# **PSO Optimized and Secured** Watermarking Scheme Based on DWT and SVD

Irshad Ahmad Ansari, Millie Pant and Chang Wook Ahn

**Abstract** The present study proposed a robust and secure watermarking scheme to authenticate the digital images for ownership claim. The proposed watermarking scheme is making use of 2-level of DWT (Discrete wavelet transform) to provide high capacity of watermark embedding. The SVD (singular value decomposition) is performed on the host and watermark images. Then, principal components are calculated for watermark image. The use of principal components for watermark embedding makes the scheme free from false positive error. PSO (particle swarm optimization) optimized multiple scaling factors along with principal components are utilized for watermark embedding in the singular values of host image. The PSO-optimized scaling factor provides a very good tradeoff between imperceptibility and robustness of watermarking scheme. The scheme is also extended to use for color images. The proposed scheme provides a secured and high data embedding with good robustness toward different signal processing attacks.

**Keywords** Discrete wavelet transform • Principal components • Secured watermarking • Particle swarm optimization • Robust watermarking

### 1 Introduction

With the developments in information technology and computer-based communication, the sharing of digital data becomes very easy on the world wide web. Such unprotected sharing of digital data increased the cases of false ownership claims and

I.A. Ansari (🖂) · M. Pant

Department of ASE, Indian Institute of Technology Roorkee, Roorkee, India e-mail: 01.irshad@gmail.com

M. Pant e-mail: millifpt@iitr.ac.in

C.W. Ahn Department of CSE, Sungkyunkwan University, Suwon, Republic of Korea e-mail: cwan@skku.edu

© Springer Science+Business Media Singapore 2016 M. Pant et al. (eds.), *Proceedings of Fifth International Conference on Soft Computing for Problem Solving*, Advances in Intelligent Systems and Computing 437, DOI 10.1007/978-981-10-0451-3\_38 copyright violations in the recent past. These digital data include images, audios, and videos. Copyrighted images can easily be manipulated with the help of powerful image processing tools in such a way that it leads to financial loss [1]. So there is a need of such tool which can detect/protect these manipulations. Digital image watermarking is one of such tools, which can protect the ownership of digital image by adding some ownership information (watermark) to the host image. Robust watermark is inserted into the host image in such a way that it remains robust to intentional/unintentional attacks and provides the ownership proof, whenever needed [2].

Broadly, image watermarking techniques are divided into visible and invisible image watermarking [1]. Visible image watermarking is a technique in which a logo (watermark) is placed in the original image which helps in identifying the owner of the image. On the other hand, invisible watermarking can again be divided into time domain and transfer domain techniques [1]. Time domain techniques are those, where the watermark is directly embedded by changing the pixel values of the image. On the other hand, original image has to undergo some transformations before the watermark embedding in transfer domain techniques. Transformed domain image watermarking techniques perform better as compared to simple time domain techniques [3]. Transformed domain techniques can further be divided into DCT (discrete cosine transform) [4], FFT (fast fourier transform), DWT (discrete wavelet transform) [5], and SVD (singular value decomposition) [6, 7] based image watermarking. A good watermarking scheme must have a high value of these four features: robustness, imperceptibility, capacity, and security [1, 3]. In this paper, we proposed an optimization of SVD (false positive free) based image watermarking technique in DWT domain using particle swarm optimization so that high value of all the four features can be attained.

Rest of the paper is organized as follows: Sect. 2 gives a brief review of related works and gaps in image watermarking domain. In Sect. 3, basics of DWT, PSO, and false positive solution are discussed, Sect. 4 talks about the proposed watermarking scheme, result and discussions are shown in Sect. 5 and finally Sect. 6 provides a brief conclusion.

#### 2 Related Work

The SVD-based scheme reportedly performs better in the recently developed watermarking algorithms [1, 5, 6]. The main reason for good performance is that the dominant singular values get very less affected by the intentional/unintentional attacks and show very small changes [7]. Generally, SVD-based watermarking is used with other transforms; because used alone increases its computational complexity to quite a high level. Ganic et al. [8] proposed the use of SVD along with DWT to provide robust watermarking scheme. Rastergar et al. [9] suggested shuffling of the host image pixels to increase the security for a 3-level DWT and SVD-based watermarking scheme. Lagzian et al. [10] proposed the use of RDWT at

the place of DWT to increase the capacity and then utilized the scheme proposed by Ganic et al. [8] for complete watermarking implementation. This scheme [10] performed better than other schemes in terms of capacity and robustness but suffers with a basic security flaw, which makes the scheme unusable [11]. Lai et al. [12] proposed a secure scheme with DWT. They decompose the watermark into two halves and embedded it into the LH and HL bands of DWT transformed host image. The main drawback of this scheme was low capacity. Makbool et al. [13] proposed a scheme with improved capacity by making use of RDWT. They claimed their scheme to be false positive free but later, it is proved by Ling et al. [14] that it also suffers with a security flaw (false positive problem), which makes their scheme vulnerable to attacks.

