

# Appendix A

## A.1 Fundamental Units and Some Physical Constants

SI: Le Système International d'Unités

### Seven SI base units

Length	meter	m
Mass	kilogram	kg
Time	second	s
Electric current	ampere	A
Thermodynamic temperature	kelvin	K
Amounts of substance	mole	mol
Luminous intensity	candela	cd

### Derived SI units with a specific name

Quantity	Term • Symbol	Relevance to other units
Frequency	Hertz Hz	$s^{-1}$
Force	Newton N	$m \cdot kg \cdot s^{-2}$
Pressure, Stress	Pascal Pa	$N/m^2 \quad m^{-1} \cdot kg \cdot s^{-2}$
Energy Work, Calorific value	Joule J	$N/m \quad m^2 \cdot kg \cdot s^{-2}$
Power	Watt W	$J/s \quad m^2 \cdot kg \cdot s^{-3}$
Electric charge	Coulomb C	$A \cdot s \quad s \cdot A$
Voltage, Potential	Volt V	$W/A \quad m^2 \cdot kg \cdot s^{-3} \cdot A^{-1}$
Electric capacity	Farad F	$C/V \quad m^2 \cdot kg^{-1} \cdot s^2 \cdot A^2$
Electrical resistivity	Ohm $\Omega$	$V/A \quad m^2 \cdot kg \cdot s^{-3} \cdot A^{-2}$
Radioactivity	Becquerel Bq	$s^{-1}$
Absorbed dose	Gray Gy	$J/kg \quad m^2 \cdot s^{-2}$
Dose equivalent	Sievert Sv	$J/kg \quad m^2 \cdot s^{-2}$
Plane angle	Radian rad	
Solid angle	Steradian sr	

Time: minute and hour, Plane angle: degree, minute, second, Volume: liter and Mass: metric ton.  
These units are non-SI units, but they are accepted for use with the SI units.

### Physical constants

Quantity	Symbol	Value	Unit	
			SI	CGS
Velocity of light in vacuum	$c$	2.997925	$10^8$ m/s	$10^{10}$ cm/s
Planck's constant	$h$	6.6260	$10^{-34}$ J·s	$10^{-27}$ erg·s
Avogadro's number	$N_A$	6.02217	$10^{23}$ /mol	$10^{23}$ /mol
Atomic mass unit <sup>a</sup>	$amu$	1.66053	$10^{-27}$ kg	$10^{-24}$ g
Universal gravitation constant	$G$	6.67259	$10^{-11}$ m <sup>3</sup> /s <sup>2</sup> ·kg	$10^{-8}$ cm <sup>3</sup> /s <sup>2</sup> ·g
Permeability of vacuum free space	$\mu_0$	$4\pi=12.56637$	$10^{-7}$ H/m	—
Permittivity of vacuum free space	$\epsilon_0$	8.854188	$10^{-12}$ F/m	—
Charge of electron	$e$	1.60219	$10^{-19}$ C	$10^{-20}$ emu
		4.80320	—	$10^{-10}$ esu
Faraday's constant	$F$	9.64853	$10^4$ C/mol	$10^3$ emu/mol
Electron rest mass	$m_e$	9.10956	$10^{-31}$ g	$10^{-28}$ g
Electron specific charge	$e/m_e$	1.7588	$10^{11}$ C/kg	$10^7$ emu/g
Electron radius	$r_e$	2.81794	$10^{-15}$ m	$10^{-13}$ cm
Electron Compton wavelength	$\lambda_e$	2.42631	$10^{-12}$ m	$10^{-10}$ cm
Proton rest mass	$m_p$	1.67262	$10^{-27}$ kg	$10^{-24}$ g
	$m_p/m_e$	1836.15	1	1
Fine structure constant	$\alpha$	7.29735	$10^{-3}$	$10^{-3}$
	$\alpha^{-1}$	137.036	1	1
Rydberg constant	$R_\infty$	1.09737	$10^7$ /m	$10^5$ /cm
Bohr radius	$a_0$	5.29177	$10^{-11}$ m	$10^{-9}$ cm
Gas constant	$R$	8.31451	J/mol·K	$10^7$ erg/mol·K
Molar volume of ideal gas at N.T.P. <sup>b</sup>	$V_m$	22.414	$10^{-3}$ m <sup>3</sup> /mol	$10^3$ cm <sup>3</sup> /mol
Boltzmann constant	$k_B$	1.38062	$10^{-23}$ J/K	$10^{-16}$ erg/K
Stefan-Boltzmann constant	$\sigma$	5.67051	$10^{-8}$ W/m <sup>2</sup> ·K <sup>4</sup>	$10^{-5}$ erg/s·cm <sup>2</sup> ·K <sup>4</sup>

<sup>a</sup>One twelfth of mass of  $^{12}C$ .

<sup>b</sup>Temperature 273.15 K, Pressure 101325 Pa(1 atm).

### Units frequently used with SI units

Quantity	Symbol	Value	Unit	
			SI	CGS
electron volt	eV	1.60219	$10^{19}$ J	$10^{-12}$ erg
angstrom	$\text{\AA}^a$		$0.1\text{nm}=10^{-10}$ m	$10^{-8}$ cm
barn	b		$10^{-28}$ m <sup>2</sup>	

<sup>a</sup>Å is also used in comparison to the electric current A.

## A.2 Atomic Weight, Density, Debye Temperature and Mass Absorption Coefficients ( $\text{cm}^2/\text{g}$ ) for Elements

