





# Improvement on a Biometric-Based Key Agreement and Authentication Scheme for the Multi-server Environments

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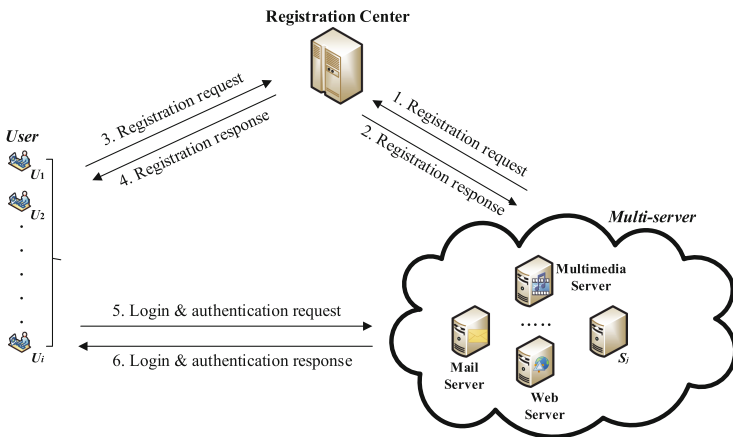
**Abstract.** With the rapid spiraling network users expansion and the enlargement of communication technologies, the multi-server environment has been the most common environment for widely deployed applications. Wang et al. recently have shown that Mishra et al.'s biohasing-based authentication scheme for multi-server was insecure, and then presented a fuzzy-extractor-based authentication protocol for key-agreement and multi-server. They continued to assert that their protocol was more secure and efficient. After a prudent analysis, however, their enhanced scheme still remains vulnerabilities against well-known attacks. In this paper, the weaknesses of Wang et al.'s protocol such as the outsider and user impersonation attacks are demonstrated, followed by the proposal of a new fuzzy-extractor and smart card-based protocol, also for key agreement and multi-server environment. Lastly, the authors shows that the new key-agreement protocol is more secure using random oracle method and Automated Validation of Internet Security Protocols and Applications (AVISPA) tool, and that it serves to gratify all of the required security properties.

**Keywords:** Multi-server · Authentication · Fuzzy-extractor  
Biometrics

## 1 Introduction

Transmission environments of the information become more open and dynamic, research on the trustworthiness of large-scale network has become progressively more crucial [1]. The typical previous user authentication schemes verify the

entered credentials with the stored databases. Since the first authentication scheme that is based on password was presented by Lamport [2] in 1981, a variety of authentication schemes [3–5] which are based on password have been presented. Regarding password authentication scheme, however, a server needs to store a list which is stored the password for the identification of the credentials of a remote user; the server thus must make arrangements for additional storage or memory for the storage of the password table. Furthermore, several researcher studies have shown that the password-based authentication protocols are vulnerable against some attacks such as the off-line password guessing or stolen smart card [6, 7]. For these reasons, many researchers have suggested a new user authentication protocol for key-agreement using biometrics. The biometrics has a major characteristic which is the uniqueness. Numerous remote user authentication schemes [8–11] have used biological characteristics. In multi-server environments (MSE), each user can approach any type of application server, regardless of their physical location, by using a single registration; for this reason, a secure remote user authentication protocol is required in the MSE. Figure 1 delineates this structure, which incorporates a one-time registration, a single smart card, and the same credentials. For this reason, the MSE requires a secure and forceful remote user authentication protocol.



**Fig. 1.** The basic architecture of multi-server

During the past decade, many researchers have presented user authentication protocols for the MSE. In 2008, Tsai [12] proposed user authentication scheme without verification record using hash function; after that, Liao and Wang [13] presented an user authentication protocol using a dynamic identity. Hsiang and Shih [14], however, have shown that Liao and Wang’s protocol was vulnerable against the replay, server spoofing, and stolen-verifier attacks, and aimed to provide mutual authentication, forward secrecy, and user anonymity.

In 2012, Li et al. [15] presented an user authentication protocol using a dynamic identity and smart card; however, Xue et al. [16] showed that Li et al.'s protocol was insecure against some attacks which are replay, eavesdropping, insider, impersonation, and denial of service (DoS), and then presented a new authentication protocol for key agreement using dynamic identity. Nevertheless, Lu et al. [17] have shown that Xue et al.'s protocol was vulnerable against some type of attacks which are masquerade, off-line password guessing and insider. To overcome these vulnerabilities, Lu et al. then presented a meliorated identity-based key-agreement protocol. Chuang and Chen [18] presented a trust computing-based authentication protocol that uses biometrics and smart cards, and they asserted that improved protocol can achieve a variety of security features; unfortunately, Mishra et al. [19] have shown that their protocol was not secure to user impersonation, server spoofing and stolen smart card attacks, and presented a new authentication protocol for key agreement using biometrics; however, Lu et al. [20] have shown that Mishra et al.'s protocol was insecure to the replay attack, and also does not provide an effective password change phase; furthermore, Wang et al. [21] have shown that Mishra et al.'s protocol was vulnerable against masquerade, replay and DoS attacks, and it cannot satisfy perfect forward secrecy. To overcome these problems, Wang et al. suggested a meliorated, authentication protocol for key agreement using biometrics; unfortunately, their proposed protocol is still insecure against some type of attacks which are outsider and user impersonation.

