

Generalized Nets for Agent-Based Modeling

Galina Ilieva^(✉) and Stanislava Klisarova

Plovdiv University “Paisii Hilendarski”, Tsar Assen 24, 4000 Plovdiv, Bulgaria
galili@uni-plovdiv.bg, stanislava.klisarova@gmail.com

Abstract. The purpose of this paper is to evaluate the applicability of generalized nets for multi-agent systems modeling. Several models of interaction among intelligent agents as economic subjects were developed. The analysis that has been conducted shows that the proposed method is suitable for modeling and assessing information systems based on agents’ technology.

Keywords: Multi-agents system modeling · Generalized nets · Economic model

1 Introduction

This paper is dedicated to applying generalized nets (GNs) for modeling economic interactions that involve participation of a large number of independent agents. The aim of the work is to enrich the tools for formal description of objects, processes and interactions in multi-agent systems (MAS).

Interest in the topic is inspired by recent changes in economics methodology, where a growing demand for alternative approaches to economic analysis is observed [3]. One option for achieving greater flexibility of economic models is employing multi-agent systems that simulate the behavior of a large number of individual participants, prominent in the literature as agent-based computational economics (ACE) [14].

ACE methods are suitable for the study of processes characterized by heterogeneity of the participants and a variety of interactions among them. These methods can successfully overcome some limitations of traditional economic models, such as requirements for the existence of equilibrium, assumptions about rationality of economic actors, etc. Modern MAS have various economic applications ranging from researching production processes [10] to modeling economic crises [12], financial markets [15] or automated auctions [8]. Despite the numerous advantages of ACE, however, research work on the specifics of building economic multi-agent systems is not plentiful. Enrichment of the tools for description, design and analysis of MAS would increase the quality of developed software and contribute to the further improvement to ACE modeling of economic objects, processes and phenomena.

The first section provides a brief overview of the basic ideas and functionality of some tools for describing MAS and emphasizes the advantages of generalized nets for modeling parallel processes in complex adaptive systems. The second section models the interaction of economic systems elements with the tools of generalized nets. The last section discusses the applicability of GNs in the design of multi-agent systems for

economic simulations. The conclusion summarizes the main findings on the importance of the proposed method for researchers and analysts who deal with economic issues.

The main contribution of the work is in the construction of formal models of interaction among economic subjects (such as bank loan approval, stock trading, and online market). The created GNs information models reflect the mechanisms of interaction among participants and can be used in the analysis and prediction of economic processes as well as in the design of agent systems for their simulation.

2 Some Instruments for MAS Modeling

The topicality of the theme of this paper stems from issues surrounding the design of MAS. Applying the appropriate modeling instruments can significantly improve the quality of the development process and thus, the quality of the software system. Despite the significance of agent-based modeling, there is no standard protocol, language or tool to support the development of multi-agent applications.

In practice, different approaches are used to describe and present agent-based software. [16] provides a comprehensive overview of techniques for agent-oriented analysis and design, dividing them in two groups: those that extend or adapt existing object-oriented (OO) methodologies and those that adapt knowledge engineering or other techniques. The last decade saw the emergence of new instruments such as ODD, AML, etc.

The ODD protocol standardizes the three main blocks in the description of MAS – Overview, Design concept and Details. The basic idea behind the protocol is always structuring the information about an agent-based model in the same sequence. This sequence consists of several elements that can be grouped in the abovementioned blocks: purpose, state variables and scales, process overview and scheduling; design concepts; initialization, input, and submodels [6]. Although ODD model descriptions are understandable and complete, this protocol has several shortcomings and has been modified multiple times. For example, [7] adds more elements to the model. The advantages of ODD are its independence from subject area, operation system и programming language. Its main disadvantage is that it requires the properties and methods to be presented separately, which obstructs OO implementations.

