The Semantics of Consistency and Trust in Peer Data Exchange Systems

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Abstract. We propose and investigate a semantics for peer data exchange systems (or peer data management systems) where different peers are pairwise related to each other by means of data exchange constraints and trust relationships. These two elements plus the data at the peers' sites and the local integrity constraints for a peer are made compatible via the proposed semantics by determining a set of solution instances, which are the intended virtual instances for the peer. The semantically correct answers from a peer to a query, called its peer consistent answers, are defined as those answers that are invariant under all its different solution instances. We show that solution instances can be specified as the models of logic programs with a stable model semantics.

1 Introduction

A peer data exchange system (PDES) consists of a finite set of peers $\{P_1, \dots P_n\}$, each of them with a local database instance. Peers may be pairwise related by means of logical sentences, called *data exchange constraints* (DECs), which are expressed in terms of the participating schemas and are expected to be satisfied by the combined data. Furthermore, a peer P may trust its data the same as or less than other peers' data, i.e. there may be trust relationships between pairs of peers. We may also have integrity constraints (ICs) that are local to each peer.

The DECs could be seen as ICs on a global database obtained by conceptually putting together all the peers' schemas and data. Most likely, these DECs will not be satisfied in this global database, but virtually enforcing their satisfaction at query time has the effect of shipping (sub)queries and data between peers. Actually, in such a PDES, a query $\mathcal Q$ is posed to a peer $\mathcal P$, who, in order to answer it, may need to consider both its own data and the data stored at other peers' sites that are related to $\mathcal P$ by DECs. Keeping $\mathcal P$'s DECs satisfied at query time may imply getting data from other peers to complement $\mathcal P$'s data, but also not using part of its own data.

The decision by a peer P on what other data to consider does not depend only on its DECs, but also on the *trust relationships* that P has with other peers. For example, if peer P trusts peer Q's data more than its own, P will accommodate its data to Q's in order to keep the DECs between them satisfied.

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In order for P to return meaningful answers, its local semantic constraints have to be taken into account. The consistency of its instance should be preserved when it is virtually updated due to the interaction with other peers. In consequence, still at query time, P may also need to "virtually repair" its data.

Our semantics makes all these elements compatible, by defining a set of virtual global instances called *solution instances* (or simply solutions) for a peer. In consequence, the "data" for a peer, the one in its solution instances, depends upon its instance, the local instances of the related peers, the satisfaction of the DECs, and the satisfaction by P of its local ICs. After that, having a precise definition of the intended solution instances for a peer P, the *peer consistent answers* (PCAs) from peer P to query $\mathcal Q$ are defined as those answers that can be retrieved from *every* possible solution for P.

The definition of solution for P may suggest that P may physically change other peers' data, but this is not the case. The notion of solution is used as an auxiliary notion to characterize the correct answers from P's point of view. Ideally, P should be able to obtain its peer consistent answers just by querying the already available local instances. This resembles the approach to *consistent query answering* (CQA) in databases, where consistent answers to a query posed to a database, which is possibly inconsistent wrt to a given set of ICs, are defined as those answers that can be retrieved from every minimally repaired version of the original instance. Methods have been developed for computing these answers without having to physically repair the given instance [1, 9, 10].

Our work goes in the direction of semantic approaches to peer-to-peer data exchange [27, 29, 28, 14, 21, 7, 15, 23]. In [7] trust relationships were introduced for the first time in this scenario and the notions of solution instance for a peer and of peer consistent answer to a query were introduced. The case of a peer and its immediate neighbors was considered and investigated. However, the situation where a peer is related by logical transitivity via DECs to other, non neighboring peers was not modelled. Actually, in [7] it was only indicated that giving a semantics to solution instances for a peer that consider the transitive relationships to other peers could be done by using logic programs with stable model semantics. We fully develop this idea here. First, we provide a general model-theoretic definition of solutions for a peer, including the transitive case, and next, we specify the solutions as the models of disjunctive logic programs with stable model semantics [24], aka. answer set programs [25, 3]. An extended version of this paper can be found in [8].

Logic programs can capture the different ways the system stabilizes after satisfying the DECs, the trust relationships, and the local ICs. Disjunctive programs allow for the specification of alternative virtual updates on data sources under certain conditions. We propose appropriate logic programs and then we establish that there is a one-to-one correspondence between the set of solution instances for a peer and the set of stable models of the program. Logic programs provide an expressive language for representing and specifying the alternative solutions for a peer, and become executable specifications for computing peer consistent

answers. This approach has been exploited in CQA, where database repairs are specified as stable models of a program [2, 26, 4, 17].

2 A Semantics for PDESs

We consider peers that have mutually disjoint relational schemas; but all of them share a possibly infinite database domain \mathcal{U} . Peers are denoted by A, B, P, Q, ...

Definition 1. A peer data exchange system \mathfrak{P} consists of: (a) A finite set \mathcal{P} of peers, with each peer P owning a relational database schema $\mathcal{R}(P)$, and a database instance D(P) conforming to schema $\mathcal{R}(P)$. The schemas determine FO languages, e.g. $\mathcal{L}(P)$, $\mathcal{L}(P,\mathbb{Q})$. (b) For each peer P, collections $\mathcal{L}(P,\mathbb{Q})$ of sentences of $\mathcal{L}(P,\mathbb{Q})$, which contain the DECs between P and a peer \mathbb{Q} . Here, $\mathcal{L}(P) := \bigcup_{\mathbb{Q}} \mathcal{L}(P,\mathbb{Q})$ and $\mathcal{L} := \bigcup_{\mathbb{P} \in \mathcal{P}} \mathcal{L}(P)$. (c) For each peer P, a set of $\mathcal{L}(P)$ -sentences IC(P) that are ICs on $\mathcal{R}(P)$. Here, $IC = \bigcup_{\mathbb{P} \in \mathcal{P}} IC(P)$. (d) A relation $trust \subseteq \mathcal{P} \times \{less, same\} \times \mathcal{P}$, with exactly one triple of the form $\langle P, \cdot, \mathbb{Q} \rangle$ for each non empty $\mathcal{L}(P,\mathbb{Q})$.

The intended semantics of $(A, less, B) \in trust$ is that peer A trusts itself less than B; while $(A, same, B) \in trust$ indicates that A trusts itself the same as B.

