

# ERRATUM

## Geometric Aspects of General Topology

Katsuro Sakai

K. Sakai, *Geometric Aspects of General Topology*, Springer Monographs in Mathematics, DOI 10.1007/978-4-431-54397-8, © Springer Japan 2013

---

**DOI 10.1007/978-4-431-54397-8.8**

The original version of the book had typos and incorrect symbols/characters which have been fixed in the respective chapters of this book.

### Preface

p. vii, line 9 from top, 1966 *should read as* 1967

### Chapter 1

- p. 1, line 12 from bottom: *Insert* “ — half line” before ‘;’.
- p. 2, line 7 from top: **cellularity** *should read as* **cellularity**
- p. 19, line 9 from top:  $n \in \Gamma$  *should read as*  $n \in \mathbb{N}$

### Chapter 2

- p. 47, **Fig. 2.7** *should read as* **Fig. 2.8**. This figure should be on p. 48
- p. 47, line 5 from bottom: Fig. 2.8 *should read as* Fig. 2.7
- p. 48: **Fig. 2.8** *should read as* **Fig. 2.9**. This figure should be on p. 50
- p. 48, line 13 from bottom: *Remove* “— Fig. 2.9”
- p. 48, line 1 from bottom: *Insert* “— Fig. 2.8” before ‘.’
- p. 49, line 10 from bottom: (Fig. 2.7) *should read as* (Fig. 2.9)
- p. 50: **Fig. 2.9** *should read as* **Fig. 2.7**. This figure should be on p. 47
- p. 51, line 1 from top: *Remove* “Let  $X$  be a paracompact space.”
- p. 51, line 3 from top: *Insert* “Let  $A$  be a subspace of  $X$ .” before ‘To find ...’
- p. 65, line 7 from bottom: with (1) *should read as* with (2)

### Chapter 4

- p. 137, line 7 from bottom: call *should read as* called
- p. 156, line 11 from top:  $f$ s *should read as*  $f$  is

- p. 160, line 10 from bottom: polyhedra *should read as* polyhedron  
 p. 186, line 4 from top:  $K'(0)$  *should read as*  $K^{(0)}$   
 p. 187, line 2 from top: *Insert* “If  $x \in K^{(0)}$  then  $K_x = K$ .”

## Chapter 5

- p. 249, line 3 from top: *Insert* “dim  $X$ ” after ‘**dimension**’  
 p. 249, line 4 from top:  $n + 1$ . and *should read as*  $n + 1$ , and  
 p. 254, line 15–21: This proof is only for the case  $X$  and  $Y$  are closed in  $\mathbb{R}^n$ .  
*For the general case, the proof should be written as follows:*

*Proof.* For each homeomorphism  $h : X \rightarrow Y$ , we will show that  $h(\text{int } X) \subset \text{int } Y$ . Then, applying this to the inverse homeomorphism  $h^{-1} : Y \rightarrow X$ , we can also obtain  $h^{-1}(\text{int } Y) \subset \text{int } X$ , that is,  $\text{int } Y \subset h(\text{int } X)$ . Thus, we will have  $h(\text{int } X) = \text{int } Y$ .

To see  $h(\text{int } X) \subset \text{int } Y$ , note that each  $x \in \text{int } X$  has a compact neighborhood  $C$  in  $\mathbb{R}^n$  with  $C \subset X$ . Since  $\text{int } h(C) \subset \text{int } Y$ , we may show that  $h(x) \in \text{int } h(C)$ . On the contrary, assume that  $h(x) \in \text{bd } h(C)$ . For each neighborhood  $U$  of  $x$  in  $C$ ,  $h(U)$  is a neighbourhood of  $h(x)$  in  $h(C)$ . We can apply Theorem 5.1.7 to find a neighbourhood  $V$  of  $h(x)$  in  $h(C)$  such that  $V \subset h(U)$  and every map  $g : h(C) \setminus V \rightarrow \mathbf{S}^{n-1}$  extends to a map  $\tilde{g} : h(C) \setminus V \rightarrow \mathbf{S}^{n-1}$ . Then,  $h^{-1}(V)$  is a neighborhood of  $x$  in  $C$  with  $h^{-1}(V) \subset U$ . For every map  $f : C \setminus h^{-1}(V) \rightarrow \mathbf{S}^{n-1}$ ,  $f h^{-1} : h(C) \rightarrow \mathbf{S}^{n-1}$  can be extended to a map  $\tilde{f} : h(C) \rightarrow \mathbf{S}^{n-1}$ . Then,  $\tilde{f} h : C \rightarrow \mathbf{S}^{n-1}$  is an extension of  $f$ . Due to Theorem 5.1.7, this means that  $x \in \text{bd } C$ , which is a contradiction. Therefore,  $h(x) \in \text{int } h(C)$ .  $\square$