In this paper, we review the authentication protocol of Wang et al. [21] and show how the adversary can impersonate a legal user. Wang et al. [21] have improved the vulnerabilities of previous authentication schemes, and shown the efficient computational cost. Their scheme consists only a hash function and fuzzy-extraction technique. After demonstrating these problems, an improved fuzzy extractor-based authentication protocol is presented for MSE. Our contribution is to prove and overcome the weaknesses of Wang et al.'s protocol [21]. Lastly, the improved protocol is analyzed according to the security properties and the computational cost.

The remainder of the paper is constituted as follows: Some definitions such as threat assumptions and fuzzy extractor that are adopted for the proposed scheme are briefly introduced in Sect. 2; in Sects. 3 and 4, Wang et al.'s protocol is reviewed and analyzed, respectively; in Sect. 5, an improved fuzzy extractor-based authentication scheme is presented; in Sect. 6, a formal and informal analysis and simulation result of the improved protocol is demonstrated; Sect. 7 shows the comparison of security and performance of the improved protocol with the previous protocols; lastly, in Sect. 8, the conclusion is demonstrated.

## 2 Preliminaries

Some definitions of the threat assumptions and the fuzzy extractor which are useful to understand this paper are demonstrated in this section.

## 2.1 Threat Assumptions

The Dolev-Yao threat model [22] is introduced here, and the risk of side-channel attacks [23] is considered for the construction of the threat assumptions [8] that are demonstrated as follows:

- (TA1) A remote user can be either an adversary  $\mathcal{AD}$  or a legal user. In other words, a legitimate user can perform as any adversary  $\mathcal{AD}$ .
- (TA2) The  $\mathcal{AD}$  can intercept, modification such as insert or delete, or reroute any transmitted communication message over public channel.
- (TA3) Using the examining the power consumption, the  $\mathcal{AD}$  can pull out the stored information from the any issued smart card.

## 2.2 Fuzzy Extractor

The fuzzy extractor can convert from the biometrics to a random string, is described here. Based on the Refs. [24,25], the fuzzy extractor is made of the two procedures ( $Gen$ ,  $Rep$ ).

- $Gen(Biometrics) \rightarrow \langle \alpha, \beta \rangle$
- $Rep(Biometrics^*, \beta) = \alpha$  if  $Biometrics^*$  is reasonably close to  $Biometrics$ .

The probabilistic generation procedure  $Gen$  can extract some binary string  $\alpha \in \{0,1\}^k$  and string  $\beta \in \{0,1\}^*$  from the biometrics, where  $\alpha$  is nearly random string and  $\beta$  is an auxiliary binary, and the deterministic reproduction procedure  $Rep$  can recover a nearly random binary string  $\alpha$  from the auxiliary string  $\beta$  and any biometrics  $Biometrics^*$  when the  $Biometrics^*$  is pretty similar the  $Biometrics$ . Additional information can be found in the research [26].

## 3 Review of Wang et al.’s Protocol

Wang et al.’s fuzzy extractor-based authentication protocol for key agreement is reviewed here. Their protocol consists of three entities, as follows: user, server, and registration authority. Six phases relate to their protocol, and they are the server registration, user registration, login, authentication, password changing, and revocation or re-registration phases. For convenience, Table 1 describes some of the expressions that are used in this paper.

### 3.1 Server Registration

- (SR1)  $S_j$  sends the message to the registration authority  $RA$  for server registration request.
- (SR2)  $RA$  sends  $PK$  which is the pre-shared key to  $S_j$  through Internet Key Exchange Protocol version 2 (IKEv2) [27] by using a secure communication route.

**Table 1.** Expressions

Notation	Description
$U_i, S_j, SC_i$	User $i$ , server $j$ and smart card of $U_i$
$AD$	Adversary
$RA$	Registration authority
$ID_i, PW_i, BIO_i, DID_i$	Identity, password, biometrics and dynamic identity of $U_i$
$SID_j$	Identity of $S_j$
$TR_i$	Registration time of $U_i$
$R_i$	Positive random integer unique to $U_i$
$x$	Master secret key selected by $RA$
$\alpha_i, \beta_i$	$U_i$ 's nearly random and auxiliary binary strings
$PK$	Secure key pre-shared by $RA$ and $S_j$
$\oplus, \parallel$	XOR and concatenation operation
$h(\cdot)$	Collision-resistance one-way hash function

### 3.2 User Registration

- (UR1)  $U_i$  gives one's biometrics  $BIO_i$  at the biometrics scan sensor. The sensor then scans the  $BIO_i$ , pulls out the two random strings  $(\alpha_i, \beta_i)$  from the computation  $Gen(BIO_i) \rightarrow (\alpha_i, \beta_i)$ , and keeps the  $\beta_i$  in the temporary storage.  $U_i$  hence chooses  $ID_i$  and  $PW_i$ , and calculates  $DPW_i = h(PW_i \parallel \alpha_i)$ . Lastly,  $U_i$  sends the message  $\langle ID_i, DPW_i \rangle$  to  $RA$  for user registration by using a secure communication network.
- (UR2)  $RA$  registers a new user record  $\langle ID_i, UR_i = 1 \rangle$  into the database, where  $UR_i$  is the registration frequency of  $U_i$ .  $RA$  then calculates  $V_i = h(ID_i \parallel x \parallel TR_i)$ ,  $W_i = DPW_i \oplus h(V_i)$ ,  $X_i = W_i \oplus h(PK)$ ,  $Y_i = PK \oplus V_i \oplus h(PK)$  and  $Z_i = h(ID_i \parallel DPW_i)$ , where  $TR_i$  is the registration time of  $U_i$ .
- (UR3)  $RA$  replies a new  $SC_i$  to  $U_i$ , which is composed of  $\langle W_i, X_i, Y_i, Z_i, h(\cdot) \rangle$  by using a secure communication network.
- (UR4) After receiving the smart card,  $U_i$  stores  $\beta_i$  into  $SC_i$ .