AML is an extension of industrial standard UML and facilitates MAS specification in agent-oriented software engineering. This language is applied in all phases of MAS development and offers opportunities for project visualization through standard flow-charts types. Despite the fact that AML is sufficiently detailed and tangible enough, some aspects of agent-based systems such as concurrency, ontologies and mobility are not adequately supported. The capabilities of AML for visualizing the collaboration of several subjects is also limited [2].

The disadvantages of the abovementioned tools for design and technical description of MAS are:

- inability to design complex composite structures with a high degree of detail,
- problems in defining the dynamic behavior of the modeled objects,
- no temporal dimension in interactions, and others.

These restrictions hinder the adequate representation of contemporary MAS. A viable alternative are Petri nets (PNs), a mathematical modeling language and a well-known instrument for the description of distributed systems [9]. Generalized nets (GNs) as their name implies are a significant extension and generalization of the concept of PNs. GNs are currently present in various developments in the field of artificial intelligence. Two of their main applications can be found in [5, 11, 13] contains a comprehensive bibliographic database. As agent-based economics studies complex distributed systems concurrent actions of a set of interacting entities and their emergent behavior, GNs constitute a modern formalism that could be applied to MAS modeling.

The main advantages of generalized nets as a discrete tool for description of models of complex systems with many different and interacting components, often involved in parallel activities are:

- the conditions of predicate-transitive PNs are replaced by a predicate matrix which defines the rules for tokens' transfer to the different output places,
- in addition to discrete time in which processes in PNs take place, GNs contains an absolute time scale which can be used for keeping the time while a net is functioning,
- specific token's feature determines plausible predicate values,
- while going through transitions, the tokens receive new characteristics through a characteristic feature,
- practically no limitations to the characteristics of the tokens [1].

These features of generalized nets turn them into a potential tool for modeling dynamic processes within MAS with heterogeneous participants. Compared to well-known instruments for MAS modeling, GNs offer a simple and effective way of adequately modeling real processes. With GNs, designers are free to define different types of data and create models suitable for OO programming. Therefore, generalized nets are a possible alternative for overcoming the shortcomings of the abovementioned modeling languages and for expanding the applications of agent technology in economic research studies.

3 Generalized Net Models for MAS Simulation of Some Economic Processes

Through GNs, economic processes are described as a complex system of objects that interact and influence each other over time. Descriptions of two GN models of examples from the field of economics are discussed below.

Assume a business process of loan approvals in a financial institution is given. Loan candidates are represented by tokens with initial characteristics that include an agent's income, age, number of children, other debts, etc. The representation of this GN model (Fig. 1) contains only three transitions.

The form of the first transition is the following:

$$Z_1 = \langle \{l_1\}, \{l_2, l_3\}, r_1, M_1, \wedge(l_1) \rangle. \tag{1}$$

The token from place l_1 splits into two tokens α_2 and α_3 , which take places l_2 and l_3 , respectively. Token α_2 obtains characteristic “number of clients who receive the loan” at place l_2 and token α_3 obtains characteristic “number of clients who do not receive the loan” at place l_3 . If we need any additional information, such as loan type, we can expand the respective token’s characteristics.

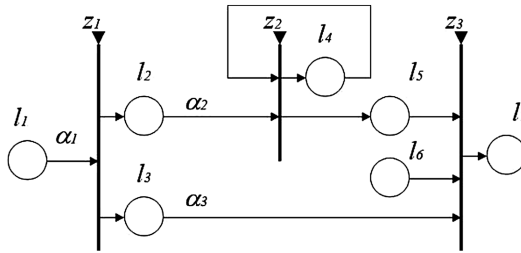


Fig. 1. A GN model for bank loan system

The transition condition r_1 is represented by the index matrix (IM):

$$r_1 = \begin{array}{c|cc} & l_2 & l_3 \\ \hline l_1 & W_{1,2} & W_{1,3} \end{array}$$

where $W_{1,2}$ and $W_{1,3}$ define the conditions for approving and declining a loan request.