Characteristic radiation	Wavelength (Å)	1 Hydrogen	2 Helium	3 Lithium	4 Beryllium	5 Boron	6 Carbon	7 Nitrogen	8 Oxygen
	Atomic weight	1.0079	4.0026	6.941	9.0122	10.811	12.011	14.0067	15.9994
	Density	8.375E-05	1.664E-04	0.533	1.86	2.47	2.27	1.165E-03	1.332E-03
	$\Theta(\text{K})$			344	1440		2230		
Cr $K\alpha$	2.2910	4.12E-01	4.98E-01	1.30E+00	3.44E+00	7.59E+00	1.50E+01	2.47E+01	3.78E+01
Cr $Kb_1$	2.0849	4.05E-01	4.25E-01	1.01E+00	2.59E+00	5.69E+00	1.12E+01	1.86E+01	2.84E+01
Fe $K\alpha$	1.9374	4.00E-01	3.81E-01	8.39E-01	2.09E+00	4.55E+00	8.99E+00	1.49E+01	2.28E+01
Fe $Kb_1$	1.7566	3.96E-01	3.35E-01	6.63E-01	1.58E+00	3.39E+00	6.68E+00	1.10E+01	1.70E+01
Co $K\alpha$	1.7903	3.97E-01	3.43E-01	6.93E-01	1.67E+00	3.59E+00	7.07E+00	1.17E+01	1.80E+01
Co $Kb_1$	1.6208	3.93E-01	3.07E-01	5.55E-01	1.27E+00	2.67E+00	5.24E+00	8.66E+00	1.33E+01
Cu $K\alpha$	1.5418	3.91E-01	2.92E-01	5.00E-01	1.11E+00	2.31E+00	4.51E+00	7.44E+00	1.15E+01
Cu $Kb_1$	1.3922	3.88E-01	2.68E-01	4.12E-01	8.53E-01	1.73E+00	3.33E+00	5.48E+00	8.42E+00
Mo $K\alpha$	0.7107	3.73E-01	2.02E-01	1.98E-01	2.56E-01	3.68E-01	5.76E-01	8.45E-01	1.22E+00
Mo $Kb_1$	0.6323	3.70E-01	1.97E-01	1.87E-01	2.29E-01	3.09E-01	4.58E-01	6.45E-01	9.08E-01
Characteristic radiation	Wavelength (Å)	9 Fluorine	10 Neon	11 Sodium	12 Magnesium	13 Aluminium	14 Silicon	15 Phosphorus	16 Sulfur
	Atomic weight	18.9984	20.1797	22.9898	24.305	26.9815	28.0855	30.9738	32.066
	Density	1.696E-03	8.387E-04	0.966	1.74	2.70	2.33	1.82(yellow)	2.09
	$\Theta(\text{K})$			75	158	400	428	645	
Cr $K\alpha$	2.2910	5.15E+01	7.41E+01	9.49E+01	1.26E+02	1.55E+02	1.96E+02	2.30E+02	2.81E+02
Cr $Kb_1$	2.0849	3.89E+01	5.61E+01	7.21E+01	9.62E+01	1.18E+02	1.51E+02	1.77E+02	2.17E+02
Fe $K\alpha$	1.9374	3.13E+01	4.52E+01	5.82E+01	7.78E+01	9.59E+01	1.22E+02	1.44E+02	1.77E+02
Fe $Kb_1$	1.7566	2.33E+01	3.38E+01	4.37E+01	5.85E+01	7.23E+01	9.27E+01	1.09E+02	1.35E+02
Co $K\alpha$	1.7903	2.47E+01	3.58E+01	4.62E+01	6.19E+01	7.64E+01	9.78E+01	1.15E+02	1.42E+02
Co $Kb_1$	1.6208	1.83E+01	2.66E+01	3.45E+01	4.63E+01	5.73E+01	7.36E+01	8.70E+01	1.07E+02
Cu $K\alpha$	1.5418	1.58E+01	2.29E+01	2.97E+01	4.00E+01	4.96E+01	6.37E+01	7.55E+01	9.33E+01
Cu $Kb_1$	1.3922	1.16E+01	1.69E+01	2.20E+01	2.96E+01	3.68E+01	4.75E+01	5.64E+01	6.98E+01
Mo $K\alpha$	0.7107	1.63E+00	2.35E+00	3.03E+00	4.09E+00	5.11E+00	6.64E+00	7.97E+00	9.99E+00
Mo $Kb_1$	0.6323	1.19E+00	1.69E+00	2.17E+00	2.92E+00	3.64E+00	4.73E+00	5.67E+00	7.11E+00
Characteristic radiation	Wavelength (Å)	17 Chlorine	18 Argon	19 Potassium	20 Calcium	21 Scandium	22 Titanium	23 Vanadium	24 Chromium
	Atomic weight	35.4527	39.948	39.0983	40.078	44.9559	47.867	50.9415	51.9961
	Density	3.214E-03	1.663E-03	0.862	1.53	2.99	4.51	6.09	7.19
	$\Theta(\text{K})$			92	91	230	360	420	380
Cr $K\alpha$	2.2910	3.16E+02	3.42E+02	4.21E+02	4.90E+02	5.16E+02	5.90E+02	7.47E+01	8.68E+01
Cr $Kb_1$	2.0849	2.44E+02	2.66E+02	3.28E+02	3.82E+02	4.03E+02	4.44E+02	4.79E+02	6.70E+01
Fe $K\alpha$	1.9374	2.00E+02	2.18E+02	2.70E+02	3.14E+02	3.32E+02	3.58E+02	3.99E+02	4.92E+02
Fe $Kb_1$	1.7566	1.52E+02	1.67E+02	2.07E+02	2.42E+02	2.56E+02	2.77E+02	3.09E+02	3.85E+02
Co $K\alpha$	1.7903	1.61E+02	1.76E+02	2.18E+02	2.55E+02	2.69E+02	2.91E+02	3.25E+02	4.08E+02
Co $Kb_1$	1.6208	1.22E+02	1.34E+02	1.66E+02	1.95E+02	2.06E+02	2.27E+02	2.50E+02	2.93E+02
Cu $K\alpha$	1.5418	1.06E+02	1.16E+02	1.45E+02	1.70E+02	1.80E+02	2.00E+02	2.19E+02	2.47E+02
Cu $Kb_1$	1.3922	7.95E+01	8.75E+01	1.09E+02	1.29E+02	1.37E+02	1.52E+02	1.66E+02	1.85E+02
Mo $K\alpha$	0.7107	1.15E+01	1.28E+01	1.62E+01	1.93E+01	2.08E+01	2.34E+01	2.60E+01	2.99E+01
Mo $Kb_1$	0.6323	8.20E+00	9.14E+00	1.16E+01	1.38E+01	1.49E+01	1.68E+01	1.87E+01	2.15E+01

$\Theta$ : Debye temperature, Unit of density:  $\text{Mg}/\text{m}^3$ .

