



Throughput Analysis for Energy Harvesting Cognitive Radio Networks with Unslotted Users

Honghao Ma, Tao Jing, Fan Zhang, Xin Fan, Yanfei Lu, and Yan Huo^(✉)

School of Electronics and Information Engineering,
Beijing Jiaotong University, Beijing, China
yhuo@bjtu.edu.cn

Abstract. Considering a cognitive radio network (CRN) with the energy harvesting (EH) capability, we design a sensing-based flexible timeslot structure for a secondary transmitter (ST). This structure focuses on an unslotted transmission mode between two primary users (PUs). In this structure, the ST can decide whether to transmit data or to harvest energy based on the sensing results. Aiming to maximize the long-term average achievable throughput of the secondary system, we study an optimal policy, including the optimal energy harvesting time as well as the optimal transmit power. To reduce the computational complexity, we also derive an effective suboptimal policy by maximizing the upper bound on the throughput. Finally, simulation results demonstrate that the proposed flexible timeslot structure outperforms the conventional fixed timeslot structure in terms of average achievable throughput.

Keywords: Cognitive radio network · Energy harvesting
Unslotted primary users · Average available throughput

1 Introduction

A cognitive radio network (CRN) with energy harvesting (EH) is expected as a promising solution for green communications [1, 2]. Different from energy-efficient protocol designs [3–5], the EH technology may increase the battery life of wireless devices by replenishing energy from various energy sources [6, 7], while CRNs can improve the spectral efficiency by opportunistic access schemes. In view of the inherent “harvesting-sensing-throughput” tradeoff in EH CRNs [8, 9], it is crucial for an EH secondary user (SU) to effectively utilize energy (i.e., charging or discharging) to improve system performance and spectral efficiency [10, 11].

Existing studies focused on the optimal energy management and spectrum sensing policies in EH CRNs with time-slotted PUs. In this scenario, the channel of a PU remains idle or busy invariably in one slot while changes with a certain probability in another. Also, SUs need to synchronize with the PUs’ slot to achieve cooperative communications. In particular, the authors presented a saving-sensing-transmitting timeslot division strategy for an EH secondary

transmitter (ST) to maximize its expected achievable throughput in [8]. In [12] the authors analyzed impacts of sensing and access probabilities as well as the energy queue capacity on the maximum achievable throughput in a multi-user EH CRN. The authors of [13] investigated the optimal energy-efficient resource allocation schemes for the EH CRNs. Moreover, information-energy cooperative strategies in [14, 15] are investigated to further improve the energy efficiency.

Yet, PUs may send signals in an unslotted manner during actual transmission [16, 17]. PUs and SUs may be hard to be synchronized because of incompatible communication protocols. As a result, it is urgent to study novel spectrum access strategies and/or power allocation schemes for SUs with unslotted primary systems. To the best of our knowledge, little has been done to improve the achievable throughput of an SU in the unslotted EH CRNs. Our exploration of this uncharted area requires addressing the following challenging questions: (i) How to formulate a primary traffic model in the unslotted scenario? (ii) How to design an unslotted data transmit policy of an SU with energy constraint?

Considering these questions, the authors formulated the duration of either an idle state or a busy one as an exponential distributed random variable in [16–18]. They calculated the prior probability of channel being idle using the mean durations of these two states. Similarly, [19, 20] employed the channel’s state transition matrix to derive stationary probabilities of channel states. Then, several solutions were proposed for the conventional CRNs without EH. The authors first derived the optimal frame duration and transmit power for energy-unconstrained SUs in [17]. Then, they studied the optimal power control policy in [16] to maximize SUs’ energy efficiency in the presence of unslotted PUs and sensing errors. In [19], the authors designed two data transmit policies with idle and busy sensing results to fully utilize unslotted channels. Also, the authors of [20] elaborated an optimal dual sensing-interval policy to maximize ST’s spectrum utilization to achieve opportunistic energy harvesting for primary signals.

By adopting the same assumption of [20], we present a novel sensing-based flexible timeslot structure for the unslotted EH CRN in this article. Instead of achieving SU’s optimal spectrum utilization, we intend to maximize its achievable throughput. Moreover, we assume that an ST may harvest energy from the ambient environment. After that, it employs a part of the stored energy to sense the primary channel. If the channel is sensed as idle, the ST will send data via the channel; otherwise, it should continue to harvest energy then re-sense the channel after energy harvesting. The main contributions are as follows:

- Considering an EH CRN with an unslotted primary system, we propose a novel sensing-based flexible timeslot structure for the EH ST to maximize its long-term average achievable throughput.
- For the throughput maximization problem, we employ a differential evolution (DE) algorithm to derive the optimal policy, including the optimal harvesting time and the optimal transmit power.
- To reduce the computational complexity, we also derive an effective suboptimal policy by maximizing the upper bound on the achievable throughput.

