Extended Private Information Retrieval and Its Application in Biometrics Authentications*

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Abstract. In this paper we generalize the concept of Private Information Retrieval (PIR) by formalizing a new cryptographic primitive, named Extended Private Information Retrieval (EPIR). Instead of enabling a user to retrieve a bit (or a block) from a database as in the case of PIR, an EPIR protocol enables a user to evaluate a function f which takes a string chosen by the user and a block from the database as input. Like PIR, EPIR can also be considered as a special case of the secure two-party computation problem (and more specifically the oblivious function evaluation problem). We propose two EPIR protocols, one for testing equality and the other for computing Hamming distance. As an important application, we show how to construct strong privacy-preserving biometric-based authentication schemes by employing these EPIR protocols.

1 Introduction

This paper describes a new primitive, Extended Private Information Retrieval (EPIR) which is a natural generalization of PIR, and two EPIR protocols, one for testing equality and the other for computing Hamming distance. This work is partially motivated by the growing privacy requirements in processing sensitive information such as biometrics.

1.1 Related Work

With respect to the functionality, an EPIR is indeed a combination of a PIR [10] and a general secure two-party computation protocol [26,49]. Next, we briefly review the literature in both areas.

The concept of PIR was proposed by Chor et al. [10]. A PIR protocol enables a user to retrieve a bit from a database which contains a bit string. Chor et al. defined user privacy for PIR in the information-theoretical setting, which captures the concept that the database (with unlimited resources) learns nothing about which bit the user has retrieved. They also proposed a number of multidatabase protocols that are secure in the information-theoretical setting. Chor

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and Gilboa [9] proposed to construct multi-database PIR under computational assumptions. Kushilevitz and Ostrovsky [32] presented a definition of user privacy in computational setting, where a PIR protocol achieves user privacy if, for any query for i-th bit, the database learns nothing about the index i. They showed that one can achieve single-database PIR under the Quadratic Residuosity assumption with communication complexity $O(N^c)$ for any c > 0, where N is the database size throughout the paper. Cachin, Micali, and Stadler [7] proposed a single-database PIR scheme with poly-logarithmic communication complexity $O((\log N)^8)$ based on the Φ -hiding assumption.

Chor et al. [10] also proposed the notion of Private Block Retrieval (PBR), a natural extension to single-bit PIR, in which instead of retrieving only one bit, the user retrieves a d-bit block. They proposed an efficient method for the transformation from PIR to PBR. Lipmaa [34] proposed a PBR scheme with communication complexity $\Theta(\Omega((\log N)^{3-o(1)})(\log N)^2 + d\log N)$. Gentry and Ramzan [23] proposed a single-database PBR protocol based on the decision subgroup problem, with communication complexity O(k+d) where $k \geq \log N$ is the security parameter.

Gertner et al. [24] introduced the notion of data privacy in the computational setting, where a PIR protocol achieves database privacy if, for any query, the user cannot tell whether it is an ideal-world execution or a real-world execution. In an ideal-world execution the user interacts with a simulator which takes only a single bit from the database as input, while in a real-world execution the user interacts with the database. If a PIR protocol achieves both user privacy and data privacy, then it is said to be SPIR (symmetrically-private information retrieval) which is also referred to as one-out-of-N oblivious transfer [13]. Mishra and Sarkar [35] proposed a single-server SPIR protocol which can have communication complexity $O(N^{\epsilon})$ for any $\epsilon > 0$. Their protocol is proven secure under the XOR assumption defined by Mishra and Sarkar.

Gasarch [22] provides a very detailed summary of PIR/PBR protocols and lower/upper bounds on communication complexity, and Ostrovsky and Skeith III [37] also provides a summary. To facilitate our discussion, we use the notation PIR to denote both PIR and PBR, and generalise the setting of PIR to be: a database \mathcal{DB} contains a list of N blocks $\mathbf{R} = (R_1, R_2, \dots, R_N)$, and a user \mathcal{U} can run a PIR protocol to retrieve R_i from \mathcal{DB} , for any $1 \leq i \leq N$.

As a special case of secure two-party computation problem, the concept of EPIR is relevant to the oblivious function evaluation [8,20,36]. Canetti et al. [8] study the problem that a client privately evaluate a public function which takes inputs from one or more servers. Note that the client does not have any private input to the function. Naor and Pinkas [36] study the problem that a receiver privately evaluates a function f(a) by interacting with a sender, where f is a secret polynomial of the sender and a is a secret input of the receiver. Freedman et al. [20] study the keyword search problem that a client privately evaluates whether a keyword is contained in a database. EPIR can be considered to be a generalization of the these problems (in the single database case). Next, we briefly review some works which are related to equality test and

hamming distance computation. In [11,19], the authors studied how to compare two commonly shared strings and determine whether they are the same. Freedman, Nissim, and Pinkas [21] studied two-party set-interaction problems and proposed a number of protocols. Du and Atallah [48,17] considered the secure computation in an environment similar to that of EPIR, and proposed protocols based on solutions to Yao's millionaire problem. Goethals et al. [25] showed the weakness in the private scalar product protocols [16,46] and proposed a new protocol based on homomorphic encryption schemes. Kiltz, Leander, and Malone-Lee [31] proposed some methods for a user to compute the mean (and other statistics) over the data in a database. However, they did not propose any specific security model for this type of computation, and their protocols either require a semi-trusted third party or are very inefficient in round and communication complexity. Note that Kiltz, Leander, and Malone-Lee [31] showed that some approach in [17] leaks information in some applications. Boneh, Goh, and Nissim [3] proposed an encryption scheme (referred to as the BGN encryption scheme) and used it for evaluating 2-DNF formulas. As an application, they showed how to construct efficient PIR protocols based on their encryption scheme.

