

# On the Security of the TLS Protocol: A Systematic Analysis

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**Abstract.** TLS is the most widely-used cryptographic protocol on the Internet. It comprises the TLS Handshake Protocol, responsible for authentication and key establishment, and the TLS Record Protocol, which takes care of subsequent use of those keys to protect bulk data. In this paper, we present the most complete analysis to date of the TLS Handshake protocol and its application to data encryption (in the Record Protocol). We show how to extract a key-encapsulation mechanism (KEM) from the TLS Handshake Protocol, and how the security of the entire TLS protocol follows from security properties of this KEM when composed with a secure authenticated encryption scheme in the Record Protocol. The security notion we achieve is a variant of the ACCE notion recently introduced by Jager et al. (Crypto '12). Our approach enables us to analyse multiple different key establishment methods in a modular fashion, including the *first proof* of the most common deployment mode that is based on RSA PKCS #1v1.5 encryption, as well as Diffie-Hellman modes. Our results can be applied to settings where mutual authentication is provided and to the more common situation where only server authentication is applied.

## 1 Introduction

TLS is the mostly widely used cryptographic protocol for secure communications on the Internet. The main purpose of TLS is to provide end-to-end security against an active, man-in-the-middle attacker. Originally deployed (as SSL) in web browsers for `https` connections, TLS is now used as a general purpose provider of secure communications to all kinds of applications: e-commerce transactions, virtual private networks (VPN), Android and iOS mobile apps [20, 21], as well as related protocols like DTLS [31, 37]. In short, TLS is one of the most important real-world deployments of cryptography.

**TLS in a Nutshell.** We begin with an informal high-level overview of the TLS protocol; a more detailed treatment is given in Section 2. The TLS protocol is executed between a client and a server. It has two main constituents: the Handshake Protocol, which is responsible for key establishment and authentication; and the Record Protocol, which provides a secure channel for handling the delivery of data. The Handshake Protocol establishes the application keys, which are in turn used to encrypt application

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data in the Record Protocol. The TLS specification offers multiple options for key establishment mechanisms in the Handshake Protocol and for symmetric key encryption schemes in the Record Protocol. The most common configuration, to which we refer as TLS-RSA, relies on RSA PKCS #1v1.5 encryption in the Handshake Protocol. Other configurations include TLS-DH and TLS-DHE, which rely on Diffie-Hellman key exchange (the first uses a static server's DH key and an ephemeral client's key while in the latter both parties contribute ephemeral DH keys). All these configurations provide server authentication, with optional client authentication in settings where clients possess public keys as well.

**Prior Work on TLS.** In view of its importance, TLS has long been the subject of intense research analysis, including, in chronological order, [41, 12, 36, 28, 25, 40, 16, 27, 5, 32, 22, 6, 33, 18, 35, 9, 2, 24, 30, 19, 13, 3, 10, 4]. The main, twin thrusts of this research have been to establish to what extent the TLS Handshake Protocol and the TLS Record Protocol are secure, for the respective tasks of key establishment and authentication and for providing a secure channel for delivery of data.

We now have a fairly complete understanding of the underlying cryptography for the Record Protocol, as studied in the works of Krawczyk [28] as well as Paterson, Ristenpart and Shrimpton [35]. These works demonstrated that, when carefully implemented to avoid timing and other attacks like those in [40, 16, 3], the stream-cipher and CBC encryption modes in the TLS Record Layer achieve the security notion of authenticated encryption; in fact, [35] puts forth and achieves a strengthening there-of, known as *stateful, length-hiding authenticated encryption* (sLHAE).

On the other hand, a complete analysis of the TLS Handshake Protocol remains elusive. A main obstacle is that the design of TLS violates the basic cryptographic principles of key indistinguishability and separation of key exchange and secure channels. This arises because the TLS Record Protocol overlaps with the TLS Handshake Protocol, and the application key is used to encrypt the last two messages of the Handshake Protocol (known as the *Finished* messages). As such, the TLS Handshake Protocol is deemed insecure by the existing security models for key exchange, initiated in the work of Bellare and Rogaway [8].

Several prior works [33, 25] circumvented this issue by analyzing *variants* of the TLS protocol (e.g. with a different message ordering, unencrypted *Finished* messages, or RSA-OAEP encryption). In particular, Morrissey, Smart and Warinschi [33] analyze the “Truncated TLS Handshake Protocol”, where the *Finished* messages are not encrypted by the application key. An important feature of [33] is the modularity of the approach. This conceptually simplifies the protocol and the security proofs, and points the way forward for subsequent analysis. However, the end result applies to truncated TLS and not to the real protocol. In addition, Morrissey et al. [33] model TLS-RSA under the assumption that RSA encryption is replaced with CCA-secure encryption which is provably false for RSA PKCS #1v1.5 encryption as used in TLS-RSA. The modularity theme from [33] is developed further in recent work by Brzuska et al. [13], who analyze the TLS protocol using a game-based framework that is designed to enable compositional results to be proved, but their analysis of TLS-RSA assumes IND-CCA security for the RSA encryption, which, again, is known not to hold. Thus,

unfortunately, given the high sensitivity of key exchange protocols in general (and TLS in particular) to small details, these results tell us little about TLS as used in practice.

In recent work, Jager et al. [24] put forth a new security notion — Authenticated and Confidential Channel Establishment (ACCE) security — which captures the desired security guarantees when the TLS Handshake and Record Protocols are used in tandem. (This circumvents the barrier pertaining to the separation of key exchange and secure channels.) In addition, they showed that the cryptographic core of the TLS-DHE protocol when both server and client authentication are applied satisfies ACCE security. Informally, this means the TLS Record Protocol when used with TLS-DHE as the Handshake Protocol constitutes a secure channel and guarantees authentication and privacy for data delivery between the server and the client. While this work constitutes a significant step forward in terms of realistic modeling and analysis of TLS, the TLS-DHE protocol is (currently) seldom used in practice, and client-side authentication via signatures is very rarely done.

Additional literature on analyzing the TLS Handshake Protocol include works on symbolic models, e.g. [36, 22, 9] and on security analysis of a TLS implementation via type-checking [10]. Works on simulation-based definitions and designs for key agreement and secure channel protocols include [39, 14, 15].

**TLS-RSA.** As noted earlier, the most commonly deployed mode of TLS, namely TLS-RSA, uses RSA PKCS #1v1.5 encryption [26]. In 1998, Bleichenbacher discovered a devastating man-in-the-middle attack on SSL, the predecessor of TLS. Specifically, Bleichenbacher presented a chosen-ciphertext attack on RSA PKCS #1v1.5 encryption [12], which in turn allows a man-in-the-middle adversary against SSL to recover the pre-master secret and thence the application keys. In fact, the attack only requires a ciphertext validity oracle. TLS, the successor to SSL, incorporates an *ad hoc fix* to thwart Bleichenbacher’s attack: decryption failures are hidden from the adversary, including via some defences against timing attacks, thereby removing access to the ciphertext validity oracle.

For over a decade, the TLS Handshake Protocol (and in particular TLS-RSA) has largely resisted attacks; however, that in itself does not rule out the possibility of an attack being discovered in future. The folklore belief is that TLS-RSA is secure if we replace RSA PKCS #1v1.5 with RSA-OAEP or any other CCA-secure encryption scheme; unfortunately, only RSA PKCS #1v1.5 is standardised in TLS and used in practice. This begs the question:

*Is TLS-RSA with RSA PKCS #1v1.5 encryption ACCE secure?*

A partial answer to the above question was provided in the work of Jonsson and Kaliski Jr. [25]: they showed that RSA PKCS #1v1.5 encryption when augmented with the *unencrypted* TLS client Finished message is CCA-secure. However, their analysis was not extended to either the TLS Handshake Protocol or the full TLS protocol; furthermore, in TLS the client Finished message is actually encrypted with the application key. We stress that RSA PKCS #1v1.5 encryption when augmented with the *encrypted* TLS client Finished message is not even a CPA-secure key-encapsulation mechanism (KEM), for the same reason that the TLS Handshake Protocol violates key indistinguishability.