- p. 261, line 6 from bottom:  $f^{-1}$  *should read as*  $h_0^{-1}$   
 p. 263, line 14 from top: *Insert the following at the end of the sentence:*

Corollary 5.2.16 is valid even if  $n = \infty$ . In fact,  $(\text{pr}_i^{-1}(0), \text{pr}_i^{-1}(1))_{i \in \mathbb{N}}$  is essential in  $\mathbf{I}^{\mathbb{N}}$ . This will be shown in the proof of Theorem 5.6.1.

- p. 264, line 6 from top: *Insert* “and” between ‘CHARACTERIZATION’ and ‘the’.  
 p. 264, line 7 from top: *Insert* “respectively” after ‘dimension’  
 p. 268, line 12 from top: Since *should read as* Note that  $\mathcal{U}_i$   
 p. 268, line 12 from top: it *should read as*  $\mathcal{U}_i$ . Then, it  
 p. 293, line 16 from bottom:  $Y$  *should read as*  $\mathbb{R}^{2n+1}$   
 p. 316, line 6 from bottom:  $\varepsilon/2$  *should read as*  $\varepsilon/3$   
 p. 319, line 13 from top:  $n \in \mathbb{N}$ , and *should read as* and  $n \in \mathbb{N}$ . For any infinite set  
 p. 319, line 14 from top: *Delete* ‘such that ... infinite. Then’.  
 p. 320, line 6 from bottom:  $B_1$  *should read as*  $B_1$  in  $\mathbf{I}^{\mathbb{N}}$ .  
 p. 320, line 6 from bottom: *Replace* ‘which implies that’ *by the following:*

By Lemma 5.3.7, if  $P$  is a partition between  $A_1 \cap S$  and  $B_1 \cap S$  in  $S$ , then there is a partition  $P'$  between  $A_1$  and  $B_1$  in  $\mathbf{I}^{\mathbb{N}}$  such that  $P' \cap S \subset P$ . Then, it follows that  $P \neq \emptyset$ . Due to Theorem 5.2.17, this means that  $\dim S \geq 1$ , that is,

## Chapter 6

p. 346, line 11 from bottom: *homotopy should read as deformation*

p. 346, line 10 from bottom: *Delete ‘ $h_0 = \text{id}$  and’.*

p. 346, line 1 from bottom: *Add the following:*

It is said that  $X$  is **deformable into**  $A (\subset X)$  if there is a deformation  $h : X \times \mathbf{I} \rightarrow X$  with  $h_1(X) \subset A$ . A retract  $A$  of  $X$  is a deformation retract of  $X$  if  $X$  is deformable into  $A$  (refer 6.2.10(9)).

p. 348: *Insert the following before Section 6.3:*

(9) A subset  $A$  of a space  $X$  is a deformation retract if and only if  $X$  is deformable into  $A$  and  $A$  is a retract of  $X$ .

To see the “if” part, let  $h : X \times \mathbf{I} \rightarrow X$  be a deformation with  $h_1(X) \subset A$  and let  $r : X \rightarrow A$  be a retraction. Using the fact that  $rh_1 = h_1$ , we can define a homotopy from  $\text{id}_X$  to  $r$ .

p. 363, line 5 from top: *Add “as a closed set” after ‘Banach space’.*

p. 371, line 5 from top: *4.9.10 should read as 4.9.11*

## Index

p. 516, right-side line 2 from bottom: *cellularity should read as cellularity*

p. 518, left-side line 12 from top: *hedgehog, 33 should read as hedgehog, 33, 296*