

Self-similarity Traffic and AQM Mechanism Based on Non-integer Order $PI^\alpha D^\beta$ Controller

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Abstract. In this paper the performance of fractional order PID controller as AQM mechanism and impact of traffic self-similarity on network utilization are investigated with the use of discrete event simulation models. The researches show the influence of selection of PID parameters and degree of traffic self-similarity on queue behavior. During the tests we analyzed the length of the queue, the number of rejected packets and waiting times in queues. In particular, the paper uses fractional Gaussian noise as a self-similar traffic source. The quantitative analysis is based on simulation.

1 Introduction

Most AQM mechanism proposed by IETF to control the network congestions are based on preventive packet dropping. For the most known active mechanism the number of discarded packets grows with the increase in queue occupancy. The basic active queue management algorithm is Random Early Detection (RED) algorithm. It was primarily proposed in 1993 by Sally Floyd and Van Jacobson [1]. Since that time a number of studies how to improve the basic algorithm have been proposed. We have also proposed and evaluated a few variants, [2–7].

In 2001 the use of the PI controller as AQM mechanism was proposed by C.V. Hollot, V. Misra and D. Towsley [8]. Based on the first implementation, a number of PI controllers have been proposed later [9–11].

In recent years the fractional order calculus becomes very popular. The articles [12–14] show that non-integer order controllers may have better performance than classic integer order. The first application of the fractional order PI controller as a AQM policy in fluid flow model of a TCP connection was presented in [15]. The detailed influence of fractional order PI controller on queue behavior was presented in article [16].

Measurements and statistical analysis (performed already in the 90s) of packet network traffic show that this traffic displays a complex statistical nature.

It is related to such statistic phenomena as self-similarity, long-range dependence and burstiness [17–20].

Self-similarity of a process means that the change of time scales does not influence the statistical characteristics of the process. It results in long-distance autocorrelation and makes possible the occurrence of very long periods of high (or low) traffic intensity. These features have a great impact on a network performance [21]. They enlarge the mean queue lengths at buffers and increase the probability of packet losses, reducing this way the quality of services provided by a network [22].

As a consequence of this fact, it is needed to propose new or to adapt known types of stochastic processes when modeling these negative phenomena in network traffic. Several models have been introduced for the purposes of modeling self-similar processes in the network traffic area. These models of traffic use fractional Brownian Motion [23], chaotic maps [24], fractional Autoregressive Integrated Moving Average (fARIMA) [25], wavelets and multifractals and processes based on Markov chains: SSMP (Special Semi-Markov Process) [26], MMPP (Markov-Modulated Poisson Process) [27, 28], HMM (Hidden Markov Model) [29].

The main purpose of the paper is to present simulation results for the AQM mechanism in which fractional discrete calculus is used. Section 2 presents theoretical bases for $PI^\alpha D^\beta$ controller next used in simulation. Section 3 briefly describes a self-similar traffic used in this article and presents the obtained results.

2 An AQM Mechanism Based on $PI^\alpha D^\beta$ Controller

A proportional-integral-derivative controller (PID controller) is a traditional mechanism used in feedback control systems. The article [12] indicates that the introduction non-integer controllers may improve closed loop control quality. Therefore here we propose to use the $PI^\alpha D^\beta$ (PID controller with non integer integral and derivative order) instead of the RED mechanism to determine the probability of packet drop. Equation (1) is based on our proposition discussed in [16] for PI^α controller and extended here to the case of $PI^\alpha D^\beta$.

This probability is calculated in the following way:

$$p = \max\{0, -(K_P e_k + K_I \Delta^\alpha e_k + K_D \Delta^\beta e_k)\} \quad (1)$$

where K_P, K_I, K_D are tuning parameters, e_k is the error in current slot $e_k = q - q_d$, q - actual queue size, q_d - desired queue size and $\Delta^\alpha e_k$ is defined as follows:

$$\Delta^\alpha e_k = \sum_{j=0}^k (-1)^j \binom{\alpha}{j} e_{k-1} \quad (2)$$

where $\alpha \in R$ is generally a not-integer fractional order, e_k is a differentiated discrete function and generalized Newton symbol $\binom{\alpha}{j}$ is defined as follows:

$$\binom{\alpha}{j} = \begin{cases} 1 & \text{for } j = 0 \\ \frac{\alpha(\alpha - 1)(\alpha - 2)\dots(\alpha - j + 1)}{j!} & \text{for } j = 1, 2, \dots \end{cases} \quad (3)$$

This definition unifies the definition of derivative and integral to one differintegral definition. We have the fractional integral of the considered function e_k for $\alpha < 0$. If the parameter α is positive, we obtain in the same way a fractional derivative and, to distinguish, we denote this parameter as β . If $\alpha = 0$ the operation (2) does not influence the function e_k .