**Proving Security of TLS-RSA and Beyond.** We provide an affirmative answer to the above question, namely, we provide the first proof of security for the *unmodified* TLS-RSA protocol with RSA PKCS #1v1.5 encryption in the commonly deployed setting of server-only authentication. More generally, we provide a systematic and modular analysis of the different modes of TLS, which include TLS-RSA, TLS-DH and TLS-DHE, in both the common setting of server-only authentication as well as with combined client and server authentication. We also validate the folklore belief that TLS Handshake with RSA replaced with any CCA-secure public-key encryption scheme (e.g., RSA-OAEP) is secure. We refer to such an instantiation as TLS-CCA. Following Jager et al. [24], we focus on the *cryptographic core* of TLS (see the full version [29] for a discussion of what we omit). We concentrate on achieving ACCE security with appropriate modifications to handle server-only authentication (in which case we speak of SACCE security). We next present an overview of our framework, summarized in Figure 1.

### 1.1 Systematic Analysis of All TLS Handshake Modes

**Our Framework.** We build an abstraction of the TLS Handshake Protocol via a generic representation using a *key-encapsulation mechanism (KEM)* (see Figure 2). Each of the TLS modes is then fully defined via a specific instantiation of the KEM. The goal is to find sufficient conditions on the KEM so that any instantiation satisfying these conditions immediately leads to a secure protocol in the sense of ACCE security (as discussed above). This approach has its roots in the work of Jonsson and Kaliski [25] that studied the underlying KEM in TLS-RSA.

We formalize this statement using the existing notion of constrained CCA (CCCA) security, introduced by Hofheinz and Kiltz [23] in the context of hybrid encryption. In the CCCA security game, the adversary is provided with a “constrained decryption oracle” that takes as input a pair  $(C, T)$  where  $C$  is a ciphertext and  $T$  is some auxiliary information; the oracle returns the decryption  $K$  of  $C$  if  $C$  is different from the challenge ciphertext and  $(K, T)$  satisfies some specified predicate, and  $\perp$  otherwise. In particular, if the oracle returns  $\perp$ , the adversary does not learn whether it is because  $K$  is  $\perp$  or because  $(K, T)$  fails to satisfy the predicate. In our framework, we consider CCCA security where  $T$  is an encrypted TLS client Finished message, and the predicate enforces validity of  $T$ . Now, if the constrained decryption oracle returns  $\perp$  on query  $(C, T)$ , the adversary does not learn whether it is because  $C$  is an invalid ciphertext or because  $T$  is an invalid Finished message – this precisely captures the intention of the TLS fix for thwarting Bleichenbacher’s attack! We note that the challenge ciphertext in the CCCA security experiment is not accompanied by the corresponding Finished message; this asymmetry between the challenge ciphertext and the oracle queries allows us to bypass the key indistinguishability barrier in TLS.

**ACCE Security from CCCA Security.** Our first result says that if the key encapsulation mechanism in the TLS Handshake Protocol satisfies CCCA security and the encryption scheme used in the TLS Record Protocol is sLHAE-secure, then TLS is ACCE secure, in the server-only authentication setting. We stress that this result is in the standard model. Importantly, the CCCA security game is conceptually and technically

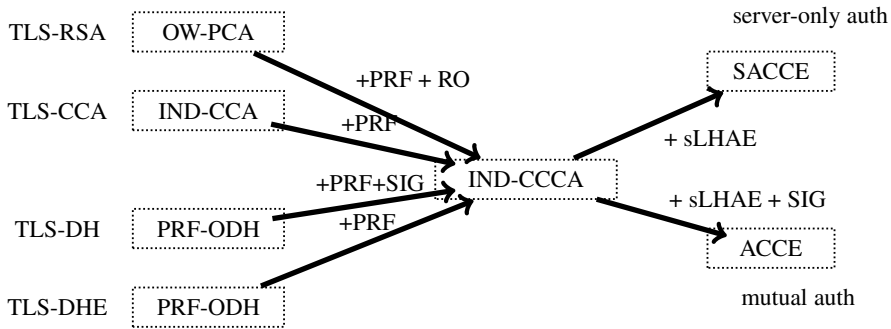


Fig. 1. Summary of our results

much simpler to analyze than the whole TLS protocol, as we do not have to worry about multiple sessions, nonces, or the multiple message flows in the full protocol.

To establish ACCE security, we need to achieve security against a (concurrent) man-in-the-middle adversary communicating with multiple honest clients and multiple honest servers. Roughly speaking, we will rely on the constrained decryption oracle in CCCA security to simulate the honest servers. The main technical difficulty in establishing this result arises when a man-in-the-middle adversary plays a relaying strategy between an honest server and client and then mauls the client’s encrypted Finished message. Here, we cannot rely on the constrained decryption oracle to simulate the honest server’s response because the adversary is using the challenge ciphertext. Moreover, we cannot immediately appeal to the non-malleability of the sLHAE-secure scheme used to encrypt the Finished message since the protocol messages leak information about the application key. To solve this problem, we exploit the fact that the CCCA security game provides us with a real-or-random key  $K^*$ , which we may use to decrypt and verify the client’s encrypted Finished message for this specific adversarial strategy. We stress that this technical difficulty goes away if the client’s Finished message is unencrypted, because the prior transcript uniquely determines an accepting Finished message.

**CCCA Security in the TLS Handshake.** Our second set of results says that the key encapsulation mechanisms underlying the TLS-RSA, TLS-CCA, TLS-DH, and TLS-DHE variants of the TLS Handshake Protocol all satisfy CCCA security. Combined with our first result, this yields ACCE security of TLS-RSA, TLS-CCA, TLS-DH and TLS-DHE (see Figure 1).

**ACCE Security of TLS with Mutual Authentication.** We extend the above results, developed for the case of server-only authentication, to the case of mutual authentication, namely, when the client authenticates itself via a digital signature. We show that also in this setting, CCCA security of the underlying KEM implies ACCE security with both server and client authentication. The extension is relatively straightforward (a positive feature!) requiring minor changes to the server-authentication-only proofs of server authentication and channel security, and the addition of a client authentication

proof. The resultant analysis is generic and independent of the different underlying KEM instantiations, thus it directly applies to TLS-RSA, TLS-CCA, TLS-DH and TLS-DHE (demonstrating the power of our modular analysis).

## 1.2 Summary of Results

As a result of the above methodology we obtain proofs of ACCE security for the TLS handshake protocol for *all* of the above TLS modes, both in the common setting of server-only authentication as well as with mutual authentication. These results are depicted in Figure 1 and are enumerated here with the assumptions used in each case. In all cases we assume a secure PRF and the TLS Record Protocol encryption implemented with an sLHAE encryption scheme. For the case of ACCE security with mutual authentication a secure client signature is also assumed. Certificates for both servers and clients are assumed to be provided by a minimally trusted CA that faithfully checks identities before issuing certificates. No other checks from the CA (such as proofs of possession, uniqueness of public keys, etc.) are assumed.