The remainder of this paper is organized as follows. An EH CRN architecture including primary and secondary systems is described in Sect. 2. In Sect. 3, we formulate and solve the achievable throughput maximization problem of the secondary system. Section 4 demonstrates the throughput performance of our flexible timeslot structure. Finally, we conclude this paper in Sect. 5.

2 System Model

Figure 1 is an EH CRN with Rayleigh fading channels. Channel power gains $|h_{pp}|^2$, $|h_{sp}|^2$ and $|h_{ss}|^2$ of PT-PR, ST-PR and ST-SR links are exponentially distributed variables with unit mean. Moreover, noise power is assumed to be N_0 for all users.

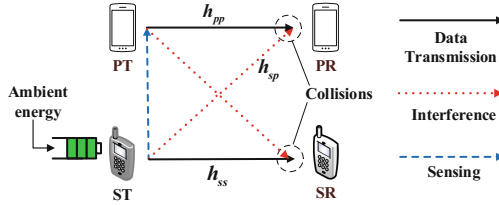


Fig. 1. System model of an EH CRN.

2.1 Primary System Model

A PT sends signals to its PR in an unslotted mode¹ with a fixed transmit power P_p . The corresponding channel state alternatively transfers between busy and idle with random durations. Similar to [17, 19, 20], busy and idle durations can be modeled as independent exponentially distributed random variables with mean $E_1 = \frac{1}{\lambda_1}$ and $E_0 = \frac{1}{\lambda_0}$.² Thus, the busy and idle probabilities are defined as

$$p_1 = \Pr\{S(t) = 1\} = \frac{\lambda_0}{\lambda_0 + \lambda_1}, \text{ and } p_0 = \Pr\{S(t) = 0\} = \frac{\lambda_1}{\lambda_0 + \lambda_1}. \quad (1)$$

where $S(t) = 1$ (or $S(t) = 0$) indicates the channel is busy (or idle) at time t . And the primary communication is successful only when the received SINR at the PR is higher than a predefined threshold β [21].

¹ In this paper, we consider a single-user unslotted primary system without sensing ability, so ST's transmit may not prevent the PT from reactivation.

² Similar to [19], λ_1 and λ_0 can be known at an ST by probing the channel in a specified learning period.

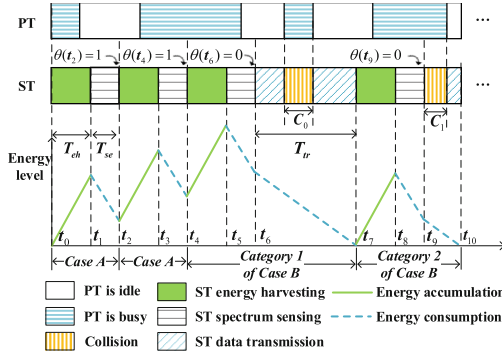


Fig. 2. The sensing-based flexible timeslot structure.

2.2 Secondary System Model

In the secondary system, an EH-enabled ST completely depends on the energy harvested from the ambient environment to communicate with its energy-unconstrained secondary receiver (SR) when the channel is idle. Here, we propose a novel sensing-based flexible timeslot structure for ST to realize effective transmissions, shown as Fig. 2. This structure includes three processes, i.e., energy harvesting, spectrum sensing, and data transmission, with durations of T_{eh} , T_{se} , and T_{tr} , respectively. Due to hardware duplex limitations [8, 22], we assume that the ST can perform only one process at any time.

Energy Harvesting. In this process, the ST harvests energy from the ambient environment. The energy flows follow an i.i.d random process with mean P_{eh} , thus the average harvested energy is $e_h = P_{eh}T_{eh}$ during T_{eh} . These energy is stored in the battery and the battery capacity is assumed to be infinite. Note that the energy loss caused by harvesting is negligible in this paper.