Figure 1 presents a comparison of the increase of packet dropping probability in PI^α and PD^β controllers as a function of the queue length increased due to arrivals of packets. Naturally, the response depends on the choice of parameters. As can be seen, the integral order affects the time of controller reaction (below a certain threshold there is no packet dropping). The derivative order influences on increases packet dropping probability.

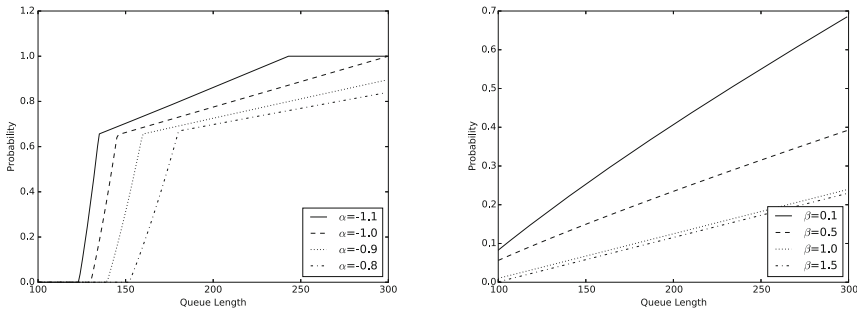


Fig. 1. Packet dropping probability in PI^α controller (the influence of the integral order α , $K_P = 0.00115$, $K_I = 0.0011$) (left), and in PD^β controller (the influence of the derivative order β , $K_P = 0.00115$, $K_D = 0.01$) (right)

3 $PI^\alpha D^\beta$ Controller Under Self-similar Traffic

In this article we use fractional Gaussian noise as an example of exactly self-similar traffic source. Fractional Gaussian noise (fGn) has been proposed as a model [30] for the long-range dependence postulated to occur in a variety of hydrological and geophysical time series. Nowadays, fGn is one of the most commonly used self-similar processes in network performance evaluation. The fGn process is the stationary Gaussian process that is exactly self-similar [31]. The Hurst parameter H characterizes a process in terms of the degree of self-similarity. The degree of self-similarity increases with the increase of H [32]. A Hurst value smaller or equal to 0.5 means the lack of long range dependence.

We use a fast algorithm for generating approximate sample paths for a fGn process, introduced in [33]. We have generated the sample traces with the Hurst parameter with the range of 0.5 to 0.90. After each trace generation, the Hurst parameter was estimated. The simulations were done using the Simpy Python simulation packet.

During the tests we analyzed the following parameters of the transmission with AQM: the length of the queue, queue waiting times and the number of rejected packets. The service time represented the time of a packet treatment and dispatching. Considered input traffic intensities were $\lambda = 0.5$, independently of Hurst parameter. The distribution of service time was also geometric. Its parameter changed during the test. The high traffic load was considered for parameter $\mu = 0.25$. The average traffic load we obtained for $\mu = 0.5$. A small network traffic was considered for parameter $\mu = 0.75$.

Table 1. FIFO queue

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	0.50	299.099	119.380	249520	49.90%
0.25	0.70	298.118	119.158	249879	49.97%
0.25	0.80	296.878	118.883	250354	50.07%
0.25	0.90	248.553	102.061	256587	51.32%
0.50	0.50	163.7547	32.7147	889	0.17%
0.50	0.70	145.8734	29.8820	13342	2.66%
0.50	0.80	141.3440	29.5832	23828	4.76%
0.50	0.90	133.8558	32.5300	89659	17.93%
0.75	0.50	1.2930	0.1586	0	
0.75	0.70	3.0506	0.5101	0	
0.75	0.80	6.9882	1.2976	0	
0.75	0.90	55.9574	11.5942	21484	4.29%

In order to better demonstrate the influence of degree of selfsimilarity on queue behavior first experiment focused on the FIFO queue. The Fig. 2 presents the distribution of the queue length. This figure clearly shows dependence of the queue occupancy on the degree of traffic selfsimilarity. The figure shows three situations: most overloaded network node ($\rho = \frac{\lambda}{\mu} = 2$), medium overloaded situation ($\rho = 1$) and almost empty buffer for ($\rho = \frac{2}{3}$). The detailed results obtained during the simulation present Table 1. For overloaded buffer ($\mu = 0.25$ and $\mu = 0.50$) the number of dropped packets increased with the traffic degree of selfsimilarity increasing. This effect becomes more evident with congestion decrease. In the case of an unloaded buffer ($\mu = 0.75$) packet loss occur only in the case of traffic with a high degree of selfsimilarity (Hurst parameter $H = 0.9$).