1.2 Practical Motivation

Biometrics, such as fingerprint and iris, have been used to a high level of security in order to cope with the increasing demand for reliable and highly-usable information security systems, because they have many advantages over cryptographic credentials. However, there are some obstacles for a wide adoption of biometrics in practice. Among them, one is that biometric features are volatile over the time so that it cannot be integrated into most of the legacy systems. This means that approximate matching might be necessary for an identification or authentication. The other is that biometrics are usually considered to be sensitive, so that there is big privacy concern in using them. To address the volatility of biometrics, error-correction concept is widely used in the literature (e.g. [4,5,12,15,14,29,30,40]). Employing this concept, some public information is firstly generated based on a reference biometric template, and later, a newlycaptured template could help to recover the reference template if their distance (in a certain space) is not too large. In [33,42,43,44,47], the authors attempted to enhance privacy protection in biometric authentication schemes, where the privacy means that the compromise of the database will not enable the attacker to recover the biometric template. Ratha, Connell, and Bolle [2,39] introduced the concept of cancelable biometrics in an attempt to solve the revocation and privacy issues related to biometric information. More recently, Ratha et al. [38] intensively elaborated this concept in the case of fingerprint-based authentication systems. In addition, Atallah et al. [1] proposed a method, in which biometric templates are treated as bit strings and subsequently masked and permuted during the authentication process. Schoenmakers and Tuyls [41] proposed to use homomorphic encryption schemes for biometric authentication schemes by employing multi-party computation techniques. Practical concerns, security issues, and challenges about biometrics have been discussed in a number of papers (e.g. [2,39,45]).

Despite these efforts, there are still some concerns which require further investigation. The most important one is that privacy may mean much more than recovering the biometric template. For example, an application server may not be trusted to store biometric information, and, even if an independent database stores biometric information, the application server's access to the biometric information still needs to be restricted. In addition, it is desirable to simplify the storage requirements for the human users and the (communication) client. Bringer et al. [6] proposed a biometric-based authentication protocol which protects the sensitive relationship between a biometric feature and relevant pseudorandom identity. Their protocol makes use of the Goldwasser-Micali encryption scheme and is less efficient in communication than those described in Section 5.

1.3 Our Contributions

We generalize the concept of PIR by formalizing a new cryptographic primitive, named Extended Private Information Retrieval (EPIR). Instead of enabling a user to retrieve a block from a database as in the case of PIR, an EPIR protocol enables a user to evaluate a function f which takes a string chosen by the user and a block from the database as input¹. If f is defined to be a function that simply returns the block from the database then the EPIR protocol is indeed a traditional PIR protocol. Analogous to the privacy properties of PIR, we define two privacy properties for EPIR, including (1) user privacy which captures the concept that, for any query, the database should know nothing about block index the user has queried and the user's input to f, (2) database privacy captures the concept that, from a single query, the user should obtain no more information than the output of function f. Note that we focus on the single-database computational setting in this paper.

We further propose two EPIR protocols: one for testing equality and the other for computing Hamming distance. The first protocol is based on a PIR protocol and the ElGamal encryption scheme (described in Appendix A)[18], and the second protocol is based on a PIR protocol and the BGN encryption scheme (described in Appendix B) [3]. In both EPIR protocols, in order to achieve database privacy, the PIR protocols employed do not need to achieve database privacy.

As an important application, we show a modular way to construct biometric-based authentication schemes by employing an EPIR protocol. Due to the privacy properties of EPIR, these schemes achieve strong privacy properties against a malicious server and a malicious database which will not collude. It is worth noting that our proposal is not focused on a specific biometric, but rather on a generalization of biometrics which can be represented as binary strings in the Hamming space. Iris is such a type of biometric that can be easily encoded into a binary string [28].

 $^{^{1}}$ We assume that the index of the block from the database is also chosen by the user.

1.4 Organization of the Paper

The remainder of the paper is organized as follows. In Section 2 we present the security definitions for EPIR. In Section 3 we describe an EPIR protocol for testing equality of two binary strings based on the ElGamal encryption scheme. In Section 4 we describe an EPIR protocol for computing Hamming distance of two binary strings based on the BGN encryption scheme. In Section 5 we propose two biometric-based authentication schemes by employing these two EPIR protocols. In Section 6 we conclude the paper.

2 Privacy Definitions for EPIR

Formally, a (single-database) EPIR protocol involves two principals: a database \mathcal{DB} which holds a set of N blocks $\mathbf{R} = (R_1, R_2, \dots, R_N)$ where $R_j \in \{0, 1\}^{\ell_1}$ and ℓ_1 is an integer, a user \mathcal{U} which retrieves the value of a function $f(R_i, X)$ where $X \in \{0, 1\}^{k_1}$ is chosen by the user, k_1 is an integer, and the index i is also chosen by the user. We assume that the description of f is public and N is a public constant integer. Without loss of generality, we further assume that the retrieval is through a retrieve(f, i, X) query.

2.1 Notation

We first describe some conventions for writing probabilistic algorithms and experiments. The notation $x \stackrel{R}{\leftarrow} S$ means x is randomly chosen from the set S. If \mathcal{A} is a probabilistic algorithm, then $\mathcal{A}(\mathsf{Alg};\mathsf{Func})$ is the result of running \mathcal{A} , which can have any polynomial number of oracle queries to the functionality Func, interactively with Alg which answers the oracle query issued by \mathcal{A} . For clarity of description, if an algorithm \mathcal{A} runs in a number of stages then we write $\mathcal{A} = (\mathcal{A}_1, \mathcal{A}_2, \cdots)$. As a standard practice, the security of a protocol is evaluated by an experiment between an attacker and a challenger, where the challenger simulates the protocol executions and answers the attacker's oracle queries. Without specification, algorithms are always assumed to be polynomial-time.

Specifically, in our case, there is only one functionality, namely retrieve. If the attacker is a malicious \mathcal{DB} , the challenger samples the index i and X from the distribution specified in the protocol and issues retrieve queries to the attacker. If the attacker is a malicious \mathcal{U} then it can freely chooses the index i and X (that may derivate from the distribution specified in the protocol) and issues retrieve queries to the challenger.

