N-way Decomposition: Towards Linking Concurrent EEG and fMRI Analysis During Natural Stimulus

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Abstract. The human brain is intrinsically a high-dimensional and multi-variant system. Simultaneous EEG and fMRI recoding offers a powerful tool to examine the electrical activity of neuron populations at high temporal and frequency resolution, and concurrent blood oxygen level dependent (BOLD) responses at high spatial resolution. Joint analysis of EEG and fMRI data could thus help comprehensively understand the brain function at multiple scales. Such analysis, however, is challenging due to the limited knowledge on the coupling principle of neuronal-electrical and hemodynamic responses. A rich body of works have been done to model EEG-fMRI data during event related design and resting state, while few have explored concurrent data during natural stimulus due to the complexity of both stimulus and response. In this paper, we propose a novel method based on N-way decomposition to jointly analyze simultaneous EEG and fMRI data during natural movie viewing. Briefly, a 4-way tensor from the EEG data, constructed in four dimensions of time, frequency, channel and subject, is decomposed into group-wise rank one components by canonical polyadic decom‐ position (CPD). We then used the decomposed temporal features to constrain a 2-way sparse decomposition of fMRI data for network detection. Our results showed that the proposed method could effectively decode meaningful brain activity from both modalities and link EEG multi-way features with fMRI func‐ tional networks.

Keywords: Simultaneous · EEG · fMRI · Natural stimulus · Joint analysis · Canonical polyadic decomposition · Sparse decomposition

1 Introduction

The human brain is a complex system that involves massive electrical and metabolic processes, which is high-dimensional and multi-variant [\[1\]](#page-7-0). We now could record brain signals using EEG and fMRI simultaneously, which opened a new window to model the brain processes across multiple dimensions [\[2](#page-7-0)]. EEG records the massive neuronalelectrical activities that are reflected on the scalp, the high sampling rate of which enables the multi-way time-frequency-space feature extraction [\[2–4](#page-7-0)]. In contrast, the fMRI imaging captures the hemodynamic response of brain with low temporal resolution but high spatial resolution, which could be modeled as functional networks on brain structures [[1–4\]](#page-7-0). The neuronal-electrical activities are believed to couple with blood oxygen

level changes [[2\]](#page-7-0), so joint analysis of both modalities could link the two processes, provide comprehensive understanding of brain function, and benefit decoding the path‐ ology of some neurology diseases, like epilepsy.

However, joint modeling of EEG and fMRI data is challenging because even though the two modalities are derived from the same brain activity, the coupling principle of them is poorly understood [\[2–4](#page-7-0)]. While many studies have developed joint analytical strategies for event-related design and resting state paradigm [[4\]](#page-7-0), few methods have been reported for analyzing simultaneous EEG and fMRI data during natural stimulus [\[5](#page-7-0)]. In recent years, the use of natural stimuli becomes increasingly popular in neuroscience research [\[4](#page-7-0), [5](#page-7-0)], therefore, methodological innovation is urgently needed in this field to fuse EEG and fMRI activity during such complexity of stimulus and response.

In this paper, we proposed a novel approach based on N-way decomposition towards linking concurrent EEG and fMRI data analysis. Our method includes 4-way canonical polyadic decomposition (CPD) [[6\]](#page-7-0) on EEG data and 2-way sparse decomposition [\[7](#page-7-0)] on fMRI data. The EEG data was first transformed into time-frequency domain [[8\]](#page-7-0). Considering electrode channel and subject as two additional dimensions, we organize the group-wise EEG data as a 4D tensor. Using the 4-way CPD, the tensor is decomposed into numbers of rank one components [[6\]](#page-7-0) which have features of time, frequency, channel topology and subject contribution. Then the temporal features convolved by hemodynamic function (HRF) serve as explanatory variables for the 2-way sparse decomposition of fMRI data, which reconstructs functional networks. Since the two decomposition share the same temporal feature, the EEG frequency and spatial topology features are associated with fMRI networks. Our method was applied to a continuous movie watching dataset, and meaningful features are linked between EEG and fMRI.