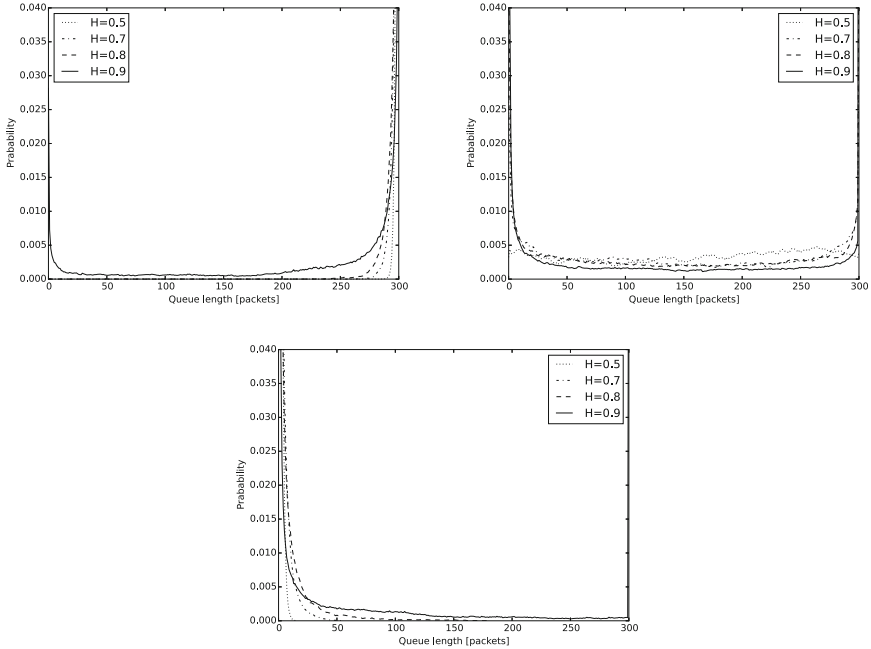


Fig. 2. The influence of degree of traffic selfsimilarity on queue distribution, FIFO queue, queue size = 300, $\lambda = 0.5$, $\mu = 0.25$ (left), $\mu = 0.5$ (right), $\mu = 0.75$ (bottom)

The presented results show how models that do not consider self-similar traffic may underestimate the queues occupancy and packet lost in routers.

In a first phase of the research we consider the influence of the PI^α controller on queue behavior. During the simulation the controller parameters were set as follows: $K_P = 0.00115$, $K_I = 0.0011$. The integral orders α changed and I received the following values: $-0.8, -1.0$ and -1.2 . For the integral orders $\alpha = -1$ the controller becomes standard PI control loop feedback mechanism. The Tables 2, 3 and 4 present the obtained results. The queues distribution are presented in Figs. 3 and 4 (the queue distribution for controller with parameter $\alpha = 0.8$ is similar to distribution shown in Fig. 3). The controller desired point was set at 100 packet. It should be noted that regardless of the integral order the controller behaved properly.

These studies showed a very interesting controller behavior. In the case of overloaded FIFO queue for traffic of the high degree of self-similarity ($H = 0.9$) compared to less self-similar traffic the mean queue length decreases rapidly (see Table 1). This phenomenon also occurs in the case of standard AQM mechanisms [34]. In the case of PI^α occurrence of this phenomenon depends on the integral term and becomes less noticeable with the decrease in α . Comparing the mean queue length for $H = 0.9$ and $H = 0.8$ can be stated that for $\alpha = -1.2$ the mean queue length decreases by 19% for $\rho = 2$ and decreases by 3% for $\rho = 1$. For $\alpha = -1.0$ the mean queue length decreases by 8% for $\rho = 2$ and decreases

by 2% for $\rho = 1$. Whereas for $\alpha = -0.8$ the mean queue length increases by 6% for $\rho = 2$ and increases by 2% for $\rho = 1$. On the other hand, the number of discarded packets analyze shows that for traffic with high degree of self-similarity ($H = 0.9$ and $H = 0.8$) with integral order growth decreases the number of dropped packets (for standard AQM queue, the situation is exactly opposite).

