Large-Scale Bioinformatics Data Mining with Parallel Genetic Programming on Graphics Processing Units

William B. Langdon

Abstract The NCBI GEO GSE3494 breast cancer dataset contains hundreds of Affymetrix HG-U133A and HG-U133B GeneChip biopsies each with a million variables. Multiple genetic programming (GP) runs on a graphics processing unit (GPU) hardware, each with a population of five million programs both winnows (selects) useful variables from the chaff and evolves small (three inputs) data models. The SPMD CUDA interpreter exploits the GPU's single instruction multiple data (SIMD) mode of parallel computing, even though the GP populations contain different programs. A 448 node nVidia Fermi C2050 Tesla graphics card delivers 8.5 giga GPops per second. In addition to describing our implementation, we survey current GPGPU work in bioinformatics and genetic programming.

1 Introduction

Since they offer cheap high-performance computing there is great interest in using mass market graphics hardware (GPUs) for scientific applications. For example the Chinese Tianhe-1A 2.566 petaflop supercomputer contains 7,168 nVidia Tesla M2050 general purpose GPUs. However a lot of scientific and engineering can be done with more modest computers, and we will concentrate on affordable personal computers or indeed laptop computers with one or more graphics cards or their Tesla compute-only equivalents. More than 100 million GPUs have been sold [\[24\]](#page-32-0). This availability and their price/performance ratio have led to the increasing use of essentially consumer gaming or entertainment hardware for research and engineering purposes. The field is often called general purpose computing on GPU (GPGPU) [\[84\]](#page-35-0). Until recently the doubling of the number of

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Fig. 1 Comparison of increase in speed of graphics cards $(+$ GPU) and CPU $(\times x86)$ (data supplied by nVidia). Similar trends hold for double precision and integer performance

transistors in computer chips every 18 months ("Moore's Law") was a fact of life [\[79\]](#page-35-1) and similar exponential rises occurred in processing speed and disk and memory storage capacity. The compound effect of Moore's Law has led to literally millionfold increases in hardware performance during careers in the software industry. Naysayers have frequently pointed out the impossibility of exponential growth continuing indefinitely; however, today it looks like they are right in at least one important aspect, and we have reached the end of Moore's Law as it has been applied to processor speed. In commercial terms, the industry remains dominated by descendants of Intel's 8086 silicon chips, yet for half a dozen years we have seen no major increase in CPU clock speed since the 3 GHz Pentium (see lower plot in Fig. [1\)](#page-1-0). If clock speeds had continued to double every 1.5 years, we would have 25 GHz Pentiums on our desks and in our laptops. This has not happened. It looks like it will never happen.

In its original sense the manufacturers of silicon chips continue to obey Moore's Law, and the number of transistors per chip has continued to increase. Recently Izydorczyk and Izydorczyk [\[37\]](#page-32-1) suggested Moore's Law will continue to hold for at least the next 22 years. However they appear to accept today's limit of about 3.5 GHz on processor clocks.

The additional transistors packed ever more densely onto chips have been used to create still bigger memory, particularly on-chip cache memory, more exotic instruction sets (e.g. vector, parallel and special purpose instructions), and especially to build multiple CPU cores on the same chip. Dual and quad cores are now commonplace. Eight- and even sixteen-core Pentium computers are now on the

horizon. It looks like we are really seeing the parallel future which has been forecast even before the transputer [\[1\]](#page-31-0).

Since our initial results on the breast cancer survival prediction dataset, GPU development has continued apace. For example, both AMD and nVidia have GPUs which claim to deliver more than a teraflop at a cost of a few hundred dollars.

The next section will describe scientific and engineering computing on GPUs. Some successful applications of GPUs to bioinformatics will be described in Sect. [3.](#page-4-0) In Sect. [4](#page-5-0) we will summarise our original RapidMind work [\[57\]](#page-33-0) in which genetic programming [\[55\]](#page-33-1) is used to data mine a small number of indicative mRNA gene transcript signals from breast cancer tissue samples taken during surgery, each with more than a million variables, to predict long-term survival. In [\[57\]](#page-33-0) we described the medical problem and the way genetic programming [\[53\]](#page-33-2) and a GPU simultaneously picked three of the million mRNA measurements available and found a simple nonlinear combination of them which predicts long-term outcomes at least as well as DLDA, SVM and KNN using 700 measurements [\[78\]](#page-34-0). Before concentrating on using genetic programming [\[3,](#page-31-1) [40,](#page-33-3) [59,](#page-34-1) [86\]](#page-35-2) in parallel on a GPU, Sect. [5](#page-6-0) briefly describes the major hardware components of GPUs and programming them. Then Sect. [6](#page-10-0) describes the new GP and CUDA code. We refer the interested reader to [\[57\]](#page-33-0) for details of the data source and how they were obtained, checked and normalised. The experiments are repeated using the new CUDA kernel. (The results are summarised in Sect. [7.](#page-22-0)) The new system avoids many restrictions imposed by RapidMind and uses modern Tesla hardware (C2050) to deliver a more than tenfold speedup (Sect. [8\)](#page-24-0). Finally in Sect. [9](#page-26-0) we consider how successfully our previous predictions about GPGPU have panned out and make new ones. We conclude (Sect. [10\)](#page-29-0) that GPGPU will be one of the parallel techniques of the future, but note that it is still held back by development tools.

2 Using Games Hardware GPUs for Science

Owens et al. [\[83,](#page-35-3) [84\]](#page-35-0) surveyed scientific and engineering applications running on mass market graphics cards. Today's GPUs can greatly exceed the floating point performance of their host CPU; see Fig. [1.](#page-1-0) This speed comes at a price.

GPUs provide a restricted type of parallel processing, often referred to as single instruction multiple data (SIMD) or more precisely single program multiple data (SPMD). Each of the many processors simultaneously runs the same program on different data items (see Fig. [2\)](#page-3-0). Being tailored for fast real-time production of interactive graphics, principally for the computer gaming market, GPUs are tailored to deal with rendering of pixels and processing of fragments of three-dimensional scenes very quickly. Each is allocated a processor and the GPU program is expected to transform it into another data item. The data items need not be of the same type. For example the input might be a triangle in three dimensions, including its orientation, and the output could be a colour expressed as four floating point numbers (RGB and alpha).

Fig. 2 An example of SIMD parallel processing. The stream processors (SP) simultaneously run the same program on different data and produce different answers. In this example the program has two inputs. One describes a *triangle* (position, colour, nature of its surface: matt, how shiny). The second input refers to a common light source and so all stream processors use the same value. Each stream processor calculates the apparent colour of its individual triangle. Notice, here, each output is independent of all the others and so they can all be calculated in parallel

Typical GPUs are optimised so that programs can read data from multiple data sources (e.g. background scenes, placement of lights, reflectivity of surfaces) but generate one output. This parallel writing of data greatly simplifies and speeds the operation of the GPU. Even so, both reading and writing from memory are still bottlenecks. This is true for the GPU's own memory but doubly so when data are transferred to/from the host PC and the GPUs.

The manufacturers continue to publish figures claiming enormous peak floating point performance. In practice such figures are not attainable. A more useful statistic is often how much faster an application runs after it has been converted to run on a GPU. However, like FLOPS, the number of GP operations per second (GPops) allows easier comparison of different GP implementations.