The arc-capacity IM M_1 for the transition Z_1 can have the form:

$$M_1 = \begin{array}{c|cc} & l_2 & l_3 \\ \hline l_1 & n & n \end{array}$$

with possibility to receive n loan requests simultaneously. In this case we must set $c(l_1) = c(l_2) + c(l_3) = c(l_6) = c(l_7) = n$, where c gives the capacities of the places.

The last element of Z_1 is the so-called transition type and it is an object having a form similar to a Boolean expression. It contains as variable the symbol that serves as label for the transition’s input place, and the Boolean connective \wedge determines that the place l_1 must contain at least one token.

The second transition is the following:

$$Z_2 = \langle \{l_5, l_6\}, \{l_7\}, r_2, M_2, \vee(l_5, l_6) \rangle \tag{2}$$

Now,

$$r_2 = \frac{\quad}{\begin{array}{c|c} & l_7 \\ \hline l_5 & W_{5,7} \\ l_6 & W_{6,7} \end{array}} \quad M_2 = \frac{\quad}{\begin{array}{c|c} & l_7 \\ \hline l_5 & n \\ l_6 & n \end{array}}$$

where $n \geq 1$.

This transition models the process of repaying the loan. If necessary, that repayment could be carried out by the loan guarantors (place l_6). In real life there are various other situations such as, for example, the borrower applying for refinancing.

The transition type $\vee(l_5, l_6)$ determines the following condition: there must be at least one token in the set of places l_5 and l_6 .

Actions at Z_3 can be represented as follows:

$$Z_3 = \langle \{l_2, l_4\}, \{l_4, l_5\}, r_3, M_3, \vee(l_2, l_4) \rangle, \quad (3)$$

Where

$$r_3 = \frac{\quad}{\begin{array}{c|cc} & l_4 & l_5 \\ \hline l_2 & W_{2,4} & W_{2,5} \\ l_4 & false & true \end{array}}$$

and predicate $W_{2,4}$ has characteristic “it is necessary to refinance the loan”, $W_{2,5} = \neg W_{2,4}$. Token α_2 enters place l_4 or l_5 and obtains suitable characteristics. The form of IM M_3 is similar to the one above.

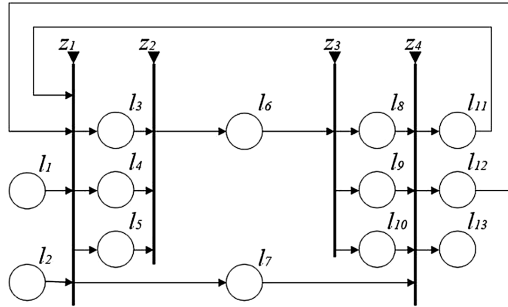


Fig. 2. A GN model of stock exchange system

In this first GN model, we discussed one of the ways to represent the process of lending a loan. All discussed situations can be broken down into further details.

Figure 2 presents a model of a part of MAS for stock exchange. Transition Z_1 models the process of receiving input orders to buy a particular amount of financial instruments and their distribution for further processing, e.g., market order (l_3), limit order (l_4) and market-to-limit order (l_5).

Here is what transition Z_1 looks like:

$$Z_1 = \langle \{l_1, l_2, l_{11}, l_{12}\}, \{l_3, l_4, l_5, l_7\}, r_1, M_1, \vee(l_1, l_2, l_{11}, l_{12}) \rangle. \quad (4)$$

The initial characteristics of the tokens from this part of MAS are: l_1 – reception of purchase orders; l_2 – presence of new information from the National Commerce

Register, which should be taken into consideration in the further implementation of the service; l_{11} – arrival of a purchase order, after the supervisory authorities denied participation for this buyer once; l_{12} – availability of information in the national database that needs to be compared with information in the submitted documents.