Interesting results were also obtained for the low traffic intensity. The mean queue length grows with integral order decreasing. The Fig. 1 explains these phenomena. The controller response to increasing queue in depends on the queue previous moments. The controller reaction is delayed with the integral order increasing.

Table 2. PI^α queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -0.8$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	050	105.2024	42.0998	250646	50.13%
0.25	070	112.1730	44.8029	250112	50.02%
0.25	080	118.2300	47.1973	249966	49.99%
0.25	090	126.4218	53.4780	263974	52.79%
0.50	050	53.8331	10.7526	3954	0.79%
0.50	070	55.8842	11.6289	23524	4.7%
0.50	080	52.0427	11.1830	38757	7.75%
0.50	090	54.3019	13.9019	112126	22.43%
0.75	050	1.2806	0.1561	0	
0.75	070	2.9819	0.4962	0	
0.75	080	6.6740	1.2359	440	0.08%
0.75	090	26.1258	5.4831	32047	6.40%

The second phase of the researches shows how derivative term changes the queue occupancy and packet waiting times. The Figs. 5, 6 and 7 present the queue distribution for PID^β controller ($\alpha = -1$). The results for PI controller were present in Fig. 3 and Table 3. Comparing the figures does not show a significant visual amendments. Differences in the controllers responses show Tables 5, 6 and 7.

The most interesting results were obtained for controller with derivative terms $\beta = 0.8$. For high traffic ($\mu = 0.25$ and $\mu = 0.5$) the controller reduces the mean queue length and at the same time reduces the number of packet losses. The further derivative order increasing (Tables 6 and 7) reduces the mean queue length and at the same time increases number of dropped packets. However, these differences are much smoother as in the case of integral order α decreasing (see Table 4).

The last phase of the simulation evaluates the impact of derivate term on PI^α controller. Controller with integral term $\alpha = -1.2$ is an example of strong mechanism. For this controller the lowest values of mean queue length and waiting

Table 3. PI^α queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	050	105.4769	42.0835	249914	49.98%
0.25	070	109.6279	43.6825	249538	49.90%
0.25	080	112.7636	45.0588	250246	50.04%
0.25	090	103.7300	43.9278	264321	52.86%
0.50	050	50.8356	10.1493	4024	0.80%
0.50	070	51.4054	10.6806	23202	4.64%
0.50	080	48.9152	10.5024	38644	7.72%
0.50	090	47.8680	12.2617	112735	22.54%
0.75	050	1.2892	0.1578	0	
0.75	070	3.0249	0.5047	0	
0.75	080	6.4268	1.1868	587	0.11%
0.75	090	25.3451	5.3177	32175	6.43%

