

# The IMPL Policy Language for Managing Inconsistency in Multi-Context Systems

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**Abstract.** Multi-context systems are a declarative formalism for interlinking knowledge-based systems (contexts) that interact via (possibly nonmonotonic) bridge rules. Interlinking knowledge provides ample opportunity for unexpected inconsistencies. These are undesired and come in different categories: some may simply be repaired automatically, while others are more serious and must be inspected by a human operator. In general, no one-fits-all solution exists, since these categories depend on the application scenario. To nevertheless tackle inconsistencies in a general and principled way, we thus propose a declarative policy language for inconsistency management in multi-context systems. We define its syntax and semantics, discuss methodologies for applying the language in real world applications, and outline an implementation by rewriting to *acthex*, a formalism extending Answer Set Programs.

## 1 Introduction

The trend to interlink data and information through networked infrastructures, which started out by the spread of the Internet, continues and more recently extends to richer entities of knowledge and knowledge processing. This challenges knowledge management systems that aim at powerful knowledge based applications, in particular when they are built by interlinking smaller existing such systems, and this integration shall be done in a principled way beyond ad-hoc approaches.

Declarative programming methods, and in particular logic programming based approaches, provide rigorous means for developing knowledge based systems through formal representation and model-theoretic evaluation of the knowledge at hand. Extending this technology to advanced scenarios of interlinked information sources is a highly relevant topic of research in declarative knowledge

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representation and reasoning. For instance, Multi-context systems (MCSs) [5], based on [7, 22], are a generic formalism that captures heterogeneous knowledge bases (contexts) which are interlinked using (possibly nonmonotonic) bridge rules.

The advantages of modular systems, i.e., of building a system from smaller parts, however, poses the problem of unexpected inconsistencies due to unintended interaction of system parts. Such inconsistencies are undesired in general, since inference becomes trivial (under common principles; reminiscent of *ex falso sequitur quodlibet*). The problem of explaining reasons for inconsistency in MCSs has been addressed in [16]: several independent inconsistencies can exist in a MCS, and each inconsistency usually can be repaired in more than one possible way.

For example, imagine a hospital information system which links several databases in order to suggest treatments for patients. A simple inconsistency which can be automatically ignored would be if a patient states her birth date correctly at the front desk, but swaps two digits filling in a form at the X-ray department. An entirely different type of inconsistency is (at least as far as the health of the patient is concerned), if the patient needs treatment, but all options are in conflict with some allergy of the patient. Attempting an automatic repair may not be a viable option in this case: a doctor should inspect the situation and make a decision.

In view of such scenarios, tackling inconsistency requires individual strategies and targeted (re)actions, depending on the type of inconsistency and on the application. In this work, we thus propose the declarative *Inconsistency Management Policy Language* (IMPL), which provides a means to specify inconsistency management strategies for MCSs. Our contributions are briefly summarized as follows.

- We define the syntax of IMPL, inspired by Answer Set Programming (ASP) [21] following the syntax of ASP programs. In particular, we specify the *input for policy reasoning*, as being provided by dedicated reserved predicates. These predicates encode inconsistency analysis results in terms of the respective structures in [16]. Furthermore, we specify *action predicates that can be derived by rules*. Actions provide a means to counteract inconsistency by modifying the MCS, and may involve interaction with a human operator.
- We define the semantics of IMPL in a three-step process. In a first step, models of a given policy are calculated. Then, in a second step, the effects of actions which are present in such a model are determined (this possibly involves user interaction). Finally, in a third step, these effects are applied to the MCS.
- On the basis of the above, we provide methodologies for utilizing IMPL in application scenarios, and briefly discuss useful language extensions.
- Finally, we give the necessary details of a concrete realization of IMPL by rewriting it to the *acthex* formalism [2] which extends ASP programs with external computations and actions.

The remainder of the paper is organized as follows: we first introduce MCS and notions for explaining inconsistency in MCSs in Sect. 2. We then define syntax and semantics of the IMPL policy language in Sect. 3, describe methodologies for applying IMPL in practice in Sect. 4, provide a possibility for realizing IMPL by rewriting to *acthex* in Sect. 5, and conclude the paper in Sect. 6.

## 2 Preliminaries

**Multi-context systems (MCSs).** A heterogeneous nonmonotonic MCS [5] consists of *contexts*, each composed of a knowledge base with an underlying *logic*, and a set of *bridge rules* which control the information flow between contexts.

A logic  $L = (\mathbf{KB}_L, \mathbf{BS}_L, \mathbf{ACC}_L)$  is an abstraction which captures many monotonic and nonmonotonic logics, e.g., classical logic, description logics, or default logics. It consists of the following components, the first two intuitively define the logic’s syntax, the third its semantics:

- $\mathbf{KB}_L$  is the set of well-formed knowledge bases of  $L$ . We assume each element of  $\mathbf{KB}_L$  is a set of “formulas”.
- $\mathbf{BS}_L$  is the set of possible belief sets, where a belief set is a set of “beliefs”.
- $\mathbf{ACC}_L : \mathbf{KB}_L \rightarrow 2^{\mathbf{BS}_L}$  assigns to each KB a set of acceptable belief sets.

Since contexts may have different logics, this allows to model heterogeneous systems.

*Example 1.* For *propositional logic*  $L_{prop}$  under the closed world assumption over signature  $\Sigma$ ,  $\mathbf{KB}$  is the set of propositional formulas over  $\Sigma$ ;  $\mathbf{BS}$  is the set of deductively closed sets of propositional  $\Sigma$ -literals; and  $\mathbf{ACC}(kb)$  returns for each  $kb$  a singleton set, containing the set of literal consequences of  $kb$  under the closed world assumption.  $\square$

A *bridge rule* models information flow between contexts: it can add information to a context, depending on the belief sets accepted at other contexts. Let  $L = (L_1, \dots, L_n)$  be a tuple of logics. An  $L_k$ -bridge rule  $r$  over  $L$  is of the form

$$(k : s) \leftarrow (c_1 : p_1), \dots, (c_j : p_j), \mathbf{not} (c_{j+1} : p_{j+1}), \dots, \mathbf{not} (c_m : p_m). \quad (1)$$

where  $k$  and  $c_i$  are context identifiers, i.e., integers in the range  $1, \dots, n$ ,  $p_i$  is an element of some belief set of  $L_{c_i}$ , and  $s$  is a formula of  $L_k$ . We denote by  $h_b(r)$  the formula  $s$  in the head of  $r$  and by  $B(r) = \{(c_1 : p_1), \dots, \mathbf{not} (c_{j+1} : p_{j+1}), \dots\}$  the set of body literals (including negation) of  $r$ .

A multi-context system  $M = (C_1, \dots, C_n)$  is a collection of contexts  $C_i = (L_i, kb_i, br_i)$ ,  $1 \leq i \leq n$ , where  $L_i = (\mathbf{KB}_i, \mathbf{BS}_i, \mathbf{ACC}_i)$  is a logic,  $kb_i \in \mathbf{KB}_i$  a knowledge base, and  $br_i$  is a set of  $L_i$ -bridge rules over  $(L_1, \dots, L_n)$ . By  $IN_i = \{h_b(r) \mid r \in br_i\}$  we denote the set of possible *inputs* of context  $C_i$  added by bridge rules. For each  $H \subseteq IN_i$  it is required that  $kb_i \cup H \in \mathbf{KB}_{L_i}$ . By  $br_M = \bigcup_{i=1}^n br_i$  we denote the set of all bridge rules of  $M$ .

The following running example will be used throughout the paper.

*Example 2 (generalized from [16]).* Consider a MCS  $M_1$  in a hospital which comprises the following contexts: a patient database  $C_{db}$ , a blood and X-Ray analysis database  $C_{lab}$ , a disease ontology  $C_{onto}$ , and an expert system  $C_{dss}$  which suggests proper treatments. Knowledge bases are given below; initial uppercase letters are used for variables and description logic concepts.

$$\begin{aligned}
kb_{db} &= \{ person(sue, 02/03/1985), allergy(sue, ab1) \}, \\
kb_{lab} &= \{ customer(sue, 02/03/1985), test(sue, xray, pneumonia), \\
&\quad test(Id, X, Y) \rightarrow \exists D : customer(Id, D), \\
&\quad customer(Id, X) \wedge customer(Id, Y) \rightarrow X = Y \}, \\
kb_{onto} &= \{ Pneumonia \sqcap Marker \sqsubseteq AtypPneumonia \}, \\
kb_{dss} &= \{ give(Id, ab1) \vee give(Id, ab2) \leftarrow need(Id, ab). \\
&\quad give(Id, ab1) \leftarrow need(Id, ab1). \\
&\quad \neg give(Id, ab1) \leftarrow not\ allow(Id, ab1), need(Id, Med). \}.
\end{aligned}$$

Context  $C_{db}$  uses propositional logic (see Example 1) and provides information that Sue is allergic to antibiotics ‘ $ab1$ ’. Context  $C_{lab}$  is a database with constraints which stores laboratory results connected to Sue: *pneumonia* was detected in an X-ray. Constraints enforce, that each test result must be linked to a *customer* record, and that each customer has only one birth date.  $C_{onto}$  specifies that presence of a blood marker in combination with pneumonia indicates atypical pneumonia. This context is based on  $\mathcal{AL}$ , a basic description logic [1]:  $\mathbf{KB}_{onto}$  is the set of all well-formed theories within that description logic,  $\mathbf{BS}_{onto}$  is the powerset of the set of all assertions  $C(o)$  where  $C$  is a concept name and  $o$  an individual name, and  $\mathbf{ACC}_{onto}$  returns the set of all concept assertions entailed by a given theory.  $C_{dss}$  is an ASP program that suggests a medication using the *give* predicate.