Definition 2. (a) A universal data exchange constraint (UDEC) between peers P1, P2 is a first-order (FO) formula of form:

$$\forall \bar{x}(\bigwedge_{i=1}^{n} R_{i}(\bar{x}_{i}) \longrightarrow (\bigvee_{j=1}^{m} Q_{j}(\bar{y}_{j}) \vee \varphi)); \tag{1}$$

where the R_i, Q_j are relations in $\mathcal{R}(P1) \cup \mathcal{R}(P2), \varphi$ is a formula containing built-in atoms¹ only, and $\bar{x}_i, \bar{y}_j \subseteq \bar{x}$. (b) A referential data exchange constraint (RDEC) between peers P1, P2 is an $\mathcal{L}(P1, P2)$ -sentence of the form:

$$\forall \bar{x}(R(\bar{x}) \longrightarrow \exists \bar{y} \ Q(\bar{x}', \bar{y})); \tag{2}$$

where
$$R, Q \in \mathcal{R}(P1) \cup \mathcal{R}(P2)$$
, and $\bar{x}' \subseteq \bar{x}$.

Notice that the sets of DECs $\Sigma(P1,P2)$ and $\Sigma(P2,P1)$ can be different. When exchanging or repairing data, the existential quantifier in RDECs will be interpreted as a null value. By having one database atom in the consequent, we avoid existential joins that, when filled with nulls, do not have a clear semantics (cf. [12] for a discussion and a FO semantics of nulls in SQL databases).²

Example 1. Consider a PDES $\mathfrak P$ with four peers and $\mathcal R(P1)=\{R^1(\cdot,\cdot)\}, \mathcal R(P2)=\{R^2(\cdot,\cdot),S^2(\cdot,\cdot)\}, \mathcal R(P3)=\{R^3(\cdot,\cdot)\}, \mathcal R(P4)=\{R^4(\cdot,\cdot,\cdot)\}, \text{ and DECs: } \mathcal E(P1,P2)=\{\forall xy(R^2(x,y)\to R^1(x,y))\}, \\ \mathcal E(P2,P3)=\{\forall xy(R^2(x,y)\wedge R^3(x,y)\to \mathbf{false})\}, \\ \mathcal E(P4,P2)=\{\forall xyz(R^2(x,y)\wedge S^2(y,z)\to R^4(x,y,z))\}, \\ \mathcal E(P4,P3)=\{\forall xy(R^3(x,y)\to \exists zR^4(x,y,z))\}.$

¹ For example, $x \neq 3$, y = z and z > 3.

² Our framework can be easily adapted to cases where, instead of *null*, one uses arbitrary elements of the database domain [13] or labelled nulls [30].

Here **false** in the second DEC is a built-in atom that is false in every instance, so the DEC specifies that relations R^2 and R^3 are disjoint. The DECs in $\Sigma(P1,P2)$, $\Sigma(P2,P3)$ and $\Sigma(P4,P2)$ are UDECs and the one in $\Sigma(P4,P3)$ is a RDEC. Finally, we could have $trust = \{(P1,less,P2), (P2,same,P3), (P4,less,P2), (P4,less,P3)\}$. Peer P1 trusts P2 more than itself, and it will import all the data from R^2 into its table R^1 . On the other hand, peer P2 trusts peer P3 as much as itself, and its DEC states that it is not possible to have the same tuple in both R^3 and R^2 . \square

Local ICs IC(P) are also of the form in Definition 2, but with all database predicates in $\mathcal{R}(P)$. So, we can identify IC(P) with $\Sigma(P,P)$. All the common ICs found in database practice can be accommodated into these syntactic classes. In particular, using the atom **false**, denial constraints are of the form (1). In Example 1, we could have $IC(P2) = \{\forall x \forall y (R^2(x,y) \land S^2(x,y) \rightarrow \mathbf{false})\}$.

Each peer P is responsible for maintaining its material instance consistent with respect to its ICs IC(P), independently from other peers; and we may assume that this is the case. However, our semantics works the same if we allow peers with locally inconsistent data. According to our semantics presented below, unsatisfied local ICs are considered when solution instances are specified, which is done by using a repair semantics and techniques developed for CQA [10, 6].

When a peer P is posed a query, it may have to submit queries to other peers according to its DECs, using data in other peers' relations appearing in them. Data brought from other peers will possibly cause virtual updates on P's data, which may create virtual violations of P's local ICs, which has to be considered.

From the perspective of a peer P, its own database may be inconsistent with respect to the data owned by another peer Q it trusts more or the same, and the DECs in $\Sigma(P,Q)$. When P queries its own database, the answers from P should be consistent with $\Sigma(P,Q)$ and its own ICs IC(P). In principle, P, which is not allowed to change other peers' data, could try to physically repair its database in order to satisfy $\Sigma(P) \cup IC(P)$. This is not a realistic approach. Rather, P should solve its semantic conflicts at query time. This leads to a set of virtual instances, the minimal repairs of P's local database, where P's DECs and ICs are satisfied, while respecting P's trust relationships to other peers. The answers returned by P to the user are those that are true of all these instances.

The solution instances of a peer will be determined not only by its relationships with its neighbors, but also by the neighbors of its neighbors, etc.

Definition 3. (a) The accessibility graph $\mathcal{G}(\mathfrak{P})$ of a PDES \mathfrak{P} contains a vertex for each peer $P \in \mathcal{P}$ and a directed edge from Pi to Pj if $\Sigma(Pi,Pj)$ is non empty. An edge from Pi to Pj is labelled with "<" when $(Pi,less,Pj) \in trust$, and with "=" when $(Pi,same,Pj) \in trust$.³ (b) Peer P' is accessible from P if there is a path in $\mathcal{G}(\mathfrak{P})$ from P to P' or if P'=P. Peer P' is a neighbor of P if there is an edge from P to P' in $\mathcal{G}(\mathfrak{P})$, or if P' = P. With $\mathcal{AC}(P)$ and $\mathcal{N}(P)$ we denote the sets of peers that are accessible from P and the neighbors of P, respectively. For $P \in \mathcal{P}$, $\mathcal{G}(P)$ is the restriction of $\mathcal{G}(\mathfrak{P})$ to $\mathcal{AC}(P)$.

³ In case a peer P trusts itself more than another peer, the information of the latter is irrelevant to P.

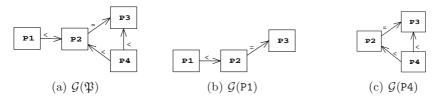


Fig. 1. Graphs for Example 2

Example 2. (Example 1 continued) In this system,
$$\mathcal{AC}(P1) = \{P1, P2, P3\}$$
, $\mathcal{AC}(P2) = \{P2, P3\}$, $\mathcal{AC}(P3) = \{P3\}$, $\mathcal{AC}(P4) = \{P2, P3, P4\}$, $\mathcal{N}(P1) = \{P1, P2\}$, $\mathcal{N}(P2) = \{P2, P3\}$, $\mathcal{N}(P3) = \{P3\}$, and $\mathcal{N}(P4) = \{P2, P3, P4\}$.