Many scientific applications and in particular bioinformatics applications are inherently suitable for parallel computing. In many cases data can be divided into almost independent chunks which can be acted upon almost independently. There are many different types of parallel computation which might be suitable for bioinformatics. Applications where a GPU might be suitable are characterised by:

- Maximum dataset size $\approx 10^9$.
- Maximum dataset data rate $\approx 10^9$ bytes/s.
- Up to 10^{11} floating point operations per second (FLOPs).
- Applications which are dominated by small computationally heavy cores, i.e. a large number of computations per data item (known as arithmetic intensity).
- Core has simple data flow. Possibly a large fan-in and simple data stream output.

Naturally as GPUs continue to become more powerful these figures continue to change.

3 GPUs in Bioinformatics and Computational Intelligence

As might be expected, GPUs have been suggested for medical image processing applications for several years now. However we concentrate here on molecular bioinformatics. We anticipate that after a few key algorithms are successfully ported to GPUs, within a few years bioinformatics will adopt GPUs for many of its routine applications. As might be expected, early results were mixed.

Charalambous et al. successfully used a relatively low-powered GPU to demonstrate inference of evolutionary inheritance trees (by porting RAxML onto an nVidia FX 5700) [\[9\]](#page-31-2). However a more conventional MPI cluster was subsequently used [\[98\]](#page-35-4). Recently a CUDA version of the alternative MrBayes tool was published [\[112\]](#page-36-0).

Sequence comparison is the life blood of bioinformatics. Liu et al. ran the key Smith–Waterman algorithm on a high-end GPU [\[68\]](#page-34-2). They demonstrated a reduction by a factor of up to 16 in the lookup times for most proteins. Smith–Waterman has also been ported to the Sony PlayStation 3 [\[106\]](#page-36-1) and the GeForce 8800 (CUDA) [\[76\]](#page-34-3). Trapnell and Schatz also used CUDA to port another sequence searching tool (MUMmer) to another G80 GPU and obtained speedups of up to $13\times$ when matching short DNA strands against much longer sequences [\[99\]](#page-35-5). More recently Vouzis and Sahinidis [\[101\]](#page-36-2) ported NCBI's Blast protein sequence alignment tool to CUDA, but report only modest speedups perhaps because of the large data volumes and their insistence on exactly emulating the original serial code. By breaking queries into GPU-sized fragments, they were able to run short sequences (e.g. 50 DNA bases) against the complete human chromosome. Successful ports and CUDA implementations of sequence tasks include GBOOST [\[111\]](#page-36-3) (40-fold), SOAP3 [\[67\]](#page-34-4) (7.5–20 \times faster) and MrBayes [\[112\]](#page-36-0) (19 \times , more with a second GPU).

Liu et al. used GPUs to model biomolecular pathways $[66]$ (26–33 \times), and Zhou et al. report speedups of $12\times$, $47\times$ and $367\times$ for Gillespie, LSODA and Euler–Maruyama using their CUDA-sim Python package [\[113\]](#page-36-4). Kannan and Ganji [\[39\]](#page-33-4) also report 10–47-fold speedup when porting AutoDock (a biomolecular drug discovery tool). Gobron et al. used OpenGL on a high-end GPU to drive a cellular automata simulation of the human eye and achieved real-time processing of webcam input [\[25\]](#page-32-2). GPUs have also been used in medical engineering, e.g. a GeForce 8800 provided a 15–20-fold speedup, improving the haptic response of a real-time interactive surgery simulation tool [\[69\]](#page-34-6). Dowsey et al. wrote 2D gel electrophoresis image registration code in Cg ("C for graphics") so that it could be offloaded onto an nVidia GPU [\[14\]](#page-31-3).

The better GPU applications may claim speedups of a factor of ten or more; however, the distributed protein folding system folding@home obtains 60 times as much free computation per donated GPU as it does per donated CPU [\[84,](#page-35-0) p. 983]. The same authors also claim an almost 3,600-fold speed up on a biomolecule dynamics simulation, albeit at the cost of using four FX 5600 GPUs [\[84,](#page-35-0) p. 995].

Computational intelligence applications of GPUs have included artificial neural networks (e.g. multilayer perceptrons [\[71,](#page-34-7) [91\]](#page-35-6), self-organising networks [\[88\]](#page-35-7) and spiking neural networks [\[110\]](#page-36-5)), fuzzy logic [\[34\]](#page-32-3), genetic algorithms [\[22,](#page-32-4) [72,](#page-34-8) [80,](#page-35-8) [85,](#page-35-9) [95,](#page-35-10) [97,](#page-35-11) [107\]](#page-36-6) and genetic programming [\[4,](#page-31-4) [6–](#page-31-5)[8,](#page-31-6) [10,](#page-31-7) [13,](#page-31-8) [15–](#page-31-9)[19,](#page-32-5) [27–](#page-32-6)[33,](#page-32-7) [35,](#page-32-8) [36,](#page-32-9) [43,](#page-33-5) [45–](#page-33-6) [47,](#page-33-7)[49,](#page-33-8)[56,](#page-33-9)[57,](#page-33-0)[62](#page-34-9)[–65,](#page-34-10)[70,](#page-34-11)[73–](#page-34-12)[75,](#page-34-13)[77](#page-34-14)[,87,](#page-35-12)[90,](#page-35-13)[92–](#page-35-14)[94,](#page-35-15)[96,](#page-35-16)[100,](#page-36-7)[102–](#page-36-8)[104,](#page-36-9)[108\]](#page-36-10). Most GPGPU applications have only required a single graphics card; however, Fan et al. have shown large GPU clusters are also feasible [\[20\]](#page-32-10). In 2008 the first computational intelligence on GPU special session (CIGPU-2008) was held in Hong Kong [\[105\]](#page-36-11). This has become an annual event. As Owens [\[83\]](#page-35-3) makes clear, games hardware has now broken out of the bedroom into scientific and engineering computing.

4 Gene Expression in Breast Cancer

We have previously [\[57\]](#page-33-0) used genetic programming to data mine gene expression measurements provided by Miller et al. [\[78\]](#page-34-0). We will mostly be concerned with updating the original RapidMind code to CUDA and its improved performance. However we start by recapping the data-mining problem. Miller et al. describe the collection and analysis of cancerous tissue from most of the women with breast tumours in the three years 1987–1989 in Uppsala in Sweden. Miller's primary goal was to investigate p53, a gene known to be involved in the regulation of other genes and implicated in cancers. In particular they studied the implications of mutations of p53 in breast cancer. The p53 genes of 251 women were sequenced so that it was known whether they were mutant or not. Affymetrix GeneChips (HG-U133A and HG-U133B) were used to measure mRNA concentrations in each biopsy. Various other data were recorded, in particular whether the cancer was fatal or not.

Each of the two types of GeneChips used contained more than half a million DNA probes arranged in a 712×712 square $(12.8 \text{ mm})^2$ array. (Current designs now exceed five million DNA probes on the same half inch square array.)

4.1 Uppsala Breast Cancer Affymetrix GeneChip Datasets

As part of our large survey of GeneChip flaws [\[60\]](#page-34-15), we had already downloaded all the HG-U133A and HG-U133B datasets in GEO [\[5\]](#page-31-10) (6,685 and 1,815, respectively) and calculated a robust average for each probe. These averages across all these human tissues were used to normalise the 251 pairs of HG-U133A and HG-U133B GeneChips and flag locations of spatial flaws [\[57\]](#page-33-0). R code to quantile normalise and

Fig. 3 Uppsala breast cancer distribution of log deviation from average value

detect spatial flaws is available via http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp[code/R. The value presented to GP is the probe's normalised value minus its average](http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp-code/R) value from GEO. This gives an approximately normal distribution centred at zero. See Fig. [3.](#page-6-1)

The GeneChip data created by [\[78\]](#page-34-0) were obtained from NCBI's GEO (dataset GSE3494). Other data, e.g. patients' age, survival time, whether breast cancer caused death and tumour size, were also downloaded. Whilst [\[78\]](#page-34-0) used the whole dataset, with more than a million inputs, we were keen to avoid over-fitting; therefore, the data were split into independent training and verification datasets. See [\[57\]](#page-33-0).