Schemas for bridge rules of  $M_1$  are as follows:

$$\begin{aligned}
r_1 &= (lab : customer(Id, Birthday)) \leftarrow (db : person(Id, Birthday)). \\
r_2 &= (onto : Pneumonia(Id)) \leftarrow (lab : test(Id, xray, pneumonia)). \\
r_3 &= (onto : Marker(Id)) \leftarrow (lab : test(Id, bloodtest, m1)). \\
r_4 &= (dss : need(Id, ab)) \leftarrow (onto : Pneumonia(Id)). \\
r_5 &= (dss : need(Id, ab1)) \leftarrow (onto : AtypPneumonia(Id)). \\
r_6 &= (dss : allow(Id, ab1)) \leftarrow \mathbf{not} (db : allergy(Id, ab1)).
\end{aligned}$$

Rule  $r_1$  links the patient records with the lab database (so patients do not need to enter their data twice). Rules  $r_2$  and  $r_3$  provide test results from the lab to the ontology. Rules  $r_4$  and  $r_5$  link disease information with medication requirements, and  $r_6$  associates acceptance of the particular antibiotic ‘ $ab1$ ’ with a negative allergy check on the patient database.  $\square$

*Equilibrium semantics* [5] selects certain belief states of a MCS  $M = (C_1, \dots, C_n)$  as acceptable. A *belief state* is a list  $S = (S_1, \dots, S_n)$ , s.t.  $S_i \in \mathbf{BS}_i$ . A bridge rule (1) is *applicable* in  $S$  iff for  $1 \leq i \leq j$ :  $p_i \in S_{c_i}$  and for  $j < l \leq m$ :  $p_l \notin S_{c_l}$ . Let  $app(R, S)$  denote the set of bridge rules in  $R$  that are applicable in belief state  $S$ . Then a belief state  $S = (S_1, \dots, S_n)$  of  $M$  is an *equilibrium* iff, for  $1 \leq i \leq n$ , the following condition holds:  $S_i \in \mathbf{ACC}_i(kb_i \cup \{hd(r) \mid r \in app(br_i, S)\})$ .

For simplicity we will disregard the issue of grounding bridge rules (see [20]), and only consider ground instances of bridge rules. In the following, with  $r_1, \dots, r_6$  we refer to the ground instances of the respective bridge rules in Example 2, where variables are replaced by  $Id \mapsto sue$  and  $BirthDay \mapsto 02/03/1985$  (all other instances are irrelevant).

*Example 3 (ctd).* MCS  $M_1$  has one equilibrium  $S = (S_{db}, S_{lab}, S_{onto}, S_{dss})$ , where  $S_{db} = kb_{db}$ ,  $S_{lab} = \{customer(sue, 02/03/1985), test(sue, xray, pneumonia)\}$ ,  $S_{onto} = \{Pneumonia(sue)\}$ , and  $S_{dss} = \{need(sue, ab), give(sue, ab2), \neg give(sue, ab1)\}$ . Moreover, bridge rules  $r_1, r_2$ , and  $r_4$  are applicable under  $S$ .  $\square$

**Explaining Inconsistency in MCSs.** *Inconsistency* in a MCS is the lack of an equilibrium [16]. Note that no equilibrium may exist even if all contexts are ‘paraconsistent’ in the sense that for all  $kb \in \mathbf{KB}$ ,  $\mathbf{ACC}(kb)$  is nonempty. No information can be obtained from an inconsistent MCS, e.g., inference tasks like brave or cautious reasoning on equilibria become trivial. To analyze, and eventually repair, inconsistency in a MCS, we use the notions of consistency-based *diagnosis* and entailment-based *inconsistency explanation* [16], which characterize inconsistency by sets of involved bridge rules.

Intuitively, a diagnosis is a pair  $(D_1, D_2)$  of sets of bridge rules which represents a concrete system repair in terms of removing rules  $D_1$  and making rules  $D_2$  unconditional. The intuition for considering rules  $D_2$  as unconditional is that the corresponding rules should become applicable to obtain an equilibrium. One could consider more fine-grained changes of rules such that only some body atoms are removed instead of all. However, this increases the search space while there is little information gain: every diagnosis  $(D_1, D_2)$  as above, together with a witnessing equilibrium  $S$ , can be refined to such a generalized diagnosis. Dual to that, inconsistency explanations (short: explanations) separate independent inconsistencies. An explanation is a pair  $(E_1, E_2)$  of sets of bridge rules, such that the presence of rules  $E_1$  and the absence of heads of rules  $E_2$  necessarily makes the MCS inconsistent. In other words, bridge rules in  $E_1$  cause an inconsistency in  $M$  which cannot be resolved by considering additional rules already present in  $M$  or by modifying rules in  $E_2$  (in particular making them unconditional). See [16] for formal definitions of these notions, relationships between them, and more background discussion.

*Example 4 (ctd).* Consider a MCS  $M_2$  obtained from  $M_1$  by modifying  $kb_{lab}$ : we replace  $customer(sue, 02/03/1985)$  by the two facts  $customer(sue, 03/02/1985)$  and  $test(sue, bloodtest, m1)$ , i.e., we change the birth date, and add a blood test result.  $M_2$  is inconsistent with two minimal inconsistency explanations  $e_1 = (\{r_1\}, \emptyset)$  and  $e_2 = (\{r_2, r_3, r_5\}, \{r_6\})$ :  $e_1$  characterizes the problem, that  $C_{lab}$  does not accept any belief set because constraint  $customer(Id, X) \wedge customer(Id, Y) \rightarrow X = Y$  is violated. Another independent inconsistency is pointed out by  $e_2$ : if  $e_1$  is repaired, then  $C_{onto}$  accepts  $AtypPneumonia(sue)$ , therefore  $r_5$  imports the need for  $ab1$  into  $C_{dss}$  which makes  $C_{dss}$  inconsistent due to Sue’s allergy. Moreover, the following minimal diagnoses exist for  $M_2$ :  $(\{r_1, r_2\}, \emptyset)$ ,  $(\{r_1, r_3\}, \emptyset)$ ,  $(\{r_1, r_5\}, \emptyset)$ , and  $(\{r_1\}, \{r_6\})$ . For instance, diagnosis  $(\{r_1\}, \{r_6\})$

removes bridge rule  $r_1$  from  $M_2$  and adds  $r_6$  unconditionally to  $M_2$ , which yields a consistent MCS.  $\square$

### 3 Policy Language IMPL

Dealing with inconsistency in an application scenario is difficult, because even if inconsistency analysis provides information how to restore consistency, it is not obvious which choice of system repair is rational. It may not even be clear whether it is wise at all to repair the system by changing bridge rules.

*Example 5 (ctd).* Repairing  $e_1$  by removing  $r_1$  and thereby ignoring the birth date (which differs at the granularity of months) may be the desired reaction and could very well be done automatically. On the contrary, repairing  $e_2$  by ignoring either the allergy or the illness is a decision that should be left to a doctor, as every possible repair could cause serious harm to Sue.  $\square$

Therefore, managing inconsistency in a controlled way is crucial. To address these issues, we propose the declarative *Inconsistency Management Policy Language* IMPL, which provides a means to create policies for dealing with inconsistency in MCSs. Intuitively, an IMPL policy specifies (i) which inconsistencies are repaired automatically and how this shall be done, and (ii) which inconsistencies require further external input, e.g., by a human operator, to make a decision on how and whether to repair the system. Note that we do not rule out automatic repairs, but — contrary to previous approaches — automatic repairs are done only if a given policy specifies to do so, and only to the extent specified by the policy.

Since a major point of MCSs is to abstract away context internals, IMPL treats inconsistency by modifying bridge rules. For the scope of this work we delegate any potential repair by modifying the *kb* of a context to the user. The effect of applying an IMPL policy to an inconsistent MCS  $M$  is a *modification*  $(A, R)$ , which is a pair of sets of bridge rules which are syntactically compatible with  $M$ . Intuitively, a modification specifies bridge rules  $A$  to be added to  $M$  and bridge rules  $R$  to be removed from  $M$ , similar as for diagnoses without restriction to the original rules of  $M$ .

An IMPL policy  $P$  for a MCS  $M$  is intended to be evaluated on a set of *system and inconsistency analysis* facts, denoted  $EDB_M$ , which represents information about  $M$ , in particular  $EDB_M$  contains atoms which describe bridge rules, minimal diagnoses, and minimal explanations of  $M$ .

The evaluation of  $P$  yields certain actions to be taken, which potentially interact with a human operator, and modify the MCS at hand. This modification has the potential to restore consistency of  $M$ .

