

# An Energy-Efficient Process Replication Algorithm in Virtual Machine Environments

Tomoya Enokido and Makoto Takizawa

**Abstract** Server cluster systems are widely used to realize fault-tolerant, scalable, and high performance application services with virtual machine technologies. In order to provide reliable application services, multiple replicas of each application process can be redundantly performed on multiple virtual machines. On the other hand, a server cluster system consumes a large amount of electric energy since multiple replicas of each application process are performed on multiple virtual machines. It is critical to discuss how to realize not only reliable but also energy-efficient server cluster systems. In this paper, we propose the redundant energy consumption laxity based (RECLB) algorithm to select multiple virtual machines for redundantly performing each application process in presence of server faults so that the total energy consumption of a server cluster and the average computation time of each process can be reduced. We evaluate the RECLB algorithm in terms of the total energy consumption of a server cluster and the average computation time of each process compared with the basic round-robin (RR) algorithm.

## 1 Introduction

Various types of business and industrial information services like data centers [10] require scalable, high performance, and fault-tolerant information systems like cloud computing systems [10]. These computing systems are realized virtual machines [5] with server cluster systems [2, 3, 4]. A server cluster system is composed

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of a large number of servers and multiple virtual machines are installed in each server in order to increase the resource utilization of servers. In fault-tolerant information systems, application processes which provide application services have to be reliably performed in presence of server faults [8]. One way to provide a fault-tolerant application service is that multiple replicas of each application process are performed on multiple virtual machines in a server cluster. However, a large amount of electric energy is consumed in a server cluster system since replicas of each application process are performed on multiple virtual machines which are performed on multiple servers. It is necessary to realize not only fault-tolerant but also energy efficient server cluster systems with virtual machines as discussed in Green computing [10].

In order to design energy-efficient server cluster systems [2, 3, 4], it is necessary to define a computation model and power consumption model of servers to perform application processes on virtual machines. In our previous studies [5], we measured power consumption of servers to perform *computation type application processes* (*computation processes*) which mainly consumes CPU resources of servers and derived the computation model of a virtual machine and power consumption model of a server to perform computation processes on multiple virtual machines from the experimentations. In this paper, we consider computation processes.

In this paper, we propose the *redundant energy consumption laxity based (RECLB)* algorithm to select multiple virtual machines for redundantly performing each application process in presence of server faults so that the total energy consumption of a server cluster and the average computation time of each process can be reduced. In this paper, we assume some servers in a server cluster might stop by fault. If a server stops by fault, every virtual machine performed on the server stops. Hence, replicas of each computation process have to be performed on multiple virtual machines which are performed on different servers in a server cluster. Here, if at least one virtual machine is operational, a computation process is successfully performed even if some servers stop by fault. In the RECLB algorithm, a set of multiple virtual machines where the total energy consumption laxity of a server cluster is the minimum is selected for redundantly performing multiple replicas of each computation process. We evaluate the RECLB algorithm in terms of the total energy consumption of a homogeneous server cluster and computation time of each request process compared with the basic round-robin (RR) algorithm [9]. The evaluation results show the total energy consumption of a homogeneous server cluster and computation time of each request process can be more reduced in the RECLB algorithm than the RR algorithm.

In section 2, we define the computation model of a virtual machine and power consumption model of a server. In section 3, we discuss the RECLB algorithm. In section 4, we evaluate the RECLB algorithm compared with the RR algorithm.