Spectrum Sensing. After energy harvesting, the ST carries out spectrum sensing with an energy detector. Since T_{se} is much smaller than E_1 and E_0 , it is reasonable to think that the channel state remains unchanged during T_{se} [19]. If the channel is sensed as idle, the ST transmits; otherwise, it converts to energy harvesting process immediately. The sensing accuracy is measured by the detection probability P_d and the false alarm probability P_f . For a target detection probability P_d^* , the false alarm probability P_f can be written as

$$P_f = Q \left(\sqrt{2\gamma_{ST} + 1} \cdot Q^{-1}(P_d^*) + \gamma_{ST} \sqrt{T_{se} \cdot f_s} \right), \tag{2}$$

where $Q(x) = \frac{1}{\sqrt{2\pi}} \int_x^\infty e^{-t^2/2} dt$ is a Q-function, f_s is the ST's sampling frequency to primary signals and γ_{ST} is the received SNR of primary signals at the ST.

For analysis simplicity, we assume the energy consumption for spectrum sensing e_s is proportional to T_{se} , i.e., $e_s = P_{se}T_{se}$, where P_{se} is the power consumption per unit of sensing time.

Data Transmission. It is assumed that the ST has perfect information of h_{ss} but only knows the distributions of h_{pp} and h_{sp} . When the channel is sensed as idle, the ST will exhaust all its residual energy E_r to transmit [8]. The transmit power, P_{tr} , is consistent during transmission and the transmit time $T_{tr} = \frac{E_r}{P_{tr}}$ varies with different E_r .

3 Problem Formulation

In this section, we first formulate the long-term achievable throughput of the secondary system, then derive a differential evolution based optimal policy to maximize this throughput. Finally, we further develop a suboptimal policy to reduce the computational complexity by maximizing the upper bound on the average achievable throughput.

3.1 Formulation of the Average Achievable Throughput

According to whether it transmits data after spectrum sensing, we classify ST's successive operations into *Case A* and *Case B*, as shown in Fig. 2.

Case A: The ST harvests energy and senses the channel, but not transmits data. *Case A* happens when the channel is sensed as busy (no matter what the exact channel state is) with the probability of $P_A = p_1P_d^* + p_0P_f$, where $p_1P_d^*$ is the probability that the channel is correctly sensed as busy and p_0P_f is the probability that ST wrongly senses the idle channel as busy.

Case B: After the channel is sensed as idle, the ST performs a data transmission. Here, *Case B* can be further divided into *Scenario 1* and *Scenario 2* according to the real channel state:

1. *Scenario 1:* It happens when the channel is really idle and no false alarm is generated with the probability of $P_{B1} = p_0(1 - P_f)$.
2. *Scenario 2:* It happens when the channel is actually busy but wrongly sensed as idle by the ST with the probability of $P_{B2} = p_1(1 - P_d^*)$.

In an unslotted primary system, PUs can start or stop transmitting at any time. Thus in *Scenario 1*, the PT might occupy the channel when ST is transmitting. This inevitably leads to interference between two systems, i.e., collisions. ST's maximum instantaneous transmit rate under the idle channel is $r(P_{tr}) = \log_2(1 + \alpha P_{tr})$, where $\alpha = \frac{|h_{ss}|^2}{N_0}$. While a collision happens, secondary transmission fails and $r(P_{tr})$ reduces to zero for P_p is much higher than P_{tr} . And the outage probability of PUs is

$$P_{out} = \Pr\left[\frac{|h_{pp}|^2 P_p}{|h_{sp}|^2 P_{tr} + N_0} < \beta\right] = 1 - \frac{P_p e^{-\frac{\beta N_0}{P_p}}}{\beta P_{tr} + P_p}. \quad (3)$$

According to [20, 23], given $S(t) = 0$, the channel's expected idle time during $[t, t + T_{tr}]$ is a function of P_{tr} , i.e.,

$$T_0^0(P_{tr}) = \frac{E_r}{P_{tr}} - C_0(P_{tr}), \quad (4)$$

where

$$C_0(P_{tr}) = \frac{E_r}{P_{tr}} p_1 + \frac{e^{\left(\frac{-(\lambda_1 + \lambda_0)E_r}{P_{tr}}\right)} - 1}{\lambda_1 + \lambda_0} p_1 \quad (5)$$

is the average collision time and has been illustrated in Fig. 2.

