

Transport Phenomena in Engineering Problems: CFD-Based Computational Modeling

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Abstract Computational Fluid Dynamics is a popular modeling approach which utilizes numerical methods and computer simulations to solve and analyze problems that involve transport phenomena in fluid flows. CFD-based models demonstrate high versatility and capability of dealing with a wide range of engineering problems. This chapter presents two examples of CFD-based computational modeling successfully applied for different fields of engineering: particle engineering by drying processes and thermal management.

Keywords Computational fluid dynamics · Design · Modeling · Numerical simulations · Particle engineering · Thermal management · Transport phenomena

1 Introduction

Many contemporary engineering problems involve flows of liquid and/or gas, transport of heat by conduction, convection and radiation mechanisms, mass transfer by diffusion and convection, flows of bubbles, drops or particles, combustion etc. These complex problems require fundamental understanding that cannot be provided only by available experimental techniques, and therefore theoretical and numerical modeling are essential.

Recent progress in computer industry stimulated fast development of computational approaches, among them Computational Fluid Dynamics (CFD). This is a wide spread modeling approach which utilizes numerical methods and computer simulations to solve and analyze problems that involve transport phenomena in fluid flows. Lots of commercial and open computer codes are implementing CFD tech-

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nique: ANSYS FLUENT, ANSYS CFX, FLOW-3D, STAR-CD, COMSOL CFD, OpenFOAM, OpenFVM and many others.

This book chapter presents two examples of CFD-based computational modeling successfully applied for different fields of engineering: particle engineering by drying processes and thermal management of a car compartment. In spite of apparent differences, these two models have common roots in description of transport phenomena of the fluid phase.

2 Particle Engineering by Drying Processes

2.1 *Spray Drying*

Spray drying is a widely applied technology utilized to transform solutions, emulsions or suspensions into dry granules, and particle agglomerates, by feeding the liquid mixture as a spray of droplets into a medium with a hot drying agent. Because spray drying can be used either as a preservation method or simply as a fast drying technique, this process is utilized in many industries, such as food manufactures, pharmaceutical, chemical and biochemical industries. Spray drying is a rapid process (up to several seconds) compared to other methods of drying (e.g., pulse combustion drying, drum drying, freeze drying) due to the small spray droplet sizes and their large specific surface areas that maximize rates of heat and mass transfer. Therefore, this technique is the preferred drying method for many thermally-sensitive materials. Spray drying also turns a raw material into a dried powder in a single step, which can be advantageous for profit maximization and process simplification. Along with other drying techniques, spray drying also provides the advantage of weight and volume reduction. Dyestuffs, paint pigments, plastics, resins, catalysts, ceramic materials, washing powders, pesticides, fertilizers, organic and inorganic chemicals, skim and whole milk, baby foods, instant coffee and tea, dried fruits, juices, eggs, spices, cereal, enzymes, vitamins, flavors, antibiotics, medical ingredients, additives, animal feeds, biomass—this list of the spray-dried products is far from being complete.

A typical spray drying tower includes an atomizer, which transforms the supplied liquid feed into a spray of droplets, and a contact mixing zone, where the spray interacts with a hot drying agent. As a result of this interaction, the moisture content of the drying agent increases due to liquid evaporation from the droplets. In turn, due to evaporation, the spray droplets shrink and turn into solid particles. The drying process proceeds until the dried particles with the desired moisture content are obtained and then the final product is recovered from the drying chamber. Depending on the production requirements, droplet sizes from 1 to 1000 μm can be achieved using either nozzle or rotating disk atomizers; for the most common applications, average spray droplet diameters are between 100 and 200 μm . Air under atmospheric pressure, steam and inert gases like nitrogen are popular drying agents used nowadays. It is

noted that inert gases are applied for drying of flammable, toxic or oxide-sensitive materials.