## 2 System Model

### 2.1 Computation Model of a Virtual Machine

Let  $S$  be a cluster of servers  $s_1, \dots, s_n$  ( $n \geq 1$ ). Let  $C_l$  be a set of cores  $c_{1l}, \dots, c_{ll}$  ( $l \geq 1$ ) and  $nc_l$  be the total number of cores in a server  $s_l$ . We assume Hyper-Threading Technology [7] is enabled on a CPU. Let  $TH_l$  be a set of threads  $th_{1l}, \dots, th_{ql}$  ( $q \geq 1$ ) in a server  $s_l$ . Let  $ct_l$  be the number of threads on each core  $c_{ht}$  in a server  $s_l$ . Threads  $th_{(h-1) \cdot ct_l + 1}, \dots, th_{h \cdot ct_l}$  ( $1 \leq h \leq l$ ) are bounded to a core  $c_{ht}$ . Let  $nt_l$  be the total total number of threads in a server  $s_l$ , i.e.  $nt_l = nc_l \cdot ct_l$ . Let  $V_l$  be a set of virtual machines  $VM_{1l}, \dots, VM_{ql}$  ( $q \geq 1$ ) in a server  $s_l$ . Each virtual machine  $VM_{kt}$  holds one virtual CPU and is bounded to a thread  $th_{kt}$  in a server  $s_t$ . In this paper, we assume any virtual machine does not migrate to another server in a server cluster  $S$ . A virtual machine  $VM_{kt}$  is referred to as *active* iff (if and only if) the virtual machine  $VM_{kt}$  is initiated on a thread  $th_{kt}$  and at least one process is performed on the virtual machine  $VM_{kt}$ . A virtual machine  $VM_{kt}$  is *idle* iff the virtual machine  $VM_{kt}$  is initiated on a thread  $th_{kt}$  but no process is performed on the virtual machine  $VM_{kt}$ . A virtual machine is *stopped* iff the virtual machine is not initiated on any thread. A core  $c_{ht}$  is referred to as *active* iff at least one virtual machine  $VM_{kt}$  is active on a thread  $th_{kt}$  in the core  $c_{ht}$ . A core  $c_{ht}$  is *idle* if the core  $c_{ht}$  is not active.

We consider *computation processes*, where CPU resources are mainly consumed. A term *process* stands for a computation process in this paper. Let  $rd^i$  be the *redundancy* of a process  $p^i$ . A notation  $p_{kt}^i$  stands for a *replica* of a process  $p^i$  performed on a virtual machine  $VM_{kt}$ . On receipt of a process  $p^i$ , the load balancer  $K$  selects a set  $VMS^i$  ( $|VMS^i| = rd^i$ ) of virtual machines in the server cluster  $S$  and forwards the process  $p^i$  to every virtual machines  $VM_{kt}$  in the set  $VMS^i$  as shown in Figure 1. We assume servers in a server cluster  $S$  might stop by fault. Let  $NF$  be the maximum number of servers which concurrently stop by fault in the cluster  $S$ . If a server  $s_t$  stops by fault, every virtual machine  $VM_{kt}$  performed on the server  $s_t$  stops. Hence, replicas of each process  $p^i$  have to be performed on  $rd^i$  virtual machines performed on different servers in a server cluster  $S$ . We assume  $NF + 1 \leq rd^i \leq n$  and replicas of each process  $p^i$  are performed on  $rd^i$  virtual machines performed on different servers. This means, each client  $cl^i$  can receive at least one reply  $r_{kt}^i$  from a virtual machine  $VM_{kt}$  even if  $NF$  servers stop by fault in a server cluster  $S$ . On receipt of a process  $p^i$ , a replica  $p_{kt}^i$  is created and performed on a virtual machine  $VM_{kt}$ . Then, the virtual machine  $VM_{kt}$  sends a reply  $r_{kt}^i$  to the load balancer  $K$ . The load balancer  $K$  takes only the first reply  $r_{kt}^i$  and ignores every other reply.

Replicas which are being performed and already terminate at time  $\tau$  are *current* and *previous*, respectively. Let  $CP_{kt}(\tau)$  be a set of current replicas on a virtual machine  $VM_{kt}$  at time  $\tau$  and  $NC_{kt}(\tau)$  be  $|CP_{kt}(\tau)|$ . Let  $T_{kt}^i$  be the total computation time of a replica  $p_{kt}^i$  [msec].  $\min T_{kt}^i$  shows the minimum computation time of a replica  $p_{kt}^i$  where the replica  $p_{kt}^i$  is exclusively performed on a virtual machine  $VM_{kt}$  and the other virtual machines are not active in a server  $s_t$ . We assume  $\min T_{1t}^i = \min T_{2t}^i = \dots = \min T_{qt}^i$  in a server  $s_t$ , i.e. the maximum computation rate of every virtual machine