For *Scenario 2*, the ST might have opportunities to enable successful transmission after the current primary transmission is finished. And the expected idle time during $[t, t + T_{tr}]$ provided that $S(t) = 1$ is

$$T_0^1(P_{tr}) = \frac{E_r}{P_{tr}} - C_1(P_{tr}), \quad (6)$$

where

$$C_1(P_{tr}) = \frac{E_r}{P_{tr}} p_1 - \frac{e^{\left(\frac{-(\lambda_1 + \lambda_0)E_r}{P_{tr}}\right)} - 1}{\lambda_1 + \lambda_0} p_0. \quad (7)$$

The ST may go through *Case A* k times before going through *Scenario 1* or *Scenario 2* of *Case B* with the probability $P_{B1}P_A^k$ or $P_{B2}P_A^k$, respectively. And the residual energy E_r for each condition is $E_r(T_{eh}) = (1+k)(T_{eh}P_{eh} - T_{se}P_{se})$. Therefore the average achievable throughput of the secondary system for a long-term period can be written as

$$R(T_{eh}, P_{tr}) = \sum_{k=0}^{\infty} \frac{r(P_{tr})\Delta(P_{tr})P_{tr}}{T(T_{eh})P_{tr} + E_r(T_{eh})} \cdot P_A^k, \quad (8)$$

where $\Delta(P_{tr}) = P_{B1}T_0^0(P_{tr}) + P_{B2}T_0^1(P_{tr})$ is ST's average effective transmit time, and $T(T_{eh}) = (1+k)(T_{eh} + T_{se})$.

3.2 Average Achievable Throughput Maximization

We formulate the maximization problem of the long-term average achievable throughput as

$$\mathbf{P1:} \quad \max_{T_{eh}, P_{tr}} R(T_{eh}, P_{tr}) \quad (9a)$$

$$s.t. \quad P_{tr} \geq 0 \quad (9b)$$

$$e_h \geq e_s \quad (9c)$$

$$P_{out} \leq P_{out}^{max} \quad (9d)$$

$$0 \leq T_{eh} \leq T_{eh}^U. \quad (9e)$$

In **P1**, (9c) refers to the average energy causality constraint. P_{out}^{max} in (9d) is the outage probability threshold of the primary system. And T_{eh}^U in (9e) is the maximum allowed energy harvesting time.

Substituting the expressions of e_h and e_s into (9c), we obtain

$$T_{eh} \geq T_{eh}^L, \text{ where } T_{eh}^L = \frac{P_{se} T_{se}}{P_{eh}}. \quad (10)$$

And according to (9d), we can get

$$P_{tr} \leq P_{tr}^U, \text{ where } P_{tr}^U = \frac{1}{\beta} \left(\frac{P_p e^{-\frac{\beta N_0}{P_p}}}{1 - P_{out}^{max}} - P_p \right). \quad (11)$$

Then **P1** can be rewritten as

$$\begin{aligned} \mathbf{P2:} \quad & \max_{T_{eh}, P_{tr}} R(T_{eh}, P_{tr}) \\ & s.t. \quad T_{eh}^L \leq T_{eh} \leq T_{eh}^U \\ & \quad \quad 0 \leq P_{tr} \leq P_{tr}^U. \end{aligned} \quad (12)$$

Here, **P2** is a non-trivial problem. We employ the differential evolution (DE) algorithm [24] to solve it. The optimal policy derivation is detailed in Algorithm 1, where the population size N_p , mutation factor F , crossover constant C_r and the maximum number of generation G_{max} are set to be 30, 0.85, 0.7 and 100, respectively. The total time complexity of Algorithm 1 is $O(2N_p G_{max})$.