The data distributed across different peers has to be appropriately gathered to build solution instances for a peer, and different semantics may emerge as candidates, depending on the granularity of the data sent between peers. We develop one of them,⁴ according to which, the data that a peer P receives from a neighbor Q to build its own solutions is the *intersection of the solutions* for Q. After P collects this data, only P's DECs and ICs are considered. This is a recursive definition since the solutions for the neighbors have to be determined, under the same semantics. Base cases of the recursion are peers with no relevant DECs. In consequence, this semantics requires an acyclic accessibility graph.

In [27] problematic cases involving cyclic dependencies through DECs are identified, which implicitly involve a cyclic accessibility graph. For example, we may have a PDES \mathfrak{P} with $\mathcal{P} = \{P1, P2, P3\}$, with relations $R^1(\cdot), R^2(\cdot), R^3(\cdot)$, resp., and DECs $\mathcal{L}(P1) = \{\forall x(R^2(x) \to R^1(x))\}$, $\mathcal{L}(P2) = \{\forall x(R^3(x) \to R^2(x))\}$, $\mathcal{L}(P3) = \{\forall x(R^1(x) \to R^3(x))\}$, each of them satisfied only by importing data into the peer who owns the DEC. The implicit trust relation $\{(P1, less, P2), (P2, less, P3), (P3, less, P1)\}$ makes $\mathcal{L}(\mathfrak{P})$ cyclic. In [27] it is assumed that no cycles of this kind appear. In the following, we will also assume that $\mathcal{L}(\mathfrak{P})$ is acyclic, and then for each particular peer P, $\mathcal{L}(P)$ is acyclic.

Null values will be used to satisfy referential DECs and local referential ICs; and the repair semantics based on introduction of null values, presented and developed in [12, 11] for single relational databases and RICs, can be adapted here, but now taking into account the trust relationships. Data sources at the peers' sites may contain null values that, as those used to satisfy referential constraints, will have a semantics that corresponds to the way nulls are handled by DBMSs that follow the SQL standard. In particular, there is only one constant, null, that is used as the null value.⁵ We use a semantics for IC satisfaction in the presence of nulls that generalizes the one implemented in DBMSs, and coincides with the first-order notion of formula satisfaction in databases without nulls [11].

⁴ In [11] also two other alternative semantics are fully developed and compared, in particular establishing some conditions under which they coincide or differ. The other semantics assume that more detailed information, such as mappings and trust relationships, can be sent between peers.

⁵ This null is obviously different from the multiple labelled null values that are considered in data exchange for satisfying existential quantifiers (cf. [30] for a survey).

A formal development of the notion of constraint satisfaction, denoted $D \models \psi$, with D possibly containing null and ψ a constraint, can be found in [12, 11] (cf. [8, appendix B] for a review). What matters most for the rest of this paper is that the satisfaction of a constraint ψ depends upon the presence of null in attributes of database relations which are also relevant attributes for ψ .

Solutions for a peer should stay close to its original physical instance while satisfying the DECs and local ICs. We do not want to import or give up more data than strictly required to satisfy the constraints. To formalize this idea, we first need to compare tuples that may contain null. A constant c provides less or equal information than a constant d, denoted $c \sqsubseteq d$, iff c is null or c = d [31]. A tuple $\bar{t}_1 = (c_1, \ldots, c_n)$ provides less or equal information than $\bar{t}_2 = (d_1, \ldots, d_n)$, denoted $\bar{t}_1 \sqsubseteq \bar{t}_2$, iff $c_i \sqsubseteq d_i$ for every $i = 1, \ldots, n$. Finally, $\bar{t}_1 \sqsubseteq \bar{t}_2$ means $\bar{t}_1 \sqsubseteq \bar{t}_2$ and $\bar{t}_1 \neq \bar{t}_2$. In the following, a database instance is identified with a finite set of ground database atoms; and $\Delta(\cdot, \cdot)$ denotes the symmetric difference of sets.

Definition 4. Let D, D', D'' be database instances for the same schema. It holds that $D' \leq_D D''$ iff for every $P(\bar{a}) \in \Delta(D, D')$, there exists $P(\bar{a}')$, such that: (a) $P(\bar{a}') \in \Delta(D, D'')$; (b) $\bar{a} \sqsubseteq \bar{a}'$; and (c) if $\bar{a} \sqsubseteq \bar{a}'$, then $P(\bar{a}') \not\in \Delta(D, D')$. Finally, $D'' <_D D'$ means $D'' \leq_D D'$ but not $D' \leq_D D''$.

If $D' \leq_D D''$, we say that D' is closer to D than D''. Condition (c) in Def. 4 ensures that a database that adds to D a tuple with null is closer to D than other that adds other constant. This condition will later ensure that the satisfaction of RDECs is enforced by using null.

For an instance D of a schema S, and S' a subschema of S, D|S' denotes the restriction of D to S'. Thus, if R is a predicate in S and D is an instance for S, $D|\{R\}$ denotes the extension of R in D. If $R(P) \subseteq S$, D|P is the restriction of D to R(P). A neighborhood solution for P and a database for its whole neighborhood is a closest database that satisfies P's DECs, ICs, and trust relationships.

Definition 5. Given a peer P in a PDES \mathfrak{P} and instances D, D' on schema $\bigcup_{\mathbb{Q} \in \mathcal{N}(\mathbb{P})} \mathcal{R}(\mathbb{Q}), \ D'$ is a neighborhood solution for P and D if: (a) $D' \models \bigcup_{\mathbb{Q} \in \mathcal{N}(\mathbb{P})} \mathcal{L}(\mathbb{P}, \mathbb{Q}) \cup IC(\mathbb{P}).$ (b) $D' | \{R\} = D | \{R\}$ for every predicate $R \in \mathcal{R}(\mathbb{Q})$ with $(\mathbb{P}, less, \mathbb{Q}) \in trust.$ (c) There is no instance D'' that satisfies (a) and (b), and such that $D'' <_D D'.$

We do not require in (a) $IC(\mathbb{Q})$ to be satisfied, because \mathbb{Q} will move data to P's site, where inconsistencies will be solved locally, according to Definition 6, where S(P) denotes the set of solutions for peer P.