In addition, we have the following definitions for negligible and overwhelming probabilities.

Definition 1. The function $P(\ell): \mathbb{Z} \to \mathbb{R}$ is said to be negligible if, for every polynomial $f(\ell)$, there exists an integer N_f such that $P(\ell) \leq \frac{1}{f(\ell)}$ for all $\ell \geq N_f$. If $P(\ell)$ is negligible, then the probability $1 - P(\ell)$ is said to be overwhelming.

2.2 User Privacy

This property is an analog to the user privacy property in the case of PIR where user privacy captures the concept that \mathcal{DB} knows nothing about block index that \mathcal{U} has queried. However, in the case of EPIR, we wish user privacy to imply more than that \mathcal{DB} knows nothing about the block index \mathcal{U} has queried. Consider a toy example, in which an EPIR protocol is constructed as follows: \mathcal{U} simply sends X to the database which computes $f(R_j, X)$ $(1 \leq j \leq N)$, and \mathcal{U} then runs a PIR to retrieve $f(R_i, X)$. It is clear that, if the PIR protocol achieves user privacy then \mathcal{DB} learns nothing about the index in the toy protocol. However, if $f(R_j, X)$ $(1 \leq j \leq N)$ are equal then \mathcal{DB} knows the result obtained by \mathcal{U} .

Informally, the user privacy for EPIR captures the concept that, for any retrieve(f, i, X) query, \mathcal{DB} knows nothing about the queried block index i and the user's string X. Formally, an EPIR protocol achieves user privacy if any attacker $\mathcal{A} = (\mathcal{A}_1, \mathcal{A}_2, \mathcal{A}_3, \mathcal{A}_4)$ has only a negligible advantage in the following game, where the attacker's advantage is $|\Pr[b' = b] - \frac{1}{2}|$.

$$\begin{aligned} \mathbf{Exp}^{\text{user-privacy}}_{\mathcal{A}} \\ \mathbf{R} &= (R_1, R_2, \cdots, R_N) &\leftarrow \mathcal{A}_1(1^{\ell}) \\ 1 &\leq i_0, i_1 \leq N; X_0, X_1 \in \{0, 1\}^{k_1} \leftarrow \mathcal{A}_2(Challenger; \text{retrieve}) \\ b & \overset{R}{\leftarrow} \{0, 1\} \\ \emptyset & \leftarrow \mathcal{A}_3(Challenger; \text{retrieve}(\mathbf{f}, i_b, X_b)) \\ b' & \leftarrow \mathcal{A}_4(Challenger; \text{retrieve}) \end{aligned}$$

In this game, the attacker \mathcal{A} is a malicious \mathcal{DB} . For the clarity, we rephrase the game as follows.

- 1. The attacker A_1 generates N blocks $\mathbf{R} = (R_1, R_2, \dots, R_N)$.
- 2. The attacker A_2 can request the challenger to start any (polynomial) number of retrieve queries. At some point, A_2 outputs (i_0, i_1, X_0, X_1) for a challenge.
- 3. The challenger randomly chooses $b \in \{0,1\}$ and issues a retrieve (f, i_b, X_b) query to the attacker A_3 .
- 4. The attacker A_4 can continue requesting the challenger to start any (polynomial) number of retrieve queries. At some point, A_4 outputs a guess b'.

Note that the symbol \emptyset means that the attacker \mathcal{A}_3 has no explicit output (besides the state information).

2.3 Database Privacy

This property is an analog to the database privacy property in the case of SPIR [24] and the formalization follows that for secure two-party computation [49,26]. Informally, database privacy captures the concept that, from a retrieve(f, i, X) query, \mathcal{U} obtains no more information than $f(R_{i'}, X')$ for some $1 \leq i' \leq N$ and $X' \in \{0, 1\}^{k_1}$. As in [24], we do not require that i' = i and X' = X because a malicious \mathcal{U} may construct the query without following the specification. The

concept can also be rephrased as follows: \mathcal{U} cannot tell whether it is an ideal-world execution and a real-world execution. In an ideal-world execution \mathcal{U} interacts with a simulator which takes $(i', f(R_{i'}, X'))$ as input, while in a real-world execution \mathcal{U} interacts with \mathcal{DB} .

For the clarity of formalization, let $\mathsf{simulator}_0$ denote \mathcal{DB} . Formally, an EPIR protocol achieves database privacy, if there exists a $\mathsf{simulator}_1$ such that any attacker $\mathcal{A} = (\mathcal{A}_1, \mathcal{A}_2)$ has only a negligible advantage in the following game, where the attacker's advantage is $|\Pr[b' = b] - \frac{1}{2}|$. For every retrieve query, $\mathsf{simulator}_1$ has an auxiliary input from a hypothetical oracle \mathcal{O} , where the input is $(i', \mathsf{f}(R_{i'}, X'))$ for some $1 \leq i' \leq N$ and $X' \in \{0, 1\}^{k_1}$.

$$\begin{bmatrix} \mathbf{Exp}_{\mathcal{A}}^{\text{database-privacy}} \\ b & \stackrel{R}{\leftarrow} \{0,1\} \\ \mathbf{R} = (R_1, R_2, \cdots, R_N) \leftarrow \mathcal{A}_1(1^{\ell}) \\ b' & \leftarrow \mathcal{A}_2(\mathsf{simulator}_b; \mathsf{retrieve}) \end{bmatrix}$$

In this game, the attacker A is a malicious U. For the clarity, we rephrase the game as follows.

- 1. The challenger randomly chooses $b \in \{0,1\}$. If b = 0 then simulator₀ answers the retrieve queries from the attacker; otherwise simulator₁ answers such queries.
- 2. The attacker A_1 generates N blocks $\mathbf{R} = (R_1, R_2, \dots, R_N)$.
- 3. The attacker A_2 can start any (polynomial) number of retrieve queries. At some point, A_2 outputs a guess b'.