2.2 Pneumatic Drying

Pneumatic (flash) drying is another example of extensively used technology in food, chemical, agricultural and pharmaceutical industries. The main advantages of this process are fast elimination of free moisture from pre-prepared feed of wet particles and operation in continuous mode. Typically, the feed is introduced into the drying column by a screw via a Venturi pipe. The particles dry out in seconds as they are conveyed by hot gas (air) stream. Then, the product is separated using cyclones which are usually followed by scrubbers or bag filters for final cleaning of the exhaust gases. In spite of its apparent simplicity, the process of pneumatic drying is a complex multi-scale multi-phase transport phenomenon involving turbulent mixing of humid gas and multi-component wet particles, heat and mass transfer interaction between the drying gas and dispersed phase, and internal heat and moisture transport within each conveyed wet particle.

3 Thermal Management of Car Compartment

One of the most energy-expensive units in contemporary vehicles is the air conditioning system (ACS). On an average, such systems consume up to 17 % of the overall power produced by vehicle engines of the world, depending on the cooling regime and environment thermal load [1]. It is remarkable that air-conditioning units in cars and light commercial vehicles burn more than 5 % of the vehicle fuel consumed annually throughout the European Union [2]. For instance, the United Kingdom emits about 3 million tons of CO₂ each year simply from powering the air-conditioning systems in vehicles. In South European and Mediterranean countries the problem of air pollution increase by ACS powering is even more acute.

Extensive theoretical and experimental studies have been performed throughout the recent years, aimed to reduce the fuel consumption and environmental pollution due to vehicle air conditioning. Proper thermal management based on the gas dynamics inside the vehicle passenger compartment is crucial for air conditioning and heating systems performance as well as for the comfort of passengers. On the other hand, the nature of the flow, namely the velocity field in combination with the temperature distribution, has a strong influence on the human sensation of thermal comfort [3].

In the present research it is proposed to develop a three-dimensional theoretical model of transport phenomena in car compartment. This model is based on Eulerian approach for the gas flow and takes into account thermal energy transfer by simultaneous conduction, convection and radiation mechanisms within the compartment

as well as outside the vehicle. The model is able to predict steady-state and transient profiles of air velocity, density, pressure, temperature and humidity for various regimes of the air conditioning, vehicle driving modes, compartment configurations and ambient conditions.

To assess the passenger level of thermal comfort, a methodology based on published studies [4, 5] may be developed and the corresponding equations may be coupled to the developed computational model. Moreover, the effect of the passengers themselves on their thermal comfort (e.g., heat emission by human body, air inhalation and gas mixture exhalation etc.) might be considered.

The CFD-based model of thermal management can be utilized as a tool for the following parametric investigations: enhancement of natural convection within a compartment, influence of thermal insulation and trim materials on the passenger thermal comfort as well as effect of introduction of innovating passive cooling techniques on energy consumption by ACS.

4 Theoretical Modeling

4.1 Spray and Pneumatic Drying

Transport phenomena in drying processes is subdivided into *external* (gas-particles mixing) and *internal* (within dispersed droplets/particles).

The fluid dynamics of continuous phase of drying gas is treated by an Eulerian approach and a standard k- ϵ model is utilized for turbulence description. The utilized three-dimensional conservation equations of continuity, momentum, energy, species, turbulent kinetic energy and dissipation rate of turbulence kinetic energy are as follows ($i, j = 1, 2, 3$):

– continuity

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_j} (\rho u_j) = S_c, \quad (1)$$

where ρ and u are drying gas density and velocity, and S_c is mass source term.

– momentum conservation

$$\begin{aligned} \frac{\partial}{\partial t} (\rho u_i) + \frac{\partial}{\partial x_j} (\rho u_i u_j) = & -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[\mu_e \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right] \\ & + \Delta \rho g_i + U_{pi} S_c + \sum F_{gp}, \end{aligned} \quad (2)$$

where p and μ_e are drying gas pressure and effective viscosity, U_p is particle velocity and $\sum F_{gp}$ is sum of the forces exerted by particles on the gas phase.

– energy conservation

$$\frac{\partial}{\partial t} (\rho h) + \frac{\partial}{\partial x_j} (\rho u_j h) = \frac{\partial}{\partial x_j} \left(\frac{\mu_e}{\sigma_h} \frac{\partial h}{\partial x_j} \right) - q_r + S_h, \quad (3)$$

where h is specific enthalpy, q_r and S_h are thermal radiation and energy source terms, respectively.