This study proposes a new watermarking scheme based on DWT, which is free from false positive error. In order to enhance the robustness further, proposed scheme also makes use of particle swarm optimization for optimal selection of scaling factors during embedding of watermark.

#### **3** Preliminaries

#### 3.1 Particle Swarm Optimization

Soft computing techniques (ANN, GA, PSO, etc.) are used in many fields for efficient problem solving [15, 16]. PSO is an optimization technique proposed by Kennedy et al. [17] in 1995. It is inspired by the swarm behavior of animals like bird flocking, animal herding, fish schooling, etc. Each member in the group learns from its own best performance as well as from the best performance of other members. This kind of property helps it to reach global optimum value in an efficient manner. PSO is a powerful tool for complex and multidimensional search [18, 19]. The very first step is the bounded initialization of swarm particles in the search space. Let each particle  $P_i$  have an initial position and velocity of  $x_i(t)$  and  $v_i(t)$  respectively at the time t. These positions assume to be the local best for the first iteration. PSO Algorithm has these steps:

- (1) Initialization of position  $x_i(t)$  and velocity  $v_i(t)$
- (2) Compute the value of fitness function for each position
- (3) Compute the local best position, i.e., each particles best position in all the iterations
- (4) Compute the global best position, i.e., best particle's position in current iteration
- (5) Update the velocity  $v_i(t)$  and position  $x_i(t)$  of each particle using Eqs. 1 and 2

$$v_i(t+1) = w * v_i(t) + c1 * \operatorname{rand}(l_{\text{best}} - x_i(t)) + c2 * \operatorname{rand}(g_{\text{best}} - x_i(t))$$
 (1)

and 
$$x_i(t+1) = x_i(t) + v_i(t)$$
 (2)

Here w is inertia weight used to determine the step size for each iteration. c1 and c2 are the learning factors, which determine the effectiveness of local and global learning and rand function is used to generate a number between (0, 1).

(6) Repeat the steps (2) to (5) till stopping criterion reached.

The stopping criterion can be the maximum number of iterations or change of fitness function below a certain threshold level.

#### 3.2 Discrete Wavelet Transform

DWT provides excellent spatio-frequency localization and this makes it very useful for watermark hiding; as it provides high value of robustness and imperceptibility. Many watermarking schemes have been proposed using this feature of DWT. Then again, DWT is not able to provide a high capacity (large amount of data hiding) due to the shift variance. Shift variance occurs because of down sampling for each level filtering. Even a small variance makes noticeable changes in the wavelet coefficients. This led to inaccurate reconstruction of cover and watermark images.

RDWT is known and implemented by many names like aa trous algorithm, discrete wavelet frames, overcomplete DWT, undecimated DWT, and shift invariant DWT [20]. First time, the implementation of RDWT was done by the aa trous algorithm. It basically removes the down sampling operator from the normal implementation of DWT [20]. To keep the spatial location intact in each sub-band, each band must be of same size as of original image. On the contrary, the size of each level band decreases as the number of level increases in DWT. So, the RDWT kept the same size on each level band and provides more accurate local texture representation [21]. It increases the capacity of RDWT. Then again, any change in RDWT (due to watermark insertion) leads to loss of complete host image because of the band's high correlation (dependence) on each other [14]. In order to get a trade off in this problem (capacity vs. data recovery), DWT is used in proposed work with 2-level of transform.

#### 3.3 Ensuring the False Positive Free Nature of Scheme

The problem of false positive error comes into picture because of complete dependence of extracted watermark on the singular vectors matrices (U and V), which are supplied by the owner. A supply of false/changed matrices (U and V) during watermark extraction process led to false/wrong watermark extraction. This dependence need to be removed from the watermarking scheme in order to provide rightful ownership check. Run et al. [22] suggest that one should embed the

principal components (PC) of watermark into the host image instead of singular values. The PC values can be obtained by multiplying the singular values to the left singular matrix. The proposed scheme is also embedding the principal components of watermark into the singular values of host image to get rid of false positive error.