We emphasize that the hypothetical oracle \mathcal{O} may have unlimited computing resources. In an attack game, a malicious \mathcal{U} may or may not generate a query by following the protocol specification, nonetheless, in order to answer the attacker's query, simulator₁ only needs to obtain $f(R_{i'}, X')$ for some $1 \leq i' \leq N$ and $X' \in \{0, 1\}^{k_1}$. As a result, if the attacker cannot distinguish the interactions with simulator₀ and simulator₁, then, for each query, it obtains no more information about \mathbf{R} than i' and $f(R_{i'}, X')$, which is what simulator₁ needs to answer the query.

2.4 Security of EPIR

Analogous to the case of other primitives, a (useful) EPIR protocol should be sound, which means that if both \mathcal{U} and \mathcal{DB} follow the protocol specification then retrieve(f, i, X) always returns the correct value of f(R_i, X) with an overwhelming probability.

Definition 2. An EPIR protocol is said to be secure if any attacker has only negligible advantage in the attack games for user privacy and database privacy.

3 EPIR Protocol for Testing Equality

In this section we present an EPIR protocol which enables \mathcal{U} to compare a string with a block from \mathcal{DB} . The function $f(R_i, X)$ is defined to be 1 if $R_i = X$ and to be 0 otherwise. Suppose every block in \mathcal{DB} has bit-length ℓ_1 , X also has bit-length ℓ_1 , and N has bit-length ℓ_2 .

The construction is based on the ElGamal scheme and a PIR protocol. It is worth noting that, due to the randomization in step 3, the employed PIR protocol does not need to be SPIR (achieving database privacy) in order to guarantee the database privacy for the EPIR.

3.1 Description of the Protocol

The EPIR protocol is as follows.

- 1. \mathcal{U} generates an ElGamal key pair (pk, sk), where pk = (p, q, g, y), $y = g^x$, and sk = x is randomly chosen from \mathbb{Z}_q . It is required that the bit-length of q is at least $\ell_1 + \ell_2 + 1$. Let "||" be the string concatenation operator.
- 2. To retrieve the value $f(R_i, X)$, for any $1 \le i \le N$ and $X \in \{0, 1\}^{\ell_1}$, \mathcal{U} first sends pk and an ElGamal ciphertext $(g^r, y^r g^{i||X})$ to \mathcal{DB} , where r is randomly chosen from \mathbb{Z}_q .
- 3. After receiving pk and $(g^r, y^r g^{i||X})$ from \mathcal{U} , \mathcal{DB} first checks that pk is a valid ElGamal public key² and $(g^r, y^r g^{i||X})$ is a valid ElGamal ciphertext. If the check succeeds, \mathcal{DB} computes C_j for every $1 \leq j \leq N$, where r_j, r'_j are randomly chosen from \mathbb{Z}_q and

$$C_j = (g^{r'_j}(g^r)^{r_j}, y^{r'_j}(y^r g^{i|X}(g^{j|R_j})^{-1})^{r_j}).$$

4. \mathcal{U} runs a PIR protocol to retrieve C_i from \mathcal{DB} . \mathcal{U} then sets f(i,X)=1 if $Dec(C_i,sk)=1$ and sets f(i,X)=0 otherwise.

It is clear that, in our case, no encoding algorithm Ω is required to guarantee the semantic security of the ElGamal scheme. As to the performance, the communication complexity is dominated by that of the PIR protocol. The computational complexity is dominated by the computation of C_j $(1 \leq j \leq N)$, say O(N) exponentiations for \mathcal{DB} . Moreover, it is straightforward to verify the following observation.

Observation 1. For every $1 \leq j \leq N$, if $g^{i||X}(g^{j||R_j})^{-1} \neq 1$, the components of $C_j = (C_{j1}, C_{j2})$ are uniformly and independently distributed over \mathbb{G} ; otherwise C_{j1} is uniformly distributed over \mathbb{G} and $C_{j2} = (C_{j1})^x$.

Due to the bit-length requirement on q, if $\ell_1 + \ell_2 + 1$ is very large then the protocol may become impractical. Note that ℓ_2 will be bounded by a reasonably small integer (say 50), because it is hard to imagine that we have a database

In practice, the validity of pk can be certified by a TTP, and the same pk can be used by the user for all his queries.

with 2^{50} records. As a result, in this situation, a simple solution is to work on the records $\mathbf{R}' = (R'_1, R'_2, \dots, R'_N)$ instead of \mathbf{R} , where $R'_j = \mathsf{H}(R_j)$ $(1 \le j \le N)$ and H is a collision-resistant hash function with a reasonable output bit-length. Inherently, \mathcal{U} issues a retrieve(f, i, $\mathsf{H}(X)$) query to retrieve the value of $\mathsf{f}(R_i, X)$. It is clear that \mathcal{U} gets the correct answer with an overwhelming probability.

Instead of employing the ElGamal encryption scheme, other homomorphic encryption schemes may also be used here though we will need a different randomization method in step 3.

3.2 Security Analysis

It is straightforward to verify that if the PIR protocol is sound then the EPIR protocol for equality is also sound. The following lemmas show that the EPIR protocol achieves user privacy and database privacy but their proofs will appear in the full version of this paper.

Lemma 1 (user privacy). If the PIR protocol achieves user privacy, then the EPIR protocol for testing equality achieves user privacy based on the DDH assumption.

Lemma 2 (database privacy). The EPIR protocol for testing equality achieves database privacy (unconditionally).