**TLS-RSA.** We obtain the first proof of security of TLS-RSA as deployed in practice, with RSA PKCS #1v1.5 and server-only authentication, in the random oracle model and under the assumption that RSA PKCS #1v1.5 is OW-PCA secure. The latter assumption, formalized in Section 5, states that inverting the encryption function is hard even given an oracle that on input a plaintext-ciphertext pair  $(K, \psi)$  checks whether the decryption of  $\psi$  equals  $K$  (for  $K \neq \perp$ ). The OW-PCA security of RSA PKCS #1v1.5 can be proven under an RSA-like assumption, known as “partial-domain RSA with decision oracle”, introduced by Jonsson and Kaliski in [25] and which we present in Section 5.2. We refer to [25] for a discussion on why this assumption is reasonable for typical parameters used in TLS; to the best of our knowledge no weakness in this assumption has been discovered since its introduction in [25]. When clients authenticate in TLS-RSA using digital signatures then full ACCE (i.e. with mutual authentication) is proven assuming a secure signature scheme. We stress that TLS-RSA is the only TLS mode whose proof is in the random oracle model; we prove all other modes in the standard model.

**TLS-CCA.** We prove that when instantiated with a CCA-secure public-key encryption scheme (instead of RSA PKCS #1v1.5), TLS is ACCE secure in the standard model. While no such schemes are currently standardised for TLS, this result confirms the intuition that IND-CCA security is the “right” target for the public key encryption scheme used in TLS. It also means that, should the current RSA-based encryption scheme used in TLS ever be replaced by a CCA-secure one, for example RSA-OAEP, then our analysis will immediately provide strong security guarantees for the protocol.

**TLS-DH and TLS-DHE.** We prove ACCE security (with and without client authentication) of TLS-DH in the standard model under the PRF-ODH assumption introduced in [24].<sup>1</sup> The PRF-ODH assumption rules out some potential related-key attacks on the

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<sup>1</sup> The assumption is a variant of the ODH assumption from [1] where the oracle is implemented via a PRF rather than by a hash function. In the proof of TLS-DH we require security against multiple oracle queries while for TLS-DHE a single query suffices, as was the case in [24].

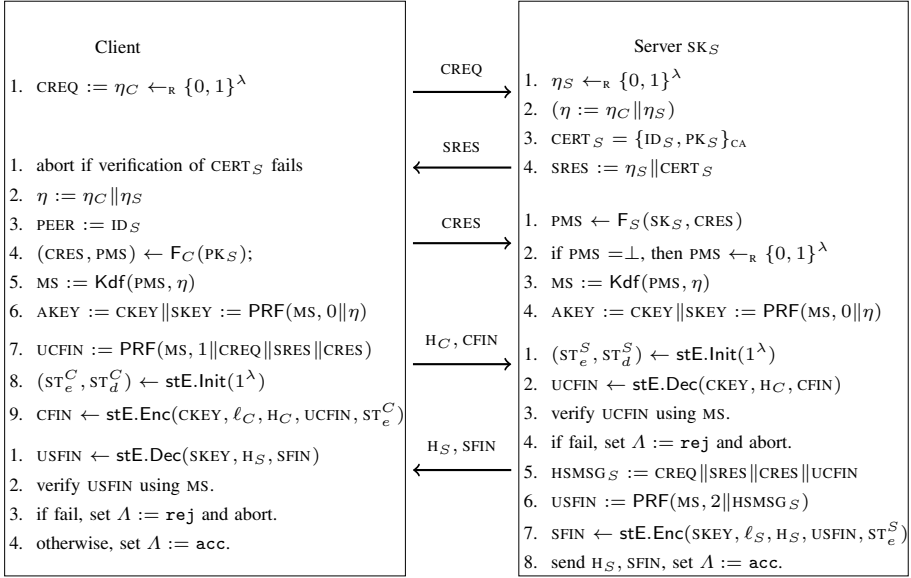
Kdf function that would render the protocol insecure. In the full version [29] we show this assumption to be *provably necessary* for the security of TLS-DH, showing attacks on the protocol with PRFs for which the assumption does not hold. We note that we can also prove TLS-DH in the random oracle model under the Strong DH assumption. Finally, we obtain security for TLS-DHE as a corollary of our results for TLS-DH security, under the PRF-ODH assumption as well as secure signatures for servers (and clients in the case of mutual authentication). Note that our results for TLS-DHE do not encompass forward security, but this is guaranteed by the results of [24].

## 2 The TLS Handshake Protocol with Server-Only Authentication

In this section, we present our model of the TLS Handshake Protocol when no client authentication takes place. As noted in the introduction, this includes TLS-RSA, the most common usage of the TLS protocol. The parties to the protocol are a client  $C$  and a server  $S$ . Each maintains an internal state variable  $ST$  and  $A \in \{\emptyset, acc, rej\}$ . The protocol makes use of a number of cryptographic components: a key derivation function (KDF)  $Kdf$ , a pseudorandom function PRF, a stateful authenticated encryption with associated data (AEAD) scheme  $stE = (stE.Gen, stE.Init, stE.Enc, stE.Dec)$ , and a KEM ( $KeyGen, F_C, F_S$ ). The protocol is shown schematically in Figure 2. We also describe below how the keys established by this protocol are subsequently used by the TLS Record Protocol.

The model is derived from the current TLS specification [17], and we believe that our model captures the *cryptographic core* of TLS. It has a comparable level of accuracy to the model of TLS-DHE used in [24]. We highlight several salient properties of our model, and defer a detailed justification and discussion to the full version [29]:

- We assume that the ciphersuites, KDF, PRF and the stateful AEAD scheme, are fixed once and for all. We do not model ciphersuite negotiation/renegotiation, nor session resumption. In particular, this means that, while our treatment covers multiple ciphersuites (such as those based on RSA key transport and various Diffie-Hellman (DH) ciphersuites) in a modular fashion, our analysis currently does not treat the case where different protocols runs may negotiate different ciphersuites. This requires the application of a suitable composability framework that is beyond the immediate scope of this paper.
- In the case of TLS-RSA,  $(KeyGen, F_C, F_S)$  represents the algorithms of the RSA PKCS#1v1.5 encryption scheme (c.f. Section 5.2). The specifics of this encoding were analysed in detail in [12, 25]. For this mode, we assume that the outcome of processing CRES at the server end is completely hidden from the adversary. Such an assumption is necessary; otherwise, TLS-RSA is susceptible to Bleichenbacher’s attack [12]. Formally, we model this by treating  $CRES || CFIN$  as a monolithic message in the proof of security.
- Our generic description includes the TLS-DH mode, where the server has a certificate on a static DH key  $PK_S$  and DH key exchange is used to establish PMS. Here  $(CRES, PMS) \leftarrow F_C(PK_S)$  denotes the client’s computation of an ephemeral DH value (CRES) and the pre-master secret (PMS);  $PMS \leftarrow F_S(SK_S, CRES)$  denotes the corresponding computation on the server side. In this situation, we may



**Fig. 2.** Basic Generic TLS Handshake Protocol Parameterized by  $(KeyGen, F_C, F_S)$

alternatively think of  $(KeyGen, F_C, F_S)$  as being the algorithms of a Diffie-Hellman (or Elgamal-type) KEM based on public key  $PK_S$ . See Section 6. Specifically, with appropriate choices of Diffie-Hellman groups, our analysis covers the DH\_DSS, DH\_RSA, ECDH\_ECDSA, and ECDH\_RSA key exchange methods from [17, 11]; here the suffix DSS/RSA/ECDSA has no meaning since the server does not sign in this mode.

