# Geoffrey R. Mitchell · Ana Tojeira *Editors*

# Controlling the Morphology of Polymers

Multiple Scales of Structure and Processing



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To our families, for all the joy and inspiration.

Dedicated to the memory of Jill Mitchell  $(1948 - 2015)$ .

### Preface

The possibility of long-chain molecules was established at the start of the twentieth century through the pioneering work of Hermann Staudinger [\(1920](#page-9-0)), who was awarded the Nobel Prize in Chemistry in 1953 "for his discoveries in the field of macromolecular chemistry." Much of the twentieth century was dominated by the ingenious work of synthetic organic chemists in producing polymers with particular chemical configurations and molecular lengths. The first to dominate the field were Giulio Natta and Karl Zeigler whose work led to the commercial production of stereoregular alpha olefins such as polypropylene (Natta [1967\)](#page-9-0). The contribution of Karl Ziegler was the discovery of the first titanium-based catalysts. Giulio Natta used such catalysis to prepare stereoregular polymers from propylene. Both were awarded the Nobel Prize in Chemistry in 1963.

Other developments have built on these early steps. In the 1950s, scientists at Phillips Petroleum discovered that chromium catalysts are very effective for the low temperature polymerization of ethylene, which launched major industrial technologies. A little later, Ziegler discovered that the combination of titanium chloride and ethyl aluminum sesquichloride gave comparable activities for the production of polyethylene. Natta used crystalline α-titanium chloride in combination with triethyl aluminum to produce the first isotactic polypropylene. In the 1960s, BASF developed a gas phase, a mechanically stirred polymerization process for making polypropylene which led to the UNIPOL process, which was commercialized by Union Carbide to produce polyethylene. Later in the 1970s, magnesium chloride was discovered to greatly enhance the activity of the Ti-based catalysts. These catalysts are so active that the residual Ti is no longer removed from the product. They enabled the commercialization of linear low-density polyethylene (LLDPE) resins and allowed the development of noncrystalline copolymers. These developments and similar research have transformed plastics from an oddity only suited to Hula-Hoops into a major technological materials industry with a total global demand of over 200 million tonnes.

Functional polymers appeared in the second half of the twentieth century. Although polyaniline was first described in the mid-nineteenth century by Henry Letheby and polypyrrole derivatives were reported to be electrically conducting in 1963 by B.A. Bolto et al. ([1963\)](#page-9-0), substantial progress was not made with intrinsically conducting polymers until the pioneering work of Hideki Shirakawa, Alan J. Heeger, and Alan MacDiarmid who reported similar high conductivity in oxidized iodine-doped polyacetylene in 1977 (Shirakawa [1977\)](#page-9-0). For this research, they were awarded the 2000 Nobel Prize in Chemistry "for the discovery and development of conductive polymers."

Liquid crystal polymers and elastomers (Donald et al. [2006\)](#page-9-0), dendrimers (Hawker and Fréchet [1990\)](#page-9-0), and block copolymers (Szwarc [1956\)](#page-9-0) also appeared in the second half of the twentieth century. Today we can select polymers with many different properties and functions. Of particular current note is the development of photovoltaic devices which are beginning to show considerable promise. However, in the field of photovoltaics, researchers have found that it is not just the ingenuity of the molecule makers that delivers the efficiency but also controlling the morphology. Controlling the morphology is a major tool in polymer science and engineering. It enables chemically the same material such as polyethylene to be exploited to produce low-cost plastic bags as well as bulletproof vests.

This book sets out to embrace this control of morphology recognizing from the outset that the different scales of structure are connected. As Natta discovered the precise positioning of the methyl group in polypropylene leads to a high crystallinity and without precise positioning to a poor quality amorphous polymer used in roofing membranes, others have identified that the control of that crystallization process leads to clear packaging material which constitutes about half of the 60 million tonnes of polypropylene-based materials used in 2013.

Like the scales of structure, the contributors to this book are all interconnected in a myriad of ways. At the core, connecting many is the highly successful Reading Polymer Physics Group, later morphing into the Polymer Science Centre at the University of Reading. It was there that Alison Hodge, Robert Olley, and David Bassett optimized the permanganic etching process for revealing the morphology of semicrystalline polymers (Olley [1979\)](#page-9-0). The advent of time-resolving X-ray scattering at synchrotron-based beamlines (Keates et al. [1994](#page-9-0)) has greatly added to the ability to follow in real time the development of structure and morphology during processing. Not all good things go on forever, and the University brought the curtain down on polymer physics at Reading in 2010 with the closure of the Department of Physics. With every closing door, another opens and so please check out controlling morphology during 3D printing in Chap. [7.](http://dx.doi.org/10.1007/978-3-319-39322-3_7) The future is direct digital manufacturing as Mr. McGuire<sup>1</sup> might say.

<sup>&</sup>lt;sup>1</sup>Mr. McGuire (played by Walter Brooke) is a character in the motion picture "The Graduate" who said in the movie "Plastics," followed by "There's a great future in plastics," to the graduate Ben Braddock played by Dustin Hoffman, which is one of all-time top 100 quotes judged by the American Film Institute.

<span id="page-9-0"></span>We would like to thank all the authors for their contributions and their positive approach to this crosscutting project. It has been a pleasure to work with them all.

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Marinha Grande, Portugal Geoffrey R. Mitchell

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## **Contents**





## Chapter 1 Scales of Structure in Polymers

Geoffrey R. Mitchell, Fred J. Davis, and Robert H. Olley

#### 1.1 Introduction

The multi-valency of the carbon atom leads immediately to a rich variety of molecular structures including long-chain polymers. At the smallest scale, the chemical bonds are anisotropic but without appropriate molecular ordering, that anisotropy is not conveyed to the macroscopic scale which has a substantial impact on the properties. This chapter focuses on detailing these scales of structures and the types of ordering processes which are observed in polymer-based materials. We consider the mechanisms for the transformation of polymer melts by these ordering processes. Finally, we consider 'top-down' manufacturing processes which lead to 'ordering' on a scale larger than that intrinsic to the polymer material.

#### 1.2 Types of Bonds

Although many inorganic systems may be considered to be polymeric, the term polymer is generally taken to refer to long chains of organic polymers. The importance of the high molecular weight is that it is this that controls their mechanical properties. The useful mechanical properties of a polymer arise from the increased magnitude of the bonding between molecules. This intermolecular

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bonding is collectively classified as Van der Waals bonding although this terminology is often used just to describe the bonding from induced dipole-induced dipole forces (London Forces). In addition to the London dispersion forces, intermolecular bonding is provided by dipole-induced dipole forces, dipole–dipole forces and hydrogen bonding. In polymers with ionic groups, there may be ionic interactions. While London forces are generally considered to be the weakest of the interaction, because of their ubiquitous nature they tend to contribute more towards the overall intermolecular bonding (except in small molecules such as water). However, the presence of interactions additional to London forces results in increased strength; thus up to a molecular weight of 10,000 Da, polyethylene which has no permanent dipole is a waxy solid, while polyamides (with hydrogen bonding) are hard solids at weights as low as 1000 Da (Stevens [1990\)](#page-39-0).

#### 1.3 Types of Polymers

There are a number of different ways to classify polymers but perhaps the simplest division is between natural polymers (biopolymers) which include proteins (polypeptides), polysaccharides, and poly(nucleotides) and synthetic polymers which include polyethylene, poly(vinyl chloride) and nylon; some natural polymers are synthetically modified as in the formation of viscose rayon from cellulose or vulcanized rubber from natural rubber [largely poly(isoprene)].

Chemists generally classify synthetic polymers by their mode of synthesis: chain growth polymers are formed by the addition of single monomers to a growing chain, while step growth polymers are formed by the reaction of (for example) bifunctional monomers to form dimers, trimers, etc. which may react together to form larger molecules. An example of a chain growth polymerization would be the formation of polystyrene [Reaction (1.1)], while an example of the second is provided by poly(ethylene terephthalate) as shown in Reaction (1.2).



Chain-growth polymers are often formed from vinyl systems ( $CH<sub>2</sub>=CHX$ ) and represent some of the most common commercial polymers; examples include



Fig. 1.2 Schematic of copolymer systems: (a) homopolymer; (b) alternating copolymer; (c) random copolymer; (d) block copolymer; and (e) graft copolymer



polyethene, polypropene, poly(methyl methacrylate) and poly (vinyl chloride). One particular feature of these polymers is that for all systems except ethene  $(X=H)$ , the resulting polymers have a stereogenic centre, resulting in a range of arrangements of the side groups, such arrangements are described in Fig. 1.1. The normal atactic (or random) arrangement might be expected from simple processes such as freeradical polymerization, more regular structures such as isotactic and syndiotactic poly(propene), are usually produced by organometallic catalysts such as the Ziegler–Natta catalyst (Stevens [1990](#page-39-0)). In general, the more stereoregular polymers have a greater tendency towards crystallization, and as such are often valued for their enhanced mechanical properties.

The repeat unit for poly(ethylene terephthalate) ([I] Reaction (1.2) above) is built up from two chemical units, but the polymer is a continuous repeat of this structure. In many cases, the structure of a polymer is modified by the addition of another monomer unit during the polymerization process, a process known as copolymerization. This for a vinyl polymer system, for example, styrene could be copolymerized with methyl methacrylate. Such copolymers can be arranged in different as shown in Fig. 1.2 and each type of material may show interesting or unique properties. For example, block copolymers may show microphase separation of the incompatible blocks of copolymer, and this can produce for example materials useful as photonic band-gap materials (Urbas et al. [1999\)](#page-40-0) (See Chap. [10.](http://dx.doi.org/10.1007/978-3-319-39322-3_10))

#### 1.4 Types of Materials

In addition to copolymerization described above, there is considerable interest in the control of polymer architecture. As this may have a considerable influence on the behaviour of polymers as materials. Thus, polymers may be linear (Fig. 1.3a), or branched (Fig. 1.3b) or may for more complex structures such as a star arrangement (Fig. 1.3c) or more sophisticated dendrimer arrangements. Some of these more complex architectures pose considerable challenges to the organic chemist in terms of reagents and equipment (Hadjichristidis et al. [2000](#page-37-0)), while others, for example, the introduction of cross-links, can be achieved using technically quite simple methodologies. Cross-linked polymers are an important class of materials in themselves and provide another classification, namely thermoplastics and thermosets; The former are those which melt and flow, the latter are materials which cannot melt or dissolve and are built up of cross-linked polymer chains.



#### <span id="page-17-0"></span>1.4.1 Thermoplastics

In terms of production of polymeric materials poly(ethene) dominates with typically 30 % of polymer production worldwide, other significant materials are poly (propene), and poly(styrene) and poly (vinyl chloride), though the latter has prompted considerable environmental debate, in terms of the toxicity of the monomer, the use of plasticisers in the products (particularly those which come into contact with children) and the production of dioxins in the ultimate disposal by pyrolysis. The major advantage of the general class of thermoplastics is that they soften and flow on heating and thus can be processed using a range of simple methodologies, which rely on the solidification of the melt into a particular form. Examples of processing methodologies include blow moulding, injection moulding, extrusion and spinning (Stevens [1990](#page-39-0)). The ability to process the polymer through melting or (less usually) through dissolution also allows for the polymer to be recycled although in this regard additives either added for appearance as stabilizers or for improved properties may influence the range of options possible.

As thermoplastics do not contain covalent bonds between chains the mechanical properties of the resultant polymers are highly dependent on the intermolecular forces holding neighbouring chains together (vide supra). That being said it is the presence of crystalline regions which often produce the high mechanical strength of many polymeric materials. Thus, careful control of polyethene morphology can result in extremely high modulus materials (Ward and Hine [2004](#page-40-0)). It should also be noted that while crystallinity can impart high mechanical strength through the close regular alignment of neighbouring molecules, the presence of amorphous regions also provides some elasticity and impact resistance.

#### 1.4.2 Thermosets

Thermosetting polymers are those systems where a network of cross-linking between chains means that the polymer cannot be dissolved or liquefied on heating. In lightly cross-linked system, there may be considerable deformation allowed at the right conditions as in the stretching of an everyday rubber band, but ultimately the bonding of neighbouring chains restricts their translational motion. In highly cross-linked systems, the polymer may have considerable dimensional stability. In both cases, the ultimate form (leaving aside issues of applied forces) is determined at the time of cross-linking and to form useful products the cross-linking process must form part of the manufacturing process. One of the first commercially important synthetic polymers was Bakelite® (Baekeland [1909](#page-36-0)) which is a phenol formaldehyde resin, since these are the two components involved in its manufacture (Fig. [1.4](#page-18-0)). This material was extremely popular in the first half of the twentieth century for the production of a range of domestic and electrical goods.

<span id="page-18-0"></span>



#### 1.4.3 Composites, Micro-Fillers, Nano-Fillers

Increasingly a range of applications require polymers with enhanced performance. This has led to a further classification, namely between engineering and commodity polymers. The latter are those that are produced in high quantities as discussed in Sect. [1.4.1;](#page-17-0) the former are generally more expensive materials, which are manufactured on a smaller scale but are valued for certain superior properties, such as increased mechanical strength or thermal stability. Perhaps the best known example of an engineering plastic is Kevlar [II], which finds use in a range of applications including body protection.



Notwithstanding the remarkable properties of materials such as Kevlar, modern engineers are constantly looking for improved performance. One of the most successful areas in this regard is the development of composites; such materials are manufactured in such a way that the final material has superior properties to the sum of its constituents. For example, fibres of Kevlar, glass or carbon are used to reinforce epoxy resins. Increasingly developments are focusing on more sophisticated materials; for example, poly (ether ether ketone) can replace epoxy as the

matrix, and more complex reinforcing materials have been used for example carbon nanotubes (Coleman et al. [2006\)](#page-37-0). Indeed, the new Boeing 'Dreamliner' airplane introduced in 2014 is structural based around composite materials.

#### 1.5 Types of Order

#### 1.5.1 Crystalline

The crystalline state is a state of matter ideally characterized by three-dimensional, long-range order on an atomic scale. A crystallizable polymer is polymer that is able to partially crystallize (IUPAC [1997\)](#page-38-0). Large single crystals of polymers are not observed except in the case of polydiacetylenes as they can be prepared via a topochemical polymerization of the single crystals of the monomer. Single crystals of polymers such as polyethylene can be prepared from solution (Geil [1963\)](#page-37-0), whereas polymers crystallized from the melt phase contain both crystalline regions and uncrystallized amorphous material. The crystalline regions are in the form of chain folded lamellae (see Sect. [1.6\)](#page-20-0).

#### 1.5.2 Liquid Crystalline

A liquid crystal polymer is a material that, under suitable conditions of temperature, pressure, and concentration, exists as a liquid crystal mesophase (IUPAC). Liquid crystal phases are those characterized by a high level of orientational order in the absence of positional order as observed in the crystalline state. The nematic state is observed with rod-like molecules with a common axis of orientation as shown in Fig. 1.5.

Fig. 1.5 Schematic representation of the molecular order present in the nematic liquid crystal phase. The line represents the rod-line molecules



<span id="page-20-0"></span>In a polymer, the rod-like structures can be attached as side groups—side-chain liquid crystal polymers or with the skeletal backbone—main chain liquid crystal polymers (Donald et al. [2006\)](#page-37-0). The latter usually exhibit liquid crystal characteristics at elevated temperatures, while some side-chain liquid crystal polymers exhibit liquid crystalline order at room temperature. A number of more ordered smectic phases can be observed as well as chiral, nematic, and smectic phases (Donald et al. [2006\)](#page-37-0).

#### 1.5.3 Amorphous

The amorphous state is a state of matter characterized by the absence of long-range molecular order. Polymers exhibit this disordered but solid state either as a consequence of a thermal history which includes cooling from the melt state at a rate which inhibits crystallization or through the presence of disorder along the polymer chain such as present in random copolymers or atactic systems. Typically glassy polymers are optically clear and a key characteristic is the glass transition temperature. The transformation in molecular dynamics from that of a polymer melt to those of the glassy state does not occur over a very short temperature range as in the case of a first-order phase transition such as melting. Rather, it extends over several Kelvins and a plot of heat capacity of thermal expansion coefficient exhibits a smooth step. The glass transition temperature is defined by convention in which the heating rate is a critical factor.

#### 1.5.4 Blends and Mixtures

As with other material systems, different types of polymers can be mixed to provide control of properties. A polymer blend is a macroscopically homogeneous mixture of two or more different species of polymer [IUPAC]. The low entropy of mixing of polymers due to the high molecular weight means that different polymers do not readily form a homogeneous blend; rather they form mixtures with a phase separated structure whose morphology will depend on the preparation route. The presence of a solvent further complicates matters.

#### 1.6 Structuring Processes

#### 1.6.1 Crystallization

It may come as a surprise to many that a large number of the common plastic items in everyday use are semicrystalline. As the IUPAC definition states, 'A crystallizable polymer ... is able to partially crystallize.'

Crystallinity in polymers was first observed by X-Ray Diffraction even before these materials were understood to be polymers. Prominent examples were polysaccharides, especially cellulose (Herzog et al. [1920\)](#page-38-0) and stretched natural rubber (Katz [1925](#page-38-0)). This was before Staudinger's macromolecular concept was widely accepted (Morawetz [1995](#page-39-0)). By the time synthetic crystalline polymers such as polyethylene (in 1933) and nylons (in 1935) were developed, it was generally acknowledged that the unit cell of a polymer crystal was based on repeating monomer units, rather than on the whole molecules.

Polymer crystallization is dominated by the process of untangling molecules and then straightening them onto the crystal growth face. Because of this, it is a comparatively slow process compared with crystallization of simple molecular species, and it may require supercooling by tens of Kelvins to occur at a significant rate.

Not all polymers can crystallize. Polyethylene does, but atactic polystyrene (the common form) does not. Though the specialized syndiotactic and the more common isotactic forms do, albeit into completely different crystal forms (de Rosa and Auriemma [2013\)](#page-37-0). Isotactic polypropylene and many nylons commonly crystallize into more than one crystal type, and polyethylene terephthalate (PET), a polyester, is commonly found in a glassy form in soft drinks bottles but crystallizes readily on appropriate thermal treatment.

#### 1.6.1.1 Lamellae to Spherulites

Up to about 1955, the only widely held model of semicrystalline polymer morphology was the fringed micelle model. In this, polymer crystallites were composed of small stacks of parallel chains, outside of which chains wandered between crystallites rather than folding back into the same bundles. This model, however, did not fit well with the observation (Bunn and Alcock [1945\)](#page-37-0) that in polyethylene spherulites, the molecular chains lay perpendicular to the radial growth direction of the spherulites, nor with their suggestion that the crystallites might grow radially like the thin plate-like crystals of high molecular weight n-paraffins.

A great advance in the understanding of polymer crystals came with the discovery that polyethylene would crystallize from solution in hot xylene to give thin crystals, known as lamellae, which could be observed under the electron microscope. Electron diffraction showed that the chains ran more-or-less perpendicular to the plane of the crystals, and subsequent investigation has shown that this is the normal mode of crystallization for almost all polymers. These were reported by several workers, among whom Keller [\(1957](#page-38-0)) deduced that the chains must fold at the top and bottom surfaces of the crystals, so that the chain re-entered, going in and coming out of both surfaces. This had been suggested (Storks [1938](#page-39-0)) from observations of thin films of gutta-percha, which however did not contain isolated individual crystals.

Polymers on the trigonal and tetragonal systems tend to form lamellae based on their crystal system, hexagonal in the case of iPS and POM, square in the case of



Fig. 1.6 Shapes of polyethylene crystals grown from solution or melt under the conditions indicated

poly4-methyl pentene-1. Polyethylene on the orthorhombic system, when grown from solution, does produce lozenges with [110] faces as at a in Fig. 1.6. When grown at the higher temperatures truncated lozenges b are formed with [100] faces at each end. For progressively poorer solvents and at higher temperatures c, the [110] faces become increasingly dominant and curved, while from the melt d only these [100] faces are observed. This is consistent with the observation that in polyethylene, the radial growth direction of spherulites is along the b-axis (Bassett et al [1979\)](#page-37-0).

At the same time, as solution crystals were observed by electron microscopy, Fischer observed screw dislocations in electron micrographs of melt crystallized polyethylene-banded spherulites (Fischer [1957\)](#page-37-0), which have since been shown to be the primary mode of branching in polymer lamellae. This, together with splaying out of the plane of the original lamellae, forms the mechanisms of threedimensional growth into spherulites. From small initial lamellae, there develop objects which are generally called axialites because they were thought to be axially symmetrical like a wheatsheaf with splaying stalks. Where the initial crystal is of high symmetry, as in the hexagonal lamellae of isotactic polystyrene, intermediate stages of growth are often called hedrites because of their resemblance to mathematical polyhedra. These early objects, however, appear very different according to which direction they are viewed: this is particularly clear in the case of isotactic polystyrene (Bassett and Vaughan [1985\)](#page-37-0) and polypropylene (Olley and Bassett [1989](#page-39-0)).

The wide variety of the morphologies observed, both in crystals formed from solution and from the melt, including precursors to spherulites and more developed versions especially banded spherulites, are presented in 'Structure of Polycrystalline Aggregates', together with discussion of current theories of their formation, by Crist [\(2013](#page-37-0)).

#### 1.6.1.2 Crystal Growth Rates

Much effort has gone into the determination of crystal growth rates in polymers. In practice, this involves determining how fast spherulites grow, so what is determined is the fast growth direction for the polymer in question, for example, the b-axis in

polyethylene and the a\*-axis for the common α-form of polypropylene. This has led to a large number of theories of crystal growth in polymers.

#### 1.6.1.3 Primary and Secondary Nucleation

One early theory which is still widely applied is that of Hoffman and Lauritzen, in which a nucleus forms on a flat crystal surface. First proposed in 1961, in 1973 it was extended to include regimes of crystallization, initially two (Lauritzen and Hoffman [1973\)](#page-38-0), later extended to three. In Regime 1 (Fig. 1.7), a single molecular chain overcomes a nucleation barrier to settle on the growth surface, producing a step from which further chains can quickly be added. In Regime II at lower temperature, several chains and sideways development are simultaneously present on the same surface, and in Regime III growth is extending outward before completion of the first new layer. In the initial presentation of regime theory, there was observed an apparent correlation of 'axialitic' growth with Regime I and more classical spherulitic growth in Regime II; this was later shown to be a consequence of the different times available for chain fold reorganization in the two regimes (Abo El Maaty and Bassett [2006\)](#page-36-0). The theory was modelled on flat crystal growth surfaces, and received a strong challenge from the discovery of curved growth (Organ 1986). A strong attempt was made to bring both nucleation and curvature into line (Point and Villers [1992\)](#page-39-0) and modifications continued (Armistead and Hoffman [2002](#page-36-0)). A state-of-the-art review (Cheng and Lotz [2005\)](#page-37-0) provides an excellent starting point for further reading. Some recent theories dealing with both growth rate and crystal thickness involve the intervention of a mesophase as the first stage of crystallization: (Keller et al. [1994;](#page-38-0) Strobl [2005](#page-39-0)).







Regime I - Spreading rate much greater than nucleation rate

Regime II - spreading and nucleation rates comparable

Regime III - niche separation approaches stem width

Fig. 1.7 Diagram of crystal growth in Regimes I to III according to the Hoffman–Lauritzen theory

#### 1.6.1.4 Folding Theories

The question of folding resolves itself into three parts: (1) the topology of folding, whether chain folds back adjacent to itself, (2) the packing in the fold surface region, particularly how liquid or solid it may be, and (3) how frequently does the chain fold, a reciprocal space way of looking at how is lamellar thickness determined?

Regarding the first question, adjacent re-entry of stems into the same lamella is only approximated in solution crystals and material crystallized very slowly from the melt. On faster crystallization, stems are more likely to re-enter the same basal surface at some distance from where they emerged, known as the 'switchboard' model. Moreover, unless crystallization is slow enough for a molecule to reconfigure themselves in the melt by the process known as reptation, only local reorganization is possible as in the solidification model pictured below (Fig. 1.8) (Dettenmaier et al. [1980](#page-37-0)). The shape of the molecule as a whole will not be grossly changed, and so its radius of gyration will not be very different from what it was in the melt. Neutron scattering experiments do indeed show that radius of gyration is very little changed on fast crystallization from the melt, but in solution crystallized lamellae it is of the same order as the lamellar thickness, even for long molecules (Sadler [1984\)](#page-39-0).

From the melt, faster crystallization is known to produce a greater proportion of 'amorphous' in relation to crystalline material, to which an change to switchboardlike rather than adjacent re-entry is only one of several contributory factors. Where there is a large amount of inter-lamellar material, there is the possibility of much of this being similar in properties to the melt. However, near the crystal surface its motion is constrained, and its reduced mobility compared to the rubbery behaviour



Fig. 1.8 Crystallization according to the solidification theory (Dettenmaier et al. [1980](#page-37-0))

of material further away from the lamellae is to be expected. It is observed as an 'interphase' measurable by  ${}^{13}$ C NMR (Kitamaru et al. [1986\)](#page-38-0), and its existence as a rigid-amorphous' phase in poly(oxy-l,4-phenyleneoxy-l,4-phenylenecarbonyl-1,4 phenylene) (PEEK) though thermal analysis (Cheng et al. [1986](#page-37-0)). Fold surfaces do not necessarily remain as they are laid down, but in polyethylene are able to reorder subsequent to initial crystallization, this process determining the characteristic S-shaped cross section of lamellae formed at all but the highest crystallization temperatures (Abo El Maaty and Bassett [2001\)](#page-36-0).

#### 1.6.1.5 Computer Modelling Theories

Lamellar thickness, folding, and growth rate are all interconnected phenomena, and in order to understand the crystallization mechanism as a whole, a wide variety of methods, mostly based on molecular dynamics and related methods have been developed to simulate polymer crystallization. For an excellent discussion, on these the reader is directed to Chap. [4](http://dx.doi.org/10.1007/978-3-319-39322-3_4) and (Rutledge [2013\)](#page-39-0).

#### 1.6.1.6 The Bell Curve

In terms of bulk polymers, we have talked so far about crystallization 'from the melt': however, if a polymer is cooled rapidly enough from the melt, it may not crystallize but instead form a glass. For polymers in general, the crystallization rate as a function of temperature passes through a maximum (Fig. 1.9). The first report



Fig. 1.9 Rate of crystallization of natural rubber over a range of temperatures, according to Wood and Bekkedahl [\(1946\)](#page-40-0)

of this is attributed to Wood and Bekkedahl [\(1946](#page-40-0)) of dilatometric measurements of the crystallization of unvulcanized rubber in an unstretched state.

The best known case of this behaviour is polyethylene terephthalate (PET), which is most commonly encountered in the amorphous state as bottles. Whether heated from the glass or cooled from the melt, it will crystallize more rapidly the further below the melting temperature or the higher above the glass transition temperature, reaching a maximum from either side. Crystallization in polymers is a nucleation-controlled phenomenon: the graph above refers to overall degree of crystallinity, but if growth rate of spherulites is plotted, the maximum will be moved to somewhat lower temperature, since nucleation is denser at lower temperatures. The increase in growth rate while cooling from the melt is a thermodynamically based phenomenon, whereas the increase from the glass transition temperature is a result of decreasing viscosity.

In polymers which crystallize very rapidly, particularly polyethylene and isotactic polypropylene homopolymers, it is not feasible to cool quickly enough to obtain a glass (though with very thin films for some copolymers may be) so the full crystallization curve cannot be obtained for these materials.

#### 1.6.1.7 Nucleation

When crystallizing a polymer such as polyethylene or polypropylene isothermally, it is generally found that the number of spherulites nucleated in a given volume at close to the melting temperature at low supercooling is relatively few, but if the temperature of crystallization is reduced, more spherulites are nucleated. A similar effect is observed where the polymer is crystallized non-isothermally during cooling, with faster cooling rates leading to overall lower crystallization temperatures. One advantage of higher crystallization temperature that may be desired is the greater lamellar thickness and higher degree of crystallinity leading to a stiffer material. Nucleating additives may be used to bring this about, along with economy due faster processing times. The lamellae which constitute spherulites are generally birefringent, so the radial orientation of lamellae in spherulites generally makes polymer objects translucent or even opaque. (Poly 4-methyl pentene-1 is an exception since the refractive indices of its optic axes are almost the same; moreover, the density of crystal and amorphous phases is very similar.) Since spherulites are optically anisotropic reduction of spherulite sizes to sub-micron levels will reduce optical scattering: in such uses the nucleating agents are known as clarifiers: clarified PP articles may be effectively as clear as glassy polystyrene (see Chap. [5](http://dx.doi.org/10.1007/978-3-319-39322-3_5)). For a comparison of different nucleating agents, see Fillon et al. [1993.](#page-37-0)

#### 1.6.1.8 Crystallization in Practice

Polymer melts are not molecularly homogeneous. Even in homopolymers, there is polydispersity of molecular weights, while with copolymers there is almost always a variation of comonomer content between different molecules. In homopolymers,

fractionation by molecular weight during crystallization can occur, with longer molecules from the original dominant structure and short ones the subsequent infilling subsidiary structure. Much more pronounced effects are found in copolymers, where on continuous cooling molecules with less comonomer content crystallize first at higher temperatures, a range of subsequent melting points can be generated (Chen et al. [2004](#page-37-0)).

#### 1.6.1.9 Crystallization and Orientation

One factor not taken into account so far is orientation of the polymers. The effect on crystallization can occur in many ways. Transient crystallization on stretching of rubbers, observed for natural rubber by Katz [\(1925](#page-38-0)), is also found in certain synthetic rubbers (Toki et al. [2004](#page-40-0)).

A study by Zachmann and Gehrke ([1986\)](#page-40-0) of crystallization of oriented amorphous films shows that in PET orientation leads to faster crystallization and in polyamide-6 leads to formation of the γ-rather than the common α-phase.

The subject of crystallization from stressed melts has been reviewed (Kumaraswamy [2005](#page-38-0)) and one frequent occurrence in the time sequence of this crystallization is the formation of row nuclei which give rise to structures known as 'shish-kebabs'. Polypropylene is the polymer best known for its remarkable propensity for forming row structures, which often contain considerable amounts of β-phase material (Olley et al. [2014](#page-39-0)), and are a major feature of the skin-core structure of injection-moulded polypropylene (Shinohara et al. [2012\)](#page-39-0), but they are also found in polyethylene (An et al. [2006](#page-36-0)), isotactic polystyrene (Azzurri and Alfonso [2008\)](#page-36-0), poly(phenylene sulfide) (Zhang et al. [2008](#page-40-0)) and polylactide (Xu et al. [2013\)](#page-40-0).

Row structures are an instance of amplification of orientation in a specimen by crystallization onto oriented nuclei, but the other extreme is represented by highly oriented fibres, especially those of ultra-high modulus polyethylene (Abo El Maaty et al. [1999\)](#page-36-0).

#### 1.6.2 Microphase Separation and Block Copolymers (BCP)

In 1956, it was found (Szwarc [1956](#page-39-0)) that anionic 'living' polymerization could generate block copolymers. (These were not the first block copolymers to be prepared: in 1937 Otto Bayer had synthesized polyurethanes, and Pluronic® surfactants consisting of blocks of polyethylene oxide and polypropylene oxide were patented in 1954.) This method of synthesis went commercial when in 1961 Shell scientists, working to increase the green strength of polyisoprene rubber for tyre applications, discovered that by adding styrene monomer sequentially to the anionic polymerization of polyisoprene, strong thermoplastic elastomers were produced which required no vulcanization yet could be moulded into different

shapes with heat. The (typically) 20 % of polystyrene (PS) would segregate into small spherical regions, effectively vulcanizing the material, in place of chemical cross-links. (These materials were called Kraton® after Kratos, the Greek god of strength and brother of Nike.) In a sense, these were 'effectively composite' materials, similar in principle to semicrystalline polyethylene but with rubber elasticity in the 'soft' phase and the glass transition of the PS allowing the material to be stable up to the boiling point of water, whereas a PE of 20 % crystallinity would melt well below this.

Although we do not know the details of commercial synthesis, in the laboratory such a polymer would be synthesized in solution in a solvent such as tetrahydrofuran (Douy and Gallot [1972\)](#page-37-0) which would be a one-phase system. On removal of solvent, a simple mixture of polystyrene and polyisoprene would segregate into a two-phase blend with a coarse structure and poor mechanical cohesion, due to low entropy of mixing. When the two materials are joined in one molecule, however, the two phases are very limited in migration, and form a microscopic structure with the two segregated phases in close connection. An increase in domain size is promoted by the drive to minimize the surface area–volume ratio of the structure, which would reduce the interfacial free energy. However, growth is limited by the localization of the junction between chain segments at the domain boundary, and increasing domain size would also stretch the chains from their random coil (Gaussian) configurations leading to a reduction in entropy.

From 1970 reports started appearing that the segregated regions in block copolymers were organized in lattices of spheres, cylinders or lamellae, depending on the relative volumes of the components. Electron micrographs showing patterned spheres (Lewis and Price [1969](#page-38-0)), lamellae and cylinders (Mayer [1974\)](#page-39-0) and (Douy and Gallot [1972](#page-37-0)). Such techniques are usable only with thin films or thin cryosections, and generally require selective staining with reagents such as osmium tetroxide or ruthenium tetroxide.

The electron micrographs in Fig. 1.10 show the (left) (100) and (right) (111) projections of the BCC macrolattice for a styrene-butadiene diblock



Fig. 1.10 Electron micrographs of two projection of the BCC microlattice of a styrene-butadiene block copolymer (Thomas et al. [1987\)](#page-40-0)



Fig. 1.11 Small angle X-ray scattering of a series of polystyrene-isoprene diblocks (Hashimoto et al. [1980](#page-38-0))

(Thomas et al. [1987\)](#page-40-0). The dark circular regions labelled 1, 2, and 3 are polystyrene spheres deposited on the section to confirm the axis and magnitude of tilt between the two projections. Optical diffraction patterns are given in the bottom right inset of each figure.

The importance of projection can be seen here: a hexagonal pattern or an apparent lamellae pattern by itself could also arise from packed cylinders, but tilting would reveal the specimen for what it is.

Graft copolymers can also produce segregated domains, similar in appearance to block copolymers, but less regular (Price et al. [1974\)](#page-39-0).

Periodic structures can also be imaged by phase contrast (defocus) techniques, but these require care as artefacts are easily produced, especially from non-periodic structures, and it has been suggested that some reports concerning polyurethanes have been misinterpreted (Roche and Thomas [1981\)](#page-39-0).

Figure 1.11 shows small angle X-ray scattering from a series of polystyreneisoprene diblocks (labelling shows PS/PI segment molecular weights  $\times 10^{-4}$ ). Shows peaks both from the lattice arrangement of the PI spheres (simple arrows at lower S) and scattering function of the original spheres (open arrows at higher S). The lower S-values at higher molecular weights derive from the ability of longer Gaussian chains to fit into larger spheres, and from the smaller proportion of chain junctions in a given volume of material.

Originally, only the 'classical' set of phases was observed, spheres, cylinders and lamellae. With time and increasing refinement of both theory and experiment other configurations, stable and metastable, were predicted and observed. The ordered bicontinuous double diamond was observed in a star block copolymer (Thomas et al. [1986](#page-40-0)) and the gyroid in a diblock copolymer (Hajduk et al. [1994\)](#page-37-0). A recent theoretical calculation (Matsen [2012\)](#page-38-0) is shown at left in the figure below, and compared with experimental observations complied from different sources (Matsen [2002](#page-38-0)) (Figs. 1.12 and 1.13).

Models predict that block copolymers are not totally segregated, but that there is an interphase in which both components interpenetrate, which increases the conformational entropy of the two parts. In highly dissimilar polymers, this will be very limited in extent, tending towards the strong segregation limit, whereas if they are quite similar, in a 50:50 system the composition profile may be almost sinusoidal, towards the weak segregation limit.