In the following we formally define syntax and semantics of IMPL.

#### 3.1 Syntax

We assume disjoint sets  $C$ ,  $V$ , *Built*, and *Act*, of constants, variables, built-in predicate names, and action names, respectively, and a set of ordinary predicate

names  $Ord \subseteq C$ . Constants start with lowercase letters, variables with uppercase letters, built-in predicate names with #, and action names with @. The set of terms  $T$  is defined as  $T = C \cup V$ .

An *atom* is of the form  $p(t_1, \dots, t_k)$ ,  $0 \leq k$ ,  $t_i \in T$ , where  $p \in Ord \cup Built \cup Act$  is an ordinary predicate name, builtin predicate name, or action name. An atom is ground if  $t_i \in C$  for  $0 \leq i \leq k$ . The sets  $A_{Act}$ ,  $A_{Ord}$ , and  $A_{Built}$ , called sets of *action atoms*, *ordinary atoms*, and *builtin atoms*, consist of all atoms over  $T$  with  $p \in Act$ ,  $p \in Ord$ , respectively  $p \in Built$ .

**Definition 1.** An IMPL policy is a finite set of rules of the form

$$h \leftarrow a_1, \dots, a_j, \text{not } a_{j+1}, \dots, \text{not } a_k. \quad (2)$$

where  $h$  is an atom from  $A_{Ord} \cup A_{Act}$ , every  $a_i$ ,  $1 \leq i \leq k$ , is from  $A_{Ord} \cup A_{Built}$ , and ‘not’ is negation as failure.

Given a rule  $r$ , we denote by  $H(r)$  its head, by  $B^+(r) = \{a_1, \dots, a_j\}$  its positive body atoms, and by  $B^-(r) = \{a_{j+1}, \dots, a_k\}$  its negative body atoms. A rule is ground if it contains ground atoms only. A ground rule with  $k = 0$  is a *fact*. As in ASP, a rule must be safe, i.e., variables in  $H(r)$  or in  $B^-(r)$  must also occur in  $B^+(r)$ . For a set of rules  $R$ , we use  $cons(R)$  to denote the set of constants from  $C$  appearing in  $R$ , and  $pred(R)$  for the set of ordinary predicate names and action names (elements from  $Ord \cup Act$ ) in  $R$ .

We next describe how a policy represents information about the MCS  $M$  under consideration.

**System and Inconsistency Analysis Predicates.** Entities, diagnoses, and explanations of the MCS  $M$  at hand are represented by a suitable finite set  $C_M \subseteq C$  of constants which uniquely identify contexts, bridge rules, beliefs, rule heads, diagnoses, and explanations. For convenience, when referring to an element represented by a constant  $c$  we identify it with the constant, e.g., we write ‘bridge rule  $r$ ’ instead of ‘bridge rule of  $M$  represented by constant  $r$ ’.

*Reserved atoms* use predicates from the set  $C_{res} \subseteq Ord$  of *reserved predicates*, with  $C_{res} = \{ruleHead, ruleBody^+, ruleBody^-, context, modAdd, modDel, diag, explNeed, explForbid\}$ . They represent the following information.

- $context(c)$  denotes that  $c$  is a context.
- $ruleHead(r, c, s)$  denotes that bridge rule  $r$  is at context  $c$  with head formula  $s$ .
- $ruleBody^+(r, c, b)$  (resp.,  $ruleBody^-(r, c, b)$ ) denotes that bridge rule  $r$  contains body literal ‘ $(c:b)$ ’ (resp., ‘**not**  $(c:b)$ ’).
- $modAdd(m, r)$  (resp.,  $modDel(m, r)$ ) denotes that modification  $m$  adds (resp., deletes) bridge rule  $r$ . Note that  $r$  is represented using  $ruleHead$  and  $ruleBody$ .
- $diag(m)$  denotes that modification  $m$  is a minimal diagnosis in  $M$ .
- $explNeed(e, r)$  (resp.,  $explForbid(e, r)$ ) denotes that the minimal explanation  $(E_1, E_2)$  identified by constant  $e$  contains bridge rule  $r \in E_1$  (resp.,  $r \in E_2$ ).

- $modset(ms, m)$  denotes that modification  $m$  belongs to the set of modifications identified by  $ms$ .

*Example 6 (ctd).* We can represent  $r_1$ ,  $r_5$ , and the diagnosis  $(\{r_1, r_5\}, \emptyset)$  as the set of reserved atoms  $I_{ex} = \{ruleHead(r_1, c_{lab}, 'customer(sue, 02/03/1985)'), ruleBody^+(r_1, c_{db}, 'person(sue, 02/03/1985)'), ruleHead(r_5, c_{dss}, 'need(sue, ab1)'), ruleBody^+(r_5, c_{onto}, 'AtypPneumonia(sue)'), modDel(d, r_1), modDel(d, r_5), diag(d)\}$  where constant  $d$  identifies the diagnosis.  $\square$

Further knowledge used as input for policy reasoning can easily be defined using additional (supplementary) predicates. Note that predicates over all explanations or bridge rules can easily be defined by projecting from reserved atoms. Moreover, to encode preference relations (e.g., as in [17]) between system parts, diagnoses, or explanations, an atom  $preferredContext(c_1, c_2)$  could denote that context  $c_1$  is considered more reliable than context  $c_2$ . The extensions of such auxiliary predicates need to be defined by the rules of the policy or as additional input facts (ordinary predicates), or they are provided by the implementation (built-in predicates), i.e., the ‘solver’ used to evaluate the policy. The rewriting to *acthex* given in Sect. 5.2 provides a good foundation for adding supplementary predicates as built-ins, because the *acthex* language has generic support for calls to external computational sources. A possible application would be to use a preference relation between bridge rules that is defined by an external predicate and can be used for reasoning in the policy.

Towards a more formal definition of a policy input, we distinguish the set  $B_M$  of ground atoms built from reserved predicates  $C_{res}$  and terms from  $C_M$ , called *MCS input base*, and the *auxiliary input base*  $B_{Aux}$  given by predicates over  $Ord \setminus C_{res}$  and terms from  $C$ . Then, the *policy input base*  $B_{Aux, M}$  is defined as  $B_{Aux} \cup B_M$ . For a set  $I \subseteq B_{Aux, M}$ ,  $I|_{B_M}$  and  $I|_{B_{Aux}}$  denote the restriction of  $I$  to predicates from the respective bases.

Now, given an MCS  $M$ , we say that a set  $S \subseteq B_M$  is a *faithful representation* of  $M$  wrt. a reserved predicate  $p \in C_{res} \setminus \{modset\}$  iff the extension of  $p$  in  $S$  exactly characterizes the respective entity or property of  $M$  (according to a unique naming assignment associated with  $C_M$  as mentioned). For instance,  $context(c) \in S$  iff  $c$  is a context of  $M$ , and correspondingly for the other predicates. Consequently,  $S$  is a faithful representation of  $M$  iff it is a faithful representation wrt. all  $p$  in  $C_{res} \setminus \{modset\}$  and the extension of  $modset$  in  $S$  is empty.

A finite set of facts  $I \subseteq B_{Aux, M}$  containing a faithful representation of all relevant entities and properties of an MCS qualifies as input of a policy, as defined next.

**Definition 2.** A policy input  $I$  wrt. MCS  $M$  is a finite subset of the policy input base  $B_{Aux, M}$ , such that  $I|_{B_M}$  is a faithful representation of  $M$ .

In the following, we denote by  $EDB_M$  a policy input wrt. a MCS  $M$ . Note that reserved predicate  $modset$  has an empty extension in a policy input (but



corresponding atoms will be of use later on in combination with actions). Given a set of reserved atoms  $I$ , let  $c$  be a constant that appears as a bridge rule identifier in  $I$ . Then  $rule_I(c)$  denotes the corresponding bridge rule represented by reserved atoms  $ruleHead$ ,  $ruleBody^+$ , and  $ruleBody^-$  in  $I$  with  $c$  as their first argument. Similarly we denote by  $mod_I(m) = (A, R)$  (resp., by  $modset_I(m) = \{(A_1, R_1), \dots\}$ ) the modification (resp., set of modifications) represented in  $I$  by the respective predicates and identified by constant  $m$ .

Subsequently, we call a modification  $m$  that is projected to rules located at a certain context  $c$  the *projection* of  $m$  to context  $c$  (and similarly for sets of modifications). Formally we denote by  $mod_I(m)|_c$  (resp.,  $modset_I(m)|_c$ ) the projection of modification (resp., set of modifications)  $m$  in  $I$  to context  $c$ .

*Example 7 (ctd).* In the previous example  $I_{ex}$ ,  $rule_{I_{ex}}(r_1)$  refers to rule  $r_1$ ; moreover  $mod_{I_{ex}}(d) = (\{r_1, r_5\}, \emptyset)$  and the projection of modification  $d$  to  $c_{dss}$  is  $(\{r_5\}, \emptyset)$ .  $\square$

A policy can create representations of new rules, modifications, and sets of modifications, because reserved atoms are allowed to occur in heads of policy rules. However such new entities require new constants identifying them. To tackle this issue, we next introduce a facility for value invention.