5 Summary of GPU Hardware and Programming

5.1 Main Hardware Components of GPUs

Figure [4](#page-7-0) shows the major components of a C2050 Tesla card. It is typical of current top-end GPUs. The card is connected to the host personal computer via the PC's PCI express bus. The effective speed of the PC–GPU connection varies both with the GPU and with the motherboard into which they both fit. How to get data into and out of the GPU via the PCI bus is one of the major design decisions in any GPU application. Although PCIe bus speeds have risen in recent years, it appears to have peaked. Recent top-end systems have relied on a hierarchy of PCI interconnects which allow simultaneous parallel transfers along their various parts.

Typical GPUs have space for several hundred megabytes or even a few gigabytes of data. The trend is still very much to increase the speed and size of onboard memory. Again, deciding which application data are stored onboard the GPU

Fig. 4 Links from GPU chip to host computer via PCIe bus and to memory on the GPU board. Fermi C2050 (ECC memory checks turned on)

(and when) is an important design decision. The GPU chip is connected by a very high-speed bus to its own high-speed onboard RAM memory.

There are some two-GPU systems. Typically, although there are two chips and two sets of RAM on the same board, they are programmed as if they were two separate GPUs in the same PC.

It is typical for a single GPU chip to contain more than one multiprocessor; see Fig. [5.](#page-8-0) These have their own connections to the onboard RAM and act more or less independently in parallel. The number of multiprocessors varies considerably between low-end and older models and high-end GPUs. The C2050 has 14 multiprocessors. There are already GPUs with 16 multiprocessors, and the trend is for the maximum number of multiprocessors to increase whilst retaining low-end GPUs with a single multiprocessor.

The multiprocessors contain banks of stream processors (SPs). These are where the essential SIMD nature of GPU computing arises. All the stream processors are locked together. They do the same calculation at the same time (albeit on different data). Thus, a C2050 multiprocessor can take 32 data items, do 32 calculations and generate 32 answers in parallel. However when a program contains an if or branch instruction, the 32 data items may cause the 32 stream processors to go in different directions. This they cannot do. Instead one branch direction is chosen, and stream processors going in that direction are free to continue calculating. The rest are held. At some time, the freely running stream processors are held long enough for the others to run. It may be quite some time later when all the stream processors return to a common instruction at the same time and all begin running at full speed in synchrony. In the meantime (when the stream processors' paths have diverged) the multiprocessor has been operating correctly but at reduced power. We shall use this property. It is important to remember that GPUs offer cheap computation, so it is okay to waste some of it.

The number of stream processors varies between GPUs. nVidia multiprocessors contain multiples of eight. As with multiprocessors themselves, both the range and maximum number of stream processors have increased and are likely to continue increasing. However the multiprocessor clock speed has not increased and may even have fallen back a little. Typical clocks speeds are now 1.1–1.5 GHz and dramatic change is not likely.

The newer Fermi designs now include both per-multiprocessor (L1) read–write data caches and L2 read–write cache shared between the multiprocessors, whereas older designs relied either on the application designing its own caches or read-only caches provided as part of graphics "texture" memory. The L2 cache also allows some limited communication between multiprocessors via atomic operations. For some time nVidia resisted the application developers' calls for caches, but now implemented in the Fermi architecture, they seem to be a great success. Future GPUs may see more and/or bigger caches.

Fig. 6 nVidia CUDA mega threading (Fermi, compute level 2.0). Each thread in a warp (32 threads) executes the same instruction. When a program branches, some threads advance and others are held. This is known as thread divergence (Sect. [5.1\)](#page-6-2). Later the other branches are run to catch up. Only the 32,768 registers (*small squares*) per block can be accessed at full processor speed. If threads in a warp are blocked waiting for off-chip memory (i.e. local, global or texture memory), another warp of threads can be started. The examples assume the requested data are not in a cache. Shared memory and cache can be traded, either 16 Kbytes or 48 Kbytes. Constant memory appears as up to 64 Kbytes via a series of small on-chip caches [\[2\]](#page-31-11)

5.2 Memory Latency: Efficiently Programming with Threads

A significant point in Figs. [4](#page-7-0) and [5](#page-8-0) which we have not discussed is why caches are important. The fact that dominates GPU programming (even with caches) is that it can take hundreds of times longer to fetch data from the GPU's off-chip memory than to calculate with it. Once data are in its registers, cache or shared memory, the multiprocessor can calculate with it blisteringly fast, but an unfortunate application can perform badly simply by having the stream processors wait for data most of the time. Figure 6 is a schematic which shows the GPU hardware interleaving threads of execution (horizontal arrows) so that as threads are blocked (e.g. waiting for offchip data to arrive) others are automatically released to run. If there are enough threads, the multiprocessor may still be busy when the data arrives, so keeping it fully loaded and enabling the application to efficiently use the GPU. However the number of active threads is limited.

Earlier nVidia GPUs limited the maximum number of threads to 512. The Fermi architecture has recently doubled this to 1,024. However there is another limit. Each execution thread will need some registers. Unlike a preemptive scheduler on the host computer, when a thread stops, there is nowhere to save these registers when a new thread is scheduled. Thus even when a thread is blocked (e.g. waiting for data to arrive) it cannot release its registers. This enables extremely rapid context switching between threads but means all the multiprocessor's registers have to be shared by its active threads. (A C2050 multiprocessor has 32,768 registers, 1,024 for each stream

Fig. 7 Speed of genetic programming interpreter [\[46\]](#page-33-10) and Park–Miller random numbers [\[44\]](#page-33-11) (excluding host–GPU transfer time) versus number of parallel threads used on a range of nVidia GPUs. *Top* three plots refer to CUDA implementations and *lowest* one to RapidMind code. Code available via [http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp-code/random-numbers/](http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp-code/random-numbers/cuda_park-miller.tar.gz) cuda park-miller.tar.gz

processor.) Although the CUDA nvcc compiler is very careful in how it allocates registers, it is possible, in complicated applications, for the number of active threads to be limited by the number of registers each thread requires before reaching the 1,024 limit.

Although GPU and application dependent, Fig. [7](#page-10-1) shows that typically a GPU starts to approach its maximum performance when there are more than about 18 threads per stream processor.

6 GeneChip Data Mining Using Genetic Programming on a GPU

6.1 A CUDA Single Instruction Multiple Data Interpreter for GP

Section [3](#page-4-0) has listed the previous experiments evolving programs with a GPU. Mostly these have represented the programs either as trees or as networks (Cartesian GP) [\[29\]](#page-32-11) and used the GPU for fitness evaluation. Harding [\[29\]](#page-32-11) compiled his networks into GPU programs before transferring the compiled code onto the GPU. However it turns out to be quite expensive to compile CUDA programs, and so it only makes sense when the program (in our case a GP individual) is to be run many times. (Harding showed the compiled approach can be improved by distributing the compilation across a local area network of workstations and obtained impressive results when each GP program was run more than 100 million times [\[32\]](#page-32-12).) Since we will be running each GP individual program on each training case (cancer patient) but we have at most only a few hundred training cases (actually only 91), it makes sense to avoid the compilation overhead and accept that interpreting the program may be slower than running compiled code, but interpreting will be faster overall. Therefore, we keep the traditional tree-based GP and use an interpreter running on the GPU.