### 3.3 Login

- (L1)  $U_i$  inserts own  $SC_i$  into a card recognizing device, enters  $ID_i$  and  $PW_i$ , and gives  $BIO_i^*$  at the biometrics scan sensor. The sensor hence scans the  $BIO_i^*$ , and recovers  $\alpha_i$  from the  $Rep(BIO_i^*, \beta_i) \rightarrow \alpha_i$ .
- (L2)  $SC_i$  then computes  $DPW_i = h(PW_i \parallel \alpha_i)$ , and checks whether  $h(ID_i \parallel DPW_i)$  is same to the stored  $Z_i$ . If this holds,  $SC_i$  further calculates  $h(PK) = W_i \oplus X_i$ .

- (L3) Next,  $SC_i$  chooses some random digits  $RN_1$ , and calculates  $DID_i = ID_i \oplus h(RN_1)$ ,  $M_1 = DPW_i \oplus RN_1 \oplus h(PK)$  and  $M_2 = h(DID_i \parallel RN_1 \parallel DPW_i \parallel SID_j \parallel TS_i)$ , where  $TS_i$  is the timestamp.
- (L4) Lastly,  $SC_i$  sends the message  $\langle DID_i, M_1, M_2, W_i, Y_i, TS_i \rangle$  to  $S_j$  for login request by using a public communication network.

### 3.4 Authentication

- (A1)  $S_j$  verifies whether  $TS_j - TS_i \leq \Delta TS$  is reasonable, where  $\Delta TS$  is the minimum acceptable time interval and  $TS_j$  is the actual arrival time of the message. If this holds,  $S_j$  proceeds on the next stage; otherwise,  $S_j$  rejects the request.
- (A2)  $S_j$  computes  $V_i = PK \oplus Y_i \oplus h(PK)$ ,  $DPW_i = W_i \oplus h(V_i)$ ,  $RN_1 = DPW_i \oplus M_1 \oplus h(PK)$ , and checks whether  $h(DID_i \parallel RN_1 \parallel DPW_i \parallel SID_j \parallel TS_i)$  is same to the received  $M_2$ .
- (A3) If this holds,  $S_j$  chooses some random digits  $RN_2$ , and calculates the common session secret key  $SK_{ji} = h(DID_i \parallel SID_j \parallel RN_1 \parallel RN_2)$ .
- (A4)  $S_j$  computes  $M_3 = RN_2 \oplus h(DID_i \parallel RN_1) \oplus h(PK)$  and  $M_4 = h(SID_j \parallel RN_2 \parallel DID_i)$ , and replies the response message  $\langle SID_j, M_3, M_4 \rangle$  to  $U_i$  by using a public communication network.
- (A5)  $SC_i$  computes  $RN_2 = M_3 \oplus h(DID_i \parallel RN_1) \oplus h(PK)$ ,  $SK_{ij} = h(DID_i \parallel SID_j \parallel RN_1 \parallel RN_2)$ , and then checks whether  $h(SID_j \parallel RN_2 \parallel DID_i)$  is same to the received  $M_4$ . If this holds,  $SC_i$  calculates  $M_5 = h(SK_{ij} \parallel RN_1 \parallel RN_2)$ , and sends  $\langle M_5 \rangle$  to  $S_j$  by using a public communication network.
- (A6)  $S_j$  checks whether  $h(SK_{ji} \parallel RN_1 \parallel RN_2)$  is equal to the received  $M_5$ . If this holds,  $S_j$  can accept the session key  $SK_{ji}$  in this session; otherwise,  $S_j$  rejects any request message.

### 3.5 Password Change

- (P1)  $U_i$  first inserts own  $SC_i$  into a card recognizing device, enters  $ID_i$  and  $PW_i$ , and gives  $BIO_i^*$  at the biometrics scan sensor. The sensor then scans  $BIO_i^*$ , and recovers  $\alpha_i$  from the computation  $Rep(BIO_i^*, \beta_i) \rightarrow \alpha_i$ .
- (P2)  $SC_i$  then computes  $DPW_i = h(PW_i \parallel \alpha_i)$ , and checks whether  $h(ID_i \parallel DPW_i)$  is same to the stored  $Z_i$ . If this holds,  $SC_i$  trying to ask the user about the new password; otherwise,  $SC_i$  immediately terminates the password change phase.
- (P3) After inputting the new  $PW_i^{new}$ ,  $SC_i$  computes  $DPW_i^{new} = h(PW_i^{new} \parallel \alpha_i)$ ,  $W_i^{new} = W_i \oplus DPW_i \oplus DPW_i^{new}$ ,  $X_i^{new} = X_i \oplus W_i \oplus W_i^{new}$  and  $Z_i^{new} = h(ID_i \parallel DPW_i^{new})$ .
- (P4) Lastly,  $SC_i$  replaces  $W_i$ ,  $X_i$  and  $Z_i$  with  $W_i^{new}$ ,  $X_i^{new}$  and  $Z_i^{new}$ .