Algorithm 1. The DE-based Optimal Policy Derivation.

```

1: Set  $G = 0$ ;
2: Randomly select  $(T_{eh}(i), P_{tr}(i))$  from  $T_{eh} \in [T_{eh}^L, T_{eh}^U]$  and  $P_{tr} \in [0, P_{tr}^U]$ ;
3: while  $G < G_{max}$  do
4:    $G = G + 1$ ;
5:   for  $i \in \{1, 2, \dots, N_p\}$  do
6:     Randomly pick  $a, b$  and  $c \in \{1, \dots, N_p\} - \{i\}$ ;
7:      $D = (T_{eh}(b), P_{tr}(b)) - (T_{eh}(c), P_{tr}(c))$ ;
8:      $(T_{eh}^{var}, P_{tr}^{var}) \leftarrow (T_{eh}(a), P_{tr}(a)) + F \cdot D$ ;
9:     Randomly pick  $k_1$  and  $k_2 \in [0, 1]$ ;
10:    if  $k_1 > C_r$  then
11:       $T_{eh}^{var} \leftarrow T_{eh}(i)$ ;
12:    end if
13:    if  $k_2 > C_r$  then
14:       $P_{tr}^{var} \leftarrow P_{tr}(i)$ ;
15:    end if
16:    if  $R(T_{eh}^{var}, P_{tr}^{var}) > R(T_{eh}(i), P_{tr}(i))$  then
17:       $(T_{eh}(i), P_{tr}(i)) \leftarrow (T_{eh}^{var}, P_{tr}^{var})$ ;
18:    end if
19:  end for
20: end while
21: return  $(T_{eh}^*, P_{tr}^*) \leftarrow \operatorname{argmax}\{R(T_{eh}(i), P_{tr}(i)), i = 1, \dots, N_p\}$ ;

```

3.3 Suboptimal Solution Derivation

Since the optimal policy of Algorithm 1 has a relatively high computational complexity, we next propose a suboptimal but effective policy as below.

Theorem 1. *The average achievable throughput of the secondary system $R(T_{eh}, P_{tr})$ is upper bounded by*

$$R_U(T_{eh}, P_{tr}) = \frac{p_0(1 - P_f)r(P_{tr})\phi_1(T_{eh})}{\phi_1(T_{eh})P_{tr} + \phi_2(T_{eh})} \cdot \frac{1}{1 - P_A}, \quad (13)$$

where $\phi_1(T_{eh}) = T_{eh}P_{eh} - T_{se}P_{se}$, $\phi_2(T_{eh}) = T_{eh} + T_{se}$.

Proof. Since $Q(x)$ is a monotonously decreasing function, $P_f \leq P_d^*$ holds according to (2). Then we have

$$\Delta(P_{tr}) \leq (1 - P_f)(p_0T_0^0(P_{tr}) + P_1T_0^1(P_{tr})). \quad (14)$$

Substituting (4) and (6) into (14), we can further derive that $\Delta(P_{tr}) \leq \frac{p_0(1 - P_f)E_r}{P_{tr}}$. Additionally, $\sum_{k=0}^{\infty} P_A^k = \frac{1}{1 - P_A}$. Therefore,

$$R(T_{eh}, P_{tr}) \leq \frac{p_0(1 - P_f)r(P_{tr})\phi_1(T_{eh})}{\phi_1(T_{eh})P_{tr} + \phi_2(T_{eh})} \cdot \frac{1}{1 - P_A}. \quad (15)$$

This completes the proof of Theorem 1.

Then we discard the constant components in $R_U(T_{eh}, P_{tr})$ and maximize it under the same constraints with **P2**, i.e.,

$$\begin{aligned} \mathbf{P3}: \quad & \max_{T_{eh}, P_{tr}} \frac{r(P_{tr})\phi_1(T_{eh})}{\phi_1(T_{eh})P_{tr} + \phi_2(T_{eh})} \\ & s.t. \quad T_{eh}^L \leq T_{eh} \leq T_{eh}^U \\ & \quad \quad 0 \leq P_{tr} \leq P_{tr}^U. \end{aligned} \quad (16)$$

To solve **P3**, we present the following Theorem 2.

Theorem 2. *For **P3**, the optimal energy harvesting time T'_{eh} is T_{eh}^U and the optimal transmit time P'_{tr} is given as*

$$P'_{tr} = \min\left\{P_{tr}^U, \frac{\varphi}{\alpha \cdot W\left(\frac{\varphi}{e}\right)} - \frac{1}{\alpha}\right\}, \quad (17)$$

where $W(\cdot)$ refers to the Lambert W function and $\varphi = \frac{\alpha(T_{eh}^U P_{eh} - T_{se} P_{se})}{T_{eh}^U + T_{se}} - 1$.

Proof. We first define a function

$$f(T_{eh}, P_{tr}) \triangleq \frac{r(P_{tr})\phi_1(T_{eh})}{\phi_1(T_{eh})P_{tr} + \phi_2(T_{eh})}. \quad (18)$$

It can be easily proved that the first order partial derivative of $f(T_{eh}, P_{tr})$ with respect to T_{eh} is positive for any $T_{eh} \in [T_{eh}^L, T_{eh}^U]$. Therefore, $f(T_{eh}, P_{tr})$ is a monotonically increasing function for T_{eh} and the optimal harvesting time T_{eh}' of **P3** is obtained at T_{eh}^U .