2 Materials and Method

2.1 Overview

The framework of the proposed method is summarized in Fig. [1](#page-2-0). The whole method includes 4-way CPD decomposition on EEG data and 2-way sparse decomposition on the fMRI data. First, the EEG data from each subject was transformed into the timefrequency domain (*t* and *f*), and the spatial topology of the channels are preserved in the dimension "*c*" as shown in Fig. [1](#page-2-0)a. Since the data records the responses of multiple subjects to the same movie, we assume the fourth dimension "*s*" to account for the similarity and variability of subjects. The 4D tensor was decomposed into *R* rank one components (Fig. [1b](#page-2-0)), or four factor matrices (Fig. [1c](#page-2-0)). We call them *R* components from the EEG data. Each component includes four factors $-t_i$, c_i , f_i and s_i , which show features in different domains and are associated with each other. For example, in Fig. [1h](#page-2-0) and i, each topological distribution is associated with one frequency power spectrum density (PSD) histogram. The most important factor is the temporal one, as it serves as a bridge to link the fMRI data. The signals in the *T* matrix of Fig. [1](#page-2-0)c was convolved with HRF and become *E* matrix, which constructs the explanatory variables to model fMRI networks. In Fig. [1](#page-2-0)d, the whole brain signals of each subject are organized into a 2D matrix Y_i , which was further decomposed by the E matrix with sparse constraint and a

corresponding coefficient matrix A_i is optimized. By repeating the decomposition for each subject and performing T-test on the coefficient matrices across subjects, we reconstruct functional networks at the group level (Fig. 1e and g). As these networks are modeled based on the *T* factor from EEG data, they inherit the association with the EEG topological distribution and frequency PSD, therefore, our method effectively links EEG features and fMRI networks.

Fig. 1. The frame work of the proposed N-way decomposition method. The whole framework includes a 4-way CPD on EEG data and a 2-way sparse decomposition on fMRI data.

2.2 Data Acquisition and Preprocessing

Twenty right-handed volunteers (mean age 27 ± 2.7) were recruited from University of Queensland. The study was approved by human ethics research committee of the University, in which simultaneous EEG and fMRI data was acquired during resting state (8 min) and passive viewing of a movie named "The Butterfly Circus" (20 min).

Functional MRI images were acquired from a 3T Siemens Trio scanner equipped with a 12-channel head coil. The acquisition parameters are: $TR = 2200$ ms, $TE = 30$ ms, $FA = 79^{\circ}$, FOV of 134 \times 134 mm, 64 \times 64 acquisition matrix, 44 axial slices, and $3 \times 3 \times 3$ mm³ voxel resolution. fMRI data was preprocessed using SPM12 ([http://](http://www.fil.ion.ucl.ac.uk/spm/) www.fil.ion.ucl.ac.uk/spm/), which include slice-timing and motion correction, temporal filtering (0.0085–0.15 Hz), spatial smoothing and registration to MNI space.

The EEG data were acquired using an MR-compatible EEG system (BrainProducts, Germany) with 64 scalp channels positioned according to the international 10–20 system. The signals were recorded at a sampling rate of 5000 Hz, and filtered online via a low-pass hardware filter at 250 Hz. The BrainProducts SyncBox ensured the EEG system were synchronized precisely to the MRI system. The EEG data was preprocessed using the EEGLAB toolbox [[8\]](#page-7-0) and the preprocessing include gradientswitching artifacts correction, head motion removal, band-pass filtering (0.5–45 Hz), down sampling to 500 Hz, ballistocardiogram artifacts and eye movement artifacts removal [\[8](#page-7-0)].

2.3 EEG Time-Frequency Transformation

Dynamic power spectrum density from the EEG data was calculated during the whole movie watching in the following way. First, the preprocessed EEG signals were divided into time windows with the length of TR $(2.2 s)$ in fMRI. The EEG signals was normalized to zero mean and standard deviation of 1 in each window on each electrode. The power spectrum density (PSD) was estimated in each time window by Welch's method [\[9](#page-7-0)] with the frequency resolution of 1 Hz. Inter-subject consistency analysis was performed on the PSD time series for each frequency interval and each electrode channel. The inter-subject consistency of the time-frequency decomposition provides a basis for the tensor decomposition, which will be discussed in Sect. [3.1](#page-4-0).