Crystallization in BCP where one or more of the segments are crystallizable can and does occur. A particularly interesting early study was of polycaprolactone/ polyoxyethylene triblock copolymers PCL-PEO-PCL. Where one of the components constitutes a distinct majority, that one crystallizes (Perret and Skoulios [1972a\)](#page-39-0),



Fig. 1.12 Classical and non-classical block copolymer phases (Matsen and Bates [1996](#page-38-0))



Fig. 1.13 Theoretical and experimental phase diagrams for an AB-type block copolymer melt (left-hand figure reproduced from Matsen [\(2012](#page-38-0)) and the right-hand figure from Matsen ([2002\)](#page-38-0))

but where the two are in close to equal proportion, below  $51^{\circ}$ , PEO crystallizes first: above 52 °C, PCL crystallizes first: between 51 and 52 °C, they crystallize simultaneously (Perret and Skoulios [1972b\)](#page-39-0). In some systems, there is reported a conflict between microphase separation and crystallization, and spherulites of the crystallizable component may or may not form, depending on thermal treatment regime (Kim et al. [2001](#page-38-0); Balsamo et al. [1998](#page-37-0), [2003](#page-37-0)).

The ability to control the morphology of block copolymers renders them suitable for applications in fuel cells: especially ion-containing block copolymers, where one block is non-ionic and one or two blocks are based on aromatic sulfonic acids, hold promise as next-generation proton exchange membranes in hydrogen and methanol fuel cells (Elabd and Hickner [2011\)](#page-37-0). Connected ion-rich nanodomains are particularly helpful in increasing conductivity. Reviews of other applications include: optoelectronics (Segalman et al. [2009](#page-39-0)) nanolithography (Jeong et al. [2013](#page-38-0)) and solar cells (Topham et al. [2011\)](#page-40-0), which often employ donor–acceptor BCPs (Nakabayashi and Mori [2014\)](#page-39-0).

#### 1.6.2.1 Photonic Crystals

BCPs of low enough molecular weight to self-assemble easily generally only attain scales able to reflect green wavelengths. However, a block copolymer made of two similar brush copolymer segments, the only difference being a phenyl substituent at the end of one of the brushes, is able to self-assemble easily. The brush configuration allows the high molecular weight required for the appropriate scale to be achieved without significant entanglement, so that reflection onto the near infrared is achievable, the exact wavelength depending on (Miyake et al. [2012](#page-39-0)). See Chap. [10](http://dx.doi.org/10.1007/978-3-319-39322-3_10). Block copolymers can form not only photonic crystals, but phononic crystals, and even the possibility of the so-called phoxonic crystals combining both properties may be possible: a most instructive and informative review of recent developments gives some idea of the versatility of these materials (Lee et al. [2014\)](#page-38-0).

#### 1.6.2.2 Micelles

Block (and graft) copolymers can form colloidal aggregates, often in the form of micelles, in organic solvents if these are selectively poor for one of the polymeric blocks. Amphiphilic systems show surfactant behaviour in water and can exhibit micelle formation. The variety of block copolymer micelles is much too large to be explored here, but today they especially find widespread application in drug delivery systems (Gaucher et al. [2005](#page-37-0)) Amphiphilic block copolymers are particularly important in this regard, and a wide variety of nanostructures are formed (Letchford and Burt [2007\)](#page-38-0). An interesting historical note is that Pluronics, among the first block copolymers to be invented, are still the topic of active research (Alakhova and Kabanov [2014](#page-36-0)), in the example cited their use to sensitize cancer cells to chemotherapy.

#### 1.6.3 Phase Separation Mixtures

Whereas metals easily form alloys, polymers are generally encountered either unmixed, except for additives in small proportions or with completely different additions such as pigments or fillers or as composites. Single phase mixtures of two or more polymers are quite rare, though materials with two or more separate polymer phases are frequently used. Polymers generally are reluctant to mix intimately at the molecular level, for thermodynamic reasons.

Simple molecular organic compounds ('solvents' and 'monomers' in polymer parlance) generally have unfavourable (positive) enthalpy of mixing, but entropy of mixing is always positive and with a large number of molecules is comparatively large. So, chemically dissimilar species (as measured by the Hildebrand solubility parameter) are nevertheless able to mix. However, with oligomers and even more so with high polymers the number of molecules is considerably smaller and so is the entropy of mixing, tending to zero with 'infinite' molecular weight. Thus, even chemically quite similar species such as polyethylene and polypropylene will form a two-phase system in the melt. Even so, there are a considerable number of polymer pairs that are miscible. One common type is a polyester which has lone pairs of electrons with an electronegative halogenated polymer. Copolymers such as poly(styrene-acrylonitrile) also tend to be compatible with other polymers because of lower cohesive energy within the copolymer itself. Blends such as these display either upper or lower critical solution temperatures, depending on the specific kind of interaction between the two polymers (Tambasco et al [2006](#page-40-0)).

Figure [1.14](#page-33-0) shows the case of a two-component blend with a lower critical solution temperature (LCST). The figure shows (upper panel) the free energy of the system as a function of composition at a chosen temperature  $T_0$ , and (lower panel) the phase diagram for the system. Between the inflexion points  $S'$  and  $S''$  the curve is concave upwards, and the mixture will spontaneously separate into components of compositions  $B'$  and  $B''$ . Plotted against temperature on the phase diagram,  $S'$ and  $S''$  form a curve called the **spinodal** with  $B'$  and  $B''$  form the **binodal**. Inside the spinodal, the mixture is unstable, but in the metastable region between the two curves, nucleation is required for droplets of the minority phase to grow.

The two types of decomposition generate completely different micro-domain structures before they reach the ultimate equilibrium state. In the nucleation and growth process, the new phase corresponding to  $B'$  or  $B''$  takes the form of discrete small droplets in a matrix progressing towards  $B''$  or  $B'$ . When separation follows the spinodal decomposition process, an interconnected bicontinuous morphology develops, which possesses a characteristic length scale, determined by the fluctuation wavelength of fastest growth. The morphology gradually coarsens, and eventually the minority phase will separate into droplets. In practice, the types of morphology are easily distinguished, except at the most mature stages.

Where one of the components of a polymer blend is crystallizable, the process of crystallization will alter the liquid composition, and phase separation can in some circumstances be brought about (Tanaka and Nishi [1985](#page-40-0)). Regarding which

<span id="page-33-0"></span>

Fig. 1.14 Phase diagram of binary polymer blend with LCST (adapted from Higgins et al. [2010\)](#page-38-0)

polymer blends display LCST and which display upper critical solution temperature (UCST) behaviour, a recent theoretical treatment incorporating the segment–segment nonbonded interaction energy (White and Lipson [2014\)](#page-40-0) appears to approach the experimental situation much more closely than previous theories. Figure [1.15](#page-34-0) shows thermodynamic parameters for UCST (left) and LCST (right) behaviour. The  $T\Delta S$  (ideal mix) corresponds to what might be calculated from the traditional Flory–Huggins approximation.

When a polymer blend is sheared, and the molecules are stretched, there will be reduction in conformation entropy of the system. This in itself might apply equally to the mixed and unmixed states. However, in terms of enthalpy there is also the energy stored by the polymer molecules during flow, and this can have a significant influence on the magnitude and direction of the change in the phase boundary caused by shear. Computer simulations (Soontaranun et al. [1996\)](#page-39-0) have indicated that flow induces mixing when the excess stored energy is negative and phase separation when the excess stored energy is positive.

Even in a phase separated mixture, each phase will contain a proportion of both components. Where the majority component of one of the phases is crystallizable, crystallization can occur rapidly in that phase, but extend into the phase where it is the minority component. This can be observed in blends of polypropylene with

<span id="page-34-0"></span>

Fig. 1.15 Plots of thermodynamic parameters for mixtures exhibiting UCST (left-hand figure) and LCST (right-hand figure) from Lipson and White [\(2014](#page-38-0))

linear-low density polyethylene, held for a period above the melting point of the LLDPE (Dong et al. [1998\)](#page-37-0) and of polypropylene with non-crystallizable ethylene-octene copolymer (Svoboda et al. [2009](#page-39-0)). Where one component starts to crystallize in the compatible region of the phase diagram, the change in composition can cause the composition of the liquid to move into the binodal region, causing phase separation as in polycaprolactone/oligo-styrene blends (Tanaka and Nishi [1985](#page-40-0))

#### 1.6.4 Phase Separation on Reaction

Reaction Injection Moulding (RIM) is a technology that enables the rapid production of complex plastic parts directly from a mixture of two reactive materials of low viscosity. The materials are kept in separate containers until required, mixed in specific quantities and injected into a mould. This process allows large complex parts to be produced without the need for high clamping pressures. A large number of materials can be processed through the RIM process, such as polyurethane, nylon, epoxy resins and polyester systems. A typical RIM machine to produce polyurethane components is shown schematically in Fig. [1.16.](#page-35-0)

In comparison to injection moulding, the RIM process has many scales of structuring, chemical reactions at the smallest scale, products phase separating in to a morphology defined by the RIM operating parameters (Mateus et al. [2013\)](#page-38-0). Multiscale evaluation of the process reveals that the scale morphology is defined at an early stage of the process, long before complete reaction has occurred (Mateus et al. [2016](#page-38-0)).

<span id="page-35-0"></span>

Fig. 1.16 A schematic of the RIM process for polyurethanes

#### 1.7 Large-Scale Processes

The processes outlined above are driven by the forces which exist at the molecular level, a situation which is often described as bottom-up. Over the years, a number of techniques have developed which allows structures to be generated using a top-down approach.

Spin coating is a technique which is used to deposit a thin film of polymer on to a substrate, by spinning that substrate at high speed and introducing a droplet of a dilute solution on to the substrate. The spinning spreads out the solution and leads to high solvent loss leaving a thin film on the surface. This is widely used in the semiconductor industry in the patterning of silicon wafers to produce Large-Scale Integrated Circuits. Cardoso et al. ([2012\)](#page-37-0) have used multilayer spin coating to prepare thin films (300 nm to 4.5 μm) of PVDF.

It is generally found for a given solvent evaporation scenario that the film thickness h is related to the rotation speed  $\omega$  by a power law of the form

$$
h \propto \omega^{-b}
$$

where  $b$  is in the range 0.4–0.9 (Yimsiri and Mackley [2006\)](#page-40-0). The thickness of the films is also strongly dependent on the solvent evaporation rate.

Dip coating is another process for preparing thin films. A substrate is lowered into a solution and then pulled out at a constant and uniform speed. The film thickness is determined by the concentration and the removal speed. Film thickness for dip-coated films also follows a power law dependence on the withdrawal speed. The effect of the solvent evaporation is smaller than in the case of spin coating (Yimsiri and Mackley [2006\)](#page-40-0).
Multilayer extrusion is a technique developed at Case Western University by Professor Eric Baer. The technique involves the co-extrusion of different polymers and can achieve multilayer films without the use of solvents (Mueller et al. [1997\)](#page-39-0).

Electrospinning is a technique for producing nanoscale and microscale fibres from solution or the melt (Mitchell [2015](#page-39-0)).

Additive manufacturing/3D printing is a family of processes for building a component layer by layer from a digital definition file (Gibson et al. [2009](#page-37-0)). There are a variety of processes ranging from stereolithography to 3D printing. The latter is the subject of Chap. [7](http://dx.doi.org/10.1007/978-3-319-39322-3_7) and involves the deposition a liquid strand of polymer on to a moving stage which then solidifies to build up a 3D structure. The process can involve more than one type of polymer.

#### 1.8 Summary

Polymers are rich in molecular structure variation at the smallest scale of structure, i.e., the scale of covalent bonds and these can give rise to structure and morphology changes at much larger scales which have a major influence on the final properties. The following chapters develop these ideas in specific and important areas of research and technology. The next chapter provides an overview of the common experimental techniques used to study these multiple scales of structures.

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## Chapter 2 Evaluating Scales of Structures

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### 2.1 Introduction

The study of polymeric materials at several scales of structure will almost certainly require the use of a number of complementary techniques. This chapter provides an overview of the experimental techniques available for visualizing and evaluating polymer morphology. The chapter sets out to provide sufficient information to enable the reader to appreciate the research work described in the following chapters. Imaging techniques can provide invaluable information of many different scales. For the nanoscale, transmission electron microscopy is the technique of choice but at the expense of a much reduced sampling volume and more involved sample preparation. Recent developments in scanning electron microscopes, particularly in terms of field emission sources mean that nanometre resolution is readily available with the attendant advantages of the ease of screening large areas. However, as a surface topology technique we need to develop a contrast, which can be readily achieved using, for example, the etching techniques described in this chapter or through examination of a fractured surface. Scattering techniques probe a volume and in some cases information can be obtained in a time-resolving manner, so that the development of structure can be followed in real time. Neutron scattering provides a different contrast to X-ray scattering which can be useful with

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halogenated polymers or with metal fillers. Recent developments in pulsed neutron sources have resulted in instruments which can provide data in a single calibrated file over length scales from 0.1 to 10 nm. We also show how indirect methods such as thermal analysis can be used to obtain morphological data.

#### 2.2 Indirect Methods

#### $2.2.1$  $\overline{\mathcal{Q}}$

Differential scanning calorimetry (DSC) has two particular historical applications to polymers. One is the study of the glass transition (McKenna [1989](#page-77-0)) and the other is the study of crystallization and melting. Compared to simple molecular materials, polymer crystallization always involves considerable supercooling and a range of melting points depending on thermal history and relation to the thickness of the polymer lamellae, ideally as described by the Gibbs–Thomson equation. DSC is most often the technique of choice for observing both crystallization and melting and, ideally, there is a relationship between the two described by the Hoffman– Weeks equation (Hoffman and Weeks [1962\)](#page-76-0).

According to Hoffman nucleation theory (see Sect. [1.6.1](http://dx.doi.org/10.1007/978-3-319-39322-3_1)), if chains in a polymer crystal stayed as they were laid down, the crystal would melt almost immediately above its crystallization temperature (solid black line at  $45^{\circ}$  in Fig. [2.1\)](#page-43-0); however, following subsequent processes the lamellar thickness increases by a thickening factor β (2 in the case of polyethylene) giving a slope with its reciprocal y (here  $1/2$ ) in a Hoffman–Weeks plot. The theory of this is quite complicated, and the simple linear plot has been called into question (Marand et al. [1998\)](#page-77-0). Nevertheless, it suffices as a very practical guide to the use of DSC in relating thermal history of a polymer specimen to lamellar morphology.

Testing this relationship was often limited by the fact that for lower crystallization temperatures or at very fast cooling rates (such as found in many industrial processes), thin crystals were formed which on melting could rapidly recrystallize and remelt at higher temperatures (a process generally referred to as reorganization). With recent advances in technology with fast scanning instruments, such crystals can simply melt once, and lower crystallization temperatures are obtainable in the instrument itself. The Hoffman–Weeks relationship has recently been thus tested and found valid for polyethylene (Toda et al. [2014](#page-78-0)); in Fig. [2.1](#page-43-0) the blue diamonds represent conditions attainable in a traditional DSC and the red circles were obtained in a fast scanning calorimeter.

Many of the morphological phenomena in polymers with their concomitant calorimetric behaviour are well displayed in one material, namely isotactic polystyrene.

Figure [2.2](#page-43-0) shows the melting endotherm of an isotactic polystyrene specimen which has been fully crystallized at 175  $\degree$ C (Plans et al. [1984](#page-77-0)). The first peak I

<span id="page-43-0"></span>

Fig. 2.1 Hoffman–Weeks plot for polyethylene crystallized in a fast DSC. The symbol open circle represents melting by fast scan DSC after isothermal crystallization, filled circle represents melting after a constant cooling rate and *filled diamond* represents the melting of a conventional DSC after isothermal crystallization. The solid black line plots  $T_M = T_C$  (Part of Figure 6 reprinted from Polymer, 55(14), 3186–3194 Toda et al. Copyright 2014 with permission from Elsevier)



Fig. 2.2 DSC thermogram of pure isotactic polystyrene crystallized at 175 °C for 1 h. An exotherm feature appears between peak II and peak III (Scanning rate:  $1.25 \text{ °C/min}$ ). Adapted with permission from figure 3 in Plans J, MacKnight WJ and Karasz FE, Equilibrium Melting Point Depression for Blends of Isotactic Polystyrene with Poly(2,6-dimethylphenylene oxide), Macromolecules 17:810–814. Copyright (1984) American Chemical Society

shows the melting of secondary crystals formed after the main spherulitic growth has taken place. At peak II the main crystal population starts to melt, but the melt is able to recrystallize rapidly on the still partly solid material, giving the exotherm (shaded). The crystals subsequently formed are more stable, and finally they melt giving peak III, at a temperature where any potential recrystallization is too slow to



Fig. 2.3 PEEK crystallized from times stated (a) cooled after crystallization (b) reheated directly from the crystallization temperature (Reproduced with permission from Al-Raheil, Thesis, [1987\)](#page-75-0)

take place over the timescale of the experiment (Plans et al. [1984\)](#page-77-0). Lemstra et al. [\(1972](#page-76-0)) previously studied this behaviour and used the DSC not only as an analytical technique, but to prepare small specimens with precise thermal history.

Some early authors, particularly those working on poly ether ethyl ketone (PEEK), interpreted the secondary crystallization peak, which occurs just above the crystallization temperature, as being a primary crystallization peak which was subject to melting and reorganization during the scan. The phenomenon was interpreted and a second explanation presented clearly for other polymers by Yagpharov [\(1986](#page-78-0)). By reheating directly from the crystallization temperature, it could be shown that the lower melting peak developed subsequently, deserving the term 'secondary crystallization', and that the higher melting peak was a primary peak, possibly but not necessarily subject to reorganization. Figure 2.3 below is from work conducted at the University of Reading, UK using this technique, taken from the thesis of Al Raheil ([1987\)](#page-75-0).

Any interpretation is, however, dependent upon the effect of a crystal's environment on the kinetics of reorganization; in the case of PEEK, irradiation can be used to suppress reorganization kinetics (Vaughan and Sutton [1995](#page-78-0)) whereupon it appears more likely that the first-formed lamellar population is best thought of in terms of a continuous spectrum that spans the range contained between the apparently distinct primary and secondary DSC peaks. Something similar was proposed earlier (Lee and Porter [1987;](#page-76-0) Lee et al. [1989](#page-76-0)). But Lee and Porter's range of experimental observation was far too limited to categorically reject the occurrence of distinct secondary crystallization.

Secondary crystallization is widely accepted today. For example Lee et al. ([2004\)](#page-76-0) write:

... we propose that secondary crystallization involves the formation of short-range molecular order in the amorphous layers of the lamellar stacks as well as in the amorphous regions between the lamellar stacks. This short-range ordered structure, which is likely a type of single thin lamella, thin lamellae, or fringed micelle-like order, has a lower electron density than the lamellar crystal formed by primary crystallization.

but in ionomers at least Loo et al. [\(2005](#page-77-0)) have ruled out the fringed micelle suggestion.

#### 2.2.1.1 Reorganization and 'Morphological Melting'

Reorganization is a very common phenomenon and can often cloud the interpretation of DSC data. Partial melting and recrystallization of a polymer specimen, generally known as annealing, gives rise to thicker crystals with a higher melting point. For specimens crystallized rapidly, this process can take place within the time frame of a typical DSC scan, often 10 min at 10 K min<sup>-1</sup> in industrial use, typically up to eight times faster in a research laboratory.

A particular case in point is polypropylene. When isotactic polypropylene is crystallized at 145  $\degree$ C and above, all the material is sufficiently stable not to undergo reorganization at usual scan rates. Typically an endotherm such as in Fig. 2.4 is seen, curve 1 (Weng et al. [2003\)](#page-78-0).



Fig. 2.4 DSC melting endotherms of high crystallinity polypropylene (1) crystallized from the melt for 3 h at 145 °C, (2) partially melting scan (3) fully remelted after the partial melting: From figure 3, Weng J, Olley RH, Bassett DC and Jääskeläinen P, Changes in the Melting Behavior with the Radial Distance in Isotactic Polypropylene Spherulites. J. Polym. Sci. Polym. Phys. 41: 2342–2354. Copyright © 2003 by John Wiley Sons, Inc. Reprinted by permission of John Wiley & Sons, Inc



Fig. 2.5 Morphological effects of the recrystallization of isotactic polypropylene at 145 °C (a) radial growth enclosing a leaf-shaped area of cross-hatched material, (b) a similar area after partial melting (From figure 4 in. Weng J, Olley RH, Bassett DC and Jääskeläïnen P, Changes in the Melting Behavior with the Radial Distance in Isotactic Polypropylene Spherulites. J. Polym. Sci. Polym. Phys. 41: 2342–2354. Copyright © 2003 by John Wiley Sons, Inc. Reprinted by permission of John Wiley & Sons, Inc.)

This can then be partially melted (following curve 2) and the specimen quickly removed and quenched, so that the material has recrystallized in a much lower melting state (curve 3). The morphological effect can be seen in Fig. 2.5. The lower melting peak is seen to relate to daughter lamellae formed between the dominant ones, and especially to highly cross-hatched regions which melt out entirely.

If a typical isotactic polypropylene is crystallized to completion at a lower temperature, say 130 °C, and heated at 10 °C/min, only one peak appears, but if heated at 40 or 80  $\degree$ C/min, a double peak is observed. Even so, for polypropylene crystallized at 130  $\degree$ C, a traditional DSC cannot heat fast enough, but in unpublished work we have seen that if the specimen is melted in a heating bath at temperature between the two peaks and quenched, then similar morphological effects are observed. Yamada et al. [\(2003b](#page-78-0)) also give an example of partial melting to reveal morphological heterogeneity.

However, the advent of superfast DSC shows that at lower crystallization temperatures, the melting difference between the two populations becomes less significant, leading to a one-peak situation (Toda et al. [2014](#page-78-0)). This technique is ideal for investigating the equilibrium melting point of isotactic polypropylene, but careful work even with traditional DSC (Yamada et al. [2003a\)](#page-78-0) can be used to deduce reorganizational effect and thereby determine this temperature.

#### 2.2.1.2 Thermal Fractionation

Polypropylene is a particularly marked example of how even a relatively homogeneous homopolymer can crystallize isothermally giving a variety of crystal populations with different melting points. A phenomenon generally observed is that the first-formed lamellae, called dominant because they form the basis of the

spherulitic architecture, tend to be higher in melting temperature than the subsidiary ones which form later. The spread of melting points in the DSC (Gedde and Jansson [1983\)](#page-76-0) can be accompanied by solvent extraction and gel permeation chromatography (Gedde et al. [1983\)](#page-76-0) to show that in a homopolymer (in this case polyethylene) the crystallization process is accompanied by molecular fractionation, with the lower molecular weights crystallizing more slowly and being concentrated in subsidiary lamellae (Gedde and Jansson [1984\)](#page-76-0).

Fractionation during crystallization occurs in copolymers also, thinking particularly of those where one comonomer constitutes 90 % or more of the monomer mixture. In these there is generally molecular heterogeneity with some molecules having greater comonomer content than others. One example is the commercially available propylene-ethylene 'random' copolymers (Weng et al. [2004](#page-78-0)) but the most significant by industrial volume are the medium and linear low-density polyethylenes. Different groups have developed their own particular thermal fractionation techniques using the DSC to investigate the heterogeneity of these materials (Arnal [2001;](#page-75-0) Müller and Arnal [2005](#page-77-0); Shanks and Amarasinghe [2000;](#page-78-0) Chen et al. [2001\)](#page-75-0).

It also gives indications as to how much blends of two different grades of polyethylene co-crystallize in blends. Figure 2.6 below is a comparison of a blend of two branched polyethylenes: at left is the melting endotherm after simple cooling, at right after a thermal fractionation technique.



Fig. 2.6 Use of the thermal fractionation technique to study branching polydispersity. (Left) Specific heat curves of LLDPE–VLDPE2 blends after cooling at  $10^{\circ}$ C/min; (*right*) the same after thermal fractionation (Reprinted from Polymer 41: 4579–4587, Shanks RA and Amarasinghe G. Crystallisation of blends of LLDPE with branched VLDPE Copyright (2000), with permission from Elsevier)

The Vaughan and Sutton ([1995\)](#page-78-0) paper is an example of how DSC can also be used to probe molecular degradation following irradiation. This can occur without gross apparent changes to morphology as revealed by TEM/etching. The paper immediately following Vaughan and Stevens [\(1995](#page-78-0)) does the same for PET, which is similar to the above-mentioned isotactic polystyrene in crystallization behaviour, although the processes occur considerably faster. However, the most salient feature of that work was that PET is easily degraded by relatively small doses of irradiation, especially compared to the highly radiation-resistant PEEK.

#### $2.2.2$ **Dynamics**  $\overline{2}$

Dynamic Mechanical Thermal Analysis (DMTA) records the temperaturedependence of the viscoelastic properties and determines the modulus of elasticity and the damping values by applying an oscillating force to the sample. Changes in the morphology such as crystallization and phase separation change the viscoelastic properties. For example, Zheng et al. have used DMTA techniques in conjunction with infrared spectroscopy (see Sect. 2.2.3) to study the interactions in semiinterpenetrating polymer networks (Zheng et al. [2013](#page-79-0)). Dielectric spectroscopy measures the dielectric properties of a sample as a function of frequency. It is based on the interaction of an external oscillating field with the electric dipole moment of the sample. It is a technique for polar molecular systems and has been widely used to study molecular relaxations. Nanocomposites have a significant interfacial area and this has a substantial impact on the dielectric properties and hence dielectric spectroscopy is a very useful tool. A recent example of this concerns the study of a nanosilica/polyethylene system, where due to the lack of strong coupling between the applied field and the materials themselves, water was used as a dielectric probe. Since the solubility of water in polyethylene is extremely low, water molecules tend to associate with residual hydroxyl groups on the nanosilica surface, such that changes in surface structure and interfacial interactions manifest themselves as modified relaxation peaks within the so-called water shell (Lau et al. [2013](#page-76-0)).

#### 2.2.3  $\overline{1}$   $\overline{1}$   $\overline{2}$

Many different spectroscopy techniques can be used to provide structural information concerning polymers. In terms of vibrational spectroscopy, Strobl and Hagedorn [\(1978](#page-78-0)) showed how the Raman spectrum of polyethylene could be considered in terms of characteristic bands associated with the crystalline phase, a melt-like amorphous phase and a disordered phase of anisotropic nature. Comparison of structural data obtained in this way with equivalent measures obtained by densitometry and X-ray scattering revealed agreement. Similar approaches have

been used to evaluate the crystallinity of isotactic polypropylene (Nielsen et al. [2002](#page-77-0)).

Nuclear magnetic resonance spectroscopy is a well-established chemical characterization technique widely exploited with polymer solutions to quantify the chemical microstructure of polymer chains (Bovey [2007\)](#page-75-0). Developments in NMR technology and computing led to the development of solid state NMR. This enables site-specific information to be obtained from the solid state. This uses interactions like the dipolar coupling and chemical shift anisotropy to extract information from the solid state. More recently, multidimensional spectroscopy (2D and 3D techniques) correlate a structural parameter such as the chemical shift with parameters that carry information about dynamics and the level of order. Solid state NMR is often seen as strongly connected with crystallography as it provides similar precision information albeit of site-specific interactions and their distances (Schmidt-Rohr and Spiess [1994\)](#page-77-0). As introduced in connection with dielectric spectroscopy, the nature of the interface between polymers and nanoparticles is an area that is of considerable interest and many different spectroscopies have been used to explore this. For example, Miwa et al.  $(2008)$  $(2008)$  used electron spin resonance (ESR) spectroscopy to examine nanocomposites of poly(methyl acrylate) (PMA) and synthetic fluoromica, in which the PMA had been modified to include a nitroxide spin label. That is, a stable free radical introduced into a material that does not have an intrinsic paramagnetic response. This work demonstrated that, in exfoliated systems, the close proximity of the polymer chains and exfoliated fluoromica reduces the PMA chain mobility within a rigid interface region of thickness 5–15 nm.

#### 2.3 Imaging Methods

Imaging techniques provide invaluable information on the morphology of polymers and nanocomposites. Of course an imaging technique is able to provide information on the spatial distribution of the structure and morphology. Each of the techniques considered here has particular advantages as well as specific sample preparation requirements. It is probable that the techniques employed in a particular project are selected as a consequence of the resolution matching the requirements, otherwise all techniques should be considered useful and effective especially when used in combination.

#### 2.3.1  $\frac{3}{2}$

The optical microscope is typically used to reveal structures between 1 μm and 1 mm in size. Although the most intricate details of polymer morphology are revealed by the transmission electron microscope, and to some extent the scanning electron microscope and atomic force microscope, these tiny structures are usually

<span id="page-50-0"></span>

Fig. 2.7 (a) Spherulites in a thin film of polypropylene (Elaine Ann Perkins, University of Reading, UK, unpublished work, 1985), (b) spherulites in polyhydroxybutyrate-co-valerate (Reprinted with permission from Macromolecules, 2010, 43: 4441–4444 Wang Z, Li Y, Yang J, Gou Q, Wu Y, Wu X, Liu Pand Gu Q ([2010\)](#page-78-0) Twisting of Lamellar Crystals in Poly (3-hydroxybutyrate-co-3-hydroxyvalerate) Ring-Banded Spherulites Copyright (2010) American Chemical Society, (c) Schematic of spherulite twisted orientations. Redrawn from Hsieh et al. ([2014\)](#page-76-0)

aggregated into larger structures; for example, the spherulites in Fig. 2.7a (left) are composed of lamellae which require electron microscopy for their resolution, but the variation in size and spatial distribution of the spherulites is much more easily studied by optical microscopy.

Optical microscopy involves a variety of different techniques, and a survey of these will illustrate the breadth of applications to polymer morphology.

The methods of specimen preparation for optical microscopy are various. In fundamental polymer studies, thin films of polymers can be crystallized between a slide and cover slip. In an apparatus such as a hot stage attached to a microscope, the crystallization process can be followed as it occurs. However, two features must be taken into account, firstly that in specimens where large spherulites form, their centres are confined to a narrow plane and are not distributed in depth as they would in a bulk specimen. Also, nucleation of crystal growth may be enhanced on the surface of the slide and cover slip, and transcrystalline layers, rather than the spherulitic structure of the bulk material, may form.

Most often, sectioning is required to examine structure of the material as a whole. For example, there will be great variation in morphology of an injection moulded item between the rapidly chilled surfaces where the polymer came in contact with the cold mould, and the interior where heat was lost much more slowly. However, sections do not have perfectly flat parallel surfaces; the most common form of damage is periodic compression giving rise to 'chatter', though with an inferior blade knife marks parallel to the cutting direction also occur. Interference from these can be greatly reduced by immersing the specimen in a liquid with a refractive index close to that of the polymer. For aliphatic polymers, glycerol  $(n = 1.47)$  is often a good general purpose liquid, since it is not taken up except by the most polar of polymers such as hydroxyethyl acrylate. For aromatic polymers such as polystyrene, Traylor ([1961\)](#page-78-0) dissolved potassium mercuric iodide in the glycerol to increase its refractive index, and there are now many commercial index matching fluids. Sections can also be compressed in such a way that originally circular features such as the bands in spherulites are distorted into ellipses; such distortion is accompanied by an overall background birefringence.

#### 2.3.1.1 Polarized Optical Microscopy (POM)

One of the earliest and most commonly used microscopical methods of examining polymers is between crossed polarizers. Some of the earliest work was determining the birefringence of fibres, then came the study of spherulites in semi-crystalline polymers. Often the spherulites show a simple 'Maltese Cross' pattern where the dark areas show zero-amplitude birefringence, which simply arises from the orientation of the crossed polars. In the polypropylene spherulites (Fig. [2.7a\)](#page-50-0), radial growth has occurred along the a\*-axis which is the fastest crystal growth direction, while the b- and c-axis are effectively randomly oriented.

Often, however, the spherulites develop with a twisting orientation (though the individual lamellae are not necessarily twisted) producing a banded pattern when observed under POM. This is illustrated in Fig. [2.7c.](#page-50-0) For example, in polyethylene the b-axis forms the radial growth direction, but under certain growth conditions the a- and c-axis rotate about the radius with increasing distance from the centre. In polyethylene, the crystals are effectively uniaxial, with the higher refractive index along the chains, namely the c-axis. Looking down at A, the two different refractive indices along b and c cause the crystal to show birefringence. Looking down the c-axis at B, the refractive indices along a and b are effectively equal. This gives a simple alternation of light and dark bands, with the dark representing zerobirefringence extinction. Many other polymers, including many polyesters, are biaxial, and often show double banding (Wang et al. [2010](#page-78-0)) as observed in Fig. [2.7b](#page-50-0).

Figure [2.8](#page-52-0) (Kumaraswamy [1999](#page-76-0)) shows how POM can display orientation and structure gradients in injection moulded materials. These images show polypropylene crystallized in a cell designed to probe the different variables (time, temperature, shear rate) found in this process, and the two parts of the figure illustrate the formation of the characteristic skin-core morphology. The oriented near-skin region

<span id="page-52-0"></span>

Fig. 2.8 Optical micrographs of sections through injection moulded polypropylene from figure 4 in Kumaraswamy, [1999](#page-76-0) (c) viewed down the neutral direction (d) viewed down the flow direction Reprinted with permission from (G. Kumaraswamy, A.M. Issaian, and J.A. Kornfield Shear-Enhanced Crystallization in Isotactic Polypropylene. 1. Correspondence between in Situ Rheo-Optics and ex Situ Structure Determination, Macromolecules, 32, 7537–7547). Copyright (1999) American Chemical Society

appears bright when viewed down the neutral direction (c) and dark when viewed down the flow direction (d) indicating that the skin has crystallites with the cylindrical symmetry characteristic of polypropylene row structures.

#### 2.3.1.2 Use of Tint Plates

A bright appearance between vertically and horizontally cross polars indicates that, in the diagonal directions, one refractive index is greater than the other, but does not indicate which is which. The ambiguity can be resolved by use of tint plates, of which the first-order compensation plate (quartz sensitive tint) is the most popular. This shifts one component of the beam by one green wavelength (550–580 nm), so that without a specimen, green light destructively interferes, and mainly red and blue are observed, giving rise to the characteristic magenta colour. One direction of the plate will be marked as slow or positive, and if the higher refractive index is parallel to this, a higher order blue interference colour will be produced, while if it is perpendicular, a lower order yellow colour will be seen.

Spherulites of aliphatic hydrocarbon polymers such as polyethylene generally have their molecular chains with the highest refractive index oriented perpendicular to the radial growth direction. This is the case with the polypropylene spherulites shown in Fig. [2.9a](#page-53-0), which were crystallized at 140  $^{\circ}$ C and consequently contain very few cross-hatched lamellae, so in this respect they are like polyethylene spherulites. The lower refractive index in this view is radial in direction, giving a yellow colour where the radius is parallel to the slow direction of the tint plate; these are therefore termed negative spherulites.

In Fig.  $2.9b$ , the specimen was crystallized at 120 °C, so that there is a preponderance of cross-hatching lamellae located roughly perpendicular to the dominant radially growing ones. This reverses the birefringence, giving positive spherulites

<span id="page-53-0"></span>

Fig. 2.9 Showing use of Quartz sensitive tint. (Left) polypropylene crystallized at 140 °C ( $-ve$ spherulite); (right) various orientations in film transcrystallized at 120 °C (+ve spherulites with ve beta inclusion) (Reproduced with permission from White HM, University of Reading thesis, 1995)

in the majority  $\alpha$ -phase. However, the isolated inclusion of the  $\beta$ -phase in the transcrystalline layer (t) does not contain any cross-hatching, and it displays strong birefringence characteristic of a negative spherulite.