**Value Invention via Builtin Predicates ‘#id<sub>k</sub>’.** Whenever a policy specifies a new rule and uses it in some action, the rule must be identified with a constant. The same is true for modifications and sets of modifications. Therefore, IMPL contains a family of special builtin predicates which provide policy writers a means to comfortably create new constants from existing ones.

For this purpose, builtin predicates of the form  $\#id_k(c', c_1, \dots, c_k)$  may occur in rule bodies (only). Their intended usage is to uniquely (and thus reproducibly) associate a new constant  $c'$  with a tuple  $c_1, \dots, c_k$  of constants (for a formal semantics see the definitions for action determination in Sect. 3.2).

Note that this value invention feature is not strictly necessary, as new constants can be obtained via defining an order relation over all constants, a pool of unused constants, and auxiliary rules that use the next unused constant for each new constant that is required by the program. However, a dedicated value invention builtin simplifies policy writing and improves policy readability.

*Example 8.* Assume one wants to consider projections of modifications to contexts as specified by the extension of an auxiliary predicate  $projectMod(M, C)$ . The following policy fragment achieves this using a value invention builtin to assign a unique identifier with every projection (recorded in the extension of another auxiliary predicate  $projectedModId(M', M, C)$ ).

$$\left\{ \begin{array}{l} projectedModId(M', M, C) \leftarrow projectMod(M, C), \\ \phantom{projectedModId(M', M, C) \leftarrow} \phantom{projectMod(M, C),} \#id_3(M', pm_{id}, M, C); \\ modAdd(M', R) \leftarrow modAdd(M, R), ruleHead(R, C, S), \\ \phantom{modAdd(M', R) \leftarrow} \phantom{modAdd(M, R),} projectedModId(M', M, C); \\ modDel(M', R) \leftarrow modDel(M, R), ruleHead(R, C, S), \\ \phantom{modDel(M', R) \leftarrow} \phantom{modDel(M, R),} projectedModId(M', M, C) \end{array} \right\} \quad (3)$$

Intuitively, we identify new modifications by new ids  $c_{pm_{id},M,C}$  obtained from  $M$  and  $C$  via  $\#id_3$  and an auxiliary constant  $pm_{id} \notin C_M$ . The latter simply serves the purpose of disambiguating constants used for projections of modifications.  $\square$

Besides representing modifications of a MCS aiming at resolving inconsistency, an important feature of IMPL is to actually apply them. Actions serve this purpose.

**Actions.** Actions alter the MCS at hand and may interact with a human operator. According to the change that an action performs, we distinguish *system actions* which modify the MCS in terms of entire bridge rules that are added and/or deleted, and *rule actions* which modify a single bridge rule. Moreover, the changes can depend on external input, e.g., obtained by user interaction. In the latter case, the action is termed *interactive*. Accumulating the changes of all actions yields an overall modification of the MCS. We formally define this intuition when addressing the semantics in Sect. 3.2.

Syntactically, we use  $@$  to prefix action names from  $Act$ , and those of the predefined actions listed below are reserved action names. Let  $M$  be the MCS under consideration, then the following predefined actions are (non-interactive) system actions:

- $@delRule(r)$  removes bridge rule  $r$  from  $M$ .
- $@addRule(r)$  adds bridge rule  $r$  to  $M$ .
- $@applyMod(m)$  applies modification  $m$  to  $M$ .
- $@applyModAtContext(m, c)$  applies those changes in  $m$  to the MCS that add or delete bridge rules at context  $c$  (i.e., applies the projection of  $m$  to  $c$ ).

Note that a policy might specify conflicting effects, i.e., the removal and the addition of a bridge rule at the same time. In this case the semantics gives preference to addition.

The predefined actions listed next are rule actions:

- $@addRuleCondition^+(r, c, b)$  (resp.,  $@addRuleCondition^-(r, c, b)$ ) adds body literal  $(c:b)$  (resp., **not**  $(c:b)$ ) to bridge rule  $r$ .
- $@delRuleCondition^+(r, c, b)$  (resp.,  $@delRuleCondition^-(r, c, b)$ ) removes body literal  $(c:b)$  (resp., **not**  $(c:b)$ ) from bridge rule  $r$ .
- $@makeRuleUnconditional(r)$  makes bridge rule  $r$  unconditional.

Since these actions can modify the same rule, this may also result in conflicting effects, where again addition is given preference over removal by the semantics. (Moreover, rule modifications are given preference over addition or removal of the entire rule.)

Eventually, the subsequent predefined actions are interactive (system) actions, i.e., they involve a human operator:

- $@guiSelectMod(ms)$  displays a GUI for choosing from the set of modifications  $ms$ . The modification chosen by the user is applied to  $M$ .

- $@guiEditMod(m)$  displays a GUI for editing modification  $m$ . The resulting modification is applied to  $M$ .<sup>1</sup>
- $@guiSelectModAtContext(ms, c)$  projects modifications in  $ms$  to  $c$ , displays a GUI for choosing among them and applies the chosen modification to  $M$ .
- $@guiEditModAtContext(m, c)$  projects modification  $m$  to context  $c$ , displays a GUI for editing it, and applies the resulting modification to  $M$ .

As we define formally in Sect. 3.2, changes of individual actions are not applied directly, but collected into an overall modification which is then applied to  $M$  (respecting preferences in case of conflicts as stated above). Before turning to a formal definition of the semantics, we give example policies.

*Example 9 (ctd).* Figure 1 shows three policies that can be useful for managing inconsistency in our running example. Their intended behavior is as follows.  $P_1$  deals with inconsistencies at  $C_{lab}$ : if an explanation concerns only bridge rules at  $C_{lab}$ , an arbitrary diagnosis is applied at  $C_{lab}$ , other inconsistencies are not handled. Applying  $P_1$  to  $M_2$  removes  $r_1$  at  $C_{lab}$ , the resulting MCS is still inconsistent with inconsistency explanation  $e_2$ , as only  $e_1$  has been automatically fixed.  $P_2$  extends  $P_1$  by adding an ‘inconsistency alert formula’ to  $C_{lab}$  if an

Policies (sets of IMPL rules)	Intuitive meaning of rules in each set
$P_1 = \{$ $expl(E) \leftarrow explNeed(E, R);$ $expl(E) \leftarrow explForbid(E, R);$ $incNotLab(E) \leftarrow explNeed(E, R),$ $ruleHead(R, C, F), C \neq c_{lab};$ $incNotLab(E) \leftarrow explForbid(E, R),$ $ruleHead(R, C, F), C \neq c_{lab};$ $incLab \leftarrow expl(E), not incNotLab(E);$ $in(D) \leftarrow not out(D), diag(D), incLab;$ $out(D) \leftarrow not in(D), diag(D), incLab;$ $\perp \leftarrow in(A), in(B), A \neq B;$ $useOne \leftarrow in(D);$ $\perp \leftarrow not useOne, incLab;$ $@applyModAtContext(D, c_{lab}) \leftarrow$ $useDiag(D)\}$	Define domain predicate for explanations. Find out whether one explanation only concerns bridge rules at $c_{lab}$ . Guess a diagnosis. Ensure that we guess exactly one diagnosis if there is a local inconsistency at $c_{lab}$ . Apply the guessed diagnosis after projecting it to context $c_{lab}$ .
$P_2 = \{$ $ruleHead(r_{alert}, c_{lab}, alert) \leftarrow;$ $@addRule(r_{alert}) \leftarrow incLab\}$ $\cup P_1$	Define new inconsistency alert rule $r_{alert}$ . Add that new rule to $c_{lab}$ . Reuse policy $P_1$ .
$P_3 = \{$ $modset(md, X) \leftarrow diag(X);$ $@guiSelectMod(md) \leftarrow\}$	Create modification set with all diagnoses. Let the user choose from that set.

**Fig. 1.** Sample IMPL policies for our running example.

<sup>1</sup> It is suggestive to also give the operator a possibility to abort, causing no modification at all to be made, however we do not specify this here because a useful design choice depends on the concrete application scenario.

inconsistency was automatically repaired at that context. Finally,  $P_3$  is a fully manual approach which displays a choice of all minimal diagnoses to the user and applies the user's choice. Note, that we did not combine automatic actions and user-interactions here since this would result in more involved policies (and/or require an iterative methodology; cf. Sect. 4).  $\square$

We refer to the predefined IMPL actions  $@delRule$ ,  $@addRule$ ,  $@guiSelectMod$ , and  $@guiEditMod$  as *core* actions, and to the remaining ones as *comfort* actions. Comfort actions exist for convenience of use, providing means for projection and for rule modifications. They can be rewritten to core actions as sketched in the following example.