2.4 Four-way Canonical Polyadic Decomposition on EEG

In Fig. [1](#page-2-0), the group-wise EEG time-frequency data is organized into a 4-way tensor, $X \in \mathbb{R}^{d_1 \times d_2 \times d_3 \times d_4}$. The CPD aims to decomposed *X* into *R* rank one components [[6\]](#page-7-0):

$$
X = \sum_{i=1}^{R} \lambda_i \cdot t_i \otimes f_i \otimes c_i \otimes s_i + e \tag{1}
$$

The operator *⊗* denotes outer product of vectors. In each component, there are four factors, i.e., t_i , f_i , c_i , and s_i correspondingly in time, frequency, channel and subject domain. Equation (1) could be rewritten into a tensor-matrix product form:

$$
X = I \times W \times T \times F \times C \times S + e = \hat{X} + e \tag{2}
$$

Where *I* is an identical tensor, $W = [\lambda_1, \lambda_2, \dots, \lambda_R] \in \mathbb{R}^{R \times 1}$ is a weight vector to balance the contribution of normalized rank one tensors [[6\]](#page-7-0). $T \in \mathbb{R}^{R \times d_1}$, $F \in \mathbb{R}^{R \times d_2}$, $C \in \mathbb{R}^{R \times d_3}$, and $S \in \mathbb{R}^{R \times d_4}$ are four factor matrices. The cost function is summarized as:

$$
f_1 = \min_{W,T,F,C,S} \frac{1}{2} ||X - CPD(W,T,F,C,S)||_F^2
$$
 (3)

The advantage of CPD comparing with other type of tensor decomposition is that the solution is unique $[6]$ $[6]$. In this work, we employ the Tensorlab toolbox [\(www.](http://www.tensorlab.net/) [tensorlab.net/](http://www.tensorlab.net/)) to estimate the CPD of EEG data. The toolbox provides various structure constraint for the CPD based on parametric transformations [\[6](#page-7-0)], and here regarding the characteristics of our data, we apply nonnegative constraint to matrix of *W*, *T*, *F*,*C*, *S*. In addition, to make the decomposed features more distinct, and to decompose fMRI data effectively, we apply the orthogonal constraint on the *T* matrix.

2.5 Two-way FMRI Sparse Decomposition and Statistics

The *T* matrix from Sect. 2.4 is composed of group-wise temporal features from the EEG data, which share the same time resolution with the fMRI data as illustrated in Sect. 2.3. To deal with the lag in the fMRI signal comparing with EEG electrical activity, we convolve the HRF $(h(t))$ to the signals in *T* to construct the explanatory variables *E*, which is used to decompose the fMRI signal matrices. Here, for the *i*-th signal: $E_i(t) = T_i(t) \star h(\tau)$, where " \star " denotes convolution.

The 2D fMRI signal matrix Y_i of each subject $(j = 1, 2...s)$ is then decomposed by *E*. A *L1* sparse penalty is introduced in the optimization to avoid overfitting and improve the feature selection. So, the final function to optimize is:

$$
f_2 = \min_{A_j} \frac{1}{2} \| Y_j - A_j E \|_F^2 + \gamma \| A_j \|_1
$$
 (4)

This sparse coding problem [[7\]](#page-7-0) can be solved by using the SPAMS toolbox [[7\]](#page-7-0). Coefficient matrix A_j is then optimized for each subject, $j = 1, 2...$ (*j*: subject ID). Two tailed t-test was applied on A_i across subjects, which derive R functional networks with group significance. Null hypothesis was rejected with p value threshold of 0.05.

2.6 Feature Selection

So far, we have linked multi-way features from EEG data and fMRI data, i.e., association is built up among components in the domains of time, frequency, scalp topology and fMRI networks. However, there are various sources of noises in both EEG and fMRI data, therefore, not all the components from our analysis are meaningful. Thus, feature selection is essential. We used the following steps to eliminate artifact or noise components: (1) We performed non-zero hypothesis test for the subject factor matrix *S* from EEG, and the components without significant non-zero mean were removed; (2) The components whose time course in the *T* matrix with abnormal fluctuation, like with one single peak in ten times intensity were removed; (3) Components with no significant fMRI networks were removed; (4) Components were removed if topological distribution was not smooth. These four steps combined thus selected meaningful results.