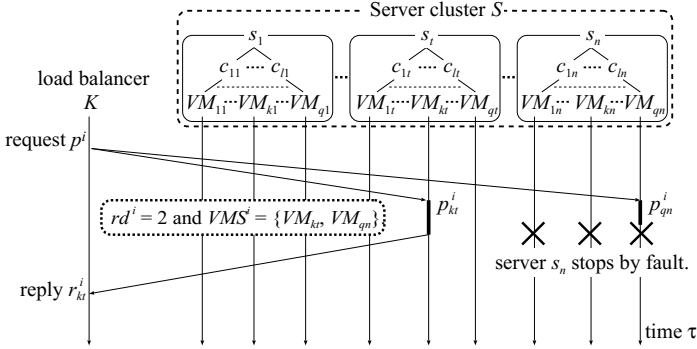


Fig. 1 System model.

$VM_{kt}$  in the server  $s_t$  is the same.  $\min T^i = \min(\min T_{k1}^i, \dots, \min T_{kn}^i)$ .  $\min T^i = \min T_{kt}^i$  on the fastest server  $s_t$ . We assume one virtual computation step is performed for one time unit on a virtual machine  $VM_{kt}$  in the fastest server  $s_t$ . That is, the maximum computation rate  $Maxf_{kt}$  of the fastest virtual machine  $VM_{kt}$  is 1 [vs/msec]. We assume  $Maxf_{1t} = Maxf_{2t} = \dots = Maxf_{qt}$  in a server  $s_t$ .  $Maxf = \max(Maxf_{k1}, \dots, Maxf_{kn})$ . A replica  $p_{kt}^i$  is considered to be composed of  $VS_{kt}^i$  virtual computation steps.  $VS_{kt}^i = \min T_{kt}^i \cdot Maxf = \min T_{kt}^i$  [vs].

The computation rate  $f_{kt}^i(\tau)$  of a replica  $p_{kt}^i$  performed on a virtual machine  $VM_{kt}$  at time  $\tau$  is defined as follows [5]:

$$f_{kt}^i(\tau) = \alpha_{kt}(\tau) \cdot VS^i / (\min T_{kt}^i \cdot NC_{kt}(\tau)) \cdot \beta_{kt}(nv_{kt}(\tau)). \quad (1)$$

Here,  $\alpha_{kt}(\tau)$  is the *computation degradation ratio* of a virtual machine  $VM_{kt}$  at time  $\tau$  ( $0 \leq \alpha_{kt}(\tau) \leq 1$ ).  $\alpha_{kt}(\tau_1) \leq \alpha_{kt}(\tau_2) \leq 1$  if  $NC_{kt}(\tau_1) \geq NC_{kt}(\tau_2)$ .  $\alpha_{kt}(\tau) = 1$  if  $NC_{kt}(\tau) \leq 1$ . Here,  $\alpha_{kt}(\tau)$  is assumed to be  $\varepsilon_{kt}^{NC_{kt}(\tau)-1}$  where  $0 \leq \varepsilon_{kt} \leq 1$ . The maximum computation rate  $maxf_{kt}^i$  of a replica  $p_{kt}^i$  is  $VS_{kt}^i / \min T_{kt}^i$  ( $0 \leq f_{kt}^i(\tau) \leq maxf_{kt}^i \leq 1$ ) where the replica  $p_{kt}^i$  is exclusively performed on a virtual machine  $VM_{kt}$  and only  $VM_{kt}$  is active on a core. Let  $nv_{kt}(\tau)$  be the number of active virtual machines on a core which performs a virtual machine  $VM_{kt}$  at time  $\tau$ . Let  $\beta_{kt}(nv_{kt}(\tau))$  be the *performance degradation ratio* of a virtual machine  $VM_{kt}$  at time  $\tau$  ( $0 \leq \beta_{kt}(nv_{kt}(\tau)) \leq 1$ ) where multiple virtual machines are active on the same core.  $\beta_{kt}(nv_{kt}(\tau)) = 1$  if  $nv_{kt}(\tau) = 1$ . The formula (1) means the computation rate  $f_{kt}^i(\tau)$  of each replica  $p_{kt}^i$  performed on a virtual machine  $VM_{kt}$  at time  $\tau$  decreases as the number of current replicas increases on the virtual machine  $VM_{kt}$ . The computation rate of a virtual machine decreases as the number of active virtual machines increases on the same core. The computation rate of a virtual machine performed on a core  $c_{ht}$  is independent of active virtual machines performed on another core  $c_{ft}$  ( $h \neq f$ ).