*Example 10.* To realize  $@applyMod(M)$  and  $@applyModAtContext(M, C)$  using the core language, we replace them by  $applyMod(M)$  and  $applyModAtContext(M, C)$ , respectively, use rules (3) from Example 8, and add the following set of rules.

$$\left\{ \begin{array}{l} @addRule(R) \leftarrow applyMod(M), modAdd(M, R); \\ @delRule(R) \leftarrow applyMod(M), modDel(M, R); \\ projectMod(M, C) \leftarrow applyModAtContext(M, C); \\ applyMod(M') \leftarrow applyModAtContext(M, C), \\ \phantom{applyMod(M')} \phantom{\leftarrow} projectedModId(M', M, C) \end{array} \right\} \quad (4)$$

$\square$

This concludes our introduction of the syntax of IMPL, and we move on to a formal development of its semantics which so far has only been conveyed by accompanying intuitive explanations.

### 3.2 Semantics

The semantics of applying an IMPL policy  $P$  to a MCS  $M$  is defined in three steps:

- *Actions* to be executed are determined by computing a *policy answer set* of  $P$  wrt. policy input  $EDB_M$ .
- *Effects of actions* are determined by executing actions. This yields modifications  $(A, R)$  of  $M$  for each action. Action effects can be nondeterministic and thus only be determined by executing respective actions (which is particularly true for user interactions).
- Effects of actions are *materialized* by building the componentwise union over individual action effects and applying the resulting modification to  $M$ .

In the remainder of this section, we introduce the necessary definitions for a precise formal account of these steps.

**Action Determination.** We define IMPL policy answer sets similar to the stable model semantics [21]. Given a policy  $P$  and a policy input  $EDB_M$ , let  $id_k$  be a fixed (built-in) family of one-to-one mappings from  $k$ -tuples  $c_1, \dots, c_k$ , where

$c_i \in \text{cons}(P \cup \text{EDB}_M)$  for  $1 \leq i \leq k$ , to a set  $C_{id} \subset C$  of ‘fresh’ constants, i.e., disjoint from  $\text{cons}(P \cup \text{EDB}_M)$ .<sup>2</sup> Then the *policy base*  $B_{P,M}$  of  $P$  wrt.  $\text{EDB}_M$  is the set of ground IMPL atoms and actions, that can be built using predicate symbols from  $\text{pred}(P \cup \text{EDB}_M)$  and terms from  $U_{P,M} = \text{cons}(P \cup \text{EDB}_M) \cup C_{id}$ , called policy universe.

The *grounding* of  $P$ , denoted by  $\text{grnd}(P)$ , is given by grounding its rules wrt.  $U_{P,M}$  as usual. Note that, since  $\text{cons}(P \cup \text{EDB}_M)$  is finite, only a finite amount of mapping functions  $\text{id}_k$  is used in  $P$ . Hence only a finite amount of constants  $C_{id}$  is required, and therefore  $U_{P,M}$ ,  $B_{P,M}$ , and  $\text{grnd}(P)$  are finite as well.

An *interpretation* is a set of ground atoms  $I \subseteq B_{P,M}$ . We say that  $I$  *models* an atom  $a \in B_{P,M}$ , denoted  $I \models a$  iff (i)  $a$  is not a built-in atom and  $a \in I$ , or (ii)  $a$  is a built-in atom of the form  $\# \text{id}_k(c, c_1, \dots, c_k)$  and  $c = \text{id}_k(c_1, \dots, c_k)$ .  $I$  models a set of atoms  $A \subseteq B_{P,M}$ , denoted  $I \models A$ , iff  $I \models a$  for all  $a \in A$ .  $I$  models the body of rule  $r$ , denoted as  $I \models B(r)$ , iff  $I \models a$  for every  $a \in B^+(r)$  and  $I \not\models a$  for all  $a \in B^-(r)$ ; and for a ground rule  $r$ ,  $I \models r$  iff  $I \models H(r)$  or  $I \not\models B(r)$ . Eventually,  $I$  is a *model* of  $P$ , denoted  $I \models P$ , iff  $I \models r$  for all  $r \in \text{grnd}(P)$ . The *FLP-reduct* [19] of  $P$  wrt. an interpretation  $I$ , denoted  $fP^I$ , is the set of all  $r \in \text{grnd}(P)$  such that  $I \models B(r)$ .<sup>3</sup>

**Definition 3 (Policy Answer Set).** *Given an MCS  $M$ , let  $P$  be an IMPL policy, and let  $\text{EDB}_M$  be a policy input wrt.  $M$ . An interpretation  $I \subseteq B_{P,M}$  is a policy answer set of  $P$  for  $\text{EDB}_M$  iff  $I$  is a  $\subseteq$ -minimal model of  $fP^I \cup \text{EDB}_M$ .*

We denote by  $\mathcal{AS}(P \cup \text{EDB}_M)$  the set of all policy answer sets of  $P$  for  $\text{EDB}_M$ .

**Effect Determination.** We define the effects of action predicates  $@a \in \text{Act}$  by nondeterministic functions  $f_{@a}$ . Nondeterminism is required for interactive actions. An action is evaluated wrt. an interpretation of the policy and yields an effect according to its type: the effect of a system action is a modification  $(A, R)$  of the MCS, in the following sometimes denoted *system modification*, while the effect of a rule action is a *rule modification*  $(A, R)_r$  wrt. a bridge rule  $r$  of  $M$ , i.e., in this case  $A$  is a set of bridge rule body literals to be added to  $r$ , and  $R$  is a set of bridge rule body literals to be removed from  $r$ .

**Definition 4.** *Given an interpretation  $I$ , and a ground action  $\alpha$  of form  $@a(t_1, \dots, t_k)$ , the effect of  $\alpha$  wrt.  $I$  is given by  $\text{eff}_I(\alpha) = f_{@a}(I, t_1, \dots, t_k)$ , where  $\text{eff}_I(\alpha)$  is a system modification if  $\alpha$  is a system action, and a rule modification if  $\alpha$  is a rule action.*

Action predicates of the IMPL core fragment have the following semantic functions.

<sup>2</sup> Disjointness ensures finite groundings; without this restriction, e.g., the program  $\{p(C') \leftarrow \# \text{id}_1(C', C); p(C)\}$  would not have finite grounding.

<sup>3</sup> We use the FLP reduct for compliance with *acthex* (used for realization in Sect. 5), but for the language considered, the Gelfond-Lifschitz reduct would yield an equivalent definition.

- $f_{@delRule}(I, r) = (\emptyset, \{rule_I(r)\})$ .
- $f_{@addRule}(I, r) = (\{rule_I(r)\}, \emptyset)$ .
- $f_{@guiSelectMod}(I, ms) = (A, R)$  where  $(A, R)$  is the user's selection after being displayed a choice among all modifications in  $\{(A_1, R_1), \dots\} = modset_I(ms)$ .
- $f_{@guiEditMod}(I, m) = (A', R')$ , where  $(A', R')$  is the result of user interaction with a modification editor that is preloaded with modification  $(A, R) = mod_I(m)$ .

Note that the effect of any core action in  $I$  can be determined independently from the presence of other core actions in  $I$ , and rule modifications are not required to define the semantics of core actions. However, rule modifications are needed to capture the effect of *comfort* actions. Moreover, adding and deleting rule conditions, and making a rule unconditional can modify the same rule, therefore such action effects yield accumulated rule modifications.

More specifically, the semantics of IMPL comfort actions is defined as follows:

- $f_{@delRuleCondition^+}(I, r, c, b) = (\emptyset, \{(c : b)\})_r$ .
- $f_{@delRuleCondition^-}(I, r, c, b) = (\emptyset, \{\mathbf{not}(c : b)\})_r$ .
- $f_{@addRuleCondition^+}(I, r, c, b) = (\{(c : b)\}, \emptyset)_r$ .
- $f_{@addRuleCondition^-}(I, r, c, b) = (\{\mathbf{not}(c : b)\}, \emptyset)_r$ .
- $f_{@makeRuleUnconditional}(I, r) = (\emptyset, \{(c_1 : p_1), \dots, (c_j : p_j), \mathbf{not}(c_{j+1} : p_{j+1}), \dots, \mathbf{not}(c_m : p_m)\})_r$  for  $r$  of the form (1).
- $f_{@applyMod}(I, m) = mod_I(m)$ .
- $f_{@applyModAtContext}(I, m, c) = mod_I(m)|_c$ .
- $f_{@guiSelectModAtContext}(I, ms, c) = (A', R')$  where  $(A', R')$  is the user's selection after being displayed a choice among all modifications in  $\{(A'_1, R'_1), \dots\} = modset_I(ms)|_c$ .
- $f_{@guiEditModAtContext}(I, m, c) = (A', R')$ , where  $(A', R')$  is the result of user interaction with a modification editor that is preloaded with modification  $mod_I(m)_c$ .

In practice, however, it is not necessary to implement action functions on the level of rule modifications, since a policy in the comfort fragment can equivalently be rewritten to the core fragment (which does not rely on rule modifications). Example 10 already sketched a rewriting for  $@applyMod$  and  $@applyModAtContext$ . For a complete rewriting from the comfort to the core fragment, we refer to the extended version of this paper [15].

The effects of user-defined actions have to comply to Definition 4.

**Effect Materialization.** Once the effects of all actions in a selected policy answer set have been determined, an overall modification is computed by the componentwise union over all individual modifications. This overall modification is then materialized in the MCS.