One hydrocarbon polymer that gives positive spherulites is isotactic polystyrene; here the effect of aromatic rings with strong polarizability perpendicular to the molecular chains dominates over the polarizability of the chain.

Another form of tint plate commonly used is the mica quarter-wave plate with a retardation of 140–155 nm. This gives a grey background becoming brighter or darker with the birefringence of the specimen, and is suitable for black-and-white imaging.

#### 2.3.1.3 Circularly Polarized Light

Dark areas observed in the use of crossed polarizers by themselves can be due to zero-amplitude or zero-birefringence extinction, and sometimes it is advantageous to remove the zero-amplitude extinction. This can be achieved by including a pair of crossed quarter-wave plates in the optical path (Olley and Bassett [1989\)](#page-77-0). When a spherulitic sample is observed in the way, the dark Maltese cross is no longer part of the picture, and one can see the spherulites as bright objects with their mutual boundaries much more clearly displayed. This is particularly helpful when looking at the early stages of spherulitic growth, where the growing object takes a form often called a 'hedrite' or 'axialite', or in the special case of isotactic polypropylene, a 'quadrite'. Figure [2.10](#page-54-0) shows a film of polypropylene with quadrites in various orientations, with the top picture displayed in circularly polarized light. The object at top left is seen in one of the 'cardinal' views, with the b-axis of the earliest formed crystals pointing towards the observer. Without the Maltese cross, the fourfold rosette form of the object is clearly displayed. Moreover, the dark 'leaflike' structure at the centre is a characteristic feature of the development. However,

<span id="page-54-0"></span>Fig. 2.10 Use of circularly polarized light (top) and phase contrast (bottom) to show development of polypropylene spherulites at 150 °C (Reprinted from Polymer 30: 399–409, Olley RH and Bassett DC. On the Development of Polypropylene Spherulites, Copyright (1989), with permission from Elsevier)



the general brightness indicates that over most of the object, the optic axis lies in the plane of the film, perpendicular to the b-axis. The two objects beneath appear very dark and sheaf-like in form, but were they developing freely in a bulk specimen they would be the same in form as the one above, but with their b-axis located in the plane of the film, and their optic axis (effectively the c-axis) pointing towards the observer.

Where spherulites of more than one crystal phase are growing together, use of circularly polarized light makes delineating and distinguishing the different types of object much easier (He and Olley [2000](#page-76-0)).

#### 2.3.1.4 Phase Contrast Microscopy

This refers to the technique invented by Zernike, which makes visible the phase shifts produced in a transparent specimen by local variations in refractive index. For the technique as applied to polymers, see Hemsley [\(1989](#page-76-0)), Chapter 2; for a description of how the technique works, see Murphy and Davidson ([2012\)](#page-77-0), Chapter 7.

An ideal phase contrast specimen is either a well-prepared section or a thin film melted between slide and cover slip. Much of the problem of knife marks or other surface structure in sections and thin films can be alleviated by 'oiling out' with a suitable liquid (Traylor [1961](#page-78-0)).

The method is very suitable for examining particle dispersions and inclusions, especially the rubbery inclusions in toughened plastics. The method is sensitive, and does not involve polarized light, so can reveal features in specimens with overall or localized orientation which might be lost where there is strong birefringence contrast. An example is the clear revelation of the outlines and some internal structure in the early development of polypropylene spherulites, as in the lower part of Fig. [2.10](#page-54-0). However, a halo is produced around the objects picked out, and where there is a large concentration of particles, or in thicker specimens, the overlapping haloes can confuse the picture.

An early application was the examination of polyethylene crystals formed from dilute solution, which are 'phase objects par excellence' (Keller [1968](#page-76-0)). As is generally the case, the technique proved an ideal precursor to electron microscopy (Keller and Bassett [1960\)](#page-76-0). Quite recently, the technique has been used to observe the development of the earliest stages of polypropylene crystals directly in the melt (Yamada et al. [2011\)](#page-78-0).

#### 2.3.1.5 Interference Microscopy (Nomarski)

There is a variety of techniques which come under the heading of interference microscopy, and one early example is the determination of the thickness of single crystals with a two beam microscope (Wunderlich and Sullivan [1962](#page-78-0)).

However, the most widely used type of interference microscopy is that giving Differential Interference Contrast (DIC), widely known as Nomarski contrast.

The Nomarski technique is directional, because the very small separation of the two beams, about 1 μm, samples small differences in height along the splitting direction only. So, for example, if one is examining a piece of polypropylene tape whose surface is covered with ridges parallel to the tape length, then if the specimen is rotated so that the ridges are perpendicular to the beam separation, they will appear heavily contrasted, but if they lie parallel, then they will almost disappear.

In the system used by the author, the two beams were separated along a diagonal in the field of view. Figure 2.11 shows how they could be used to determine whether a blemish in an otherwise flat surface was a pit or a dome.



Fig. 2.11 Appearance of domes and pits in an otherwise flat surface under Nomarski: for description see text

Normally the microscope can be adjusted so that, on a flat surface, the two beams were out of phase by 1 wavelength of green light, so that the surface appeared first order purple (the same colour as given by a quartz sensitive tint). Higher or lower order colours appeared according to whether the slope on the element of surface being sampled increased or decreased the phase difference. At right, the microscope is adjusted to give a smaller path difference, grey on the Newton colour scale, and this configuration is suitable for black-and-white photography.

This technique works very well for solution-grown crystals, but much better contrast is achieved if a reflective gold (or carbon) is applied. If the crystals are deposited on mica and carbon coated, they can be floated off for electron microscopy.

Where the surface itself is of interest, this is the technique par excellence. For example, blown polypropylene films used in food packaging sometimes show submillimetre 'haze rings', which degrade their appearance. These were studied by, among other techniques, Nomarski reflection, and related to the presence of defects in the polypropylene tube prior to blowing (Olley and Bassett [1994\)](#page-77-0).

One very productive use of Nomarski contrast is examination of etched surfaces prior to electron microscopy. Here one does not want to coat the specimen, so in looking at an etched disc prior to replication, it is better to put it on some black card (surface to be replicated uppermost) to eliminate much of the scattered and reflected light from below.

Figure 2.12 shows (a, left) a micrograph (crossed polars) of section from a specimen of poly ether ether ketone (PEEK) taken as it was being prepared for etching, and (b, right) the etched specimen examined under Nomarski contrast. First



Fig. 2.12 Section of PEEK film and etched stub from which section was taken (Reprinted with permissions from Al-Raheil IAM, University of Reading thesis, 1987)

to notice is the strong correspondence between the morphology of the section and the etched morphology, though it is not exact because of a small depth difference in the specimen. The asterisks at the top mark a pair of 'comet-like' spherulites which are easily discerned in both views.

This pair was taken during the development of the etching procedure, and besides the spherulitic morphology displays some small artefacts (arrowed) which were eliminated with the reagent as eventually published.

This technique is also very useful for examining replicas of etched specimens after they have been extracted and placed on number grids, enabling one to locate specific features under the transmission electron microscope.

#### 2.3.1.6 Ancillary Techniques

One advantage of optical microscopy is that it is easily used in conjunction with ancillary techniques, where heating, stretching and other processes are applied to the specimen. Various manufacturers supply hot stages in which the specimen can be studied while being heated or cooled, allowing direct observation of crystallization and melting processes, and phase separation in blends (Shabana et al. [2000\)](#page-78-0).

As well as simple mechanical testing, it is also possible to study the evolution of morphology under shear conditions, again both in terms of crystallization (Shen et al. [2013](#page-78-0); Chan and Gao [2005](#page-75-0)) and phase separation and ordering in blends (Lin et al. [2012](#page-77-0); Zou et al. [2012;](#page-79-0) Trindade et al. [2004;](#page-78-0) Kielhorn et al. [2000](#page-76-0)).

In the authors' experience, the optical microscope is an invaluable first port of call, even when the target is the finest level of morphology only resolvable by the transmission electron microscope. It is best to start with a very low-power objective, and to move to higher ones. This practice can show up variations in structure throughout a specimen which might totally be missed when going straight to the higher power technique. In addition, sometimes it becomes apparent that what one is looking at is not what one is looking for; it may reveal films or deposits of foreign material, or even that the specimens may have been mixed up. To quote from Hemsley [\(1989](#page-76-0)): 'In no sense is the light microscope the poor relation of the electron microscope, neither is the latter to be considered by the light specialist only when all else fails .... One hesitates to insist that any examination with an electron microscope should be preceded by light microscopy, but polymer science and technology would benefit if this were a more frequent procedure'.

#### 2.3.2  $2.2$  Scanning Electron Microscopy

Scanning electron microscopy (SEM) is a widely available technique in which a fine electron beam is rastered across the sample surface. The electrons interact with atoms in the surface component of the sample, producing various signals (Fig. [2.13](#page-58-0)) that can be detected and that contain information about the sample's surface

<span id="page-58-0"></span>

topography and composition. The electron beam is generally scanned in a raster scan pattern, and the beam's position is combined with the detected signal to produce an image. The so-called secondary electrons are the most commonly used signal. These are produced by excitation of atoms close to the sample surface or in the gold coating often applied to insulating samples to dissipate the build-up of charge. These electrons are of low energy and hence originate in the surface layers. In contrast, the back scattered electrons, electrons from the incident beam that have been scattered by the atoms in the sample, are of high energy and may come from much deeper in the sample as shown in Fig. 2.13. In this case, the efficiency of scattering depends on the atomic number, the larger the value of Z the greater the scattering. As a consequence, an image formed from back scattered electrons may reveal elemental composition variations which can be helpful in revealing the structure of composites. However, due to the larger interaction volume, the resolution of the image will be lower than that formed using secondary electrons. The electrons in the probe beam can excite characteristic X-rays from the atoms in the sample. Which X-rays are excited will depend upon the accelerating voltage. With a suitable energy dispersive X-ray detector images can be formed from the distribution of particular elements in the sample. Again because the interaction volume is large, the resolution of the image will be lower. Recently techniques have been developed which provide for elemental imaging at the nanoscale.

#### 2.3.2.1 Contrast

As the SEM is a topological technique, we need to reveal the morphology of the sample. If there are compositional variations, then the images formed by characteristic X-rays or by back scattered electrons may suffice. However, if this is insufficient, another very common approach is to prepare a fractured surface. Here the samples are broken under brittle conditions, often by first freezing in liquid nitrogen, then fracturing to reveal the variation in morphology. For polymer blends and mixtures, the staining technique often used in TEM (discussed under TEM) may be helpful in providing a contrast to discern between materials. Another approach is to etch the surface, preferentially removing material and revealing the underlying morphology. The etching technique is described in the following section.

#### 2.3.2.2 Sandwiching and Embedding Techniques

While often simply exposing a microtomed surface is sufficient for the purpose, sometimes specimens require support, especially thin films which cannot stand by themselves and where the top and bottom layers would be removed by the etchant. Sandwiching techniques have been developed, whereby the top and bottom surfaces are supported and protected by a material which can be etched along with the polymer specimen. An example is a work on woven polypropylene tapes, both before and after consolidation (Jordan et al. [2003\)](#page-76-0).

Fibre and weaves can be embedded in a mounting medium which can be etched along with the polymer composing the fibre (Abo El Maaty et al. [1999\)](#page-75-0). Details of such a technique are shown in the Fig. 2.14 below.

In the micrographs below, an original weave is shown in a sandwich. At left, A is the high-impact polystyrene and B is the epoxy resin (Fig. [2.15\)](#page-60-0).

At right, in the regions marked C, one tape is emerging, so an etch cross-section of the tape is seen. At D, another tape is running parallel to the surface.



Fig. 2.14 A comparison of two sandwiching techniques, applicable to solid specimens (*left*) and those with open texture (right). Adapted from Jordan et al. [\(2003](#page-76-0))

<span id="page-60-0"></span>

Fig. 2.15 SEM of etched polypropylene weave specimens, showing (left) sandwiching technique (right) different structures of polypropylene tapes in transverse and longitudinal directions (Image taken by Robert Olley, 2003, University of Reading, UK. The specimen was provided by the University of Leeds)

#### $2.3.3$  $\overline{a}$

Both SEM and TEM (to follow) generally require some preparation to make the morphology visible. The etching technique is equally applicable to both, and so is included here between the two sections.

Etching of polymers is very similar to the process in metallography, where a surface is treated with a chemical agent to reveal the underlying phase or crystalline structure, which are then studied under the electron or optical microscopes. A variety of etching procedures are reviewed in (Bassett et al. [2003](#page-75-0)).

Most etching techniques involve a liquid etchant. Most commonly used are permanganic reagents, generally consisting of a dilute solution of potassium permanganate in a mixture of sulfuric and orthophosphoric acids, either dry or with a certain amount of water. Different compositions are suitable for different classes of polyethylene (Shahin et al. [1999\)](#page-78-0), other polyolefins (Patel and Bassett [1994](#page-77-0); Weng et al. [2003,](#page-78-0) [2004\)](#page-78-0), isotactic polystyrene (Bassett and Vaughan [1985](#page-75-0)), PEEK (Olley et al. [1986](#page-77-0)), etc. This is the most common of the oxidizing etchants, though chromic reagents are also used. Polyesters are generally treated with an alkaline reagent, typically a solution of potassium hydroxide in an alcohol.

Etching of a semi-crystalline polymer can be visualized by a simple model of plate-like crystals embedded in a rubbery matrix. Three etching rates are observed: the fastest etching is the removal of the amorphous polymer constituting the matrix; the broad basal surfaces of the plate-like crystals are almost totally resistant to etching, but the thin side-surfaces are eroded at an intermediate rate (Fig. [2.16\)](#page-61-0). This is described more fully in Olley [\(1986](#page-77-0)).

The morphology of banded spherulitic polyethylene as in Fig. [2.17](#page-61-0) (left) illustrates this well. The orientation of crystals rotate periodically along the spherulite radius; at A the resistant basal surfaces of the crystals are seen standing proud of the general etched plane; at B the lamellae are displayed edge-on, so are somewhat less

<span id="page-61-0"></span>



Fig. 2.17 (Left) etched banded spherulitic polyethylene (From figure 6c in, Shahin MM and Olley RH. Novel Etching Phenomena in Poly(3-hydroxy butyrate) and Poly(oxymethylene) Spherulites. J Polym Sci Part B: Polym Phys 40: 124–133. Copyright © 2002 by John Wiley Sons, Inc. Reprinted by permission of John Wiley & Sons, Inc.); (*right*) Original caption: TEM micrographs showing the morphology of sample BPA 124/20 (20 % LPE). It is clear that distinct boundary regions exist between the lamellar aggregates that grow at  $124 \text{ °C}$ . J. Mater. Sci.,1997, 32, (17), 4523–31, Structure-property relationships in polyethylene blends: the effect of morphology on electrical breakdown strength. Hosier, I. L., Vaughan, A. S. and Swingler, S. G, Figure 8 Reprinted with kind permission from Springer Science and Business Media

resistant to the etch. The amorphous regions are more highly etched, and lie below the protruding crystalline parts (Shahin and Olley [2002\)](#page-78-0).

The specimen at right in Fig. 2.17 is an example of crystallizing a polyethylene blend as a proposed cable material under a controlled thermal regime in order to optimize the morphology in regard to electrical breakdown behaviour (Hosier et al. 1997). We have included a TEM image here as the higher resolution is useful

in identifying the features. Large spherulitic objects made largely of high-density PE are revealed in a matrix where low-density PE predominates.

Etching is used to display not only semi-crystalline morphology, but also multiphase structure in polymer blends which may be totally non-crystalline. An early example is work on high-impact polystyrene and similar materials by Bucknall et al. ([1972\)](#page-75-0). From the abstract: 'These techniques reveal details of orientation in injection mouldings, of internal structure in composite rubber particles, and of crazing and shear band formation. The etch method avoids the specimen distortion inherent in sectioning'. A more recent example is one following the spinodal decomposition of blends of tetramethyl polycarbonate and polystyrene (Shabana et al. [1993\)](#page-78-0). During blend decomposition, one or more of the components may crystallize, and the crystal morphology as well as the phase structure can be observed, for example, in a phase-separating copolymer of polyethylene naphthoate with polyhydroxybenzoate (Shabana et al. [1996](#page-78-0)) or a blend of polycaprolactone with oligo-styrene (Shabana et al. [2000](#page-78-0)). The technique may also be used to reveal texture in liquid crystal polymers (Ford et al. [1990](#page-75-0)).

#### $2.3.4$  $\overline{13}$

In transmission electron microscopy (TEM), a beam of electrons is passed through a thin sample, such that an image is formed as a result of absorption or diffraction contrast. In the case of polymers, a combination of disorder and radiation sensitivity means that, of these, absorption contrast is most important, in which case, high resolution images can be generated where image contrast is based on the spatial variation in electron density. In the case of materials such as nanocomposites, the distribution of the nanoparticles can therefore easily be imaged, as a result of the difference in the atomic number between the nanoparticles and the matrix polymer, as shown in Fig. [2.18](#page-63-0).

However, obtaining useful structural information concerning the lamellar texture of semi-crystalline polymers or the phase distribution in polymer blends or block copolymers is often complicated by the fact that the variation in electron density between the structural components of interest is insufficient to provide meaningful image contrast. In such circumstances, additional sample preparation procedures, beyond ensuring that the sample is sufficiently thin, are required.

#### 2.3.4.1 Inducing Contrast

If etching of polymers, as described above, is equivalent to similar process in metallography, then staining has analogues in biology, where the very same TEM contrast problems exist. Essentially, staining involves exposing a polymeric sample to a chemical reagent, which diffuses into the structure and becomes preferentially located at certain sites. The classic example of this concerns studies of the structure

<span id="page-63-0"></span>

Fig. 2.18 Colloidal silver embedded in an epoxy matrix (Image provided courtesy of Dr Suvi Virtanen/Alun Vaughan, University of Southampton, UK)

of rubber toughened polymer blends in which osmium tetroxide  $(OsO<sub>4</sub>)$  reacts with and preferentially stains unsaturated rubbery phases. The more aggressive analogue, which consequently has greater utility, is ruthenium tetroxide  $(RuO<sub>4</sub>)$ ; Trent et al. [\(1983](#page-78-0)) provide an excellent overview of the staining methodologies and polymer types where  $RuO<sub>4</sub>$  has been applied with success. While many different stains have been developed to enhance image contrast in the TEM, a major issue with such reagents concerns their aggressive nature, which raises safety concerns during use and in disposal. In the case of staining reagents such as  $OsO<sub>4</sub>$  and  $RuO<sub>4</sub>$ that can be used to stain polymers in the vapour phase, the staining device described by Owen and Vesely ([1985\)](#page-77-0) has been found to be extremely convenient. A related issue concerns 'overstaining', whereby exposure to the stain introduces artefacts into the specimen (Chou et al. [2002\)](#page-75-0). Figure [2.19](#page-64-0) shows images of two different materials stained with  $RuO<sub>4</sub>$ ; (a) from Trent et al. (1983) is a spherulitic morphology in a sample of high density polyethylene while (b) is a section from a block copolymer of polyethylene and atactic polypropylene (Hong et al. [2001](#page-76-0)); the amorphous atactic polypropylene is much more heavily stained overall than the semi-crystalline polyethylene in which the stain has also revealed the fine semicrystalline lamellar morphology.

The etching techniques described above in connection with SEM can also be used for TEM, in conjunction with so-called replication. In this, an accurate facsimile of the sample's surface topography is produced, frequently in the form of a thin carbon film, which is then coated at an oblique with an electron dense metal (shadowed). As a consequence, the distribution of metal on the surface is non-uniform and directly related to the surface topography of the specimen and, hence, the morphological features present within it. Figure [2.20a](#page-64-0) shows an equivalent structure, as revealed by etching followed by replication, to the lamellar

<span id="page-64-0"></span>

Fig. 2.19 TEM micrographs of (a) a spherulite centre in a thin film of high density polyethylene stained with RuO4, (b) section of polyethylene-atactic polypropylene block copolymer stained with RuO<sub>4</sub>. Reproduced with permission (a) from Figure 15 in Trent, Scheinbeim and Couchman, Macromolecules, 1983, 16: 589–598 (Copyright 1983) American Chemical Society. (b) from Figure 3 in Hong, Copyright (2001) with permission from Elsevier



Fig. 2.20 TEM micrographs of 60 % LPE/LDPE blends cooled at  $1 \degree$ C/min. (a) Sample prepared through etching and replication Scale bar is  $1 \mu m$  (b) Stained sections, cut from material fixed with chlorosulfonic acid. Scale bar is 200 nm. Reprinted from Polymer, 40:337–348, Morgan RL, Hill MJ and Barham PJ, Morphology, melting behaviour and co-crystallization in polyethylene blends: the effect of cooling rate on two homogeneously mixed blends, Copyright (1999), with permission from Elsevier

texture shown in Fig. 2.20b which was prepared by staining with chlorosulfonic acid and sectioning. Fig. 2.20a represents a case of a direct replica, where the carbon and shadowing metal are applied directly to the etched polyethylene. Removal of the replica is typically performed using a polyacrylic glue (Morgan et al. [1999\)](#page-77-0) or polyacrylic acid. Two stage (indirect) replicas are more commonly used; a thin sheet of cellulose acetate is applied to the etched surface, peeled off and coated with shadowing metal and carbon. The replica is then placed on top of a TEM grid and freed by dissolving the cellulose acetate away with acetone. Weng et al. ([2003,](#page-78-0) [2004](#page-78-0)) showed examples of replicas prepared by this technique.

# $\overline{1}$

Scanning probe microscopy involves a family of techniques in which atomic force microscopy (AFM) is the most popular which is relevant to this work. Scanning tunnelling microscopy can yield atomistic level images under good conditions. In AFM, the so-called contact mode provides an image of the surface topology. The resolution can approach the nanometre scale under ideal conditions but tip adhesion may limit the usefulness with soft materials such as polymers. The non-contact method involves an oscillating cantilever and under appropriate conditions, images of the spatial distribution of different phases or material can be formed where the contrast essentially arises from the differences in the stiffness of the phases.

Although for the highest resolution care has to be taken to isolate vibrations and screen electric fields, AFM is essentially performed in the laboratory environment. As such, it is possible to perform experiments such as heating and cooling in the AFM and the sample does not require treatment to reveal the morphology as in the case of SEM. Time-resolving studies are now possible with the latest developments and this has been used to good effect by Hobbs et al. to observe the growth of polyethylene crystals (Hobbs [2007](#page-76-0)). Further developments to the technology have allowed for the use of higher frame rate AFM, termed a video AFM, which has been utilized to good effect to show the growth of polyethylene oxide crystals (Hobbs et al. [2005](#page-76-0)).

#### 2.4 Scattering Methods

Scattering methods are a collection of powerful techniques for evaluation the molecular organization of materials including polymers. One of the earliest applications of X-ray diffraction at the start of the twentieth century was with polymers. There is considerable diversity in the instrumentation available for use with polymers using both laboratory sources and synchrotron national facilities. The type of instrumentation used relates to the type and scale of the information required. Figure [2.21](#page-66-0) shows a schematic of the scales of structures which can be studied using readily available equipment.

In a typical scattering experiment, the incident beam on a sample is elastically scattered by the sample through an angle,  $\theta$ , described by the equation  $|Q|$  =  $Q = 4\pi \sin(\theta)/\lambda$ , where  $2\theta$  is the scattering angle,  $\lambda$  is the wavelength of the incident beam and  $Q$  is the scattering vector. The angle through which the beam is scattered will determine the structural information that can be discerned as shown Fig. [2.21](#page-66-0). For example, small angle scattering can be utilized to determine features on the length scales of several to a hundred nanometres, such as the long period and lamellae thickness, whilst wide angle examines the features from several nanometres down to angstrom levels where it can be used in determination of the crystalline unit cell, crystal size and the polymer chain conformation.

<span id="page-66-0"></span>

Fig. 2.21 Various length scales examinable by scattering methods (Reproduced with the permission of the author of the chapter)

#### $2.4.1$  $\sim$

X-ray scattering arises from electrons where the observed intensity of scattering is dependant on the number of electrons present on an atomic species contained within the sample  $(I \sim Z^2)$ , hence heavier elements scatter more intensely than lighter ones.

#### 2.4.1.1 Small Angle X-Ray Scattering

Numerous small angle X-ray scattering (SAXS) experiments have been conducted on extracting information regarding the long period which, with knowledge of the degree of crystallinity, can be used to calculate the crystalline and amorphous thicknesses from SAXS data. This is done by considering the material as a two-phase system of periodic alternatively stacked lamellar crystals and amorphous regions. The methodology utilizes a Fourier transform of the data to extract an interface distribution function (Ruland [1977](#page-77-0)) or the correlation function (Strobl and Schneider [1980\)](#page-78-0) containing the information on the materials long period. Strobl used the correlation function to extract information from polyethylene SAXS data with further consideration of how inhomogeneities and lamellar curvature would impact the results (Strobl and Schneider [1980](#page-78-0)). Some knowledge of the crystallinity is required in order to determine the values for the crystal and amorphous thicknesses, which would make the combination of wide angle X-ray scattering and SAXS a useful tool in a thorough analysis of a material. An example of a 2D SAXS pattern, and the corresponding data reduction to a one-dimensional plot of intensity



Fig. 2.22 SAXS curve of a crystallizable copolymers of l-lactide, ε-caprolactone and glycolide. Wavelength of X-rays are 1.4 Å. Reprinted from figure 9a in Polymer 46 (17), 6411–6428 W. Channuan, J. Siripitayananon, R. Molloy, M. Sriyai, F.J. Davis and G.R. Mitchell, The structure of crystallisable copolymers of l-lactide, ε-caprolactone and glycolide, Copyright (2005) with permission from Elsevier

as a function of  $Q$ , is provided in Fig. 2.22. The scattering pattern was obtained from an annealed fibre of a crystallizable copolymer of l-lactide, ε-caprolactone and glycolide. The 2D scattering pattern exhibits highly anisotropic features (Channuan et al. [2005](#page-75-0)).

Another instance where SAXS has been a useful tool for polymer characterization relates to the examination of block copolymers. Block copolymers can form structural domains that are on length scales detectable by the small angle scattering technique. A series of scattering peaks occur with each peak position having a separation indicative of the structure formed. Examples of this would be if a peak occurred at  $Q = 1 \text{ Å}^{-1}$ , reflections would occur at 2, 3, 4, 5,... for lamellar domains, whilst body centred cubic will have peak positions  $\sqrt{2}$ ,  $\sqrt{3}$ ,  $\sqrt{4}$ ,  $\sqrt{5}$ ,... (Hamley and Castelletto [2004\)](#page-76-0).

The use of SAXS as a characterization technique for polymeric materials has been extended to include studies of liquid crystal polymers, polymer blends, nanocomposite materials, polymer gels and solutions (Chu and Hsiao [2001\)](#page-75-0).

#### 2.4.1.2 Wide Angle X-Ray Scattering

Wide angle X-ray scattering (WAXS) provides information on the unit cells where the data obtained can be utilized in determination of the lattice parameters, hkl reflection planes and hence the lattice structure i.e. face centred cubic, hexagonal, etc. In addition to the unit cell information, the level of crystallinity can be determined by considering the polymer as a two-phase material, amorphous and crystalline. The ratio of the second moment of the data corresponding to the sharp



crystalline peaks to the total second moment of the scattering curve provides the degree of crystallinity of the sample from the scattering data. However, suitable corrections for incoherent backgrounds, air scattering, thermal motion and lattice imperfections need to be accounted for (Ruland [1961](#page-77-0), [1964\)](#page-77-0). Ruland first applied this method to determine the degree of crystallinity in nylon 6 and 7 (Ruland [1964\)](#page-77-0). An example of a wide angle scattering curve is observed below in Fig. 2.23 for a sample of polyethylene oxide.

2D WAXS patterns can be used to determine the direction of preferred orientation and the orientation distribution function or a set of orientation parameters,  $P_{2n}$ , which describe the orientation distribution function  $D(\alpha)$ .

$$
D(\alpha) = \sum_{2n=0}^{2n=\infty} D(\alpha) P_{2n}(cos\alpha)
$$

where  $P_2 = (3\cos^2 \alpha - 1)/2$ 

In many works, attention is focused on  $\langle P_2 \rangle$ , although X-ray scattering is a technique able to provide quantitative estimates of all of the orientation parameters. In contrast, birefringence is only related to  $\langle P_2 \rangle$  as it is a second rank tensor property. Similar restrictions relate to all other second rank properties. For a perfectly aligned sample, the value of  $\langle P_2 \rangle$  is 1, whereas a randomly orientated distribution with no preferential alignment  $\langle P_2 \rangle$  has a value of 0. Methods are available for examination of preferential alignment in semi-crystalline and amorphous materials as described by Mitchell  $(2016)$  $(2016)$ . The methodology developed by Mitchell and co-workers in which the scattering is described in terms of a series of spherical harmonics provides a powerful tool box for the analysis of 2D scattering patterns. These techniques were successfully applied to isotactic polypropylene containing a thermotropic liquid crystal (Mitchell et al. [2005](#page-77-0)). This same methodology was used by Edwards et al. to examine the orientation of polymer lamellae in PCL electrospun fibres collected onto a rotating collector at differing take-up speeds. An increasing level of orientation was observed in the scattering patterns



Fig. 2.24 PCL electrospun fibre scattering for samples collected at differing take-up speeds. Wide angle X-ray scattering patterns *(top)* for electrospun fibres of PCL prepared using the indicating tangential velocities and the small angle X-ray scattering patterns (bottom) for the same samples. The outer edge of the SAXS patterns corresponds to  $|Q| = 0.08 \text{ Å}^{-1}$ . Reprinted from European Polymer Journal, 46 (6). pp. 1175–1183, Edwards, M. D., Mitchell, G. R., Mohan, S. D. and Olley, R. H. Copyright (2010) Development of orientation during electrospinning of fibres of poly (ε-caprolactone) with permission from Elsevier

(Fig. 2.24), shown by the azimuthal arcing of the intensity distribution with increasing collection speed until a critical speed was reached that induced fibre breakage (Edwards et al. [2010\)](#page-75-0). The obtained scattering patterns were described as a convolution of the fibre orientation and crystal orientation, for which fibre misalignment can be corrected for to establish the orientation of the crystals in a perfectly aligned sample. Similar methodologies can be applied to small-angle scattering data.

The use of WAXS is not limited to the study of semi-crystalline materials but can also be applied to purely amorphous materials. WAXS patterns obtained can contain information on the inter- and intra-chain segments and the trans-gauche conformation of the chains. For example, Lovell et al. performed WAXS on atactic polystyrene showing the scattering contributions from the inter- and intra-chain segments, and estimated the trans-gauche conformational arrangement of the chain by comparison to the scattering one would expect for various trans-gauche configurations. An example of this is given below in Fig. [2.25](#page-70-0) for atactic polystyrene (Lovell et al. [1979\)](#page-77-0).

#### 2.4.1.3 SAXS/WAXS Instruments

WAXS techniques have become commonly used in characterization of polymer samples with lab scale equipment available for use. Although small angle X-ray lab

<span id="page-70-0"></span>

Fig. 2.26 NCD Beamline at ALBA. (a) Image of the WAXS detector (*Blue box* in the top centre of image) (Picture taken by Sergio Ruiz) and (b) Image of part of the SAXS beamline (Picture taken by Juan Carlos Martίnez). Images provided courtesy of Alba Synchrotron

sources are available, there is significantly higher flux available at synchrotron sources allowing for rapid and in situ studies of samples (Fig. 2.26).

#### $2.4.2$  $\mathbf{e}$

Neutron scattering occurs from the nucleus of the molecule as opposed to the X-rays which scatter from electrons. As the neutrons scatter from the atomic nucleus, which occupies a significantly smaller volume than that of the electron clouds surrounding atoms, neutron scattering is considered a point scattering technique, hence the observed pattern does not fall off with increasing scattering angle as observed with X-ray scattering. Whilst the observed X-ray intensity is

proportional to the atomic number of the scattering atom, neutron scattering lengths exhibit no particular order, with scattering lengths appearing random with atomic species. However, there is a difference in scattering lengths between isotopic species, hence a contrast can be provided by utilizing an isotopic labelling technique.

#### 2.4.2.1 Small Angle Neutron Scattering

Small angle neutron scattering (SANS) can be utilized to study structural development in a polymer; similar to the SAXS technique, however, the unique isotopic labelling techniques available in a SANS experiment allow for study of the polymer chain dimensions in the bulk and solution state. For example, a hydrogenous polymer matrix that contains perdeuterated polymer chains can provide a contrast which allows the study of the macroscopic chain conformation in the bulk state. The perdeuterated polymer chain is considered to be chemically identical to that of the hydrogenous polymer, hence a study of the polymer in its natural state can be conducted. If a similar experiment were to be conducted with SAXS, it would require the substitution of a heavier element on the polymer chains to provide a scattering contrast, meaning a different chemical species is being studied compared to the normal material. This unique isotopic scattering length difference provided for neutron scattering experiments makes it a powerful tool for the investigation of polymer systems. Various examples are present in the literature where the study of the polymer chain dimensions has been conducted on a variety of polymers. Comparisons of the literature results for these SANS measurements show the theta, glassy and molten polymer state have similar conformation reflecting an ideal random walk as shown in a review collated by Wignall and Melnichenko [\(2005](#page-78-0)). For example, both atactic polymers, polystyrene and poly methyl methacrylate were shown to have radii of gyration that varied with the molecular weight of the sample by the relation  $R_g = 0.275 M_{\rm W}^{0.5}$ , similar to that measured in the theta state (Wignall and Melnichenko [2005\)](#page-78-0). In addition to bulk materials, thin films and fibres can be studied by SANS to examine the chain conformation. Studies of isotopically labelled electrospun fibres were conducted by Mohan et al. with results showing a small level of preferential alignment of the polymer chain along the fibre axis induced by the electrospinning process, with further extension possible due to mechanical deformation from a rotating collector (Fig. [2.27\)](#page-72-0) (Mohan et al. [2011](#page-77-0)).

#### 2.4.2.2 Broad Q Neutron Diffraction

Wide angle neutron scattering, commonly referred to as broad  $Q$  neutron diffraction, has been performed on various crystalline and amorphous polymers. Exploiting the contrast variation between isotopes as was done in SANS, the broad Q neutron scattering can be used to examine various scattering features. For example, neutron diffraction was performed on amorphous atactic polystyrene, which had selectively deuterated components. This allowed for the examination of
<span id="page-72-0"></span>

Fig. 2.27 Scattering curves for an electrospun fibre sample of (50/50) hydrogenous/perdueterated polystyrene collected onto a rotating collector. The data has been reduced to a 1D plot of the differential scattering cross section as a function of  $O$ , where the curves represent the scattering both parallel (solid line) and perpendicular (dotted line) to the fibre axis (vertical on page) obtained from the 2D scattering pattern (inset). Inset runs from  $-0.05 \text{ Å}^{-1} < Q < 0.05 \text{ Å}^{-1}$ (Adapted from Mohan et al. [2011](#page-77-0) with permission from The Royal Society of Chemistry)



Fig. 2.28 (a) Structure factors for selectively deuterated polystyrene. (b) Fourier transform of (a) fully deuterated monomer and (b) partial correlation function relating to backbone atoms (Reproduced from Mitchell et al. [1994](#page-77-0), with permission of The Royal Society of Chemistry)

the contribution to the scattering from various components on the polymer chain (Fig. 2.28). The structure factor for these scattering patterns is shown below in Fig. 2.28a where it can be seen that the various deuteration levels influence the scattering obtained. Here the scattering at approximately  $Q \sim 1-1.5 \text{ Å}^{-1}$  arises from scattering between molecules from neighbouring chains, whilst  $Q > 1.5 \text{ Å}^{-1}$  relates to the correlations from molecules on the same chain. The Fourier transform into a real space correlation function is provided in Fig. 2.28b. The lower values relate to



Fig. 2.29 (a) Wide-angle X-ray scattering curve for a sample of perdeuterated poly (vinylchloride) (b) Neutron scattering function for the sample subjected to X-ray scattering in the left hand image (Reproduced from Mitchell [2011\)](#page-77-0)

bond lengths present, C–D and C–C, whilst the higher length terms reflect the interand intra-chain segment contributions. Figure [2.28b](#page-72-0) shows a repeating oscillation at approximately 10 Å, 15 Å, 20 Å, 25 Å which relates to the scattering from the phenyl rings along the polymer chain.