### 3.6 Revocation or Re-registration

If any user  $U_i$  wants to revoke his/her right, it is necessary that the  $U_i$  sends the message  $\langle DPW_i \rangle$  to  $RA$  for revocation and verification by using a secure communication network.  $RA$  checks whether  $U_i$  is legitimate. If this holds,  $RA$  then updates the user's record by setting  $\langle ID_i, UR_i = 0 \rangle$ . Similarly, after receiving the message for re-registration request by using a public communication network,  $RA$  performs the same steps explained in Sect. 3.2, and it changes the user record from  $\langle ID_i, UR_i \rangle$  to  $\langle ID_i, UR_i = UR_i + 1 \rangle$ .

## 4 Cryptanalysis of Wang et al.'s Protocol

Security weaknesses of Wang et al.'s protocol is shown here, and the authors shows that Wang et al.'s protocol is vulnerable to outsider, user impersonation and privileged insider attacks.

### 4.1 Outsider Attack

Outsider attack means that a legitimate user who issued a smart card uses his/her card to extract a meaningful value for attack. Let  $AD$ , who is the legitimate user but malicious, he/she then can extract the stored information  $\{W_{AD}, X_{AD}, Y_{AD}, Z_{AD}, \beta_{AD}, h(\cdot)\}$  from the one's smart card; then, the  $AD$  can easily calculate  $h(PK) = W_{AD} \oplus X_{AD}$ , which is the same for any legitimate user and the pre-shared server key's hash result.

### 4.2 User Impersonation Attack

Suppose an adversary  $AD$  eavesdrops any user  $U_i$ 's request message  $\langle DID_i, M_1, M_2, W_i, Y_i, TS_i \rangle$  for login.  $AD$  can then perform the user impersonate attack by using message modification.

- (UA1) Outsider adversary  $AD$  obtains  $h(PK) = W_{AD} \oplus X_{AD}$  from his/her smart card.
- (UA2)  $AD$  randomly generates some nonce  $RN_{AD}$ .
- (UA3)  $AD$  then computes  $W_i^* = W_i \oplus h(PK)$ ,  $Y_i^* = h(PK)$ ,  $M_1^* = W_i \oplus RN_{AD} \oplus h(PK)$  and  $M_2^* = h(DID_i \parallel RN_{AD} \parallel W_i \parallel SID_j \parallel TS_{AD})$ , where the  $TS_{AD}$  is the current timestamp.
- (UA4)  $AD$  sends the message  $\langle DID_i, M_1^*, M_2^*, W_i^*, Y_i^*, TS_{AD} \rangle$  to the server  $S_j$  for login by using a public communication network.
- (UA5)  $S_j$  checks whether  $TS_j - TS_{AD} \leq \Delta TS$  is valid. This holds, because the  $TS_{AD}$  has a fresh value.
- (UA6)  $S_j$  retrieves  $V_i = PK \oplus Y_i^* \oplus h(PK) = PK \oplus h(PK) \oplus h(PK) = PK$ ,  $DPW_i = W_i^* \oplus h(V_i) = W_i \oplus h(PK) \oplus h(PK) = W_i$  and  $RN_{AD} = DPW_i \oplus M_1^* \oplus h(PK) = W_i \oplus W_i \oplus RN_{AD} \oplus h(PK) \oplus h(PK)$ , and verifies whether  $h(DID_i \parallel RN_{AD} \parallel W_i \parallel SID_j \parallel TS_{AD})$  is equal to the received  $M_2^*$ .

- (UA7) This holds,  $S_j$  then proceeds on the protocol without being detected. Lastly,  $AD$  and  $S_j$  “successfully” conclude the session; unfortunately, the  $S_j$  faultily decides that he/she is communicating with  $U_i$ .

## 5 The Improved Authentication Protocol

In this section, a new fuzzy extractor-based authentication protocol is proposed. Six phases relate to the proposed protocol, and they are the server registration, user registration, login, authentication, password changing, and revocation or re-registration phases.

### 5.1 Server Registration

- (SR1)  $S_j$  sends the message to  $RA$  for registration request.  
 (SR2)  $RA$  replies  $PK$  which is pre-shared key and second master key  $x$  to  $S_j$  using the Internet Key Exchange Protocol version 2 (IKEv2) [27] by using secure communication network.

### 5.2 User Registration

- (UR1)  $U_i$  imprints own biometrics  $BIO_i$  at the biometrics scan sensor. The sensor then scans the  $BIO_i$ , pulls out the two random strings  $(\alpha_i, \beta_i)$  from the computation  $Gen(BIO_i) \rightarrow (\alpha_i, \beta_i)$ , and keeps the  $\beta_i$  in the temporary storage.  $U_i$  hence chooses  $ID_i$  and  $PW_i$ , and calculates  $T_i = h(ID_i \parallel \alpha_i)$  and  $DPW_i = h(PW_i \parallel \alpha_i)$ . Lastly, the  $U_i$  sends the request message  $\langle ID_i, DPW_i \rangle$  to  $RA$  for user registration by using a secure communication network, and stores  $T_i$  in the memory.  
 (UR2)  $RA$  registers a new user record  $\langle ID_i, UR_i = 1 \rangle$  to the database, where  $UR_i$  is the registration frequency of  $U_i$ .  $RA$  then calculates  $V_i = h(ID_i \parallel x \parallel R_i)$ ,  $W_i = DPW_i \oplus h(V_i)$ ,  $X_i = h(R_i \parallel PK)$ ,  $Y_i = PK \oplus R_i \oplus h(PK)$  and  $Z_i = h(ID_i \parallel DPW_i)$ , where  $R_i$  is a positive random integer unique to the user.  
 (UR3)  $RA$  replies the new  $SC_i$  to  $U_i$ , which is composed of  $\{W_i, X_i, Y_i, Z_i, h(\cdot)\}$  by using a secure communication network.  
 (UR4)  $U_i$  computes  $X_i^* = X_i \oplus T_i$ , replaces  $X_i$  with  $X_i^*$ , stores  $\beta_i$  into  $SC_i$ , removes  $\beta_i$  and  $T_i$  from the memory, and initialize the authentication environments.