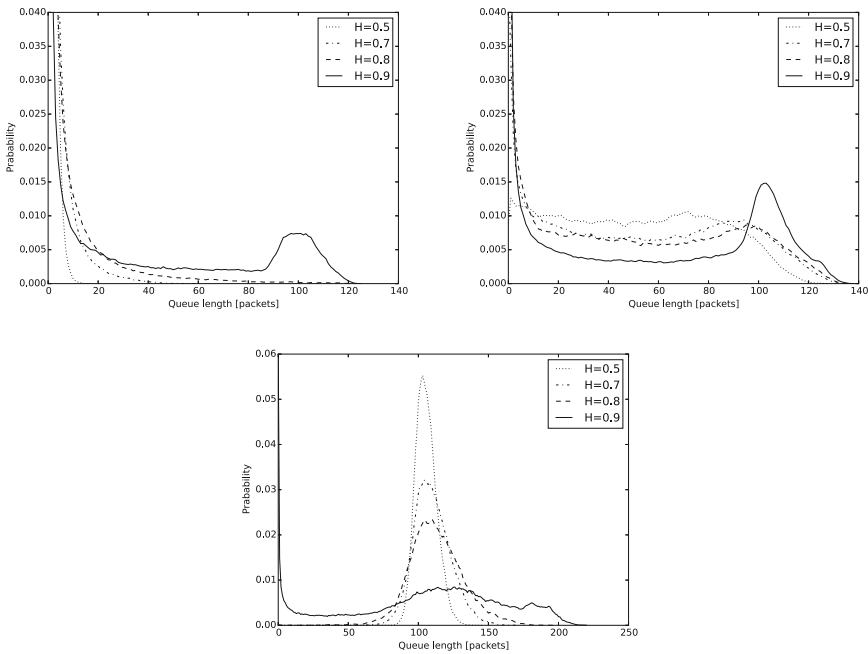


Fig. 3. The influence of degree of traffic selfsimilarity on queue distribution, PI^α queue, queue size = 300, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $\lambda = 0.5$, $\mu = 0.75$ (left), $\mu = 0.5$ (right), $\mu = 0.25$ (bottom)

Table 4. PI^α queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.2$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	050	102.9224	41.0802	250026	50.0%
0.25	070	103.0052	41.1281	250100	50.01%
0.25	080	102.2977	40.8632	250214	50.04%
0.25	090	81.8945	34.7584	265013	53.0 %
0.50	0.50	49.525675	9.8806	3789	0.75%
0.50	0.70	50.429557	10.4798	23351	4.67%
0.50	0.80	47.869046	10.2771	38708	7.74%
0.50	0.90	46.207823	11.8211	112356	22.47%
0.75	0.50	1.283052	0.1566	0	
0.75	0.70	3.016572	0.5031	0	
0.75	0.80	6.400407	1.1817	655	0.13%
0.75	0.90	24.920464	5.2269	32173	6.43%

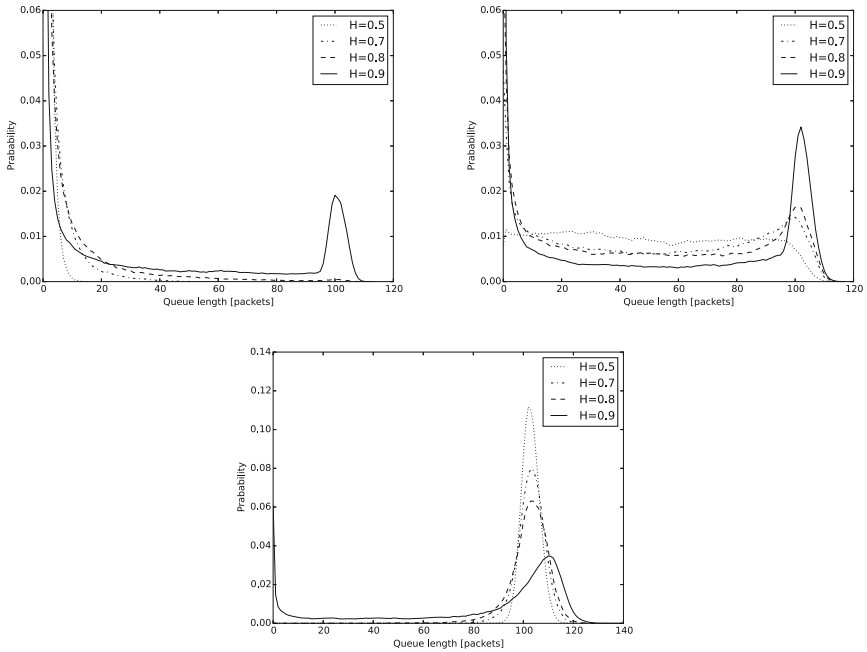


Fig. 4. The influence of degree of traffic selfsimilarity on queue distribution, PI^α queue, queue size = 300, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.2$, $\lambda = 0.5$, $\mu = 0.75$ (left), $\mu = 0.5$ (right), $\mu = 0.25$ (bottom)

Table 5. PID queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $K_D = 0.01$, $\beta = 0.8$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	0.50	105.2382	41.9506	249687	49.93%
0.25	0.70	109.0697	43.5297	249941	49.98%
0.25	0.80	111.5187	44.5991	250457	50.0%
0.25	0.90	102.2642	43.2207	263868	52.77%
0.50	0.50	52.9857	10.5912	4385	0.87%
0.50	0.70	51.2877	10.6640	23537	4.70%
0.50	0.80	49.3514	10.6034	38920	7.78%
0.50	0.90	47.5944	12.1854	112550	22.50%
0.75	0.50	1.2878	0.1575	0	
0.75	0.70	3.0133	0.5025	0	
0.75	0.80	6.3137	1.1643	0	
0.75	0.90	25.2454	5.2913	31734	6.34%