The host part of the program is a more-or-less traditional GP but with fitness evaluation transferred to the GPU. However it represents evolving genetic programming individuals as trees which are linearised into reverse Polish expressions [\[53\]](#page-33-2) so that the GPU can interpret them straightforwardly in a single pass without recursive calls. The three mutation operations and crossover act directly on the reverse Polish expressions. This enables them to be passed directly to the GPU without the need to change format between the host and the GPU. Next we shall recap how to interpret multiple programs simultaneously on an SIMD computer [\[42\]](#page-33-12) before going into the details of the CUDA implementation (Sects. [6.2](#page-11-0)[–6.10\)](#page-19-0). Section [6.11](#page-20-0) describes how we use hundreds of GP runs to progressively refine the GeneChip data, how the largest ever GP populations are created and evolve under fitness selection, mutation and crossover. It also describes the non-panmictic fine-grained distributed population and short evolution times used to maintain diversity. All these operations take place on the host PC and are implemented in C source code.

Essentially the interpreter trick is to recognise that in the SIMD model (Sect. [5.1\)](#page-6-2), the "single instruction" belongs to the interpreter and the "multiple data" are the multiple GP trees. The single interpreter is used by millions of programs. It is quite small and needs to be compiled only once. It is loaded onto every stream processor within the GPU. Thus, every clock tick, the GPU can interpret a part of up to 448 different GP trees. The guts of a standard interpreter is traditionally an n-way switch where each case statement executes a different GP opcode; however, Fig. [8](#page-12-0) gives an alternative view in which the interpreter works on all possible opcodes and each GP program uses just those that it contains. The CUDA implementation is given in Figs. [9](#page-13-0)[–11.](#page-14-0)

6.2 CUDA Interpreter for GP

The CUDA code is given in Fig. [9.](#page-13-0) Potentially it could be improved further: (1) Each program must end in a NOP so the for loop test $PC <$ LEN-1 could be removed; (2) The array-indexing operation Pop[PC] could be replaced by using the pointer Pop directly and incrementing it by 4 bytes on each iteration of the loop, which would allow the variable PC to be removed.

Fig. 8 The original idea for the SIMD interpreter was that it should loop continuously through the whole genetic programming terminal, and function sets with GP individuals select which operations they want as they go past and apply them to their own data and their own stacks. However this can be refined by noting that individual multiprocessors act independently. If all 32 stream processors (SPs) in a warp run the same GP program, they will be synchronised and the SIMD interpreter behaves more like a conventional interpreter acting in parallel 32 times. There is some loss in efficiency if they act on multiple GP individuals and lose synchronisation, since this may cause thread divergence (Sect. [5.1\)](#page-6-2); however, the GPU still performs well

6.3 CUDA Interpreter Stack for GP

The interpreter evaluates each GP tree as a reverse Polish notation expression by pushing and popping intermediate values onto a stack (see Fig. [8\)](#page-12-0). Each expression needs its own stack. Each GPU thread works on its own expression and so needs its own stack.

Since there is no communication between threads, with read–write caches, it might be possible to place the interpreter's stacks in per-thread "local" memory. There is only a little shared memory, whereas there is lots of local memory, but if a cache line holding the stack were displaced, performance would be hit hard.

To avoid the possibility of any stack being moved to off-chip memory, we chose to put them in shared memory. (See code fragment in Fig. [10.](#page-13-1)) Many GP systems restrict tree depth and function arity. For example, our GP genetic operations ensure

```
int SP = 0:
for(unsigned int PC = 0; PC < LEN-1; PC++) {
 const optype OPCODE = Pop[PC];
 if(OPCODE==OPNOP) break;
 float d;
 if(OPCODE<= lastconst) {
   d = constants[OPCODE];
  } else if(OPCODE<= lastleaf) {
    d = d_Train0[(OPCODE-firstinput)*nexamples];
  } else {
   const float sp1 = stack(--SP);
   const float sp2 = stack(--SP);
   switch(OPCODE) {
   case OPADD: d = sp2+sp1; break;
   case OPSUB: d = sp2-sp1; break;
   case OPMUL: d = sp2*sp1; break;case OPDIV: d = sp2/sp1; break;
   }
 }
 push(d);
}
```
Fig. 9 GPU Reverse Polish Notation SIMD interpreter. The interpreter is invoked by every thread in the block (1,001) in parallel and cycles through each of the programs' instructions leaving the answer generated by each on the programs' stacks. (Fitness calculation in Figs. [13](#page-17-0)[–15.](#page-18-0)) Notice division is not protected [\[40\]](#page-33-3). Pop is a pointer to the start of the RPN program which is being evaluated on this stream processor. d_Train0 points to the data for the current cancer victim (see Sect. [6.6\)](#page-16-0)

```
extern shared float shared array[];
const int pStackMax = (MaxArity-1)*(pMaxDepth-1)+1;#define stack(sp) shared_array[(sp)*blockDim.x+threadIdx.x]
#define push(x) {stack(S\overline{P}) = x; SP++,}}
```
Fig. 10 CUDA implementation of stack required by SIMD interpreter (given in Fig. [9\)](#page-13-0). The stack is placed in shared memory to ensure it remains on-chip. CUDA allows indexed access to shared memory and so implementing a stack is much simpler than it was with RapidMind (version 2.0) and using deeper stacks is also straightforward. Indexing by threadIdx.x ensures each thread accesses adjacent words of shared memory so there are no bank conflicts

tree depth does not exceed eight (pMaxDepth) and Koza [\[40\]](#page-33-3) enforces a depth limit of 17. If unusually deep trees were needed or the function set contained functions with more than just two inputs (our data-mining trees use binary functions), more memory would be required. In this case the limited shared memory could start to restrict the number of threads that the interpreter can use.

Examining the PTX assembler produced by the nvcc compiler suggests that although accessing shared memory should be almost as fast as the threads' own registers, a surprisingly large number of PTX instructions are needed to implement push and pop. However it is not clear why and also the mapping between PTX assembler and final machine code is far from straightforward. Even though efficient stack operations are vital, this makes further optimisation of the stack tricky.

```
float* const constants = \&shared array[pStackMax*blockDim.x];
for(unsigned int i=threadIdx.x; i <= lastconst; i += blockDim.x){
  constants[i] = float(-5.0) + float(i) * float(0.01);
}
syncthreads();
```
Fig. 11 Setting up GP constants in shared memory. The 1,001 constants are stored immediately above the interpreter's stack (Figs. [10](#page-13-1) and [12\)](#page-15-0). The calculation is spread across all the available threads. _syncthreads() prevents any thread moving on to interpret any program until all the constants have been initialised. As the calculation happens before any global data is read, _syncthreads() causes little overhead. Usually adjacent threads interpret the same GP individual so they will simultaneously read the same constant. This does not cause a bank conflict. Since there are multiple banks of shared memory, only occasionally will a delay occur as a bank conflict arises from threads in the same warp interpreting two different programs simultaneously

6.4 Constants

In this application the GP system needs 1,001 constants (with values between -5.0 and $+5.0$, every 0.01). To simplify the interpreter, the old RapidMind system precalculated these and loaded them as part of the training data. However pushing constants onto the stack is one of the most common operations, and so to avoid reading them from global data (as has to be done with the training data), originally the new CUDA interpreter calculated them as required. This overhead was reduced by precalculating them once per multiprocessor and saving them in shared memory (see Figs. [11](#page-14-0) and [12\)](#page-15-0). This only occupies 4,004 bytes of shared memory, but the speedup was modest.