Definition 6. Given a peer P in a PDES \mathfrak{P} with local instance D(P), an instance D over $\mathcal{R}(P)$ is a solution instance for P if: (a) D = D(P) and $\Sigma(P) = \emptyset$; or (b) $\Sigma(P) \neq \emptyset$, $D = \overline{D}|P$ where \overline{D} is a neighborhood solution for P and the database instance $D(P) \cup \bigcup_{\mathbb{Q} \in (\mathcal{N}(P) \setminus \{P\})} \bigcap_{I \in S(\mathbb{Q})} I$ over schema $\bigcup_{\mathbb{Q} \in \mathcal{N}(P)} \mathcal{R}(\mathbb{Q})$.

Intuitively, before constructing P's solutions, P has its local instance D(P) and each of its neighbors has as local instance the intersection of its own solutions. This produces a combined database. After that, the solutions for P are obtained by restricting to P the neighborhood solutions for the combined instance. The

neighborhood solution captures the minimal virtual updates that are necessary to satisfy the DECS and local ICs. As there may be several neighborhood solutions, several solutions for a peer are possible.

Example 3. (Example 1 and 2 continued) Consider the following instances of peers P1, P2 and P3 : $D(P1) = \{R^1(a,2)\}$, $D(P2) = \{R^2(c,4), R^2(d,5)\}$, $D(P3) = \{R^3(c,4)\}$ and $D(P4) = \{R^4(d,5,1)\}$. If we want the solutions for P1, the solutions for P2 are needed, who will need in turn the solutions for P1. Since P3 has no DECs with other peers, its only neighborhood solution is it local instance D(P3). This data is sent back to P2, who needs to repair $\{R^2(c,4), R^2(d,5), R^3(c,4)\}$ now wrt $\Sigma(P2,P3)$. As P2 trusts P3 the same as itself, it can modify its own data or the data it got from P3. There are two neighborhood solutions for P2: $\{R^2(c,4), R^2(d,5)\}$ and $\{R^2(d,5), R^3(c,4)\}$, that lead to two solutions for P2: $\{R^2(c,4), R^2(d,5)\}$ and $\{R^2(d,5)\}$. Peer P2 will send to P1 the intersection of its solutions: $\{R^2(d,5)\}$. Now, P1 has to repair $\{R^1(a,2), R^2(d,5)\}$ wrt $\Sigma(P1,P2) = \{\forall xy \ (R^2(x,y) \to R^1(x,y))\}$. Since P1 trusts its own data less than the data of P2, it will solve inconsistencies by modifying its own data. There is only one neighborhood solution, $\{R^1(a,2), R^2(d,5)\}$, and the solution for P1 is $\{R^1(a,2), R^1(d,5)\}$.

To compute the solutions for P4, the solutions of P2 and P3 are computed as shown before. Neighborhood solutions for P4 are obtained by repairing $\{R^4(d,5,1),R^2(d,5),R^3(c,4)\}$ wrt $\Sigma(P4,P2)$, and $\Sigma(P4,P3)$. The DECs in $\Sigma(P4,P2)$ are already satisfied, but not the ones in $\Sigma(P4,P3)$. Since P4 trusts the data in P3 more, a repair is obtained by adding a tuple with null into P4. The unique neighborhood solution for P4 is $\{R^4(d,5,1),R^2(d,5),R^3(c,4),R^4(c,4,null)\}$. Consequently, $S(P4) = \{\{R^4(d,5,1),R^4(c,4,null)\}\}$.

The peer consistent answers are the semantically correct answers to a query returned by a peer who consistently considers the data of- and trust relationships with its neighbors.

Definition 7. Given a FO query $\mathcal{Q}(\bar{x}) \in \mathcal{L}(P)$ posed to P, a ground tuple \bar{t} is a *peer consistent* answer (PCA) to \mathcal{Q} from P iff $D \models \mathcal{Q}(\bar{t})$ for every solution instance D for P.

Example 4. (Example 3 continued) If P2 is posed the query $Q: R^2(x, y)$, from its first solution instance we get $\{(c, 4), (d, 5)\}$, and from the second, $\{(d, 5)\}$.

Even in the absence of cycles in $\mathcal{G}(\mathfrak{P})$, there may be no solutions for a peer. Furthermore, still with acyclic $\mathcal{G}(\mathfrak{P})$, the decision problem of peer consistent answering, i.e. deciding if a tuple is a PCA to a query, may be undecidable if consistency wrt RDECs is achieved using arbitrary values in the domain.⁶ However, using null instead avoids this problem, making the problem decidable. Actually, by reduction from CQA to PCA and known results on the data complexity of CQA [12], we obtain

Theorem 1. The problem of peer consistent answering is Π_2^P -complete. \Box

⁶ The undecidability result for CQA in [13] can be reconstructed in our framework, because even with $\mathcal{G}(\mathfrak{P})$ acyclic, DECs can have ref-cycles (cf. Example 5).

3 Answer Set Programs and the Solutions for a Peer

In order to define the solutions for a peer P, we have to consider P's relevant peers, which are those in $\mathcal{AC}(P)$. The presence of cycles, through trust relationships or constraints (DECs or ICs), have an impact on the semantics. The former cycles appear in a cyclic $\mathcal{G}(P)$. The latter appear when the DECs and local ICs of peers in $\mathcal{AC}(P)$ put together present cycles through the implications that involve an RDEC or a local referential IC (a RIC). Sets of local ICs of this kind are called RIC-cyclic in [12]. For example, $IC = \{\forall x(S(x) \to Q(x)), \forall x (Q(x) \to S(x)), \forall x(Q(x) \to \exists y \ T(x,y))\}$ is not RIC-cyclic, whereas $IC' = IC \cup \{\forall xy \ (T(x,y) \to Q(y))\}$ is, because there is a cycle involving the RIC $\forall x(Q(x) \to \exists y \ T(x,y))$. RIC-cyclicity at the level of local ICs may lead to more solutions than intended when capturing the repair semantics by means of logic programs [12].

In order to deal with the new issues arising in PDESs, we will assume that, for each peer P, IC(P) is RIC-acyclic (cf. Section 4 for a discussion). Cycles through DECs and ICs will be crucial for a logic programming-based specification of solutions for a peer. We will say that the PDES \mathfrak{P} is ref-acyclic when in $\Sigma \cup IC$ there are no cycles that involve an RDEC or a RIC.

As Example 5 below shows, even assuming the acyclicity of $\mathcal{G}(\mathfrak{P})$, and RIC-acyclicity at the level of local ICs (or no local ICs at all), we may have ref-cycles in the set of all DECs. This is due to the generality of DECs, where we can have relations of any of the two peers on both sides of the implication.