Matrices r_1 and M_1 have the following contents:

$$r_1 = \begin{array}{c|cccc} & l_3 & l_4 & l_5 & l_7 \\ \hline l_1 & W_{1,3} & W_{1,4} & W_{1,5} & false \\ l_2 & false & false & false & W_{2,7} \\ l_{11} & W_{11,3} & W_{11,4} & W_{11,5} & false \\ l_{12} & false & false & false & W_{12,7} \end{array}$$

$$M_1 = \begin{array}{c|cccc} & l_3 & l_4 & l_5 & l_7 \\ \hline l_1 & n & n & n & 0 \\ l_2 & 0 & 0 & 0 & n \\ l_{11} & n & n & n & 0 \\ l_{12} & 0 & 0 & 0 & n \end{array}$$

Transition Z_2 models the process of structuring the received applications as market orders (l_3), limit orders (l_4) and market-to-limit orders (l_5):

$$Z_2 = \langle \{l_3, l_4, l_5\}, \{l_6\}, r_2, M_2, \vee(l_3, l_4, l_5) \rangle. \tag{5}$$

The process of buying a stock under the defined deal parameters is modeled with transition Z_3 :

$$Z_3 = \langle \{l_6\}, \{l_8, l_9, l_{10}\}, \{t_3\}, \{t_{31}, t_{32}, t_{33}\}, r_3, M_3, \vee(l_6) \rangle. \tag{6}$$

The times of occurrence of transitions Δt_{3-31} , Δt_{3-32} и Δt_{3-33} depend on the length of the corresponding auction sessions.

Transition Z_4 represents the outcome of information system:

$$Z_4 = \langle \{l_7, l_8, l_9, l_{10}\}, \{l_{11}, l_{12}, l_{13}\}, r_4, M_4, \vee(l_7, l_8, l_9, l_{10}) \rangle. \tag{7}$$

For this transition IM have the following contents:

$$r_4 = \begin{array}{c|ccc} & l_{11} & l_{12} & l_{13} \\ \hline l_7 & false & W_{7,12} & W_{7,13} \\ l_8 & W_{8,11} & W_{8,12} & W_{8,13} \\ l_9 & W_{9,11} & W_{9,12} & W_{9,13} \\ l_{10} & W_{10,11} & W_{10,12} & W_{10,13} \end{array}$$

$$M_4 = \begin{array}{c|ccc} & l_{11} & l_{12} & l_{13} \\ \hline l_7 & 0 & n & n \\ l_8 & n & n & n \\ l_9 & n & n & n \\ l_{10} & n & n & n \end{array}$$

The presented model reflects only a small part of the actions included in the procedures of an agent-based exchange information system.

4 Generalized Net Model of Electronic Market Simulation

Both examples above demonstrate the possibilities for real use of GN in agent-based economic modeling. The first one represents a bank activity in a credit department whose basic processes are described. This model can be used for predicting different situations that may arise at the department (delaying payments, modifying credit terms and conditions, refinancing, etc.).

The second model visualizes purchases at a stock exchange. This model can be expanded to present a market where every agent, buyer or dealer, could pursue their own strategy for buying or selling. Both models could also be improved to provide mechanisms for reporting the impact of external effects on interest rates, stock prices and more.

The main advantages of both GN models from Sect. 3 are:

- describing and modeling of real-life parallel processes,
- simulating of processes,
- monitoring and controlling of processes.

However, these two examples do not demonstrate the essence of applying a GN model to an agent-based system, which is the representation of the behaviors and interactions of many agents, each of which has unique characteristics. For demonstrating these advantages of GNs, we will build a model of MAS for many-to-many negotiation (Fig. 3).

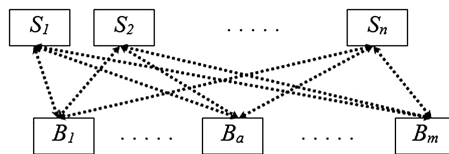


Fig. 3. Many-to-many negotiation

In order to describe the interactions between buyer $B_i, i = 1, \dots, m$ and seller $S_j, j = 1, \dots, n$ [4] proposes a model of bilateral agents' negotiation, where each agent's behavior depends on a scoring function and the remaining time that an agent has. The corresponding GN model of buyer B_a behavior is shown on Fig. 4.

