)}$ | $\lambda_5^{\prime(j)}$ |
| x_{19} | 0.2500 | 0.0050 | x_{20} | 0.0000 | 0.0014 | x^{1} | 1.0000 | 0.5337 | x_{21} | 0.2500 | 0.0040 | x_{11} | 0.2500 | 0.0017 |
| x_{12} | 0.4727 | 0.0078 | x_6 | 0.4259 | 0.0066 | <i>x</i> ₉ | 0.1129 | 0.0071 | <i>x</i> 5 | 1.0000 | 0.1565 | x_8 | 0.0000 | 0.0005 |
| x_{18} | 0.0000 | 0.0010 | <i>x</i> ₃ | 1.0000 | 0.1431 | x_4 | 0.4000 | 0.0146 | x_2 | 0.8837 | 0.0347 | x_{10} | 0.0000 | 0.0004 |
| x_{16} | 0.0000 | 0.0009 | x_{13} | 1.0000 | 0.1236 | x_3 | 0.8319 | 0.0698 | <i>x</i> ₁₃ | 0.1485 | 0.0022 | <i>x</i> 7 | 0.2842 | 0.0015 |
| x_{15} | 0.1143 | 0.0036 | x_4 | 0.0090 | 0.0026 | <i>x</i> ₆ | 0.1549 | 0.0098 | x_3 | 1.0000 | 0.3109 | x_{14} | 0.0000 | 0.0009 |
| x_{20} | 0.0000 | 0.0013 | x_{15} | 1.0000 | 0.1830 | x_{19} | 0.2679 | 0.0110 | x_{15} | 0.0820 | 0.0019 | x_{22} | 0.6818 | 0.0052 |
| x_2 | 0.0173 | 0.0029 | x_{17} | 0.0018 | 0.0027 | x_7 | 0.1915 | 0.0102 | x_{12} | 0.0000 | 0.0022 | x_{16} | 1.0000 | 0.1438 |
| x_{14} | 0.0130 | 0.0030 | x_{18} | 0.0018 | 0.0028 | x_{20} | 0.0991 | 0.0088 | <i>x</i> 9 | 0.0000 | 0.0023 | <i>x</i> ₁₇ | 1.0000 | 0.1498 |
| x_1 | 0.0000 | 0.0007 | x_2 | 0.0000 | 0.0006 | x_{10} | 1.0000 | 0.2521 | <i>X</i> 22 | 0.5000 | 0.0067 | <i>x</i> 9 | 1.0000 | 0.0351 |
| x_{13} | 0.0000 | 0.0029 | X22 | 0.0000 | 0.0027 | <i>x</i> 5 | 0.1607 | 0.0097 | x_1 | 0.0000 | 0.0023 | x_6 | 1.0000 | 0.1480 |
| x_5 | 0.0000 | 0.0031 | x_5 | 0.0000 | 0.0029 | <i>X</i> 22 | 0.0000 | 0.0076 | x_4 | 0.0000 | 0.0025 | x_4 | 1.0000 | 0.1572 |
| x_7 | 1.0000 | 0.2747 | χ_8 | 0.0000 | 0.0018 | x_2 | 0.0000 | 0.0046 | x_{19} | 0.7500 | 0.0181 | x_1 | 0.0000 | 0.0006 |
| χ_8 | 0.1450 | 0.0024 | <i>x</i> ₇ | 1.0000 | 0.1414 | x_8 | 0.0461 | 0.0038 | <i>x</i> ₆ | 0.9410 | 0.0581 | x_{15} | 0.0000 | 0.0003 |
| x_{11} | 0.3243 | 0.0054 | x_{11} | 0.0000 | 0.0022 | x_{14} | 0.0882 | 0.0081 | <i>x</i> ₁₇ | 0.0286 | 0.0022 | x_{20} | 1.0000 | 0.1204 |
| x_{21} | 0.8706 | 0.0236 | x_{21} | 1.0000 | 0.0557 | x_{13} | 0.0000 | 0.0010 | x_{14} | 0.8706 | 0.0190 | x_{18} | 0.2248 | 0.0011 |
| x_{10} | 0.8571 | 0.0439 | x_{10} | 0.0000 | 0.0015 | x_{18} | 0.0000 | 0.0039 | x_{11} | 0.0000 | 0.0013 | x_{21} | 1.0000 | 0.0807 |
| X22 | 0.0000 | 0.0012 | x_{19} | 0.9533 | 0.0920 | x_{11} | 0.0000 | 0.0031 | x_8 | 0.0371 | 0.0012 | x_{19} | 1.0000 | 0.0634 |
| χ_6 | 1.0000 | 0.2119 | x_{14} | 0.8214 | 0.0306 | x_{21} | 0.0280 | 0.0045 | x_{10} | 0.0000 | 0.0011 | x_5 | 0.0864 | 0.0008 |
| x_{17} | 1.0000 | 0.3899 | x_{12} | 0.0000 | 0.0025 | x_{12} | 0.2174 | 0.0108 | x_7 | 0.0909 | 0.0027 | x_{12} | 0.0000 | 0.0009 |
| x_3 | 0.5714 | 0.0101 | x_{16} | 1.0000 | 0.1931 | x_{16} | 0.1667 | 0.0093 | x_{16} | 0.0000 | 0.0011 | x_2 | 0.1667 | 0.0013 |
| x_4 | 0.0000 | 0.0031 | x_1 | 0.0000 | 0.0029 | x_{17} | 0.0000 | 0.0076 | x_{18} | 1.0000 | 0.3642 | x_3 | 0.0000 | 0.0011 |
| χ_{0} | 0.0000 | 0.0017 | χ_{0} | 0.2358 | 0.0044 | x_{15} | 0.1351 | 0600.0 | x_{20} | 0.3364 | 0.0046 | x_{13} | 1.0000 | 0.0855 |