The technique can also be applied to the examination of semi-crystalline polymer systems, for example, Fig. 2.29 shows the WAXS and broad Q neutron diffraction from the same sample of d-PVC. In the X-ray scattering data (Fig. 2.29a) the material appears very disordered, whilst the neutron scattering from the same perdeuterated sample of PVC shows a typical melt structure factor similar to polyethylene although the first peak is somewhat sharper reflecting a higher level of order which perhaps is a consequence of the more polar structure (Mitchell [2011\)](#page-77-0).

As the intensities of scattered X-rays depend on the atomic number,  $I \sim Z^2$ , the scattering for a sample of PVC will be dominated by the scattering from the Cl Atoms ( $Z = 17$ ), compared with the scattering from C ( $Z = 6$ ) or H ( $Z = 1$ ). In contrast, neutron scattering arises from changes in the neutron scattering length b which is determined by the atomic nucleus. For d-PVC  $b_{\text{cl}} = 9.577$ ,  $b_{\text{C}} = 6.646$ ,  $b<sub>D</sub>$  = 6.671, hence the scattering is not dominated over by the presence of the chlorine allowing for a more detailed study of the structure.

#### 2.4.2.3 Neutron Scattering Instruments

Neutrons are produced either in a nuclear reactor (e.g. the Institut Laue Langevin) or at a spallation source (i.e. ISIS Neutron Facility). In the latter most scattering experiments are performed using angular dispersion as in a typical X-ray scattering experiment, whereas at a spallation source, experiments are performed using time of flight techniques which opens up new possibilities as described below. Typically neutron scattering fluxes are lower and the interaction with the sample weaker and





Fig. 2.31 Time-resolved data obtained on NIMROD for PCL in both the semi-crystalline and melt phases. Inset shows time-resolved data captured during crystallization

hence the neutron scattering signals are much diminished. Much effort has been made to reduce the data collection cycle time, for example, using an area detector (LOQ ISIS first target station Heenan et al. ([1997](#page-76-0)) or many detectors (e.g. NIMROD (Fig. 2.30) second target station ISIS Bowron et al. [\(2010](#page-75-0))).

Figure 2.31 shows such data obtainable for a time-resolved study of PCL on the instrument NIMROD at ISIS, STFC, Didcot, UK with a cycle time of 400 s. The scattering data shown ranges from  $Q = 0.02$  to 50  $\text{\AA}^{-1}$  and is on a single vertical scale in absolute units.

STFC, Didcot, UK)

# <span id="page-75-0"></span>2.5 Summary

We have covered a wide range of techniques in this chapter. We can see a continual improvement in the facilities for the study of structure at multiple scales. Simultaneous SAXS and WAXS experiments are now routinely performed at synchrotronbased beam lines, while the NIMROD instruments take this a further step by routinely providing multiple scale data on a single intensity scale. Despite these developments, however exciting, there remains a need to utilize a range of complementary techniques involving both imaging and scattering both to cover the structural scales and to probe the scientific issues.

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# Chapter 3 Crystallization in Nanocomposites

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## 3.1 Introduction

Nanocomposites based on polymer matrices have been studied extensively (Paul and Robeson [2008](#page-109-0)). In the majority of these studies, the focus has been the enhancements in properties through the addition of relatively small quantities of nanoparticles. In this chapter, we centre our attention on the effects, if any, of the nanoparticles on the behaviour of the polymer matrix and in particular the nucleation and growth of crystal phases in the case of crystallizable polymers. We first consider the influence of macroscopic particles on this behaviour by examining the influence of polymer fibres on the matrix behaviour. We then consider the situation in polydisperse melts where extended objects can be formed from the high molecular weight fraction in the melt, and then finally we review work reported in this field in the context of nanoscale fillers.

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## <span id="page-81-0"></span>3.2 Templating

## 3.2.1 Linear Nucleation

Preferred orientation in polymers (see Sect. [1.6.1](http://dx.doi.org/10.1007/978-3-319-39322-3_1)) can deliver enhanced mechanical properties, especially when the level of preferred orientation is high. Most familiar to many is the case of nylon rope. Polyethylene is another material where very high strength fibres have been used to make ropes and bullet-proof vests. Two kinds of these are commercially available, namely Dyneema® from DSM and Spectra® from Honeywell.

To incorporate these advantages into bulk items, the making of polymer fibre-based composites has been investigated. Where the matrix is of a different material such as an epoxy resin, compatibility is a problem, both in terms of differential thermal expansion and adhesion. To avoid this, self-composites have been prepared by the technology of hot compaction (Ward and Hine [2004\)](#page-110-0). The initial research focused on exploiting high modulus melt spun polyethylene fibres. These were laid down in parallel in a metal mould, which was heated under a small contact pressure to prevent the fibres contracting, to a temperature where the material was just beginning to melt. A much higher pressure was briefly applied to force the fibres together, with perhaps some deformation, and to eliminate the air in order that the fibres were bathed in molten polyethylene. On cooling the molten polyethylene recrystallized, producing a fibre composite with a semi-crystalline matrix of the same polymer as the fibres.

In these composites, much of the original mechanical strength is retained in the composite (Hine et al. [1993\)](#page-108-0) which is achieved due to the development of a particular characteristic morphology (Olley et al. [1993](#page-109-0)). This is shown in Fig. 3.1



Fig. 3.1 The morphology of fibre compaction from Olley et al. [\(1993](#page-109-0)): reproduced with permission from the Royal Society. (a) The left hand image shows an etched section taken normal to the initial fibre direction,  $(b)$  the *right hand image* shows an etched section taken parallel to the initial fibre direction

which demonstrates sections transverse and parallel to the initial fibre axis. Figure [3.1a](#page-81-0) is a transverse section which has been etched (see Chap. [2](http://dx.doi.org/10.1007/978-3-319-39322-3_2)): this composite was prepared from fibres with a circular cross-section, inside of which are seen pits developed round nanovoids which run along the length of the fibre. Between the fibres the surfaces of lamellae are seen, indicating that molecular axes in the crystals are also parallel to the fibre length. Figure [3.1b](#page-81-0) is a section parallel to the fibres. To the left and right of this micrograph are parts of two fibres aligned vertically; in the middle lamellae are seen which have grown out from the surface of each fibre. This is the characteristic morphology of compacted fibre composites.

The first examples of self-composites were unidirectional composites based on polyethylene, but later the technique was modified by laying down alternating perpendicular layers of polyethylene fibres producing a two-dimensional composite sheet, which maintained a sizeable fraction of the strength of the original fibres in all directions along the plane of the sheet (Hine et al. [2000](#page-108-0)). The technique was extended to other materials including polypropylene. This polymer is available as high-modulus tapes woven into cloths, for example geotextiles, which can be compacted (Amornsakchai et al. [2000;](#page-107-0) Jordan et al. [2003](#page-108-0)). This is currently the largest commercial application of the technique, which is used in Samsonite Curv<sup>®</sup> luggage.

Figure 3.2 shows the results of a crystallization experiment, where a highmodulus polyethylene fibre (Tekmilon®) has been inserted into molten polyethylene; the high molecular weight and orientation of the fibre allow it to remain solid a few degrees above the melting point of the surrounding polymer. On cooling the sample to the crystallization temperature, crystals nucleate on the surface of the fibre (Fig. 3.2) as they do in fibre compactions (Fig. [3.1\)](#page-81-0).



Fig. 3.2 Sclair 2907 polyethylene (high density, crystallized at 123 °C for 70 s) (Abo el Maaty and Bassett [2005](#page-106-0))

Fig. 3.3 Polypropylene row structure: adapted from (White and Bassett 1998)



Initially, the crystal growth follows a direction normal to the orientation of the fibre (right hand picture above). With a fibre isolated in the melt, this closely parallel mode of growth is only sustainable for a short distance, owing to the presence of non-crystallized cilia, and after a short distance the closely spaced parallel lamellae give way to a form of cylindrulitic growth whose morphology resembles that of the outer regions of a large spherulite (See Chap. [1\)](http://dx.doi.org/10.1007/978-3-319-39322-3_1). This geometry has been extensively studied with respect to variations in the crystallization processes (Abo el Maaty and Bassett [2005](#page-106-0), [2006\)](#page-106-0), in order to give a basis for the formation of banding in polymer spherulites.

Polypropylene can be easily induced to form row structures by extension of the melt. An example of the resultant morphology is shown below. Closely spaced shish-kebab lamellae have grown directly out from the central row nucleus, but as growth proceeds outwards, increasing numbers of cross-hatching lamellae are found. The cross-hatching lamellae are found almost perpendicular to the lamellae growing out from the initial nucleus (Fig. 3.3).

In injection-moulded polypropylene products, densely packed row structures are typically found near the surface of the object. At least one process has been developed which is able to deliver this morphology throughout the moulded object, namely shear-controlled orientation injection moulding (SCORIM) (Kalay and Bevis [1997](#page-108-0)).

Polyethylene, especially a material containing a proportion of high molecular chain lengths, can be induced to form row structures by applying sufficient shear to the melt (An et al. [2006](#page-107-0)). If these are closely spaced, the material will be filled with parallel "shish-kebab" growth as in the Fig. [3.4](#page-84-0):

## 3.3 Crystallization and Flow

We have seen in the previous section that objects such as fibres or bundles of polymer chains can act as nucleating surfaces for polymer lamellae. The geometry of the lamellae is normal to the surface as can be seen clearly in Fig. [3.1](#page-81-0). As a

<span id="page-84-0"></span>

Fig. 3.4 Representative TEM morphology seen in quenched linear PE crystallized isothermally at 115°C. Sample had been sheared at 25 s<sup>-1</sup>. The arrow indicates the shear flow direction in the melt. Y. An et al. ([2006\)](#page-107-0) Polymer 47: 5643–5656

consequence, the morphology of the sample is determined by the orientation of the nucleating object. The most common form of a nucleating object is approximately spherical. Although interesting in themselves spherical nucleants do not lead to morphological control other than in the density of nucleating sites. In contrast, if we are able to develop anisotropic nuclei such as rod-shaped particles, then this leads directly to a common orientation of the polymer lamellar crystals. We describe these objects as directing the crystallization. As we have seen in the previous section, this directing does not continue forever, as other processes cause the lamellar crystals to diverge and lose their initial preferred orientation. If we wish to define the morphology throughout the material, we need to provide sufficient directing nuclei such that the directed volumes associated with each nucleus fill space (see Chap. [5\)](http://dx.doi.org/10.1007/978-3-319-39322-3_5). Moreover, we will need to provide the nuclei themselves with a common alignment. In principle, this could be achieved using an electric, magnetic, or thermal field but for ease of application we restrict our discussion to the use of flow fields as widely used in conventional polymer processing.

We expect that a rod-like object embedded in an elastic medium will rotate as the matrix is deformed. Anisotropic objects within an elastic medium which retain their integrity on deformation will follow the predictions of the pseudo-affine model with respect to the orientation of the objects as shown in Fig. [3.5](#page-85-0).

Polymer processing involves shear flow as well as simple extensional flow. Shear flow is a more complex arrangement with a three-dimensional nature to it (Fig. [3.6](#page-85-0)) and a weak extensional flow component. Rigid rods in a viscous fluid were first considered theoretically by Jeffery [\(1922](#page-108-0)). Jeffery showed that objects exhibited a trajectory often called a Jeffery's orbit which rotated the axis of the

<span id="page-85-0"></span>

Fig. 3.5 A plot of the orientation parameter  $\langle P_2 \rangle_c$  against extension ratio  $\lambda$  calculated on the basis of the pseudo-affine model for non-deformable rods embedded in an elastic medium



anisotropic unit from parallel to the vorticity vector to parallel to the flow direction. The frequency of that orbit depends on the aspect ratio of the object, Jeffrey considered ellipsoidal particles and in some cases a stable alignment could be obtained which was also related to the aspect ratio and the properties of the fluid matrix.

Hobbie et al. ([2003\)](#page-108-0) used optical measurements of semi-dilute dispersions of polymer dispersed multiwalled carbon nanotubes to determine that for a weakly elastic polymer melt, the tubes aligned preferentially parallel to the flow direction at low stresses with a transition to alignment with the vorticity vector above a critical stress, corresponding to a Deborah number of 0.15. The Deborah number is defined as the ratio of the relaxation time characterizing the time it takes for a material to adjust to applied stresses, and the characteristic time scale of an experiment probing the response of the material. At low Deborah numbers, the material is fluid-like but at higher Deborah numbers the material exhibits non-Newtonian behaviour that is typical of solid materials. For a highly elastic polymer solution, the tubes align parallel to the flow field at high shear rates.

In summary, the behaviour in flow of nanoparticles will depend upon their shape size and the nature of the polymer matrix.

#### 3.4 Nanoparticles

#### 3.4.1 Introduction

Eric Drexler introduced the term nanotechnology to describe the act of engineering materials on a very small scale. Since then, the production of nanomaterials and nanoparticles has blossomed. A "Nanoparticle" is a particle with an upper particle size limit of 100 nm. They are a link between bulk materials and atomic or molecular structures. While bulk materials have constant physical properties regardless of its size, among nanoparticles the size often dictates the physical and chemical properties. This indicates that properties of materials change as their size approaches the nanoscale. This feature can be attributed to the change in surface-tovolume ratio. A higher surface-to-volume ratio provides the opportunity that the structure of interest can interact with its environment (e.g. polymer matrix) more efficiently leading to property enhancement. Moreover, the main reason why nanoparticles have different optical, electrical, magnetic, chemical, and mechanical properties from their bulk counterparts are that in this size-range quantum effects start to predominate (Hristozov and Malsch [2009\)](#page-108-0). By means of quantum effects one can intuitively understand that they start to display quantum physics effects.

The major challenges, for nanoparticle applications, are their strong tendency of aggregation, agglomeration, and rapid sedimentation which limit the property enhancement in different matrices. Two approaches have been commonly used in improving nanoparticle stability: electrostatic and steric stabilization. Electrostatic repulsion is achieved by imparting or increasing the surface charge while steric stabilization is typically attained by the adsorption of long-chain organic molecules (e.g. surfactants). Combined electro-steric stabilization is also promising with the use of ionic polymeric molecules (e.g. polyelectrolytes).

Nanoscale particles can be classified in two ways, i.e. based on (i) structure and (ii) nature of nanoparticles. Structurally, they can be further distinguished as 1-D, 2-D and 3-D nanoparticles where 1-D, 2-D and 3-D indicate one-dimensional, two-dimensional and three-dimensional nanoparticles. Practically speaking, a



Fig. 3.7 A schematic depiction of 1-D, 2-D and 3-D nanoparticles

one-dimensional nanoparticle does not exist at all but what we mean as 1-D nanoparticle is that the length along two of the sides are relatively much smaller than the other side such that it that looks like a 1-D nanoparticle. For example, a long cylindrical particle having more than couple of hundred nanometres length and a few nanometres in diameter can be considered as a 1-D nanoparticle. 2-D nanoparticles are plate-like or two-dimensional sheets while 3-D nanoparticles can be thought of as spherical or sphere-like particle, e.g. a balloon or football as depicted in Fig. 3.7. Carbon nanotubes, graphene and fullerene are examples of 1-D, 2-D and 3-D nanoparticles, respectively.

The nature of nanoparticles can be categorized as carbonaceous nanoparticles, metallic nanoparticles and clay nanoparticles, all of which are well-studied nanoparticle families. Carbonaceous nanoparticles are a family of nanoparticles including single wall carbon nanotubes (SWCNT), double wall carbon nanotubes (DWCNT), multiwall wall carbon nanotubes (MWCNT), graphene, graphene oxide and fullerenes. The metallic nanoparticle is a large class of nanomaterials including but not limited to silver (Ag) nanoparticles, Gold (Au) nanoparticles, iron (Fe) nanoparticles and copper nanoparticles. Clay nanoparticles are receiving attention not only due to their competitive prices but also due to the tubular-shaped as well as plate-like structures. The size and shape of such nanoparticles depends on the synthesis method. The choice of nanoparticle for use in a composite material will depend on both the structure and nature of the nanoparticle to achieve a particular functionality. Members from the carbonaceous and clay families are further discussed before considering their behaviour in polymeric matrices.

## 3.4.2 Carbon Nanotubes

Since their discovery over two decades ago, carbon nanotubes have been heralded as a material to initiate a wave of major technological advancements during the twenty-first century. The low density of carbon in comparison to other elements, i.e. metal or clay makes it a versatile family. The incorporation of carbon nanotubes into a matrix material often leads to property enhancement in the material.



Fig. 3.8 Schematic diagram showing how a hexagonal sheet of graphene is rolled to form a CNT with chiral vector (Wilder et al. [1998\)](#page-110-0) [Reproduced Courtesy of Nature Publishing Group]

Carbon nanotubes (CNTs) are members of the Fullerene structural family. Their name is derived from their long, hollow structure with the walls formed by oneatom-thick sheets of carbon, called graphene (Fig. 3.8). The manner in which these sheets are connected to form tubes at specific and discrete ("chiral") angles and the combination of the angle and radius decides the nanotube properties; for example, whether the individual nanotube exhibits metal or semiconductor like behaviour. The values of  $n$  and  $m$  are used not only for the chirality or "twist" but also to draw a line between metallic and semiconducting nanotubes. In other words, chirality in turn affects the conductance, density, lattice structure, and certain other properties of the nanotube. A nanotube is considered metallic if the value  $n - m$  is divisible by three. Otherwise, the nanotube is semiconducting.

Consequently, when tubes are formed with random values of  $n$  and  $m$ , we would expect that two-thirds of nanotubes would be semiconducting, while the other third would be metallic, and this has been experimentally confirmed to be the case (Wilder et al. [1998](#page-110-0)). The diameter of a carbon nanotube is related to the chiral vector  $(n, m)$  using the relation

$$
d = (n^2 + m^2 + nm)^{1/2} 0.0783 \,\text{nm} \tag{3.1}
$$

where " $d$ " is diameter of the tube and n, m are integers of the vector equation  ${\bf R} = n{\bf a}_1 + m{\bf a}_2$  as shown in Fig. 3.8 (Wilder et al. [1998](#page-110-0)). Metallic and semiconducting single-walled carbon nanotubes on  $SiO<sub>2</sub>$  can have obviously different contrast in scanning electron microscopy due to their conductivity difference and thus can be effectively and efficiently identified as shown in Fig. [3.9](#page-89-0) (Jie 2012, Li [2012](#page-109-0)).

The structure of CNTs consists of one, two or more, graphene sheets rolled up to make the tubes leading to variations from single (S), double (D) and multi-wall (MW) carbon nanotubes, respectively. Nanotubes naturally align themselves into "ropes" held together by van der Waals forces, more specifically, pi-stacking. The nature of the dispersion problem for CNTs is rather different from other

<span id="page-89-0"></span>

Fig. 3.9 Identification of metallic and semiconducting single-walled carbon nanotubes in Scanning Electron Microscopy. Adapted with permission from Jie (2012). Copyright (2015) American Chemical Society

conventional fillers, such as spherical particles and carbon fibres, because CNTs are characterized by a small tube diameter on the nanometre scale and with a high aspect ratio ( $>1000$ ) and thus possess an extremely large surface area. A variety of techniques have been used to disperse carbon nanotubes in the matrix material to obtain the desired properties. These include but are not limited to use of polar solvents, mechanical mixing, ultrasonication and functionalization of carbon nanotubes. Functionalization can be achieved in two different ways, i.e. ionic functionalization and covalent functionalization. In ionic functionalization, an ionic salt is used to disperse carbon nanotubes while in covalent functionalization carbon nanotubes are acid treated to get attach the carboxylic group on the surface of tubes. The repulsion between these attached carboxylic groups restricts or hinders the aggregation process which consequently leads towards improved dispersions of the CNTs. Scanning electron microscope (SEM) and transmission electron microscope (TEM) are the most widely used techniques to observe how well the tubes are dispersed. Figure [3.10](#page-90-0) shows multiwall carbon nanotubes observed using TEM, revealing that tubes are not only curled but even highly entangled due to van der Waals forces of attraction leading to bundles of tubes.

Because of their elongated cylindrical structure, CNTs are more favourable for enhancing electronic and charge transport properties. Besides their interesting electronic properties CNTs show a set of unique mechanical properties as well owing to an extremely high level of strength due to the bonds between the single carbon atoms. The chemical bonding in CNTs is composed entirely of  $sp<sup>2</sup>$  bonds which are stronger than the  $sp<sup>3</sup>$  bonds found in diamond making them a unique candidate with the highest tensile strength, elastic modulus and perhaps the stiffest material on earth with extra light weight (Rasmussen and Ebbesen [2014\)](#page-109-0).

Graphene: The development of graphene has a very high pace due to its two-dimensional structure having a variety of impressive properties. The most common properties associated with graphene on which it is selected for different applications range from high electron mobility, Young's modulus, high thermal conductivity and optical absorbance. In other words, graphene is super-strong and stiff, amazingly thin, almost completely transparent, extremely light weight, and an amazing conductor of electricity and heat. The properties associated with the

<span id="page-90-0"></span>Fig. 3.10 Transmission electron microscopy (TEM) images of MWCNTs



HV=200.0kV Direct Mag: 115000x

graphene structure depends on the synthesis method. Currently, chemical vapour deposition (CVD) is considered to be the best method for fabricating high-quality graphene in large quantities. This method involves depositing gaseous carbon atoms on a copper foil, then transferring the graphene film to a wide range of substrates, such as silicon. The CVD process can be controlled to minimize the amount of defects. Although weak points at grain boundaries and multilayer regions are quite common in CVD graphene, they have been shown to have a minimal effect on performance in most cases. The favourable price/quality ratio makes CVD graphene (Fig. [3.11](#page-91-0)) suitable for many applications such as flexible/transparent electronics, gas barriers, and anti-corrosion coating. Liquid phase and thermal exfoliation both involve splitting up graphite to form graphene flakes—either using chemical solvents or thermal shock. These methods are very scalable to large-scale production—however, the flakes are usually multilayered, not single layered, and the number of layers can be hard to control. The process can also introduce impurities into the graphene. Silicon carbide can be used to synthesize graphene layers when Si atoms are sublimated; the remaining face of the silicon carbide becomes a thin graphite surface. Nowadays, it is possible to control the number of graphene layers and to obtain a very high quality over a wide area. The high cost of silicon carbide and the requirement for elevated temperatures to achieve the sublimation are the main shortcomings of this process.

An issue in graphene research, which is similar to that which arises with carbon nanotubes, is the use of terms. The term "graphene" is used in a generic manner and not in a precise way to describe many graphene-based materials synthesized and studied (Bianco et al. [2013\)](#page-107-0). Peter (2014) recently proposed a model which considers the number of graphene layers, the average lateral size, and the carbon-

<span id="page-91-0"></span>

Fig. 3.11 A general trend to describe graphene quality over price for different synthesis methods

to-oxygen (C/O) atomic ratio as the three fundamental properties that cover the largest set of current graphene-based materials (GBMs) encountered in practice. One can distinguish easily the different types of graphene structure from this model which is depicted in Fig. [3.12.](#page-92-0)

The electronic properties of graphene are sensitive to geometry. For electronic applications, graphene is generally laid on a substrate made of a bulk material. Owing to the presence of dangling chemical bonds, 3D materials tend to be poor substrates for 2D materials such as graphene. One solution is to use hexagonal boron nitride (h-BN), which is both an insulator and a 2D material, and so does not have the problematic bonds. For a complete electronic characterization of the graphene film, down to submicrometre grains, synchrotron-based conventional and nanoresolved photoelectron spectroscopies are used (Razado-Colambo et al. [2015](#page-110-0)).

There are numerous potential applications for graphene. One particular application may be as a gas barrier, for example, blocking water vapour or oxygen from interacting with sensitive materials. In addition, the strong carbon–carbon bonds within a sheet of graphene open up the possibility for using either sheets of pure graphene in applications where the strength can be exploited directly or adding graphene to other materials to improve their mechanical strength. It is also used as anti-corrosion coating. It is the most promising nanofiller due to its high surface area, aspect ratio, tensile strength, thermal and electrical conductivity, EMI shielding ability, flexibility and transparency (Potts et al. [2011\)](#page-109-0).

<span id="page-92-0"></span>

Fig. 3.12 Classification grid for the categorization of different graphene types according to three fundamental GBM properties: number of graphene layers, average lateral dimension and atomic carbon/oxygen ratio. The different materials drawn at the six corners of the box represent the ideal cases according to the lateral dimensions and the number of layers reported in the literature. The values of the three axes are related to the GBMs at the nanoscale, but it is feasible to expand the values to the microscale (Wick et al [2014](#page-110-0)) Courtesy: Reproduced with permission of John Wiley and Sons

## 3.4.3 Nanoclay

In terms of chemistry, all clay minerals may simply be described as hydrous silicates. In terms of their natural locations, clay minerals can be divided into two classes, residual clay and transported clay (or sedimentary clay) (Siddiqui and Ahmed [2005\)](#page-110-0). Residual clays could be produced by the chemical decomposition of rocks caused by weathering conditions, e.g. granite containing silica and alumina; by the solution of rocks, i.e. limestone; and by the disintegration and solution of shale. The second type, transported clay, is removed from the original deposit through erosion and deposited to a distant place. Clay minerals may be divided into four major groups, mainly in terms of the variation in the layered structure. These include the Kaolinite group, the Montmorillonite/smectite group, the Illite group, and the Chlorite group and are summarized in Table [3.1](#page-93-0) with general formula (Uddin [2008\)](#page-110-0).

	Group name	Member minerals	General formula	Remarks	
	Kaolinite	Kaolinite, dickite, nacrite	$Al_2Si_2O_5$ (OH) <sub>4</sub>	Members are polymorphs (composed of the same) formula and different structure)	
$\mathcal{D}_{\mathcal{L}}$	Montmorillonite or Smectite	Montmorillonite, pyrophyllite, talc, vermiculite, sauconite, sapo- nite, nontronite	(Ca, Na, H)(Al, Mg, Fe, $Z_n$ <sub>2</sub> $(Si, Al)4O10(OH)2 - XH2O$	<b>X</b> indicates varying level of water in mineral type	
$\mathbf{3}$	Illite	Illite	(K,H)Al <sub>2</sub> (Si, $Al)_{4}O_{10}(OH)_{2}$ -XH <sub>2</sub> O	<b>X</b> indicates varying level of water in mineral type	
$\overline{4}$	Chlorite	Amesite (i)	(Mg, (i) $Fe)_{4}Al_{4}Si_{2}O_{10}(OH)_{8}$	Each member mineral has separate formula; this	
		(ii) Chamosite	$(ii)$ $(Fe, Mg)3Fe3$ $AlSi3O10(OH)8$	group has relatively larger member minerals and is	
		(iii) Cookeite	$(iii)$ LiAl <sub>5</sub> Si <sub>3</sub> O <sub>10</sub> $(OH)_8$	sometimes considered as a separate group, not as part of clays	
		Nimite, etc. (iv)	(Ni, Mg, Fe, (iv) $Al$ <sub>6</sub> $AlSi3O10(OH)8$		

<span id="page-93-0"></span>Table 3.1 Four major groups of clay minerals, mainly in terms of the variation in the layered structure

(Uddin [2008](#page-110-0)) Courtesy: With permission from Springer Publications

In general, nanoclays have a large class of categories with different compositions which will alter the properties hence only two members, halloysite and montmorillonite nanoparticles, are thoroughly discussed to give an insight to nanoclays in general.

Halloysites Nanotubes: Halloysite is a naturally occurring eco-friendly clay mineral which is predominantly composed of multi-walled nanotubular-shaped crystals and characterized by a high specific surface area and unique surface properties (Joussein et al. [2005](#page-108-0)). In terms of chemical composition, Halloysite nanotubes (HNT) are similar to Kaolin and can be considered as rolled Kaolin sheets with an inner diameter of 10–20 nm, outer diameters of 40–70 nm and lengths of 500–1500 nm. The empirical formula for halloysites is  $Al_2Si_2O_5(OH)_4$ and its main constituents are aluminium  $(20.90\%)$ , silicon  $(21.76\%)$  and hydrogen (1.56 %). Halloysite typically forms by hydrothermal alteration of alumino-silicate minerals. The internal side of Halloysite is composed of  $Al_2O_3$  while the external is mainly SiO2. The layers have a tendency to roll into nanotubes to correct the lateral misfit between the silicate and aluminate sheets. Since Halloysite nanotubes belong to an aluminosilicate group, they can be decomposed by both strong inorganic acids and bases, resulting in changes to their morphology and structure. An example HNTs are shown in the electron micrographs in Fig. [3.13](#page-94-0) (Wei et al. [2014](#page-110-0)).

Due to the easy dispensability of HNTs, it is expected that they could be dispersed relatively uniformly in thermoplastics by direct melt blending, especially for polymers with high polarity such as polyamides. Due to the variety of

<span id="page-94-0"></span>

Fig. 3.13 Images of halloysite clay, (a) Transmission electron micrograph of tubes dispersed in water and dried on a copper grid; (b) Scanning electron micrograph of dry HNT powder (Wei et al. [2014](#page-110-0)) [Reproduced with permission of "The Royal Society of Chemistry"]

crystallization conditions and geological occurrence, HNTs adopt different morphologies such as tubular, spheroidal and plate-like particles, of which the tubular structure is the most common. Empty tubular structures of halloysite makes it a versatile container for loading with active chemical agents. It has been loaded with organic and inorganic substances including corrosion inhibitors, biocides, metals and salts to prepare functional polymer nanocomposites. Halloysite exhibits higher adsorption capacity for both cationic and anionic dyes because it has negative  $SiO<sub>2</sub>$ outermost and positive  $A_1O_3$  inner tube surface; therefore, these clay nanotubes have efficient bivalent absorbency (Zhao et al. [2013](#page-111-0)). The flexural properties, tensile strength and impact strength all are noticeably improved with the incorporation of HNTs (Du et al. [2010](#page-107-0)) (Table [3.2\)](#page-95-0).

HNTs have a wide range of applications such as for use in anticancer therapy, for sustained delivery of certain agents, acting as a template or nanoreactor for biocatalyst, use in personal care and cosmetics and even used as environment protective (Ravindra et al. [2012](#page-109-0)).

Montmorillonite (MMT) nanoclays have attracted much research interests over the past decade and are widely used for dispersion in polymers due to the high aspect ratio and the large interface of the polymer–nanoclay interaction. MMT is a hydrophilic and inorganic 2-D structure belonging to the nanoclay family (Fig. [3.14](#page-95-0)). MMT is a subclass of smectite with 2:1 phyllosilicate mineral characterized as having greater than 50 % octahedral charge. It is generally represented as  $(Na,Ca)_{0.33}$   $(Al,Mg)_2$   $(Si_4O_{10})(OH)_2nH_2O$  with repeating units and monoclinic prismatic structure. MMT is less effective than halloysite when employed with a matrix material in context to electrical, mechanical and thermal properties. Naturally available MMT clays are hydrophilic, and they must be made organophilic (hydrophobic) to have compatibility with most host polymers. Organic treatment is

<span id="page-95-0"></span>Table 3.2 Comparison of mechanical property enhancement of three polymer matrices material [polypropylene (PP), polybutylene terephthalate (PBT) and polyamide (PA)] when employed with HNTs

Material	Flexural modulus (GPa)	Flexural strength (MPa)	Tensile strength (MPa)	Impact strength $(kJm^{-2})$
Neat PP	1.37	44.5	33.5	4.05
PP/HNT/(100/5)	1.75	51.5	35.2	5.51
Neat PBT	2.3	79.7	52.3	5.65
PBT/HNT/(100/5)	2.6	82.7	54.9	4.65
Neat PA	2.71	110	77.0	5.25
PA/HNT/(100/5)	3.23	118.5	82.1	5.75

(Mingliang [2010](#page-109-0)) Reproduced, courtesy of "John Wiley and Sons"



Fig. 3.14 (a, b) Montmorillonite (MMT) nanoclay. (Wallace [2015](#page-110-0)). Source [\[https://nice.asu.edu/](https://nice.asu.edu/nano/montmorillonite-mmt-nanoclays-ashpalt) [nano/montmorillonite-mmt-nanoclays-ashpalt](https://nice.asu.edu/nano/montmorillonite-mmt-nanoclays-ashpalt)]

typically accomplished via organic cations, namely onium or quaternary ammonium-based salts in MMT clays. When treated MMT clays are mixed into the host matrix polymer, two types of morphologies evolve, intercalated and delaminated/exfoliated structure. The intercalated structure is a well-ordered multilayered structure of silicates, where the polymer chains gets into the interlayer spaces (inter-gallery region). On the other hand, in the exfoliated/delaminated structure the polymer chains separate individual silicate layers well apart, e.g. 80–100 Å or more, and no longer close enough to interact with each other.

MMT nanoclay has a potential to alter material properties when used as a filler material (Ogata et al [1997,](#page-109-0) You et al [2011](#page-110-0)). Epoxy-MMT nanocomposite is one of the key examples indicating an increase in storage modulus  $(E')$  with an increase in MMT loading. It was also reported that volume conductivity and surface conductivity values of the nanocomposites decreased with increasing DC voltage (Rashmi et al. [2011\)](#page-109-0). A more recent study reveals the significance and use of MMT in hydrogels to improve its properties (Ting et al [2015\)](#page-110-0). Li et al. [\(2015](#page-109-0)) observed the influence of the MMT on the swelling degree at equilibrium of P(ATC-AAm)/MMT nanocomposite hydrogels was shown in Fig. [3.15.](#page-96-0) The nanocomposite hydrogels showed normal swelling behaviour at low loading while

<span id="page-96-0"></span>

Fig. 3.15 The swelling degree at equilibrium of nanocomposite hydrogels with various MMT contents (Ting et al [2015\)](#page-110-0) [Reproduced with permission of "John Wiley and Sons"]



Fig. 3.16 Tensile stress–strain curves of P(ATC-AAm)/MMT nanocomposite hydrogels. (Ting et al [2015\)](#page-110-0) [Reproduced with permission of "John Wiley and Sons"]

increasing the MMT amount in the nanocomposite gels led to decrease the swelling degree at equilibrium. Moreover, the tensile stress–strain curves are shown in Fig. 3.16, obviously, the addition of MMT led to an increase in Young's modulus. The reported work clearly signifies the MMT platelets as cross-linkers in hydrogel resulted in the enhanced mechanical properties.

#### 3.5 Nanocomposites with Carbon Nanotubes

The outstanding properties of individual carbon nanotubes (CNT) combined with their low mass density make them ideal candidates as reinforcing nanoparticles for high performance polymer materials. The idea is that, due to their aspect ratio, they can modify the properties of the polymer matrix even at very low concentrations. However, mechanical properties of CNT nanocomposites, are still very far from the theoretical value of the filler particles. In order to transfer the CNT properties to the composite material one essential and difficult step involves the fine dispersion of the nanotubes within the polymer matrix. However, because of van der Waals attraction among nanotubes and their large surface areas, CNT tend to form agglomerates. CNT arrange themselves into bundles or ropes that may achieve the micron size. Without proper dispersion, the properties of the nanocomposite are more similar to those of a regular composite than to those of individual CNT.