3 Results

3.1 Inter-subject Consistency Analysis for EEG Time-Frequency Data

The CPD decomposition is usually based on low rank assumption, i.e., there are a lot of repeated information in the data [\[6\]](#page-7-0). To test this low-rank assumption across subjects, we examined inter-subject consistency in the EEG data. Here we employed Cronbach's α [[10\]](#page-7-0) as a measurement of consistency. In our experiment, the raw EEG signals during natural stimulus show surprisingly low inter-subject consistency. Only after trans‐ forming the data into time-frequency domain, we found significant consistency amongst many electrodes and frequency bands (Alpah: 7–14 Hz, Beta: 16–28 Hz and Gamma: 29–40 Hz) during natural stimulus as shown in Fig. [2](#page-5-0)b. As a comparison, inter-subject consistency from resting state activity is very low (Fig. [2](#page-5-0)a). Therefore, it's feasible to apply 4-way CPD to the time-frequency EEG data during natural stimulus.

Fig. 2. Inter-subject Consistency of spectral time courses on electrode channels during resting state (a) and natural stimulus (b). X-axis: electrode channels. Y-axis: frequency bands.

3.2 The Linked EEG Components and FMRI Networks

Our proposed method and feature selection steps in Sect. [2](#page-1-0) were able to decode and associate meaningful EEG components and fMRI networks, as shown in Figs. 3, [4](#page-6-0), [5](#page-6-0) and [6.](#page-6-0) According to the pattern of the fMRI networks, we categorized the components into visual components (Fig. 3), auditory components (Fig. [4\)](#page-6-0), attention components (Fig. [5\)](#page-6-0) and others with interaction of multiple networks (Fig. [6](#page-6-0)). Interestingly, the EEG components within category show similar topology of electrode spatial patterns (Figs. 3a, [4a](#page-6-0), [5a](#page-6-0) and [6a](#page-6-0)). As shown in Figs. 3b, [4b](#page-6-0), [5](#page-6-0)b and [6b](#page-6-0), these components are primarily related to Alpha band activity, and a few of them involve Beta band activity (C7–C9). The predominant presence of Alpha band reflects its roles in the attention and sensory processing $[11]$ $[11]$, and evidently multiple sensory systems (visual & auditory) could possibly invoke Alpha oscillation [[11\]](#page-7-0).

Fig. 3. The visual components. (a) Scalp topology. (b) Frequency PSD. (c) fMRI network. (d) fMRI network mapped on white matter surface.

Fig. 4. The auditory components. (a) Scalp topology. (b) Frequency PSD. (c) fMRI network. (d) fMRI network mapped on white matter surface.

Fig. 5. The attention related components. (a) Scalp topology. (b) Frequency PSD. (c) fMRI network. d) fMRI network mapped on white matter surface.

Fig. 6. Components with interactions of multiple network. (a) Scalp topology. (b) Frequency PSD. (c) fMRI network. (d) fMRI network mapped on white matter surface.

It's interesting that in C1–C4 (Fig. [3](#page-5-0)) different parts of visual cortex are associated with low, middle and high Alpha frequencies. Meanwhile, auditory networks in C5 and C6 (Fig. [2\)](#page-5-0) are more associated with low Alpha frequencies. The attention networks in Fig. [3](#page-5-0) focused in Alpha band but also involve certain level of Beta oscillation, which could be related to the role of Beta band in emotional and cognitive processes [12]. The networks from fMRI in Fig. [6](#page-6-0) involve multiple networks, e.g. C10 with visual and auditory networks; C11 with auditory and attention networks; C12 with visual, auditory and attention networks. These components show evidence of interaction among visual, auditory and attention networks (Fig. [6](#page-6-0)) during natural stimulus. We didn't find Gamma components with our method even though we see high inter-subject consistency in Fig. [2,](#page-5-0) possibly because of huge variability in Gamma activities. Note that, based on two tailed t-test activations in the fMRI networks were not further categorized as positive or negative, but treated as equally important in this work.

4 Discussion

In this paper, we proposed a joint analyzing method for concurrent EEG and fMRI data based on N-way decomposition. Experiment results have shown that our method could detect meaningful EEG components associated with fMRI networks. This work could open a new window to link two data modalities and provide a comprehensive way to understand brain function during natural stimulus. Future efforts will be devoted to further interpret the associated EEG components and fMRI networks.

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