### 5.3 Login

- (L1)  $U_i$  first inserts own  $SC_i$  into a card recognizing device, enters  $ID_i$  and  $PW_i$ , and gives  $BIO_i^*$  at the biometrics scan sensor. The sensor then scans the  $BIO_i^*$ , and recovers  $\alpha_i$  from the computation  $Rep(BIO_i^*, \beta_i) \rightarrow \alpha_i$ .  
 (L2)  $SC_i$  then computes  $DPW_i = h(PW_i \parallel \alpha_i)$ , and checks whether  $h(ID_i \parallel DPW_i)$  is same to the stored  $Z_i$ . If this holds,  $SC_i$  further calculates  $h(R_i \parallel PK) = X_i \oplus h(ID_i \parallel \alpha_i)$ .



- (L3) Next,  $SC_i$  chooses some random digits  $RN_1$ , and calculates  $DID_i = ID_i \oplus h(RN_1)$ ,  $M_1 = RN_1 \oplus h(R_i \parallel PK)$  and  $M_2 = h(DID_i \parallel RN_1 \parallel DPW_i \parallel SID_j \parallel TS_i)$ , where  $TS_i$  is the current timestamp.
- (L4) Lastly,  $SC_i$  sends the message  $\langle DID_i, M_1, M_2, W_i, Y_i, TS_i \rangle$  to  $S_j$  for login request by using a public communication network.

#### 5.4 Authentication

- (A1)  $S_j$  verifies whether  $TS_j - TS_i \leq \Delta TS$  is reasonable, where  $\Delta TS$  is the minimum acceptable time interval and  $TS_j$  is the actual arrival time of the message. If this holds,  $S_j$  proceeds on the next stage; otherwise,  $S_j$  rejects the login request.
- (A2)  $S_j$  retrieves  $R_i = PK \oplus Y_i \oplus h(PK)$ ,  $RN_1 = M_1 \oplus h(R_i \parallel PK)$  and  $ID_i = DID_i \oplus h(RN_1)$ , and computes  $V_i^* = h(ID_i \parallel x \parallel R_i)$  and  $DPW_i = W_i \oplus h(V_i^*)$ , and checks whether  $h(DID_i \parallel RN_1 \parallel DPW_i \parallel SID_j \parallel TS_i)$  is same to the received  $M_2$ .
- (A3) If this holds,  $S_j$  chooses some random digits  $RN_2$ , and calculates the common session secret key  $SK_{ji} = h(DID_i \parallel SID_j \parallel h(V_i) \parallel RN_1 \parallel RN_2)$ .
- (A4)  $S_j$  computes  $M_3 = RN_2 \oplus RN_1$  and  $M_4 = h(SID_j \parallel SK_{ji} \parallel RN_1 \parallel RN_2 \parallel DID_i)$ , and replies the authentication response message  $\langle M_3, M_4 \rangle$  to  $U_i$  by using a public communication network.
- (A5)  $SC_i$  computes  $RN_2 = M_3 \oplus RN_1$ ,  $SK_{ij} = h(DID_i \parallel SID_j \parallel W_i \oplus DPW_i \parallel RN_1 \parallel RN_2)$ , and then checks whether  $h(SID_j \parallel SK_{ij} \parallel RN_1 \parallel RN_2 \parallel DID_i)$  is same to the received  $M_4$ . If this holds,  $SC_i$  can accept the session key  $SK_{ij}$  in this session; otherwise,  $U_i$  terminates this session.

#### 5.5 Password Change

- (P1)  $U_i$  first inserts own  $SC_i$  into a card recognizing device, enters  $ID_i$  and  $PW_i$ , and gives  $BIO_i^*$  at the biometrics scan sensor. The sensor then scans the  $BIO_i^*$ , and recovers  $\alpha_i$  from the computation  $Rep(BIO_i^*, \beta_i) \rightarrow \alpha_i$ .
- (P2)  $SC_i$  then computes  $DPW_i = h(PW_i \parallel \alpha_i)$ , and checks whether  $h(ID_i \parallel DPW_i)$  is same to the stored  $Z_i$ . If this holds,  $SC_i$  trying to ask the user about the new password; otherwise,  $SC_i$  immediately terminates the password change phase.
- (P3) After inputting the new  $PW_i^{new}$ ,  $SC_i$  computes  $DPW_i^{new} = h(PW_i^{new} \parallel \alpha_i)$ ,  $W_i^{new} = W_i \oplus DPW_i \oplus DPW_i^{new}$  and  $Z_i^{new} = h(ID_i \parallel DPW_i^{new})$ .
- (P4) Lastly,  $SC_i$  replaces  $W_i$  and  $Z_i$  with  $W_i^{new}$  and  $Z_i^{new}$  into the smart card.