4 EPIR Protocol for Computing Hamming Distance

In this section we present an EPIR protocol which enables \mathcal{U} to compute Hamming distance between a string chosen by itself and a block from \mathcal{DB} . Especially, the protocol allows the user to assign a weight for every bit. For an ℓ_1 -bit string S, let $S^{(k)}$ denote the k-th bit of S. Let the weight vector be $(w_1, w_2, \dots, w_{\ell_1})$ where w_k $(1 \leq k \leq \ell_1)$ are integers. The function f is defined as follows.

$$f(R_i, X) = \sum_{k=1}^{\ell_1} w_k(R_i^{(k)} \oplus X^{(k)})$$

The construction is based on the BGN encryption scheme [3], the GOS NIZK protocol [27], and a PIR protocol. It is worth noting that, due to the randomization in step 3, the employed PIR protocol does not need to be SPIR (achieving database privacy) in order to guarantee the database privacy for the EPIR.

4.1 Description of the Protocol

Suppose every block in \mathcal{DB} has bit-length ℓ_1 . The EPIR protocol is as follows.

1. \mathcal{U} generates a key pair (pk, sk) for the BGN encryption scheme, where $pk = (n, \mathbb{G}, \mathbb{G}_1, \hat{e}, g, h)$, and $sk = q_1$.

- 2. To retrieve the value of $f(R_i, X)$, for any $1 \leq i \leq N$ and $X \in \{0, 1\}^{\ell_1}$, \mathcal{U} first sends BGN ciphertexts c and c_k $(1 \leq k \leq \ell_1)$ to \mathcal{DB} , where $c = g^i h^r$, $c_k = g^{X^{(k)}} h^{s_k}$ $(1 \leq k \leq \ell_1)$, r and s_k $(1 \leq k \leq \ell_1)$ are randomly chosen from \mathbb{Z}_n . In addition, \mathcal{U} also sends $proof_k$ $(1 \leq k \leq \ell_1)$ to \mathcal{DB} , where, for every $1 \leq k \leq \ell_1$, $proof_k$ is the GOS NIZK parameter for proving $X^{(k)} \in \{0, 1\}$.
- 3. After receiving c, c_k $(1 \le k \le \ell_1)$, and $proof_k$ $(1 \le k \le \ell_1)$ from \mathcal{U} , \mathcal{DB} first checks that pk is a valid BGN public key³ and c, c_k $(1 \le k \le \ell_1)$ are valid BGN ciphertexts. If the check succeeds, \mathcal{DB} verifies $proof_k$ $(1 \le k \le \ell_1)$. If the verification succeeds, \mathcal{DB} computes C_j for every $1 \le j \le N$ as follows.
 - (a) For every $1 \le k \le \ell_1$, compute $m_{i,k}$ where

$$\begin{split} m_{j,k} &= \frac{\hat{e}(c_k g^{R_j^{(k)}}, g)}{\hat{e}(c_k, g^{R_j^{(k)}})^2} \\ &= \frac{\hat{e}(g^{X^{(k)}} h^{s_k} g^{R_j^{(k)}}, g)}{\hat{e}(g^{X^{(k)}} h^{s_k}, g^{R_j^{(k)}})^2} \\ &= \frac{\hat{e}(g^{X^{(k)}} h^{s_k}, g^{R_j^{(k)}})^2}{\hat{e}(g^{X^{(k)}}, g^{R_j^{(k)}})^2 \hat{e}(h^{s_k}, g)} \\ &= \frac{\hat{e}(g^{X^{(k)}} g^{R_j^{(k)}}, g) \hat{e}(h^{s_k}, g^{R_j^{(k)}})^2}{\hat{e}(g^{X^{(k)}}, g^{R_j^{(k)}})^2 \hat{e}(h^{s_k}, g^{R_j^{(k)}})^2} \\ &= \hat{e}(g, g)^{X^{(k)} + R_j^{(k)}} \hat{e}(h, g)^{s_k(1 - 2R_j^{(k)})} \\ &= \hat{e}(g, g)^{X^{(k)} \oplus R_j^{(k)}} \hat{e}(h, g)^{s_k(1 - 2R_j^{(k)})} \end{split}$$

(b) Compute C_j , where r_j, r'_j are randomly chosen from \mathbb{Z}_n and

$$C_{j} = \hat{e}(cg^{-j}h^{r'_{j}},g)^{r_{j}} \prod_{k=1}^{\ell_{1}} (m_{j,k})^{w_{k}}$$

$$= \hat{e}(g^{i-j}h^{r+r'_{j}},g)^{r_{j}} \prod_{k=1}^{\ell_{1}} \hat{e}(g,g)^{w_{k}(X^{(k)} \oplus R_{j}^{(k)})} \hat{e}(h,g)^{w_{k}s_{k}(1-2R_{j}^{(k)})}$$

$$= \hat{e}(g,g)^{r_{j}(i-j) + \sum_{k=1}^{\ell_{1}} w_{k}(X^{(k)} \oplus R_{j}^{(k)})} \hat{e}(h,g)^{r_{j}(r+r'_{j}) + \sum_{k=1}^{\ell_{1}} w_{k}s_{k}(1-2R_{j}^{(k)})}$$

Otherwise, \mathcal{DB} aborts the protocol execution.

4. \mathcal{U} runs a PIR protocol to retrieve C_i from \mathcal{DB} , and sets f(i,X) = d if $C_i^{q_1} = \hat{e}(g^{q_1}, g)^d$.

As to the performance, the communication complexity is dominated by that of the PIR protocol and the transmission of c_k , $proof_k$ $(1 \le k \le \ell_1)$. For \mathcal{U} , the computational complexity is dominated by generating c_k , $proof_k$ $(1 \le k \le \ell_1)$: $O(\ell_1)$ exponentiations. For \mathcal{DB} , the computational complexity is dominated by checking the GOS NIZK proofs and the computation of C_j $(1 \le j \le N)$: $O(N + \ell_1)$

³ In practice, the validity of pk can be certified by a TTP, and the same pk can be used by the user for all his queries.

pairing computations and O(N) exponentiations. Moreover, it is straightforward to verify the following observation.