Among the different methods of dispersion of CNT into a polymer matrix, one may distinguish two: mechanical methods and solution methods. Mechanical methods have been extensively employed (Linares et al. [2008;](#page-109-0) Jin and Park [2011\)](#page-108-0). In order to destroy the bundles, very energetic mechanical methods should be employed. Among this mechanical methods are ball milling (Song et al. [2013\)](#page-110-0), stirring and extrusion (Zhang et al. [2004\)](#page-111-0) and ultrasonication (Bin et al. [2003\)](#page-107-0). These high energy methods are very effective in dispersing nanotubes in liquid matrices, but it shows severe problems when trying to disperse CNTs in high viscosity matrices. This is one of the reasons why solution methods have been developed. CNT are dispersed into a polymer solution, and the mixture is allowed to coprecipitate or it is casted (Chae et al. [2005](#page-107-0); Fornes et al. [2006\)](#page-107-0). A variation of this method consists on in situ polymerization of the polymer in a solvent with CNT dispersed (Broza et al. [2005;](#page-107-0) Nogales et al. [2004a](#page-109-0), [b](#page-109-0); Garcia-Gutiérrez et al. [2006;](#page-107-0) Hernández et al. [2006\)](#page-107-0).

The mixing method has a strong impact on the properties of the nanocomposites. In general, low percolation thresholds for electrical conductivity are achieved in the case of solution mixed systems, than in direct melt mixing methods. As an example, in situ polymerized nanocomposites with Poly(butylene terephthalate) as the polymer matrix and single wall carbon nanotubes as filler has shown one of the lowest percolation threshold for electrical conductivity in thermoplastic polymer nanocomposites (Nogales et al. [2004a,](#page-109-0) [b](#page-109-0)). A comparison can be made between the conductivity of the nanocomposite prepared by different methods (Fig. [3.17\)](#page-98-0), and in general, it has been observed that solution mixing is a more efficient method for dispersion.

However, in some cases, the properties of the matrix polymer and those of the carbon nanotubes, results in synergetic effects in the form of new materials with desirable combined properties, like shape recovery materials (Cho et al. [2005\)](#page-107-0) or conducting transparent polymer materials as shown in Fig. [3.18](#page-98-0) (Hernandez et al. [2009a,](#page-107-0) [b](#page-108-0)).

<span id="page-98-0"></span>

Fig. 3.17 Electrical conductivity versus SWCNT weight concentration for nanocomposites of Poly(Butylene Terephthalate) prepared by direct mixing (DM) and for nanocomposites prepared by in situ polymerization (I-SP). Reprinted with permission from Elsevier (Hernández et al. [2006\)](#page-107-0)

Fig. 3.18 Transparency of conducting nanocomposites of similar thickness with 0.1 wt% of SWCNT prepared by direct mixing (left side) and by in situ polymerization (right side). Reprinted with permission from Elsevier (Hernández et al. [2006](#page-107-0))



The final property of a CNT/polymer nanocomposite cannot be predicted simply by considering the addition of those of each of the components. The presence of CNT in a polymer melt has a strong impact on the subsequent morphology of the crystallized composite. In general, it is accepted that CNT may act as heterogeneous nucleating agents in the polymer matrix (Lim et al. [2015;](#page-109-0) Bhattacharyya et al. [2003](#page-107-0)). Polymer processing involves the application of combination of shear and elongational flows coupled with complex temperature profile. Due to the high

aspect ratio of CNT, they tend to align with the flow (Garcia-Gutiérrez et al.  $2006$ ). In order to disentangle all these effects, emphasis has been focused on the physical aspects of these modifications. For that, scattering experiments to assess the structure have been performed, either in rheometer or in shear cell, so that thermal and flow effects can be separated (García-Gutiérrez et al. [2008;](#page-107-0) Hernández et al. [2009a,](#page-107-0) [b](#page-108-0), Chen et al [2011](#page-107-0)).

#### 3.5.1 Nanocomposites with Halloysites

Ning [\(2007](#page-109-0)) have studied i-PP loaded with 1 and 10 % w/w of Halloysite nanotubes with diameters reported to be in the range of 50–300 nm and a length/diameter ratio of 3–10. As the non-isothermal crystallization curves (Fig. 3.19) show there is a clear but small nucleation effect from the halloysite nanotubes. Despite this the larger scale morphology was reported to remain the same for samples containing halloysite nanotubes as displayed for the i-PP alone.

Mitchell and Duraccio [\(2011](#page-109-0)) carried out similar studies using polyethylene oxide and 2 % of halloysite nanotubes using a small shear cell which facilitated the sample being sheared in the melt before cooling to crystallize. The shear cell was mounted to an SAXS beamline at the Elettra Sychrotron Facility and SAXS patterns were recorded throughout the heating-shearing-cooling cycle. They found that when shearing took place at lower temperatures, the system crystallized during shear with an isotropic distribution of lamellar crystals as revealed by the SAXS



Fig. 3.19 Non-isothermal crystallization curves for i-PP and i-PP/HNT composites. Cooling rate is 10 C/min. Reproduced from Polymer 48 (2007) 7374–7384 with permission from Elsevier— Ning [\(2007\)](#page-109-0)

data (Mitchell and Duraccio [2011\)](#page-109-0). As the shear temperature increased, the orientation distribution of lamellar crystals became anisotropic presumably as a consequence of crystallization nucleated by the halloysite nanotubes became a more dominant feature of the crystallization. On shearing at even higher temperature, the distribution of crystals became isotropic as the memory of the anisotropy induced in the melt relaxed before the crystallization took place.

#### 3.5.2 Nanocomposites with Clay Platelets

Processing operations such as injection and compression moulding, extrusion, fibre spinning, etc. are likely involved for the preparation and commercialization of polymer/clay nanocomposites. The flow applied during processing play a decisive role in crystallization kinetics and in the morphology obtained. For neat polymers, it has been demonstrated that the flow accelerates crystallization kinetics when compared with the quiescent melts (Keller and Kolnaar [1997](#page-108-0); Kumaraswamy et al. [1999\)](#page-108-0) and some crystallization mechanism has been proposed (Somani et al. [2000](#page-110-0); Seki et al. [2002\)](#page-110-0), whereas for polymer/clay nanocomposites, studies are still lacking and most of results have been reported for iPP and nylon 6/clay nanocomposites.

As in the static conditions, the incorporation of nanoscale-layered silicates impacts the crystallization under shear in terms of kinetics, structure and degree of crystallinity. In particular, two main effects have to be taken into account during the crystallization of a polymer: (a) the enhancement of nucleating speed and crystallization rate (Sun et al. [2009;](#page-110-0) Nowacki et al. [2004;](#page-109-0) Somwangthanaroj et al. [2003\)](#page-110-0), being the clay is a heterogeneous nucleating agent; (b) the decrease of crystallinity and degree of perfection of the crystal (Wang et al. [2005\)](#page-110-0), due to the physical hindrance of nanoclay layers to the motion of polymer chains.

Two other aspects should be considered during crystallization under shear: the clay nanolayer orientation with respect to the flow direction and polymer matrix orientation due to the influence of clay on the viscoelastic behaviour of the melt polymer. Both affect the final polymer/clay nanocomposite morphology and its macroscopic properties. The two-dimensional (2D) clay may align in three primary directions under shear, often referred to as a, b and c orientations (Butler [1999\)](#page-107-0). In the perpendicular (a) orientation, the surface normal aligns parallel to the vorticity direction, and the particles lie in the flow-gradient plane; in the transverse (b) orientation, the surface normal aligns parallel to the flow direction, and the particles lie in the vorticity gradient plane; in the parallel (c) direction, the surface normal aligns parallel to the shear gradient direction, and the particles lie in the flow-vorticity plane. As reported in literature, the orientation of the clay platelets depend on many parameters such as their structure in the polymer matrix (Rozanski et al. [2009](#page-110-0)), their concentration (Sun et al. [2009\)](#page-110-0) and shear rate (Lele et al. [2002\)](#page-108-0). The general or intuitive response of the clay platelet orientation in a polymer matrix is in the c orientation. This has been described by studies such as for nylon–clay

nanocomposites (Krishnamoorti and Vaia [2001;](#page-108-0) Krishnamoorti and Yurekli [2001;](#page-108-0) Medellin-Rodriguez et al. [2001](#page-109-0); Medellin-Rodríguez et al. [2003](#page-109-0)). Anyway different orientations have also been found (Medellin-Rodríguez et al. [2003](#page-109-0); Okamoto et al. [2001](#page-109-0)) as for example particular superstructure called "house of cards structure" reported by Okamoto et al. in polypropylene/clay nanocomposite melt under elongational flow (Okamoto et al. [2001\)](#page-109-0).

In a recent work (Dykes et al. [2012](#page-107-0)), there has been found an unexpected resistance of nanoclay to shear flow-induced orientation in PS/clay nanocomposites. Despite the small magnitude of the estimated rotational diffusivity of a single clay platelet, significant orientation in steady shear flow only develops at shear rates greater than 1  $s^{-1}$ . Similarly, flow-induced orientation in largeamplitude oscillatory shear only develops at frequencies greater than 0.1 Hz. The inability of shear at low rates and frequencies to produce significant alignment suggests the existence of a structural relaxation process that is much faster than that of rotational Brownian motion of the clay particles. Direct evidence of such a fast process is found in measurements of orientation relaxation following cessation of shear flow. In the article, it is hypothesized that the fast nanoclay relaxation arises from either relaxation of shear-induced distortion of partially flexible exfoliated clay sheets in a highly entangled nanoparticle network, or a direct coupling of particle and polymer dynamics through the chemical tethering of particle chains that occurs during the in situ polymerization synthesis of these materials. Analogously (Rozanski et al. [2009\)](#page-110-0), it has been found in iPP/clay exfoliated nanocomposites that the shear-induced orientation of the clay platelets is very weak in spite of the shear rate of  $2 s^{-1}$ .

The effect of shear on the orientation of polymer–clay nanocomposites has been examined by a number of groups (Somani et al. [2000](#page-110-0), [2001](#page-110-0); Fong et al. [2002;](#page-107-0) Jimenez et al. [1997](#page-108-0)), and in some cases, the three-dimensional (3D) orientation of the polymer and clay has been determined (Kojima et al. [1994](#page-108-0); Bafna et al. [2003;](#page-107-0) Varlot et al. [2001\)](#page-110-0).

Different authors (Nowacki et al. [2004](#page-109-0); Somwangthanaroj et al. [2003](#page-110-0); Wang et al. [2005;](#page-110-0) Yalcin et al. [2003](#page-110-0); Koo et al. [2005\)](#page-108-0), studying early stage of shearinduced crystallization, reported stronger orientation of polymer crystals in nanocomposites with organo-modified MMT (o-MMT) processed by injection moulding and extrusion than that in neat polymers with the same thermomechanical history.

A typical "shish-kebab" crystalline structure has been found by Maiti and Okamoto [\(2003](#page-109-0)) and Kim et al. ([2001\)](#page-108-0) in polyamide/organoclay nanocomposite and by Choi and Kim ([2004\)](#page-107-0) in PP/EPR/talc nanocomposite where a preferential orientation of polymer lamellae perpendicular to the surface of organoclay layers was inspected by TEM measurements. The unique observation of lamellar orientation on the clay layers was ascribed to nucleation and epitaxial crystallization at the interface between layered silicate and polymer matrix especially the surfaces of clay platelets acted as heterogeneous nucleation sites. Orientation of iPP crystals was also enhanced in iPP/PP-MA/o-MMT injection-moulded parts, especially manufactured by dynamic packing injection moulding (Wang et al. [2005\)](#page-110-0). MMT

platelets aligned along the flow direction contributed to oriented crystallization by constraining the growth of iPP crystals. Koo et al. ([2005\)](#page-108-0) found that the clay enhanced iPP orientation in extruded iPP/PP-MA/o-MMT nanocomposites resulting in two iPP crystal fractions with either c or a\* axis oriented along the flow direction and with b axis oriented in the film thickness direction. Analogously, the amount of crystal orientation in injection-moulded nylon6/clay nanocomposites were found higher than that of pure nylon (Yalcin et al. [2003](#page-110-0)), and this was attributed to the so-called shear amplification mechanism that a great enhancement of local stress occurred in the small interparticles region of two adjacent layered tactoids with different velocities. In another work (Medellin-Rodríguez et al. [2003\)](#page-109-0), the complete spherulitic formation was suppressed even in the core region of specimen at high mould temperature due to the nucleation density that was significantly increased through orientation of macromolecules and the foreign particle effect of the nanoclay.

In contrast with the above results, Zhang et al. [\(2003](#page-111-0)) reported a decreased orientation of iPP in iPP/PP-MA/o-MMT nanocomposites during dynamic packing injection moulding as compared to that of neat iPP solidified under the same conditions. Similarly, Medellin-Rodriguez et al. [\(2001](#page-109-0)) found that the overall molecular orientation of the crystals was found to decrease with the clay content in Nylon 6/clay nanocomposites subject to uniaxial deformation, with some clay platelets oriented perpendicular to the film surface and the molecular axis of the Nylon 6 crystals parallel to the stretching direction. This was explained by the presence of the clay platelets as well as the rotation of the clay platelets during deformation, which hindered the orientation of the nylon crystals.

Sun et al. ([2009\)](#page-110-0) have proposed a model for iPP/organomodified clay composites when the content of clay is higher than the percolation threshold (Fig. 3.20).



Fig. 3.20 The proposed model for the shear-induced crystallization of iPP/OMMT composite with OMMT content higher than the percolation threshold. Reproduced with permission from Sun et al. ([2009\)](#page-110-0)

In particular, they found that when the shear strain was not big enough to destroy the fillers network in the matrix, the crystallization of iPP was similar with that of the unsheared sample. When shear strain was large enough, the fillers network was destroyed and clay layers were aligned along the flow direction. There formed oriented crystals including cylindrites and strings of spherulites, which were small in size because the aligned clay layers acted as heterogeneous nucleation agents to promote crystallization of iPP.

Rozanski et al. [\(2009\)](#page-110-0) studied iPP/PPMA/OMMT nanocomposites in order to clarify the augmented nucleation. They found that the level of clay dispersion was more important than molecular weight of iPP in the nucleation effect. Better exfoliation and dispersion of the clay in nanocomposites with the same o-MMT content denotes a decreased amount of iPP chains intercalated in o-MMT galleries and a larger interphase area between o-MMT platelets exposed and a surrounding polymer. Therefore, the orientation-induced nucleation is enhanced by the clay dispersion as also observed by Wang et al.  $(2005)$  $(2005)$  $(2005)$ . The morphology shown by crystallized iPP/PPMA/OMMT nanocomposites after shearing at  $2 s<sup>-1</sup>$  is reported in Fig. 3.21a and compared with that obtained in static conditions for the same nanocomposites (Fig. 3.21b). In Fig. 3.21a spherulites are clearly visible, whereas in Fig. [3.22b](#page-104-0) different polycrystalline aggregates composed by elongated sectors radiating from the same centres are evident. The authors stated that such structure might originate from instantaneous nucleation on neighbouring site or because the secondary growth did not fill sufficiently the space between earlier crystallized lamellae.

#### 3.5.3 Nanocomposites with Graphene

As we have seen some nanoparticles are able to direct the crystallization of the matrix material. Mitchell et al. [\(2015](#page-109-0)) have used time-resolving x-ray scattering techniques at a synchrotron beam line to follow the structural evolution in a



Fig. 3.21 SEM micrographs of etched iPP/clay nanocomposites crystallized (a) in static conditions (b) crystallized after shearing at 2  $s^{-1}$  in a plane parallel to the shear direction, shear direction—horizontal. Reproduced with permission from Rozanski et al. ([2009\)](#page-110-0)

<span id="page-104-0"></span>

Fig. 3.22 Schematic of the shear cell used with the scattering vector Q lies in the plane defined by the flow direction and the vorticity vector (Nogales et al [2004a\)](#page-109-0)





graphene/PCL composite. The composites were prepared by melt mixing using PCL ( $M = 65,000$  Da) and 14 nm graphene nanoplatelets. The compounded mixture was formed in discs or cylinders to facilitate mounting in the x-ray shear cells shown in Figs. 3.22 and 3.23.

The Couette arrangement shown in Fig. 3.22 is to allow the three-dimensional nature of the shear flow to be explored. Details of the design are described elsewhere (Mitchell et al. [2015\)](#page-109-0). As we can see in Fig. [3.24](#page-105-0), the graphene nanoflakes have a lateral extent of more than  $1 \mu m$ . Thus although we might anticipate the plane of the flake to lie parallel to the flow direction, it must lie normal to the velocity gradient, otherwise it will rotate and probably breakup.

The SAXS pattern (Fig. [3.25](#page-106-0)) shows the scattering typical of lamellar crystals which preferentially lie normal to the flow direction. The central streak we attribute to the graphene flakes which lie preferentially parallel to the flow direction. We know from previous work (See Chap. [5\)](http://dx.doi.org/10.1007/978-3-319-39322-3_5), that without the addition of the graphene nanoflakes, the sample would exhibit an isotropic distribution of lamellar crystal



<span id="page-105-0"></span>Fig. 3.24 TEM micrographs of the graphene nanoflakes

orientations. Clearly, the graphene nanoflakes have aligned in the shear flow, and these have templated the direction of the lamellar crystal growth, normal to the graphene sheet.

Lee et al. ([2003\)](#page-108-0) have studied the effect of graphene on the crystallization of poly(vinyl alcohol), where they found that samples containing  $0.5\%$  wt graphene exhibited a higher level of crystallinity (up to 19 %).

# 3.5.4 Summary

This chapter has shown that the addition of nanoparticles to polymer matrices or the formation of nanoparticles within a polymer matrix, as in the case of high molecular weight chains can have a dramatic effect on the morphology of the polymer matrix. In some cases, the nanoparticles act as an efficient nucleating agent and as such can direct the crystallization of the polymer in the case of a crystallizable polymer. The impact of the nanoparticles, clearly depends on the nature of the nanoparticles in terms of shape and chemical composition, the particular polymer matrix and on the nature of the dispersion of the particles within the polymer. What is clear is that the ability to control the morphology of a polymer using the behaviour of the

<span id="page-106-0"></span>

Fig. 3.25 SAXS pattern for a sample of PCL/graphene sheared for 1000 shear units at 1  $s^{-1}$ using the arrangement shown in Fig.  $3.22$  at  $100^{\circ}$ C and cooled to room temperature at  $10$  C/min. The flow direction is vertical and the velocity gradient horizontal

nanoparticles provides a powerful approach to control the scales of structure in these novel polymer composites, and this is explored in the remaining chapters of this book.

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# Chapter 4 Theoretical Aspects of Polymer Crystallization

Wenbing Hu and Liyun Zha

# 4.1 Introduction

A vast amount of natural and synthetic polymers are semicrystalline. From this standpoint alone, it is necessary to understand the process of polymer crystallization, which dominates the structure formation of semicrystalline polymers and thus allows us to control their morphologies and properties. Polymer crystallization is influenced by many factors, such as chemical structures, compositions, temperatures, and thermal history. The theoretical models serve as a powerful tool for us to comprehend these factors in polymer crystallization.

Thermodynamics and kinetics are the two most fundamental theoretical aspects of polymer crystallization. Thermodynamics addresses why, or under which circumstances, polymer crystallization will begin, or in the opposite direction polymer crystals will start to melt. Kinetics addresses how fast polymer crystallization will be initiated, be developed, and be further improved. Both aspects decide crystal morphologies that eventually influence the properties of polymer materials.

This chapter intends to make a brief survey on our current theoretical understanding about the basic thermodynamics and kinetics of polymer crystallization. On thermodynamics, we will introduce the melting point, metastable states, phase diagrams, mesophase formation, as well as those factors governing melting points. On this aspect, the mean-field lattice theory on the statistical thermodynamics of crystallizable polymer solutions will be focused. On kinetics, we will introduce the basic knowledge about crystal nucleation, crystal growth, and crystal annealing. On this aspect, the classical nucleation theory and the related kinetic equations will be focused.

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Due to length limitation of this chapter, many theoretical approaches on the phenomenological aspects of polymer crystallization have to be skipped. The isothermal and non-isothermal kinetic analysis of overall crystallization appears as technically important in the data treatment of DSC measurements. Some theoretical considerations on the metastable aspects of crystal morphologies and their evolution under various circumstances appear as practically important and case sensitive (see Chap. [1](http://dx.doi.org/10.1007/978-3-319-39322-3_1)). In this sense, a combination of this chapter with other contributions of this book will provide reader a broad cutting-edge knowledge about our basic understanding of polymer crystallization.

### 4.2 Thermodynamics of Polymer Crystallization

### 4.2.1 Basic Concepts

Polymers are either in the fully amorphous state or in the fully crystalline state, or in the states partial between them. When they are in the amorphous state of homogeneous solutions or melt, polymer chains are fully disordered, as described by a random-coil model. The random-coil model was first proposed by Kuhn [\(1934](#page-151-0)) as well as by Guth and Mark [\(1934](#page-150-0)) to predict the entropic elasticity of polymer chains, and then was used to describe the amorphous state of polymers by Flory [\(1953](#page-150-0)) and others.

Polymer crystallization and melting are typically first-order phase transitions between the amorphous phase and the crystalline phase. When these two phases are in thermodynamic equilibrium, two phase transitions are thermodynamically reversible under a certain temperature. This temperature is referred to the equilibrium melting point of polymer crystallization. The free energy changes of amorphous phase and crystalline phase under various temperatures are depicted in Fig. [4.1,](#page-114-0) illustrating the definition of the equilibrium melting point  $T_{\text{m}}^0$ .

In the bulk system of pure polymers, the free energy change of melting becomes zero when the system is under its equilibrium melting point, as given by

$$
\Delta F_{\rm m} = \Delta Q_{\rm m} - T_{\rm m}^0 \Delta S_{\rm m} = 0 \tag{4.1}
$$

The equilibrium melting point can accordingly be calculated by

$$
T_{\rm m}^0 = \Delta Q_{\rm m}/\Delta S_{\rm m} \tag{4.2}
$$

In practice, to get over the nucleation barrier via thermal fluctuations, the initiation of primary crystal nucleation requires a crystallization temperature  $T_c$ something lower than  $T_{\text{m}}^0$ , and thus a supercooling for crystallization is defined as

<span id="page-114-0"></span>

Fig. 4.1 Schematic free energy curves of amorphous phase and crystalline phase versus temperature. The temperature at which two curves intersect with each other is defined as the equilibrium melting point of polymers



Fig. 4.2 Illustration pictures on the models of (a) fringed-micelle (Hermann et al. [1930](#page-150-0)) and (b) adjacent chain-folding (Keller [1957](#page-151-0))

$$
\Delta T = T_{\rm m}^0 - T_{\rm c} \tag{4.3}
$$

In order to overcome the kinetic barrier under a certain supercooling, polymer crystallization commonly chooses a pathway favoring its kinetics, which will result in metastable semicrystalline states (Cheng [2008](#page-150-0)). It took a long time for people to figure out the structure features of the metastable semicrystalline polymers, with two dominant models, i.e., fringed-micelle and chain-folding models, as illustrated in Fig. 4.2. Here, the metastable state holds either a thermodynamic meaning as its local minimum in the free energy landscape, or a dynamic meaning with its negligible changes over the time window of our observations upon a very slow evolution towards more stable states.

In 1930, Hermann et al. set up the fringed-micelle model (Hermann et al. [1930;](#page-150-0) Hermann and Gerngross [1932](#page-150-0)) to describe the high elasticity of low-density



Fig. 4.3 Illustration pictures on the models of (a) Switchboard (Flory [1962\)](#page-150-0) and (b) variable clusters (Hoffman [1983\)](#page-150-0)

polyethylene products. But later on, this model could not explain the spherulite morphologies of polymer crystals often observed under optical microscopy. In 1957, Keller set up the adjacent chain-folding model (Keller [1957\)](#page-151-0) on the basis of the facts that polymer stems in single lamellar crystal grown from dilute solutions were perpendicular to the lamellar surface, and the lamellar thickness was only in the scale of one tenth of chain lengths. This model was then confirmed by the small-angle neutron scattering (SANS) experiments of single crystal grown in dilute solutions (Spells et al. [1980\)](#page-153-0) as well as by the integer folding of short chains in lamellar crystals grown in the melt (Arlie et al. [1966](#page-149-0), [1967](#page-149-0); Ungar et al. [1985;](#page-153-0) Organ and Keller [1987\)](#page-152-0). For lamellar crystals grown in the longchain melt, Flory proposed the "Switchboard" model (Flory [1962\)](#page-150-0), which was then developed into the interzonal Switchboard model as discussed by Mandelkern [\(1964](#page-152-0)). Since both adjacent chain-folding and Switchboard models have their own interpretations on the same SANS experiment data, there was a hot debate in 68<sup>th</sup> Faraday Discussion Meeting. It is now well accepted that either model describes a certain aspect of structural features on lamellar crystals grown in the melt. The variable cluster model synthesizing both features of local chain-folding and global random-coil was discussed by Hoffman [\(1983](#page-150-0)). The loops, cilia, and tie molecules (Fig. 4.3) are restricted at the fold-end surfaces of lamellar crystals, which constitute the rigid amorphous phase near the crystalline region. The latter pretends to be the third phase besides the mobile amorphous phase and the crystalline phase, and appears as important in the thermal and mechanical properties of semicrystalline polymers (Wunderlich [2003](#page-153-0)).

As will be introduced in the following kinetic aspects of polymer crystallization, secondary intramolecular crystal nucleation favors chain-folding upon crystal growth, which dominates the lamellar feature of crystal morphologies. The metastable lamellar crystals intend to perform thickening into a more thermodynamically stable state upon annealing. Before they are able to reach the most stable state, their melting points appear as lower than the equilibrium melting point of infinitely large crystals. This is mainly because of a limited dimension in lamellar thickness. The lowered melting point of lamellar crystals  $T_m$  is described by the well-known Gibbs–Thomson equation, as given by

$$
T_{\rm m} = T_{\rm m}^0 - \frac{2\sigma_{\rm e}T_{\rm m}^0}{l\Delta h} \tag{4.4}
$$

where  $\sigma_e$  is the free energy density of the fold-end surface, l is the lamellar thickness, and  $\Delta h$  is the heat of fusion.

A wide distribution of lamellar thickness in polymer crystals results in a broad range of melting temperature, shown as a wide melting peak in the heating curve of differential scanning calorimetry (DSC). We pragmatically define the peak temperature as the experimentally observed melting point of polymer crystals, which could be far below the equilibrium melting point due to the limited lamellar thickness.

Crystallization under various temperatures yields different corresponding lamellar thicknesses, exhibiting different variable melting points. This phenomenon allows us to derive the equilibrium melting point at the infinitely large crystal according to the Gibbs–Thomson equation, provided that there is no annealing effect upon heating the crystals for the measurement of their melting points. However, most of metastable crystals do perform annealing behaviors upon heating towards melting. Hoffman and Weeks [\(1965\)](#page-150-0) supposed that lamellar crystals will thicken into a metastable state with the thickness several times larger than the minimum thickness, and derived the equilibrium melting point as the crossover point of the extrapolated  $T_{\rm m}$  versus  $T_{\rm c}$ curve at  $T_m = T_c$ . Although the fixed folds of thickness increase appear as a big assumption, this method has been widely applied to derive the equilibrium melting points of various semicrystalline polymers in the literature.

Besides crystallization, liquid–liquid (L–L) demixing is another basic phase transition in polymer solutions, and both of them are functions of polymer concentrations and temperatures. The schematic L–L binodal and liquid–solid (L–S) coexistence curves in polymer solutions are separately shown in Fig. 4.4. The



Fig. 4.4 Schematic pictures of (a) L–L binodal curve and (b) L–S coexistence curve in polymer solutions



polymer volume fraction

illustrated L–L binodal contains an upper critical solution temperature. Some solution binodals may contain a lower critical solution temperature, or even both.

When the L–S curve intersects with the L–L curve in the overlapping temperature windows, both curves will be terminated at the intersection point, which is referred to the monotectic triple point. The typical phase diagram in polymer solutions is shown in Fig. 4.5.

In between the amorphous phase and the crystalline phase, there sometimes occurs an important intermediate phase for polymers carrying anisotropic groups (called mesogen groups) either on the chain backbone or on the chain branches, which is referred to mesophase. The mesogen groups become orientational-ordered under suitable thermodynamic conditions. This ordered state could be the wellknown liquid crystal (LC) state, as a typical mesomorphic state between the amorphous state and the crystalline-ordered state for LC polymers.

The transition temperature from LC mesophase to melt is often named as the clearing point or the isotropization point  $T_i$ . If the LC mesophase is thermodynamically stable, it will occur in both heating and cooling curves when detected by DSC measurements. This mesophase is also referred to the enantiotropic mesophase. If the mesophase is kinetically favored due to large supercooling required for the initiation of crystallization, it will occur only in the cooling curve but not in the heating curve. This mesophase is then referred to the monotropic mesophase. The free energy plots for the two kinds of mesophases are demonstrated in Fig. [4.6](#page-118-0).

When L–S phase transition is accompanied by LC transition, the above phase diagram of polymer solution becomes more complicated as illustrated in Fig. [4.7.](#page-118-0)

According to the phase diagram schematically shown in Fig. [4.7](#page-118-0), two types of liquid crystal ordering with different preparation methods can be categorized. One is the lyotropic liquid crystal approached by changing the concentration in solutions. The other is the thermotropic liquid crystal approached by changing the

<span id="page-118-0"></span>

Fig. 4.6 Schematic pictures of (a) enantiotropic mesophase and (b) monotropic mesophase



temperature in the concentrated solutions or in the bulk phase. Their conventional preparation methods are schematically shown in Fig. 4.7. According to Onsager's interpretation (Onsager [1949](#page-152-0)), the lyotropic liquid crystal results from an entropydriven phase transition due to anisotropic excluded-volume interactions of mesogens. When the concentration of rod-like molecules becomes high enough, the space for anisotropic particles to move freely appears limited, resulting in an entropic loss. In this case, if parts of rodlike particles are aligned in parallel with each other in a domain of higher concentration, they release part of their space for the movement of other particles and thus increase the total entropy. This entropydriven phase transition makes the ordered system stable. For the thermotropic liquid crystal, Maier and Saupe's theory ([1959\)](#page-152-0) considers that the thermotropic liquid crystal is a result of orientation-dependent dispersion interactions between mesogens. With the decrease of temperature, spontaneous orientational ordering lowers the attractive potential energy. Combination of the above two theories gave a better interpretation to the orientational ordering for the formation of liquid crystals as well as a better calculation of phase diagrams (Jähnig [1979;](#page-151-0) Ronca and Yoon [1982,](#page-152-0) [1984;](#page-152-0) ten Bosch et al. [1983a,](#page-153-0) [b](#page-153-0); Khokhlov and Semenov [1985;](#page-151-0) Gupta and Edwards [1993](#page-150-0); Lekkerkerker and Vroege [1993\)](#page-152-0).

### 4.2.2 Statistical Thermodynamics of Polymer Crystallization

Statistical thermodynamic theories provide a powerful tool to bridge between the microscopic chemical structures and the macroscopic properties. Lattice models have been widely used to describe the solution systems (Prigogine [1957](#page-152-0)). Chang [\(1939](#page-149-0)) and Meyer ([1939\)](#page-152-0) reported the earliest work related with the lattice model of polymer solution. The lattice model was then successfully established by Flory [\(1941](#page-150-0), [1942](#page-150-0)) and Huggins [\(1942](#page-151-0)) to deal with the solutions of flexible polymers by using a mean-field approximation, and to derive the well-known Flory–Huggins equation.

In the lattice model of polymer solutions, polymer chain is simply represented by a number of consecutively occupied lattice sites, each site corresponding to one chain unit. The rest single sites are assigned to solvents. This simple lattice treatment of polymer solutions allows a very convenient way to calculate thermodynamic properties of flexible and semiflexible polymer solutions from the statistical thermodynamic approach. By the mean-field assumption, the entropy part and the enthalpy part of partition function can be separately calculated.

Following Flory's treatment of semiflexible polymer solutions (Flory [1956\)](#page-150-0), the entropy part of partition function for polymer solutions is given by

$$
Z_{\rm comb} \approx \left(\frac{n}{n_1}\right)^{n_1} \left(\frac{n}{n_2}\right)^{n_2} \left(\frac{q z_{\rm c}^{r-2}}{2e^{r-1}}\right)^{n_2}
$$
(4.5)

where  $n_1$  is the number of solvent molecules,  $n_2$  is the number of polymer chains, each chain composed of r monomers, and  $n = n_1 + n_2r$  is the total lattice sites occupied by solvent and polymer chains.  $q$  is the coordination number of the lattice space.  $z_c$  is the conformational partition function defined as

$$
z_{\rm c} = 1 + (q - 2) \exp\left(-\frac{E_{\rm c}}{kT}\right) \tag{4.6}
$$

<span id="page-120-0"></span>where  $E_c$  is the energy penalty for the  $q-2$  noncollinear consecutive bonds along the polymer chain with a reference to the collinear connection,  $k$  is Boltzmann constant, and T is system temperature.

The partition function related with the mixing enthalpy of solvent and monomers is given by

$$
z_{\rm m} = \exp\left[ -(q-2)\frac{n_1}{n} \times \frac{B}{kT} \right]
$$
 (4.7)

where  $\hat{B}$  is the energy change for a pair of solvent and monomer before and after mixing as defined by

$$
B = E_{12} - \frac{E_{11} + E_{12}}{2} \tag{4.8}
$$

As polymer crystals are commonly featured with parallel packing of polymer chains, the driving force for crystallization can be modeled as the parallel packing of bonds in the lattice model (Hu [2000](#page-151-0)). Assuming the energy penalty for nonparallel packing of two bonds is  $E_p$ , deviating from the ground state with parallel-packed bonds, the partition function related to nonparallel packing of neighboring bonds around a chain bond is given by Hu and Frenkel ([2005\)](#page-151-0)

$$
z_{\rm p} = \exp\left\{-\frac{q-2}{2}\left[1 - \frac{2(r-1)n_2}{qn}\right]\frac{E_{\rm p}}{kT}\right\} \tag{4.9}
$$

Thus after integrating different parts, the total partition function of polymer solutions can be described as

$$
Z = \left(\frac{n}{n_1}\right)^{n_1} \left(\frac{n}{n_2}\right)^{n_2} \left(\frac{q}{2}\right)^{n_2} e^{-(r-1)n_2} z_{\rm c}^{(r-2)n_2} z_{\rm m}^{rn_2} z_{\rm p}^{(r-1)n_2} \tag{4.10}
$$

The corresponding free energy density is calculated according to Boltzman's relationship, as given by

$$
\frac{f(\phi)}{k_{\rm B}T} = (1 - \phi)\ln(1 - \phi) + \frac{\phi}{r}\ln\phi \n+ \phi \left( -\frac{\ln(qr/2)}{r} - (1 - 2/r)\ln z_{\rm c} + (1 - 1/r) + (q - 2)\frac{B}{k_{\rm B}T} + (1 - 1/r)\frac{q - 2}{2}\frac{E_p}{k_{\rm B}T} \right) \n- \phi^2 \left( (q - 2)\frac{B}{k_{\rm B}T} + (1 - 1/r)^2 \frac{q - 2}{q}\frac{E_p}{k_{\rm B}T} \right)
$$
\n(4.11)

Equation (4.11) can be used to calculate various thermodynamic properties of polymers, in particular, the equilibrium melting point. It can be used to calculate the mixing free energy and the binodal L–L curve, as well as the coexistence L–S curve in polymer solutions.