– species conservation

$$\frac{\partial}{\partial t} (\rho Y_v) + \frac{\partial}{\partial x_j} (\rho u_j Y_v) = \frac{\partial}{\partial x_j} \left(\frac{\mu_e}{\sigma_Y} \frac{\partial Y_v}{\partial x_j} \right) + S_c, \quad (4)$$

where Y_v is mass fraction of vapour in humid gas.

– turbulence kinetic energy

$$\frac{\partial}{\partial t} (\rho k) + \frac{\partial}{\partial x_j} (\rho u_j k) = \frac{\partial}{\partial x_j} \left(\frac{\mu_e}{\sigma_k} \frac{\partial k}{\partial x_j} \right) + G_k + G_b - \rho \varepsilon, \quad (5)$$

where k is turbulent kinetic energy and ε is dissipation rate of turbulent kinetic energy.

– dissipation rate of turbulence kinetic energy

$$\frac{\partial}{\partial t} (\rho \varepsilon) + \frac{\partial}{\partial x_j} (\rho u_j \varepsilon) = \frac{\partial}{\partial x_j} \left(\frac{\mu_e}{\sigma_\varepsilon} \frac{\partial \varepsilon}{\partial x_j} \right) + \frac{\varepsilon}{k} (C_1 G_k - C_2 \rho \varepsilon). \quad (6)$$

The production of turbulence kinetic energy due to mean velocity gradients is equal to:

$$G_k = \mu_T \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \frac{\partial u_i}{\partial x_j}. \quad (7)$$

The production of turbulence kinetic energy due to buoyancy is given by:

$$G_b = -\beta g_j \frac{\mu_T}{\sigma_T} \frac{\partial T}{\partial x_j}, \quad (8)$$

where T is gas temperature and β is coefficient of gas thermal expansion:

$$\beta = -\frac{1}{\rho} \left(\frac{\partial \rho}{\partial T} \right)_p. \quad (9)$$

The utilized constants are $C_1 = 1.44$, $C_2 = 1.92$, and the Prandtl numbers are equal to $\sigma_k = \sigma_h = \sigma_Y = \sigma_T = 0.9$ and $\sigma_\varepsilon = 1.3$. The effective viscosity, μ_e , is defined as:

$$\mu_e = \mu + \mu_T, \quad (10)$$

where μ_T is turbulent viscosity

$$\mu_T = C_\mu \rho \frac{k^2}{\varepsilon}. \quad (11)$$

In the above expression $C_\mu = 0.09$.

The constitutive relationship between air temperature, pressure and density is given by the ideal gas law (such model is sufficient because of small humidity of the gas involved in the considered multiphase flow):

$$p = \frac{\rho}{M} \Re T, \quad (12)$$

where \Re is universal gas constant and M is molecular weight of the gas phase.

To track the trajectories and other valuable parameters of spray of droplets and particles, a Discrete Phase Model (DPM) based on Lagrangian formulation is utilized. The motion of the droplets/particles is described by Newton's Second Law:

$$\frac{d\vec{U}_p}{dt} = \vec{g} + \frac{\sum \vec{F}_p}{m_p}. \quad (13)$$

Here $\sum \vec{F}_p$ is sum of the forces exerted on given spray droplet/particle by the gas phase, by other particles and walls of the spray drying chamber; \vec{g} is gravity acceleration, and \vec{U}_p and m_p are droplet/particle velocity and mass, respectively. In general, the acting forces on spray droplet/particle are as follows:

$$\sum \vec{F}_p = \vec{F}_D + \vec{F}_B + \vec{F}_A + \vec{F}_{PG} + \vec{F}_C + \vec{F}_{other}, \quad (14)$$

where \vec{F}_D is drag force, \vec{F}_B is buoyancy force, \vec{F}_A is added mass force, \vec{F}_{PG} is pressure gradient force and \vec{F}_C is contact force (neglected in the present work). The term \vec{F}_{other} represents other forces, usually important for submicron particles and/or at specific conditions, e.g., phoretic, Basset, Saffman, Magnus forces etc., and neglected in the present work for simplicity.

The drag force is determined by the expression:

$$\vec{F}_D = \frac{\pi d_p^2}{8} \rho C_D \left| \vec{u} - \vec{U}_p \right| \left(\vec{u} - \vec{U}_p \right), \quad (15)$$

where d_p is droplet/particle diameter and \vec{u} is velocity of gas phase. The drag coefficient, C_D , is calculated according to well-known empirical correlations for spherical particles.