Observation 2. For every $1 \leq j \leq N$, given that $i \neq j$, the components of $C_j = (C_{j1}, C_{j2})$, where

$$C_{j1} = \hat{e}(g,g)^{r_j(i-j) + \sum_{k=1}^{\ell_1} w_k(X^{(k)} \oplus R_j^{(k)})}, C_{j2} = \hat{e}(h,g)^{r_j(r+r_j') + \sum_{k=1}^{\ell_1} w_k s_k(1-2R_j^{(k)})},$$

are uniformly and independently distributed over \mathbb{G}_1 and the subgroup of order q_1 of \mathbb{G}_1 , respectively. If i=j, then $C_{j1}=\hat{e}(g,g)^{\sum_{k=1}^{\ell_1} w_k(X^{(k)} \oplus R_j^{(k)})}$ and C_{j2} is uniformly distributed over the subgroup of order q_1 of \mathbb{G}_1 .

4.2 Security Analysis

It is straightforward to verify that if the PIR protocol is sound then the EPIR protocol is also sound. First, we have the following lemma whose proof will appear in the full version of this paper.

Lemma 3. Given any $M \geq 1$, the attacker's advantage in the following game is negligible for the BGN encryption scheme.

$$\begin{aligned} \mathbf{Exp}_{\mathcal{A}}^{P\text{-}IND\text{-}CPA} & \leftarrow \mathsf{Gen}(1^{\ell}) \\ ((m_{0,1}, \dots, m_{0,M}), (m_{1,1}, \dots, m_{1,M})) & \leftarrow \mathcal{A}_1(pk) \\ b & \leftarrow \{0, 1\} \\ \mathbf{c} & \leftarrow (\mathsf{Enc}(m_{b,1}, pk), \dots, \mathsf{Enc}(m_{b,M}, pk)) \\ b' & \leftarrow \mathcal{A}_2(\mathbf{c}) \end{aligned}$$

The following lemmas show that the EPIR protocol achieves user privacy and database privacy but their proofs will appear in the full version of this paper.

Lemma 4 (user privacy). If the PIR protocol achieves user privacy, the EPIR protocol for computing Hamming distance achieves user privacy based on the subgroup decision assumption.

Lemma 5 (database privacy). The EPIR protocol for computing Hamming distance achieves database privacy (unconditionally).

5 Authentication Schemes Using Biometrics

5.1 Preliminaries

In our security model, besides human users, we assume that a biometric-based (remote) authentication system consists of the following types of components:

- Authentication client C, which is responsible for extracting human user's biometric template using some biometric sensor and communicating with authentication server.
- Authentication server S, which is responsible for dealing with the human user's authentication requests by querying the database which stores user's biometric template.

- Centralized database \mathcal{DB} , which stores the relevant biometric information for authentication⁴.

Like most existing biometric-based systems (and many traditional cryptosystems), a biometric-based authentication scheme consists of two phases: an enrollment phase and a verification phase.

- 1. In the enrollment phase, user U_i registers his biometric template b_i at the database \mathcal{DB} and his identity information ID_i at the authentication server \mathcal{S} .
- 2. In the verification phase, user U_i issues an authentication request to the authentication server S through a client C. The authentication server S retrieves U_i 's biometric information from the database DB and makes a decision.

Human users and S trust C to be honest, and S trusts \mathcal{DB} to provide the correct biometric information. We further make the following assumptions on the system components: The communication links between any two components are authenticated and encrypted. In practice, the security links can be implemented using a standard protocol such as SSL or TLS. In addition, the following assumptions are indispensable for all biometrics-based systems.

- 1. Biometric Distribution assumption: Let H be the distance function in the Hamming space. We assume that, there is a threshold value λ , the probability that $H(b_i, b_j) > \lambda$ is close to 1^5 , where b_i is Alice's biometric template and b_j is Bob's biometric template, while the probability that $H(b_i, b'_i) \leq \lambda$ is close to 1, where b_i and b'_i are Alice's biometric templates in two measurements.
- Liveness assumption: We assume that, with a high probability, the biometric template captured by the sensor is from a live human user. In other words, it is difficult to produce a faked biometric template that can be accepted by the sensor.

For a biometric-based authentication scheme, two types of security properties are mainly concerned. One is the resistance to impersonation attacks, in which case we only consider outside adversaries by assuming that all the system components are honest. The other is preserving privacy properties, in which case we only consider malicious inside adversaries including a malicious \mathcal{S} and a malicious \mathcal{DB} . But we assume that \mathcal{S} and \mathcal{DB} will not collude. In practice, many methods (for example, issuing a smart-card to every user) can be used to guarantee these properties against other kinds of adversaries, but we omit them in this paper since our main aim is to demonstrate the application of the EPIR protocols.

 $^{^4}$ It is worth emphasizing that \mathcal{DB} and \mathcal{S} are two different principles and \mathcal{DB} may serve as a trusted storage for a number of authentication servers. This is different from the conventional environment where we say a server has its own database for storing the authentication secrets.

⁵ Note that this probability is related to the false accept and false reject rates of biometrics, but we omit a detailed discussion in this paper.

5.2 The First Biometric-Based Authentication Scheme

This biometric-based authentication scheme is constructed based on the EPIR protocol for equality as described in Section 3.1. In this scheme, due to the secure sketch scheme, the user does not need to store any private information and the client $\mathcal C$ does not need to store any user specific information. The enrollment phase works as follows.

- \mathcal{C} implements a (m, m', λ) -secure sketch (SS, Rec) (an example is described in Appendix C), where m' is the system security parameter.
- $-\mathcal{S}$ generates an ElGamal key pair (pk, sk).
- U_i generates his unique pseudorandom identifier ID_i and registers it at the server S, and registers (ID_i, R_i) at the database \mathcal{DB} , where b_i is U_i 's reference biometric template and

$$R_i = \operatorname{Enc}(g^{ID_i||b_i}, pk)$$
$$= (R_{i1}, R_{i2}).$$

In addition, U_i publicly stores a sketch $sketch_i = SS(b_i)$.