<span id="page-121-0"></span>Following the protocols of molecular interactions set up in the lattice statistical thermodynamic theory introduced above, Monte Carlo simulations appear as a powerful tool in the study of both thermodynamics and kinetics of polymer crystallization (Hu and Frenkel [2005](#page-151-0)). Polymer motions in the simulations can be realized by a micro-relaxation model (Hu [1998](#page-151-0)). Its acceptance is judged by the Metropolis importance sampling algorithm (Metropolis et al. [1953](#page-152-0)), with the potential energy change in each step of micro-relaxation composed of three contributions, noncollinear connections of consecutive bonds along polymer chains  $(E_c)$  (Flory [1956\)](#page-150-0), mixed pairs of polymer monomer and solvent (B) (Flory [1942;](#page-150-0) Huggins [1942](#page-151-0)), and nonparallel packing of neighboring bonds  $(E_n)$  (Hu [2000\)](#page-151-0). The micro-relaxation model is highly efficient in relaxing local chain conformation and is a suitable approach for the study of polymer crystallization. Results from Monte Carlo simulations will be introduced along with theories of polymer crystallization in the following paragraphs.

## 4.2.3 Properties of Equilibrium Melting Points

### 4.2.3.1 Interaction Parameters

Although a precise measurement of the equilibrium melting point appears as a big challenge to the practical experiments, the statistical thermodynamic theory can predict equilibrium melting point on the basis of the mean-field assumption. Taking the fully ordered extended chains as the ground state, and considering bulk polymers with infinitely long polymer chains,  $r \rightarrow \infty$ ,  $n_1 = 0$ ,  $n = rn_2$ , one can get the free energy of the amorphous state from [\(4.11\)](#page-120-0),

$$
\frac{F}{nkT} = 1 - \ln z_c + \frac{(q-2)^2}{2q} \times \frac{E_p}{kT}
$$
(4.12)

At the equilibrium melting point, the free energy of the amorphous state is equal to that of the ground crystalline state (zero), so inserting the expression of  $z_c$ , one can derive

$$
1 + (q - 2)\exp\left(-\frac{E_c}{kT_m}\right) = \exp\left[1 + \frac{(q - 2)^2}{2q} \times \frac{E_p}{kT_m}\right] \tag{4.13}
$$

Supposing that the first term "1" in the left-hand side of the equation is relatively small, one can omit it and derives the equilibrium melting point of bulk polymers, as given by

$$
T_{\rm m} \approx \frac{E_{\rm c} + \frac{(q-2)^2}{2q} E_{\rm p}}{k \ln(q-2) - k}
$$
 (4.14)

From [\(4.14\)](#page-121-0), we can clearly see that a larger  $E_c$  (a higher rigidity of polymer chains) favors a higher equilibrium melting point. For polyolefins, larger substitute groups benefit their higher melting points because internal rotation of polymer chains becomes more difficult. For instance, the melting point of polyethylene (–  $(-CH_2CH_2)_n$ ) is 146 °C, the melting point of polypropylene  $(-CH_2CH(CH_3))_n$ –) is 187 °C while for poly-3-methyl-1-butene  $(-CH_2CH(CH(CH_3)_2))_n$ -), its melting point is 304 °C. Apparently, more rigid groups on the backbones benefit their higher melting point as well. For instance, the melting point of polyethylene  $( CH_2CH_2$ <sub>n</sub>–) is 146 °C, while with increasing benzene-ring density on the polymer chains the melting point of poly-p-xylene  $(-CH_2-\phi-CH_2-)_{n-1}$  is 375 °C and that of polyphenylene  $\left(-\left(-\phi-\right)<sub>n</sub>\right)$  is as high as 530 °C. Another example, the melting point of polyethylene adipate  $(-\text{CH}_2\text{CH}_2-\text{OCO}-\text{C}_6\text{H}_{12}-\text{OCO})_n$ -) is 52 °C, while the melting point of polyethylene terephthalate  $(-(CH_2CH_2-OCO-\phi-OCO)<sub>n</sub>$  is 265 °C, and that of polyethylene naphthalene-2,6-dicarbonoxylate  $(-CH_2CH_2)$ OCO– $\phi$ – $\phi$ –OCO)<sub>n</sub>–) reaches the highest 355 °C. Melting point of polymers with extremely high rigidity may be even higher than their thermal degradation temperature where their melt phase cannot be reached. On the other hand, a larger  $E_p$  favors also a higher equilibrium melting point. Longer side groups do not help the compact packing of backbone chains. Taking the melting points of  $(CH_2\text{-CHR})_n$  for example, if R group represents –CH<sub>3</sub>, –CH<sub>2</sub>CH<sub>3</sub>, –CH<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub>, and –CH<sub>2</sub>CH<sub>2</sub>CH<sub>2</sub>CH<sub>3</sub>, respectively, the corresponding melting points are 187 °C, 138 °C, 130 °C, and  $-55$  °C, respectively. The larger polarity of side groups also benefits the higher melting point of polymers. For instance, the melting point of polyethylene  $(-CH_2CH_2)<sub>n</sub>$  is 146 °C, while the melting point of polyvinyl chloride  $(-CH_2CHCl)<sub>n</sub>$  is 227 °C and that of polyacrylonitrile  $(-CH_2CHCN)<sub>n</sub>$  is 265 °C. In the last case, the sequence regularity becomes a minor factor for the capability of crystallization.

The linear relationship between the melting points and  $E_p/E_c$  values in [\(4.14\)](#page-121-0) is further confirmed by Monte Carlo simulations of polymers, and the results are shown in Fig. [4.8](#page-123-0). The high consistency in the results between the lattice theory and Monte Carlo simulations validates the mean-field treatment in the lattice theory of polymer solutions.

#### 4.2.3.2 Molecular Weights

In the equilibrium states of polymer crystals, the chain ends can be regarded as the crystalline defects in the infinitely large crystals formed by extended chains, which will apparently result in a depression of melting points with the increase of concentrations of chain ends, or in other words, with the decrease of chain lengths.

In the calculation of melting point of polymers with different molecular weights, Flory and Vrij [\(1963](#page-150-0)) divided the free energy change of melting into three parts. The first part is the free energy change for the melting of infinitely long polymers, the second part is the free energy change by introducing chain-end defects in the crystals, and the third part is the conformational entropy change when the infinitely

<span id="page-123-0"></span>

Fig. 4.8 Melting temperature ( $T_m/E_c/k_B$ ) of bulk polymers with variable  $E_p/E_c$  values. The Solid line is calculated from  $(4.13)$  $(4.13)$  and the *circles* are simulation results of 32-mer polymer solutions with a concentration of 0.9375 in a  $32<sup>3</sup>$  cubic lattice (Hu and Frenkel [2005\)](#page-151-0)

long polymer chain is cut into the segments with limited chain length r. So the total free energy change of melting can be described as

$$
\Delta F_{\rm m} = r \Delta F_{\rm u} + \Delta F_{\rm e} - kT_{\rm m} \ln r = 0 \tag{4.15}
$$

 $\Delta F_u$  is the free energy change of fusion, it can be calculated by

$$
\Delta F_{\rm u} = \Delta h_{\rm u} - T_{\rm m} \Delta s_{\rm u}
$$
  
=  $E_{\rm c} + \frac{(q-2)^2}{2q} E_{\rm p} - k_{\rm B} T_{\rm m} [\ln(q-2) - 1]$  (4.16)

 $\Delta F_e$  is the extra free energy change due to the existence of chain ends, which can be calculated from the equilibrium condition  $f = 0$  in [\(4.11\)](#page-120-0) by setting the chain length  $r = 2$  in the melt phase.

$$
\Delta F_e = \frac{(q-2)(q-1)}{2q} E_p - k_B T_m (\ln q - 1) - 2\Delta f_u \tag{4.17}
$$

The term  $\ln(r)$  represents a change of conformational entropy upon cutting. Inserting  $(4.16)$  and  $(4.17)$  into  $(4.15)$ , the equilibrium melting point predicted by the Flory–Vrij theory can be calculated.

One can also directly calculate the equilibrium melting point from ([4.11](#page-120-0)). Under equilibrium melting temperature,

$$
\mu^c = \mu^s \tag{4.18}
$$

where  $\mu^c$  and  $\mu^s$  are the chemical potentials of polymers in crystals and in solutions, respectively. We assume that  $\mu^c = 0$  by omitting any disorder defects in the crystals. When the chemical potentials in solid and liquid are equal, we can obtain the equation

$$
(1 - r)\frac{n_2r}{n} + \ln\frac{qn}{2n_2} + (r - 2)\ln\left[1 + (q - 2)\exp\left(-\frac{E_c}{k_B T_m}\right)\right]
$$
  
= 
$$
\frac{(r - 1)(q - 2)}{2}\left[1 - \frac{2(r - 1)n_2(n + n_1)}{qn^2}\right]\frac{E_p}{k_B T_m} + \frac{rn_1^2}{n^2}\frac{(q - 2)B}{k_B T_m}
$$
(4.19)

The equilibrium melting point of polymers can be calculated by taking into account all the parameters and solving (4.19).

Figure 4.9 compares the melting temperatures of bulk polymers with different chain lengths derived from the lattice theory, the Flory–Vrij equation and Monte Carlo simulations, respectively. The dimension of the temperature unit is reduced as  $E_c/(k_B T_m)$ . Although they hold various assumptions, their agreements are satisfying.

#### 4.2.3.3 Comonomer Contents in Random Copolymers

Real polymers are not structurally uniform along the sequences of the chain, and more or less there exist various kinds of irregularities, such as different chemical compositions, different geometrical connections, or different stereo optical isomers



Fig. 4.9 Melting temperature ( $T_m/E_c/k_B$ ) of polymers with different chain length. The Solid line is calculated from (4.19) and dashed line is results of Flory–Vrij equation. The Circles are results from Monte Carlo simulations of polymer solutions with a  $0.9375$  concentration in a  $32<sup>3</sup>$  cubic lattice for short chains and a  $64<sup>3</sup>$  cubic lattice for long chains (Hu and Frenkel [2005\)](#page-151-0)

of monomers. Because of the spatial mismatch between irregular and regular sequences for the compact packing in crystalline order, the irregular sequences will result in a lowered melting point. If the regular sequences are referred to monomer A and the irregular sequences are referred to comonomer B, Flory [\(1955](#page-150-0)) considered this AB random copolymer as an ideal solution and its chemical potential deviation from the sequence-uniform homopolymer A is

$$
\mu_{\rm A}^{\rm co} - \mu_{\rm A}^0 = -RT_{\rm m} \ln X_{\rm A} \tag{4.20}
$$

Thus, the chemical potential change of crystallization is

$$
\mu_{\mathbf{A}}^{\mathbf{c}} - \mu_{\mathbf{A}}^{\mathbf{co}} = \Delta H_{\mathbf{u}} - T_{\mathbf{m}} \Delta S_{\mathbf{u}} \tag{4.21}
$$

The subscript "u" represents the unit of mole chain monomers.

For homopolymer composed of monomer A, the chemical potential change of crystallization is

$$
\mu_{A}^{c} - \mu_{A}^{0} = \Delta H_{u}^{0} - T_{m}^{0} \Delta S_{u}^{0} = 0
$$
\n(4.22)

Considering  $\Delta H_u^0 \approx \Delta H_u$  and  $\Delta S_u^0 \approx \Delta S_u$ , the melting point of copolymers can be derived as

$$
\frac{1}{T_{\rm m}} - \frac{1}{T_{\rm m}^0} = \frac{R}{\Delta H_{\rm u}} \ln X_{\rm A}
$$
 (4.23)

The similar equation for stereo-optical-isomer copolymers with comonomers homogeneously distributed in the crystallites was also given by Coleman ([1958\)](#page-150-0).

Flory assumed all the comonomers staying only in the amorphous phase. By considering comonomers coexisting with monomers in the crystallites, Colson and Eby [\(1966](#page-150-0)), and later on Sanchez and Eby [\(1975](#page-152-0)) gave another expression for melting point of random copolymers, as given by

$$
T_{\rm m} = T_{\rm m}^0 \left( 1 - \frac{\Delta H_{\rm B}}{\Delta H_{\rm u}} X_{\rm B} \right) \tag{4.24}
$$

In (4.24),  $\Delta H_{\text{B}}$  is the heat of fusion for each comonomer as a defect in the crystalline phase, and  $X_B$  is the mole fraction of comonomers.

### 4.2.4 Phase Diagrams of Polymer Solutions

From ([4.11](#page-120-0)), the theoretical curves of L–S coexistence curve and L–L binodal curve can be separately calculated, provided by the absence of each counterpart.

At the equilibrium melting point, the chemical potential of polymers in the amorphous phase  $\mu^s$  is equal to that in the crystalline phase  $\mu^c$ , thus

$$
\mu^s - \mu^0 = \mu^c - \mu^0 \tag{4.25}
$$

where  $\mu^0$  is the chemical potential of the ground state where polymer chains are totally extended and packed in parallel with each other. Since in the crystalline phase,  $\mu^c$  is almost the same as  $\mu^0$ , we can thus derive that

$$
\mu^s - \mu^0 = \frac{\partial \Delta F^s}{\partial n_2} = -kT \frac{\partial \ln Z}{\partial n_2} \approx 0 \tag{4.26}
$$

It means

$$
\frac{\partial \ln Z}{\partial n_2} = 0 \tag{4.27}
$$

Thus, the equilibrium melting point can be calculated by solving the above equation. Changing the polymer concentrations, one can obtain the theoretical phase diagram of L–S coexistence.

The L–L binodal curve can be calculated by the chemical potential equivalence of components between the dense phase and the dilute phase after phase separation. That is,

$$
\begin{cases}\n\Delta\mu_{1a} = \Delta\mu_{1b} \\
\Delta\mu_{2a} = \Delta\mu_{2b}\n\end{cases} (4.28)
$$

where the subscripts "a" and "b" are used to represent the dense and dilute phases, respectively. Before reaching the final result, the mixing free energy as defined as the free energy change of polymer solutions from that of bulk amorphous polymers before mixing should be calculated, as given by

$$
\frac{\Delta F_{\text{mix}}}{kT} = \frac{F_{\text{solution}} - F_{\text{bulk}}}{kT} = -(\ln Z - \ln Z_{n_1=0})
$$
\n
$$
= n_1 \ln \phi_1 + n_2 \ln \phi_2 + n_1 \phi_2 \left[ (q - 2) \frac{B}{kT} + \left( 1 - \frac{2}{q} \right) \left( 1 - \frac{1}{r} \right)^2 \frac{E_P}{kT} \right]
$$
\n(4.29)

One can calculate the chemical potentials from (4.29) and insert them into (4.28), the equilibrium concentrations of dense and dilute phases under a certain temperature can be calculated. By changing temperature, the L–L binodal curve is thus obtained.

Monte Carlo simulations can calculate the phase diagrams of polymer solutions in a different way. In the lattice model of polymer solutions, each step of micro<span id="page-127-0"></span>relaxation in Monte Carlo simulations is determined by Metropolis sampling method with a potential energy barrier as described as

$$
\frac{\Delta E}{kT} = \frac{cE_{\rm c} + pE_{\rm p} + bB}{kT} = \left(c + p\frac{E_{\rm p}}{E_{\rm c}} + b\frac{B}{E_{\rm c}}\right) / \frac{kT}{E_{\rm c}}\tag{4.30}
$$

where  $c, p$ , and  $b$  are the numbers of net changes in noncollinear connection, nonparallel packing and mixing pairs of polymer unit and solvent after and before each step, respectively. Figure 4.10 shows the parallel results of liquid–liquid demixing curves and liquid–solid coexistence curves in polymer solutions with different energy parameter sets, obtained from the lattice mean-field theory and Monte Carlo simulations. Theoretical calculations and Monte Carlo simulations agree well with each other, again validating the mean-field theory.

In Fig. 4.10, one can clearly see that the L–S curve is mainly determined by  $E_p/$  $E_c$ , and the L–L curve is mainly controlled by  $B/E_c$  but is also slightly affected by  $E_p/E_c$ . By changing the values of  $E_p/E_c$  and  $B/E_c$ , the interplay between crystallization and liquid–liquid demixing can be studied in a combination of the lattice theory and parallel molecular simulations (Hu and Frenkel [2004;](#page-151-0) Ma et al. [2007](#page-152-0), [2008\)](#page-152-0), which has been introduced in the author's book (Hu [2013](#page-151-0)).

In the practical processing of polymers, many organic small molecules such as plasticizers, anti-UV agents and releasing agents are added as diluents, which also result in a depression of melting points. As deduced from Flory–Huggins equation, the chemical potential change in polymer solution is

$$
\mu_2^L - \mu_2^0 = RT_m \left[ \ln \phi_2 - (r - 1)\phi_1 + r\chi \phi_1^2 \right] \approx rRT_m \left( -\phi_1 + \chi \phi_1^2 \right) \tag{4.31}
$$

The chemical potential change upon melting is



Fig. 4.10 Theoretical calculation (a) and Monte Carlo simulations (b) of liquid–liquid demixing curves (dashed lines) and liquid–solid curves (solid lines) of polymer solutions with different energy parameter combinations, denoted by  $T(E_p/E_c, B/E_c)$  (Hu et al. [2003a\)](#page-151-0)



Fig. 4.11 Rescaled data from Fig. [4.10b](#page-127-0) according to (4.33). The bulk equilibrium melting temperature  $(E_c/k_BT_m^0)$  is chosen to be approximately 0.2. *Lines* are linear regressions of symbols at the same values of  $B/E<sub>c</sub>$  as labeled (Hu et al. [2003a](#page-151-0))

$$
\mu_2^s - \mu_2^0 \approx r \Delta H_u \left( 1 - \frac{T_m}{T_m^0} \right) \tag{4.32}
$$

 $\Delta H_{\text{u}}$  is the melting enthalpy of polymers per mole of monomers. When the amorphous phase and the crystalline phase become in equilibrium, their chemical potentials are equal. By combining [\(4.31\)](#page-127-0) with [\(4.32\)](#page-127-0) and making them equal to each other, the melting point of polymers in solution is derived as

$$
\frac{1}{T_{\rm m}} - \frac{1}{T_{\rm m}^0} = \frac{R}{\Delta H_{\rm u}} \left( \phi_1 - \chi \phi_1^2 \right) \tag{4.33}
$$

This equation was fitting well with experimental results (Prasad and Mandelkern [1989\)](#page-152-0). It was also verified by the results of Monte Carlo simulations (Hu et al. [2003a\)](#page-151-0). Figure 4.11 shows the linear relationship according to (4.33), with the data points adopted from Fig. [4.10b](#page-127-0).

### 4.3 Kinetics of Polymer Crystallization

### 4.3.1 Crystal Nucleation

Polymer crystallization can be roughly divided into two sequential processes: crystal nucleation and crystal growth. When the sizes of ordered domains generated by thermal fluctuations become so large that the trend to increase the surface free

<span id="page-129-0"></span>energy can be overcome by the trend to decrease the body free energy, larger domains intend to be more stable (Kelton [1991](#page-151-0)). The critical sizes and the related free energy barriers depend on the crystallization temperature. Therefore, a certain supercooling is required for crystal nucleation. Considering nucleus as a sphere with a radius  $r$ , the free energy change of nucleation can be estimated as

$$
\Delta G = -\Delta g \times \frac{4}{3}\pi r^3 + \sigma \times 4\pi r^2 \tag{4.34}
$$

 $\Delta g$  is the melting free energy of unit volume, and  $\sigma$  is the specific surface free energy. Schematic plot for the free energy change with the increasing radius of nucleus is shown in Fig. 4.12,

 $\Delta$ g in (4.34) is calculated as

$$
\Delta g = \Delta h - T_c \Delta s \approx \Delta h - T_c \frac{\Delta h}{T_m} = \Delta h \frac{T_m - T_c}{T_m} \propto \Delta T \tag{4.35}
$$

Generally speaking, there are three different types of nucleation according to various dimensions, i.e., primary nucleation, secondary nucleation, and tertiary nucleation. Primary nucleation is a nucleus newly formed by thermal fluctuations, with six extra nucleus surfaces if the nucleus is considered to be cubic. Secondary nucleation is two-dimensional nucleation on the advancing surface of nucleus, with four extra surfaces produced. Secondary nucleation is easier than primary nucleation as its free energy barrier is lower. Tertiary nucleation is one-dimensional nucleation at the step edge of the spreading layer on the advancing surface of nucleus, with only two extra surfaces produced. Tertiary nucleation is so fast that it can rarely be observed. The schematic pictures of different types of nucleation are shown in Fig. [4.13](#page-130-0).

Primary nucleation is the most observable phenomenon for the initiation of polymer crystallization, which can be categorized further into homogeneous nucleation and heterogeneous nucleation. In homogeneous nucleation, polymer nuclei can be treated as a cylindrical bunch of stems due to the anisotropic molecular structure, as depicted in Fig. [4.14.](#page-130-0)

Thus its free energy change during nucleation is

$$
\Delta G = -\pi r^2 l \Delta g + 2\pi r l \sigma + 2\pi r^2 \sigma_e \tag{4.36}
$$

Fig. 4.12 Schematic curve of the free energy change as the radius of nucleus formed in the amorphous phase



<span id="page-130-0"></span>

Fig. 4.13 Schematic pictures of (a) primary nucleation, (b) secondary nucleation, and (c) tertiary nucleation



Here, r and l are the radius and the length of the cylinder, respectively;  $\sigma$  is the specific free energy on the lateral surface, and  $\sigma_e$  is the specific free energy on the end surface.

By taking the minimum of  $\Delta G$  with respect to r and l, the critical free energy barrier for nucleation is derived as

$$
\Delta G^* = \frac{8\pi\sigma^2 \sigma_e}{\Delta g^2} \propto \Delta T^{-2}
$$
 (4.37)

The critical sizes are separately calculated as

$$
r^* = \frac{2\sigma}{\Delta g} \propto \Delta T^{-1} \tag{4.38}
$$

$$
l^* = \frac{4\sigma_e}{\Delta g} \propto \Delta T^{-1} \tag{4.39}
$$

So the length-to-radius ratio of the critical nucleus is

$$
\frac{l^*}{r^*} = \frac{2\sigma_e}{\sigma} \tag{4.40}
$$

<span id="page-131-0"></span>

For polymers, homogeneous nucleation can be realized through two typical ways. One is the so-called *intramolecular nucleation* (Wunderlich [1976](#page-153-0)) featured with adjacent chain-folding, which can be called as chain-folding nucleation. The other is the so-called intermolecular nucleation composed of parallel stacking among neighboring chains, which can be called as fringed-micelle nucleation. Schematic illustration of these two models can be found in Fig. 4.15.

Let us first consider the intramolecular nucleation. The specific free energy on the lateral surfaces of PE crystals was estimated to be  $11.8 \text{ erg/cm}^2$ , and its specific free energy on the fold-end surface was about 90  $\text{erg/cm}^2$  (Hoffman and Miller [1997\)](#page-150-0). By [\(4.40\)](#page-130-0), the optimized aspect ratio of critical nucleus is 15.3. Now look at the intermolecular nucleation. The end surface has an extra free energy of about 245 erg/cm<sup>2</sup> as estimated by Zachmann  $(1967, 1969)$  $(1967, 1969)$  $(1967, 1969)$  $(1967, 1969)$ , due to the entropy loss of disordered chains. So the aspect ratio of critical nucleus in intermolecular nucleation is as high as 56.8, and it appears very difficult to produce such kind of fibril nucleus through thermal fluctuations for primary nucleation. Moreover, by [\(4.36\)](#page-129-0), the higher end-surface free energy results in a higher nucleation barrier than the chain-folding model. So from both kinetics aspects of the critical nucleation barrier and of thermal fluctuations, the intramolecular nucleation is preferred in the process of primary nucleation.

Heterogeneous nucleation is primary crystal nucleation on the foreign surfaces of other materials such as catalysts, dusts, and container walls. Because less extra surface free energy is required, heterogeneous nucleation is much easier than homogeneous nucleation. Assuming that heterogeneous nucleus is a cubic nucleus, its free energy barrier is similar like homogeneous nucleation, again depending upon inverse square supercooling. When the foreign surface free energy is close to that of polymer crystals, the heterogeneous nucleation is more like a layer-by-layer growth on the foreign surface. We assume that  $a, b<sub>0</sub>$ , and l are its width, depth, and length, respectively, as shown in Fig. [4.16,](#page-132-0) the free energy change of nucleation is given by

$$
\Delta G = -ab_0 l \Delta g + 2b_0 l \sigma + al \Delta \sigma + 2ab_0 \sigma_e \tag{4.41}
$$

<span id="page-132-0"></span>

Fig. 4.16 Schematic picture of heterogeneous nucleation

In [\(4.41\)](#page-131-0),

$$
\Delta \sigma = \sigma + \sigma_{\rm cs} - \sigma_{\rm ms} \tag{4.42}
$$

 $\sigma_{\rm cs}$  is the surface free energy between crystal nucleus and substrate, and  $\sigma_{\rm ms}$  is the surface free energy between melt and substrate. If the free energy of substrate is almost the same as crystal nucleus,  $\Delta \sigma \approx 0$ , by minimizing  $\Delta G$  of a and l separately, the critical Gibbs free energy is

$$
\Delta G^* = \frac{4b_0 \sigma \sigma_e}{\Delta g} \propto \Delta T^{-1} \tag{4.43}
$$

There is also another type of primary nucleation called self-nucleation investigated first by Blundell et al. [\(1966](#page-149-0)). The foreign surfaces for self-nucleation are provided by crystals of the same species which survived during thermal history. Since there is no extra surface free energy change during self-nucleation, it is also called athermal nucleation. This type of nucleation is an important source of memory effects for polymer crystallization.

The nucleation rate is dominated by two factors. One is the critical free energy barrier of nucleation. Its exponential dependence was first proposed by Volmer and Weber [\(1926](#page-153-0)). The other is the diffusion energy barrier for molecules crossing over the liquid–solid interfaces. Its exponential dependence was first proposed by Becker and Döring  $(1935)$  $(1935)$ . The quantitative expression of the prefactor in the kinetic equation of the nucleation rate is given by Turnbull and Fisher [\(1949](#page-153-0)) as

$$
I = I_0 \exp\left(-\frac{\Delta E + \Delta G^*}{kT}\right) \tag{4.44}
$$

where  $\Delta E$  is the activation barrier for short-range diffusion over the liquid–solid boundary, and  $I_0$  is the prefactor. The critical free energy barrier is proportional to



Fig. 4.17 Schematic illustration on the temperature dependence (a) of the critical free energy barrier and the activation barrier for diffusion, and (b) of the bell-shape curve of the nucleation rates

the inverse square supercooling of primary nucleation. So when temperature is high with a high free energy barrier, the nucleation rate is small. However, when temperature is low with a high activation barrier for polymer diffusion, the nucleation rate is again small. Thus, the temperature-dependence curve of the nucleation rate is somewhat like a bell shape between the glass transition temperature and the melting temperature, as illustrated in Fig. 4.17.

At high temperatures, the kinetic studies of polymer crystallization is mostly focused on the nucleation. In this region, heterogeneous nucleation takes place and the resulted mechanical properties of the semicrystalline polymers are usually hard and brittle. While in the region of low temperatures, as a result of high density of small crystallites, the semicrystalline polymers become soft and tough.

Intramolecular nucleation is preferred in polymer crystal nucleation, both primary and secondary. The secondary intramolecular nucleation explains why chainfolding is a kinetic preference, which results in lamellar shapes during crystal growth. The typical intramolecular nucleation was investigated by Monte Carlo simulations of crystal nucleation of a single-chain system (Hu et al. [2003b](#page-151-0)). Taking the extended single chain in a crystal composed of extended parallel polymer chains as the ground state, and assuming the number of melting bonds  $n$ , the free energy change of the chain is

$$
\Delta F = \Delta f n + \sigma (N - n)^{2/3} \tag{4.45}
$$

where  $\Delta f$ *n* is the bulk free energy change and  $\sigma (N - n)^{2/3}$  is the surface free energy change. The free energy change of one bond during melting is

$$
\Delta f = \frac{q-2}{2} E_{\rm p} - kT \ln(q-1)
$$
\n(4.46)

The first term on the right-hand side means  $q - 2$  parallel bonds around the bond in the ground state, and the denominator "2" is the symmetric factor. The number of total conformation of a chain with *n* melting bonds is  $(q - 1)^n$ , so the second term is the average conformational entropy change of each bond during melting.

When the system is in equilibrium, the free energy in the disordered state is equal to that in the ordered state, then

$$
\Delta f_{\rm e} = \sigma N^{-1/3} \tag{4.47}
$$

And the equilibrium free energy barrier for primary nucleation is (Fig. 4.18)

$$
\Delta F_e = \frac{4\sigma^3}{27\Delta f_e^2} \tag{4.48}
$$

The free energy barriers for crystallization and melting of a single chain are separately calculated as follows,

$$
\Delta F_{\rm c} = \frac{4\sigma^3}{27\Delta f^2} \tag{4.49}
$$

$$
\Delta F_{\rm m} = \frac{4\sigma^3}{27\Delta f^2} + \Delta f N - \sigma N^{2/3}
$$
\n(4.50)

Equations (4.49) and (4.50) are confirmed by Monte Carlo simulations, as shown in Fig. [4.19.](#page-135-0) Single chains with different lengths will crystallize at the same temperature on cooling, but will melt at different temperatures on heating, with higher melting temperatures for higher chain lengths. In bulk polymers, the nucleation rates appear chain-length dependent, probably because the prefactor in the kinetic equation of nucleation could also be of chain-length dependence.



Fig. 4.18 Schematic free energy of single chain with number of melting bonds under thermal equilibrium state (Hu et al. [2003b\)](#page-151-0)

<span id="page-135-0"></span>

Fig. 4.20 (a) Strain-evolution curves of chain-folding probability of small crystalline clusters containing 50–200 parallel packed bonds under different temperatures. The lines are vertically shifted by  $0, 0.15, 0.25, 0.35, 0.45,$  and  $0.55$ , respectively. (b) Comparison between the onset strains of crystallization and the critical strain for fringed-micelle nuclei under different temperatures (Nie et al. [2013](#page-152-0))

It should be noted that intermolecular nucleation could coexist with intramolecular nucleation. Intermolecular nucleation is often observed with short chains, rigid chains, polymerizing chains, or when chains are stretched. Recently, upon stretching network polymers, the transition from intramolecular nucleation to intermolecular nucleation was observed in Monte Carlo simulations (Nie et al. [2013](#page-152-0)). By analyzing the probability of adjacent chain-folding of those newly formed crystallites with a size between 50 to 200 parallel packed bonds at each step of stretching, an obvious reduction was observed in its evolution curve under each temperature as shown in Fig. 4.20a. The corresponding critical strain was considered to be the transition point under which intramolecular nucleation is the favorite and above which intermolecular nucleation becomes the dominant.

Compared the critical strain with the onset strain of crystallization during stretching under each temperature as shown in Fig. [4.20b,](#page-135-0) it is found that at low temperatures (the dimension-reduced  $T < 4.0$ ) intramolecular nucleation dominates the initiation of polymer crystallization with a smaller strain than the critical value, and when temperature becomes higher, intermolecular nucleation begins to dominate the initiation of crystallization.

Recently, some researchers proposed a preordered structure in the polymer melt before nucleation. Imai and coworkers attributed the preordered structures to spinodal decomposition during orientational fluctuations at low temperatures for cold crystallization of PET (Imai et al. [1993,](#page-151-0) [1994\)](#page-151-0). The main proof came from the observation of small-angle X-ray scattering (SAXS) signal before wide-angle X-ray diffraction (WAXD) during isothermal crystallization at low temperatures (Terrill et al. [1998\)](#page-153-0). Sirota and Herhold [\(1999](#page-153-0)) and Kraack et al. ([2000\)](#page-151-0) observed a mesophase of chain cluster at the early stage of nucleation of long alkane chains and there is almost no supercooling for nucleation although the mesophase disappears as soon as chain-folding occurs in the crystallization of long-enough chains (Sirota [2000\)](#page-153-0). The idea of nucleation initiated by spinodal decomposition was then prevailing in many theoretical models. Olmsted and coworkers [\(1998](#page-152-0)) thought spinodal decomposition is a result of coupling between orientational-order fluctuations and density fluctuations at low temperatures. The spinodal decomposition will enhance crystal nucleation at a certain supercooling. In molecular dynamics simulations, Gee and coworkers [\(2005](#page-150-0)) observed that the crystallization behaviors of PVDF under 600 K and PE under 450 K in a time scale of nanoseconds appear as spinodal decomposition. Milner calculated the free energy change of PE crystal nucleation through a rotated mesophase, and it is lower than the surface free energy of orthogonal crystalline phase. He thought this could be the free energy barrier for crystal nucleation (Milner [2011](#page-152-0)). However, the prior occurrence of SAXS signal could be attributed to a limited instrument sensitivity or improper experiment treatment. Howard Wang thought that the signal like that of spinodal decomposition could be expected as a result of improper over-reduction in the empty correction (Wang [2006](#page-153-0)). Wang et al. ([2000\)](#page-153-0) attributed the phenomenon to instrument sensitivity of WAXD for the small number of crystallites in the early stage of crystallization. Indeed, improving the sensitivity of WAXD by four magnitudes, the difference between SAXS and WAXD disappeared at low temperatures as observed by Heeley et al. [\(2003](#page-150-0)). The remained difference at high temperatures can be associated to heterogeneous nucleation rather than homogeneous nucleation.

### 4.3.2 Crystal Growth

#### 4.3.2.1 Secondary Nucleation Models

After primary crystal nucleation, crystals begin to grow. The crystal growth may be diffusion-controlled or interface-controlled. If crystal grows under a large supercooling in dilute polymer solutions, the growth rate is mainly controlled by

a long-distance diffusion from the far-away bulk solution to the crystal surface. This is referred to the diffusion-controlled mechanism. The linear crystal growth rate is

$$
v = \frac{\mathrm{d}r}{\mathrm{d}t} \propto t^{-1/2} \tag{4.51}
$$

The diffusion-controlled mechanism means that the crystal size is not linearly dependent on the growth time (Holland and Lindenmeyer [1962](#page-151-0)). In the commonly practical cases, crystal growth is controlled by the process at the advancing surface of the crystal. This is referred to the interface-controlled mechanism. When controlled by this mechanism, the linear crystal growth rate is independent of time. The interface-controlled mechanism can be further separated into three categories, i.e., secondary nucleation growth, screw dislocation growth, and surface roughing growth. The secondary nucleation is prevailing in the description of the kinetics of lamellar polymer crystal growth (Flory and McIntyre [1955](#page-150-0); Burnett and Mcdevit [1957;](#page-149-0) Wunderlich and Cormier [1966;](#page-153-0) Wunderlich et al. [1967](#page-154-0)).

In experiments, for example, by small-angle laser scattering (SALS) on small crystallites, or by polarized light microscope (PLM) on large crystallites, it is found that the growth rate of lamellar crystals is independent of time. This behavior implies the surface-controlled mechanism for crystal growth. Thickening at the growth front is also observed in many experiments (Wunderlich and Mielillo [1968;](#page-153-0) Abo El Maaty and Bassett [2005](#page-149-0); Mullin and Hobbs [2011\)](#page-152-0). So the crystal growth process can be treated as two steps at the wedge-shaped growth front, secondary nucleation occurs first, followed with instant thickening until thickness becomes larger than the minimum thickness for further growth of lamellar crystals. Secondary nucleation dominates the temperature dependence of the growth rate, and thickening provides the driving force for crystal growth. As will be introduced below, Lauritzen-Hoffman model and its developments dominated the present understanding of growth kinetics of lamellar crystals. The intramolecular nucleation model recently provided a promising progress.