Characteristic radiation	Wavelength (Å)	25	26	27	28	29	30	31	32
	Manganese	Iron	Cobalt	Nickel	Copper	Zinc	Gallium	Germanium	
	Atomic weight	54.9381	55.845	58.9332	58.6934	63.546	65.39	69.723	72.61
	Density	7.47	7.87	8.8	8.91	8.93	7.13	5.91	5.32
Cr Ka	2.2910	9.75E+01	1.13E+02	1.24E+02	1.44E+02	1.53E+02	1.71E+02	1.83E+02	1.99E+02
Cr Kb <sub>1</sub>	2.0849	7.53E+01	8.69E+01	9.60E+01	1.12E+02	1.18E+02	1.32E+02	1.42E+02	1.55E+02
Fe Ka	1.9374	6.16E+01	7.10E+01	7.85E+01	9.13E+01	9.68E+01	1.08E+02	1.16E+02	1.27E+02
Fe Kb <sub>1</sub>	1.7566	3.75E+02	5.43E+01	6.00E+01	6.98E+01	7.40E+01	8.27E+01	8.86E+01	9.69E+01
Co Ka	1.7903	3.93E+02	5.72E+01	6.32E+01	7.35E+01	7.80E+01	8.71E+01	9.34E+01	1.02E+02
Co Kb <sub>1</sub>	1.6208	3.06E+02	3.42E+02	4.81E+01	5.60E+01	5.94E+01	6.64E+01	7.12E+01	7.78E+01
Cu Ka	1.5418	2.70E+02	3.02E+02	3.21E+02	4.88E+01	5.18E+01	5.79E+01	6.21E+01	6.79E+01
Cu Kb <sub>1</sub>	1.3922	2.07E+02	2.32E+02	2.48E+02	2.79E+02	3.92E+01	4.38E+01	4.70E+01	5.14E+01
Mo Ka	0.7107	3.31E+01	3.76E+01	4.10E+01	4.69E+01	4.91E+01	5.40E+01	5.70E+01	6.12E+01
Mo Kb <sub>1</sub>	0.6323	2.38E+01	2.71E+01	2.96E+01	3.40E+01	3.57E+01	3.93E+01	4.15E+01	4.46E+01
Characteristic radiation	Wavelength (Å)	33	34	35	36	37	38	39	40
	Arsenic	Selenium	Bromine	Krypton	Rubidium	Strontium	Yttrium	Zirconium	
	Atomic weight	74.9216	78.96	79.904	83.8	85.4678	87.62	88.9059	91.224
	Density	5.78	4.81	3.12 (liq.)	3.488E-03	1.53	2.58	4.48	6.51
Cr Ka	282	90		72	56	147	280	291	
Cr Kb <sub>1</sub>	2.2910	2.19E+02	2.34E+02	2.60E+02	2.77E+02	3.03E+02	3.28E+02	3.58E+02	3.86E+02
Fe Ka	2.0849	1.70E+02	1.82E+02	2.02E+02	2.15E+02	2.36E+02	2.56E+02	2.79E+02	3.00E+02
Fe Kb <sub>1</sub>	1.9374	1.39E+02	1.49E+02	1.65E+02	1.76E+02	1.93E+02	2.10E+02	2.29E+02	2.47E+02
Co Ka	1.7566	1.06E+02	1.14E+02	1.27E+02	1.35E+02	1.48E+02	1.61E+02	1.76E+02	1.91E+02
Co Kb <sub>1</sub>	1.7903	1.12E+02	1.20E+02	1.33E+02	1.42E+02	1.56E+02	1.70E+02	1.85E+02	2.00E+02
Cu Ka	1.5418	8.55E+01	9.16E+01	1.02E+02	1.09E+02	1.19E+02	1.30E+02	1.42E+02	1.54E+02
Cu Kb <sub>1</sub>	1.3922	5.65E+01	6.05E+01	6.74E+01	7.21E+01	7.90E+01	8.59E+01	9.40E+01	1.01E+02
Mo Ka	0.7107	6.61E+01	6.95E+01	7.56E+01	7.93E+01	8.51E+01	9.06E+01	9.70E+01	1.63E+01
Mo Kb <sub>1</sub>	0.6323	4.82E+01	5.08E+01	5.55E+01	5.84E+01	6.30E+01	6.72E+01	7.21E+01	7.61E+01
Characteristic radiation	Wavelength (Å)	41	42	43	44	45	46	47	48
	Niobium	Molybdenum	Technetium	Ruthenium	Rhodium	Palladium	Silver	Cadmium	
	Atomic weight	92.9064	95.94	[99]	101.07	102.9055	106.42	107.8682	112.411
	Density	8.58	10.22	11.50	12.36	12.42	12.00	10.50	8.65
Cr Ka	275	450		600	480	274	225		209
Cr Kb <sub>1</sub>	2.2910	4.16E+02	4.42E+02	4.74E+02	5.01E+02	5.36E+02	5.63E+02	6.02E+02	6.26E+02
Fe Ka	2.0849	3.25E+02	3.45E+02	3.70E+02	3.92E+02	4.20E+02	4.41E+02	4.72E+02	4.90E+02
Fe Kb <sub>1</sub>	1.9374	2.67E+02	2.84E+02	3.05E+02	3.23E+02	3.46E+02	3.63E+02	3.89E+02	4.05E+02
Co Ka	1.7566	2.05E+02	2.19E+02	2.35E+02	2.49E+02	2.67E+02	2.81E+02	3.01E+02	3.13E+02
Co Kb <sub>1</sub>	1.7903	2.16E+02	2.30E+02	2.47E+02	2.62E+02	2.80E+02	2.95E+02	3.16E+02	3.29E+02
Cu Ka	1.5418	1.45E+02	1.54E+02	1.66E+02	1.76E+02	1.89E+02	1.99E+02	2.13E+02	2.22E+02
Cu Kb <sub>1</sub>	1.3922	1.10E+02	1.17E+02	1.26E+02	1.34E+02	1.44E+02	1.51E+02	1.63E+02	1.69E+02
Mo Ka	0.7107	1.77E+01	1.88E+01	2.04E+01	2.17E+01	2.33E+01	2.47E+01	2.65E+01	2.78E+01
Mo Kb <sub>1</sub>	0.6323	8.10E+01	1.38E+01	1.49E+01	1.58E+01	1.70E+01	1.80E+01	1.94E+01	2.02E+01

Θ: Debye temperature, Unit of density: Mg/m<sup>3</sup>.