The first transition Z_{1a} has $n + 1$ input places, labeled $l_{1,a}, l_{2,a}, \dots, l_{n,a}$ – receiving sellers' offers (the notation used here is $l_{i,j}$, where i is buyer number, and j is seller number) and l_{ago} means that the buyer is ready to receive the next offer (i.e. it has finished processing the previous one). There is only one output– l_a and it is the offer that is currently being processed.

$$r_{Z1a} = \begin{array}{c|c} & l_a \\ \hline l_{1,a} & W_1 \\ l_{2,a} & W_2 \\ \dots & \dots \\ l_{n,a} & W_n \\ l_{ago} & false \end{array} \quad M_{Z1a} = \begin{array}{c|c} & l_a \\ \hline l_{1,a} & 1 \\ l_{2,a} & 1 \\ \dots & \dots \\ l_{n,a} & 1 \\ l_{ago} & 0 \end{array}$$

Transition Z_{1a} chooses an offer to process provided that processing the previous offer has been completed and place l_{ago} contains a token:

$$Z_{1a} = \langle \{l_{1,a}, l_{2,a}, \dots, l_{n,a}, l_{ago}\}, \{l_a\}, r_{Z1a}, M_{Z1a}, \wedge(l_{ago}, \vee(l_{1,a}, l_{2,a}, \dots, l_{n,a})) \rangle. \quad (8)$$

The transition condition r_{Z1a} and arc-capacity M_{Z1a} are represented by IMs, where W_1, \dots, W_n are predicates, through which the next offer for processing is determined. Its choice may depend on negotiation history with a certain buyer, offer conditions, etc. As only one offer can be processed at a time, it is implied that only one of the predicates W_1, \dots, W_n can be assigned a value of *true* in case a certain choice is made. A value of *false* assigned to transfer predicate $l_{ago} - l_a$ means that the token of l_{ago} could not be assigned to l_a .

The second transition is the following:

$$Z_{2a} = \langle \{l_{ainit}, l_a, l_{atm}\}, \{l_{a\alpha}, l_{a\beta}, l_{a\gamma}\}, \{0, 0, t_{prop}\}, r_{Z2a}, M_{Z2a}, \vee(l_{ainit}, l_a, l_{atm}) \rangle \quad (9)$$

and it models the process of assessing the currently processed offer and making a decision. The offer l_a chosen in transition Z_{1a} serves as input. Output could be $l_{a\alpha}, l_{a\beta}$

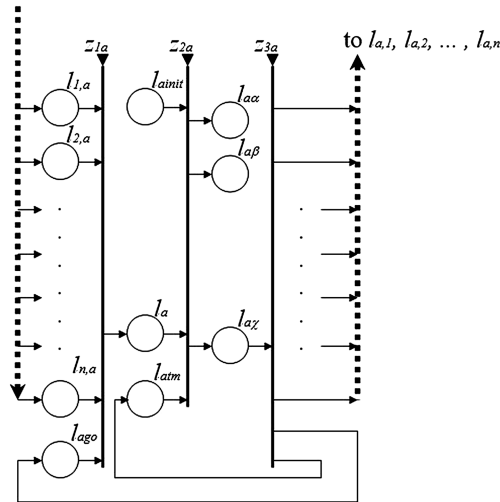


Fig. 4. GN model of buyer agent in electronic market MAS

and $l_{a\gamma}$, which correspond respectively to decisions to withdrawing from negotiations due to time running out (timeout); accepting the processed offer and making a deal; preparing a counteroffer. Additional input for this transition may also be provided: l_{ainit} – for initializing an agent’s activity and making an opening offer and l_{atm} – for forceful activation of a transition in case of prolonged lack of new offers.