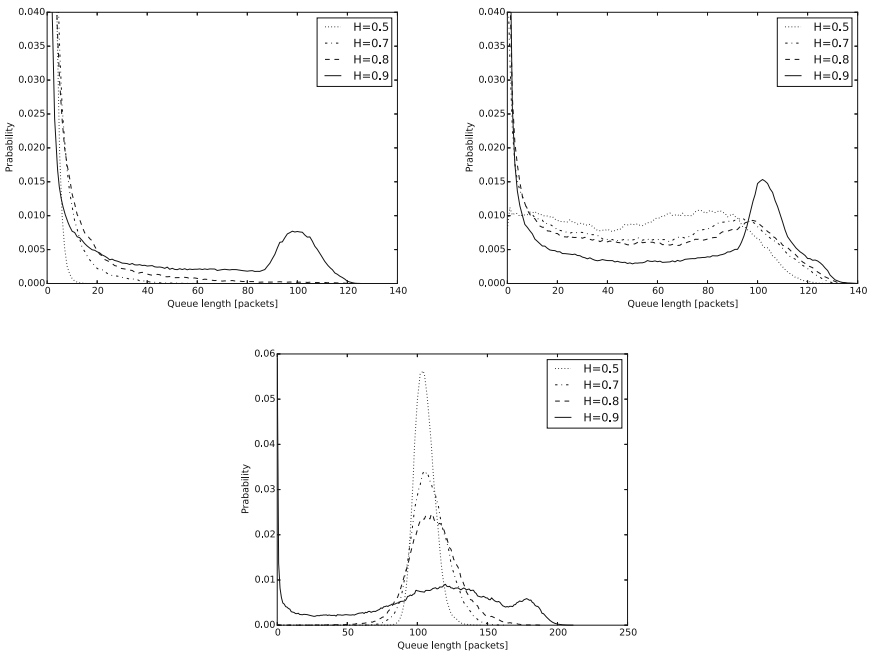


Fig. 5. The influence of degree of traffic selfsimilarity on queue distribution, $PI^\alpha D^\beta$ queue, queue size = 300, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $K_D = 0.01$, $\beta = 0.8$, $\lambda = 0.5$, $\mu = 0.75$ (left), $\mu = 0.5$ (right), $\mu = 0.25$ (bottom)

Table 6. PID queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $K_D = 0.01$, $\beta = 1.0$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	0.50	105.1122	41.9762	250138	50.02%
0.25	0.70	109.4128	43.4958	248962	49.79%
0.25	0.80	112.3291	44.8387	249994	49.99%
0.25	0.90	104.6598	44.3687	264588	52.91%
0.50	0.50	52.6690	10.5310	4544	0.90%
0.50	0.70	51.1150	10.6226	23324	4.66%
0.50	0.80	48.9330	10.5084	38738	7.74%
0.50	0.90	47.6431	12.1726	111753	22.35%
0.75	0.50	1.2823	0.1564	0	
0.75	0.70	2.9884	0.4975	0	
0.75	0.80	6.4988	1.2012	581	0.11%
0.75	0.90	25.2075	5.2839	31798	6.35%