- By suitably extending  $CERT_S$  to include the server’s signature on its choice of ephemeral DH value, our description captures the TLS-DHE mode, where now  $PK_S$  is a signature verification key and  $PMS$  is the result of a DH key exchange based on the ephemeral values chosen by client and server. This then covers the DHE\_DSS, DHE\_RSA, ECDHE\_ECDSA, and ECDHE\_RSA key exchange methods from [17, 11], where the suffix DSS/RSA/ECDSA refers to the signature scheme used by the server.
- Our description also captures TLS-CCA, where  $(KeyGen, F_C, F_S)$  represents the algorithms of an IND-CCA-secure encryption scheme, such as RSA-OAEP.
- For notational simplicity, we use the same symbol  $\lambda$  to denote the security parameter, as well as the bit length of  $PMS, MS, CKEY$  and  $SKEY$ .

**TLS Record Protocol.** A party that concludes the TLS Handshake protocol successfully continues to use the application key  $AKEY = CKEY \parallel SKEY$  in the TLS Record Protocol. Specifically, the client uses  $CKEY$  to encrypt messages to the server, and the server uses the same key  $CKEY$  to decrypt these messages. Similarly, the server uses  $SKEY$  to encrypt messages to the client, and the client uses the same key  $SKEY$  to



decrypt these messages. As noted above, the client and server `Finished` messages are already encrypted in this way. As in [24], we model the TLS Record Protocol via a stateful AEAD scheme `stE` which we will assume to be sLHAE-secure in the sense of [35]. For further details, see the full version [29].

### 3 Authenticated and Confidential Channel Establishment (ACCE)

We begin with the definition of *authenticated and confidential channel establishment (ACCE)* from [24, 8]. We will describe the syntax for a general ACCE protocol but for security, we consider a specialization to the setting where only the server is authenticated – we call this *server-only authenticated and confidential channel establishment (SACCE)*.

**ACCE Protocol.** An ACCE protocol is a protocol executed between two parties, a client and a server. In the original description [24], an ACCE protocol has two distinct phases, called the ‘pre-accept’ phase and the ‘post-accept’ phase, corresponding to whether a party has accepted a session key in a particular session or not. We dispense with this distinction (though it is still expressed in our security model by making the queries that are available to the adversary depend on an oracle’s acceptance state). The parties in the protocol first compute as the session key an application key `AKEY`. Then, encrypted and authenticated data is transmitted using a symmetric encryption scheme with the application key `AKEY`. More specifically, `AKEY` is parsed as `CKEY||SKEY`, the client uses `CKEY` in a stateful AEAD scheme `stE` to send data to the server, and the server uses `SKEY` in `stE` to protect data sent to the client. Henceforth, we will only refer to application keys and not to session keys. Parties also maintain internal state  $\Lambda$ , and clients keep an additional `PEER` variable. We assume that an ACCE protocol is such that, when a party reaches the state  $\Lambda = \text{acc}$ , it has already computed an application key `AKEY` and executed `stE.Init`. TLS meets this requirement.

#### 3.1 Execution Environment

**Protocol Entities.** Following [24, 8], we consider a set of parties  $\mathcal{P} = \mathcal{S} \cup \mathcal{C}$ , where  $\mathcal{S}$  and  $\mathcal{C}$  are disjoint and each party  $P \in \mathcal{P}$  is a (potential) protocol participant. Moreover, each  $P \in \mathcal{S}$  (the servers) have a *unique* key pair  $(\text{PK}_P, \text{SK}_P)$ , an identity  $\text{ID}_P \in \{0, 1\}^\lambda$  along with a certificate  $\text{CERT}_P := (\text{ID}_P, \text{PK}_P)_{\text{CA}}$  signed by a certification authority  $\text{CA}$ . We also assume that all the parties in  $\mathcal{S}$  have distinct identities.

**Session Oracles.** To model several sequential and parallel executions of the protocols and sessions, each party  $P$  maintains a collection of oracles  $\{\pi_1^P, \pi_2^P, \dots\}$ . The oracle  $\pi_i^P$  models party  $P$  executing a single instance of a protocol in “session”  $i$ . We stress that the session numbers  $i$  are just an artefact of our security game – they are designed to provide a means for the adversary to deliver messages to different sessions at different parties. In particular, the protocols and oracles need not even be “aware” of what their session numbers are (i.e. those numbers need not form part of the state).

Each oracle  $\pi_i^P$  maintains as internal state a set of variables comprising:

- $\Lambda \in \{\emptyset, \text{acc}, \text{rej}\}$ ;
- $\text{AKEY} = \text{CKEY} \parallel \text{SKEY} \in \{0, 1\}^{2\lambda}$ , where  $\{0, 1\}^{2\lambda}$  is the application key space of the protocol;
- if  $P \in \mathcal{C}$ , then it has an additional  $\text{PEER}$  variable to denote the intended partner (only client oracles have the  $\text{PEER}$  variable because only servers have identities);
- if  $P \in \mathcal{S}$ , then  $\pi_i^P$  also knows the party identity  $\text{ID}_P$ .

The internal state of each oracle is initialized to  $(\Lambda, \text{AKEY}, \text{PEER}) = (\emptyset, \emptyset, \emptyset)$ , where  $\emptyset$  denotes undefined.

**Adversarial Queries.** The adversary interacts with the oracles via the following queries:

$\text{Send}(\pi_i^P, m)$ : the adversary uses this query to send a message  $m$  to oracle  $\pi_i^P$ ; the oracle will respond with an outgoing message according to the protocol specification and its internal state. If  $\pi_i^P$  has reached state  $\Lambda = \text{acc}$ , then it replies with  $\perp$ . When the attacker asks the first  $\text{Send}$ -query to an oracle  $\pi_i^C$  where  $C \in \mathcal{C}$ , the oracle checks whether  $m$  is a special “Initiate client session” symbol  $\top$ , and if so, responds with the first protocol message (which will be a fresh client nonce). The variables  $\Lambda, \text{AKEY}$  are also set according to the protocol specification.

$\text{Reveal}(\pi_i^P)$ : the oracle  $\pi_i^P$  responds with the contents of the application key  $\text{AKEY}$ . Note that this query can be issued to  $\pi_i^P$  before it has reached state  $\Lambda = \text{acc}$ .

$\text{Encrypt}(\pi_i^P, \ell, \text{H}, m_0, m_1)$ : if  $\pi_i^P$  has *not* reached state  $\Lambda = \text{acc}$ , this oracle returns  $\perp$ . Otherwise, prior to reaching state  $\text{acc}$ ,  $\pi_i^P$  has (by assumption) computed  $\text{AKEY}$  and run the  $\text{stE.Init}$  algorithm of a stateful AEAD scheme  $\text{stE} = (\text{stE.Gen}, \text{stE.Init}, \text{stE.Enc}, \text{stE.Dec})$  to define states  $\text{ST}_e, \text{ST}_d$  specific to the oracle  $\pi_i^P$ ; the game also samples a random bit  $b_i^P$  at this point, parses  $\text{AKEY}$  as  $\text{CKEY} \parallel \text{SKEY}$ , and adds the 5-tuple  $(\text{ST}_e, \text{ST}_d, b_i^P, \text{CKEY}, \text{SKEY})$  to the oracle state  $\text{ST}$ . Now, when receiving the  $\text{Encrypt}$  query, the message  $m_{b_i^P}$  is encrypted along with header data  $\text{H}$  using algorithm  $\text{stE.Enc}$  and key  $K = \text{CKEY}$  (if  $P \in \mathcal{C}$ ) or key  $K = \text{SKEY}$  (if  $P \in \mathcal{S}$ ) to form a ciphertext of length  $\ell$ , and to update the encryption state  $\text{ST}_e$ . The resulting ciphertext is returned to the adversary. For details, see Figure 3.