It would also be possible to store them in constant memory, so avoiding calculating them on the GPU at all, but where two different programs cause the interpreter to simultaneously read different constants, there is a surprising overhead [\[50,](#page-33-13) [61\]](#page-34-16).

6.5 Thread Layout

As we described under the heading of "The Computational Cube" in [\[47\]](#page-33-7), one of the virtues of the SIMD GP interpreter is that it gives different ways to access the huge amount of parallelism inherent in having a population of individuals and multiple training cases on which they need to be evaluated. As we showed in Fig. [7,](#page-10-1) the efficient use of GPUs requires many active threads. While it will vary between applications, Fig. [7](#page-10-1) suggests even something as simple as generating random values will need at least 8,000 threads to fully load a C2050. With this in mind we designed the thread layout to use as many of the 1,024 threads per multiprocessor block as possible. However we decided to combine the fitness calculation with the interpreter into one CUDA kernel so all the threads interpreting one program must be in the

Fig. 12 On each of the 14 C2050 Tesla multiprocessors, 11 GP programs of between 1 and 15 instructions (11 middle arrows) are interpreted in parallel, each processing data for 91 of the breast cancer gene expression datasets. This uses $11 \times 91 = 1,001$ of the 1,024 available threads (97.8 %). Each interpreter thread has its own stack in shared memory (slab between the two sets of arrows). Apart from warp divergence the 1,001 threads act independently until fitness calculation. After comparing each program's output with the actual class, the CUDA kernel uses seven reduce operations to sum the number of training cases which the program got right and convert these to a fitness value which is written to global memory (11 arrows on right)

same block, and they are forced to synchronise when fitness is calculated. Also we decided to use one thread per GP program per test case. With 91 training cases, this means each block simultaneously interprets 11 programs using 1,001 threads (98 % of the 1,024 maximum). See Fig. [12.](#page-15-0) This gives a maximum of 14,014 active threads per C2050.

The interpreter threads are tightly packed, which means ignoring the 32 thread warp boundaries [\[93\]](#page-35-17). Thus 10 of our 32 warps will be interpreting two GP programs at once and so will suffer from divergence. For 91 training examples, we could have packed the thread into three warps (using 95 % of the available threads), allowing ten programs per block and up to 12,740 active threads per C2050. However, tightly packing the programs into warps has the advantage that the number of training cases can be readily changed without detailed consideration of its impact. For example, the system worked well (without modification) with 41 training cases.

Other approaches are also possible. For example, all 91 fitness cases for one program could be interpreted by warps in the same block. This would simplify the across-thread summations needed to calculate the program's final fitness value and remove the need to use Lsynchreads () in the fitness reduction (Sect. [6.8\)](#page-17-1). Alternatively we could have used one thread per program, so avoiding the need for any data transfers between threads. This also avoids any idle threads. However as well as problems of the threads diverging (Sect. [5.1\)](#page-6-2), having a large number of separate programs independently requesting uncorrelated data items would overwhelm the data caches.

A potential good compromise would be to allocate each program a whole warp (avoiding thread divergence), enabling it to read and use training data a cache line at a time. Having read and processed it, typically the program would not re-read it. With 91 training cases, each interpreter thread would have to process the program between two and three times. (This also uses 95 % of the available threads.)

As the computational cube approach makes clear, other compromises are possible. While their efficiency will vary according to circumstances, many are viable.

6.6 Training Data

Each training example has data from both HG-U133A and HG-U133B, i.e. $2 \times$ $712^2 = 1,013,888$ floats. The training data are not modified. (This is usual in machine learning applications.) They are stored in the GPU (left-hand side of Fig. [12\)](#page-15-0) at the start of the run and then only read. This transfer happens only once so there would only be a marginal advantage in using non-paged ("pinned") memory on the host to speed up the transfer. Once loaded onto the GPU, the host does not use it again. Placing the data in normal host memory allows the operating system to page them out to re-use the RAM they were occupying if need be.

When the training data are read in, they are effectively transposed so that all the data for the same GeneChip probe are placed consecutively. This enables probe data to be read into a few cache lines in a small number of operations (three or four depending upon alignment).

6.7 Thread Divergence

Although all our reverse Polish (RPN) flatten trees will start with pushing a data item, in a usual GP population, the second, third, fourth and so on instruction will tend to be different. As the code in Fig. [9](#page-13-0) shows, if a warp of threads interprets two different GP individuals, their paths through the interpreter code will be different and only a small part (the top and bottom of the main loop) will be common. Since this is impossible, we get "divergence" (Sect. 5.1). This means one set of threads proceed, with the others headed to different code, held up. Sometime later the first

```
const unsigned int correct = (pos \hat{ } (stack(0) \leq 0)) & 1;
volatile unsigned int *sdata = (unsigned int*) shared array;
sdata[threadIdx.x] = correct;
```
Fig. 13 Final part of runprog () (Fig. [9\)](#page-13-0). The value calculated by GP (on the top of the stack, Fig. [10\)](#page-13-1) is compared with the class of training examples pos, converted into a Boolean (was it correct or not) and then saved in shared memory, overwriting part of the stack (which is no longer needed)

set of threads is held up and the second set allowed to run. At some later point all the threads in the warp resynchronise. Obviously this is slower than the usual case where the whole warp is interpreting the same GP program. From the computational point of view, we would expect such a warp to take a bit less than twice as long as a single program warp.

Potentially more important is reading data. Two different programs (even though adjacent in the GP population) will typically access different data. In the first set of runs there is a huge volume of training data and reading different parts of it will probably mean they are not in the L1 cache; hence, the threads will have to wait until it can be read into the GPU chip. Hopefully there will be other threads elsewhere on the same multiprocessor ready to run, but even so delays caused by reading data may be more important than thread divergence.

Unfortunately it is difficult to tune the code to get the best from the GPU, and it could need re-tuning for other datasets and problems [\[50\]](#page-33-13). Nonetheless, while this may not be the absolute optimum code, we feel it is a good compromise.

6.8 Fitness Calculation

There are three stages to fitness calculation (arrows right-hand side of Fig. [12\)](#page-15-0):

- 1. Each thread compares the sign of the value calculated by the GP individual with that desired. For the 21 positive cases it should be positive. For the 70 negative cases it should not be positive. The value (0 or 1) is saved in shared memory; see Fig. [13.](#page-17-0)
- 2. The 91 correct or not values are summed using a reduction technique to give the number of true negatives (TN) and number of true positives (TP) the GP individual scored. See Fig. [14.](#page-18-1)
- 3. A single thread is used to convert (TN) and (TP) into a single fitness value which is stored in the GP individual's output (see Fig. [15\)](#page-18-0) for later transfer to the host.