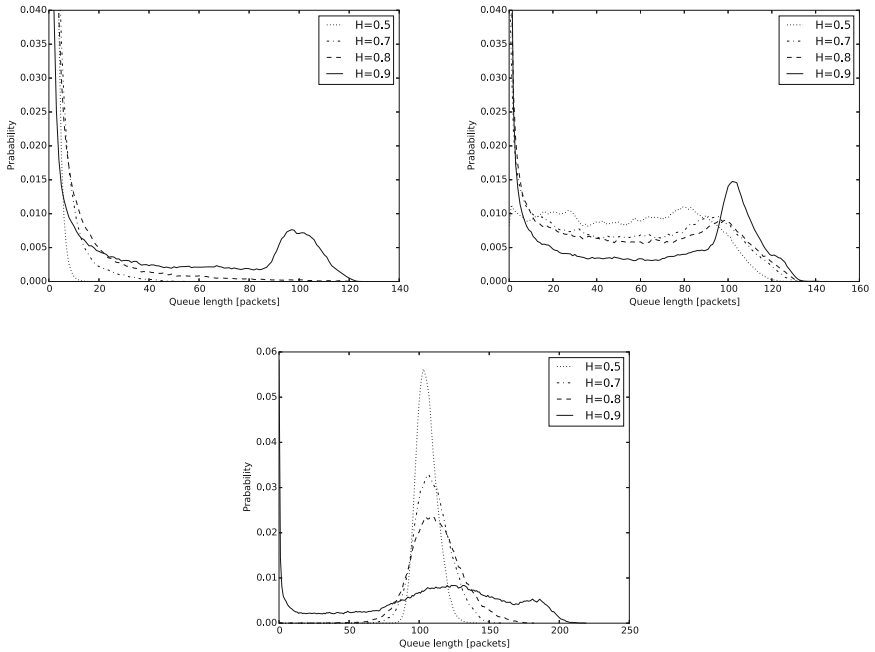


Fig. 6. The influence of degree of traffic selfsimilarity on queue distribution, $PI^\alpha D^\beta$ queue, queue size = 300, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $K_D = 0.01$, $\beta = 1.0$, $\lambda = 0.5$, $\mu = 0.75$ (left), $\mu = 0.5$ (right), $\mu = 0.25$ (bottom)

Table 7. PID queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $K_D = 0.01$, $\beta = 1.2$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets	
0.25	0.50	105.3953	42.0064	249638	49.92%
0.25	0.70	109.8195	43.8410	250000	50.00%
0.25	0.80	112.8646	44.9803	249592	49.91%
0.25	0.90	105.0905	44.5343	264473	52.89%
0.50	0.50	50.5028	10.0713	3482	0.69%
0.50	0.70	50.6084	10.5039	22747	4.54%
0.50	0.80	48.2802	10.3441	37731	7.54%
0.50	0.90	47.9325	12.2640	112284	22.45%
0.75	0.50	1.2882	0.1576	0	
0.75	0.70	3.0119	0.5022	0	
0.75	0.80	6.3877	1.1789	561	0.11%
0.75	0.90	25.1610	5.2733	31731	6.34%

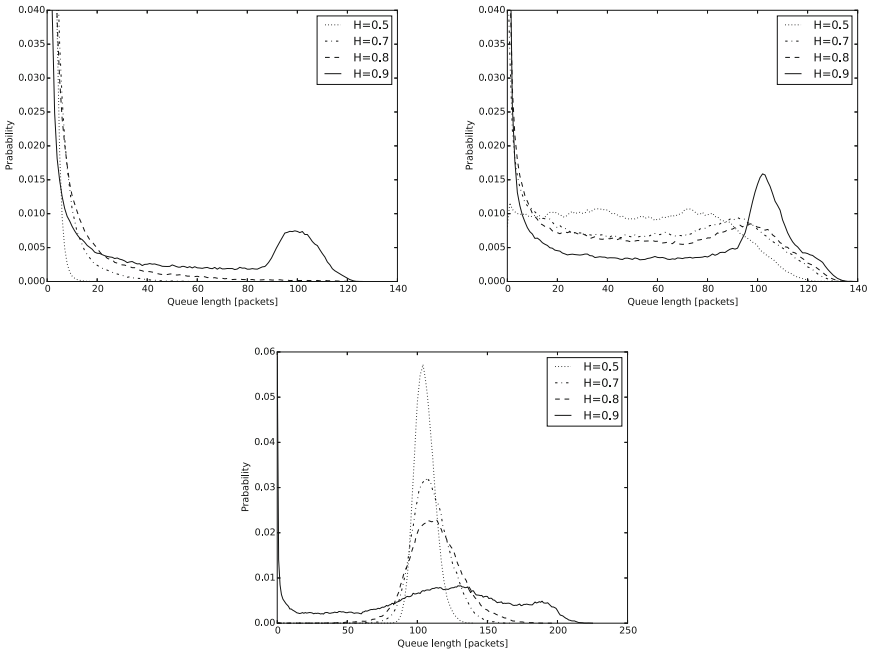


Fig. 7. The influence of degree of traffic selfsimilarity on queue distribution, $PI^\alpha D^\beta$ queue, queue size = 300, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.0$, $K_D = 0.01$, $\beta = 1.2$, $\lambda = 0.5$, $\mu = 0.75$ (left), $\mu = 0.5$ (right), $\mu = 0.25$ (bottom)

times were obtained. At the same time increase the number of dropped packets is insignificant. The results of the controller with derivative term and derivative order $\beta = 0.8$ are shown in Fig. 8. Table 8 presents the detailed results. In this case, the controller with derivative term response is softer.