Characteristic radiation	Wavelength (Å)	49	50	51	52	53	54	55	56
		Indium	Tin	Antimony	Tellurium	Iodine	Xenon	Caesium	Barium
	Atomic weight	114.818	118.71	121.76	127.6	126.9045	131.29	132.9054	137.327
	Density	7.29	7.29	6.69	6.25	4.95	5.495E-03	1.91(263K)	3.59
Cr Ka	2.2910	6.63E+02	6.91E+02	7.23E+02	7.40E+02	7.96E+02	7.21E+02	7.60E+02	5.70E+02
Cr Kb <sub>1</sub>	2.0849	5.19E+02	5.42E+02	5.70E+02	5.85E+02	6.31E+02	6.52E+02	6.86E+02	6.45E+02
Fe Ka	1.9374	4.28E+02	4.47E+02	4.71E+02	4.83E+02	5.22E+02	5.40E+02	5.69E+02	5.86E+02
Fe Kb <sub>1</sub>	1.7566	3.32E+02	3.47E+02	3.65E+02	3.74E+02	4.08E+02	4.22E+02	4.46E+02	4.61E+02
Co Ka	1.7903	3.49E+02	3.64E+02	3.83E+02	3.94E+02	4.25E+02	4.40E+02	4.65E+02	4.80E+02
Co Kb <sub>1</sub>	1.6208	2.69E+02	2.81E+02	2.96E+02	3.04E+02	3.30E+02	3.43E+02	3.63E+02	3.76E+02
Cu Ka	1.5418	2.36E+02	2.47E+02	2.59E+02	2.67E+02	2.88E+02	2.99E+02	3.17E+02	3.25E+02
Cu Kb <sub>1</sub>	1.3922	1.80E+02	1.88E+02	1.98E+02	2.04E+02	2.20E+02	2.29E+02	2.43E+02	2.52E+02
Mo Ka	0.7107	2.95E+01	3.10E+01	3.27E+01	3.38E+01	3.67E+01	3.82E+01	4.07E+01	4.23E+01
Mo Kb <sub>1</sub>	0.6323	2.16E+01	2.26E+01	2.39E+01	2.47E+01	2.68E+01	2.80E+01	2.98E+01	3.10E+01
Characteristic radiation	Wavelength (Å)	57	58	59	60	61	62	63	64
		Lanthanum	Cerium	Praseodymium	Neodymium	Promethium	Samarium	Europium	Gadolinium
	Atomic weight	138.9055	140.115	140.9077	144.24	[145]	150.36	151.965	157.25
	Density	6.17	6.77	6.78	7.00		7.54	5.25	7.87
Cr Ka	142								200
Cr Kb <sub>1</sub>	2.2910	2.25E+02	2.38E+02	2.38E+02	2.51E+02	2.94E+02	2.79E+02	3.09E+02	2.98E+02
Fe Ka	2.0849	7.44E+02	4.94E+02	1.88E+02	1.98E+02	2.32E+02	2.21E+02	2.44E+02	2.35E+02
Fe Kb <sub>1</sub>	1.9374	6.18E+02	5.61E+02	4.48E+02	4.55E+02	1.94E+02	2.04E+02	2.03E+02	1.95E+02
Co Ka	1.7566	4.83E+02	5.10E+02	5.39E+02	4.92E+02	5.88E+02	1.63E+02	4.08E+02	1.53E+02
Co Kb <sub>1</sub>	1.7903	5.07E+02	5.35E+02	5.65E+02	5.05E+02	4.00E+02	1.76E+02	4.19E+02	1.61E+02
Cu Ka	1.6208	3.95E+02	4.17E+02	4.41E+02	4.57E+02	4.82E+02	3.54E+02	4.80E+02	3.35E+02
Cu Kb <sub>1</sub>	1.5418	3.48E+02	3.68E+02	3.90E+02	4.04E+02	4.26E+02	4.34E+02	4.34E+02	4.03E+02
Mo Ka	1.3922	2.66E+02	2.82E+02	2.99E+02	3.10E+02	3.28E+02	3.35E+02	3.52E+02	3.60E+02
Mo Kb <sub>1</sub>	0.7107	4.49E+01	4.77E+01	5.07E+01	5.30E+01	5.63E+01	5.78E+01	6.09E+01	6.26E+01
Cr Ka	0.6323	3.29E+01	3.49E+01	3.72E+01	3.88E+01	4.13E+01	4.24E+01	4.47E+01	4.60E+01
Characteristic radiation	Wavelength (Å)	65	66	67	68	69	70	71	72
		Terbium	Dysprosium	Holmium	Erbium	Thulium	Ytterbium	Lutetium	Hafnium
	Atomic weight	158.9253	162.5	164.9303	167.26	168.9342	173.04	174.967	178.49
	Density	8.27	8.53	8.80	9.04	9.33	6.97	9.84	13.28
Cr Ka	210						120	210	252
Cr Kb <sub>1</sub>	2.2910	3.32E+02	3.25E+02	3.47E+02	3.52E+02	3.86E+02	3.87E+02	4.31E+02	4.25E+02
Fe Ka	2.0849	2.63E+02	2.57E+02	2.72E+02	2.78E+02	3.05E+02	3.04E+02	3.39E+02	3.34E+02
Fe Kb <sub>1</sub>	1.9374	2.19E+02	2.14E+02	2.28E+02	2.32E+02	2.53E+02	2.51E+02	2.80E+02	2.77E+02
Co Ka	1.7566	1.71E+02	1.68E+02	1.78E+02	1.82E+02	1.96E+02	1.96E+02	2.18E+02	2.16E+02
Co Kb <sub>1</sub>	1.7903	1.80E+02	1.76E+02	1.87E+02	1.91E+02	2.06E+02	2.06E+02	2.29E+02	2.27E+02
Cu Ka	1.6208	3.60E+02	1.38E+02	1.46E+02	1.49E+02	1.59E+02	1.59E+02	1.78E+02	1.76E+02
Cu Kb <sub>1</sub>	1.5418	3.21E+02	3.62E+02	1.29E+02	1.32E+02	1.40E+02	1.42E+02	1.56E+02	1.55E+02
Mo Ka	1.3922	3.76E+02	3.87E+02	4.02E+02	4.17E+02	1.08E+02	1.08E+02	1.21E+02	1.20E+02
Mo Kb <sub>1</sub>	0.7107	6.58E+01	6.83E+01	7.13E+01	7.44E+01	7.79E+01	8.04E+01	8.40E+01	8.69E+01
Cr Ka	0.6323	4.83E+01	5.02E+01	5.24E+01	5.48E+01	5.74E+01	5.93E+01	6.19E+01	6.41E+01

Θ: Debye temperature, Unit of density: Mg/m<sup>3</sup>.