Substituting $T_{eh}' = T_{eh}^U$ into (18), we have $f(P_{tr}) = \frac{r(P_{tr})\phi_3}{\phi_4 P_{tr} + \phi_3}$, where $\phi_3 = T_{eh}^U P_{eh} - T_{se} P_{se}$ and $\phi_4 = T_{eh}^U + T_{se}$. We denote the stationary point of $f(P_{tr})$ by P_{tr}^s and it can be derived as

$$\begin{aligned} \left. \frac{\partial f(P_{tr})}{\partial P_{tr}} \right|_{P_{tr}=P_{tr}^s} = 0 &\Rightarrow \alpha\phi_4 P_{tr} + \phi_3 - \phi_4(1 + \alpha P_{tr}) \ln(1 + \alpha P_{tr}) = 0 \\ \Rightarrow P_{tr}^s &= \frac{\varphi}{\alpha \cdot W\left(\frac{\varphi}{\alpha}\right)} - \frac{1}{\alpha}, \end{aligned} \quad (19)$$

where $W(\cdot)$ refers to the Lambert W function and $\varphi = \frac{\alpha\phi_4}{\phi_3} - 1$. Since $\frac{\partial f(P_{tr})}{\partial P_{tr}} \geq 0$ when $0 \leq P_{tr} \leq P_{tr}^s$ and $\frac{\partial f(P_{tr})}{\partial P_{tr}} \leq 0$ when $P_{tr} \geq P_{tr}^s$, the optimal transmit power of **P3** is $P_{tr}' = \min\{P_{tr}^U, P_{tr}^s\}$. This completes the proof of Theorem 2.

Now, we can derive (T_{eh}', P_{tr}') as a suboptimal policy to maximize the average achievable throughput by using Theorem 2. Next, we will evaluate its performance in Sect. 4.

4 Simulation Results

In this section, simulation results are presented to evaluate the performance of our proposed sensing-based flexible timeslot structure. Unless mentioned explicitly, simulation parameters (mainly referred to [21, 25]) are set as Table 1.

Table 1. Simulation parameters

Notations	Meanings	Values
β	SINR threshold of the PR	5
P_{out}^{max}	Outage probability threshold of PUs	0.1
P_p	PT's transmit power	50 mW
P_{se}	ST's sensing power	110 mW
T_{se}	ST's sensing time	1 ms
f_s	ST's sampling frequency	1 MHz
γ_{ST}	SINR of primary signal at the ST	-10 dB
N_0	Noise power	-40 dBm

Firstly, we present the impacts of average idle duration E_0 and average busy duration E_1 on the maximum average achievable throughput of the optimal policy, as shown in Fig. 3. The target detection probability P_d^* and P_{eh} are set to be 0.9 and 20 mW, respectively. As we can see, the maximum average

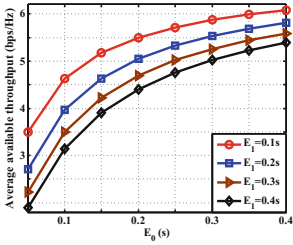


Fig. 3. R versus E_0 .

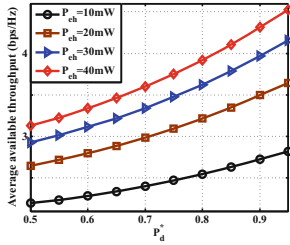


Fig. 4. R versus P_d^* .

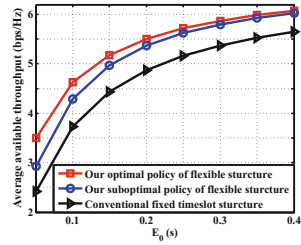


Fig. 5. Throughput.

achievable throughput increases with E_0 for a given E_1 . The reasons come from two aspects. One is that the increase of E_0 results in a higher p_0 and a lower P_A when E_1 is kept constant. And the decreased P_A provides the ST with more spectrum access opportunities. The other is that the increase of E_0 prolongs ST’s average effective transmit time and finally leads to a throughput improvement. In addition, it can be seen that the maximum average achievable throughput raises up with a slow-down tendency, due to p_0 converges to 1 as E_0 enlarges. These also explain the throughput decline resulting from the increase of E_1 for a fixed E_0 . In the case of the same p_0 (i.e., $E_0 = 0.1$ s with $E_1 = 0.2$ s and $E_0 = 0.2$ s with $E_1 = 0.4$ s), the throughput is absolutely dominated by E_0 thus a higher E_0 gains a better throughput performance.