Example 5. Peers P1, P2 have relations R^1, R^2 , resp. $\Sigma(P1) = \{ \forall xz (R^1(x, z) \rightarrow \exists y R^2(x, y)), \forall xz (R^2(x, z) \rightarrow \exists y R^1(x, y)) \}, \ \Sigma(P2) = \emptyset; \ \text{and} \ (P1, less, P2) \in trust.$ Here, $\mathcal{AC}(\mathfrak{P})$ is acyclic, but $\Sigma(P1) \cup \Sigma(P2)$ has a ref-cycle.

Now we will show how to specify solutions for a peer, given instances for the other peers, as the stable models of disjunctive logic programs. These programs use annotation constants to indicate the atoms that may become true or false (virtually inserted or deleted) in order to satisfy the DECs and local ICs. For each database predicate P we generate a new copy P with an extra argument to accommodate the annotation. In P- $(\bar{a}, \mathbf{t_a})$, annotation $\mathbf{t_a}$ means that the atom is advised to be made true; and $\mathbf{f_a}$, that the atom should be made false. For each DEC and local IC ψ , a rule captures through its disjunctive head the alternative virtual updates that can be performed to satisfy ψ (cf. rules 2. and 3. in Definition 9 for DECs, and 4. and 5. for local ICs).

Annotation \mathbf{t}^* indicates that the atom is true or becomes true in the program. It is introduced in order to execute a sequence of virtual updates that is needed due to interacting DECs and ICs. Finally, atoms annotated with \mathbf{t}^{**} are those that become true in a solution. They are the relevant atoms, and are used to read off the database atoms in the solutions (rules 8. below).

The relevant attributes of a constraint are those where the occurrence of *null* is relevant for its satisfaction [12], and then, they receive a special treatment in the logic programs. For the DEC in $\Sigma(P4,P3)$ in Example 1, the two attributes of R^3 and the first two of R^4 are relevant, but not the third attribute of R^4 .

Definition 8. For a constraint $\psi \in \mathcal{L}(\mathcal{R})$ and a variable or a domain constant $t, pos^{R}(\psi, t)$ is the set of positions in predicate $R \in \mathcal{R}$ where t appears in ψ . The set of relevant variables for ψ is $\mathcal{V}(\psi) = \{x \mid x \text{ is a repeated variable in } \psi\}$. The set of relevant attributes for ψ is $\mathcal{A}(\psi) = \{R[i] \mid x \in \mathcal{V}(\psi) \text{ and } i \in pos^R(\psi, x)\} \cup \{R[i] \mid x \in \mathcal{V}(\psi) \text{ and } i \in pos^R(\psi, x)\}$ $\{R[i] \mid c \text{ is a constant in } \psi \text{ and } i \in pos^{R}(\psi,c)\}, \text{ where } R[i] \text{ denotes the attribute}$ in position i in R.

Definition 9. Consider a PDES \mathfrak{P} , a peer $P \in \mathcal{P}$ with $\mathcal{N}(P) = \{P, P1, \dots, Pn\}$, and $\mathcal{I} = \{I_1, \dots, I_n\}$, where I_j is a database instance over the schema of Pj. The solution program $\Pi(\mathfrak{P}, P, \mathcal{I})$ for P contains:

- 1. dom(a), for every $a \in (\mathcal{U} \setminus \{null\})$. $R(\bar{a})$, for each atom $R(\bar{a}) \in D(P)$. $R(\bar{a})$, for each $R(\bar{a}) \in I$ with $I \in \mathcal{I}$.
- 2. For every UDEC $\psi \in \Sigma(P, P_j)$ of the form (1) with $P_j \in \mathcal{N}(P)$ and $(P, \{same \})$ or less, Pj) $\in trust$, the rule:

$$\bigvee_{R \in R_{\mathbb{P}}} R(\bar{x}_{i}, \mathbf{f_{a}}) \vee \bigvee_{Q \in Q_{\mathbb{P}}} Q_{\cdot}(\bar{y}_{j}, \mathbf{t_{a}}) \leftarrow \bigwedge_{i=1}^{n} R_{i\cdot}(\bar{x}_{i}, \mathbf{t}^{\star}), \bigwedge_{j=1}^{m} Q_{j\cdot}(\bar{y}_{j}, \mathbf{f}^{\star}), \bigwedge_{x_{l} \neq null, \bar{\varphi}, \mathbf{t}^{\star}} q_{i\cdot}(\bar{y}_{j}, \mathbf{f}^{\star}), \bigvee_{x_{l} \in \mathcal{A}(\psi)} q_{i\cdot}(\bar{y}_{j}, \mathbf{f}$$

- 3. For every RDEC $\psi \in \Sigma(P,Pj)$ of the form (2) such that $Pj \in \mathcal{N}(P)$ and $(P, \{same \text{ or } less\}, Pj) \in trust:$
 - (a) If $(P, same, Pj) \in trust$, the rule: $R(\bar{x}, \mathbf{f_a}) \vee Q(\bar{x}', \overline{null}, \mathbf{t_a}) \leftarrow R(\bar{x}, \mathbf{t^*}), \text{ not } aux_{\psi}(\bar{x}'), \bar{x}' \neq null.$
 - (b) If $(P, less, Pj) \in trust$ and $R \in \mathcal{R}(P)$, the rule: $R_{-}(\bar{x}, \mathbf{f_a}) \leftarrow R_{-}(\bar{x}, \mathbf{t^*}), \ not \ aux_{\psi}(\bar{x}'), \ \bar{x}' \neq null.$
 - (c) If $(P, less, Pj) \in trust$ and $Q \in \mathcal{R}(P)$, the rule: $Q_{\underline{\cdot}}(\bar{x}', null, \mathbf{t_a}) \leftarrow R_{\underline{\cdot}}(\bar{x}, \mathbf{t^*}), \ not \ aux_{\psi}(\bar{x}'), \ \bar{x}' \neq null.$

Plus the auxiliary rules:

$$aux_{\psi}(\bar{x}') \leftarrow Q(\bar{x}', \overline{null}), \text{ not } Q(\bar{x}', \overline{null}, \mathbf{f_a}), \bar{x}' \neq null.$$

For every $y_i \in \bar{y}$:

$$aux_{\psi}(\bar{x}') \leftarrow Q(\bar{x}', \bar{y}, \mathbf{t}^*), \text{ not } Q(\bar{x}', \bar{y}, \mathbf{f_a}), \bar{x}' \neq null, y_i \neq null.$$

4. For every UIC
$$\psi \in IC(P)$$
 of the form (1), the rule:

$$\bigvee_{i=1}^{n} P_{i-}(\bar{x}_{i}, \mathbf{f_{a}}) \vee \bigvee_{j=1}^{m} Q_{j-}(\bar{y}_{j}, \mathbf{t_{a}}) \leftarrow \bigwedge_{i=1}^{n} P_{i-}(\bar{x}_{i}, \mathbf{t^{*}}), \bigwedge_{j=1}^{m} Q_{j-}(\bar{y}_{j}, \mathbf{f^{*}}), \bigwedge_{x_{l} \in \mathcal{A}(\psi)} x_{l} \neq null, \ \bar{\varphi}.$$