Characteristic radiation	Wavelength (Å)	73 Tantalum	74 Tungsten	75 Rhenium	76 Osmium	77 Iridium	78 Platinum	79 Gold	80 Mercury
	Atomic weight	180.9479	183.84	186.207	190.23	192.217	195.08	196.9665	200.59
	Density	16.67	19.25	21.02	22.58	22.55	21.44	19.28	13.55
	$\Theta$ (K)	240	400	430	500	420	240	165	71.9
Cr Ka	2.2910	4.32E+02	4.57E+02	5.01E+02	4.99E+02	5.20E+02	5.41E+02	5.51E+02	5.41E+02
Cr Kb <sub>1</sub>	2.0849	3.39E+02	3.61E+02	3.94E+02	3.92E+02	4.11E+02	4.23E+02	4.34E+02	4.16E+02
Fe Ka	1.9374	2.83E+02	3.01E+02	3.27E+02	3.27E+02	3.40E+02	3.57E+02	3.61E+02	3.39E+02
Fe Kb <sub>1</sub>	1.7566	2.20E+02	2.34E+02	2.57E+02	2.55E+02	2.65E+02	2.61E+02	2.79E+02	2.60E+02
Co Ka	1.7903	2.31E+02	2.46E+02	2.68E+02	2.68E+02	2.78E+02	2.76E+02	2.95E+02	2.73E+02
Co Kb <sub>1</sub>	1.6208	1.79E+02	1.91E+02	2.09E+02	2.09E+02	2.16E+02	2.14E+02	2.29E+02	2.16E+02
Cu Ka	1.5418	1.58E+02	1.68E+02	1.87E+02	1.84E+02	1.91E+02	1.88E+02	2.01E+02	1.88E+02
Cu Kb <sub>1</sub>	1.3922	1.22E+02	1.30E+02	1.43E+02	1.42E+02	1.48E+02	1.45E+02	1.55E+02	1.41E+02
Mo Ka	0.7107	9.04E+01	9.38E+01	9.74E+01	1.00E+02	1.04E+02	1.07E+02	1.12E+02	1.15E+02
Mo Kb <sub>1</sub>	0.6323	6.67E+01	6.92E+01	7.19E+01	7.41E+01	7.70E+01	7.97E+01	8.29E+01	8.54E+01
Characteristic radiation	Wavelength (Å)	81 Thallium	82 Lead	83 Bismuth	84 Polonium	85 Astatine	86 Radon	87 Francium	88 Radium
	Atomic weight	204.3833	207.2	208.9804	[210]	[210]	[222]	[223]	[226]
	Density	11.87	11.34	9.80			4.40 (liq., 211K)		
	$\Theta$ (K)	78.5	105	119					
Cr Ka	2.2910	5.97E+02	6.43E+02	6.66E+02	6.91E+02	6.80E+02	7.34E+02	7.58E+02	7.43E+02
Cr Kb <sub>1</sub>	2.0849	4.87E+02	5.07E+02	5.24E+02	5.44E+02	5.33E+02	5.76E+02	5.97E+02	5.85E+02
Fe Ka	1.9374	4.03E+02	4.20E+02	4.34E+02	4.52E+02	4.44E+02	4.77E+02	4.93E+02	4.87E+02
Fe Kb <sub>1</sub>	1.7566	3.14E+02	3.27E+02	3.39E+02	3.54E+02	3.45E+02	3.73E+02	3.84E+02	3.80E+02
Co Ka	1.7903	3.31E+02	3.43E+02	3.55E+02	3.70E+02	3.63E+02	3.92E+02	4.03E+02	3.98E+02
Co Kb <sub>1</sub>	1.6208	2.57E+02	2.67E+02	2.76E+02	2.88E+02	2.82E+02	3.04E+02	3.12E+02	3.10E+02
Cu Ka	1.5418	2.26E+02	2.35E+02	2.44E+02	2.54E+02	2.48E+02	2.67E+02	2.77E+02	2.73E+02
Cu Kb <sub>1</sub>	1.3922	1.75E+02	1.81E+02	1.88E+02	1.96E+02	1.86E+02	2.05E+02	2.13E+02	2.10E+02
Mo Ka	0.7107	1.18E+02	1.22E+02	1.26E+02	1.32E+02	1.17E+02	1.08E+02	8.70E+01	8.80E+01
Mo Kb <sub>1</sub>	0.6323	8.79E+01	9.08E+01	9.41E+01	9.83E+01	1.02E+02	1.01E+02	1.04E+02	1.08E+01
Characteristic radiation	Wavelength (Å)	89 Actinium	90 Thorium	91 Protactinium	92 Uranium	93 Neptunium	94 Plutonium	95 Americium	96 Curium
	Atomic weight	[227]	232.0381	231.0359	238.0289	[237]	[239]	[243]	[247]
	Density		11.72		19.05		19.81		
	$\Theta$ (K)		163		207				
Cr Ka	2.2910	7.39E+02	7.68E+02	7.38E+02	7.66E+02	8.00E+02	7.60E+02	7.95E+02	8.12E+02
Cr Kb <sub>1</sub>	2.0849	6.18E+02	5.09E+02	5.82E+02	6.17E+02	6.30E+02	6.00E+02	6.27E+02	6.40E+02
Fe Ka	1.9374	5.30E+02	4.85E+02	4.82E+02	5.28E+02	5.52E+02	4.98E+02	5.81E+02	5.90E+02
Fe Kb <sub>1</sub>	1.7566	4.44E+02	3.89E+02	3.75E+02	4.00E+02	4.10E+02	3.89E+02	4.07E+02	4.21E+02
Co Ka	1.7903	4.61E+02	4.06E+02	3.94E+02	4.20E+02	4.30E+02	4.08E+02	4.26E+02	4.37E+02
Co Kb <sub>1</sub>	1.6208	3.81E+02	3.48E+02	3.06E+02	3.26E+02	3.35E+02	3.17E+02	3.33E+02	3.43E+02
Cu Ka	1.5418	3.17E+02	3.06E+02	2.71E+02	2.88E+02	3.14E+02	2.80E+02	3.22E+02	3.38E+02
Cu Kb <sub>1</sub>	1.3922	2.85E+02	2.19E+02	2.08E+02	2.22E+02	2.27E+02	2.16E+02	2.27E+02	2.32E+02
Mo Ka	0.7107	9.08E+01	9.65E+01	1.01E+02	1.02E+02	4.22E+01	3.99E+01	4.81E+01	4.90E+01
Mo Kb <sub>1</sub>	0.6323	1.10E+02	9.87E+01	1.19E+02	7.49E+01	1.25E+02	1.29E+02	1.31E+02	1.34E+02

$\Theta$ : Debye temperature, Unit of density: Mg/m<sup>3</sup>.

### A.3 Atomic Scattering Factors as a Function of $\sin \theta / \lambda$

$\frac{\sin \theta}{\lambda} (\text{\AA}^{-1})$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
H	1	0.81	0.48	0.25	0.13	0.07	0.04	0.03	0.02	0.01
He	2	1.88	1.46	1.05	0.75	0.52	0.35	0.24	0.18	0.14
Li	3	2.2	1.8	1.5	1.3	1.0	0.8	0.6	0.5	0.4
Be	4	2.9	1.9	1.7	1.6	1.4	1.2	1.0	0.9	0.7
B	5	3.5	2.4	1.9	1.7	1.5	1.4	1.2	1.2	1.0
C	6	4.6	3.0	2.2	1.9	1.7	1.6	1.4	1.3	1.16
N	7	5.8	4.2	3.0	2.3	1.9	1.65	1.54	1.49	1.39
O	8	7.1	5.3	3.9	2.9	2.2	1.8	1.6	1.5	1.4
F	9	7.8	6.2	4.45	3.35	2.65	2.15	1.9	1.7	1.6
Ne	10	9.3	7.5	5.8	4.4	3.4	2.65	2.2	1.9	1.65
Na	11	9.65	8.2	6.7	5.25	4.05	3.2	2.65	2.25	1.95
Mg	12	10.5	8.6	7.25	5.95	4.8	3.85	3.15	2.55	2.2
Al	13	11.0	8.95	7.75	6.6	5.5	4.5	3.7	3.1	2.65
Si	14	11.35	9.4	8.2	7.15	6.1	5.1	4.2	3.4	2.95
P	15	12.4	10.0	8.45	7.45	6.5	5.65	4.8	4.05	3.4
S	16	13.6	10.7	8.95	7.85	6.85	6.0	5.25	4.5	3.9
Cl	17	14.6	11.3	9.25	8.05	7.25	6.5	5.75	5.05	4.4
A	18	15.9	12.6	10.4	8.7	7.8	7.0	6.2	5.4	4.7
K	19	16.5	13.3	10.8	9.2	7.9	6.7	5.9	5.2	4.6
Ca	20	17.5	14.1	11.4	9.7	8.4	7.3	6.3	5.6	4.9
Sc	21	18.4	14.9	12.1	10.3	8.9	7.7	6.7	5.9	5.3
Ti	22	19.3	15.7	12.8	10.9	9.5	8.2	7.2	6.3	5.6
V	23	20.2	16.6	13.5	11.5	10.1	8.7	7.6	6.7	5.9
Cr	24	21.1	17.4	14.2	12.1	10.6	9.2	8.0	7.1	6.3
Mn	25	22.1	18.2	14.9	12.7	11.1	9.7	8.4	7.5	6.6
Fe	26	23.1	18.9	15.6	13.3	11.6	10.2	8.9	7.9	7.0
Co	27	24.1	19.8	16.4	14.0	12.4	10.7	9.3	8.3	7.3
Ni	28	25.0	20.7	17.2	14.6	12.7	11.2	9.8	8.7	7.7
Cu	29	25.9	21.6	17.9	15.2	13.3	11.7	10.2	9.1	8.1
Zn	30	26.8	22.4	18.6	15.8	13.9	12.2	10.7	9.6	8.5

(Continued)