Suppose that a replica  $p_{kt}^i$  starts and terminates on a virtual machine  $VM_{kt}$  at time  $st_{kt}^i$  and  $et_{kt}^i$ , respectively. Here,  $T_{kt}^i = et_{kt}^i - st_{kt}^i$  and  $\sum_{\tau=st_{kt}^i}^{et_{kt}^i} f_{kt}^i(\tau) = VS^i$ . At time  $st_{kt}^i$  a

replica  $p_{kt}^i$  starts, the computation laxity  $lc_{kt}^i(\tau) = VS^i$  [vs]. The computation laxity  $lc_{kt}^i(\tau)$  [vs] of a replica  $p_{kt}^i$  at time  $\tau$  is given as follows:

$$lc_{kt}^i(\tau) = VS^i - \sum_{x=st_t^i}^{\tau} f_{kt}^i(x). \quad (2)$$

## 2.2 Power Consumption Model of a Server

$E_t(\tau)$  shows the electric power [W] of a server  $s_t$  at time  $\tau$ . Let  $maxE_t$  and  $minE_t$  be the maximum and minimum electric power [W] of a server  $s_t$ , respectively. Let  $ac_t(\tau)$  be the number of active cores in a server  $s_t$  at time  $\tau$ .  $minC_t$  shows the electric power [W] where at least one core  $c_{ht}$  is active on a server  $s_t$ . Let  $mv_t(\tau)$  be the number of virtual machines which concurrently migrate from a server  $s_t$  to the other servers at time  $\tau$ . Let  $cE_t$  be the electric power [W] where one core gets active on a server  $s_t$ . Let  $mE_t$  be the electric power [W] where one virtual machine migrates from a server  $s_t$  to the other server  $s_u$ .

The electric power  $E_t(\tau)$  [W] of a server  $s_t$  to perform processes on virtual machines at time  $\tau$  is given as follows [5]:

$$E_t(\tau) = minE_t + \sigma_t(\tau) \cdot (minC_t + ac_t(\tau) \cdot cE_t) + \lambda_t(\tau) \cdot (mv_t(\tau) \cdot mE_t). \quad (3)$$

Here,  $\sigma_t(\tau) = 1$  if at least one core  $c_{ht}$  is active on a server  $s_t$  at time  $\tau$ . Otherwise,  $\sigma_t(\tau) = 0$ .  $\lambda_t(\tau) = 1$  if at least one virtual machine migrates from a server  $s_t$  to another server at time  $\tau$ . Otherwise,  $\lambda_t(\tau) = 0$ .

The total energy consumption  $TE_t(\tau_1, \tau_2)$  [Ws] of a server  $s_t$  from time  $\tau_1$  to  $\tau_2$  is  $\int_{\tau_1}^{\tau_2} E_t(\tau) d\tau$ . The processing power  $PE_t(\tau)$  [W] of a server  $s_t$  at time  $\tau$  is  $E_t(\tau) - minE_t$ . The total processing energy consumption  $TPE_t(\tau_1, \tau_2)$  of a server  $s_t$  from time  $\tau_1$  to  $\tau_2$  is  $\int_{\tau_1}^{\tau_2} PE_t(\tau) d\tau$ .