5. For every RIC $\psi \in IC(P)$ of the form (2), the rules: $P_{-}(\bar{x}, \mathbf{f_a}) \vee Q_{-}(\bar{x}', null, \mathbf{t_a}) \leftarrow P_{-}(\bar{x}, \mathbf{t^*}), \ not \ aux_{\psi}(\bar{x}'), \ \bar{x}' \neq null.$ $aux_{\psi}(\bar{x}') \leftarrow Q(\bar{x}', \overline{null}), not Q(\bar{x}', \overline{null}, \mathbf{f_a}), \bar{x}' \neq null.$ For every $y_i \in \bar{y}$:

$$aux_{\psi}(\bar{x}') \leftarrow Q_{\bar{x}}(\bar{x}', \bar{y}, \mathbf{t}^*), \quad not \ Q_{\bar{x}}(\bar{x}', \bar{y}, \mathbf{f_a}), \ \bar{x}' \neq null, \ y_i \neq null.$$

6. For each predicate $R \in \mathcal{R}(\mathcal{N}(P))$, the annotation rules:

$$R_{\cdot}(\bar{x}, \mathbf{f}^{\star}) \leftarrow dom(\bar{x}), \ not \ R(\bar{x}).$$
 $R_{\cdot}(\bar{x}, \mathbf{f}^{\star}) \leftarrow R_{\cdot}(\bar{x}, \mathbf{f_a}).$ $R_{\cdot}(\bar{x}, \mathbf{t}^{\star}) \leftarrow R_{\cdot}(\bar{x}, \mathbf{f_a}).$

7. For each predicate $R \in \mathcal{R}(\mathcal{N}(P))$, the program constraint: $\leftarrow R_{-}(\bar{x}, \mathbf{t_a}), R_{-}(\bar{x}, \mathbf{f_a}).$

8. For each predicate $R \in \mathcal{R}(P)$, the interpretation rule: $R(\bar{x}, \mathbf{t}^{**}) \leftarrow R(\bar{x}, \mathbf{t}^{*})$, not $R(\bar{x}, \mathbf{f_a})$.

In bodies of rules associated to DECs or ICs ψ , the conditions of the form $x \neq null$, with x a variable appearing in a relevant attribute of ψ are used to capture the semantics of null values as used in SQL (cf. [12] for details). An atom of the form $P(\bar{x}, \overline{null}, ...)$ in the program represents an atom with possibly several occurrences of null, not necessarily in its last arguments, e.g. P(x, null, y, null, ...). For $\bar{x} = x_1, ..., x_n$, $\bar{x} \neq null$ abbreviates $x_1 \neq null, ..., x_n \neq null$. The program constraints in 7. discard models where an atom is both inserted and deleted.

The facts of the program are those in instance D(P) of P and those in instances I(Pi) for P's neighbors Pi. The instances I(Pi) used in the program may not coincide with the physical instances D(Pi). Actually, as shown below, if each I(Pi) is the intersection of the solutions of Pi, then the stable models of the program are in one-to-one correspondence with the solutions of peer P.

Since virtual updates are executed on the peers' instances, their local ICs have to be kept satisfied. That is the role of rules 4. (for universal ICs) and 5. (for referential ICs) above. We adopt the stable model semantics for the solution programs [24], i.e. their intended models are their stable models.

Example 6. (Example 1 continued) Consider $D(\mathtt{P1}) = \{R^1(a,2)\}$, and the instance $I_2 = \{R^2(d,5)\}$ for P2, the neighbor of P1. The solution program $\Pi(\mathfrak{P},\mathtt{P1},\{I_2\})$ contains: dom(a). dom(c). . . . $R^1(a,2)$. $R^2(d,5)$. $R^1(x,y,\mathbf{t_a}) \leftarrow R^2(x,y,\mathbf{t^*})$, $R^1(x,y,\mathbf{f^*})$, $x \neq null, y \neq null$. $R^1(x,y,\mathbf{t^*}) \leftarrow R^1(x,y,\mathbf{t_a})$. $R^1(x,y,\mathbf{t^*}) \leftarrow R^1(x,y)$. $R^1(x,y,\mathbf{f^*}) \leftarrow R^1(x,y,\mathbf{f^*})$. $R^1(x,y,\mathbf{f^*}) \leftarrow dom(x), dom(y), \ not \ R^1(x,y)$. $C(x,y,\mathbf{f^*}) \leftarrow R^1(x,y,\mathbf{f^*})$. With similar rules to the 2nd-6th for $R^1(x,y,\mathbf{f^*})$. The first rule makes sure that an $R^1(x,y,\mathbf{f^*})$ trusts P2 more than itself, virtual changes affect only peer P1.

Example 7. Consider a PDES \mathfrak{P} with $\mathcal{R}(P1) = \{R^1(\cdot, \cdot)\}$, $D(P1) = \{R^1(s, t), R^1(a, null)\}$, $\mathcal{R}(P2) = \{R^2(\cdot, \cdot)\}$, $D(P2) = \{R^2(c, d), R^2(a, e)\}$, $\Sigma(P1, P2) = \{\forall xy \ (R^2(x, y) \to \exists z \ R^1(x, z))\}$, $IC(P1) = \{\forall xyz \ (R^1(x, y) \land R^1(x, z) \to y = z)\}$, $\Sigma(P2, P1) = IC(P2) = \emptyset$, and $trust = \{(P1, less, P2)\}$. The program $\Pi(\mathfrak{P}, P1, \{I_2\})$ for P1 needs an instance for P2 that may be different from D(P2), but in this case we choose $I_2 = D(P2)$, obtaining the following program (omitting rules 6., 7.): dom(a). dom(b). ... $R^1(a, null)$. $R^1(s, t)$. $R^2(c, d)$. $R^2(a, e)$.

$$\begin{split} R^1_{-}(x,null,\mathbf{t_a}) \leftarrow R^2_{-}(x,\mathbf{t^{\star}}), \ not \ aux(x), x \neq null. \\ aux(x) \leftarrow R^1(x,null), \ not \ R^1_{-}(x,null,\mathbf{f_a}). \\ aux(x) \leftarrow R^1(x,y,\mathbf{t^{\star}}), \ not \ R^1_{-}(x,y,\mathbf{f_a}), x \neq null, y \neq null. \\ R^1(x,y,\mathbf{f_a}) \vee R^1(x,z,\mathbf{f_a}) \leftarrow R^1(x,y,\mathbf{t^{\star}}), R^1(x,z,\mathbf{t^{\star}}), \ x \neq null, \ y \neq z. \\ R^1_{-}(x,y,\mathbf{t^{\star \star}}) \leftarrow R^1_{-}(x,y,\mathbf{t^{\star}}), \ not \ R^1_{-}(x,y,\mathbf{f_a}). \end{split}$$

The first rule has the role of satisfying the RDEC by introducing a null into R^1 . The fourth rule takes care of the local functional dependency.