$\text{Decrypt}(\pi_i^P, \text{H}, c)$ : this query is intended to allow the adversary to decrypt ciphertexts that would be processed by the communication partner of the oracle  $\pi_i^P$  (a server  $S$  if  $P \in \mathcal{C}$ , and a client  $C$  if  $P \in \mathcal{S}$ ). When  $b_i^P = 0$ , the response is always  $\perp$ ; when  $b_i^P = 1$ , this query involves the decryption of  $\text{H}$  and  $c$  using algorithm  $\text{stE.Dec}$  and the appropriate key  $K$  obtained from  $\text{ST}$  at the oracle: if  $P \in \mathcal{C}$ , this will be  $\text{CKEY}$ , and if  $P \in \mathcal{S}$ , then it will be  $\text{SKEY}$ . The resulting message (or failure symbol  $\perp$ ) is returned if the query is “out-of-sync”. For details, see Figure 3.

**Certificate Authority.** We assume that there is a single certificate authority (CA), which uses a secure signature scheme  $\text{casig}$  and its public key is distributed to all the clients. For each  $S \in \mathcal{S}$  with public key  $\text{PK}_S$ , the CA signs the pair  $(\text{ID}_S, \text{PK}_S)$  to

<p> <math>\text{Encrypt}(\pi_i^P, \ell, H, m_0, m_1)</math>:  <math>u \leftarrow u + 1</math>  <math>(c^0, \text{ST}_e^0) \leftarrow_{\text{R}} \text{stE.Enc}(K, \ell, H, m_0, \text{ST}_e)</math>  <math>(c^1, \text{ST}_e^1) \leftarrow_{\text{R}} \text{stE.Enc}(K, \ell, H, m_1, \text{ST}_e)</math>                      If <math>c_i^0 = \perp</math> or <math>c_i^1 = \perp</math> then return <math>\perp</math>                      Set <math>c_u = c^{b_i^P}</math>, <math>H_u = H</math> and <math>\text{ST}_e = \text{ST}_e^{b_i^P}</math>                      Ret <math>c_u</math> </p>	<p> <math>\text{Decrypt}(\pi_i^P, H, c)</math>:                      If <math>b_i^P = 0</math> then Ret <math>\perp</math>  <math>v \leftarrow v + 1</math>  <math>(m, \text{ST}_d) \leftarrow \text{stE.Dec}(K, H, c, \text{ST}_d)</math>                      If <math>v &gt; u</math> or <math>c \neq c_v</math> or <math>H \neq H_v</math> then phase <math>\leftarrow 1</math>                      If phase = 1 then Ret <math>m</math>                      Ret <math>\perp</math> </p>
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**Fig. 3.** The Encrypt and Decrypt oracles in the ACCE security game

provide a certificate  $\text{CERT}_S := (\text{ID}_S, \text{PK}_S)_{\text{CA}}$ . We also allow the adversary access to the CA to register any number of parties, not in the set  $\mathcal{S}$ , with any public key of the adversary's choice.

**Matching Conversations.** We consider a definition of matching conversation which is specific to TLS (and differs from the one in [24]):

**Definition 1 (Matching conversations).** We say that  $\pi_i^P$  has a matching conversation with  $\pi_j^{P'}$  if (i) either  $P \in \mathcal{C}$  and  $P' \in \mathcal{S}$ , or  $P \in \mathcal{S}$  and  $P' \in \mathcal{C}$ ; and (ii)  $\pi_i^P$  accepts; and (iii) the transcripts at both  $\pi_i^P$  and  $\pi_j^{P'}$  begin with the same three messages (CREQ, SRES, CRES).

*Remark 1.* Defining matching conversations as above means that we may treat the vector (CREQ, SRES, CRES) as a post-specified session identifier. Observe that these three messages uniquely determine the parties' nonces and server's identity as well as the key PMS which in turn determines the application keys. In addition, these three messages determine the client's Finished message, as well as the server's Finished message if the server reaches the accept state.

### 3.2 Correctness and Security

**Correctness.** For every honest  $C \in \mathcal{C}$  and  $S \in \mathcal{S}$ , if two sessions  $\pi_i^C, \pi_j^S$  have matching conversations with each other, then we require that they have the same application key AKEY and  $\pi_i^C$  has its PEER variable set to  $\text{ID}_S$ . We also require that the encryption scheme stE used to model the secure channel is correct.

**SACCE Security.** Security of an ACCE protocol with server-only authentication (SACCE) is defined by requiring that (i) the protocol provides server authentication (but with no guarantee of client authentication, and that (ii) the subsequent use of the application keys in the stateful AEAD scheme stE provides stateful Length Hiding Authenticated Encryption (sLHAE), as per [35]. We consider a game played between the adversary  $\mathcal{A}$  and a challenger. This game is obtained by adapting [24, Definition 7] to our setting. At the beginning of the game, the challenger generates the long-term key-pair  $(\text{PK}_S, \text{SK}_S)$  along with the certificate  $\text{CERT}_S := (\text{ID}_S, \text{PK}_S)_{\text{CA}}$  for all  $S \in \mathcal{S}$  and gives all the certificates to  $\mathcal{A}$  as input. Now the adversary issues a sequence of queries

defined before. The challenger answers all queries to  $\pi_i^C$  by running the honest client protocol, and all queries to  $\pi_j^S$  by running the honest server protocol using the key  $SK_S$ . The challenger will also provide certificates along with signatures to the adversary for any identities outside the set  $\{ID_S : S \in \mathcal{S}\}$ .

**Advantage Measures.** We associate to an adversary  $\mathcal{A}$  against an ACCE protocol  $\Pi$  two advantage measures:

- (server authentication, i.e. client accepts  $\Rightarrow$  matching conversations.)  
 $\text{Adv}_{\Pi}^{\text{sacce-sa}}(\mathcal{A})$  is the probability that when  $\mathcal{A}$  terminates, there is a (honest) client  $C$  and oracle  $\pi_i^C$  that reaches an accept state with honest  $\text{PEER} = ID_S$ , but there is no unique oracle  $\pi_j^S$  for which  $\pi_i^C$  has had a matching conversation with  $\pi_j^S$ .
- (channel security.)  
 $\text{Adv}_{\Pi}^{\text{sacce-ae}}(\mathcal{A})$  is defined to be  $p - 1/2$ , where  $p$  is the probability that  $\mathcal{A}$  outputs  $(P, i, b')$  such that  $b' = b_i^P$  where  $b_i^P$  is set during the  $\text{Encrypt}(\pi_i^P, \dots)$  query and we define  $b'$  to be  $\perp$  unless the following conditions hold: (i)  $\pi_i^P$  reaches an accept state; (ii)  $\pi_i^P$  is not the subject of a Reveal query, and if there is an oracle  $\pi_j^{P'}$  with which  $\pi_i^P$  has a matching conversation then  $\pi_j^{P'}$  is not the subject of a Reveal query either; and (iii)  $P \in \mathcal{C}$ .

**Definition 2 (SACCE-secure).** We say that an ACCE protocol  $\Pi$  is SACCE-secure if  $\Pi$  satisfies correctness, and for all PPT adversaries  $\mathcal{A}$ , both  $\text{Adv}_{\Pi}^{\text{sacce-sa}}(\mathcal{A})$  and  $\text{Adv}_{\Pi}^{\text{sacce-ae}}(\mathcal{A})$  are a negligible function of the security parameter  $\lambda$ .