## 3 Selection Algorithm

The total processing energy consumption laxity  $tpel_t(\tau)$  [Ws] shows how much electric energy a server  $s_t$  has to consume to perform every current replica on every active virtual machine in the server  $s_t$  at time  $\tau$ . Suppose a load balancer  $K$  receives a new request process  $p^{new}$  and allocates a replica  $p_{kt}^{new}$  to a virtual machine  $VM_{kt}$  performed on a server  $s_t$  at time  $\tau$ . Here, the replica  $p_{kt}^{new}$  is added to the current replica set  $CP_{kt}(\tau)$  of a virtual machine  $VM_{kt}$ , i.e.  $CP_{kt}(\tau) = CP_{kt}(\tau) \cup \{p_{kt}^{new}\}$ . Let  $\mathbf{CP}_t(\tau)$  be a family  $\{CP_{1t}(\tau), \dots, CP_{qt}(\tau)\}$  of current replica sets of every virtual machine  $VM_{kt}$  in a server  $s_t$  at time  $\tau$ . The total energy consumption laxity  $tpel_t(\tau)$  of

a server  $s_t$  at time  $\tau$  is obtained by the **ELaxity**( $s_t, \tau$ ) procedure [6]:

```

ELaxity( $s_t, \tau$ ) { /* a term VM stands for a virtual machine. */
  if every  $CP_{kt}(\tau) = \phi$  in  $\mathbf{CP}_t(\tau)$  and  $mv_t(\tau) = 0$ , return(0);
  for each core  $c_{ht}$  in a server  $s_t$ , {
     $nv$  = the number of active VMs on  $c_{ht}$  at time  $\tau$ ;
     $mv$  = the number of VMs migrating from  $c_{ht}$  at time  $\tau$ ;
    if  $nv \geq 1$ ,  $ac_t(\tau) = ac_t(\tau) + 1$ ; /* count of active cores on  $s_t$ . */
     $mv_t(\tau) = mv_t(\tau) + mv$ ; /* count of VMs migrating from  $s_t$ . */
    for each  $VM_{kt}$  on a core  $c_{ht}$ , {
      for each  $p_{kt}^i \in CP_{kt}(\tau)$ , {
         $lc_{kt}^i(\tau + 1) = lc_{kt}^i(\tau) - f_{kt}^i(\tau)$ ;
        if  $lc_{kt}^i(\tau + 1) \leq 0$ ,  $CP_{kt}(\tau) = CP_{kt}(\tau) - \{p_{kt}^i\}$ ;
      }
    }
  }
   $tpel_t(\tau) = E_t(\tau) - \min E_t$ ; /* processing power consumption */
  return( $tpel_t(\tau) + \mathbf{ELaxity}(s_t, \tau + 1)$ );
}

```

We discuss the *redundant energy consumption laxity based (RECLB)* algorithm to select multiple virtual machines to redundantly perform each process in presence of server fault so that the total processing energy consumption of a server cluster and average computation time of each replica can be reduced. Let  $TPE_{kt}^S(\tau)$  be the total processing energy consumption laxity of a server cluster  $S$  where a replica  $p_{kt}^i$  of a new request process  $p^i$  is allocated to a virtual machine  $VM_{kt}$  at time  $\tau$ . Suppose a load balancer  $K$  receives a new request process  $p^i$  at time  $\tau$ . Then, the load balancer  $K$  selects a set  $VMS^i$  of  $rd^i$  virtual machines in a server cluster  $S$  by the following procedure **RECLB**( $p^i, \tau$ ):

```

RECLB( $p^i, \tau$ ) { /* a term VM stands for a virtual machine. */
   $VMS^i = \phi$ ;
  while ( $rd^i > 0$ ) {
    for each  $VM_{kt}$  in a server cluster  $S$ , {
       $CP_{kt}(\tau) = CP_{kt}(\tau) \cup \{p^i\}$ ;
       $TPE_{kt}^S(\tau) = \sum_{t=1}^n \mathbf{ELaxity}(s_t, \tau)$ ;
    }
     $vm$  = a virtual machine  $VM_{kt}$  where  $TPE_{kt}^S(\tau)$  is the minimum;
     $VMS^i = VMS^i \cup \{vm\}$ ;
     $S = S - \{s_t\}$ ; /* the server  $s_t$  which performs the virtual machine  $vm$  is removed. */
     $rd^i = rd^i - 1$ ;
  }
  return( $VMS^i$ );
}