The atoms annotated with \mathbf{t}^{**} in a stable model of P's program have predicates of P only. They define a database instance for P. In Example 7, only R^1_{-} -atoms become annotated with \mathbf{t}^{**} . The program has only one stable model, with associated instance $\{R^1(a, null), R^1(s, t), R^1(c, null)\}$.

Definition 10. The database instance for peer P associated to a stable model \mathcal{M} of program $\Pi(\mathfrak{P}, P, \mathcal{I})$ is $D_{\mathcal{M}} = \{R(\bar{a}) \mid R(\bar{a}, \mathbf{t}^{\star\star}) \in \mathcal{M}\}.$

Theorem 2. Given a PDES \mathfrak{P} , $P \in \mathcal{P}$, $\mathcal{N}(P) = \{P, P1, \dots, Pn\}$, $n \geq 0$, D(P) an instance for P, and $\mathcal{I}^* = \{I_1, \dots, I_n\}$ instances for P1, ..., Pn, resp. If $\mathcal{L} \cup IC$ is ref-acyclic and each of the I_i is the intersection of the solution instances for peer Pi, then the instances of the form $D_{\mathcal{M}}$, where \mathcal{M} is a stable model of $\Pi(\mathfrak{P}, P, \mathcal{I}^*)$, are the all and only solution instances for P.

In Example 7, given that D(P2) is already the only solution instance for P2 (P2 has neither DECs nor local ICs) and $\Sigma(P1,P2)$ is ref-acyclic, the only solution instance for P is $D = \{R^1(s,t), R^1(a,null), R^1(c,null)\}$. However, if there are ref-cycles, the stable models may correspond to a strict superset of the solutions for a peer. In this case, post-processing that deletes models corresponding to non-minimal "solutions" is necessary.

Under the assumption that we have already computed the (intersection of the) solution instances for the neighbors of P, the program for P allows us to compute its solution instances. This generates a recursive process that can be applied because $\mathcal{G}(P)$ is acyclic. The terminal peers Pt, i.e. those with no outgoing edges in $\mathcal{G}(P)$, will become the base cases for the recursion. If a peer P' has Pt as one of its neighbors, the instance I_t to be used for Pt in the program for P' is simply D(Pt), Pt's original local instance.

Theorem 2 still holds if peer P, instead of collecting the intersection I_i of the solutions of a neighbor Pi, uses the intersection of the solutions for Pi restricted to the subschema of Pi that contains Pi's relations that appear in $\Sigma(P, Pi)$, which are those P needs to run its program.

With a solution program for P, PCAs for a query \mathcal{Q} posed to P can be obtained by running under the stable model semantics a query program $\Pi(\mathcal{Q})$ that represents the query in combination with $\Pi(\mathfrak{P}, P, \mathcal{I}^*)$.

Example 8. (Example 6 continued) In order to obtain the PCAs to the query $Q_1: R^1(x,y)$, asking for the tuples in R^1 , the rule $ans_1(x,y) \leftarrow R^1(x,y,\mathbf{t}^{\star\star})$ has to be added to $\Pi(\mathfrak{P},\mathsf{P1},\{I_2\})$ (assuming that I_2 is the intersection of the solution instances for P2). The ground ans_1 -atoms in the intersection of all stable models correspond to the PCAs. For the query $Q_2: \exists y R^1(x,y)$, the projection of R^1 on its first attribute, the query rule is $ans_2(x) \leftarrow R^1(x,y,\mathbf{t}^{\star\star})$.

Our semantics could be naively implemented as follows. When P is posed a query, P has to run its program, for which it needs as facts those in the intersections of the solutions of its neighbors. So, P sends to each neighbor P' queries of the form $Q: R(\bar{x})$, where R is a relation of P' that appears in $\Sigma(P,P')$. P expects to receive from P' the set of PCAs to Q, because they corresponds to the extension of R in the intersection of solutions for P'. In order to return to P the PCAs to

its queries, the neighboring peers have to run their own programs (except for the facts, each peer has a fixed solution program that can be used with any query). As before, they will need PCAs from their own neighbors; etc. This recursion will eventually reach peers that have no DECs (and its local ICs will be satisfied), who will offer answers from their original instances to queries by other peers. Now, propagation of PCAs goes backwards until reaching P, and P gets the facts to run its program and obtain the PCAs to the original query.

Example 9. (Example 6 continued) Consider local instances $D(P1) = \{R^1(a,2)\}$, $D(P2) = \{R^2(c,4), R^2(d,5)\}$, and $D(P3) = \{R^3(c,4)\}$. A user poses the query $Q_0 : R^1(x,y)$ to P1, expecting its PCAs. To run its program, P1 needs the intersection of the solutions of peer P2. So, P1 sends to P2 the queries $Q_1^1 : R^2(x,y)$ and $Q_2^1 : S^2(x,y)$ (actually, P1 does not need the latter, S^2 is not relevant to P1). In order to peer-consistently-answer these queries, P2 needs from P3 the PCAs to $Q_3^2 : R^3(x,y)$. Since P3 has no neighboring peers, it returns to P2 the entire extension in its local database of relation $R^3 : I_3 = D(P3) = \{R^3(c,4)\}$ is given to P2. Now, P2 can run its solution program $\Pi(\mathfrak{P}, P2, \{I_3\})$, containing: dom(c). dom(d). ... $R^2(c,4)$. $R^2(d,5)$. $R^3(c,4)$.

$$R^{2}(x,y,\mathbf{f_{a}}) \vee R^{3}(x,y,\mathbf{f_{a}}) \leftarrow R^{2}(x,y,\mathbf{t^{\star}}), R^{3}(x,y,\mathbf{t^{\star}}), x \neq null, y \neq null.$$

$$R^{2}(x,y,\mathbf{t^{\star \star}}) \leftarrow R^{2}(x,y,\mathbf{t^{\star}}), \ not \ R^{2}(x,y,\mathbf{f_{a}}).$$

$$S^{2}(x,y,\mathbf{t^{\star \star}}) \leftarrow S^{2}(x,y,\mathbf{t^{\star}}), \ not \ S^{2}(x,y,\mathbf{f_{a}}).$$

We obtain two solutions: $\{\{R^2(d,5)\}\}$ and $\{R^2(c,4), R^2(d,5)\}\}$. So, the intersection of P2's solutions is $I_2 = \{R^2(d,5)\}$. Finally, the program $\Pi(\mathfrak{P}, P1, \{I_2\})$ given in Example 6 is run. It has only one solution, namely $\{R^1(a,2), R^1(d,5)\}\}$. Therefore, the peer consistent answers to \mathcal{Q}_0 are (a,2) and (d,5).