The buoyancy force opposes gravity and in the present study it is much smaller than the latter, because the densities of spray droplets and drying gas differ more than thousand times. For this reason the buoyancy of droplets/particles is currently neglected.

The added mass (“virtual-mass”) force, required to accelerate the gas surrounding the droplet/particle, is given by:

$$\vec{F}_A = \rho \frac{\pi d_p^3}{12} \frac{d}{dt} (\vec{u} - \vec{U}_p). \quad (16)$$

For flow in dryers, this force may be important in the droplets/particles entrance region, where the velocities of injected dispersed phase and drying gas are substantially different and their intensive mixing leads to high change rates of the relative velocities.

The pressure gradient in the gas phase additionally accelerates droplets/particles and results in the following force:

$$\vec{F}_{GP} = -\frac{\pi d_p^3}{6} \vec{\nabla} p. \quad (17)$$

This force can be essential and worth consideration in the dryer regions with fast pressure changes like inlet, outlet and swirling zones of the gas phase.

In the present work the *internal transport phenomena* within each droplet/particle are described with the help of previously developed and validated two-stage drying kinetics model, see [6]. The drying process of droplet containing solids is divided in two drying stages. In the first stage of drying, an excess of moisture forms a liquid envelope around the droplet solid fraction, and unhindered drying similar to pure liquid droplet evaporation results in the shrinkage of the droplet diameter. At a certain moment, the moisture excess is completely evaporated, droplet turns into a wet particle and the second stage of a hindered drying begins. In this second drying stage, two regions of the wet particle can be identified: layer of dry porous crust and internal wet core. The drying rate is controlled by the rate of moisture diffusion from the particle wet core through the crust pores towards the particle outer surface. As a result of the hindered drying, the particle wet core shrinks and the thickness of the crust region increases. The particle outer diameter is assumed to remain unchanged during the second drying stage. After the point when the particle moisture content decreases to a minimal possible value (determined either as an equilibrium moisture content or as a bounded moisture that cannot be removed by drying), the particle is treated as a dry non-evaporating solid sphere. It is worth noting that all droplets and particles are assumed to be spherical and a full radial symmetry of inter-droplet physical parameters (temperature, moisture content etc.) is believed. The concept of two-stage droplet drying kinetics is illustrated by Fig. 1.

4.2 Thermal Management of Car Compartment

The conservation equations of the above 3D model of transport phenomena in particle engineering processes can also be applied to describe the gas flow and heat

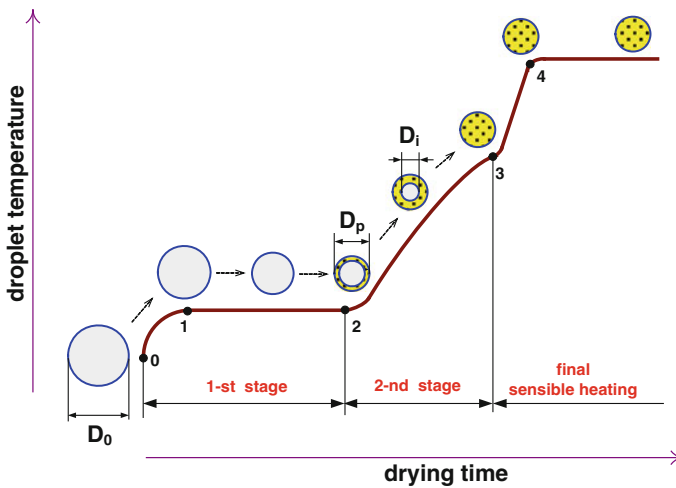


Fig. 1 The concept of two-stage droplet drying kinetics

and mass transfer within a car passenger compartment and in its surroundings. Particularly, in the present study 3D compressible Reynolds Averaged Navier-Stokes (RANS) equations including k - ε turbulence formulation (1–12) are utilized to predict flow patterns of the gas mixture (air, vapor, carbon dioxide) inside a passenger compartment and air flow outside the cabin. These equations are solved by applying a Finite Volumes Method (FVM). The computational model formulated in such way is capable of predicting air velocity, temperature and species flow patterns inside the compartment under different ambient conditions. Moreover, the model can be used to prognosticate energy consumption of ACS that is necessary for providing passengers comfort at given outside thermal load. In addition, numerical simulations with this 3D model may facilitate revealing weak design points and optimization of existing/newly designed car air conditioning systems.