```

Suppose there are three servers  $s_1, s_2,$  and  $s_3$  in a server cluster  $S$ , i.e.  $S = \{s_1, s_2, s_3\}$ . Each server  $s_t$  is equipped with a single-core CPU and two threads  $th_{1t}$  and  $th_{2t}$  are bounded to the single-core. Hence, two virtual machines  $VM_{1t}$  and  $VM_{2t}$  are performed on each server  $s_t$ . Suppose a load balancer  $K$  receives a new request process  $p^i$  at time  $\tau$  and the redundancy  $rd^i$  of the process  $p^i$  is two ( $rd^i = 2$ ). Then, the load balancer  $K$  calculates the total processing energy consumption laxity  $TPE_{kt}^S(\tau)$  where a replica  $p_{kt}^i$  of the process  $p^i$  is allocated to each virtual machine  $VM_{kt}$  ( $k = \{1, 2\}$  and  $t = \{1, 2, 3\}$ ) according to the **ELaxity**( $s_t, \tau$ ) procedure. Suppose  $TPE_{11}^S(\tau)$  is the minimum, i.e.  $TPE_{11}^S(\tau) \leq TPE_{kt}^S(\tau)$  ( $k = \{1, 2\}$  and  $t = \{1, 2, 3\}$ ). Then, the load balancer  $K$  includes a virtual machine  $VM_{11}$  into the set  $VMS^i (= \{VM_{11}\})$  and removes the server  $s_1$  which performs the virtual machine  $VM_{11}$  from the server set  $S (= \{s_2, s_3\})$ . Next, the load balancer  $K$  calculates the total processing energy consumption laxity  $TPE_{kt}^S(\tau)$  where a replica  $p_{kt}^i$  is allocated to each virtual machine  $VM_{kt}$  ( $k = \{1, 2\}$  and  $t = \{2, 3\}$ ) in the server set  $S (= \{s_2, s_3\})$ . Suppose  $TPE_{23}^S(\tau)$  is the minimum. Then, the load balancer  $K$  includes a virtual machine  $VM_{23}$  into the set  $VMS^i (= \{VM_{11}, VM_{23}\})$  and removes the server  $s_3$  which performs the virtual machine  $VM_{23}$  from the server set  $S (= \{s_2\})$ . Here,  $rd^i = |VMS^i| = 2$ . The load balancer  $K$  forwards the process  $p^i$  to a pair of virtual machines  $VM_{11}$  and  $VM_{23}$  in the set  $VMS^i$ .

## 4 Evaluation

We evaluate the RECLB algorithm in terms of the total processing energy consumption of a homogeneous server cluster  $S$  and average computation time of each process  $p^i$  compared with the basic round-robin (RR) [9] algorithm.

A homogeneous cluster  $S$  is composed of five servers  $s_1, \dots, s_5$  ( $n = 5$ ) as shown in Table 1. Every server  $s_t$  ( $1 \leq t \leq 5$ ) follows the same computation model and the same power consumption model. Every server  $s_t$  is equipped with a dual-core CPU ( $nc_t = 2$ ). Hyper-Threading Technology [7] is enabled on a CPU in every server  $s_t$ . Two threads are bounded for each core in a server  $s_t$ , i.e.  $ct_t = 2$ . The number of threads  $nt_t$  in each server  $s_t$  is four, i.e.  $nt_t = nc_t \cdot ct_t = 2 \cdot 2 = 4$ .  $minE_t = 14.8$  [W],  $minC_t = 6.3$  [W],  $cE_t = 3.9$  [W],  $mE_t = 1.25$  [W], and  $maxE_t = 33.8$  [W]. The parameters of each server  $s_t$  are obtained from the experiment [5]. Each virtual machine  $VM_{kt}$  holds one virtual CPU and is bounded to a thread  $th_{kt}$  in a server  $s_t$  ( $k = 1, \dots, 4$  and  $t = 1, \dots, 5$ ). Hence, there are twenty virtual machines in the server cluster  $S$ . Every virtual machine  $VM_{kt}$  follows the same computation model as shown in Table 1. The maximum computation rate  $Maxf_{kt}$  is 1 [vs/msec]. The parameter  $\varepsilon_{kt}$  in the computation degradation ratio  $\alpha_{kt}(\tau)$  is 1. The performance degradation ratios  $\beta_{kt}(1) = 1$  and  $\beta_{kt}(2) = 0.5$ . The parameters of each server  $s_t$  and each virtual machine  $VM_{kt}$  are obtained from the experiment [5]. We assume the fault probability  $fr_t$  for every server  $s_t$  is the same  $fr = 0.1$ . We assume any virtual machine does not migrate to the other servers.