#### 5.6 Revocation or Re-registration Phase

User revocation phase is same as the user revocation phase in Wang et al.'s protocol. If user  $U_i$  want to re-registration, the registration authority  $RA$  reissues the smart card to the user. The  $RA$  checks the  $UR_i$  value at the time of the user's login request, and if the  $UR_i$  is greater than 1,  $RA$  uses the value  $UR_i$  to calculate  $V_i^*$ .

- (RR1) After receiving the request from  $U_i$  for re-registration,  $RA$  updates a user record  $\langle ID_i, UR_i = UR_i + 1 \rangle$  to the database.  $RA$  then calculates  $V_i = h(ID_i \parallel x \parallel UR_i \parallel R_i)$ ,  $W_i = DPW_i \oplus h(V_i)$ ,  $X_i = h(R_i \parallel PK)$ ,  $Y_i = PK \oplus R_i \oplus h(PK)$  and  $Z_i = h(ID_i \parallel DPW_i)$ , where  $R_i$  is a positive random integer unique to the user.
- (RR2)  $RA$  replies the new  $SC_i$  to  $U_i$ , which is composed of  $\{W_i, X_i, Y_i, Z_i, h(\cdot)\}$  by using a secure communication network.
- (RR3)  $U_i$  computes  $X_i^* = X_i \oplus T_i$ , replaces  $X_i$  with  $X_i^*$ , stores  $\beta_i$  into  $SC_i$ , removes  $\beta_i$  and  $T_i$  from the memory, and initialize the authentication environments.

## 6 Cryptanalysis of the Proposed Protocol

The improved protocol, which maintains the merits of Wang et al.'s protocol, is demonstrated, and it can resist some type of possible attacks and supports all of the security features. The cryptanalysis of the improved protocol was organized with threat assumptions.

### 6.1 Informal Security Analysis

We explain the improved protocol can resist various kinds of known attacks.

*Outsider Attack.* Outsider attack means that a legitimate user who issued a smart card uses his/her card to extract a meaningful value for attack. Assume that an adversary  $AD$  who issued a smart card extracts  $\{W_{AD}, X_{AD}, Y_{AD}, Z_{AD}, \beta_{AD}, h(\cdot)\}$  from the one's smart card.  $AD$  can retrieve  $h(R_{AD} \parallel PK) = X_{AD} \oplus h(ID_{AD} \parallel \alpha_{AD})$ ; however,  $R_{AD}$  is a positive random integer that has the different value, and  $PK$  is the pre-shared key between  $RA$  and  $S_j$ .  $AD$  cannot obtain and use this value to the other attack, and the proposed protocol can therefore avoid the outsider attack.

*Modification Attack.* Assume that  $AD$  intercepts the transmitted informations  $\{DID_i, M_1, M_2, W_i, Y_i, TS_i, M_3, M_4\}$ ; however, the  $AD$  cannot retrieve  $R_{N_1}$ ,  $R_{N_2}$ ,  $R_i$  and  $PK$  from these messages. Even if  $AD$  uses his/her  $h(R_{AD} \parallel PK)$ ,  $A$  cannot generate  $M_1$  without the  $DPW_i$ . To compute  $DPW_i$ , the second master key  $x$  is needed. The proposed protocol can therefore avoid the modification attack.

*Off-Line Password Guessing Attack.* Assume that  $U_i$ 's  $SC_i$  is lost or  $AD$  steals  $SC_i$  of  $U_i$ ,  $AD$  can then obtain  $\{W_i, X_i, Y_i, Z_i, \beta_i, h(\cdot)\}$ ; however, he/she cannot guess the password of  $U_i$ . To guess the password from  $h(PW_i \parallel \alpha_i)$ ,  $\alpha_i$  is needed; however,  $\alpha_i$  is in possession of the high entropy; moreover, the same biometrics are not present between any two people. The proposed protocol can therefore avoid the off-line password guessing attack.

*User Impersonation Attack.* Assume that  $\mathcal{AD}$  intercepts the transmitted informations  $\{DID_i, M_1, M_2, W_i, Y_i, TS_i, M_3, M_4\}$ ; however,  $\mathcal{AD}$  cannot make the reasonable message  $\{DID_i, M_1, M_2, W_i, Y_i, TS_i\}$  for login request. This is because  $R_i$  is a positive random integer that is different from the other user's thing, and  $R_{N_1}$  is some random digits that is selected by  $U_i$ . To make  $M_2$ , the second master key  $x$  is needed. The proposed protocol can therefore avoid the user impersonation attack.

*Stolen Smart Card Attack.* Suppose that  $\mathcal{AD}$  steals  $U_i$ 's  $SC_i$ , he/she then extracts  $\{W_i, X_i, Y_i, Z_i, \beta_i h(\cdot)\}$ ; however,  $\mathcal{AD}$  cannot obtain any sensitive information of  $U_i$ . Although  $\mathcal{AD}$  obtains the  $h(R_{AD} \parallel PK)$  from one's smart card,  $R_{AD}$  and  $R_i$  are the different values. The proposed protocol can therefore avoid the stolen smart card attack.