Given a MCS  $M$  and a policy answer set  $I$  (for a policy  $P$  and a corresponding policy input  $EDB_M$ ), let  $I_M$ , respectively  $I_R$ , denote the set of ground system actions, respectively rule actions, in  $I$ . Then,  $M_{eff} = \{eff_I(\alpha) | \alpha \in I_M\}$  is the set of effects of system action atoms in  $I$ , and  $R_{eff} = \{eff_I(\alpha) | \alpha \in I_R\}$  is

the set of effects of rule actions in  $I$ . Furthermore,  $Rules = \{r \mid (A, R)_r \in R_{eff}\}$  is the set of bridge rules modified by  $R_{eff}$ , and for every  $r \in Rules$ , let  $\mathcal{R}_r = \bigcup_{(A,R)_r \in R_{eff}} R$ , respectively  $\mathcal{A}_r = \bigcup_{(A,R)_r \in R_{eff}} A$ , denote the union of rule body removals, respectively additions, wrt.  $r$  in  $R_{eff}$ .

**Definition 5.** *Given a MCS  $M$ , and an IMPL policy  $P$ , let  $I$  be a policy answer set of  $P$  for a policy input  $EDB_M$  wrt.  $M$ . Then, the materialization of  $I$  in  $M$  is the MCS  $M'$  obtained from  $M$  by replacing its set of bridge rules  $br_M$  by the set*

$$(br_M \setminus \mathcal{R} \cup \mathcal{A}) \setminus Rules \cup \mathcal{M},$$

where  $\mathcal{R} = \bigcup_{(A,R) \in M_{eff}} R$ ,  $\mathcal{A} = \bigcup_{(A,R) \in M_{eff}} A$ , and  $\mathcal{M} = \{(k:s) \leftarrow Body \mid r \in Rules, r \in br_k, h_b(r) = s, Body = B(r) \setminus \mathcal{R}_r \cup \mathcal{A}_r\}$ .

Note that, by definition, the addition of bridge rules has precedence over removal, and the addition of body literals similarly has precedence over removal. There is no particular reason for this choice; one just has to be aware of it when specifying a policy. Apart from that, no order for evaluating individual actions is specified or required.

Eventually, we can define modifications of a MCS that are accepted by a corresponding IMPL policy.

**Definition 6.** *Given a MCS  $M$ , an IMPL policy  $P$ , and a policy input  $EDB_M$  wrt.  $M$ , a modified MCS  $M'$  is an admissible modification of  $M$  wrt.  $P$  and  $EDB_M$  iff  $M'$  is the materialization of some policy answer set  $I \in \mathcal{AS}(P \cup EDB_M)$ .*

*Example 11 (ctd).* For brevity we here do not give a full account of a proper  $EDB_{M_2}$  of our running example. Intuitively  $EDB_{M_2}$  represents all bridge rules, minimal diagnoses and minimal explanations, in a similar fashion as already shown in Ex. 6. We assume, that the two explanations and four diagnoses given in Ex. 4 are identified by constants  $e_1, e_2, d_1, \dots, d_4$ , respectively.

Evaluating  $P_2 \cup EDB_{M_2}$  yields four policy answer sets, one is  $I_1 = EDB_{M_2} \cup \{expl(e_1), expl(e_2), incNotLab(e_2), incLab, in(d_1), out(d_2), out(d_3), out(d_4), useOne, ruleHead(r_{alert}, c_{lab}, alert), @addRule(r_{alert}), @applyModAtContext(d_1, c_{lab})\}$ . From  $I_1$  we obtain a single admissible modification of  $M_2$  wrt.  $P_2$ : add bridge rule  $r_{alert}$  and remove  $r_1$ .

Evaluating  $P_3 \cup EDB_{M_2}$  yields one policy answer set, which is  $I_2 = EDB_{M_2} \cup \{modset(md, d_1), modset(md, d_2), modset(md, d_3), modset(md, d_4), @guiSelectMod(md)\}$ . Determining the effect of  $I_2$  involves user interaction; thus multiple materializations of  $I_2$  exist. For instance, if the user chooses to ignore Sue's allergy and birth date (and probably imposes additional monitoring on Sue), then we obtain an admissible modification of  $M$ : it adds the unconditional version of  $r_6$  and removes  $r_1$ .  $\square$

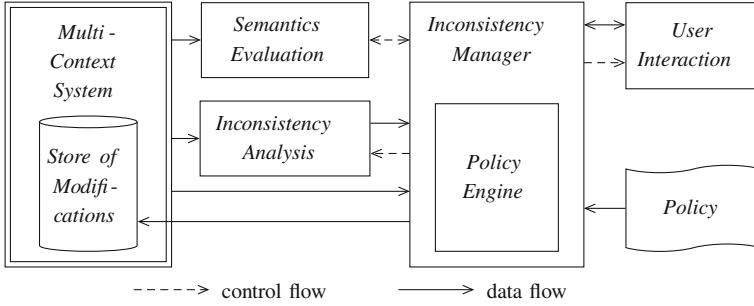


Fig. 2. Policy integration data flow and control flow block diagram.

## 4 Methodologies of Applying IMPL and Realization

Based on the simple system design shown in Fig. 2, we next briefly discuss elementary methodologies of applying IMPL for the purpose of integrating MCS reasoning with potential user interaction in case of inconsistency. Due to space constraints, we restrict ourselves to an informal discussion.

We maintain a representation of the MCS together with a *store of modifications*. The *semantics evaluation* component performs reasoning tasks on the MCS and invokes the *inconsistency manager* in case of an inconsistency. This inconsistency manager uses the *inconsistency analysis* component<sup>4</sup> to provide input for the *policy engine* which computes policy answer sets of a given IMPL *policy* wrt. the MCS and its inconsistency analysis result. This policy evaluation step results in action executions potentially involving user interactions and causes changes to the store of modifications, which are subsequently materialized. Finally the inconsistency manager hands control back to the semantics evaluation component. Principal modes of operation, and their merits, are the following.

**Reason and Manage once.** This mode of operation evaluates the policy once, if the effect materialization does not repair inconsistency in the MCS, no further attempts are made and the MCS stays inconsistent. While simple, this mode may not be satisfying in practice.

However, one can improve on the approach by extending actions with priority: the result of a single policy evaluation step then may be a sequence of sets of actions (of equal priority), corresponding to successive *attempts* (of increasing priority) for repairing the MCS. This can be exploited for writing policies that ensure repairs, by first attempting a ‘sophisticated’ repair possibly involving user interaction, and — if this fails — to simply apply some diagnosis to ensure consistency while the problem may be further investigated.

<sup>4</sup> For realizations of this component we refer to [3, 16].



**Reason and Manage iteratively.** Another way to deal with failure to restore consistency is to simply invoke policy evaluation again on the modified but still inconsistent system. This is useful if user interaction may involve trial-and-error, especially if multiple inconsistencies occur: some might be more difficult to counteract than others.

Another positive aspect of iterative policy evaluation is, that it allows for policies to be structured, e.g., as follows: (a) classify inconsistencies into automatically versus manually repairable; (b) apply actions to repair one of the automatically repairable inconsistencies; (c) if such inconsistencies do not exist: apply user interaction actions to repair one (or all) of the manually repairable inconsistencies. Such policy structuring follows a divide-and-conquer approach, trying to focus on individual sources of inconsistency and to disregard interactions between inconsistencies as much as possible. If user interaction consists of trial-and-error bugfixing, fewer components of the system are changed in each iteration, and the user starts from a situation where only critical (i.e. not automatically repairable) inconsistencies are present in the MCS. Moreover, such policies may be easier to write and maintain. On the other hand, termination of iterative methodologies is not guaranteed. However, one can enforce termination by limiting the number of iterations, possibly by extending IMPL with a *control action* that configures this limit.

In iterative mode, passing information from one iteration to the next may be useful. This can be accomplished by considering additional user-defined add and delete actions which modify an iteration-persistent *knowledge base*, provided to the policy as further input (by means of dedicated auxiliary predicates). For more details we refer to [15].

## 5 Realizing IMPL in acthex

In this section, we demonstrate how IMPL can be realized using *acthex*. First we give preliminaries about *acthex* which is a logic programming formalism that extends HEX programs with executable actions. We then show how to implement the core IMPL fragment by rewriting it to *acthex* in Sect. 5.2. A rewriting from the comfort to the core fragment of IMPL is given in the extended version of this paper [15].

### 5.1 Preliminaries on acthex

The *acthex* formalism [2] generalizes HEX programs [18] by adding dedicated action atoms to heads of rules. An *acthex* program operates on an *environment*; this environment can influence external sources in *acthex*, and it can be modified by the execution of actions.

**Syntax.** By  $\mathcal{C}$ ,  $\mathcal{X}$ ,  $\mathcal{G}$ , and  $\mathcal{A}$  we denote mutually disjoint sets whose elements are called constant names, variable names, external predicate names, and action predicate names, respectively. Elements from  $\mathcal{X}$  (resp.,  $\mathcal{C}$ ) are denoted with first

letter in upper case (resp., lower case), while elements from  $\mathcal{G}$  (resp.,  $\mathcal{A}$ ) are prefixed with “&” (resp. “#”). Names in  $\mathcal{C}$  serve both as constant and predicate names, and we assume that  $\mathcal{C}$  contains a finite subset of consecutive integers  $\{0, \dots, n_{max}\}$ .