$\frac{\sin \theta}{\lambda} (\text{\AA}^{-1})$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Ga	31	27.8	23.3	19.3	16.5	14.5	12.7	11.2	10.0	8.9
Ge	32	28.8	24.1	20.0	17.1	15.0	13.2	11.6	10.4	9.3
As	33	29.7	25.0	20.8	17.7	15.6	13.8	12.1	10.8	9.7
Se	34	30.6	25.8	21.5	18.3	16.1	14.3	12.6	11.2	10.0
Br	35	31.6	26.6	22.3	18.9	16.7	14.8	13.1	11.7	10.4
Kr	36	32.5	27.4	23.0	19.5	17.3	15.3	13.6	12.1	10.8
Rb	37	33.5	28.2	23.8	20.2	17.9	15.9	14.1	12.5	11.2
Sr	38	34.4	29.0	24.5	20.8	18.4	16.4	14.6	12.9	11.6
Y	39	35.4	29.9	25.3	21.5	19.0	17.0	15.1	13.4	12.0
Zr	40	36.3	30.8	26.0	22.1	19.7	17.5	15.6	13.8	12.4
Nb	41	37.3	31.7	26.8	22.8	20.2	18.1	16.0	14.3	12.8
Mo	42	38.2	32.6	27.6	23.5	20.8	18.6	16.5	14.8	13.2
Tc	43	39.1	33.4	28.3	24.1	21.3	19.1	17.0	15.2	13.6
Ru	44	40.0	34.3	29.1	24.7	21.9	19.6	17.5	15.6	14.1
Rh	45	41.0	35.1	29.9	25.4	22.5	20.2	18.0	16.1	14.5
Pd	46	41.9	36.0	30.7	26.2	23.1	20.8	18.5	16.6	14.9
Ag	47	42.8	36.9	31.5	26.9	23.8	21.3	19.0	17.1	15.3
Cd	48	43.7	37.7	32.2	27.5	24.4	21.8	19.6	17.6	15.7
In	49	44.7	38.6	33.0	28.1	25.0	22.4	20.1	18.0	16.2
Sn	50	45.7	39.5	33.8	28.7	25.6	22.9	20.6	18.5	16.6
Sb	51	46.7	40.4	34.6	29.5	26.3	23.5	21.1	19.0	17.0
Te	52	47.7	41.3	35.4	30.3	26.9	24.0	21.7	19.5	17.5
I	53	48.6	42.1	36.1	31.0	27.5	24.6	22.2	20.0	17.9
Xe	54	49.6	43.0	36.8	31.6	28.0	25.2	22.7	20.4	18.4
Cs	55	50.7	43.8	37.6	32.4	28.7	25.8	23.2	20.8	18.8
Ba	56	51.7	44.7	38.4	33.1	29.3	26.4	23.7	21.3	19.2
La	57	52.6	45.6	39.3	33.8	29.8	26.9	24.3	21.9	19.7
Ce	58	53.6	46.5	40.1	34.5	30.4	27.4	24.8	22.4	20.2
Pr	59	54.5	47.4	40.9	35.2	31.1	28.0	25.4	22.9	20.6
Nd	60	55.4	48.3	41.6	35.9	31.8	28.6	25.9	23.4	21.1
Pm	61	56.4	49.1	42.4	36.6	32.4	29.2	26.4	23.9	21.5
Sm	62	57.3	50.0	43.2	37.3	32.9	29.8	26.9	24.4	22.0
Eu	63	58.3	50.9	44.0	38.1	33.5	30.4	27.5	24.9	22.4
Gd	64	59.3	51.7	44.8	38.8	34.1	31.0	28.1	25.4	22.9
Tb	65	60.2	52.6	45.7	39.6	34.7	31.6	28.6	25.9	23.4

(Continued)

$\frac{\sin \theta}{\lambda} (\text{\AA}^{-1})$	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
Dy	66	61.1	53.6	46.5	40.4	35.4	32.2	29.2	26.3	23.9
Ho	67	62.1	54.5	47.3	41.1	36.1	32.7	29.7	26.8	24.3
Er	68	63.0	55.3	48.1	41.7	36.7	33.3	30.2	27.3	24.7
Tm	69	64.0	56.2	48.9	42.4	37.4	33.9	30.8	27.9	25.2
Yb	70	64.9	57.0	49.7	43.2	38.0	34.4	31.3	28.4	25.7
Lu	71	65.9	57.8	50.4	43.9	38.7	35.0	31.8	28.9	26.2
Hf	72	66.8	58.6	51.2	44.5	39.3	35.6	32.3	29.3	26.7
Ta	73	67.8	59.5	52.0	45.3	39.9	36.2	32.9	29.8	27.1
W	74	68.8	60.4	52.8	46.1	40.5	36.8	33.5	30.4	27.6
Re	75	69.8	61.3	53.6	46.8	41.1	37.4	34.0	30.9	28.1
Os	76	70.8	62.2	54.4	47.5	41.7	38.0	34.6	31.4	28.6
Ir	77	71.7	63.1	55.3	48.2	42.4	38.6	35.1	32.0	29.0
Pt	78	72.6	64.0	56.2	48.9	43.1	39.2	35.6	32.5	29.5
Au	79	73.6	65.0	57.0	49.7	43.8	39.8	36.2	33.1	30.0
Hg	80	74.6	65.9	57.9	50.5	44.4	40.5	36.8	33.6	30.6
Tl	81	75.5	66.7	58.7	51.2	45.0	41.1	37.4	34.1	31.1
Pb	82	76.5	67.5	59.5	51.9	45.7	41.6	37.9	34.6	31.5
Bi	83	77.5	68.4	60.4	52.7	46.4	42.2	38.5	35.1	32.0
Po	84	78.4	69.4	61.3	53.5	47.1	42.8	39.1	35.6	32.6
At	85	79.4	70.3	62.1	54.2	47.7	43.4	39.6	36.2	33.1
Rn	86	80.3	71.3	63.0	55.1	48.4	44.0	40.2	36.8	33.5
Fr	87	81.3	72.2	63.8	55.8	49.1	44.5	40.7	37.3	34.0
Ra	88	82.2	73.2	64.6	56.5	49.8	45.1	41.3	37.8	34.6
Ac	89	83.2	74.1	65.5	57.3	50.4	45.8	41.8	38.3	35.1
Th	90	84.1	75.1	66.3	58.1	51.1	46.5	42.4	38.8	35.5
Pa	91	85.1	76.0	67.1	58.8	51.7	47.1	43.0	39.3	36.0
U	92	86.0	76.9	67.9	59.6	52.4	47.7	43.5	39.8	36.5
Np	93	87	78	69	60	53	48	44	40	37
Pu	94	88	79	69	61	54	49	44	41	38
Am	95	89	79	70	62	55	50	45	42	38
Cm	96	90	80	71	62	55	50	46	42	39
Bk	97	91	81	72	63	56	51	46	43	39
Cf	98	92	82	73	64	57	52	47	43	40