**Table 2.** Algorithm  $EXP_{HASH,A}^{BASMK}$

```

1. Eavesdrop the login request message  $\langle DID_i, M_1, M_2, W_i, Y_i, TS_i \rangle$ 
2. Call the oracle. Let  $(RN'_1, DPW'_i) \leftarrow Reveal(M_2)$ 
3. Eavesdrop the authentication response message  $\langle M_3, M_4 \rangle$ 
4. Use the oracle. Let  $(SK'_{ij}, RN''_1, RN'_2) \leftarrow Reveal(M_4)$ 
5. if  $(RN'_1 = RN''_1)$  then
6.   Compute  $ID'_i = DID_i \oplus h(RN'_1)$  and  $H_1 = M_1 \oplus RN'_1 = h(R_i \parallel PK)$ 
7.   Use the oracle. Let  $(R'_i, PK') \leftarrow Reveal(H_1)$ 
8.   Compute  $H_2 = Y_i \oplus R'_i \oplus PK' = h(PK)$ 
9.   Use the oracle. Let  $(PK'') \leftarrow Reveal(H_2)$ 
10.    if  $(PK' = PK'')$  then
11.      Compute  $RN''_2 = M_3 \oplus RN'_1$ 
12.      if  $(RN'_2 = RN''_2)$  then
13.        Call the oracle. Let  $(PW'_i, \alpha'_i) \leftarrow Reveal(DPW'_i)$ 
14.        Compute  $h(V_i) = W_i \oplus DPW'_i$ 
15.        Compute  $SK'_{ij} = h(DID_i \parallel SID_j \parallel h(V_i) \parallel RN'_1 \parallel RN''_2)$ 
16.        if  $(SK'_{ij} == SK'_{ij})$  then
17.          Accept  $ID'_i, PW'_i, \alpha'_i, R'_i$  as the correct  $ID_i, PW_i, \alpha_i, R_i$ ,
           $PK', SK_{ij}$  as the correct  $PK$  and  $SK_{ij}$ , respectively.
18.          return 1 (Success)
19.        else
20.          return 0 (Failure)
21.        else
22.          return 0 (Failure)
23.        end if
24.      else
25.        return 0 (Failure)
26.      end if
27.    else
28.      return 0 (Failure)
29.    end if

```

### 6.2 Formal Security Analysis

The formal analysis using random oracle method is demonstrated here, and its security is shown. First, the following hash function is defined Refs. [8, 28]:

**Definition 1.** *The secure and collision-resistance hash function  $\mathcal{H}(\cdot) : \{0, 1\}^* \rightarrow \{0, 1\}^k$  picks up any input as a binary string  $a \in \{0, 1\}^*$  which has a randomly length, extracts a binary string  $\mathcal{H}(a) \in \{0, 1\}^k$ , and satisfies the following conditions:*

- (i) Given the  $b \in B$ , it's mathematically impossible to find out a  $a \in A$  such that  $b = \mathcal{H}(a)$ .
- (ii) Given the  $a \in A$ , it's mathematically impossible to find out the another  $a' \neq a \in A$ , such that  $\mathcal{H}(a') = \mathcal{H}(a)$ .
- (iii) It's mathematically impossible to find out a pair  $(a', a) \in A' \times A$ , with  $a' \neq a$ , such that  $\mathcal{H}(a') = \mathcal{H}(a)$

**Theorem 1.** *According to the assumptions that if the hash function  $\mathcal{H}(\cdot)$  closely performs like an oracle, then the protocol is certainly secure to the adversary  $\mathcal{AD}$  for the protection of the meaningful information including the identity  $ID_i$ , the password  $PW_i$ , the nearly random binary string  $\alpha_i$ , the positive random integer  $R_i$ , the pre-shared key  $PK$  and the common session key  $SK_{ij}$ .*

**Proof.** Formal proof of the proposed protocol is analogous to those in Refs. [8, 20, 28, 29], and it uses the following random oracle model to construct the  $\mathcal{AD}$ , who will have the ability to recover the  $ID_i, PW_i, \alpha_i, R_i, PK$  and  $SK_{ij}$ .

**Reveal.** The random oracle can obtain the input  $a$  from the hash result  $b = \mathcal{H}(a)$  without failure.  $\mathcal{AD}$  now performs the experimental algorithm as shown in Table 2,  $EXP_{HASH, A}^{BASMK}$  for the proposed protocol as BASMK. Let's define the probability of success for  $EXP_{HASH, A}^{BASMK}$  as  $Success_{HASH, A}^{BASMK} = |Pr[EXP_{HASH, A}^{BASMK} = 1] - 1|$ , where  $Pr(\cdot)$  means the probability of  $EXP_{HASH, A}^{BASMK}$ . The advantage function for this algorithm then becomes  $Adv_{HASH, A}^{BASMK}(t, q_R) = max_{Success}$ , where  $t$  and  $q_R$  are the execution cost and number of queries. Consider the algorithm as shown in Table 2. If the  $\mathcal{AD}$  has the capability to crack the problem of hash function given in Definition 1,  $\mathcal{AD}$  can then immediately obtain the  $ID_i, PW_i, \alpha_i, R_i, PK$  and  $SK_{ij}$ . In that case,  $\mathcal{AD}$  will detect the complete connections between the  $U_i$  and  $S_j$ ; however, the inversion of the input from the given hash result is impossible computationally, i.e.,  $Adv_{HASH, A}^{BASMK}(t) \leq \epsilon$ , for all  $\epsilon > 0$ . Therefore,  $Adv_{HASH, A}^{BASMK}(t, q_R) \leq \epsilon$ , since  $Adv_{HASH, A}^{BASMK}(t, q_R)$  depends on  $Adv_{HASH, A}^{BASMK}(t)$ . In conclusion, it is no method for  $\mathcal{AD}$  to detect the complete connections between the  $U_i$  and  $S_j$ , the proposed protocol thus is certainly secure to  $\mathcal{AD}$  for retrieving  $(ID_i, PW_i, \alpha_i, R_i, PK, SK_{ij})$ .