Table 3. The evaluation index priority order and dominance of the science popularization base

104

| Number of | Optimization | Fitness values for | or convergence | | |
|-----------|--------------|--------------------|----------------|---------------|------------|
| particles | algorithm | Optimal value | Worst value | Mean value | Standard |
| | | | | | deviation |
| 10 | SPSO | -0.9534409174 | -0.9534373473 | -0.9534403495 | 8.3018E-07 |
| | MPSO | -0.9534409298 | -0.9534409257 | -0.9534409293 | 9.0273E-10 |
| | IPSO | -0.9534409298 | -0.9534409288 | -0.9534409296 | 2.3167E-10 |
| | TACPSO | -0.9534409298 | -0.9534409295 | -0.9534409297 | 8.7945E-11 |
| 20 | SPSO | -0.9534409295 | -0.9534386345 | -0.9534404503 | 6.0019E-07 |
| | MPSO | -0.9534409298 | -0.9534409288 | -0.9534409296 | 2.1754E-10 |
| | IPSO | -0.9534409298 | -0.9534409291 | -0.9534409296 | 1.9105E-10 |
| | TACPSO | -0.9534409298 | -0.9534409296 | -0.9534409297 | 3.9564E-11 |
| 50 | SPSO | -0.9534409293 | -0.9534404423 | -0.9534408261 | 1.2766E-07 |
| | MPSO | -0.9534409298 | -0.9534409297 | -0.9534409297 | 1.2102E-11 |
| | IPSO | -0.9534409298 | -0.9534409297 | -0.9534409297 | 3.3404E-11 |
| | TACPSO | -0.9534409298 | -0.9534409297 | -0.9534409297 | 1.0032E-11 |