Each thread always works on the same training case for each of the \approx 34,000 GP programs it interprets each generation. Therefore, $pos¹$ $pos¹$ $pos¹$ (Fig. [13\)](#page-17-0), like d_Train0

¹pos is 1 for positive training cases and 0 for negative cases.

```
device
void reduce sum(const unsigned int start, const unsigned int n){
//Ok to overlay on Stack as used syncthreads to ensure all done
volatile unsigned int *sdata = (unsigned int*) shared array;
const unsigned int tid = threadIdx.x;
const unsigned int top = start+n;
// do reduction in shared mem
//__syncthreads() needed as operate across warp boundaries
if(tid>=start && tid<top) sdata[tid] += fsdata(tid+128,top);
 syncthreads();
\overline{if}(tid>=start \& tidlttop) sdata[tid] += fsdata(tid+64,top);
 syncthreads();
\overline{\text{if}}(tid>=start && tid<top) sdata[tid] += fsdata(tid+32,top);
 syncthreads();
if(tid>=start && tid<top) sdata[tid] += fsdata(tid+16,top);
 syncthreads();
if(tid>=start && tid<top) sdata[tid] += fsdata(tid +8,top);
 syncthreads();
if(tid>=start && tid<top) sdata[tid] += fsdata(tid +4,top);
 syncthreads();
if(tid>=start && tid<top) sdata[tid] += fsdata(tid +2,top);
 syncthreads();
\overline{if(tid)} =start && tid<top) sdata[tid] += fsdata(tid +1,top);
 syncthreads();
}
```
Fig. 14 Reduction code to add n items in $log_2(n)$ steps. It calculates the sum of both correct (Fig. [13\)](#page-17-0) negative and positive training examples simultaneously. \Box device \Box function fsdata() ensures the reduction code does not include data from threads running other programs or indeed different classes for the same thread. Totals are left in shared memory index start. It will cope with up to 256 negative and 256 positive training cases. Clever use of templates and/or conditional compilation could eliminate operations which are not needed with fewer training cases. Atomic or barrier synchronisation might be an alternative to _syncthreads()

```
reduce_sum(start1,n);
  syncthreads();
if(threadIdx.x==start) {
 volatile unsigned int *sdata = (unsigned int*) shared array;
  const unsigned int TN = \text{sdata}[\text{start}];const unsigned int TP = \text{sdata}[\text{start}+ \text{nneq}];
  const int penalty = (TP==0 | TN==0)? 0 : 2*npos*nneg;
  *d Output = 1 + penalty + TP*nneg + TN*npos;
}
```
Fig. 15 sumfit () uses reduce_sum() (Fig. [14\)](#page-18-1) to give the number of correct negative (TN) and positive (TP) training examples. One thread per program calculates AUROC fitness without division (and keeping integer values) but keeping the same relative weighting of TN, TP and the penalty (Table [1\)](#page-22-1). To aid debugging 1 is added to ensure fitness is never zero. Finally the thread writes fitness to global memory (d_Output)

(Fig. [9\)](#page-13-0), and the boundaries of the negative and positive cases (given by start1 and n in Fig. [15\)](#page-18-0) are calculated once when the thread starts and then are reused.

6.9 Fermi L1 Caches

GP individuals are stored as 16 unsigned int $(LEN = 16)$. Thus when the first thread interprets the first instruction, it will actually cause the whole individual (Pop) to be loaded from off-chip global memory into L1 cache and remain in cache on the multiprocessor until the interpreter finishes with it. Actually since each program occupies only half a cache line, the first instruction can also trigger the loading of Pop for the adjacent program. (A C2050 cache line covers 128 contiguous bytes). Since all the threads in a block work on 11 contiguous programs (Fig. [12\)](#page-15-0), they should fit into six cache lines. Eventually all of Pop will have to be read, but this is done efficiently, and it does not have to be read more than once by that individual. Notice we also avoid explicitly caching the population in shared memory [\[93\]](#page-35-17).

As mentioned in Sect. [6.6,](#page-16-0) the training data are organised to be adjacent to each other, so if one part of a training case is loaded into the multiprocessor L1 cache, then 31 data items in the corresponding training cases are also loaded into the cache at the same time. It appears that with 91 training cases three cache lines per data item are needed. (Perhaps four, depending upon how the cache handles alignment.) Thus in the initial runs where there are thousands or indeed millions of data items, the L1 cache cannot hope to avoid reloading. However all the training data required to interpret each GP individual will be read efficiently into the multiprocessor and it will only be read once by that individual.

In the final run, in which we interpret many millions of GP programs, they read only eight training cases. Since the L1 cache occupies 16 Kbytes, these 728 values of training data will fit into it and so should remain cached. (Pop still occupies 80 Mbytes and so now becomes the major data item.) The interpreter in the final run achieves only about 200 million more GPops/s than it does on the large training data runs. This hints that the kernel data I/O is working well and it is operating near the Fermi's computational limit.

6.10 CUDA Gives Improvements

Whereas RapidMind 2.0 imposed a 2^{22} bit addressing limit (i.e. no more than \approx 4 million items per array) and no more than 16 arrays per GPU, CUDA imposes no such limits. Instead all the GPU's memory is directly addressable. Thus originally the population of five million GP programs had to be split into 20 parts and the training data split into eight or more arrays. Therefore 256,000 GP programs were passed to the GPU (a GTX 8800) which, on average, took slightly less than a second to interpret them and return their fitness values. This had to be done with each of the 20 parts of the population. Now the whole population is passed to the Tesla C2050 in one go, interpreted and five million fitness values returned to the host, in under a second.

Originally the multiple program outputs (required by splitting the training data into four separate arrays) were summed and combined into a single fitness value per GP individual by three additional GPU programs, making a total of seven GPU programs. Now with the simplification allowed by bigger address ranges, the complete GP interpreter and fitness calculation is done by a single CUDA kernel.

6.11 GP for Large-Scale Data Mining

We previously described using genetic programming to data mine GeneChip data [\[55\]](#page-33-1). Our intention was to automatically evolve a simple (possibly non-linear) classifier which uses a few simple inputs to predict the future about 10 years ahead. To ensure the solutions are simple (and for speed), the GP trees are limited to 15 nodes. (Whilst this is obviously small, it is not unreasonable. For example, Yu et al. successfully evolved classifiers limited to only eight nodes [\[109\]](#page-36-12).) Since many GPUs offer more than a gigabyte of onboard RAM, both the population size and length of individuals could be increased. Indeed since GPUs can now directly access the host computer's RAM, larger populations might be accommodated in large-RAM 64 bit servers without explicit direct transfer to the Tesla. Undoubtedly there will be performance implications, but assuming reasonable locality, so the data caches now available are not overwhelmed, this might be quite a successful approach. However we have not tried this as yet and instead have kept the explicit data transfer. Typically this takes 55 ms (PCIe bandwidth 5.7 Gbytes/s). Explicit transfer of the five million fitness values in the other direction back to the host server takes 3 ms (PCIe bandwidth 5.9 Gbytes/s). Both transfers are to/from nonpaged ("pinned") host memory. These large data transfers make the best use of the PCIe bus. If they were replaced by the GPU directly accessing the host ("zero copy" transfers), presumably they would be replaced by data transfers limited to the width of the GPU cache, which might be less efficient. However they would seamlessly allow the GPU to overlap data transfers and computation, whilst we have not attempted such asynchronous use of the GPU.

Previously [\[55\]](#page-33-1) we demonstrated GP on datasets with more than 7,000 inputs (created by pre-processed raw data). Now we have more than a million individual probe values (and the compute power to use them). Therefore we asked GP to evolve combinations of the probe values rather than use Affymetrix or other humandesigned combinations of them. In our approach the first step is to use GP as its own feature selector.