If U_i wants to authenticate himself to the server S through the authentication client C, then the procedure is as follows.

- 1. C extracts U_i 's biometric template b_i^* and computes the adjusted template $b_i' = \text{Rec}(b_i^*, sketch_i)$. Then C sends ID_i to S and sends X to \mathcal{DB} , where $X = \text{Enc}(g^{ID_i||b_i'}, pk)$. Otherwise, C aborts the operation.
- 2. After receiving X, \mathcal{DB} performs as in the EPIR protocol for testing equality as described in Section 3.1, where \mathcal{DB} computes C_j for every $1 \leq j \leq N$, where r_j, r'_j are randomly chosen from \mathbb{Z}_q and

$$C_i = (g^{r'_j}(g^r(R_{i1})^{-1})^{r_j}, y^{r'_j}(y^r g^{ID_i||X}(R_{i2})^{-1})^{r_j})$$

3. The server runs a PIR to retrieve C_i . If $Dec(C_i, sk) = 1$, S accepts the request; otherwise rejects it.

It is easy to verify that impersonation attacks are prevented based on the biometric distribution assumption, i.e. an adversary can not force \mathcal{C} to output U_j 's template by letting \mathcal{C} measure U_i 's biometric if U_i and U_j are different human users.

Every authentication is indeed an execution of the EPIR protocol for testing equality between S and DB, though X is sent to DB by a trusted C. From the user privacy property of the EPIR protocol, DB learns nothing about which user is authenticating himself and what is the authentication result. In addition, DB obtains nothing about the registered biometric templates because they are encrypted by S's public key. From the database privacy property of the EPIR protocol, S learns nothing about a user's biometric template. In fact, S only obtains the information whether the authentication request is made by the legitimate user or not.

5.3 The Second Biometric-Based Authentication Scheme

This biometric-based authentication scheme is constructed based on the EPIR protocol for computing Hamming distance as described in Section 4.1. In this scheme, the user does not need to store any private or public information and the client $\mathcal C$ does not need to store any user specific information. The server $\mathcal S$ is enabled to make its decision based on an exact matching between a user's biometric templates. The overall matching result can be more accurate by allocating a score (or a weight) for the matching result of every single bit. The enrollment phase works as follows.

- $-\mathcal{S}$ generates a BGN encryption key pair (pk, sk).
- U_i generates his pseudorandom identifier ID_i and registers it at the server \mathcal{S} , and registers $(ID_i, \alpha_i^{(k)} (1 \leq k \leq \ell_1))$ at the database \mathcal{DB} , where b_i is U_i 's reference biometric template with bit-length ℓ_1 , $\alpha_i^{(k)} = g^{b_i^{(k)}} h^{\beta_{ik}}$ $(1 \leq k \leq \ell_1)$, and β_{ik} $(1 \leq k \leq \ell_1)$ are randomly chosen from \mathbb{Z}_n .

If U_i wants to authenticate himself to the server S through the authentication client C, then the procedure is as follows.

- 1. C extracts U_i 's biometric template b_i' , and sends c and c_k $(1 \le k \le \ell_1)$ to \mathcal{DB} , where $c = g^{ID_i}h^r$, $c_k = g^{b_i'^{(k)}}h^{s_k}$ $(1 \le k \le \ell_1)$, r and s_k $(1 \le k \le \ell_1)$ are randomly chosen from \mathbb{Z}_n . Simultaneously, C sends ID_i to S.
- 2. After receiving c and c_k $(1 \le k \le \ell_1)$, \mathcal{DB} performs in a similar way as in the EPIR protocol for computing Hamming distance except that it computes C_j for every $1 \le j \le N$ as follows.
 - (a) For every $1 \leq k \leq \ell_1$, compute $m_{j,k}$ where

$$\begin{split} m_{j,k} &= \frac{\hat{e}(c_k \alpha_j^{(k)}, g)}{\hat{e}(c_k, \alpha_j^{(k)})^2} \\ &= \frac{\hat{e}(c_k g^{b_j^{(k)}} h^{\beta_{jk}}, g)}{\hat{e}(c_k, g^{b_j^{(k)}} h^{\beta_{jk}}, g)} \\ &= \frac{\hat{e}(g^{b_i^{(k)}} h^{\beta_{jk}}, g)}{\hat{e}(g^{b_i^{(k)}} h^{s_k + \beta_{jk}} g^{b_j^{(k)}}, g)} \\ &= \frac{\hat{e}(g^{b_i^{(k)}} h^{s_k + \beta_{jk}} g^{b_j^{(k)}}, g)}{\hat{e}(g^{b_i^{(k)}} h^{s_k}, g^{b_j^{(k)}} h^{\beta_{jk}})^2} \\ &= \frac{\hat{e}(g^{b_i^{(k)}} g^{b_j^{(k)}}, g) \hat{e}(h^{s_k + \beta_{jk}}, g)}{\hat{e}(g^{b_i^{(k)}}, g^{b_j^{(k)}})^2 \hat{e}(h, g)^{2(s_k b_j^{(k)} + b_i^{(k)} \beta_{jk} + s_k \beta_{jk} \log_g h)}} \\ &= \hat{e}(g, g)^{b_i^{(k)} + b_j^{(k)} - 2b_i^{(k)} b_j^{(k)}} \hat{e}(h, g)^{s_k (1 - 2\beta_{jk} \log_g h - 2b_j^{(k)}) + \beta_{jk} (1 - 2b_i^{(k)})} \\ &= \hat{e}(g, g)^{b_i^{(k)} \oplus R_j^{(k)}} \hat{e}(h, g)^{s_k (1 - 2\beta_{jk} \log_g h - 2b_j^{(k)}) + \beta_{jk} (1 - 2b_i^{(k)})} \end{split}$$