## 4 From CCCA KEM Security to SACCE Security of TLS

In this section we state the following theorem which is our core intermediate result for proving ACCE security of all TLS modes. It uses the notion of CCCA security and the definition of the TLS KEM  $\text{tlkem}$  introduced below in Sections 4.1 and 4.2, respectively.

**Theorem 1.** *If  $\text{tlkem}$  is IND-CCCA secure,  $\text{casig}$  is an existentially unforgeable signature scheme and  $\text{stE}$  is sLHAE-secure then TLS is SACCE-secure.*

The IND-CCCA security of the KEMs arising from all TLS modes (and hence the SACCE security of these modes) is shown in the subsequent sections.

### 4.1 IND-CCCA Security

We consider a variant of IND-CCCA security from [23]:

**Definition 3 (IND-CCCA).** For a stateful adversary  $\mathcal{A}$ , an LKEM  $\text{lkem}$  and a predicate  $\text{pred}$ , we define the advantage function

$$\text{Adv}_{\text{lkem}, \text{pred}}^{\text{ind-ccca}}(\mathcal{A}) := \Pr \left[ \begin{array}{l} (\text{PK}, \text{SK}) \leftarrow \text{KeyGen}(1^\lambda); \\ L^* \leftarrow \mathcal{A}^{\text{CDec}(\text{SK}, \cdot, \cdot)}(\text{PK}); \\ b = b' : (C^*, K^*) \leftarrow \text{Enc}(\text{PK}, L^*); \\ K_0 := K^*; K_1 \leftarrow_{\text{R}} \{0, 1\}^\lambda; b \leftarrow_{\text{R}} \{0, 1\}; \\ b' \leftarrow \mathcal{A}^{\text{CDec}(\text{SK}, \cdot, \cdot)}(C^*, K_b) \end{array} \right] - \frac{1}{2}$$

with the restriction that (1)  $L^*$  must be different from all previously queried  $L$ , and (2) the restriction on the decryption oracle for queries after getting the challenge ciphertext is  $(L, C) \neq (L^*, C^*)$ ; and where the “constrained” decryption oracle  $\text{CDec}$  is given by:

$$\begin{aligned} & \text{CDec}(\text{SK}, L, C, T) : \\ & K \leftarrow_{\text{R}} \text{Dec}(\text{SK}, L, C) \\ & \text{if } K = \perp \text{ or } \text{pred}(K, T) = 0 \text{ then return } \perp \\ & \text{else return } K \end{aligned}$$

A LKEM  $\text{lkem}$  is said to be IND-CCCA-secure if for all PPT adversaries  $\mathcal{A}$ , the advantage  $\text{Adv}_{\text{lkem}, \text{pred}}^{\text{ind-ccca}}(\mathcal{A})$  is a negligible function in  $\lambda$ .

*Remark 2 (comparison with [23]).* We point out the differences between our formulation and that in [23]. First, we consider a setting with labels. Second, in [23], the predicate is specified by the adversary via a circuit. Here, we consider a fixed predicate that takes an additional input  $T$ . To capture the prior formulation, the predicate would be circuit evaluation and  $T$  would be a circuit. Third, by fixing the predicate, we avoid having to explicitly consider plaintext uncertainty.

## 4.2 The TLS Labeled KEM

Following [25], we describe a labeled KEM which is extracted from the TLS protocol. Unlike [25] which stopped at analyzing (labeled) CCA-security of the ensuing scheme for the RSA mode of TLS, we show how to derive SACCE security of TLS (for any mode) based on the IND-CCCA security of the labeled KEM. We then prove this IND-CCCA property to hold for the KEMs arising in various TLS modes, namely TLS-RSA, TLS-CCA, TLS-DH, and TLS-DHE.

**LKEMs from TLS.** Given a generic TLS protocol parameterized by  $(\text{KeyGen}, F_C, F_S)$  (see Fig. 2) along with cryptographic components  $\text{Kdf}$  and  $\text{PRF}$ , we consider the LKEM  $\text{tlskem}$  with algorithms  $(\text{tls.Gen}, \text{tls.Enc}, \text{tls.Dec})$ , in which  $\text{tls.Gen}(1^\lambda)$  is the same as  $\text{KeyGen}$  and the algorithms  $\text{tls.Enc}, \text{tls.Dec}$  are as below.

$\begin{aligned} & \underline{\text{tls.Enc}(\text{PK}, \eta \  \text{CERT}_S)} : \\ & (\text{CRES}, \text{PMS}) \leftarrow F_C(\text{PK}); \\ & \text{MS} := \text{Kdf}(\text{PMS}, \eta); \\ & \text{UCFIN} := \text{PRF}(\text{MS}, 1 \  \eta \  \text{CERT}_S \  \text{CRES}); \\ & \text{AKEY} := \text{PRF}(\text{MS}, 0 \  \eta); \\ & \text{USFIN} := \\ & \text{PRF}(\text{MS}, 2 \  \eta \  \text{CERT}_S \  \text{CRES} \  \text{UCFIN}); \\ & \text{output } (\text{CRES}, \text{AKEY} \  \text{USFIN} \  \text{UCFIN}). \end{aligned}$	$\begin{aligned} & \underline{\text{tls.Dec}(\text{SK}, \eta \  \text{CERT}_S, \text{CRES})} : \\ & \text{PMS} \leftarrow F_S(\text{SK}, \text{CRES}); \\ & \text{if } \text{PMS} = \perp, \text{ set } \text{PMS} \leftarrow_{\text{R}} \{0, 1\}^\lambda; \\ & \text{MS} := \text{Kdf}(\text{PMS}, \eta); \\ & \text{UCFIN} := \text{PRF}(\text{MS}, 1 \  \eta \  \text{CERT}_S \  \text{CRES}); \\ & \text{AKEY} := \text{PRF}(\text{MS}, 0 \  \eta); \\ & \text{USFIN} := \text{PRF}(\text{MS}, 2 \  \eta \  \text{CERT}_S \  \text{CRES} \  \text{UCFIN}); \\ & \text{output } \text{AKEY} \  \text{USFIN} \  \text{UCFIN}. \end{aligned}$
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In order to consider CCCA security we augment  $\text{tlskem}$  with the following predicate.

$$\begin{aligned} & \underline{\text{tls.Pred}(\text{AKEY} \| \text{USFIN} \| \text{UCFIN}, \text{CFIN})} : \\ & (\text{ST}_e^S, \text{ST}_d^S) \leftarrow \text{stE.Init}(1^\lambda); \\ & \text{check if } \text{UCFIN} = \text{stE.Dec}(\text{CKEY}, \text{H}_C, \text{CFIN}, \text{ST}_d^S). \end{aligned}$$

## 5 TLS-RSA: Instantiations from OW-PCA

Here, we show that if the underlying KEM  $(\text{KeyGen}, F_C, F_S)$  is OW-PCA secure, then the  $\text{tlskem}$  scheme in Section 4.2 is IND-CCCA-secure in the random oracle model. Hence, by Theorem 1, the corresponding TLS scheme is SACCE-secure. In Section 5.2 we apply this result to show the security of TLS-RSA.