Essentially the idea is to use Price's theorem [\[89\]](#page-35-18). Price showed that the number of fit genes in the population will increase each generation and the number of unfit genes will decrease. We run GP 100 times. We ignore the performance of the

Fig. 16 Screen shot of a 512×400 GP population, i.e. 204,800 programs (from runs approximating π [\[53\]](#page-33-2)) evolving under selection, crossover and subtree mutation after 100 generations. Colour indicates fitness (*left*) and syntax (*right*). *Below* are two histograms (log scale) showing distribution of population by fitness and genotypic distance from the first optimal solution. (Colour scales below each histogram.) Local convergence and the production of species is visible (especially right). See [http://www.cs.ucl.ac.uk/staff/W.Langdon/pi2](http://www.cs.ucl.ac.uk/staff/W.Langdon/pi2_movie.html)_movie.html and Google [videos](http://video.google.co.uk/videoplay?docid=7513698947919634338) for animation and more explanation

best-of-run individual and instead look at the genes it contains. Thus the first pass starts with a million inputs, and we select in the region of 10,000 for the second pass and so on until we get down to a reasonable number. Finally GP is run with a much-enriched terminal set containing only inputs which have showed themselves to be highly fit in previous GP runs. See Sect. [7.](#page-22-0)

The question of how big to make the GP population can be solved by considering the coupon collector problem [\[21,](#page-32-13) p. 284]. On average $n(\log(n) + 0.37)$ random trials are needed to collect all of n coupons. Since we are using GP to filter inputs, we insist that the initial random population contains at least one copy of each input. That is, we treat each input as a coupon (so $n = 1,013,888$) and ask how many randomly chosen inputs must we have in the initial random population to be reasonably confident that we have them all. The answer is 14 million. The spread in the distribution of answers to the coupon collector problem is of the order of square root of n . Therefore if we overshoot by a few thousands, we are sure to get all the inputs (GP tree leafs) into the initial population. Since a program of 15 nodes has eight leafs and half of these are constants, we need at least $(1/4)(14$ million) = 3.6 million random trees. An initial population of five million ensures this.

At the end of the first pass, we want on the order of 100,000 inputs to chose from. This means we need about 25,000 good programs (each with about four inputs). We do not want to run our GP 25,000 times. The compromise is to use overlapping fine-grained demes [\[41\]](#page-33-14) to delay convergence of the population; see Fig. [16.](#page-21-0) The GP population is laid out on a rectangular 2560×2048 grid (see Fig. [17\)](#page-22-2). This is

Fig. 17 *Left*: The GP population of five million programs is arranged on a 2560×2048 grid, which does not wrap around at the edges. At the end of the run the best individual in each 256×256 tile is recorded. *Right*: (note different scale) parents are drawn by 4-tournament selection from within a 21×21 region centred on their offspring

divided into $80\,256 \times 256$ squares. At the end of the run, the genetic composition of the best individual in each square is recorded. Note that to prevent the best of one square invading the next, parents are selected to be within ten grid points of their offspring. Thus genes can travel at most 100 grid points in ten generations. The GP parameters are summarised in Table [1.](#page-22-1)

7 Experimental Results

The new CUDA system is much faster, but, as expected, the results are similar. GP was run 100 times with all inputs taken from the 91 training examples using the parameters given in Table [1.](#page-22-1) After ten generations the best program in each of

Fig. 18 Distribution of usage of Affymetrix probes in 8,000 best generation-10 GP programs. Both distributions are almost straight lines (note log scales, cf. Zipf's law [\[114\]](#page-36-13)) and closely agree with earlier runs [\[57\]](#page-33-0)

the 80 256 \times 256 squares was recorded. The distribution of inputs used by these 100×80 programs is given in Fig. [18.](#page-23-0) Most probes were not used by any of the 8,000 programs, 24,892 were used by only one, 2,029 by two and so on.

The 28,305 probes which appeared in any of the 8,000 best generation-ten programs were used in a second pass. In the second pass GP was also run 100 times. (The GP parameters were kept the same.)

Eight probes which appeared in more than 200 of the best 8,000 programs of the second pass were the inputs to a final GP run. (The GP parameters were again kept the same.) See also upper trace in Fig. [18](#page-23-0) and Table [2.](#page-24-1)

As Fig. [19](#page-25-0) shows, GP finds many good matches to the 91 training examples, most of the 80 score above 90 % and several score more than 92 %. Ever mindful of overfitting [\[12\]](#page-31-12), in the original RapidMind runs as a solution we chose one with the fewest inputs (three). GP found a non-linear combination of two PM probes and one MM probe from near the middle of HG-U133A; see Fig. [20](#page-26-1) and Table [2.](#page-24-1) The evolved predictor is the sum of two non-linear combinations of two human genes; see Fig. [21\)](#page-26-2). Both sub-expressions have some predictive ability. The three probes chosen by GP are each highly correlated with all PM probes in their probeset [\[58\]](#page-33-16) and so can be taken as a true indication of the corresponding gene's activity. The gene names used in Fig. [20](#page-26-1) were given by the manufacturer Netaffx's www pages. Possibly terms like decorin/C17orf81 are simply using division as a convenient way to compare two probe values. Indeed the sign indicates whether two values are both above or both below average. (Division appears in all 80 of the best generation-ten programs, slightly more often than $+$ and $-$ but much more often than multiplication: $/80, +72, -71, \times 27.$

		Used	X,Y	chip	Affy id	NetAffx gene title
1	2	579	350,514	A	200903 _{-8-at.mm8}	S-adenosylhomocysteine hydrolase
2	10	493	325,511	A	219260 _{-8-at.pm7}	C17orf81. chromosome 17 open reading frame 81
3	6	363	254,667	А	201893 _{-X-at.pm2}	Decorin
4	1	291	392,213	A	219778 _{-at.pm4}	Zinc finger protein, multitype 2
5	4	286	366,310	в	230984_s_at.mm10	230984_s_at was annotated using the accession-mapped cluster-based pipeline to a UniGene identifier using 17 transcript (s) . This assignment is strictly based on mapping accession IDs from the original UniGene design cluster to the latest UniGene design cluster
6	3	265	324,484	А	216593_s_at.mm9	Phosphatidylinositol glycan anchor biosynthesis, class C
7	19	263	542,192	B	233989_at.mm4	EST from clone 35214, full insert. UniGene ID Build 201 (01 Mar 2007) Hs.594768 NCBI
8	41	245	269,553	в	223818 _{-8-at.pm2}	Remodelling and spacing factor 1

Table 2 Eight Affymetrix probes used the most in 8,000 best generation-10 second pass Rapid-Mind GP programs which were used in the final RapidMind run [\[57\]](#page-33-0). See Fig. [18.](#page-23-0) The second column gives rank in these experiments

The chosen solution compares well with that produced by Miller et al. [\[78\]](#page-34-0), which used more than 704 data items compared to GP's three. We also showed in [\[57\]](#page-33-0) that the RapidMind interpreted 535 million GP operations per second (535 MGPop/s). This corresponded to a $7.59\times$ speedup compared to an Intel 2.40 GHz CPU.

8 Genetic Programming Interpreter Speed on Tesla C2050 GPU

On average across the 201 GP runs the C2050 processed 8.5 billion GP primitives per second. This is fairly consistent, even on the last run, where there are only eight inputs (effectively 3 Kbytes of global training data). The server has two C2050 Teslas, so the 100 runs of each phase can be split into two and 50 run on each one. On the four-core server, there is little interaction between them, and so the combined speed of fitness evaluation using two C2050s is 17 billion GPop/s.