(b) Let $x_{jk} = s_k(1 - 2\beta_{jk}\log_g h - 2b_j^{(k)}) + \beta_{jk}(1 - 2b_i^{(k)})$ $(1 \le k \le \ell_1)$, compute C_j , where r_j, r_j' are randomly chosen from \mathbb{Z}_n and

$$C_{j} = \hat{e}(cg^{-ID_{j}}h^{r'_{j}},g)^{r_{j}} \prod_{k=1}^{\ell_{1}} (m_{j,k})^{w_{k}}$$

$$= \hat{e}(g^{ID_{i}-ID_{j}}h^{r+r'_{j}},g)^{r_{j}} \prod_{k=1}^{\ell_{1}} \hat{e}(g,g)^{w_{k}(b_{i}^{\prime(k)} \oplus b_{j}^{(k)})} \hat{e}(h,g)^{w_{k}x_{jk}}$$

$$= \hat{e}(g,g)^{r_{j}(ID_{i}-ID_{j}) + \sum_{k=1}^{\ell_{1}} w_{k}(b_{i}^{\prime(k)} \oplus b_{j}^{(k)})} \hat{e}(h,g)^{r_{j}(r+r'_{j}) + \sum_{k=1}^{\ell_{1}} w_{k}x_{jk}}$$

3. S runs a PIR to retrieve C_i , and computes d satisfying $C_i^{q_1} = \hat{e}(g^{q_1}, g)^d$. S accepts the request if d is smaller than a threshold value; otherwise rejects it.

We first emphasize that the GOS NIZK proofs are omitted in this authentication scheme because c and c_k $(1 \le k \le \ell_1)$ are sent by \mathcal{C} which is trusted by all parties.

It is easy to verify that impersonation attacks are prevented based on the biometric distribution assumption. Every authentication is indeed an execution of the EPIR protocol for computing Hamming distance between \mathcal{S} and \mathcal{DB} , though we have made some small modifications. As a result, this scheme achieves the same security properties as those of the previous scheme.

Compared with the previous scheme, this scheme is more convenient for human users and the the client \mathcal{C} , where a human user does not need to store any information and secure sketch is not needed to be implemented in \mathcal{C} . Another advantage of this protocol is that it works even when secure sketches are not practical (i.e. when noise is high).

6 Conclusion

In this paper we formulated the concept of EPIR and proposed two protocols: one for testing equality and the other for computing Hamming distance. The randomizations in both protocols are performed to avoid using a SPIR protocol in order to achieve the privacy for the database. In addition, the randomizations also guarantee that the privacy for the database is unconditionally achieved (without any computational assumption). It is a challenging task to design more efficient EPIR protocols, especially to reduce the computational complexity. In this paper, we also showed how to construct strong privacy-preserving biometric-based authentication schemes by employing these EPIR protocols. Some further work is required to evaluate the performance of these schemes in practice.

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Appendix A: Introduction to the ElGamal Encryption Scheme

The algorithms (Gen, Enc, Dec) of the ElGamal public key encryption scheme [18] are defined as follows:

- 1. The key generation algorithm Gen takes a security parameter 1^k as input and generates two primes p,q satisfying q|p-1. Let $\mathbb G$ be the subgroup of order q in $\mathbb Z_p^*$, g be a generator of $\mathbb G$. The private key x which is randomly chosen from $\mathbb Z_q$, and the public key is $y=g^x$. Let Ω be a bijective map from $\mathbb Z_q$ to $\mathbb G$.
- 2. The encryption algorithm Enc takes a message m and the public key y as input, and outputs the ciphertext $c = (c_1, c_2) = (g^r, y^r \Omega(m))$ where r is randomly chosen from \mathbb{Z}_q^* .

3. The decryption algorithm Dec takes a ciphertext $c = (c_1, c_2)$ and the private key x as input, and outputs the message $m = \Omega^{-1}((c_1^{-x}c_2))$.

It is well-known that the ElGamal scheme is semantically secure based on the DDH assumption.

Appendix B: Introduction to the BGN Scheme

The algorithms (Gen, Enc, Dec) of the BGN encryption scheme [3] are defined as follows:

- 1. The key generation algorithm Gen takes a security parameter 1^k as input and generates a tuple $(n, q_1, q_2, \mathbb{G}, \mathbb{G}_1, \hat{e}, g, u, h)$, where q_1 and q_2 are two primes, $n = q_1 q_2$, \mathbb{G} and \mathbb{G}_1 are two cyclic groups of order n, g and u are generators of \mathbb{G} , and $h = u^{q_2}$. The private key $sk = q_1$, and the public key is $pk = (n, \mathbb{G}, \mathbb{G}_1, \hat{e}, g, h)$.
- 2. The encryption algorithm Enc takes a message $m \in \mathbb{Z}_{q_2}$ and the public key pk as input, and outputs the ciphertext $c = g^m h^r$ where r is randomly chosen from \mathbb{Z}_n .
- 3. The decryption algorithm Dec takes a ciphertext c and the private key sk as input, and outputs the message $c^{q_1} = (g^{q_1})^m$. Then compute the discrete log of c^{q_1} base g^{q_1} .

It is proved by Boneh, Goh, and Nissim that this scheme is semantically secure given the subgroup decision problem is hard for $(n, \mathbb{G}, \mathbb{G}_1, \hat{e})$.

Appendix C: Introduction to Secure Sketches

Roughly speaking, a secure sketch scheme (SS, Rec) allows recovery of a hidden value from any value close to this hidden value. Informally, the algorithm SS take a value x as input and outputs some public value y, and the algorithm Rec takes a value x' and y as input and outputs a value x''. If x' and x are close enough, then x'' = x.

We take the Code-Offset Construction given in [15] as an example. let C be a [n, k, 2t+1] error-correction code over a field \mathbb{F} . With input $x \in \mathbb{F}^n$, y is computed as SS(x) = x - c, where c is a random codeword. With input (x', y), Rec computes x'' in the following way: compute c' = x' - y, decode c' to obtain c'', and set x'' = c'' + y.