**OW-PCA for KEM [34].** For a stateful adversary  $\mathcal{A}$  and a KEM  $\text{kem}$  with algorithms  $(\text{KeyGen}, \text{Enc}, \text{Dec})$ , we define the advantage function

$$\text{Adv}_{\text{kem}}^{\text{ow-pca}}(\mathcal{A}) := \Pr \left[ \begin{array}{l} (\text{PK}, \text{SK}) \leftarrow \text{KeyGen}(1^\lambda); \\ K' = K^* : (\psi^*, K^*) \leftarrow \text{Enc}(\text{PK}); \\ K' \leftarrow \mathcal{A}^{\text{PCA}(\text{SK}, \cdot, \cdot)}(\psi^*) \end{array} \right]$$

where  $\text{PCA}(\text{SK}, \cdot, \cdot)$  is the oracle that takes as input  $(K, \psi)$  with  $K \neq \perp$  and outputs 1 if  $\text{Dec}(\text{SK}, \psi) = K$  and 0 otherwise. An encryption scheme is said to be *one-way against plaintext checking attacks* (OW-PCA) if for all PPT adversaries  $\mathcal{A}$ , the advantage  $\text{Adv}_{\text{kem}}^{\text{ow-pca}}(\mathcal{A})$  is a negligible function in  $\lambda$ .

### 5.1 IND-CCCA from OW-PCA

The following lemma is similar to that in [25, Theorem 3], with some significant differences: (i) the KEM key in [25, Theorem 3] is  $\text{AKEY}$  and the ciphertext is  $\text{CRES} \parallel \text{UCFIN}$ , whereas our KEM key is  $\text{AKEY} \parallel \text{USFIN} \parallel \text{UCFIN}$  and the ciphertext is simply  $\text{CRES}$ ; (ii) [25] models PRF (referred to as  $h_s$  and  $h_z$  therein) also as a random oracle; (iii) [25] proves (labeled) IND-CCA security and does not consider encryption of  $\text{UCFIN}$ .

**Lemma 1 (IND-CCCA from OW-PCA).** *If  $(\text{KeyGen}, F_C, F_S)$  is OW-PCA secure, PRF is a pseudorandom function, and we model  $\text{Kdf}()$  as a random oracle, then the  $\text{LKEM}$   $\text{tlskem}$  with predicate  $\text{tls.Pred}$  (in Section 4.2) is IND-CCCA secure in the random oracle model (c.f. Section 4.1). That is, for any adversary  $\mathcal{A}$  that makes at most  $Q$  decryption queries, there exists adversaries  $\mathcal{A}_1, \mathcal{A}_2, \mathcal{A}_4$  such that*

$$\text{Adv}_{\text{kem}, \text{pred}}^{\text{ind-ccca}}(\mathcal{A}) \leq Q \cdot (\text{Adv}_{\text{PRF}}^{\text{prf}}(\mathcal{A}_1) + 2^{-\lambda}) + \text{Adv}_{\text{kem}}^{\text{ow-pca}}(\mathcal{A}_2) + \text{Adv}_{\text{PRF}}^{\text{prf}}(\mathcal{A}_4).$$

Moreover, the running times of  $\mathcal{A}_1, \mathcal{A}_2, \mathcal{A}_4$  are roughly that of  $\mathcal{A}$ .

### 5.2 Implications for TLS-RSA

**TLS-RSA KEM.** The definition of the TLS-RSA KEM follows from the RSA PKCS #1v1.5 standard [26] adopted in TLS. Building on [25] we abstract the specification with parameters  $\lambda_0 = \Theta(\lambda)$ ,  $\lambda_1 = \Theta(\lambda)$  with  $\lambda_0 \leq \lambda_1 - 88$  as follows:

- $\text{KeyGen}(1^\lambda)$  is standard RSA key generation that outputs  $(\text{PK}, \text{SK}) := ((N, e), d)$  where  $de = 1 \pmod{\phi(N)}$  and  $N$  has  $\lambda_1$  bits, where we assume that  $\lambda_1$  is a multiple of 8.

- $F_C : \{0, 1\}^{\lambda_0} \rightarrow \mathbb{Z}_N^*$  takes as input  $\lambda_0$ -bit  $r$ , picks a padding  $P \leftarrow_{\mathcal{R}} \{0, 1\}^{\lambda_1 - \lambda_0 - 24}$  at random (subject to none of the bytes of  $P$  being 00), sets  $x := 00\|02\|P\|00\|r$  (where 00, 02 are byte encodings), and outputs  $y := x^e \pmod{N}$ .
- $F_S : \mathbb{Z}_N^* \rightarrow \{0, 1\}^{\lambda_0}$  takes as input  $y$ , and attempts to parse  $y^d \pmod{N}$  as a byte sequence of the form  $00\|02\|P\|00\|r$  where  $P$  contains no zero bytes and  $r$  has exactly  $\lambda_0$  bits. The procedure then outputs  $r$  if the parsing is successful (and  $\perp$  if the parsing fails).

Here, the condition that  $\lambda_0 \leq \lambda_1 - 88$  ensures that the random padding  $P$  has at least 8 bytes, as required by the standard [26]. We also assume in our description that KEM decapsulation involves performing a strict set of parsing checks.

The assumption that RSA PKCS #1v1.5 is OW-PCA is justified in [25, Theorem 1] via a reduction to an RSA-like assumption, known as “partial-domain RSA with decision oracle”. The latter, given in [25, Section 2.3], asserts that the RSA permutation is one-way, even given an oracle that is parameterized by  $\lambda_0 < \lambda_1$ , takes as input  $(x_0, y)$ , and reports whether the first  $\lambda_0$  bits of  $y^d \pmod{N}$  equals  $x_0$  or not. A close examination of the proof of [25, Theorem 1] shows that the theorem holds no matter what set of parsing checks are carried out during decapsulation (so long as the decapsulation algorithm is correct). This is convenient because, as recent work [7] has shown, there is a good deal of variation in how the required parsing is done in different PKCS #1v1.5 implementations.<sup>2</sup>

In TLS-RSA,  $\lambda_0$  is fixed to 384, reflecting the fixed size of PMS (at 48 bytes) in the TLS specification, while  $\lambda_1$  (the bit-size of  $N$ ) is typically 1024 or 2048 in TLS deployments. Jonsson and Kaliski in [25] discuss at some length why the above assumption is reasonable for typical parameters  $\lambda_0, \lambda_1$  used in practice. While seemingly strong, it seems hard to avoid using an assumption of this type given the many known weaknesses in RSA-PKCS#1 v1.5. We are not aware of any further significant work studying this assumption. In particular, in spite of the importance of the widely-deployed PKCS #1v1.5 scheme and its use in TLS, to the best of our knowledge no weaknesses on the assumption have been reported since its introduction in [25] over 10 years ago.

The security of TLS-RSA follows from Theorem 1 and Lemma 1:

**Theorem 2.** *Under the following assumptions:*

- RSA PKCS #1v1.5 is OW-PCA;
- PRF is a secure pseudorandom function;
- stE is a sLHAE encryption scheme,

*the TLS-RSA Protocol is a secure SACCE protocol in the random oracle model.*

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<sup>2</sup> This property of the proof would also allow us to incorporate into our analysis the additional check from the TLS specification that the leading 2 bytes of  $r$  should be an encoding of the TLS protocol version as sent by the client, at the cost of reducing  $\lambda_0$ , the bit-size of  $r$ , by 16. However, we omit this fine detail.

## 6 TLS-DH: Instantiation from PRF-ODH

We prove the security of TLS-DH following our methodology: We show that the KEM  $(\text{KeyGen}, F_C, F_S)$  that instantiates this mode in accordance with our generic representation of TLS (Figure 2) induces a labeled KEM,  $\text{dh.tlskem}$ , that is IND-CCCA secure. Then, by Theorem 1 we conclude that TLS-DH is a secure SACCE protocol. Finally, we apply these results to TLS-DHE, namely, when both client and server provide ephemeral DH keys. Here, we merely provide a summary of our results; details can be found in the full version [29].