**Table 1** Parameters of each server  $s_t$  and each virtual machine  $VM_{kt}$ .

Server	$nc_t$	$ct_t$	$nt_t$	$minE_t$	$minC_t$	$cE_t$	$mE_t$	$maxE_t$
$s_t$	2	2	4	14.8 [W]	6.3 [W]	3.9 [W]	1.25 [W]	33.8 [W]
Virtual machine	$Maxf_{kt}$			$\epsilon_{kt}$	$\beta_{kt}(1)$	$\beta_{kt}(2)$		
$VM_{kt}$	1 [vs/msec]			1	1	0.5		

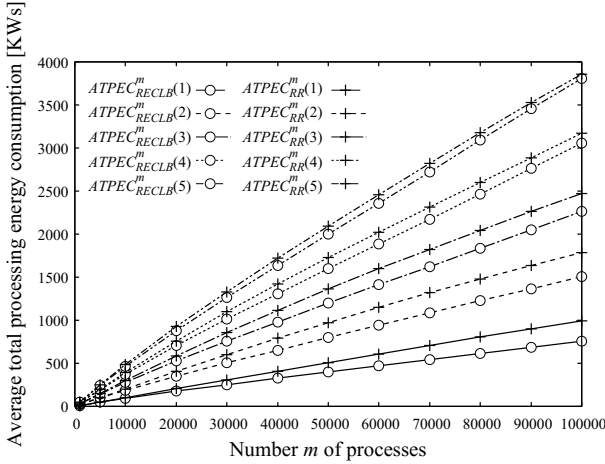
( $k = 1, \dots, 4, t = 1, \dots, 5$ , and  $minT^i = 1$  [msec]).

The number  $m$  of processes  $p^1, \dots, p^m$  ( $0 \leq m \leq 10,000$ ) are issued in the simulation. The starting time of each process  $p^i$  is randomly selected in a unit of one millisecond between 1 and 60 [sec]. The minimum computation time  $minT^i$  of every process  $p^i$  is assumed to be 1 [msec]. This means it takes one milli-second to exclusively perform a replica  $p_{kt}^i$  on a virtual machine  $VM_{kt}$  if the other virtual machines are not active on the same core where the virtual machine  $VM_{kt}$  is performed. We assume the redundancy  $rd^i$  for each process  $p^i$  is the same  $rd$  ( $= \{1, 2, 3, 4, 5\}$ ) and  $N_{fault} = rd - 1$  holds.

Let  $TPEC_{tm}^m(rd)$  be the total processing energy consumption [Ws] to perform the total number  $m$  of processes ( $0 \leq m \leq 10,000$ ) with redundancy  $rd$  ( $= \{1, 2, 3, 4, 5\}$ ) obtained in the  $tm$ th simulation. The total processing energy consumption  $TPEC_{tm}^m(rd)$  is measured 5 times for each redundancy  $rd$  ( $= \{1, 2, 3, 4, 5\}$ ) and each number  $m$  of processes. The average total processing energy consumption  $ATPEC^m(rd)$  [Ws] to perform the total number  $m$  of processes with redundancy  $rd$  is calculated as  $\sum_{tm=1}^5 TPEC_{tm}^m(rd) / 5$ . Here,  $ATPEC_{algo}^m(rd)$  stands for the average total processing energy consumption with an algorithm type  $algo \in \{\text{RECLB}, \text{RR}\}$  to perform the total number  $m$  of processes with redundancy  $rd$ . Figure 2 shows the average total processing energy consumption  $ATPEC_{algo}^m(rd)$  of the RECLB and RR algorithms where the fault probability  $fr$  for every server  $s_t$  is 0.1. In the RECLB and RR algorithms, the average total processing energy consumption increases as the number  $m$  of processes increases. In the RECLB algorithm, a virtual machine  $VM_{kt}$  where the total processing energy consumption laxity of a server cluster  $S$  is the minimum is selected for each replica. Hence, the average total processing energy consumption to perform the number  $m$  of processes can be more reduced in the RECLB algorithm than the RR algorithm for each redundancy  $rd$ .