5 Numerical Simulations

5.1 Spray Drying

A cylinder-on-cone spray dryer with co-current flow of drying air and spray of droplets (Fig. 2) is adopted from the literature [6, 7]. Preheated atmospheric air at temperature 468 K and absolute humidity of 0.009 kg H₂O/kg dry air is supplied into the drying chamber through a central round inlet of the flat horizontal ceiling, without swirling and at angle of 35°, with respect to the vertical axis. The air inlet velocity is 9.08 m/s, whereas its turbulence kinetic energy is equal to 0.027 m²/s²

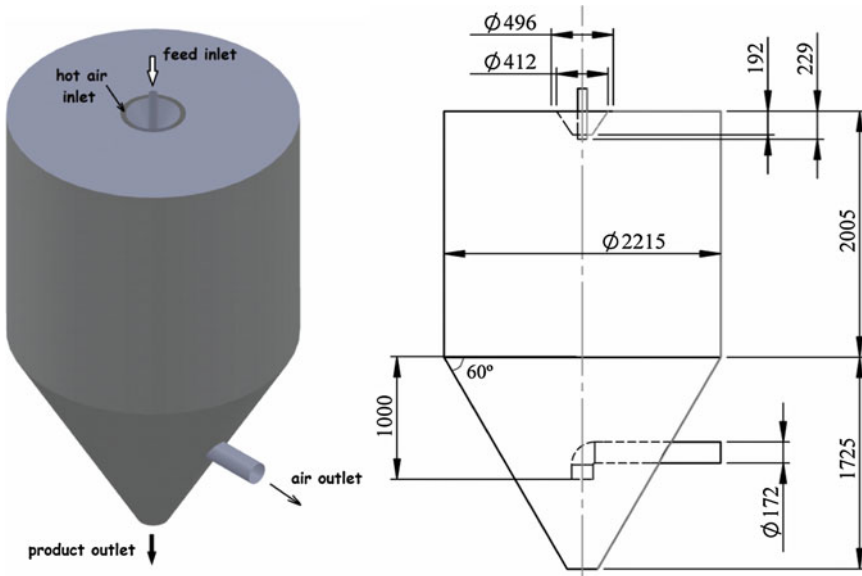


Fig. 2 Sketch of spray drying tower

and turbulence energy dissipation rate is $0.37 \text{ m}^2/\text{s}^3$. The spray of liquid droplets is obtained by atomizing the liquid feed in a pressure nozzle. The spray cone angle is assumed to be 76° , the droplet velocities at the nozzle exit are assigned to 59 m/s , and the temperature of the feed is set at 300 K . The distribution of droplet diameters in the spray is assumed to obey the Rosin-Rammler distribution function, where the mean droplet diameter is assumed to be $70.5 \mu\text{m}$, the spread parameter is set at 2.09 , and the corresponding minimum and maximum droplet diameters are taken as $10.0 \mu\text{m}$ and $138.0 \mu\text{m}$, respectively. The overall spray mass flow rate is equal to 0.0139 kg/s (50 kg/hr). The walls of drying chamber are assumed to be made of 2 mm stainless steel, and the coefficient of heat transfer through the walls is set to zero as though there is a perfect thermal insulation of the chamber. The gage air pressure in the outlet pipe of the drying chamber is set to -100 Pa .

The numerical solution and simulations have been performed by utilizing a 3D pressure-based solver incorporated in CFD package ANSYS FLUENT 13. The solver is based on the finite volumes technique and enables two-way coupled Euler-DPM algorithm for treatment of the continuous and discrete phases. The chamber geometry has been meshed by $619,711$ unstructured grid cells of tetrahedral and polyhedral shape with the various mesh sizes.