Next, we analyze the impact of the target detection probability P_d^* on the maximum average achievable throughput of the optimal policy in Fig. 4. Here, E_0 and E_1 are set to be 0.05s and 0.1s, respectively. As shown in Fig. 4, the maximum average achievable throughput grows significantly with the growth of P_d^* . Since P_A monotonically increases with P_d^* , the ST has fewer spectrum access opportunities. To take full advantages of these rare opportunities, the ST may reduce T_{eh} to sense the spectrum more frequently and then improve P_{tr} to acquire a higher instantaneous transmit rate. The decrease of T_{eh} and the increase of P_{tr} jointly result in a higher maximum average achievable throughput.

4.1 Impacts of Key Parameters on the Optimal Policy

Finally, we discuss the impact of P_{eh} on the throughput performance. From Fig. 4 we can observe that a higher average achievable throughput can be achieved by employing a higher P_{eh} . But the higher P_{eh} is, the smaller the throughput gain is obtained. This implies that blindly promoting energy harvesting performance is not always desirable. The reason is that the increment of harvesting rate could not lead to a proportional throughput gain as we expected.

4.2 Analysis of the Average Achievable Throughput

In this subsection, we compare the maximum average achievable throughput of the optimal policy and suboptimal policy of our proposed flexible timeslot structure in Fig. 5. A conventional fixed timeslot structure proposed in [8] is introduced as our reference. Note the difference of throughput between the optimal

and suboptimal policies is quite small, which indicates that our suboptimal policy can provide a proper approximation to the optimal policy. In addition, the average available throughput grows gradually when the growth of E_0 . The reason is that the larger E_0 can provide more spectrum access opportunities for an ST. Accordingly, the results in Fig. 5 illustrate that our policies (including the optimal policy and suboptimal policy) outperform the conventional one both in achievable throughput. This demonstrates that our proposed flexible structure has more freedom to harvest and sense than a fixed timeslot structure.

5 Conclusion

In this paper, we propose a flexible timeslot structure for an EH CRN. The ST with the energy harvesting capability in this structure can share the same spectrum with an unslotted primary system without degrading primary transmission. To achieve this goal, we formulate an optimal policy derivation problem to maximize the long-term average achievable throughput of the secondary system under energy causality constraint and the SINR requirement of the primary system. Then, we design a DE-based optimal policy derivation to find the optimal solution and further provide a relative suboptimal policy to reduce the computational complexity. Numerical results demonstrate that our flexible timeslot structure is superior to the conventional fixed one. These results also indicate that it is necessary to design this flexible structure for the secondary system when PUs communicate with each other in the unslotted mode.

Acknowledgments. This work was supported by the National Natural Science Foundation of China (Grant No. 61471028, 61571010, and 61572070), and the Fundamental Research Funds for the Central Universities (Grant No. 2017JBM004 and 2016JBZ003).

References

1. Ren, J., Hu, J., Zhang, D., Guo, H., Zhang, Y., Shen, X.: RF energy harvesting and transfer in cognitive radio sensor networks: opportunities and challenges. *IEEE Commun. Mag.* **56**(1), 104–110 (2018)
2. Ahmed, M.E., Kim, D.I., Kim, J.Y., Shin, Y.: Energy-arrival-aware detection threshold in wireless-powered cognitive radio networks. *IEEE Trans. Veh. Technol.* **66**(10), 9201–9213 (2017)
3. Cheng, S., Cai, Z., Li, J., Gao, H.: Extracting kernel dataset from big sensory data in wireless sensor networks. *IEEE Trans. Knowl. Data Eng.* **29**(4), 813–827 (2017)
4. Li, J., Cheng, S., Li, Y., Cai, Z.: Approximate holistic aggregation in wireless sensor networks. In: *IEEE International Conference on Distributed Computing Systems*, p. 11 (2015)
5. Cheng, S., Cai, Z., Li, J., Fang, X.: Drawing dominant dataset from big sensory data in wireless sensor networks. In: *Computer Communications*, pp. 531–539 (2015)
6. Shi, T., Cheng, S., Cai, Z., Li, J.: Adaptive connected dominating set discovering algorithm in energy-harvest sensor networks. In: *IEEE INFOCOM 2016 - The IEEE International Conference on Computer Communications*, pp. 1–9 (2016)