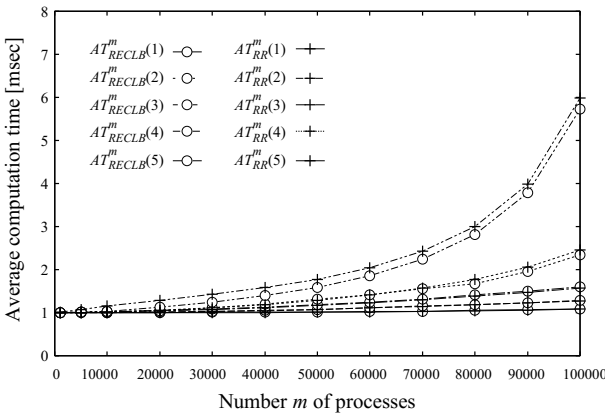
The computation time  $T^i$  for each process  $p^i$  is the computation time  $T_{kt}^i$  of a replica  $p_{kt}^i$  earliest committed in the replicas of the process  $p^i$ . The computation time  $T^i$  for each process  $p^i$  is measured 5 times for each redundancy  $rd$  and each number  $m$  of processes. Let  $T_{tm}^{i,m}(rd)$  be the computation time  $T^i$  [msec] of a process  $p^i$  obtained in the  $tm$ -th simulation for redundancy  $rd$  and total number  $m$  of processes. Here,  $AT_{algo}^m(rd)$  stands for the average computation time [msec] of each process with an algorithm type  $algo \in \{\text{RECLB}, \text{RR}\}$  to perform the total number  $m$  of processes with redundancy  $rd$ . The average computation time  $AT_{algo}^m(rd)$  is calculated as  $\sum_{tm=1}^5 \sum_{i=1}^m T_{tm}^{i,m}(rd) / (m \cdot 5)$ . Figure 3 shows the average computation time





**Fig. 2** Average total processing energy consumption  $ATPEC_{algo}^m(rd)$  in the homogeneous server cluster  $S$  (number  $m$  of processes are issued in 60 [sec] and  $fr = 0.1$ ).

$AT_{algo}^m(rd)$  in the RECLB and RR algorithms where the fault probability  $fr$  for every server  $s_t$  is 0.1. The average computation time  $AT_{algo}^m(rd)$  increases as the number  $m$  of processes and redundancy  $rd$  increase in the RECLB and RR algorithms. For  $1 \leq rd \leq 4$  and  $0 \leq m \leq 10,000$ , the average computation time in the RECLB algorithm is the same as the RR algorithm. For  $rd = 5$  and  $0 \leq m \leq 10,000$ , the average computation time in the RECLB algorithm can be more reduced than the RR algorithm since the computation resources in the homogeneous server cluster  $S$  can be more efficiently utilized in the RECLB algorithm than the RR algorithm.



**Fig. 3** Average computation time  $AT_{algo}^m(rd)$  of each process in the homogeneous server cluster  $S$  (number  $m$  of processes are issued in 60 [sec] and  $fr = 0.1$ ).

Following the evaluation, we conclude the RECLB algorithm is more useful in a homogeneous server cluster than the RR algorithm.

## 5 Concluding Remarks

In this paper, we proposed the RECLB algorithm to select multiple servers for redundantly performing each computation process issued by a client in presence of server fault so that the total energy consumption of a server cluster and the average computation time of each process can be reduced. In the RECLB algorithm, a set of multiple virtual machines where the total processing energy consumption laxity of a server cluster is the minimum is selected to perform multiple replicas of each process. We evaluated the RECLB algorithm in terms of the total energy consumption of a homogeneous server cluster and computation time of each process compared with the RR algorithm. The average total processing energy consumption of the homogeneous server cluster and computation time of each process are shown to be more reduced in the RECLB algorithm than the RR algorithm.

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