Table 4. The statistical data of fitness values for convergence

Table 5. The statistical data of iteration numbers for convergence

| Number of | Optimization | Iteration numbers for convergence | | | | |
|-----------|--------------|-----------------------------------|---------|-------|----------------|--|
| particles | algorithm | Maximum | Minimum | Mean | Standard | |
| | | value | value | value | deviation | |
| 10 | SPSO | 96 | 47 | 75.00 | 13.9812 | |
| | MPSO | 67 | 11 | 51.10 | 14.4801 | |
| | IPSO | 68 | 37 | 54.45 | 8.0163 | |
| | TACPSO | 65 | 21 | 49.85 | 12.7497 | |
| 20 | SPSO | 85 | 37 | 67.25 | 13.0015 | |
| | MPSO | 65 | 20 | 46.35 | 11.5953 | |
| | IPSO | 57 | 23 | 46.00 | 8.973 6 | |
| | TACPSO | 66 | 22 | 46.70 | 9.7877 | |
| 50 | SPSO | 77 | 10 | 50.15 | 19.4970 | |
| | MPSO | 55 | 8 | 39.10 | 10.9299 | |
| | IPSO | 51 | 7 | 36.75 | 12.8345 | |
| | TACPSO | 53 | 1 | 32.30 | 12.7159 | |

STEP4. Solve the self-determined evaluation value, give the evaluation results According to the Table 6, $y^{(i)}$ is constructed to evaluate the matrix Y, get the characteristic root diagonal matrix D and its corresponding eigenvectors matrix V.

$$\mathbf{D} = \begin{bmatrix} 0.4316 & & & \\ & 0.6358 & & & \\ & & 0.7586 & & \\ & & & 1.0772 & \\ & & & & 2.5229 \end{bmatrix}.$$
(11)

106 T. Zang et al.

$$\mathbf{V} = \begin{bmatrix} 0.1258 & 0.4023 & 0.7196 & -0.4176 & 0.3608 \\ -0.2434 & -0.8126 & 0.1601 & -0.1695 & 0.4755 \\ 0.8412 & -0.0708 & -0.2310 & 0.1763 & 0.4504 \\ -0.2957 & 0.3288 & -0.6242 & -0.4505 & 0.4602 \\ -0.3602 & 0.2544 & 0.1161 & 0.7502 & 0.4787 \end{bmatrix}.$$
(12)

The largest eigenvalue of YY^T is $\lambda_{max} = 2.5229$, by the Perron-Frobenius decision eigenvalue theorem, its corresponding eigenvalue column vector is the optimal



Fig. 2. The convergence curve of the average fitness (the number of particles is 50) (Color figure online)

| Science popularization | q value | Minimum | Evaluation value vector $y^{(i)}$ |
|------------------------|---------|---------------|-----------------------------------|
| base | | fitness | |
| E_1 | 0.1869 | -0.9590986825 | (0.9716,0.1171,0.0582, |
| | | | $0.1811, 0.0796)^T$ |
| E_2 | 0.1941 | -0.9545581273 | (0.2250,0.9976,0.2336, |
| | | | $0.1995, 0.2473)^T$ |
| E_3 | 0.2480 | -0.9621242911 | (0.1291,0.1979,0.9124, |
| | | | $0.3415, 0.4745)^T$ |
| E_4 | 0.1781 | -0.9587023359 | (0.0852,0.1341,0.0567, |
| | | | $0.9827, 0.0045)^T$ |
| <i>E</i> ₅ | 0.1988 | -0.9534409298 | (0.0125,0.0072,0.0283, |
| | | | $0.0057, 0.9996)^T$ |

Table 6. The evaluation value vector of science popularization bases

self-determined evaluation value $y^* = (0.3608, 0.4755, 0.4504, 0.4602, 0.4787)^T$. So far, the science popularization level of the 5 science popularization bases are ranked as $E_5 > E_2 > E_4 > E_3 > E_1$.

6 Conclusion

- (1) Overall considered science popularization personnel, space, fund, media, activity and influence these 6 aspects, established a science popularization evaluation index system, which ensure the systematicness of the evaluation.
- (2) Combined the IOWA operator and PSO algorithm, studied the science popularization level self-determined method, fully considered the index value differences of the science popularization bases, and provided a new scientific quantitative analysis method for the science popularization evaluation.
- (3) The PSO algorithm was employed to solve the position weight vector, which having the advantages of fast computation speed, high accuracy and good stability, could ensure the accuracy of the evaluation value vector.

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