## A.4 Quadratic Forms of Miller Indices for Cubic and Hexagonal Systems

$h^2+k^2+l^2$	Cubic				Hexagonal	
	$h \ k \ l$				$h^2+hk+k^2$	$h \ k$
	Simple	Face centered	Body centered	Diamond		
1	100				1	10
2	110				2	
3	111	111		110	3	11
4	200	200		200	4	20
5	210				5	
6	211			211	6	
7					7	21
8	220	220		220	8	
9	300,221			220	9	30
10	310		310		10	
11	311	311		311	11	
12	222	222		222	12	
13	320				13	22
14	321			321	14	31
15					15	
16	400	400		400	16	
17	410,322			400	17	40
18	411,330			411,330	18	
19	331	331			19	
20	420	420		420	20	32
21	421				21	41
22	332			332	22	
23					23	
24	422	422		422	24	
25	500,430				25	
26	510,431			510,431	26	50
27	511,333	511,333			27	
28				511,333	28	
29	520,432				29	
30	521		521		30	42
31					31	
32	440	440		440	32	
33	522,441				33	
34	530,433			530,433	34	
35	531	531			35	
36	600,442	600,442		600,442	36	
37	610				37	60
38	611,532			611,532	38	
39					39	
40	620	620		620	40	52
41	621,540,443				41	
42	541			541	42	
43	533	533			43	
44	622	622		622	44	
45	630,542				45	
46	631			631	46	
47					47	
48	444	444		444	48	
49	700,632			444	49	
50	710,550,543			710,550,543	50	70,53
51	711,551	711,551			51	
52	640	640		640	52	
53	720,641				53	
54	721,633,552			721,633,552	54	
55					55	
56	642	642		642	56	
57	722,544				57	
58	730			730	58	
59	731,553	731,553			59	

## A.5 Volume and Interplanar Angles of a Unit Cell

### Cellvolumes

Cubic :  $V = a^3$

Tetragonal :  $V = a^2c$

Hexagonal :  $V = \frac{\sqrt{3}a^2c}{2} = 0.866a^2c$

Trigonal :  $V = a^3\sqrt{1 - 3\cos^2\alpha + 2\cos^3\alpha}$

Orthorhombic :  $V = abc$

Monoclinic :  $V = abc \sin\beta$

Triclinic :  $V = abc \sqrt{1 - \cos^2\alpha - \cos^2\beta - \cos^2\gamma + 2\cos\alpha\cos\beta\cos\gamma}$

### Interplanar angles

The angle  $\phi$  between the plane ( $h_1k_1l_1$ ) of spacing  $d_1$  and the plane ( $h_2k_2l_2$ ) of  $d_2$  is estimated from the following equation, where  $V$  is the volume of a unit cell:

$$\text{Cubic : } \cos\phi = \frac{h_1h_2 + k_1k_2 + l_1l_2}{\sqrt{(h_1^2 + k_1^2 + l_1^2)(h_2^2 + k_2^2 + l_2^2)}}$$

$$\text{Tetragonal : } \cos\phi = \frac{\frac{h_1h_2+k_1k_2}{a^2} + \frac{l_1l_2}{c^2}}{\sqrt{\left(\frac{h_1^2+k_1^2}{a^2} + \frac{l_1^2}{c^2}\right)\left(\frac{h_2^2+k_2^2}{a^2} + \frac{l_2^2}{c^2}\right)}}$$

$$\text{Hexagonal : } \cos\phi = \frac{h_1h_2 + k_1k_2 + \frac{1}{2}(h_1k_2 + h_2k_1) + \frac{3a^2}{4c^2}l_1l_2}{\sqrt{(h_1^2+k_1^2+h_1k_1+\frac{3a^2}{4c^2}l_1^2)(h_2^2+k_2^2+h_2k_2+\frac{3a^2}{4c^2}l_2^2)}}$$

$$\begin{aligned} \text{Trigonal : } \cos\phi &= \frac{a^4d_1d_2}{V^2}[\sin^2\alpha(h_1h_2 + k_1k_2 + l_1l_2) \\ &\quad + (\cos^2\alpha - \cos\alpha)(k_1l_2 + k_2l_1 + l_1h_2 + l_2h_1 + h_1k_2 + h_2k_1)] \end{aligned}$$

$$\text{Orthorhombic : } \cos\phi = \frac{\frac{h_1h_2}{a^2} + \frac{k_1k_2}{b^2} + \frac{l_1l_2}{c^2}}{\sqrt{\left(\frac{h_1^2}{a^2} + \frac{k_1^2}{b^2} + \frac{l_1^2}{c^2}\right)\left(\frac{h_2^2}{a^2} + \frac{k_2^2}{b^2} + \frac{l_2^2}{c^2}\right)}}$$

$$\text{Monoclinic : } \cos\phi = \frac{d_1d_2}{\sin^2\beta} \left[ \frac{h_1h_2}{a^2} + \frac{k_1k_2 \sin^2\beta}{b^2} + \frac{l_1l_2}{c^2} - \frac{(l_1h_2 + l_2h_1) \cos\beta}{ac} \right]$$

$$\begin{aligned} \text{Triclinic : } \cos\phi &= \frac{d_1d_2}{V^2} [S_{11}h_1h_2 + S_{22}k_1k_2 + S_{33}l_1l_2 \\ &\quad + S_{23}(k_1l_2 + k_2l_1) + S_{13}(l_1h_2 + l_2h_1) + S_{12}(h_1k_2 + h_2k_1)] \end{aligned}$$

$$S_{11} = b^2c^2 \sin^2\alpha \quad S_{12} = abc^2(\cos\alpha \cos\beta - \cos\gamma)$$

$$S_{22} = a^2c^2 \sin^2\beta \quad S_{23} = a^2bc(\cos\beta \cos\gamma - \cos\alpha)$$

$$S_{33} = a^2b^2 \sin^2\gamma \quad S_{13} = ab^2c(\cos\gamma \cos\alpha - \cos\beta)$$

## A.6 Numerical Values for Calculation of the Temperature Factor

Values of  $\phi(x) = \frac{1}{x} \int_0^x \frac{\xi}{e^\xi - 1} d\xi$      $x = \frac{\Theta}{T}$ ,  $\Theta$ : Debye temperature

$x$	.0	.1	.2	.3	.4	.5	.6	.7	.8	.9
0	1.000	0.975	0.951	0.928	0.904	0.882	0.860	0.839	0.818	0.797
1	0.778	0.758	0.739	0.721	0.703	0.686	0.669	0.653	0.637	0.622
2	0.607	0.592	0.578	0.565	0.552	0.539	0.526	0.514	0.503	0.491
3	0.480	0.470	0.460	0.450	0.440	0.431	0.422	0.413	0.404	0.396
4	0.388	0.380	0.373	0.366	0.359	0.352	0.345	0.339	0.333	0.327
5	0.321	0.315	0.310	0.304	0.299	0.294	0.289	0.285	0.280	0.276
6	0.271	0.267	0.263	0.259	0.255	0.251	0.248	0.244	0.241	0.237

For  $x$  larger than 7,  $\phi(x)$  values are approximated by  $(1.642/x)$ .

Debye temperatures are compiled in Appendix A.2 using the following reference:  
(C.Kittel: *Introduction to Solid State Physics*, 6th Edition, John Wiley & Sons, New York (1986), p.110.)