Elements from  $\mathcal{C} \cup \mathcal{X}$  are called *terms*. A *higher-order atom* (or *atom*) is a tuple  $(Y_0, Y_1, \dots, Y_n)$ , where  $Y_0, Y_1, \dots, Y_n$  are terms, and  $n \geq 0$  is the arity of the atom. Intuitively,  $Y_0$  is the predicate name, and we thus also use the more familiar notation  $Y_0(Y_1 \dots Y_n)$ . An atom is ordinary if  $Y_0$  is a constant. An external atom is of the form  $\&g[Y_1, \dots, Y_n](X_1, \dots, X_m)$  with  $Y_1, \dots, Y_n$  and  $X_1, \dots, X_m$  being lists of terms. An action atom is of the form  $\#g[Y_1, \dots, Y_n]\{o, r\}[w : l]$  where  $\#g$  is an action predicate name,  $Y_1, \dots, Y_n$  is a list of terms (called input list), and each action predicate  $\#g$  has fixed length  $in(\#g) = n$  for its input list. Attribute  $o \in \{b, c, c_p\}$  is called the *action option*; depending on  $o$  the action atom is called *brave*, *cautious*, and *preferred cautious*, respectively. Attributes  $r, w$ , and  $l$  are called *precedence*, *weight*, and *level* of  $\#g$ , denoted by  $prec(a)$ ,  $weight(a)$ , and  $level(a)$ , respectively. They are optional and range over variables and positive integers.

A *rule*  $r$  is of the form  $\alpha_1 \vee \dots \vee \alpha_k \leftarrow \beta_1, \dots, \beta_n, not \beta_{n+1}, \dots, not \beta_m$ , where  $m, n, k \geq 0$ ,  $m \geq n$ ,  $\alpha_1, \dots, \alpha_k$  are atoms or action atoms, and  $\beta_1, \dots, \beta_m$  are atoms or external atoms. We define  $H(r) = \{\alpha_1, \dots, \alpha_k\}$  and  $B(r) = B^+(r) \cup B^-(r)$ , where  $B^+(r) = \{\beta_1, \dots, \beta_n\}$  and  $B^-(r) = \{\beta_{n+1}, \dots, \beta_m\}$ . An *acthex program* is a finite set  $P$  of rules.

*Example 12.* The acthex program  $\{\#robot[goto, charger]\{b, 1\} \leftarrow \&sensor[bat](low); \#robot[clean, kitchen]\{c, 2\} \leftarrow night; \#robot[clean, bedroom]\{c, 2\} \leftarrow day; night \vee day \leftarrow \}$  uses action atom  $\#robot$  to command a robot, and an external atom  $\&sensor$  to obtain sensor information. Precedence 1 of action atom  $\#robot[goto, charger]\{b, 1\}$  makes the robot recharge its battery before executing cleaning actions, if necessary.  $\square$

**Semantics.** Intuitively, an acthex program  $P$  is evaluated wrt. an *external environment*  $E$  using the following steps: (i) *answer sets* of  $P$  are determined wrt.  $E$ , the set of *best models* is a subset of the answer sets determined by an objective function; (ii) one best model is selected, and one *execution schedule*  $S$  is generated for that model (although a model may give rise to multiple execution schedules); (iii) the *effects of action atoms* in  $S$  are applied to  $E$  in the order defined by  $S$ , yielding an updated environment  $E'$ ; and finally (iv) the process may be iterated starting at (i), unless no actions were executed in (iii) which terminates an iterative evaluation process. Formally the acthex semantics is defined as follows.

Given an acthex program  $P$ , the *Herbrand base*  $HB_P$  of  $P$  is the set of all possible ground versions of atoms, external atoms, and action atoms occurring in  $P$  obtained by replacing variables with constants from  $\mathcal{C}$ . Given a rule  $r \in P$ , the grounding  $grnd(r)$  of  $r$  is defined accordingly, the grounding of program  $P$  is given as the grounding of all its rules. Unless specified otherwise,  $\mathcal{C}$ ,  $\mathcal{X}$ ,  $\mathcal{G}$ , and  $\mathcal{A}$  are implicitly given by  $P$ .

An *interpretation*  $I$  relative to  $P$  is any subset  $I \subseteq HB_P$  containing ordinary atoms and action atoms. We say that  $I$  is a *model* of atom (or action atom)  $a \in HB_P$ , denoted by  $I \models a$ , iff  $a \in I$ . With every external predicate name  $\&g \in \mathcal{G}$ , we associate an  $(n+m+2)$ -ary Boolean function  $f_{\&g}$ , assigning each tuple  $(E, I, y_1, \dots, y_n, x_1, \dots, x_m)$  either 0 or 1, where  $n = in(\&g)$ ,  $m = out(\&g)$ ,  $x_i, y_j \in \mathcal{C}$ ,  $I \subseteq HB_P$ , and  $E$  is an environment. Note that this slightly generalizes the external atom semantics such that they may take  $E$  into account, which was left implicit in [2]. We say that an interpretation  $I$  relative to  $P$  is a *model* of a ground external atom  $a = \&g[y_1, \dots, y_n](x_1, \dots, x_m)$  wrt. environment  $E$ , denoted as  $I, E \models a$ , iff  $f_{\&g}(E, I, y_1, \dots, y_n, x_1, \dots, x_m) = 1$ . Let  $r$  be a ground rule. We define (i)  $I, E \models H(r)$  iff there is some  $a \in H(r)$  such that  $I, E \models a$ , (ii)  $I, E \models B(r)$  iff  $I, E \models a$  for all  $a \in B^+(r)$  and  $I, E \not\models a$  for all  $a \in B^-(r)$ , moreover (iii)  $I, E \models r$  iff  $I, E \models H(r)$  or  $I, E \not\models B(r)$ . We say that  $I$  is a *model* of  $P$  wrt.  $E$ , denoted by  $I, E \models P$ , iff  $I, E \models r$  for all  $r \in grnd(P)$ . The *FLP-reduct* of  $P$  wrt.  $I$  and  $E$ , denoted as  $fP^{I,E}$ , is the set of all  $r \in grnd(P)$  such that  $I, E \models B(r)$ . Eventually,  $I$  is an *answer set* of  $P$  wrt.  $E$  iff  $I$  is a  $\subseteq$ -minimal model of  $fP^{I,E}$ . We denote by  $\mathcal{AS}(P, E)$  the collection of all answer sets of  $P$  wrt.  $E$ .

The set of *best models* of  $P$ , denoted  $\mathcal{BM}(P, E)$ , contains those  $I \in \mathcal{AS}(P, E)$  that minimize the objective function  $H_P(I) = \sum_{a \in A} (\omega \cdot level(a) + weight(a))$ , where  $A \subseteq I$  is the set of action atoms in  $I$ , and  $\omega$  is the first limit ordinal. (This definition using ordinal numbers is equivalent to the definition of weak constraint semantics in [8].)

An action  $a = \#g[y_1, \dots, y_n]\{o, r\}[w : l]$  with option  $o$  and precedence  $r$  is *executable in  $I$  wrt.  $P$  and  $E$*  iff (i)  $a$  is brave and  $a \in I$ , or (ii)  $a$  is cautious and  $a \in B$  for every  $B \in \mathcal{AS}(P, E)$ , or  $a$  is preferred cautious and  $a \in B$  for every  $B \in \mathcal{BM}(P, E)$ . An *execution schedule* of a best model  $I$  is a sequence of all actions executable in  $I$ , such that for all action atoms  $a, b \in I$ , if  $prec(a) < prec(b)$  then  $a$  has a lower index in the sequence than  $b$ . We denote by  $\mathcal{ES}_{P,E}(I)$  the set of all execution schedules of a best model  $I$  wrt. acthex program  $P$  and environment  $E$ ; formally, let  $A_e$  be the set of action atoms that are executable in  $I$  wrt.  $P$  and  $E$ , then  $\mathcal{ES}_{P,E}(I) = \{[a_1, \dots, a_n] \mid prec(a_i) \leq prec(a_j), \text{ for all } 1 \leq i < j \leq n, \text{ and } \{a_1, \dots, a_n\} = A_e\}$ .