The 3D spray from pressure nozzle is modeled by 20 spatial droplet streams. In turn, each droplet stream is represented by 10 injections of different droplet diameters: minimum and maximum diameters are $10.0 \mu\text{m}$ and $138.0 \mu\text{m}$, whereas the intermediate droplet sizes are calculated by applying Rosin-Rammler distribution

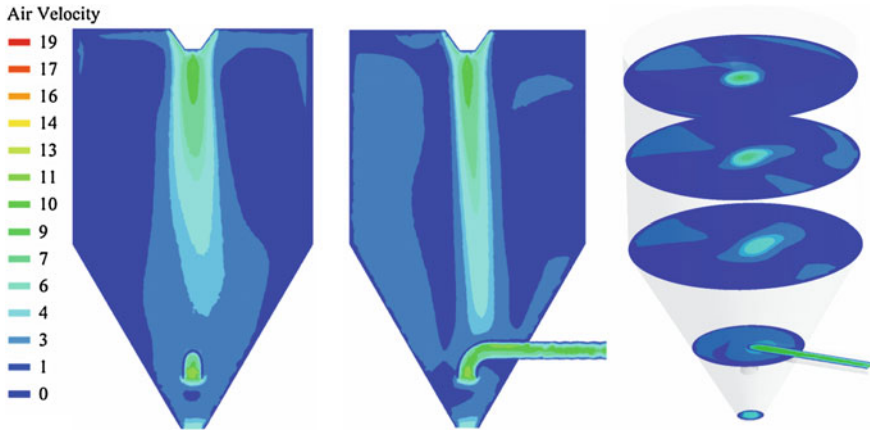


Fig. 3 Flow fields of air velocity (m/s) in spray dryer: frontal (*left*), side (*middle*) and isometric (*right*) cuts

function with $70.5 \mu\text{m}$ of droplet average size. In this way, totally 200 different droplet injections have been introduced into the computational domain.

All the numerical simulations of spray drying process have been performed in steady-state two-way coupling mode of calculations. For continuous phase, the spatial discretization was performed by upwind scheme of second order for all conservation equations (except pressure solved by PRESTO! procedure) and SIMPLE scheme was used for coupling between the pressure and velocity. For the dispersed phase, the tracking scheme was automatically selected between low order implicit and high order trapezoidal schemes based on the solution stability. DPM sources were updated every iteration of the continuous phase. The overall steady-state numerical formulation was of the second order of accuracy.

The computation of internal transport phenomena for the discrete phase was accomplished using the concept of user defined functions (UDF). The numerical solution was implemented as a subroutine and linked to the ANSYS FLUENT solver via a set of the original UDFs. The results of simulations are shown in Figs. 3, 4, and 5.

5.2 Pneumatic Drying

For the purposes of the theoretical study the geometry of Baeyens et al. [8] experimental set-up was adopted. Hot dry air and wet particles are supplied to the bottom of vertical pneumatic dryer with 1.25 m internal diameter and 25 m height (see Fig. 6). The developed theoretical model was numerically solved with the help of Finite Volume Method and 3D simulations of pneumatic drying were performed using the CFD package ANSYS FLUENT. To this end, the 3D numerical grid with 9078 distributed



Fig. 4 Flow patterns of air temperature (Kelvin) in spray dryer: frontal (*left*), side (*middle*) and isometric (*right*) cuts

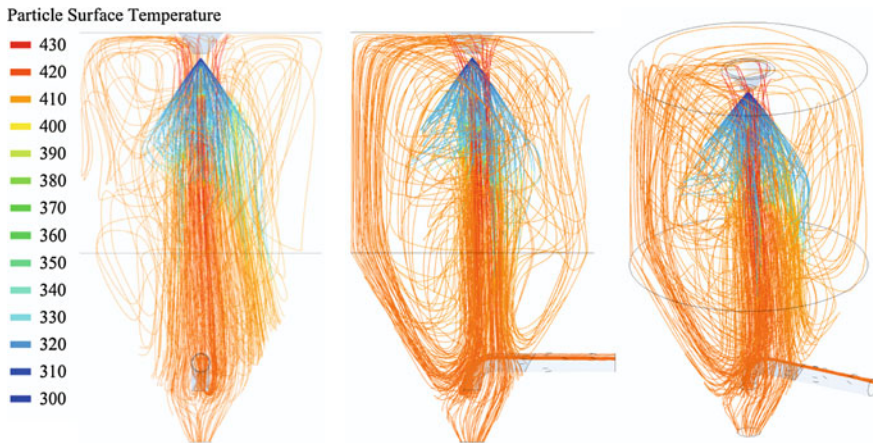


Fig. 5 Particle trajectories in spray dryer colored by particle surface temperature (Kelvin): frontal (*left*), side (*middle*) and isometric (*right*) views

hexahedral/ wedge cell volumes was generated in GAMBIT 2.2.30 using the Cooper scheme.