The linear crystal growth rate of lamella by lateral-surface advancing can be treated as the competition result between advancing rate and melting rate of the growth front. Taking intramolecular secondary nucleation as the rate-determining steps for both crystal growth and melting, they need to overcome the same nucleation energy barriers from mutually opposite directions. It is the difference of the two energy barriers  $\Delta G$  that determines the linear growth rate, as derived according to ([4.44](#page-132-0)) by

$$
v = v_{\text{growth}} - v_{\text{melting}} = v_{\text{growth}} \left( 1 - \frac{v_{\text{melting}}}{v_{\text{growth}}} \right)
$$

$$
= v_{\text{growth}} \left( 1 - \exp \left( -\frac{\Delta G}{kT_c} \right) \right) \tag{4.52}
$$

Assuming  $\Delta G$  is very small as reflected by the excess lamellar thickness above the minimum, and replacing the exponential term by the first two terms of Maclaurin expansion  $(\exp(x) = 1 + x + x^2/2 + x^3/6 + \cdots + x^i/i! + \cdots)$ , we can get the linear growth rate as

$$
v \approx v_{\text{growth}} \frac{\Delta G}{kT_{\text{c}}} = v_{\text{growth}} (l - l_{\text{min}}) \frac{b^2 \Delta g}{kT_{\text{c}}} \tag{4.53}
$$

In (4.53), the term  $l - l_{\text{min}}$  determines the net free energy for crystal growth, b is the average distance between stems inside the crystal, and  $\Delta g$  is the free energy change for melting of unit volume. Thus, we can treat  $v_{growth}$  in (4.53) as the free energy barrier for crystal growth and the rest part as the driving force for crystal growth (Ren et al. [2010\)](#page-152-0). Under low temperatures,  $l > l_{\min}$  and the crystal will grow, while under high temperatures,  $l < l_{\text{min}}$  and the crystal will melt. So temperature variation can lead to a continuous switching between growth and melting at the lateral growth front of lamellar crystals (Ren et al. [2010](#page-152-0)).

Lauritzen–Hoffman (LH) theory is still the most widely used theoretical model in the explanation of the growth kinetics of lamellar crystals. Figure 4.21 schematically shows the basic assumptions of folded stems at the growth front in the LH theory, without considering the thickening at the lateral growth front.

The LH theory holds four basic assumptions as listed below.

- 1. The growth front of polymer crystal is smooth. Secondary nucleation begins with a first stem deposited at the growth front, and follows with lateral spreading until reaching the lateral edges of the front substrate.
- 2. The chain-folded length l is constant during crystal growth. The width, thickness and number of stems are separately  $a_0$ ,  $b_0$  and v.
- 3. The number of growth fronts holding v stems  $N_v$  is in a steady-state distribution.
- 4. Each stem should go through an activation state before entering the crystal lattice where the fraction in each stem successfully entering the crystal lattice is  $\phi$ .

If the number of grown stems is  $v$ , the change of Gibbs free energy is

$$
\Delta G = 2b_0 l \sigma + 2(\nu - 1)a_0 b_0 \sigma_e - \nu a_0 b_0 l \Delta g \qquad (4.54)
$$

Fig. 4.21 Schematic picture of folded stems at the growth front considered in the LH theory



When  $v = 1$ , the growth rate for the first stem is

$$
A_0 = \beta \exp\left(-\frac{2b_0 l \sigma - \phi a_0 b_0 l \Delta g}{kT}\right) \tag{4.55}
$$

The melting rate of the first stem is

$$
B_0 = \beta \exp\left(-\frac{(1-\phi)a_0b_0l\Delta g}{kT}\right) \tag{4.56}
$$

If  $v > 1$ , the growth rate of the rest stems is

$$
A = \beta \exp\left(-\frac{2a_0b_0\sigma_e - \phi a_0b_0l\Delta g}{kT}\right) \tag{4.57}
$$

The melting rate of the rest stems is

$$
B = B_0 \tag{4.58}
$$

where  $\beta$  is a kinetic prefactor defined as

$$
\beta = \frac{kT}{h} \exp\left(-\frac{\Delta E}{kT}\right) \tag{4.59}
$$

By the assumption of a stable distribution of the growth fronts in the steady state, the growth flux of fronts is

$$
S = N_0 \beta \exp\left[ -(2b_0 \sigma - \phi a_0 b_0 \Delta g_f) \frac{l}{kT} \right] \left[ 1 - \exp\left( \frac{2a_0 b_0 \sigma_e - a_0 b_0 \Delta g_f}{kT} \right) \right] \tag{4.60}
$$

Different growth crystals contain different folded lengths.  $S(l)$  is the crystal growth flux with folded length l. Thus, the average length of all the crystals is calculated as

$$
\langle l \rangle = \frac{\int_{l_{\text{min}}}^{\infty} IS(l)dl}{\int_{l_{\text{min}}}^{\infty} S(l)dl}
$$
(4.61)

The result of (4.61) is

$$
\langle l \rangle = \frac{2\sigma_{\rm e}}{\Delta g} + \frac{kT}{2b_0\sigma} \times \frac{2 + (1 - 2\phi)a_0\Delta g/(2\sigma)}{[1 - \phi a_0\Delta g/(2\sigma)][1 + (1 - \phi)a_0\Delta g/(2\sigma)]}
$$
(4.62)

where  $2\sigma_e/\Delta g$  is the minimum length for steady growth. Equation (4.62) is used to predict the average thickness of lamellar crystals grown at different temperatures.

Besides an explanation of chain-folding lengths, the phenomenon of regime transitions can also be explained by the LH theory. If crystal growth is controlled by secondary nucleation, the temperature dependence of crystal growth rates can be dominated by

$$
G = G_0 \exp\left(-\frac{U}{T - T_0}\right) \exp\left(-\frac{K_g}{T \Delta T}\right) \tag{4.63}
$$

The first exponential term is attributed to short-range diffusion across the interface and the second term is attributed to secondary nucleation with the nucleation barrier proportional to the inverse supercooling. When temperature is high enough, crystal growth rate becomes mainly controlled by secondary nucleation. In this case, the curve of  $lgG + U/(T - T_0)$  versus  $-1/T/\Delta T$  can be divided into three linear regimes with the lowering of temperature, and the ratios of  $K_{\varrho}$  among three regimes are

$$
K_g(I) : K_g(II) : K_g(III) = 2 : 1 : 2
$$
\n(4.64)

The above ratio is the so-called regime-transition phenomenon, which can be explained on the basis of secondary nucleation assumed in the LH theory. When crystallization takes place at a very high temperature, the rate of secondary nucleation  $i$  becomes the rate-determining step, and the followed surface spreading rate g is very large, so  $i < g$ . The secondary nucleation is supposed under the determination of the free energy barrier for depositing the first stem (Lauritzen and Hoffman [1960](#page-151-0); Hoffman and Lauritzen [1961;](#page-150-0) Hoffman et al. [1976](#page-151-0)). Once the nucleus becomes stable, it will spread to the two lateral sides very fast with a layer thickness of  $b$ . The growth front with the width  $L$  is smooth until the next nucleus shows up. This temperature range is referred to Regime I and the crystal growth rate in this regime is

$$
G_{\rm I} = ibL \tag{4.65}
$$

Molecular simulations have reproduced regime-transition phenomena (Hu and Cai [2008\)](#page-151-0). However, the growth front of Regime I is rather rough, favoring an alternative interpretation based on the intramolecular secondary nucleation model (Hu and Cai [2008](#page-151-0)).

When temperature is lower than Regime I, the rate of secondary nucleation becomes higher and  $i \sim g$ . Several nuclei will grow together and the growth front will no longer be smooth. This temperature range is referred to Regime II. The advancing rate is proportional to the square root of secondary nucleation rate  $i$ , as given by

$$
G_{\rm II} = b(2gi)^{1/2} \tag{4.66}
$$

If the temperature is further lower than Regime II, secondary nucleation rate becomes much larger than the spreading rate,  $i > g$ . In this case, several crystal layers will grow at the same time, each layer with several nuclei and the distance between two nuclei is  $L'$ . This temperature range is referred to Regime III and the crystal growth rate is

$$
G_{\rm III} = ibL' \tag{4.67}
$$

In the LH theory, chain-folded length was assumed to be constant and thickening was omitted during crystal growth. Also the free energy barrier for secondary nucleation was assumed to be determined by the first stem, and no more stem was considered. These assumptions are not so reasonable and many other models (Armistead and Goldbeck-Wood [1992](#page-149-0)) have been proposed in order to reach a better understanding about the growth kinetics of lamellar crystals.

Wunderlich and Arakawa observed the layer structure of PE crystal under atmospheric pressures higher than 3 kbar and the crystallinity was almost 100 % (Prime and Wunderlich [1969\)](#page-152-0). In the crystals, polymer chains were perpendicular to the lamella and the largest thickness was even larger than the molecular length, which indicated the existence of extended chains in the crystals (Olley and Bassett [1977\)](#page-152-0). By further observation of the lamella growth front, Wunderlich found the wedge-shaped growth front and proposed a thickening-growth mechanism under high pressures (Wunderlich [1976\)](#page-153-0). In his explanation, molecular nucleation or secondary nucleation firstly took place at the growth front, and later-on developed into extended-chain crystals by fast thickening. By observing the growth process of PE folded-chain crystal (FCC) and extended-chain crystal (ECC), Hikosaka developed the growth mechanism with chain-sliding diffusion for thickening, on the basis of the LH theory (Hikosaka [1987,](#page-150-0) [1990](#page-150-0)). In his equation of nucleation rate, the free energy barrier for short-range diffusion across the interface was also considered besides the free energy barrier of critical nucleus. The growth appears as two-dimensional, which holds both lateral and longitudinal growth of the chain stems. The two-dimensional nucleation growth mechanism can be used to explain the dependence of lamella thickness on supercooling near the triple point of high pressures (Hikosaka et al. [1995](#page-150-0)).

Wunderlich and Mehta put forward the concept of molecular nucleation (Wunderlich and Mehta [1974](#page-153-0); Mehta and Wunderlich [1975](#page-152-0); Wunderlich [1979;](#page-153-0) Cheng and Wunderlich [1986\)](#page-150-0) in order to explain the molecular weight effect in crystallization of PE and some other polymers. At very high temperatures, the fraction of high molecular weights will crystallize first. It was proposed that each molecule entered the crystal with an additional nucleation barrier. Chain-folded secondary nucleus formed by molecules with enough lengths can only be stabilized over the critical size, while short-chain nucleus will be melted again, as illustrated in Fig. [4.22.](#page-142-0) The concept of molecular nucleation can be regarded as a patch on the LH model.

The free energy change of molecular nucleation at the growth front is

$$
\Delta G = -ab \Delta g + 2bl \sigma + 2(n-1)ab \sigma_e + 2ab \sigma_e' \qquad (4.68)
$$

<span id="page-142-0"></span>

Fig. 4.22 Schematic picture of molecular nucleation (Wunderlich [2005\)](#page-153-0)

 $\sigma_e$  is the surface free energy with chain cilia, thus the free energy change of critical nucleus is

$$
\Delta G^* = \frac{4b\sigma\sigma_e}{\Delta g} + 2ab\sigma_e' \tag{4.69}
$$

This critical free energy barrier is higher than normal secondary nucleation and thus the molecular nucleation can be the rate-determining step of crystal growth.

The intramolecular nucleation was then developed by supposing that all the secondary nucleation is mainly controlled by intramolecular nucleation (Hu et al. [2003b](#page-151-0); Hu [2007](#page-151-0)) and the basic crystal lamella is resulted due to the preference of chain-folding in this unique style of secondary nucleation.

Assuming secondary nucleation of a single chain at the two-dimensional locally smooth growth front, the free energy change based on the classical nucleation theory is

$$
\Delta F = \Delta f n + \sigma (N - n)^{1/2} \tag{4.70}
$$

The free energy barrier for crystal nucleation is

$$
\Delta F_{\rm c} = \frac{\sigma^2}{4\Delta f} \tag{4.71}
$$

And the equilibrium free energy barrier is

$$
\Delta F_{\rm e} = \frac{\sigma^2}{4\Delta f_{\rm e}}\tag{4.72}
$$

The free energy barrier for critical intramolecular nucleation under a certain temperature is independent of chain length, but not for the opposite direction, i.e., melting. Therefore, a critical molecular length exists for the equilibrium intramolecular melting at the growth front under each temperature. For a polymer sample with a polydispersity of molecular weights, only the fractions of chain lengths larger than the critical length can be stable and thus enter the crystal during secondary nucleation. This is the reason why molecular segregation occurs upon lamellar crystal growth. Molecular segregation can be observed only in polymer crystallization under very high temperatures.

Under a low temperature, the critical chain length for secondary nucleation may be much smaller than the chain length, and several events of intramolecular nucleation could happen along the same chains. If they occur in the same lamellar crystal, loops are formed; and if in different lamellar crystals, tie molecules are formed. The intramolecular nucleation model allows a statistical treatment on the semicrystalline texture.

The spreading right after the event of intramolecular nucleation may be stopped by the entanglements of long chains, collisions of nuclei at the same growth fronts, or the limited width at the growth front. Monte Carlo simulations (Hu et al. [2003c](#page-151-0)) have demonstrated that a single chain enters into the crystal growth front via several events of surface nucleation along the chain, as a result of limited growth-front sizes.

Besides molecular segregation (Hu [2005](#page-151-0)), many other phenomena unique for polymer crystal growth also favor the intramolecular nucleation model, such as co-crystallization of long and short chains (Cai et al. [2008;](#page-149-0) Jiang et al. [2015](#page-151-0)) as well as the interpretation of regime transitions (Hu and Cai [2008](#page-151-0)).

### 4.3.2.2 Other Non-nucleation Models

There are some models based on non-nucleation mechanisms for lamellar crystal growth. The (200) growth front of PE single crystals will become curvature when crystallization temperatures are very high, which could not be explained by the LH theory based on secondary nucleation growth on smooth surface. Also a pair of concave (110) surfaces were observed in the twin single crystal, which means the free energy barrier from side surfaces may not be the main problem for the advancing of the growth front (Sadler et al. [1986](#page-152-0)). Based on these observations, Sadler and Gilmer ([1988\)](#page-152-0) (SG) proposed the row model of continuous growth along the direction perpendicular to the growth front, as illustrated in Fig. [4.23](#page-144-0).

In the SG model, crystal unit will be randomly added in or be removed from the growth front with a free energy change. On the one hand, the longer the growth stem, the larger the driving force for advancing the growth front. The driving force is proportional to the difference between the stem length and the critical length for a stable stem. On the other hand, the thicker the growth front, the longer time needed to reach the critical stem length because chain extending is pinned by the metastable chain-folding or loops. The possibility of stem lengths among all the conformations is only


Fig. 4.23 Schematic pictures of the row model proposed by Sadler and Gilmer ([1988\)](#page-152-0)

$$
P = e^{-kl} \tag{4.73}
$$

Thus, the total growth rate is

$$
G \propto e^{-kl} (l - l_{\min}) \Delta g / (kT) \tag{4.74}
$$

The stem lengths exhibit two opposite trends of contributions to the total growth rate, and the maximum of growth rate will be realized at a certain stem length, which explains the growth thickness of the lamellar crystals. The thickness can be calculated as

$$
\langle l \rangle = l_{\min} + \frac{1}{k} \tag{4.75}
$$

Like in the LH theory, the free energy barrier for crystal growth in the SG model is related directly with the lamellar thickness without considering further thickening after crystal growth. Also, the proposed thermal roughening may still be flat at the crystal edge, without the necessity of curvature at the growth surface.

In both LH and SG models, the growth front was supposed to directly reach the critical thickness in the growth process, and the thickening after growth was neglected, which appears not so reasonable. Keller and coworkers (Keller [1992;](#page-151-0) Keller et al. [1994\)](#page-151-0) proposed a wedge-shaped growth-front model considering an obvious thickening in the crystal growth process of PE, as illustrated in Fig. [4.24](#page-145-0).

In the wedge-shaped growth model, the melt may first grow into a mesophase (hexagonal phase) in the thinnest region of the growth front. The mesophase is stable because of large specific surface energy of small crystallites, which is referred as the finite-size effect. Then, the thin lamella thickens into the stable orthogonal phase, which decides the lamellar thickness. There is a triple point Q, as demonstrated in Fig. [4.25.](#page-145-0) If temperature is above the triple point temperature, the melt will grow into the orthogonal phase directly. If temperature is below the triple point, there will be mesophase.

<span id="page-145-0"></span>

Fig. 4.24 Schematic picture of wedge-shaped growth front of PE lamella



reciprocal size

This model was later on expanded by Strobl ([2000,](#page-153-0) [2005](#page-153-0), [2006](#page-153-0), [2009\)](#page-153-0) to other polymers, in order to explain the experimental observations of his group, as illustrated in Fig. [4.26](#page-146-0).

There is a linear relationship between the crystallization temperatures and the inverse lamella thicknesses, which is quite in accordance with Gibbs–Thomson equation. There is also a linear relationship between the melting temperatures and the inverse lamella thicknesses. Crossover of these two linear curves is considered to be the triple point of mesophase transition. Recently, the crossover was reproduced in the molecular simulations of lattice polymers, and the interpretation was updated to an uplimit of instant thickening at the lateral growth front of lamellar crystals (Jiang et al. [2016\)](#page-151-0).

Allegra (Allegra [1977](#page-149-0), [1980;](#page-149-0) Allegra and Meille [1999](#page-149-0), [2005\)](#page-149-0) proposed statistical thermodynamic theory for the mesophase of small crystallites or crystal cluster in the metastable disordered phase before crystallization. The cluster will first grow into a stable size and then joins into the crystal, as illustrated in Fig. [4.27.](#page-146-0) The thickness of lamella is decided by the cluster size. Zhang and Muthukumar [\(2007](#page-154-0)) performed simulations of clusters to form single crystals grown in dilute solutions, consistent with the experimental observations.

<span id="page-146-0"></span>

Fig. 4.26 Schematic picture of mesophase at the growth front in lamella (Strobl [2009\)](#page-153-0)



Fig. 4.27 Schematic picture of equilibrium-sized cluster growth model (Allegra and Meille [2005\)](#page-149-0)

Muthukumar and coworkers (Welch and Muthukumar [2001;](#page-153-0) Muthukumar [2005](#page-152-0)) gave a thermodynamic explanation to the lamella thickness. He thought that the finite lamella thickness was a result of the largest thermodynamic stability of small crystallites. The crystalline chain will find the folded length related to the minimum free energy of the whole crystallite although there is a free energy barrier for the thickening of integer folding. The mechanism for crystal growth to select a limited lamellar thickness is recently addressed by the combination of secondary nucleation and instant thickening at the lateral growth front of lamellar crystals (Jiang et al. [2016\)](#page-151-0).

### 4.3.3 Crystal Annealing

Annealing is a procedure to keep the temperature of a crystal body near its melting point so as to relax its inner stress and to remove defects. When annealing is used for polymer materials, it can make metastable polymer crystals more perfect and more stable. If the annealing temperature is low, it just makes the crystal more

perfect by removing defects from crystal lattice. As a result, crystallinity is increased. If the annealing temperature is high, crystal thickening will happen and results in more stable crystals. If the annealing temperature is very high, even higher than the melting point of metastable crystals, crystals may melt and recrystallize into a more stable state unless the temperature is close to the equilibrium melting point of infinitely large crystals.

There are two mechanisms to explain lamellar thickening, one is *solid-chain* sliding-diffusion mechanism, and another is *melting-recrystallizaiton* mechanism. Peterlin ([1963\)](#page-152-0) proposed an activation energy barrier for sliding diffusion of folded chains in monolayer crystals, trying to explain why the folded length of polymer chains increases linearly with the logarithm of time. The sliding-diffusion mechanism was then developed into a more general theory by Sanchez and his collaborators [\(1973](#page-153-0), [1974\)](#page-153-0). Dreyfus and Keller [\(1970](#page-150-0)) proposed the fold-dislocation thickening model, in which the lamellar thickness can be doubly increased, as schematically demonstrated in Fig. 4.28. Another is the melting-recrystallization mechanism, which was firstly reviewed by Fischer ([1969\)](#page-150-0) and then introduced by Wunderlich [\(1976](#page-153-0)) in his famous book. This mechanism was confirmed by several experimental phenomena, such as decrease-then-increase of crystallinity in the annealing process (Matsuoka [1962\)](#page-152-0).

The phenomenon that lamella thickness increases with the logarithm of time has been observed in many experiments (Fischer and Schmidt [1962](#page-150-0); Wunderlich and Mielillo [1968\)](#page-153-0). This continuous thickening of mobile high-molecular-weight polymer crystals was simulated by Monte Carlo simulations (Wang et al. [2012\)](#page-153-0). Figure [4.29a](#page-148-0) demonstrates the wedge-shaped profile of the growth front resulted from the continuous thickening by chain-sliding diffusion at the growth front. Figure [4.29b](#page-148-0) provides three different growth-front profiles at different temperatures, which can be fitted into a logarithmic function of distances to the growth front. This function implies a logarithmic time dependence of crystal thickness. The prefactor in the function indicates an increasing thickening rate with increasing temperatures.



Fig. 4.28 Schematic picture of the fold-dislocation thickening model (Dreyfus and Keller [1970\)](#page-150-0).  $(a) \rightarrow (e)$  shows the thickening process of folded chain in a lamellar crystal. The space generated in this process should be filled by other stems  $(b')$  or be discharged by merging of stems  $(b'')$ 

<span id="page-148-0"></span>

Fig. 4.29 (a) Snapshot of the wedge-shaped lamellar crystal of high-molecular-weight polymers grown for 35000MCc under  $T = 4.6 E_c/k_b$  in the 64<sup>3</sup> cubic lattice and polymer occupation density was 0.9375. Parameters were set as  $E_p/E_c = 1$  for flexible chains and  $E_f/E_c = 0.02$  to allow chainsliding diffusion. The template was placed at the left end and only crystalline bonds were shown in yellow color. (b) Lamellar thickness as a function of distance to the growth front at three different temperatures  $T = 4.6$ , 4.8, and 5.0, respectively. The equations shown in the picture are the calculated logarithmic functions of distance  $D$  to the growth front (Wang et al. [2012](#page-153-0))

This continuous thickening is obviously controlled by the chain-sliding diffusion in the crystals. The similar thickness profiles at the edges of lamellar polymer crystals have been observed in experiments (Reiter [2014](#page-152-0)).

The logarithmic-time dependence of crystal thickness can be deduced easily. By assuming a frictional barrier ( $\Delta E<sub>s</sub>$ ) for chain-sliding diffusion proportional to the lamella thickness  $(l)$ , thus the thickening rate of monolayer lamellar crystal under a certain temperature is

$$
\frac{\mathrm{d}l}{\mathrm{d}t} \propto b e^{-al/k_b T} \tag{4.76}
$$

Equation (4.76) can be solved by

$$
l = c \ln t + d \tag{4.77}
$$

In the above equations,  $a, b, c$ , and  $d$  are the coefficients.

# 4.4 Summary

We made a brief introduction about our current theoretical models of thermodynamics and kinetics of polymer crystallization. We first introduced basic thermodynamic concepts, including the melting point, the phase diagram, the metastable state, and the mesophase. The mean-field statistical thermodynamics based on a <span id="page-149-0"></span>classic lattice model of polymer solutions, and its predictions on the melting points and phase diagrams were emphasized. Those molecular factors governing the melting points were also introduced. We then introduced crystal nucleation, crystal growth, and crystal annealing as the three basic stages of polymer crystallization. The classical nucleation theory as well as some recent ideas about primary nucleation were emphasized. On crystal growth, we introduced the secondary nucleation model, in particular, the well-known Lauritzen–Hoffman theory. The recently developed intramolecular nucleation model can be regarded as an updated version of secondary nucleation models. Some other models based on non-nucleation ideas were also introduced in a balanced way. The kinetics of crystal thickening, which is usually dominating crystal annealing, was also introduced under three typical circumstances.

Due to the length limitation, we have to skip many other theoretical aspects of polymer crystallization. We hope that our selected content above has already been strong enough to demonstrate the power of theoretical approaches, as a complemental to experimental approaches to gain a better understanding of the complicated polymer crystal morphologies.

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# Chapter 5 Controlling Morphology Using Low Molar Mass Nucleators

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# 5.1 Introduction

Crystallisation is a hugely important process in physical sciences and is crucial to many areas of, for example, chemistry, physics, biochemistry, metallurgy and geology. The process is typically associated with solidification, for example, in the purification of solids from a heated saturated solution familiar to all chemistry undergraduates. Crystalline solids are also often the end result of cooling liquids, or in some cases gases, but in order to form require nucleation, in the absence of nucleation supercooling of liquids well below the melting point is possible (Cavagna [2009](#page-170-0)). The quality of crystals, as gauged by size and levels of order, is highly variable, and will depend on factors such as material purity and the rate of cooling; rapid cooling may result in poor crystallisation, or even the formation of amorphous materials with no long-range order. In geological systems rates of cooling may vary over many orders of magnitude, for example, obsidian is a largely amorphous material produced when lava is rapidly cooled (Tuffen et al. [2013\)](#page-171-0),

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Fig. 5.1 Giant gypsum crystals in the Cueva de los Cristales in Chihuahua, Mexico, the scale is indicated by the person (photo A. Van Driessche)

while the gypsum crystals found in the Cueva de los Cristales in Chihuahua, Mexico can reach 10 m in length (Fig. 5.1) and are formed over hundreds of thousands of years. In this latter case, the formation of such large spectacular structures as shown in Fig. 5.1 can only be explained by a low nucleation rate (García-Ruiz et al.  $2007$ ; Van Driessche et al.  $2011$ ).

Crystallisation from solution is a core technology in major areas of the chemical industry and it is the critical initial step in many scientific programmes including structural studies of proteins and pharmaceuticals. The process of nucleation by which embryonic crystals form within a supersaturated solution remains largely unexplained. In classical nucleation theory, the volume excess free energy of the nuclei at a critical radius balances the surface excess free energy; nuclei larger than this critical radius grow, and smaller entities dissolve back into the solution. Recently, other pathways of transformation have been identified theoretically in which structure and density fluctuations are separated (Kashchiev et al. [2005](#page-170-0)). In terms of controlling morphology in polymers, nucleation of polymer crystals plays an important part in the production of several commodity plastics, giving the potential for control of the polymer microstructure and therefore the subsequent properties (Bassett [2006](#page-170-0)). Nucleating agents are thus of considerable commercial and scientific interest. One well-known example of a nucleating agent is 1,3:2,4-dibenzyline sorbitol (I) (DBS) the structure of which is shown in I; this is extensively used as a clarification agent with polypropylene. Its use leads to transparent materials with improved mechanical properties (Zweifel [2001](#page-171-0)). This chapter focuses on the use of nucleating agents to control the structure and morphology of polymers and focuses particularly on DBS and its derivatives (Nogales and Mitchell [2005](#page-170-0) Nogales et al [2003b;](#page-170-0) Nogales et al. [2016](#page-170-0)). In particular the work describes the self-assembly of such materials to form a template which can direct the crystallisation of polymers such as  $poly(\varepsilon$ -caprolactone) (Siripitayananon [2004](#page-171-0)).





#### 5.2 Organic Gelators

In general, gels are viscoelastic solid-like materials comprising an elastic crosslinked network and a solvent, which is the major component. The solid-like appearance of a gel is a result of the entrapment and adhesion of the liquid in the large surface area solid 3D matrix. DBS is an example of a low molar mass organic gelator (Terech and Weiss [1997](#page-171-0)) whose structure is shown in I; that is a gel derived from low molar mass compounds formed through self-aggregation of the small gelator molecules to produce entangled self-assembled fibrils (Smith [2009;](#page-171-0) Sangeetha and Maitra [2005](#page-171-0)). In the case of DBS typically these fibrils are of the order of about 10 nm in diameter and at sufficiently high DBS concentrations (generally less than 2 wt% depending on factors such as temperature and matrix polarity), the nanoscale fibrils form a three-dimensional network that promotes physical gelation in a wide variety of organic solvents and polymers.

The structures and properties of DBS-organogels formed in different solvents are well studied by Yamasaki and Tsutsumi (Yamasaki and Tsutsumi [1994](#page-171-0), [1995;](#page-171-0) Yamasaki et al. [1995](#page-171-0); Watase and Itagaki [1998\)](#page-171-0). All of those studies show that DBS builds up helically twisted fibres in low viscosity solvents. This is accompanied by a tremendous change in the rheological properties of these materials, as selfassembly leads to gelation. This gelation is based on physical interaction between the molecules. Gelation depends on various factors, such as gelator concentration, temperature and solvent polarity. It has also been shown (Yamasaki and Tsutsumi [1995\)](#page-171-0) that the DL-racemate is not able to self-aggregate; thus, chirality seems important in the self-organisation of DBS (though it might be expected that the L-enantiomorph would assemble in a similar form). Wangsoub et al. ([2016a,](#page-171-0) [b](#page-171-0)) have reported the properties and structure of gels formed from alkanes and dibenzylidene sorbitol, and the results are relevant in part to the use of DBS with polyethylene.

Gels of low molecular mass compounds are usually prepared by heating the gelator in an appropriate solvent and cooling the resulting isotropic supersaturated solution to room temperature. When the hot solution is cooled, the molecules start to condense and three situations are possible Fig.  $5.2$ : (1) a highly ordered aggregation giving rise to crystals i.e. crystallisation, (2) a random aggregation resulting

<span id="page-158-0"></span>

Fig. 5.2 Schematic representation of aggregation modes (redrawn after Sangeetha and Maitra [2005\)](#page-171-0)

in an amorphous precipitate, and (3) and aggregation process intermediate between these two yielding a gel (1). The process of gelation involves self-association of the gelator molecules to form long, polymer-like fibrous aggregates, which get entangled during the aggregation process forming a matrix that traps the solvent mainly by surface tension. This process prevents the flow of solvent under gravity and the mass appears like a solid. At the microscopic level, the structures and morphologies of molecular gels have been investigated by conventional imaging techniques such as SEM, TEM and AFM. At the nanoscale, X-ray diffraction, small angle neutron scattering and X-ray scattering (SANS, SAXS) are required to elucidate the structures(Grubb et al [1975\)](#page-170-0).

#### 5.3 Synthesis of Sorbitol Derivatives

D-Sorbitol, or D-glucitol, is a sugar alcohol that is produced commercially by the reduction of glucose, but is also found naturally in many fruits. It finds many uses as an ingredient in the food industry and as such is designated E420 (Hanssen and Marsden [1984\)](#page-170-0), though its use has been tainted with problems such as diarrhoea and flatulence. The dibenzylidene derivative is the main product of treatment with benzaldehyde, though mono and trisubstituted by-products may also be formed. Degradation and other studies confirmed that it is the 1,3:2,4 diacetal that is formed (Okesola et al. [2015](#page-170-0)). A range of other derivatives can be readily formed by the acid catalysed reaction of sorbitol with the appropriate substituted aldehyde (e.g. benzaldehyde, benzaldehyde  $d_6$  or 4-chlorobenzaldehyde) in cyclohexane

<span id="page-159-0"></span>

Scheme 5.1 Synthesis of Sorbitol derivatives

(Wangsoub et al. [2008\)](#page-171-0). A typical procedure that for 1,3:2,4-di(4-chlorobenzylidene) sorbitol (Scheme  $5.1$ ) was as follows. An aqueous solution of  $p$ -sorbitol  $(0.1 \text{ mol}, 70\% \text{ w/v})$  was placed into a round bottom flask equipped with Dean-Stark trap and condenser. To this was added 4-chlorobenzaldehyde (0.2 mol) and methanesulfonic acid (1 mL), cyclohexane (200 mL) and dimethylsulfoxide (6 mL). The mixture was heated to reflux with constant stirring. The mixture of cyclohexane and water was condensed and separated in the Dean-Stark arrangement. Once no further water was produced the reaction was stopped, and following neutralisation with triethylamine the white precipitate collected. Following purification by washing with dioxane and water 1,3:2,4-di(4-chlorobenzylidene) sorbitol was obtained as a white powder. The product was greater than 98% pure by  ${}^{1}H$ NMR, with a yield of 19.7 g,  $(46\%)$  and a melting point of 187 °C.

#### 5.4 DBS in Polymers

DBS and its derivatives can be easily dispersed in polymers using either melt mixing or mixing using a common solvent and drying. For the results shown here, the latter approach was used due to the small volume of material required. In this work we used the shear flow cell (Nogales et al. [2004](#page-170-0)) shown in Chap. [3](http://dx.doi.org/10.1007/978-3-319-39322-3_3) (Fig. [3.22](http://dx.doi.org/10.1007/978-3-319-39322-3_3)) and for this, samples were prepared by co-solvent mixing, for example, with PCL we employed butanone, drying and then melt pressing into discs.

Figure [5.3](#page-160-0) shows the phase behavior of the Cl-DBS/PCL system (Wangsoub et al. [2008](#page-171-0)). The line for the crystallisation temperature shows that the addition of the Cl-DBS increases the crystallisation temperature by  $\sim$ 10 °C due to the nucleating effect of the DBS derivative. This effect saturates at 1 % with Cl-DBS/PCL in contrast to  $\sim$ 3 % for DBS/PCL (Wangsoub et al. [2005](#page-171-0)). The upper curve shows the liquidus line separating the high temperature homogenous melt from the lower temperature 2-phase state of molten PCL and crystalline Cl-DBS fibrils. The liquidus line is shifted upwards by  $\sim$ 20 °C from the equivalent line for the DBS/PCL system (Wangsoub et al. [2005\)](#page-171-0) indicating a reduced solubility for Cl-DBS in PCL.

<span id="page-160-0"></span>

Fig. 5.4 A plot of the SAXS invariant  $\Omega$ , ([5.1](#page-161-0)) obtained from a sequence of time-resolving SAXS patterns recorded whilst cooling a 3 % Cl-DBS/PCL system from the higher temperature single phase region to room temperature at 10 °C/min (redrawn from Mitchell [2013](#page-170-0)). The *insets* show SAXS patterns taken at the temperatures corresponding to their position on the temperature scale

The phase behavior of the DBS or DBS derivative is dependent on both the chemical nature of the additive and the polarity of the polymer. For example, with DBS in PCL, the nucleating effect saturates at  $\sim$ 3 % whereas in polyethylene it saturates at a much lower concentration (Nogales et al. [2003a\)](#page-170-0).

Figure 5.4 shows the results of a cooling experiment from the single homogenous phase of a composition of 3 % Cl-DBS in PCL in which we plot the invariant [\(5.1\)](#page-161-0) calculated from the SAXS patterns recorded in a time-resolved manner. Each <span id="page-161-0"></span>SAXS pattern was recorded as a 2d dataset  $I(Q, \alpha)$ . The invariant  $\Omega$  was calculated using  $(5.1)$  (Mitchell [2013](#page-170-0)):

$$
\Omega = \int_0^{\pi/2} \int_{Q=0}^{Q_{\text{max}}} \left| \underline{Q} \right|^2 I\left( \left| \underline{Q} \right|, \alpha \right) \sin \alpha \, dQ \, d\alpha \tag{5.1}
$$

The invariant is related to the average of the electron density differences and for example in the early stages of crystallisation, it is proportional to the volume of crystals. In (5.1), Q is the scattering vector, whose magnitude is given by  $4\pi \sin(\theta)/\lambda$ , where 2 $\theta$  is the scattering angle and  $\lambda$  is the wavelength of the incident X-rays.  $\alpha$  is the angle between a specific direction and the scattering vector.

Initially the invariant has a low value and falls slightly with reduced temperature. At  $T \sim 127$  °C, the invariant increases sharply and this corresponds to formation of nanofibrils. Eventually at lower temperatures, the invariant plateaus and slightly falls. When the temperature reaches  $40\degree C$ , there is a second increase in the invariant which corresponds to the crystallisation of the PCL. It is clear that these two different ordering processes occur quite separately from each other. We can obtain more information about the state of the Cl-DBS in the 2-phase region by subjecting the material to a shear flow which leads to alignment of the Cl-DBS fibrils.