4 Discussion

The domain predicate, *dom*, in the solution programs can always be instantiated in a finite active domain; actually *dom* can be eliminated by adding rules [11].

In the most common PDESs, let us call them the unrestricted import case, peers P only import data from other peers they trust more than themselves; and using DECs $\Sigma(P)$ of the form (1) or (2) that have only one database predicate in the consequent which belongs to $\mathcal{R}(P)$, and all predicates in the antecedent belonging to another peer's schema. In this case, the relevant part of the intersection of the solutions of each neighbor can be obtained as the PCAs to a single conjunctive query, namely the one in the antecedent of the DEC.

Proposition 1. For the unrestricted import case of PDES, a peer P with an empty set IC(P) of local ICs always has a solution instance.

This result still holds under rather weak conditions, e.g. if the ICs in IC(P): (a) have a consequent that contains at least one database predicate (not a built-in); or (b) if only built-ins appear in the consequent, e.g. **false**, there is a predicate in the antecedent of the IC that does not appear in any of P's DECs.

If a PDES has no local ICs, then it is easy to see that the solution program is head-cycle free [18], and we obtain

Proposition 2. In the unrestricted import case, the solution program for a peer with an empty set of local ICs is equivalent to a non-disjunctive program. \Box

The hypothesis on local ICs in this result can be much weakened by assuming that local ICs are of the form identified in [5, 12], that lead to head-cycle free repair programs. Since cautious reasoning from normal logic programs is coNP-complete [18], peer consistent answering is in coNP in data complexity.

We have assumed that $\mathcal{G}(\mathfrak{P})$ is acyclic. However, the peers, not being aware of being in a cyclic $\mathcal{G}(\mathfrak{P})$, could attempt to do data exchange as described above. In order not to detect an infinite loop, for each query a unique identifier can be created and kept in all the queries that have origin in it.

The assumption of acyclicity of the accessibility graph is quite cautious in the sense that it excludes cases where a reasonable semantics could be given and the logic programs would work correctly, because the cycles in $\mathcal{G}(\mathfrak{P})$ are not relevant.

We have also assumed that the sets IC(P) of local ICs of peers P are each ref-acyclic. Even under this assumption, and also with $\Sigma(P)$ ref-acyclic, $IC(P) \cup \Sigma(P)$ can have ref-cycles. For example, with $IC(P1) = \{ \forall x (R^1(x) \to S^1(x)) \}$, $\Sigma(P1, P2) = \{ \forall x (S^1(x) \to \exists y R^2(x, y)), \forall x (R^2(x, y) \to R^1(x)) \}$. There are also cases with an acyclic $\mathcal{G}(\mathfrak{P})$, but with ref-cycles in the DECs, where the logic programming counterpart of the semantics is correct due to the role of the trust relationships.

It becomes clear that it is possible to find more relaxed conditions, both on the accessibility graph and ref-cycles, under which a sensible semantics for solutions and semantically corresponding logic programs can be given. Also, with general cyclic accessibility graphs, *super peers* [32] could be used to detect cycles and prune certain DECs, making the graph acyclic if necessary; and then our semantics could be applied.

In [14, 16, 15], the semantics of a PDES is given in terms of epistemic logic. The mappings (our DECs) are of the form $cq_i \rightarrow cq_j$, with cq_i and cq_j conjunctive queries over Pi and Pj's schemas, resp. Those DECs keep the schemas separate. It is implicitly assumed that peers trust themselves less than other peers. The semantics can be applied in the presence of cycles in the accessibility graph.

The treatment of local ICs differs from ours in two ways: (a) A peer that is inconsistent wrt its local ICs is not considered for data exchange, while in our case such a peer may apply a repair semantics, as in CQA. (b) Atoms are imported into a peer by interaction with other peers only if this does not produce a local IC violation. In our case, under the same trust conditions, the data is accepted and the peer applies again a local repair semantics.

In order to answer a query [15], a peer traverses the network eventually collecting at its site all DECs, ICs and data of other logically related peers. With these elements, the peer can construct its epistemic theory, that is used for query answering. An accessibility cycle can be detected by using request identifiers. The use of epistemic logic makes sure that *certain data*, the one a peer really knows, is passed to another peer. In our case, a peer collects only data from its neighbors; and certainty is achieved by using the PCAs of a peer, or more generally, the intersection of its solutions. A more detailed comparison can be found in [11].

The semantics in [21, 22] coincides with the epistemic semantics in [16]. They provide a distributed algorithm, where peers' data is updated by instruction of a super peer. When a query is posed to a peer, it can answer the query right away with its data because the PDES is already updated.

5 Conclusions

We have introduced a framework for peer data exchange with trust relationships. Each peer solves its data and semantic conflicts at query time, when querying its own and other peers' data.

Logic programs can be used to specify solutions for a peer and to obtain peer consistent answers. Techniques to partially compute the solution instances can be useful, since we are not interested in them per se, but in the PCAs. Techniques used in CQA, such as magic sets for stable model semantics [20] and identification of predicates that are relevant to queries and constraints, could also be used in this setting, to restrict the number of rules and the amount of data that are needed to run the program [17, 19].

The problem of query evaluation from disjunctive programs is Π_2^P -complete [18], which matches the complexity of PCA. In spite of this, it is possible to identify syntactic classes of PDESs for which peer consistent query answering has a lower complexity, and specifically tailored mechanisms to solve this problem could be developed, as for CQA (cf. [10] for a survey).

The concepts and results presented in this paper smoothly extend the semantics for *local solutions* for a peer as introduced in [7] to the transitive case. Basically, those local solutions correspond to the neighborhood solutions we introduced above. No general solution programs were presented in [7].

Semantics for PDESs have been introduced and analyzed in [27, 21, 29, 28, 22, 14, 16, 15, 23], but without considering trust relationships. In them, if there is a DEC from P to Q, it is implicitly assumed that P trusts itself less than Q. Also, all the research so far, has concentrated on the unrestricted import case. In our setting, a DEC may also restrict the data that can belong to a peer.

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