#### 4 Watermarking Scheme

The watermarking scheme is divided into three stages: Embedding process, Extraction process, and optimization of scaling factors.

#### 4.1 Embedding Process

The block diagram of proposed scheme is shown in Fig. 1 and it contains following steps:

- (1) Perform DWT (2-level) on the host image (H) and obtain (2-level) four bands  $I_i$  (i = LL, HL, LH and HH) of transformed host image.
- (2) Perform singular value decomposition of these bands using Eq. 3. Here *i* = LL, HL, LH, HH.

$$I_i = U_i S_i V_i^T \tag{3}$$

- (3) Perform DWT (1-level) on the watermark image and obtain four bands  $W_i$  (*i* = LL, HL, LH and HH) of watermark (1-level).
- (4) Perform singular value decomposition of the watermark image using Eq. 4 and compute principal components (PC's) using Eq. 5. Here i = LL, HL, LH, HH.



Fig. 1 Block diagram of embedding process

$$W_i = U_{wi} S_{wi} V_{wi}^T \tag{4}$$

$$PC_i = U_{wi}S_{wi} \tag{5}$$

(5) Modify the singular values of host image (each band) with the scaled principal components of watermark (each band) using Eq. 6.

$$S_i' = S_i + \alpha_i P C_i \tag{6}$$

where  $\alpha$  is the scaling factor and PC is the principal components.

(6) Use matrix  $S'_i$  along with  $U_i$  and  $V_i$  to create the watermarked sub bands  $I_{wi}$  for each band as shown in the Eq. 7.

$$I_{wi} = U_i S'_i V_i^T \tag{7}$$

(7) Perform inverse DWT on  $I_{wi}$  to generate watermarked Image  $H_w$ .

## 4.2 Extraction Process

The attacked watermarked image is represented by  $H_w^*$ . For proper extraction of watermark, we need original host image. Firstly, DWT is performed on the watermarked image to obtain  $I_{wi}^*$ . The extraction process is performed as shown in Fig. 2 and described in following steps:

- (1) Perform DWT (1-level) on the original host image and watermarked image to obtain transformed  $I_i$  and  $I_{wi}^*$  respectively.
- (2) Perform subtraction of watermarked bands from the original host bands to obtain  $P_i$  using Eq. 8. Here i = LL, HL, LH, HH.



Fig. 2 Block diagram of extraction process

PSO Optimized and Secured Watermarking Scheme ...

$$X_i = I_{wi}^* - I_i \tag{8}$$

(3) Calculate probably corrupted principal components  $PC_i^*$  using Eq. 9.

$$PC_i^* = U_i^T X_i V_i / \alpha_i \tag{9}$$

(4) Use  $PC_i^*$  along with user's supplied matrix  $V_{wi}^T$  to regenerate watermark image (wavelet domain) with the help of Eq. 10. Here i = LL, HL, LH, HH.

$$W_i^* = PC_i^* V_{wi}^T \tag{10}$$

(5) Perform Inverse DWT to regenerate time domain watermark image W.

## 4.3 Optimization of Scaling Factors Using PSO

It is quite visible from the embedding and extraction process that the quality of formed watermarked image and extracted watermark greatly depends on the scaling factor  $\alpha$ . A low value of scaling factor degrades the robustness of watermark where a high value minimizes the imperceptibility so there is a need to choose an optimal value of scaling factor, which provides a balance between imperceptibility and robustness. These two factors are defined below:

Imperceptibility = correlation
$$(I, I_w)$$
 (11)

$$Robustness = correlation(W, W^*)$$
(12)

Here *I* is host image,  $I_w$  is watermarked image, *W* is original watermark, and *W*\* is extracted watermark. Suppose that *N* type of attacks has been considered then the robustness will become

Inverse Robustness = 
$$\frac{N}{\sum_{i=1}^{N} \text{correlation}(W, W_i^*)}$$
 (13)

As the objective is to maximize both imperceptibility and robustness, the following objective function has been created for minimization:

$$\operatorname{Error} = \frac{N}{\sum_{i=1}^{N} \operatorname{correlation}(W, W_i^*)} - \operatorname{correlation}(A, A_w)$$
(14)

The error function will become a multidimensional search, which cannot be visualized graphically and needs special tool like PSO for optimal value search of scaling factors  $[\alpha]$ .