7. Shi, T., Cheng, S., Cai, Z., Li, Y., Li, J.: Exploring connected dominating sets in energy harvest networks. *IEEE/ACM Trans. Netw.* **25**(3), 1803–1817 (2017)
8. Yin, S., Qu, Z., Li, S.: Achievable throughput optimization in energy harvesting cognitive radio systems. *IEEE J. Sel. Areas Commun.* **33**(3), 407–422 (2015)
9. Hu, C., Li, H., Huo, Y., Xiang, T., Liao, X.: Secure and efficient data communication protocol for wireless body area networks. *IEEE Trans. Multi-Scale Comput. Syst.* **2**(2), 94–107 (2016)
10. Zhang, F., Jing, T., Huo, Y., Jiang, K.: Outage probability minimization for energy harvesting cognitive radio sensor networks. *Sensors* **17**(2), 224 (2017)
11. Hu, C., Li, R., Mei, B., Li, W., Alrawais, A., Bie, R.: Privacy-preserving combinatorial auction without an auctioneer. *EURASIP J. Wirel. Commun. Netw.* **2018**(1), 38 (2018)
12. Yun, H.B., Baek, J.W.: Achievable throughput analysis of opportunistic spectrum access in cognitive radio networks with energy harvesting. *IEEE Trans. Commun.* **64**(4), 1399–1410 (2016)
13. Yadav, R., Singh, K., Gupta, A., Kumar, A.: Optimal energy-efficient resource allocation in energy harvesting cognitive radio networks with spectrum sensing. In: *Vehicular Technology Conference*, pp. 1–5 (2017)
14. Xu, B., Chen, Y., Carrin, J.R., Zhang, T.: Resource allocation in energy-cooperation enabled two-tier NOMA hetnets toward green 5G. *IEEE J. Sel. Areas Commun.* **35**(12), 2758–2770 (2017)
15. Zhang, R., Chen, H., Yeoh, P.L., Li, Y., Vucetic, B.: Full-duplex cooperative cognitive radio networks with wireless energy harvesting. In: *IEEE International Conference on Communications* (2017)
16. Ozcan, G., Gursoy, M.C., Tang, J.: Spectral and energy efficiency in cognitive radio systems with unslotted primary users and sensing uncertainty. *IEEE Trans. Commun.* **65**(10), 4138–4151 (2017)
17. Ozcan, G., Gursoy, M.C., Tang, J.: Power control for cognitive radio systems with unslotted primary users under sensing uncertainty. In: *IEEE International Conference on Communications*, pp. 1428–1433 (2015)
18. Zhang, F., Jing, T., Huo, Y., Jiang, K.: Throughput optimization for energy harvesting cognitive radio networks with save-then-transmit protocol. *Comput. J.* **60**(6), 911–924 (2017)
19. Messina, A.: Power and transmission duration control in un-slotted cognitive radio networks. In: *Computer Applications and Information Systems*, pp. 1–6 (2014)
20. Pratibha, P., Li, K.H., Teh, K.C.: Optimal spectrum access and energy supply for cognitive radio systems with opportunistic RF energy harvesting. *IEEE Trans. Veh. Technol.* **66**(8), 7114–7122 (2017)
21. Che, Y.L., Duan, L., Zhang, R.: Spatial throughput maximization of wireless powered communication networks. *IEEE J. Sel. Areas Commun.* **33**(8), 1534–1548 (2014)
22. Luo, S., Rui, Z., Teng, J.L.: Optimal save-then-transmit protocol for energy harvesting wireless transmitters. *IEEE Trans. Wirel. Commun.* **12**(3), 1196–1207 (2013)
23. Mehanna, O., Sultan, A.: Inter-sensing time optimization in cognitive radio networks. *Comput. Sci.* **72**, 5533 (2010)
24. Yin, S., Zhang, E., Yin, L., Li, S.: Saving-sensing-throughput tradeoff in cognitive radio systems with wireless energy harvesting. In: *2013 IEEE Global Communications Conference (GLOBECOM)*, pp. 1032–1037, December 2013
25. Park, S., Kim, H., Hong, D.: Cognitive radio networks with energy harvesting. *IEEE Trans. Wirel. Commun.* **12**(3), 1386–1397 (2013)