The flow of wet PVC particles in the pneumatic dryer was simulated through 89 injections of spherical particles. Each injection began on the bottom of the dryer at the centroid of one of the 89 bottom plane mesh elements. The particle injections were normal to the dryer bottom plane and parallel to each other.

The numerical simulations were performed in the following way. First, the flow of drying air was simulated without the discrete phase until converged solution was obtained. At the next step, wet particles were injected into the domain and two-way coupled simulations were performed until convergence.

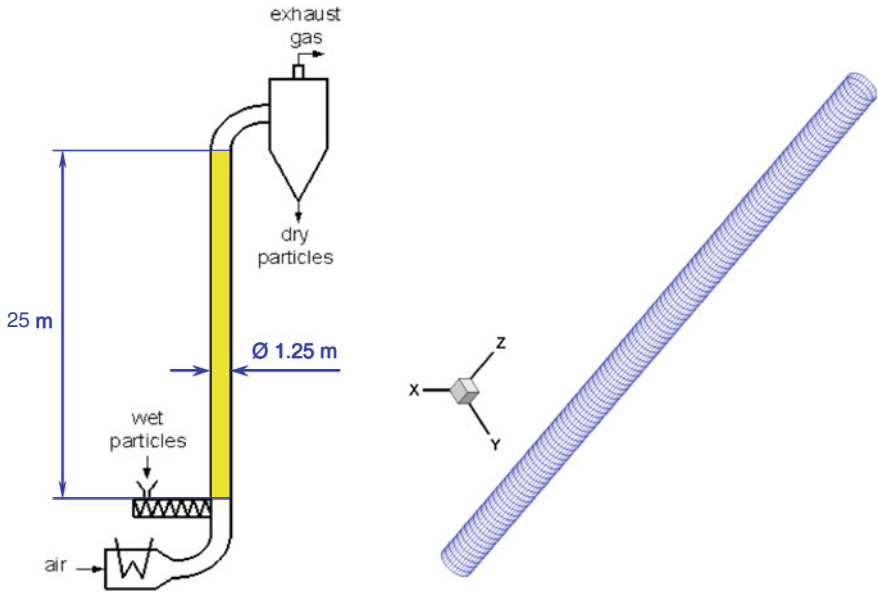


Fig. 6 Schematic sketch of pneumatic dryer [8] (left) and corresponding numerical grid (right)

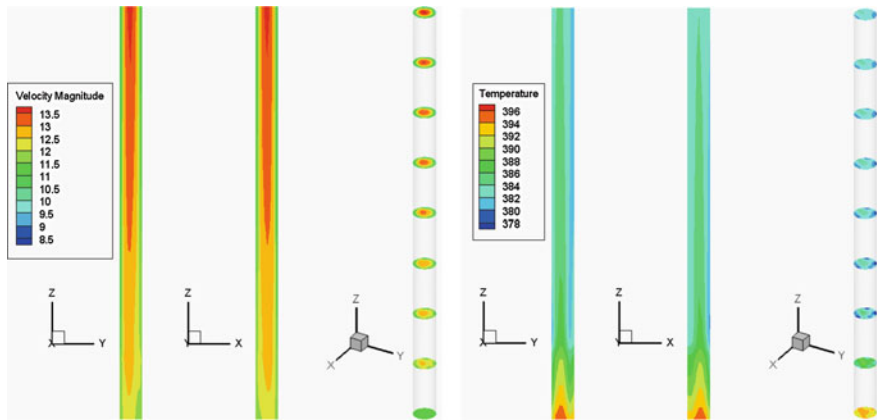


Fig. 7 Calculated flow patterns for drying of PVC wet particles in pneumatic dryer(adiabatic flow). *Left*—air velocity magnitude, m/s, *right*—air temperature, K

The convergence of the numerical simulations was determined by means of residuals of the transport equations. Particularly, the converged values of the scaled residuals were ensured to be lower than 10^{-6} for the energy equation and 10^{-3} for the rest of equations. The convergence was also verified by negligibly small values of the global mass and energy imbalances. The predicted flow patterns are given in Fig. 7.