Fig. 3 Block diagram of scaling factor optimization

A bounded initialization of population size of 50 has been done in the range of 0.001–0.8. 200 generations have been used in the PSO optimization. The value of PSO's step size with other parameters has been kept low (w = 0.1, c1 = 0.8, c2 = 0.12) through out the search in order to get better local search as the single optimal value of  $\alpha$  was known beforehand. The block diagram of optimization process is shown in Fig. 3.

## 5 Results and Discussions

Three host images (Lena, Man and Baboon) are used in this study as shown in Fig. 4. All the hosts are of size  $512 \times 512$ . The DWT provides the half size of all the bands as that of the size of time domain host image. This makes the capacity of



Fig. 4 Host images and watermark: Lena, Man, Baboon, and Watermark logo (left to right)

DWT-based watermarking scheme half as compared to the size of host image. So the watermark is also taken as half size of host image, i.e.,  $256 \times 256$  and the same is shown in Fig. 4. PSNR (Peak signal to noise ratio) is used to show the similarity between host images and watermarked images. Normal cross-correlation is used to compare the similarity of extracted watermarks with original watermark. Suppose that the size of two images *X* and *X*\* is  $n \times n$  and they can attain a maximum pixel value as  $X_{\text{max}}$ . Then PSNR and normalized cross-correlation can be defined as:

$$PSNR = 10 \log_{10} \left( \frac{n \times n \times (X_{\max})^2}{\sum_{i=1}^n \sum_{i=1}^n (X(i,j) - X^*(i,j))^2} \right)$$
(15)

$$\operatorname{correlation}(X, X^*) = \frac{\sum_{i=1}^{n} \sum_{j=1}^{n} \overline{X_{(i,j)} \operatorname{XOR} X^*_{(i,j)}}}{n \times n}$$
(16)

## 5.1 Imperceptibility and Robustness of Scheme

The quality of watermarked image (Imperceptibility) and extracted watermark (Robustness) with different scaling factors is shown in this section. Table 1 is showing the PSNR of watermarked images with different scaling factors. Table 2 is showing the normalized cross-correlation of watermarked host (Host (W)) and extracted watermark with respect to original host and original watermark, respectively.

Table 1 Variation of PSNR   of watermarked images with scaling factors	Host image	PSNR (dB)		
		$\alpha = 0.01$	$\alpha = 0.05$	$\alpha = 0.25$
	Lena	38.5334	32.6533	24.4235
	Man	37.6545	31.7243	23.7534
	Baboon	37.5343	31.2476	23.5464

Host image	NCC (normalized cross co-relation)					
	$\alpha = 0.01$		$\alpha = 0.05$		$\alpha = 0.25$	
	Host (W)	Watermark	Host (W)	Watermark	Host (W)	Watermark
Lena	0.9754	0.8743	0.9264	0.9634	0.7943	0.9934
Man	0.9643	0.8856	0.9153	0.9554	0.7865	0.9832
Baboon	0.9676	0.8875	0.9132	0.9564	0.7912	0.9859

Table 2 Variation of NCC of watermarked image and extracted watermark with scaling factors

## 5.2 Optimization of Scaling Factors

As we can see from the Tables 1 and 2 that the imperceptibility and robustness are dependent on scaling factor and are inversely proportional to each other. So, PSO-optimized multiple scaling factors are used to find an optimal trade off between them; as explained in Sect. 4.3. Figure 5 is showing the watermarked images and Table 3 is showing the imperceptibility and robustness (without any attack) of proposed scheme after the scaling factor optimization.

Table 4 is showing the proposed watermarking scheme's performance under different attacks for three host images.



Fig. 5 Watermarked images: Lena, Man, and Baboon (left to right)

Table 3	Imperceptibility	and robustness	(without any	attack) o	f proposed	scheme a	fter the	scaling
factor op	timization							

Host image	PSNR of watermarked image	NCC of extracted watermark
Lena	34.3563	0.9942
Man	33.5346	0.9874
Baboon	33.6455	0.9894

Attack	NCC of extracted watermarks		
	Lena	Man	Baboon
Average filtering $(3 \times 3)$	0.9454	0.9353	0.9376
Rescaling $(512 \rightarrow 256 \rightarrow 512)$	0.9778	0.9664	0.9687
Gamma correction (0.8)	0.9675	0.9535	0.9543
Median filtering $(3 \times 3)$	0.9784	0.9687	0.9676
Histogram equalization	0.9687	0.9554	0.9576
Gaussian noise (mean = $0$ , variance = $0.01$ )	0.8875	0.8754	0.8754
JPEG compression (QF = $50$ )	0.9885	0.9776	0.9787
Gaussian low-pass filter	0.9902	0.9812	0.9814
Sharpening	0.9054	0.8954	0.8976
Contrast adjustment 20 %	0.9243	0.9165	0.9198

Table 4 NCC of extracted watermarks under different attacks with respect to original watermark

## 5.3 Applicability of Scheme to Color Images

The proposed scheme is not directly applicable to the color images as the color images contain three channels contrary to single channel of gray host. Figure 6 is showing the color host images used in this study.