**Table 3.** The result of the analysis using OFMC backend

```

% OFMC
% Version of 2006/02/13
SUMMARY
  SAFE
DETAILS
  BOUNDED_NUMBER_OF_SESSIONS
PROTOCOL
  /home/span/span/testsuite/results/testrv4.if
GOAL
  as_specified
BACKEND
  OFMC
COMMENTS
STATISTICS
  parseTime: 0.00s
  searchTime: 71.86
  visiteNodes: 11440 nodes
  depth: 9 piles

```

### 6.3 Simulation Using AVISPA

We perform to simulate the improved protocol for formal analysis using the widely accepted AVISPA. The main contribution of this simulation is to verify whether the proposed protocol is invulnerable to two attacks which are replay and man-in-the middle. AVISPA is composed of four back-ends: (1) On-the-fly Model-Checker; (2) Constraint-Logic-based Attack Searcher; (3) SAT-based Model Checker; and (4) Tree Automata based on Automatic Approximations for the Analysis of Security Protocols. The protocol is implemented in High Level Protocol Specification Language (HLPSL) [28] in AVISPA. The fundamental classes available in the HLPSL are [30]. The simulation result of the proposed protocol using OMFC is shown in Table 3. The result shows that two attacks which are man-in-the middle and replay have no effect on the proposed protocol.

## 7 Functionality and Performance Analysis

The comparisons of the functionality and computational cost of the proposed protocol with the other previous protocols [15, 16, 18–21] are demonstrated here.

### 7.1 Functionality Analysis

Table 4 itemizes the avoidance comparisons of various biometric-based key agreement protocols for MSE. The result shows that the proposed protocol is distinctly secure and achieves all of the security requirements.

**Table 4.** The comparison of the attack resistance

	Li et al. [15]	Xue et al. [16]	Chuang et al. [18]	Mishra et al. [19]	Lu et al. [20]	Wang et al. [21]	Ours
P1	×	×	×	×	×	×	✓
P2	×	×	✓	×	✓	✓	✓
P3	✓	✓	✓	✓	✓	×	✓
P4	×	×	✓	✓	✓	✓	✓
P5	×	×	✓	✓	✓	✓	✓
P6	✓	×	✓	✓	✓	×	✓
P7	×	✓	×	✓	×	×	✓
P8	✓	✓	×	✓	×	×	✓
P9	✓	✓	×	×	✓	✓	✓
P10	✓	×	✓	✓	✓	✓	✓

✓: Resist to the attack; ×: Vulnerable to the attack; P1: outsider attack; P2: replay attack; P3: modification attack; P4: stolen verifier attack; P5: off-line guessing attack; P6: insider attack; P7: stolen smart card attack; P8: user impersonation attack; P9: DoS attack; P10: server spoofing attack.

**Table 5.** The comparison of computational cost

	Registration	Login	Authentication	Total	Time(ms)
Li et al. [15]	$6T_H$	$6T_H$	$13T_H$	$25T_H$	5.0
Xue et al. [16]	$7T_H$	$6T_H$	$19T_H$	$31T_H$	6.4
Chuang et al. [18]	$3T_H$	$4T_H$	$13T_H$	$20T_H$	4.0
Mishra et al. [19]	$7T_H$	$6T_H$	$11T_H$	$24T_H$	4.8
Lu et al. [20]	$5T_H$	$5T_H$	$12T_H$	$22T_H$	4.4
Wang et al. [21]	$5T_H$	$4T_H$	$11T_H$	$20T_H$	4.0
Our proposed	$7T_H$	$5T_H$	$9T_H$	$21T_H$	4.2

## 7.2 Performance Analysis

The computational costs are compared. Table 5 itemizes a comparison of the computational spending of the protocol with the related previous protocols, where the definition of  $T_H$  is hash function’s computational times. According to the results obtained in [31],  $T_H$  is less than 0.2ms on average, in MSE (Core: 3.2 GHz, Memory: 3.0 G). Compared with Wang et al.’s protocol, the proposed protocol requires a slightly higher computational overhead, as the proposed scheme computes the one extra hash operations; however, the proposed scheme possesses all of the properties in terms of the security.

## 8 Conclusion

Recently, Wang et al. demonstrated the security weaknesses of Mishra et al., and presented a fuzzy extractor-based authentication protocol. They also asserted that their protocol is more secure and guarantees user anonymity; however, Wang et al.'s protocol was insecure to outsider and user impersonation attacks. To overcome these security weaknesses, the authors propose an improved fuzzy extractor-based authentication protocol for the multi-server environment that continues to have the merits of Wang et al.'s scheme. Furthermore, the proposed protocol comprises inclusive security properties. The formal and informal analysis of this paper make clear or explain why the proposed protocol is more secure.

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