## A.7 Fundamentals of Least-Squares Analysis

Let us consider that the number of  $n$ -points have coordinates  $(x_1, y_1), (x_2, y_2) \dots (x_n, y_n)$ , and the  $x$  and  $y$  are related by a straight line with the form of  $y = a + bx$ . Our problem is to find the best value of  $a$  and  $b$  which makes the sum of the squared errors a minimum by using the least-squares method. In this case, we use the following two normal equations:

$$\sum y = \sum a + b \sum x, \quad (1)$$

$$\sum xy = a \sum x + b \sum x^2. \quad (2)$$

For given  $n$ -points, the following four steps are suggested:

- (i) Substitute the experimental data into  $y = a + bx$  for obtaining  $n$ -equations.

$$\left. \begin{array}{l} y_1 = a + bx_1 \\ y_2 = a + bx_2 \\ \vdots \\ y_n = a + bx_n \end{array} \right\}. \quad (3)$$

- (ii) Multiply each equation by the coefficient of  $a$  (1 in the present case) and add for obtaining the first normal equation.

$$\begin{aligned} y_1 &= a + bx_1, \\ y_2 &= a + bx_2, \\ &\vdots \\ y_n &= a + bx_n, \\ \hline \sum^n y &= \sum a + b \sum x. \end{aligned} \quad (4)$$

- (iii) Multiply each equation by the coefficient  $b$  and add for obtaining the second normal equation.

$$\begin{aligned} x_1 y_1 &= x_1 a + b x_1^2, \\ x_2 y_2 &= x_2 a + b x_2^2, \\ &\vdots \\ x_n y_n &= x_n a + b x_n^2 \\ \hline \sum^n xy &= a \sum x + b \sum x^2 \end{aligned} \quad (5)$$

- (iv) Simultaneous solution of the two equations of (4) and (5) yields the value of  $a$  and  $b$ .

## A.8 Prefixes to Unit and Greek Alphabet

Notation	Symbol	Factor	Notation	Symbol	Factor
exa	E	$10^{18}$	deci	d	$10^{-1}$
peta	P	$10^{15}$	centi	c	$10^{-2}$
tera	T	$10^{12}$	milli	m	$10^{-3}$
giga	G	$10^9$	micro	μ	$10^{-6}$
mega	M	$10^6$	nano	n	$10^{-9}$
kilo	k	$10^3$	pico	p	$10^{-12}$
hecto	h	$10^2$	femto	f	$10^{-15}$
deca	da	10	atto	a	$10^{-18}$

### Greek alphabet

$A, \alpha$ .....	Alpha	$N, \nu$ .....	Nu
$B, \beta$ .....	Beta	$\Xi, \zeta$ .....	Xi
$\Gamma, \gamma$ .....	Gamma	$O, \sigma$ .....	Omicron
$\Delta, \delta$ .....	Delta	$\Pi, \pi$ .....	Pi
$E, \varepsilon$ .....	Epsilon	$P, \rho$ .....	Rho
$Z, \zeta$ .....	Zeta	$\Sigma, \sigma$ .....	Sigma
$H, \eta$ .....	Eta	$T, \tau$ .....	Tau
$\Theta, \vartheta, \theta$ .....	Theta	$Y, \upsilon$ .....	Upsilon
$I, \iota$ .....	Iota	$\Phi, \varphi, \phi$ .....	Phi
$K, \kappa$ .....	Kappa	$X, \chi$ .....	Chi
$\Lambda, \lambda$ .....	Lambda	$\Psi, \psi$ .....	Psi
$M, \mu$ .....	Mu	$\Omega, \omega$ .....	Omega

## A.9 Crystal Structures of Some Elements and Compounds

Elements or compounds	Crystal systems	Lattice parameter	
Al	<i>fcc</i>	$a = 0.40497 \text{ nm}$	
$\alpha\text{-Al}_2\text{O}_3$	hexagonal (corundum structure)	$a = 0.4763 \text{ nm}$	$c = 0.13003 \text{ nm}$
Au	<i>fcc</i>	$a = 0.40786 \text{ nm}$	
CaO	NaCl	$a = 0.48105 \text{ nm}$	
CaF <sub>2</sub>	ZnS	$a = 0.5463 \text{ nm}$	
Cr	<i>bcc</i>	$a = 0.28847 \text{ nm}$	
CsCl	CsCl	$a = 0.4123 \text{ nm}$	
Cu	<i>fcc</i>	$a = 0.36148 \text{ nm}$	
CuCl	ZnS	$a = 0.54057 \text{ nm}$	
Cu <sub>2</sub> O	CsCl(cuprite structure)	$a = 0.42696 \text{ nm}$	
Fe $\alpha$	<i>bcc</i>	$a = 0.28665 \text{ nm}$	
$\gamma$	<i>fcc</i>	$a = 0.36469 \text{ nm}$	
$\delta$	<i>bcc</i>	$a = 0.29323 \text{ nm}$	
FeS	NaCl(pyrite structure)	$a = 0.5408 \text{ nm}$	
K	<i>bcc</i>	$a = 0.5247 \text{ nm}$	
Mg	<i>hcp</i>	$a = 0.32095 \text{ nm}$	$c = 0.52107 \text{ nm}$
MgO	NaCl	$a = 0.42112 \text{ nm}$	
Mo	<i>bcc</i>	$a = 0.31469 \text{ nm}$	
NaCl	NaCl	$a = 0.56406 \text{ nm}$	
NaF	NaCl	$a = 0.4620 \text{ nm}$	
Ni	<i>fcc</i>	$a = 0.35239 \text{ nm}$	
NiO	NaCl	$a = 0.41769 \text{ nm}$	
Pt	<i>fcc</i>	$a = 0.39240 \text{ nm}$	
Si	diamond	$a = 0.54309 \text{ nm}$	
SiO <sub>2</sub>	$\alpha\text{-quartz}$ (Rhombohedral)	$a = 0.4913 \text{ nm}$	$c = 0.5405 \text{ nm}$
	$\beta\text{-quartz}$ (hexagonal)	$a = 0.501 \text{ nm}$	$c = 0.547 \text{ nm}$
	Tridymite (hexagonal)	$a = 0.503 \text{ nm}$	$c = 0.822 \text{ nm}$
	$\alpha\text{-crystobalite}$ (hexagonal)	$a = 0.4973 \text{ nm}$	$c = 0.6926 \text{ nm}$
Ti	<i>hcp</i>	$a = 0.29512 \text{ nm}$	$c = 0.46845 \text{ nm}$
TiC	NaCl	$a = 0.43186 \text{ nm}$	
TiO <sub>2</sub>	CsCl(rutile structure)	$a = 0.45929 \text{ nm}$	$c = 0.29591 \text{ nm}$
W	<i>bcc</i>	$a = 0.31653 \text{ nm}$	
Zn	<i>hcp</i>	$a = 0.26650 \text{ nm}$	$c = 0.49470 \text{ nm}$
$\beta\text{-ZnS}$	ZnS	$a = 0.54109 \text{ nm}$	

These data are taken from the following references.

B.D. Cullity: Elements of X-ray Diffraction (2nd Edition), Addison-Wesley (1978).

F.S. Galasso: Structure and Properties of Inorganic Solids, PergamonPress (1970).