The color host is first divided into the RGB (Red-green-blue) channels and then one/multiple channels are selected for watermark embedding. In case of multiple channels, same watermark is embedded in all the channels. PSO-optimized multiple scaling factors are utilized in this embedding. The imperceptibility is shown in Table 5 and robustness of scheme toward different signal processing attacks is shown in Table 6 for host "RGB-Lena." The scheme performs quite similar with the host "RGB-Baboon" also.



Fig. 6 Color host images: RGB-Lena and RGB-Baboon (left to right)

Image name	PSNR (dB)				
	Red channel	Green channel	Blue channel	All channel	
RGB-Lena	48.4256	47.9739	48.5734	34.4795	
RGB-Baboon	48.5457	47.9374	48.6385	34.5645	

Table 5 Imperceptibility of color hosts during single and multiple channel embedding

Table 6 Robustness of scheme toward different signal processing attacks for host "RGB-Lena"

Attack	NCC of extracted watermarks			
	Red	Green	Blue	All
	channel	channel	channel	channel
Average filtering $(3 \times 3)$	0.9636	0.9665	0.9644	0.9464
Rescaling $(512 \rightarrow 256 \rightarrow 512)$	0.9869	0.9843	0.9875	0.9763
Gamma correction (0.8)	0.9765	0.9753	0.9743	0.9664
Median filtering $(3 \times 3)$	0.9868	0.9832	0.9886	0.9786
Histogram equalization	0.9822	0.9853	0.9876	0.9665
Gaussian noise (mean $= 0$ ,	0.9476	0.9432	0.9476	0.8876
variance = 0.01)				
JPEG compression ( $QF = 50$ )	0.9953	0.9965	0.9987	0.9875
Gaussian low-pass filter	0.9982	0.9978	0.9975	0.9963
Sharpening	0.9554	0.9576	0.9575	0.9065
Contrast adjustment 20 %	0.9443	0.9473	0.9487	0.9274

# 6 Conclusion

This work utilized embedding to principal components of watermark in the singular values of host to make the watermarking free from false positive error. The watermarking was done in the domain of DWT, so proposed scheme provided decent data embedding. The robustness and imperceptibility of scheme was improved by making use of PSO-optimized multiple scaling factors instead of single scaling factor. After a bit modification in the scheme, it worked almost similar with the color hosts also. In future, more variants of PSO and other soft computing techniques [23–27] will be applied to proposed scheme in order to improve the scheme's performance.

Acknowledgments This work was supported by Ministry of Human Resource Development, India.