**TLS-DH KEM.** Let  $G = \langle g \rangle$  be a cyclic group of prime order  $q$  generated by an element  $g$ . We define the TLS-DH KEM  $(\text{KeyGen}, F_C, F_S)$  via the following three algorithms.

- $\text{KeyGen}(1^\lambda)$ : Set  $(\text{PK}, \text{SK}) := (g^v, v)$ ,  $v \leftarrow_{\mathbb{R}} \mathbb{Z}_q$ ,  $|q| = \lambda$ .
- $F_C(\text{PK} = g^v)$ : Set  $(\psi, K) := (g^u, g^{uv})$ ,  $u \leftarrow_{\mathbb{R}} \mathbb{Z}_q$ .
- $F_S(\text{SK} = v, h)$ : Check that  $h \in G$ , if yes, output  $h^v$ , else output  $\perp$  (reject).

We show the security of TLS-DH in the standard model based on the PRF-ODH assumption on the function  $\text{Kdf}$ . This assumption is an adaptation of the Oracle Diffie-Hellman (ODH) assumption [1] to the PRF setting and was introduced in [24] for their proof of TLS-DHE. For the proof of TLS-DH we need the multi-query version of the assumption while for TLS-DHE the single-query case is sufficient, as in [24]. In [29] we describe the assumption and also prove its necessity by constructing secure pseudorandom functions for which PRF-ODH does not hold and with which TLS-DH violates ACCE security.

**Theorem 3.** *Protocol TLS-DH obtained by instantiating the generic TLS protocol from Figure 2 with the above defined TLS-DH KEM is a secure SACCE protocol provided  $\text{Kdf}$  is PRF-ODH, PRF is a secure pseudorandom function, and  $\text{stE}$  is an sLHAE-secure encryption scheme.*

*Extension to TLS-DHE with server-signed ephemeral DH (and no client authentication).* In this variant of TLS-DH, the certified server’s public key corresponds to a signature algorithm and the DH value, typically an ephemeral one, is signed by the server itself. All other details are exactly as in TLS-DH. The security of this protocol follows essentially from the analysis of TLS-DH by replacing  $\text{CERT}_S = \{\text{ID}_S, \text{PK} = g^v\}_{\text{CA}}$  with  $\text{CERT}_S = (\text{CERTSIG}_S, \text{sig}_S(g^v, \dots), g^v)$ , where  $\text{CERTSIG}_S = \{\text{ID}_S, \text{PKSIG}_S\}_{\text{CA}}$ ,  $\text{PKSIG}_S$  is a public key of  $S$  for a secure signature scheme, and  $\text{sig}_S$  is a signature produced by  $S$  under the corresponding signature key.

We note that [24] provided a specialized proof of TLS-DHE with client authentication. We obtain a proof for that particular case in Section 7 (Corollary 1). However, while [24] show forward security we do not include this property in our general treatment as it is not achieved by any of the other TLS modes.



## 7 The TLS Handshake Protocol with Mutual Authentication

In the full version [29] we augment server-only authentication, the SACCE model, with client authentication to obtain mutual authentication. The resultant model, ACCE, is mostly the same as in [24] except for the definition of matching sessions presented in Section 3. In this setting, the TLS client possesses a signature key (with a corresponding certificate  $CERT_C$ ) which it uses to authenticate to the server (by computing a signature on the session transcript up to the CRES message). In this case both the definition of matching conversations and the TLS LKEM are augmented with  $CERT_C$ .

We first extend Theorem 1 to the case of mutual authentication, namely, showing that if  $tlskem$  is IND-CCCA secure and  $stE$  is sLHAE-secure then TLS with client and server authentication is ACCE-secure. Then we immediately obtain the following powerful corollary:

**Corollary 1.** *TLS-RSA, TLS-CCA, TLS-DH and TLS-DHE where the client is authenticated using a secure signature scheme are all ACCE secure under the same assumptions stated for the SACCE security of these modes.*

## 8 Conclusions and Discussion

Establishing the security of a central protocol like TLS is clearly a significant result. The fact that we achieve this in a systematic way that covers the different TLS modes (TLS-RSA, TLS-DH, and TLS-DHE, as well as the hypothetical TLS-CCA), has clear methodological advantages and may be seen as indicating that the core design of the protocol is sound. Yet, we find it important to stress the many shortcomings of the TLS protocol that would be best avoided in future secure channel protocol designs. We summarise these issues here, expanding on them in [29].

**On the TLS Design.** A main weakness in the overall TLS design is the unfortunate interaction of the TLS Handshake and the Record protocols with respect to the Finished messages. Instead, these two conceptually and functionally different parts of a secure channel protocol can and should be designed as separate components. This separation makes engineering sense for implementing and maintaining the protocol, especially in evolving application settings as is the case with TLS. It also makes formal security analysis of the protocol easier, which in turn increases the likelihood that this analysis will be correct and applicable to the actual protocol under study.

In addition to the above structural weakness of the protocol, TLS has suffered from the early implementation of its public key encryption mode, TLS-RSA, with RSA PKCS#1v1.5. Rather than moving to a CCA-secure implementation of the encryption function (e.g., via RSA-OAEP), the TLS community responded to Bleichenbacher's attack by keeping RSA PKCS#1v1.5 as the default implementation but disabling the error message in case of a decryption error. We stress that our proof of security for TLS-RSA relies crucially on there being no side channel that would reveal the existence of decryption failures to the attacker. While the TLS specification now takes care to avoid some explicit forms of leaking this information, implementations may still find ways

of leaking it. This makes the security of the protocol non-robust and shows the clear advantage of using a CCA-secure scheme in TLS that, as we show, would avoid these complications and potential weaknesses.

The fragility of the TLS-RSA design is further illustrated by the somewhat “accidental” nature of its security. The security of this mode relies crucially on the fact that the client’s *Finished* message, CFIN, is sent immediately after the CRES message (containing the RSA ciphertext in TLS-RSA) and before the server responds with its own *Finished* message SFIN. Had CFIN been omitted or sent after SFIN, TLS-RSA would be completely insecure, e.g. subject to Bleichenbacher’s attack.

**On Our Attack Model.** We caution that, while our work shows that accurate descriptions of already-deployed, complex protocols can be analysed using the provable security paradigm, we only analyse the “cryptographic core” of TLS. This means that our analysis rules out many (but not all) attacks. More specifically:

- Several recent attacks on the TLS Record Protocol are possible because TLS supports symmetric encryption algorithms that have turned out *not* to be sLHAE-secure: see, for example, the BEAST attack [18], the short MAC attack [35], Lucky 13 [3], and the RC4 attacks in [4]. Such attacks can be mounted by the adversary in our security model but are ruled out by our theorem statements, which assume the use of an sLHAE-secure encryption scheme.
- Our description of TLS-RSA includes the standard countermeasures to Bleichenbacher’s attack, and our security proof then gives assurance that these countermeasures are effective in the context of the entire TLS protocol.

On the other hand, we do not treat ciphersuite (re)negotiation nor the TLS Record Protocol’s compression or fragmentation features, meaning that, for example, none of the attacks from [19, 30, 38] are covered by our analysis.

**A Final Thought.** We believe that one cannot overstate the importance of adopting protocols in practice that have been first rigorously analyzed and proven in a plausible cryptographic model. Such proofs are necessarily limited by the expressiveness of the underlying model and do not guarantee security in every imaginable deployment setting, yet they can serve as a major source of confidence in the soundness of the design. This is particularly important given the practical difficulty in changing protocols when weaknesses are found – and TLS serves as a good example for the latter.

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