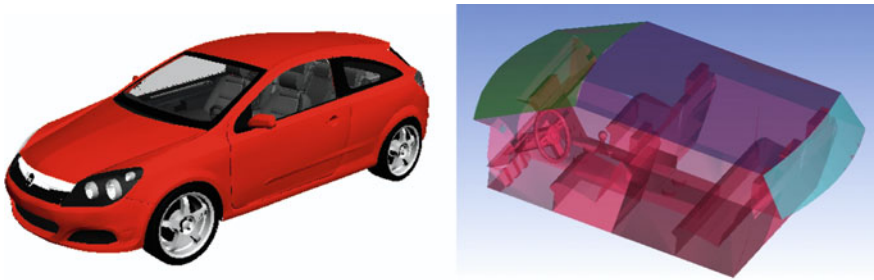


Fig. 8 Car model in 3D Studio Max software (*left*) and extracted compartment geometry (*right*)

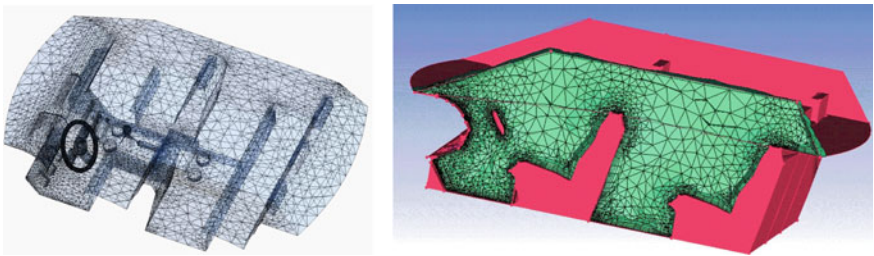


Fig. 9 Numerical grid of car passenger compartment

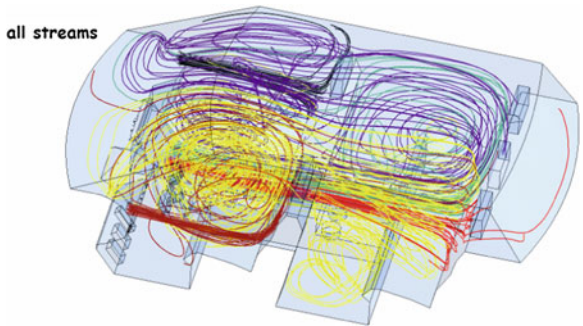


Fig. 10 Calculated streamlines of air velocity in car passenger compartment

5.3 Air Flow Patterns in Car Passenger Compartment

A simplified model of conventional car passenger compartment was adopted for numerical simulations. The original car model was created in 3D Studio Max software, whereas the extracted compartment geometry was processed in ANSYS ICEM CFD program and meshed with 518,705 polyhedral (3–6 faces) grid cells (Figs. 8 and 9). Then, steady state 3D numerical simulations using ANSYS FLUENT code were performed.

Figure 10 demonstrates the results of numerical simulations of air flow patterns in the compartment. Four air inlets with velocity 1 m/s and temperature 12 °C and two air outlets with -150 Pa gage pressure were established. The ambient temperature was taken 37 °C and heat transfer coefficient was set to $10 \text{ W}/(\text{m}^2 \cdot \text{K})$, assuming parked car.

6 Conclusion

The computational CFD-based modeling is a powerful tool for description, simulation and analysis of variety of engineering problems involving macroscopic transport phenomena (fluid/gas dynamics, turbulence, heat transfer and mass transfer). CFD-based models demonstrate high versatility and capability of dealing with a wide range of engineering problems. Basic knowledge in CFD-based modeling and ability to work with CFD software are becoming to be necessary skills for contemporary engineers and researchers.

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