Now,

$$r_{Z2a} = \begin{array}{c|ccc} & l_{a\alpha} & l_{a\beta} & l_{a\gamma} \\ \hline l_{ainit} & false & false & Init \\ l_a & F_1 & F_2 & F_3 \\ l_{atm} & T_1 & T_2 & T_3 \end{array} \quad M_{Z2a} = \begin{array}{c|ccc} & l_{a\alpha} & l_{a\beta} & l_{a\gamma} \\ \hline l_{ainit} & 0 & 0 & 1 \\ l_a & 1 & 1 & 1 \\ l_{atm} & 1 & 1 & 1 \end{array}$$

where *Init* is a predicate for making an opening offer, F_1, \dots, F_3 and T_1, \dots, T_3 are predicates for transitions to the respective output places. The two *false* predicates in r_{Z2a} guarantee that, during initialization no timeout or making a deal may occur. The third element of a transition’s definition gives the length of the transfer to output states (places) where t_{prop} indicates the time needed for preparing a new offer (transfer to $l_{a\gamma}$).

The last transition Z_{3a} is as follows:

$$Z_{3a} = \langle \{l_{a\gamma}\}, \{l_{a,1}, l_{a,2}, \dots, l_{a,n}, l_{ago}, l_{atm}\}, \{0, 0, \dots, 0, 0, t_{timeout}\}, r_{Z3a}, M_{Z3a}, \wedge(l_{a\gamma}) \rangle. \quad (10)$$

The last transition directs the prepared specific offer ($l_{a\gamma}$) to the respective seller S_1, S_2, \dots, S_n . Moreover, activating this transition ensures unconditional (predicate *true* in r_{Z3a}) tokens for l_{ago} and l_{atm} , which are necessary for allowing transition Z_{1a} and activating transition Z_{2a} in case of timeout, respectively. Transfer time of token to l_{atm} is given by the parameter $t_{timeout}$ (Eq. 10). This guarantees periodic self-activation of this transition when there are no new offers.

The IMs are:

$$r_{Z3a} = \begin{array}{c|cccccc} & l_{a,1} & l_{a,2} & \dots & l_{a,n} & l_{ago} & l_{atm} \\ \hline l_{a\gamma} & Y_1 & Y_2 & \dots & Y_n & true & true \end{array} \quad M_{Z3a} = \begin{array}{c|cccccc} & l_{a,1} & l_{a,2} & \dots & l_{a,n} & l_{ago} & l_{atm} \\ \hline l_{a\gamma} & 1 & 1 & \dots & 1 & 1 & 1 \end{array}$$

where Y_1, \dots, Y_n are predicates for directing the generated offer to the respective seller. Only one of predicates Y_1, \dots, Y_n may be assigned a value of *true* when activating the transition.

A GN model of agent-buyer in MAS for simulating an e-market is very similar.

The model that was described earlier demonstrates modeling time-related characteristics via a GN. For example, to measure the time needed for generating new offers in different bidding strategies, the t_{prop} characteristic is used, and for ensuring activity when there are no offers, $t_{timeout}$ is set.

The three GN models that were presented demonstrate some of the advantages of GN. For example, detailed and individualized description of the mechanism of interaction among participants facilitates the software realization of MAS via an OO programming language. Agents' behaviors and interactions can be described in detail and time-related characteristics can also be added.

5 Conclusion

In this paper we show that generalized nets are detailed, comprehensive and tangible enough to be a useful tool for building multi-agent information systems. A comparative analysis has been conducted on instruments for multi-agent modeling. The advantages of GNs as a generalization of Petri nets variations were listed. Simplified generalized nets which model some business processes were developed. Employing GNs, a new model of agent-participant (buyer or seller) in MAS for electronic market simulation was built. The analysis that was performed shows that GNs are a suitable instrument for preliminary modeling of basic parts of large scale ACE applications before their software implementation. Due to their features GNs might form a significant contribution to the effort of bringing about widespread adoption of intelligent agents across various areas of applications, such as economic research. Future work will include integrating the developed models in complex models in MAS for electronic commerce.

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