## References

- 1. Haouzia, A., Noumeir, R.: Methods for image authentication: a survey. Multimedia Tools Appl. **39**(1), 1–46 (2008)
- Ansari, I.A., Pant, M.: SVD Watermarking: particle swarm optimization of scaling factors to increase the quality of watermark. In: Proceedings of Fourth International Conference on Soft Computing for Problem Solving, pp. 205–214. Springer, India (2015)
- 3. Potdar, V.M., Han, S., Chang, E.: A survey of digital image watermarking techniques. In: 3rd IEEE International Conference on Industrial Informatics INDIN'05, pp. 709–716 (2005)
- Lin, S., Chen, C.F.: A robust DCT based watermarking for copyright protection. IEEE Trans. Consum. Electron. 46(3), 415–421 (2000)
- Ansari, I.A., Pant, A., Ahn, C.W.: Robust and false positive free watermarking in IWT domain using SVD and ABC. Eng. Appl. Artif. Intell. 49, 114-125 (2016)
- Ansari, I.A., Pant, A., Ahn, C.W.: SVD based fragile watermarking scheme for tamper localization and self-recovery. Int. J. Mach. Learn. & Cyber. 1–15 (2015), doi:10.1007/ s13042-015-0455-1
- Ansari, I.A, Pant, M., Neri, F.: Analysis of gray scale watermark in RGB host using SVD and PSO. In: IEEE Computational Intelligence for Multimedia, Signal and Vision Processing (CIMSIVP), pp. 1–7 (2014)
- Ganic, E., Eskicioglu, A.M.: Robust embedding of visual watermarks using discrete wavelet transform and singular value decomposition. J. Electron. Imaging 14(4), 043004–043009 (2005)
- Rastegar, S., Namazi, F., Yaghmaie, K., Aliabadian, A.: Hybrid watermarking algorithm based on singular value decomposition and radon transform. Int. J. Electron. Commun. (AEU) 65(7), 658–663 (2011)
- Lagzian, S., Soryani, M., Fathy, M.: A new robust watermarking scheme based on RDWT– SVD. IJIIP Int. J. Intell. Inform. Process. 2(1), 22–29 (2011)
- Guo, J.M., Prasetyo, H.: Security analyses of the watermarking scheme based on redundant discrete wavelet transform and singular value decomposition. AEU-Int. J. Electron. Commun. 68(9), 816–834 (2014)
- 12. Lai, C.C., Tsai, C.C.: Digital image watermarking using discrete wavelet transform and singular value decomposition. IEEE Trans. Instrum. Meas. **59**(11), 3060–3063 (2010)
- Makbol, N.M., Khoo, B.E.: Robust blind image watermarking scheme based on redundant discrete wavelet transform and singular value decomposition. AEU-Int. J. Electron. Commun. 67(2), 102–112 (2013)
- Ling, H.-C., Phan, R.C.-W., Heng, S.H.: Comment on robust blind image watermarking scheme based on redundant discrete wavelet transform and singular value decomposition. AEU-Int. J. Electron. Commun. 67(10), 894–897 (2013)
- Ansari, I.A., Singla, R., Singh, M.: SSVEP and ANN based optimal speller design for brain computer interface. Comput. Sci. Tech. 2(2), 338–349 (2015)
- Kant, S., Ansari, I. A.: An improved K means clustering with Atkinson index to classify liver patient dataset. Int. J. Syst. Assur. Eng. Manage. 1–7 (2015). doi:10.1007/s13198-015-0365-3
- Eberhart, R.C., Kennedy, J.: A new optimizer using particle swarm theory. In: Proceedings of the sixth international symposium on micro machine and human science, vol. 1, pp. 39–43 (1995)
- Kiranyaz, S., Ince, T., Yildirim, A., Gabbouj, M.: Fractional particle swarm optimization in multidimensional search space. IEEE Trans. Syst. Man Cybern. B Cybern. 40(2), 298–319 (2010)
- Messerschmidt, L., Engelbrecht, A.P.: Learning to play games using a PSO-based competitive learning approach. IEEE Trans. Evol. Comput. 8(3), 280–288 (2004)
- Fowler, J.: The redundant discrete wavelet transform and additive noise. IEEE Signal Process. Lett. 12(9), 629–632 (2005)

- Cui, S., Wang, Y.: Redundant wavelet transform in video signal processing. In: International conference on image processing, computer vision, pattern recognition, pp. 191–196 (2006)
- Run, R.-S., Horng, S.-J., Lai, J.-L., Kao, T.-W., Chen, R.-J.: An improved SVD- based watermarking technique for copyright protection. Expert Syst. Appl. 39(1), 673–689 (2012)
- 23. Jalhar, S.K., Pant, M., Nagar, M.C.: Differential evolution for sustainable supplier selection in pulp and paper industry: a DEA based approach. Comput. Methods Mater. Sci. **15** (2015)
- Zaheer, H., Pant, M.: A differential evolution approach for solving integer programming problems. In: Proceedings of Fourth International Conference on Soft Computing for Problem Solving, pp. 413–424. Springer, India (2015)
- 25. Jauhar, S.K., Pant, M., Abraham, A.: A novel approach for sustainable supplier selection using differential evolution: a case on pulp and paper industry. In: Intelligent Data analysis and its Applications, vol. II, pp. 105–117. Springer International Publishing (2014)
- Zaheer, H., Pant, M., Kumar, S., Monakhov, O., Monakhova, E., Deep, K.: A new guiding force strategy for differential evolution. Int. J. Syst. Assur. Eng. Manag. 1–14 (2015), doi:10. 1007/s13198-014-0322-6
- Jauhar, S.K., Pant, M.: Genetic algorithms, a nature-inspired tool: review of applications in supply chain management. In: Proceedings of Fourth International Conference on Soft Computing for Problem Solving, pp. 71–86. Springer, India (2015)