*Example 13.* In Example 12, if the robot has low battery, then  $\mathcal{AS}(P, E) = \mathcal{BM}(P, E)$  contains models  $I_1 = \{night, \#robot[clean, kitchen]\{c, 2\}, \#robot[goto, charger]\{b, 1\}\}$  and  $I_2 = \{day, \#robot[clean, bedroom]\{c, 2\}, \#robot[goto, charger]\{b, 1\}\}$ . We have  $\mathcal{ES}_{P,E}(I_1) = \{\#robot[goto, charger]\{b, 1\}, \#robot[clean, bedroom]c, 2\}$ .  $\square$

Given a model  $I$ , the *effect of executing a ground action*  $\#g[y_1, \dots, y_m]\{o, p\}[w : l]$  on an environment  $E$  wrt.  $I$  is defined for each action predicate name  $\#g$  by an associated  $(m+2)$ -ary function  $f_{\#g}$  which returns an updated environment  $E' = f_{\#g}(E, I, y_1, \dots, y_m)$ . Correspondingly, given an execution schedule  $S = [a_1, \dots, a_n]$  of a model  $I$ , the *execution outcome* of  $S$  in environment  $E$  wrt.  $I$  is defined as  $EX(S, I, E) = E_n$ , where  $E_0 = E$ , and  $E_{i+1} =$

$f_{\#g}(E_i, I, y_1, \dots, y_m)$ , given that  $a_i$  is of the form  $\#g[y_1, \dots, y_m]\{o, p\}[w : l]$ . Intuitively the initial environment  $E_0 = E$  is updated by each action in  $S$  in the given order. The set of possible execution outcomes of a program  $P$  on an environment  $E$  is denoted as  $\mathcal{EX}(P, E)$ , and formally defined by  $\mathcal{EX}(P, E) = \{EX(S, I, E) \mid S \in \mathcal{ES}_{P,E}(I) \text{ where } I \in \mathcal{BM}(P, E)\}$ .

In practice, one usually wants to consider a single execution schedule. This requires the following decisions during evaluation: (i) to select one best model  $I \in \mathcal{BM}(P, E)$ , and (ii) to select one execution schedule  $S \in \mathcal{ES}_{P,E}(I)$ . Finally, one can then execute  $S$  and obtain the new environment  $E' = EX(S, I, E)$ .

## 5.2 Rewriting IMPL to acthex

Using `acthex` for realizing IMPL is a natural and reasonable choice because `acthex` already natively provides several features necessary for IMPL: external atoms can be used to access information from a MCS, and `acthex` actions come with weights for creating ordered execution schedules for actions occurring within the same answer set of an `acthex` program. Based on this, IMPL can be implemented by a rewriting to `acthex`, with `acthex` actions implementing IMPL actions, `acthex` external predicates providing information about the MCS to the IMPL policy, and `acthex` external predicates realizing the value invention builtin predicates.

We next describe a rewriting from the IMPL core language fragment to `acthex`. We assume that the environment  $E$  contains a pair  $(\mathcal{A}, \mathcal{R})$  of sets of bridge rules, and an encoding of the MCS  $M$  (suitable for an implementation of the external atoms introduced below, e.g., in the syntax used by the MCS-IE system [3], which provide the corresponding policy input). A given IMPL policy  $P$  wrt. the MCS  $M$  is then rewritten to an `acthex` program  $P^{act}$  as follows.

1. Each core IMPL action  $@a(t)$  in the head of a rule of  $P$  is replaced by a brave `acthex` action  $\#a[t]\{b, 2\}$  with precedence 2. These `acthex` actions implement semantics of the respective IMPL actions according to Def. 4: interpretation  $I$  and the original action's argument  $t$  are used as input, the effects are accumulated as  $(\mathcal{A}, \mathcal{R})$  in  $E$ .
2. Each IMPL builtin  $\#id_k(C, c_1, \dots, c_k)$  in  $P$  is replaced by an `acthex` external atom  $\&id_k[c_1, \dots, c_k](C)$ . The family of external atoms  $\&id_k[c_1, \dots, c_k](C)$  realizes value invention and has as semantics function  $f_{\&id_k}(E, I, c_1, \dots, c_k, C) = 1$  for one constant  $C = auxc_{c_1} \dots c_k$  created from the constants in tuple  $c_1, \dots, c_k$ .
3. We add to  $P^{act}$  a set  $P_{in}$  of `acthex` rules containing (i) rules that use, for every  $p \in C_{res} \setminus \{modset\}$ , a corresponding external atom to 'import' a faithful representation of  $M$ , and (ii) a preparatory action  $\#reset$  with precedence 1, and a final action  $\#materialize$  with precedence 3:  $P_{in} = \{p(\mathbf{t}) \leftarrow \&p(\mathbf{t}) \mid p \in C_{res} \setminus \{modset\}\} \cup \{\#reset[]\{b, 1\}; \#materialize[]\{b, 3\}\}$ , where  $\mathbf{t}$  is a vector of different variables of length equal to the arity of  $p$  (i.e., one, two, or three).

The first two steps transform IMPL actions into `acthex` actions, and  $\#id_k$ -value invention into external atom calls. The third step essentially creates policy

input facts from `acthex` external sources. External atoms in  $P_{in}$  return a representation of  $M$  and analyze inconsistency in  $M$ , providing minimal diagnoses and minimal explanations. Thus, the respective rules in  $P_{in}$  yield an extension of the corresponding reserved predicates which is a faithful representation of  $M$ . Moreover, action `#reset` resets the modification  $(\mathcal{A}, \mathcal{R})$  stored in  $E$  to  $(\emptyset, \emptyset)$ .<sup>5</sup> Action `#materialize` materializes the modification  $(\mathcal{A}, \mathcal{R})$  (as accumulated by actions of precedence 2) in the MCS  $M$  (which is part of  $E$ ).

*Example 14 (ctd).* Policy  $P_3$  from Ex. 9 translated to `acthex` contains the following rules  $P_3^{act} = P_{in} \cup \{ \text{modset}(md, X) \leftarrow \text{diag}(X); \#guiSelectMod[md]\{b, 2\} \}$ .  $\square$

Note, that actions in the rewriting have no weights, therefore all answer sets are best models. For obtaining an admissible modification, any policy answer set can be chosen, and any execution schedule can be used.

**Proposition 1.** *Given a MCS  $M$ , a core IMPL policy  $P$ , and a policy input  $EDB_M$  wrt.  $M$ , let  $P^{act}$  be as above, and consider an environment  $E$  containing  $M$  and  $(\emptyset, \emptyset)$ . Then, every execution outcome  $E' \in \mathcal{EX}(P^{act} \cup EDB_M|_{B_A}, E)$  contains instead of  $M$  an admissible modification  $M'$  of  $M$  wrt.  $P$  and  $EDB_M$ .*

The proof of this correctness result can be found in the extended version [15].

## 6 Conclusion

Related to IMPL is the action language *IMPACT* [26], which is a declarative formalism for actions in distributed and heterogeneous multi-agent systems. *IMPACT* is a very rich general purpose formalism, which however is more difficult to manage compared to the special purpose language IMPL. Furthermore, user interaction as in IMPL is not directly supported in *IMPACT*; nevertheless most parts of IMPL could be embedded in *IMPACT*.

In the fields of access control, e.g., surveyed in [4], and privacy restrictions [13], policy languages have also been studied in detail. As a notable example, *PDL* [12] is a declarative policy language based on logic programming which maps events in a system to actions. *PDL* is richer than IMPL concerning action interdependencies, whereas actions in IMPL have a richer internal structure than *PDL* actions. Moreover, actions in IMPL depend on the content of a policy answer set. Similarly, inconsistency analysis input in IMPL has a deeper structure than events in *PDL*.

In the context of relational databases, logic programs have been used for specifying repairs for databases that are inconsistent wrt. a set of integrity constraints [14, 23, 24]. These approaches may be considered fixed policies without user interaction, like an IMPL policy simply applying diagnoses in a homogeneous MCS. Note however, that an important motivation for developing IMPL is the

<sup>5</sup> This reset is necessary if a policy is applied repeatedly.

fact that automatic repair approaches are not always a viable option for dealing with inconsistency in a MCS.

*Active integrity constraints (AICs)* [9–11] and *inconsistency management policies (IMPs)* [25] have been proposed for specifying repair strategies for inconsistent databases in a more flexible way. AICs extend integrity constraints by introducing update actions, for inserting and deleting tuples, to be performed if the constraint is not satisfied. On the other hand, an IMP is a function which is defined wrt. a set of functional dependencies mapping a given relation  $R$  to a ‘modified’ relation  $R'$  obeying some basic axioms.

Although suitable IMPL policy encodings can mimic database repair programs—AICs and (certain) IMPs—for specific classes of integrity constraints, there are fundamental conceptual differences between IMPL and the above approaches to database repair. Most notably, IMPL policies aim at restoring consistency by modifying bridge rules leaving the knowledge bases unchanged rather than considering a set of constraints as fixed and repairing the database. Additionally, IMPL policies operate on heterogeneous knowledge bases and may involve user interaction.

**Ongoing and Future Work.** Regarding an actual prototype implementation of IMPL, we are currently working on improvements of *acthex* which are necessary for realizing IMPL using the rewriting technique described in Sect. 5.2. In particular, this includes the generalization of taking into account the environment in external atom evaluation. Other improvements concern the support for implementing model and execution schedule selection functions.

An important feature of IMPL is the user interface for selecting or editing modifications. There the number of displayed modifications might be reduced considerably by grouping modifications according to nonground bridge rules. This would lead to a considerable improvement of usability in practice.

Also, we currently just consider bridge rule modifications for system repairs, therefore an interesting issue for further research is to drop this convention. A promising way to proceed in this direction is to integrate IMPL with recent work on managed MCSs [6], where bridge rules are extended such that they can arbitrarily modify the knowledge base of a context and even its semantics. Accordingly, IMPL could be extended with the possibility of using management operations on contexts in system modifications.

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