The GPU interpreter's performance of 8.5 gigaGPOP/s (line marked \circ in Table [3\)](#page-27-0) is very good. It is by far the fastest for a floating point GP data-mining application, being surpassed only by our Boolean multiplexor benchmarks [\[46\]](#page-33-10), graphics applications [\[32\]](#page-32-12) and a special bench mark [\[64\]](#page-34-17). The number of successful applications has expanded in recent years. Where GP operations rates (rather than just

Fig. 19 Spread of performance on training data v. program size. 80 best generation-10 programs in final CUDA GP run with eight inputs. Size is given in *top* graph by the number of different inputs and by the number of GP instructions in the *bottom* graph. Noise added to spread data horizontally. Whilst most of these high fitness predictors are of the maximum size (15) most use only three or four of the eight available inputs

speedup ratios) were given, the result is included in Table [3.](#page-27-0) Interpreter performance is expected to vary somewhat with the size of the terminal and function sets (columns 2–4) [\[38\]](#page-33-17). The performance of compiled GPs on GPUs can vary widely, e.g. with program size (column 6) and number of training examples (column 8).

Fig. 20 GP-evolved three-input classifier. The figure uses gene names. We could also use Affymetrix probe names. Using probe names, the evolved tree says survival is predicted if $1.54 \frac{201893 \cdot x \cdot at.2 \text{pm}}{219260 \cdot s \cdot at.7 \text{pm}} - 2.94219260 \cdot s \cdot at.7 \text{pm} - \frac{219260 \cdot s \cdot at.7 \text{pm}}{200903 \cdot s \cdot at.8 \text{mm}}$ $\frac{219260 \text{ s_at.}7 \text{pm}}{200903 \text{ s_at.}8 \text{mm}} < 0$

Fig. 21 The GP classifier (Fig. [20\)](#page-26-1) is the weighted addition of two input classifiers (*left* and *right*)

Table [3](#page-27-0) gives the maximum speeds; see the individual references for details of which factors affect speed.

Run time in most genetic programming systems is dominated by the time to calculate fitness; now this is done by the GPU, the remaining operations (still done on the host) become more important. Our host code is almost identical to the original RapidMind experiments and has not been optimised. As fitness evaluation speeds up, it may become necessary to parallelise these other parts of the evolutionary process.

The earliest evolutionary computation GPGPU [\[22\]](#page-32-4) implemented both genetic operations and fitness evaluation on the GPU. More recently Pospichal et al. [\[87\]](#page-35-12) ported both genetic operations and fitness of grammatical evolution onto a GTX 480 with CUDA.

9 The Future of General Purpose GPU Computing

It is gratifying to note that some of our earlier predictions [\[57\]](#page-33-0) have already come about. For example, we see more and more on-chip transistors being used to introduce on-chip caches and more on-chip memory. We also see routine support for double precision, removal of the 22 bit limit on data sizes, direct access to host PC RAM, routine support for 64 bit addressing and direct transfer of data between

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GPU in the same host computer. The concept of GPGPU has broaden out and is directly supported by nVidia's Tesla range (of non-graphics card GPUs). GPGPU continues to grow.

Like the x86 processor range, modern GPU chips are accumulating functionality with the manufacturers showing great reluctance to remove transistors designed to support older graphics applications such as anti-aliasing. This hardware is unlikely to be useful for scientific computing and so represents an overhead.

Published GPGPU computation has been dominated by nVidia. Initial publications were by people programming scientific applications using graphics tools (e.g. Cg). There was then a move to nVidia's CUDA. In the last couple of years there has been a little interest in OpenCL applications on nVidia cards. OpenCL offers the possibility of porting applications between different graphics hardware. Indeed recently some new GPGPU applications [\[26\]](#page-32-14) have been coded to use OpenCL on ATI cards.

It is clear that GPU programming is aimed squarely at the high-level language programmer. Even the CUDA assembler language PTX is remote from the machine code that the GPU actually runs. Both PTX and high-level language sources must be compiled before the GPU can use them. The compilation tools are aimed at one programmer working on one (or a few) program at a time and aim to produce the very best machine code for the GPU and do not worry about how long it will take to compile. This is fundamentally not suitable for populations of programs. We have worked around this problem. Harding [\[32\]](#page-32-12) (and now more recently others) ran the CUDA compiler multiple times in parallel. Lewis showed evolving PTX can reduce the compilation overhead by more than 20 % [\[64\]](#page-34-17). We have taken the approach of not compiling the GP programs but instead interpreting them. Whilst this allows a single GPU to run millions of programs simultaneously, an interpreter will always be slower than machine code. Nordin $[81]$ was the first to recognise this and built GP systems that both genetically manipulated and ran first SUN machine code and later Intel x86 code. Indeed his x86 system is now the basis of a successful commercial GP system [\[23\]](#page-32-15). Whilst GPU machine code is not straightforward [\[64\]](#page-34-17), we anticipate soon someone will bite the bullet and remove the compiler/interpreter bottleneck by implementing a GP system which evolves GPU machine code directly.

Despite improving tools, both debugging (see [\[48\]](#page-33-20) and the chapter "Understanding NVIDIA GPGPU Hardware") and performance tuning [\[50\]](#page-33-13) remain difficult. There is still a risk that if GPUs remain difficult to use, they will remain limited to specialised niches. To quote John Owens, "It's the software, stupid" [\[82\]](#page-35-20).

10 Conclusions

Previously [\[57\]](#page-33-0) we took a large GeneChip breast cancer biopsy dataset with more than a million inputs and demonstrated genetic programming running in parallel on an nVidia GeForce 8800 GTS and showed a $7.6\times$ speedup compared to a

single-core PC. The compute-intensive fitness evaluation has now been recoded in CUDA and run on modern hardware, the C2050 Tesla. With the new kernel a single nVidia C2050 delivers about 8.5 billion GP operations per second, i.e. 16 times faster than the old code with an 8800 GTS, even though in simple terms of peak floating point (single-precision) performance, the C2050 is just 2.5 times faster.

Two C2050s can deliver 17 GPop/s. This includes interaction times between host and GPU, but not selection, crossover and mutation, which are still done by the original $C++$ code on the host.

In some ways a genetic programming interpreter is an ideal GPU application. The cross product of the GP population and training case sizes is already huge. If we also include running multiple GP runs in parallel, in these experiments we have 48 billion almost independent calculations which could be done in parallel. Sometimes highly parallel applications can give disappointing results on GPUs because there is little computation per data item and so more time is spent moving data than computing with it. We estimate very roughly 30 machine instructions are needed to interpret each GP primitive. This gives an "arithmetic intensity" (i.e. the ratio of calculations per data item) of about 20, which puts the GP interpreter in the upper part of the typical range of arithmetic intensities of 4–64 FLOP/TDE for successful parallel applications $[11, p. 206]$ $[11, p. 206]$.

Sections [2](#page-2-0) and [3](#page-4-0) showed that general-purpose computation on graphics processing units is becoming established, and there are an expanding range of GPGPU applications, particularly in bioinformatics. Today GPGPU is dominated by nVidia's GPUs and CUDA. It may be OpenCL will soon open the way, not to portable GPGPU applications but to more use of ATI and Intel GPU hardware. Undoubtedly the 3GHz ceiling on CPU clocks will mean that the future of computing is parallel and GPGPU will be one of the popular approaches whereby desktop and other applications will exploit parallel hardware.

C++ Source Code

CUDA code can be downloaded via anonymous ftp from ftp.cs.ucl.ac.uk or via [http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp-code/gpu](http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp-code/gpu_gp_cuda.tar.gz) gp cuda.tar.gz. The large dataset GSE3494 can also be downloaded from the UCL ftp site [ftp.cs.ucl.](ftp.cs.ucl.ac.uk/genetic/gp-code/GSE3494/) [ac.uk/genetic/gp-code/GSE3494/.](ftp.cs.ucl.ac.uk/genetic/gp-code/GSE3494/)

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