Table 8. PID queue, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.2$, $K_D = 0.01$, $\beta = 0.8$

μ	Hurst parameter	Mean queue length	Mean waiting time	Rejected packets
0.25	0.50	102.8881	41.0135	249696 49.93%
0.25	0.70	102.9803	41.1081	250038 50.00%
0.25	0.80	102.2453	40.8194	250084 50.01%
0.25	0.90	81.9062	34.7162	264699 52.93%
0.50	0.50	52.6182	10.5227	4659 0.93%
0.50	0.70	49.8837	10.3693	23532 4.70%
0.50	0.80	48.0090	10.3122	38918 7.78%
0.50	0.90	46.0250	11.7805	112565 22.51%
0.75	0.50	1.2859	0.1571	0
0.75	0.70	3.0204	0.5039	0
0.75	0.80	6.5480	1.2112	610 0.12%
0.75	0.90	24.9491	5.2310	31991 6.39%

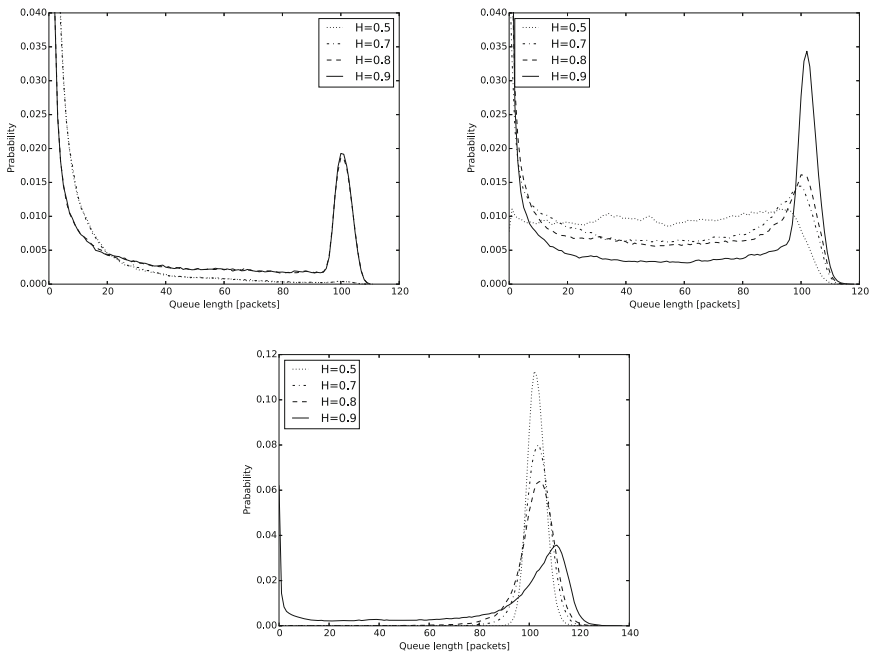


Fig. 8. The influence of degree of traffic selfsimilarity on queue distribution, $PI^\alpha D^\beta$ queue, queue size = 300, $K_P = 0.00115$, $K_I = 0.0011$, $\alpha = -1.2$, $K_D = 0.01$, $\beta = 0.8$, $\lambda = 0.5$, $\mu = 0.75$ (left), $\mu = 0.5$ (right), $\mu = 0.25$ (bottom)

4 Conclusions

Our article presents the impact of the degree of self-similarity (expressed in Hurst parameter) on the length of the queue, queue waiting times and the number of rejected packets. Obtained results are closely related to the degree of self-similarity. The experiments are carried out for the four types of traffic ($H = 0.5, 0.7, 0.8, 0.9$). During the test we also changed the parameter of distribution of service time. This change allowed us to consider the different queues loading.

The article presents an evaluation of the fractional order $PI^\alpha D^\beta$ controller used as an active queue management mechanism. The effectiveness of the controller as an AQM mechanism depends on proper parameters of the PID selection. In the case of fractional order controller we need to consider two additional parameters: fractional derivative (β) and integral (α) orders. The controllers behavior was also compared to FIFO queue.

The results showed the usefulness of the $PI^\alpha D^\beta$ controller as AQM mechanism. The proper selection of the controller parameters is important in adaptation to various types of traffic (degree of self-similarity or various intensity).

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