Figure [5.7a](#page-163-0) shows the SAXS pattern recorded in the 2-phase region. The horizontal streak corresponds to highly anisotropically shaped objects aligned parallel to the shear flow direction. Analysis of this scattering shows that it arises from objects with a radius of  $\sim$ 14 nm and a length greater than 100 nm (Wangsoub and Mitchell [2009](#page-171-0)). It is clear that a high level of anisotropy of these objects is achieved at modest shear rates. The level of anisotropy that can be achieved will also depend on the polymer and its molecular weight distribution.

Wangsoub et al. have reported the effects of the molecular weight distribution in the Polyethylene/DBS system (Wangsoub et al. [2016a,](#page-171-0) [b\)](#page-171-0). Samples were subjected to the same shear/temperature profile of 1000 shear units at 10  $s^{-1}$  at temperatures considerably higher than the melting point of each material. After cooling to room temperature at 10  $\mathrm{C/min}$  the samples were examined using wide-angle X-ray scattering and the azimuthal profiles for the 110 reflection are shown in Fig. [5.5](#page-162-0). The lowest two molecular weight matrix polymers, PE190 and GA, show only a modest level of anisotropy as judged from the small variation in intensity with azimuthal angle, whereas the highest two molecular weight matrix polymers, GX and PE26, show a marked level of anisotropy. We attribute this to the stress which develops during shearing in the melt and its effect of the orientation of the DBS fibrils. In the curve for 1 %DBS/PE26, the high molecular weight matrix polymer, there is evidence for a range of lamellar tilt angles, in the form of a four point pattern which usually occurs when the matrix polymer is under stress in the typical shish kebab structures (Pople et al. [1999](#page-171-0); Olley et al. [2014](#page-171-0)).

We have tested the effect of the DBS on the long period of the polyethylene GX and as Fig. [5.6](#page-162-0) shows for samples crystallised at different temperatures the long

<span id="page-162-0"></span>

Fig. 5.5 WAXS Azimuthal profiles for the 110 reflection in Linear Polyethylene samples with different molecular weight distributions as listed in Table 5.1 containing 1 % DBS crystallised from a sheared melt as described in the text





Table 5.1 Molecular weight characteristics of polymers used in the experiments reported in Fig. 5.5

Polymer	Mw	Mn	Mv	Type
Polymer code	Mw	Mn	Mv	Type
PE190	18,700	5410	10,000	Linear
GA	70.950	6250	45,000	Linear
G X	163,100	17,650	105,000	Linear
<b>PE26</b>	424,150	97,650	350,000	Linear

<span id="page-163-0"></span>

Fig. 5.7 (a) SAXS and (b) WAXS patterns recorded for a sample of Cl-DBS/PCL during shear flow 10 s<sup>-1</sup> in the 2-phase region of the phase diagram

period for GX alone or GX/DBS is essentially the same. In other words the role of the DBS is to direct the crystallisation of the polymer, the lamellar structure remaining unaffected.

Figure 5.7b shows the WAXS pattern for the equivalent system to that shown in Fig. 5.7a. The figure is a difference between the pattern recorded in the 2-phase region and that recorded in the homogenous high temperature phase. As the scattering from the molten polymer and the crystallised DBS will be additive, we can subtract the polymer scattering to give a clearer view of the pattern of the additive.

It is clear that the Cl-DBS exhibits an ordered crystalline phase. It is interesting that the DBS fibrils are crystalline. This gives them different physical characteristics to other fibrillar gel systems such as self-assembling polypeptide gels and the worm-like micellar systems. The crystal structure leads to very rapid crystal growth in one direction, whereas in the lateral direction, the crystal growth is slower and more fragile. As discussed elsewhere this may be a consequence of the chiral nature of the structures. Optical microscopy studies have shown that the DBS nucleates crystallisation of the DBS from the single phase melt of polymer and DBS. Shear flow may lead to breakage of fibrils whereas the self-assembled micellar systems are virtual polymers and can pass through each other by breaking and reforming. There is good experimental evidence that shear flow leads to some breakage of fibrils. Of course reheating to the single phase region and subsequent crystallisation would lead to repair but loss of any anisotropy which had developed.

Prolonged shearing of the system shown in Fig. 5.7 leads to some unexpected changes. The sequence of SAXS patterns in Fig. [5.8](#page-164-0) shows the effect increasing shear strain. We attribute the appearance of additional peaks in the pattern to a narrowing of the fibril diameter distribution. We have analysed the results using a Monte Carlo methodology to fit to Gaussian Distribution of Cylinder radii

<span id="page-164-0"></span>

Fig. 5.8 Selected SAXS patterns corresponding to shear strains of (a) 0, (b) 100 su, (c) 10,000 su and (d) 28,000; (e–h) Equatorial sections (*broken lines*) corresponding to shear strains of (e) 1000 su (f) 4000 su, (g) 13,000 su and (h) 28,000 su taken from patterns from the same series as shown in  $(a-d)$  but for the shear strains indicated. The *full lines* in the sections correspond to the best-fit

(Wangsoub and Mitchell [2009\)](#page-171-0). The extracted results are shown in Fig. [5.9](#page-166-0) with plots of the mean radius which is largely unchanged and the Gaussian radius distribution b. The width reduces sharply and reaches a plateau value between 5000 and 10,000 shear units (shear rate  $\times$  time of shearing).

Of other sugar alcohols, debenzylidene xylitol is widely used as a gelling agent; moreover, the three enantiomeric carbons in xylitol are arranged like a sequence of three carbons in xylitol. Dibenzylidene xylitol has been specified in the literature as a nucleating agent for polymers, but was not found to have any significant directing effect in polypropylene or polycaprolactone.

In contrast to the generation of row nuclei in polymers with a high molecular weight tail in the distribution, cessation of shear flow does not immediately lead to the relaxation of the oriented row nuclei. The aligned DBS fibrils remain aligned for quite some period (hours) which will doubtlessly in some cases lead to difficulty with experiments whilst attempting to remove prior history. Of course it may also prompt some novel methods of developing the anisotropy.

#### 5.5 DBS Directing Crystallisation

⁄-

We have shown in Sect. [5.4](#page-159-0) how by using shear flow in conjunction with a polymer containing a DBS derivative we can obtain aligned nanoscale fibrils which are arranged parallel to the shear flow. This can be achieved while the matrix polymer is in the molten state. If we now crystallise the sample, we can exploit these extended objects as row nuclei to direct the crystalline morphology of the matrix polymer. Figure [5.10](#page-166-0) shows a SAXS pattern recorded at Diamond on beamline I22 using the shear flow cell with Cl-DBS/PCL sample, after a cycle of shearing and cooling. The horizontal streak around the beam stop corresponds to the highly extended fibrils about 14–15 nm radius and greater than 100 nm long. The features above and below the beam stop are typical of small-angle scattering from semicrystalline polymers and relate to the lamellar crystal morphology. Clearly the level of preferred orientation of both the nanofibrils and the crystal lamellae is very high.

Figure [5.11](#page-167-0) shows the same type of information but revealed using electron microscopy coupled with differential etching. The extended object in the centre of the image is the impression of the DBS fibrils left in the polymer matrix after it was removed by etching. We can see that the main object is made up of smaller fibrils fused together. The highly aligned lamellae, seen here edge on, are easily visible and their geometric arrangement to the DBS nanofibrils is clear. In the following two images, the directing influence of the DBS nanofibrils can be easily observed. In Fig. [5.9b](#page-166-0) to the left beyond the end of the impression left by the nanofibril we can

Fig. 5.8 (continued) model for a set of polydisperse cylinders. The fitting parameters are plotted in Fig. [5.9.](#page-166-0) The horizontal black bar in the lower half of each pattern arises from a defect in the detector system during the measurements

<span id="page-166-0"></span>

Fig. 5.9 Plots of the mean diameter and the standard deviation of the Gaussian radius distribution as a function of increasing shear strain obtained from SAXS data using a Monte Carlo approach (redrawn from Wangsoub and Mitchell [\(2009\)](#page-171-0))

Fig. 5.10 Shows the SAXS pattern recorded for the 3 % Cl-DBS/PCL system after shearing at 80 $\degree$ C at a shear rate of  $10 s^{-1}$  This pattern was obtained at the Diamond Light Source beam line I22 (redrawn from Mitchell [2013\)](#page-170-0)



see a more random arrangement of lamellae. In fact we can now see some face on. Furthermore between the two nanofibrils which are not quite parallel with each other we can the two sets of directed lamellae impacting in the centre portion (Fig. [5.12](#page-167-0)).

<span id="page-167-0"></span>

Fig. 5.12 (a) Detail of a single cluster of DBS fibres (b) Polyethylene development from DBS fibres, right, compared with general development, left

Figure [5.13](#page-168-0) shows the interior surface of DBS/PE system (Wangsoub et al 2016b) prepared by cutting a sheared disc in half. We are now looking in a direction parallel to the aligned nanofibrils. The holes correspond to where the nanofibrils were, and subsequent etching has broadened the hole from its original size. We can see the excellent dispersion of the DBS nanofibrils.

<span id="page-168-0"></span>Fig. 5.13 A scanning electron micrograph of the surface of section cut through a sheared disc which was crystallised from a sheared melt of PE/DBS. The surface is perpendicular to the alignment of the DBS fibrils



#### 5.6 Model of Directed Crystallisation

In the case of highly aligned fibrils, consideration of the templating process reduces to a 2-d matter. The number density of fibrils is given by Wangsoub et al. [\(2008](#page-171-0))

$$
N = \frac{(f - f_c)}{nr_f^2}
$$

where f is the fraction of the additive and  $f_c$  is the upper limit of solubility of the additive in the polymer matrix. We consider all fibrils to have the same radius  $r_f$ .

If we associate a templated zone of radius  $r_t$  with each fibril, the fraction of templated material,  $f_t$ , (Fig. [5.14](#page-169-0)) is given by:

$$
f_{\rm t} = (f - f_{\rm c}) \frac{\pi r_{\rm t}^2}{\pi r_{\rm f}^2}
$$

Clearly, this is a very simple model without any distribution of fibril dimensions and the templated zone size does not account for a random spatial distribution of fibrils. However, we do have an estimate of the fibril radius of  $\sim$ 7.5 nm from the SAXS measurements and we have estimated for polyethylene that the templated zone has a radius ~100 nm. This suggests that the value of  $(f - f_c)$  needs to be greater than 0.014 to achieve full templating. Clearly the solubility of the sorbitol derivative in the polymer matrix is critical in determining the actual amount of additive required to achieve this. We previously estimated that the solubility limit of DBS in PCL was ~0.01 and we attribute in large part the enhanced templating of Cl-DBS to a reduction in the solubility limit in PCL. This is shown in the DSC and

<span id="page-169-0"></span>

liquidus line. In the examples of the morphology shown in Figs. [5.8,](#page-164-0) [5.9](#page-166-0) and [5.10](#page-166-0), the directing is more or less perfect and the hence the orientation parameter  $\langle P_2 \rangle$ describing the preferred orientation of the lamellae with respect to the flow axis is given by the fraction of material templated:

$$
\langle P_2 \rangle_{\rm L} = -0.5(f - f_{\rm c}) \frac{\pi r_{\rm t}^2}{\pi r_{\rm f}^2}
$$

The factor  $-0.5$  (Lovell and Mitchell [1981](#page-170-0)) takes account of the fact that the lamellae are arranged normal to the flow axis. The efficacy of the templating or directing process depends on the number density of the DBS fibrils. For a given amount of DBS, the number density can be optimised by making the nanofibrils as thin as possible. The processes described in this chapter are effective because of the lateral nanoscale of the fibrils.

# 5.7 Summary

We have shown that the inclusion of small amounts of DBS or selected derivatives leads to the formation of a well-dispersed system of nanofibrils. These are particularly effective in directing the crystallisation of polyethylene, polypropylene and  $poly(\varepsilon$ -caprolactone) due to the high number density of the fibrils in the sample. It may well be possible to extend to other polymer systems. Such work is underway. The approach offers distinct advantages over the other approaches described in other chapters in this volume. It avoids the use of viscous high molecular fractions to produce row nuclei. By using a nanoparticle it may be possible to achieve other

<span id="page-170-0"></span>orientations of the nanoparticles than parallel to the flow axis. The latter takes place because of the high level of anisotropy of the nanofibrils. The high aspect ratio of the nanofibrils means that any deformation of the polymer melt is likely to lead to a high level of orientation of the nanofibrils leading to a high level of preferred orientation of the lamellar crystals.

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# Chapter 6 Crystallization in Nanoparticles

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# 6.1 Introduction

Under particular circumstances, some polymers may crystallize. However, a polymer melt consists of an assembly of polymer chains that are coiled and mutually interpenetrated, and therefore it is impossible to attain an ideal crystalline state of extended straight chains with the endgroups assembled in planar interfaces, purely due to kinetic reasons. The required complete disentangling would need a very long time, as it is associated with an extremely high entropic activation barrier. Instead, a polymer melt cooled below the equilibrium melting point produces a system which is only in part crystalline. Semicrystalline polymers consist of a complex puzzle of crystalline lamellae, crystal-amorphous interphases, stacks of crystalline lamellae, liquid pockets, rigid amorphous phases, and fringed micellar crystals. The arrangement of these structural elements in a given polymer depends on different factors, including chemical structure, chain flexibility, thermal history, and orientation. The structure of semicrystalline polymers exhibits characteristic features depending on the length scales. In the  $10^{-8}$  m scale, in highly crystalline polymers, such as polyethylene (PE) (Wunderlich [1973](#page-188-0)) and in intermediate crystalline polymers, such as polyethylene terephthalate (PET) (Santa Cruz et al. [1991](#page-187-0)) or poly(etherketone)s (Bassett et al. [1988](#page-185-0)), there is an alternation between crystalline regions (lamellar crystals) and amorphous regions (interlamellar amorphous regions). With the exception of highly crystalline polymers, this alternation does not extend to the whole volume of the sample (Santa Cruz et al. [1991](#page-187-0)). The lamellae are packed into stacks which are separated by broad amorphous regions. The stacks can assemble

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themselves into superstructures, generally with spherical symmetry (spherulites) which can reach microns or even several millimeters.

Nowadays, current interest in the properties of polymers confined into nanometer scale is very intense, both from the fundamental and practical perspectives (Soles and Ding [2008](#page-188-0)). Polymers are extensively used in processes to fabricate nano-objects like wires of nanometer-scale diameters (Martín and Mijangos [2009;](#page-187-0) Chen et al.  $2012$ ; Martín et al.  $2012$ ) nanoimprinting (Soles and Ding [2008](#page-188-0)), and nanoscale polymeric particles (Landfester [2001\)](#page-186-0). Confined polymers are central to a broad range of advanced materials and emerging nanotechnologies (Coakley and Mcgehee [2004;](#page-186-0) Chen et al. [2012\)](#page-186-0), with applications including biomaterials (Yu et al. [2011](#page-188-0); Bonanno and Segal [2011\)](#page-186-0), micro- and optoelectronics (Yuan et al. [2011](#page-188-0); Tong et al. [2011](#page-188-0); Di Benedetto et al. [2008\)](#page-186-0), energy capture/storage (Li et al. [2012](#page-186-0); Cai et al. [2012](#page-186-0); Li and Malardier-Jugroot [2011](#page-186-0); Guan et al. [2011;](#page-186-0) Mohapatra et al. [2009\)](#page-187-0), among others. Besides cutting-edge fabrication strategies, control over the changes in properties induced by nanoscale confinement is a central issue to be taken into account. The rapid development of nano-science and nanotechnology in the twentieth and twenty-first centuries raises a lot of questions about the structure and surface properties of nano-materials (Svorcik et al. [2013](#page-188-0)). The prefix nano- is used in a broad way to describe systems where one or several physical dimensions have been reduced to length scales between 1 and 100 nm, and also to the application of concepts and understanding of properties (physical, chemical, biological, mechanical, ...) that derive as a result of the reduced length scale (Gates et al. [2005](#page-186-0); Martín Gago et al. [2008](#page-187-0)). The possible change in properties, when a material is nanostructured, is understood as confinement effects (Alcoutlabi and McKenna [2005\)](#page-185-0).

As for smaller molecules (Grigoriadis et al. [2011\)](#page-186-0), crystallization becomes even more sluggish when the chains are confined at the nanoscale level (Vanroy et al. [2013](#page-188-0); Liu and Chen [2010](#page-186-0)). Confinement is able to induce different morphologies (Asada et al. [2012](#page-185-0); Maillard and Prud'homme [2008\)](#page-186-0), reduce crystallization rates by several orders of magnitude (Despotopoulou et al. [1996](#page-186-0); Massa et al. [2003\)](#page-187-0), and in some cases, inhibition of crystallization within the experimental time scale (Capitán et al.  $2004$ ). Therefore, in order to widen the applicability of semicrystalline polymers at the nanoscale, the effect of confinement on the crystallinity and morphology should be considered.

Polymers confined in nanometer-sized geometries have been intensively investigated in the last decades, aiming both to achieve a deeper understanding of finitesize effects in soft matter and to improve the performance of nano-devices and hybrid materials (Napolitano et al. [2013](#page-187-0)). When designing and preparing nanostructures, one or several physical dimensions can be affected. For example, if a nanostructured polymer system is prepared in a way that two dimensions have macroscopic dimensions, while the remaining is in the nanometer scale, the resulting material is said to be one dimensionally confined (1D-confinement). This is the case of *polymer thin films*. If two dimensions have nanometer scales, one can talk about two dimensional confinement (2D-confinement), which is the case of *nanowires* and nanotubes. Finally, when all three dimensions are in the nanometer length scale,

such as in *nanoparticles*, the polymer is said to be three-dimensionally confined (3D-confinement). Moreover, confined polymer structures can be further processed to obtain *à la carte* nano-features, such as nanostructured surfaces on polymer thin films (Rebollar et al. [2011](#page-187-0)), alignment of polymer nanowires by percolation into nanoporous membranes (Garcia-Gutierrez et al. [2013;](#page-186-0) Martin et al. [2014\)](#page-187-0), or even physical responsive polymer nanoparticles (Deng et al. [2013](#page-186-0)).

Among the most studied confining geometries are thin films, probably due to their presence in a large number of technological applications, and also because it provides an easy control of the level of confinement and tunability of interfacial interactions between polymers and substrates (Rotella et al. [2011\)](#page-187-0). In this geometry, the sample thickness becomes a crucial parameter controlling crystallization (Vanroy et al. [2013](#page-188-0)), while surface effects mostly lead to a competition between adsorption to the solid surface and nucleation of polymer crystals (Reiter and Sommer [1998](#page-187-0); Vanroy et al. [2013;](#page-188-0) Napolitano and Wübbenhorst [2007](#page-187-0); Asada et al. [2012;](#page-185-0) Bertoldo et al. [2010\)](#page-185-0). Also, polymer thin films represent highly metastable forms of matter, presenting unexpected properties (Reiter and DE Gennes [2001\)](#page-187-0) which have been widely discussed by the scientific community in the past years (Forrest et al. [1997](#page-186-0); Tsui and Zhang [2001;](#page-188-0) Schönhals et al. [2002](#page-187-0); McKenna [2003;](#page-187-0) Wübbenhorst and Lupascu [2005](#page-188-0); Napolitano et al. [2013;](#page-187-0) Napolitano and Cangialosi [2013;](#page-187-0) Boucher et al. [2012](#page-186-0)). It is also possible to attain information of the role of interfacial interactions by intercalating a polymer thin film in between two adsorbing layers (Napolitano et al. [2013](#page-187-0)) although the introduction of burying interfaces limits the possible experimental protocols; for example, metallization of both polymer faces does not permit an optical access to the polymer surface.

On the other hand, using confined polymers into droplets and nanoparticles might serve as starting point in order to prepare nanocrystals and also to better understand the mechanisms involved during nucleation and crystallization in confined geometries (Massa and Dalnoki-Veress [2004;](#page-187-0) Li [2009](#page-186-0)) without including any preferential confined dimension. In this chapter, we present the crystallization behavior of polymers in confined nanoparticles.

#### 6.2 Generation of Polymer Nanoparticles

The formation of structured polymeric nanoparticles is of great importance for many applications. In general, polymer nanoparticles can be prepared from several heterophase methods. One of the most known methods, developed extensively by Landfester et al. during the last decade, is the so-called miniemulsion method (Landfester [2001,](#page-186-0) [2009](#page-186-0); Kietzke et al. [2007](#page-186-0)).

An emulsion consists of well-dispersed droplets of a substance into a continuous phase. This is formed by mixing two immiscible phases that are subjected to high shear, resulting in small, homogeneous, and narrowly distributed nanodroplets. The miniemulsion can be stabilized by means of surfactants. The protocol is sketched in Fig. [6.1.](#page-175-0)

<span id="page-175-0"></span>

Fig. 6.1 Sketch of the miniemulsion protocol to generate polymer nanoparticles

By using this method, polymer nanoparticles of different polymers have been reported (Martínez-Tong et al. [2013](#page-187-0), [2014;](#page-187-0) Landfester [2001](#page-186-0)). For amorphous polymers, the shape of the nanoparticles generated by this technique is spherical (Fig. [6.2](#page-176-0)). Variations of physical properties like the glass transition temperature of the polymer confined into the shape of this nanoparticles have been reported in the literature (Martínez-Tong et al. [2013](#page-187-0), [2014\)](#page-187-0).

Another approach for obtaining polymer nanoparticles is the so-called reprecipitation method, previously proposed by Shimizu et al. [\(2007](#page-188-0)). This method relays on crashing out hydrophobic polymer chains in solution by displacing a solvent with a non-solvent, generally water. Both polymer solvent and non-solvent must be miscible. As in the miniemulsion technique, reprecipitation can be used by starting from the bulk polymer of known molecular weight as the precursor material; only the nanoparticle diameter needs to be adjusted during the process by controlling solution concentration. The method is schematically described in Fig. [6.3.](#page-176-0)

Figure [6.4](#page-177-0) shows an AFM image of polyethylmethacrylate (PEMA) nanoparticles prepared by reprecipitation.

<span id="page-176-0"></span>Fig. 6.2 Atomic Force Microscopy (AFM) topography image of polystyrene (PS) nanoparticles prepared by the miniemulsion method after spin casting the miniemulsion on a silicon wafer. The starting material is the bulk polymer



 $1 \mu m$ 



Fig. 6.3 Sketch of the reprecipitation protocol to generate polymer nanoparticles

# 6.3 Modification of the Crystalline Morphology by Confinement into Nanoparticles

By the two previously mentioned methods it is possible to nanostructure, within the shape of particles, polymers that are either inherently semicrystalline or that are able to crystallize. One example of this type of polymers is poly(lactic acid), from now on abbreviated as PLA. PLA is an aliphatic thermoplastic polymer, commonly

<span id="page-177-0"></span>

made from  $\alpha$ -hydroxy acids which are considered biodegradable, biocompatible, and compostable (Garlotta [2001](#page-186-0); Anderson and Shive [2012](#page-185-0)). Although the term acid is generally included in its name, PLA is a polyester instead of a *polyacid* (Garlotta [2001\)](#page-186-0). Generally, PLA grades are copolymers of poly(L-lactic acid)  $(PLLA)$  and  $poly(D,L-lactic acid)$  (PDLLA), which are produced from L-lactides and  $D,L$ -lactides, respectively (Martin and Avérous [2001](#page-187-0)). The sketch of these molecules is shown in Fig. 6.5.

The letters D and L are related to Dextrorotation (D) and Levorotation (L) and refer to the polymer property of rotating plane polarized light. If the light rotates clockwise as it approaches an observer, this is known as dextrorotation (light with a rotation to the right). If the light rotates counterclockwise as it approaches the observer, then the light exhibits levorotation (rotation to the left). The ratio of L- to D,L- enantiomers is known to affect the properties of PLA, such as the melting temperature and the degree of crystallinity (Martin and Avérous [2001](#page-187-0)).

PDLLA (NatureWorks, PLA 2002D, D-content 4.25%,  $\rho = 1.24$  g/cm<sup>3</sup>) nanoparticles can be prepared either by the miniemulsion method or the reprecipitation method. In the present case, for the miniemulsion method PDLLA was dissolved in chloroform (CHCl<sub>3</sub>), at a 0.2 wt% concentration. The polymer solution was added to a 1 wt% aqueous surfactant solution of sodium dodecyl sulfate (SDS). Pre-emulsification was obtained by stirring at room temperature for

Fig. 6.4 AFM topography image of PEMA nanoparticles prepared by the reprecipitation method after spin casting on a silicon wafer

<span id="page-178-0"></span>60 min and, afterwards, the stirred mixture was ultrasonicated for 15 min in an ultrasound bath. This allowed obtaining a miniemulsion. Evaporation of the organic solvent, under stirring the miniemulsion at 66  $\degree$ C for 180 min, yields a dispersion of polymeric nanospheres in a non-solvent medium. To eliminate the excess of SDS, suspensions were dialyzed against distilled water, using a dialysis membrane. The size of the obtained nanospheres is governed principally by the concentration of the polymeric solution and by the concentration of the surfactant, as previously reported (Martínez-Tong et al. [2013](#page-187-0)).

PDLLA nanoparticles were also prepared by the reprecipitation method. Specifically, 15 mg of PDLLA were dissolved in 5 mL of tetrahydrofuran (THF). The solution was left under stirring at room temperature for 30 min. Afterwards, in order to remove any macroscopic residues, the solution was filtered. Finally, the polymer solution was rapidly injected into a beaker filled with distilled water. This emulsion was left under stirring at room temperature for 90 min and then for 120 min at 66  $^{\circ}$ C to allow complete removal of the solvent. Figure 6.6 shows AFM topography images of the prepared PDLLA nanoparticles.

Figure 6.6a, b show AFM topography images of the PDLLA nanoparticles prepared by the miniemulsion and reprecipitation method, respectively. In both cases, the nanoparticles consist of polymer nanospheres, without signs of



Fig. 6.6 AFM topography images and size distribution of PDLLA nanoparticles prepared by the miniemulsion method  $(a, c)$  and reprecipitation method  $(b, d)$ . Size distribution was quantified on the AFM images by measuring the nanoparticles diameters. Continuous black line represents a Gaussian fit to the distribution

coalescence and/or ripening. From the AFM images the size distributions of the polymer nanoparticles could be quantified and the results are shown in Fig. [6.6c, d](#page-178-0). For both preparation methods, a similar mean value of the PDLLA nanoparticles diameter (d) was found, namely  $d_{\text{miniemulsion}} = (46 \pm 1)$  nm, and  $d_{\text{reprecipitation}} =$  $(53 \pm 3)$  nm. To take into consideration the width of the size distributions, it is possible defining a *quality factor* of the resulting nanospheres by  $Q = W/\langle d \rangle$ , where W is the width of the distribution (nm) and  $\langle d \rangle$  is the mean diameter (nm). The closer the factor  $Q$  is to zero, the better is the resulting preparation in terms of size monodispersity. In this work, we found small  $Q$  values for both preparation methods,  $Q_{\text{miniemulston}} = 0.57 \pm 0.06$  and  $Q_{\text{reprecription}} = 0.28 \pm 0.07$ , indicating that size monodispersity was within acceptable values.

#### 6.3.1 Crystallization in Nanoparticles

Figure [6.7](#page-180-0) shows the X-ray diffraction patterns of the nanoparticles, annealed at different temperatures, together with the diffraction from the bulk treated at the same temperatures for comparison. In general, as the samples were annealed, the development of diffraction peaks is evidenced. This indicates that all samples were able to crystallize. Specifically, bulk and miniemulsion nanoparticles patterns are quite similar between each other for the whole temperature range. At 30  $\degree$ C, these two samples show an amorphous halo, indicating their amorphous nature. As temperature increased up to 70  $\degree$ C, the development of a diffraction peak, around  $2\theta = (17.0 \pm 0.3)$ °, is seen. This peak has been reported to be associated with the diffraction from the (200) and/or (110) planes of the  $\alpha$  form of PDLLA (Mano et al. [2004\)](#page-186-0). At higher temperatures, the diffraction patterns show the development of several other peaks. This behavior indicates that as the samples were annealed crystallization continues. At 110  $^{\circ}$ C, diffraction peaks show their highest intensity. Comparing with the literature (Mano et al. [2004;](#page-186-0) Zhang et al. [2008](#page-189-0); Wang et al. [2014](#page-188-0); Wei et al. [2014](#page-188-0); Wasanasuk et al. [2011\)](#page-188-0), we have indexed the peaks as shown at the 110 °C temperature in Fig.  $6.7$ . Results show that the PDLLA has crystallized in the ordered α-phase (Wei et al. [2014;](#page-188-0) Xiong et al. [2013;](#page-188-0) Wasanasuk et al. [2011](#page-188-0)), which is expected when the polymer is crystallized at temperatures below 100  $\degree$ C. Indexing results are summarized in Table [6.1.](#page-180-0)

The diffraction patterns of PDLLA reprecipitation nanoparticles are shown in the right column of Fig. [6.7](#page-180-0). In this case, patterns are noisier in comparison to the others. This might be related to the amount of material enclosed in the aluminum sheets, which in this case was lesser. As stated previously, as temperature increases crystallization evolves; however, comparing with bulk and miniemulsion nanoparticles there are important differences. At 30  $^{\circ}$ C, besides the amorphous halo, an increase of the diffraction signal is observed at small values of  $2\theta (2^{\circ}-5^{\circ})$ . This result can be related to the possible existence of some ordering in the PDLLA chains within the nanoparticles, which lengthscale is above of WAXS range. It has been reported that poly(lactic acid) polymers can show a mesophase (Zhang
<span id="page-180-0"></span>

Fig. 6.7 Wide Angle X-ray Scattering (WAXS) diffraction patterns for bulk PDLLA (left) and PDLLA miniemulsion (center) and reprecipitation (right) nanoparticles

Index	Bulk	Miniemulsion	Reprecipitation
(010)	$(15.4 \pm 0.3)$ °	$(15.3 \pm 0.3)^{\circ}$	
(200)/(110)	$(17.0 \pm 0.3)$ °	$(17.1 \pm 0.3)^{\circ}$	$(17.2 \pm 0.3)^{\circ}$
(203)	$(19.5 \pm 0.5)$	$(19.5 \pm 0.5)$	$(19.5 \pm 0.5)$
(105)	$(22.7 \pm 0.3)$ °	$(22.7 \pm 0.3)$ °	$(22.8 \pm 0.3)$ °

**Table 6.1** Crystalline peaks and 2 $\theta$  position, as observed at 130 °C (Fig. 6.7)

et al. [2010](#page-189-0); Wasanasuk and Tashiro [2011](#page-188-0)), with distinct chain packing and chain conformation. Mesophases in semicrystalline polymers can be obtained by the melt-quenched methods (Strobl [2006\)](#page-188-0); for example, isotactic polypropylene can be solidified into an intermediate state between crystal and amorphous states when a thin specimen of molten state is rapidly quenched (Qiu et al. [2007](#page-187-0)). Also, Stoclet and collaborators have shown that it is possible to induce a mesophase in PDLLA when an external strain was applied (Stoclet et al. [2010a,](#page-188-0) [b](#page-188-0)). Collecting all these facts, we argue that the preparation procedure used in the reprecipitation method might have led to the formation of a mesophase in the resulting PDLLA nanoparticles. We recall that in this method, the polymer solution is rapidly injected into a non-solvent. In the solution, the polymer chains have maximum mobility, which can be somehow compared to the behavior in the melt state. As the solvent is quickly removed from the nanoparticles, while the polymer is being transferred to a non-solvent medium (chains have no mobility), it is possible to assume that the polymer chains are being subjected to a quenching-like procedure that ultimately leads to the formation of the mesophase. It can also be argued that during the fast precipitation, the polymer chains retain residual stresses and thus a sort of straininduced mesophase takes place. These strains could arise from the physical procedure involved in going from separated chains to nanospheres.

The preparation method argument just explained can be also justified by comparing the results between reprecipitation and miniemulsion PDLLA nanoparticles. In the miniemulsion method, nanodroplets of solvent/polymer are formed simultaneously during ultrasonication. After the formation, solvent is slowly evaporated and thus nanoparticles do not suffer a melt-quench like procedure. Also, the solvent/polymer nanodroplets serve as precursors to the resulting polymer nanoparticles and thus, during solvent evaporation process, polymer chains have enough mobility to lose possible strains. Since the solvent is evaporated at a temperature in which no Bragg peaks are observed, and since there is not enough mobility to crystallize, the resulting nanoparticles are amorphous, without any mesophases.

The WAXS signature of the so-called mesophase in the PDLLA reprecipitation nanoparticles vanishes with temperature, in the range 30–60 °C. At 70 °C (Fig. [6.7](#page-180-0)) the increase a low  $2\theta$  is not observed anymore. Figure [6.8](#page-182-0) shows the Differential Scanning Calorimetry (DSC) trace of the reprecipitation nanoparticles. Glass transition  $(T_g)$ , crystallization and melting temperatures are highlighted throughout the curve.

The glass transition temperature of the nanoparticles is observed around 60  $\degree$ C indicating no change in comparison to the bulk (Bitinis et al. [2011](#page-186-0)). Comparing WAXS and DSC results, we observe that the mesophase signature in the diffraction pattern disappears at temperatures above  $T_{\rm g}$ . Also, in the DSC curve, just below  $T_{\rm g}$ an endothermic peak can be seen, highlighted with the symbol \*. DSC endothermic peaks in semi-crystalline polymers are related to first-order transitions, such as the melting of the crystalline structure. Gathering results, it is possible to speculate that this peak is related to the disordering of the polymer chains in the mesophase, that happens just when the polymer start getting mobility due to the incipient glass

<span id="page-182-0"></span>

transition. At temperatures above  $T_{g}$ , the calorimetric curve shows a crystallization peak. The onset of crystallization can be observed around  $90^{\circ}$ C and its maximum at 125 °C. Finally, the polymer nanoparticles melt at  $145$  °C. DSC results of crystallization and melting of the nanoparticles agree with the WAXS patterns.

### 6.3.2 From Polymer Nanoparticles to Polymer Nanocrystals

WAXS results in the previous section showed that polymer nanoparticles of PDLLA were able to crystallize when heated above certain temperatures. The diffraction patterns also show that nanoparticles prepared via the miniemulsion protocol showed a crystallization behavior quite similar to the bulk polymer. Based on these results, we have evaluated the morphological change of PDLLA nanoparticles prepared by the miniemulsion method, when subjected to thermal treatments.

Figure [6.9](#page-183-0) shows  $(3 \times 3)$  µm AFM topography images of the deposited PDLLA nanoparticles annealed at 75 °C for different times (*t*). This temperature is above  $T_{\rm g}$ of the PDLLA and according to the WAXS patterns crystallization must take place. Annealing was performed on a hot stage, by heating the Si wafers on where the particles were originally deposited. Each annealing treatment was carried out on independent wafers.

Image at  $t = 0$  s corresponds to the deposited nanoparticles without annealing, showing their spherical geometry. After annealing for 5 min, the nanoparticles lose their spherical shape, turning into islands, which show a bigger diameter and lower height in comparison to the original nanoparticles. This is an indication of agglomeration and coalescence of neighbor particles, as previously reported for nanospheres of amorphous polymers, where the height:width ratio increased from 1:1 to 1:5 (Martínez-Tong et al. [2013](#page-187-0), [2014](#page-187-0)). The morphology of the nanoparticles

<span id="page-183-0"></span>

Fig. 6.9 AFM images of PDLLA nanoparticles prepared by the miniemulsion protocol, annealed at  $75^{\circ}$ C for different times (t)

suffers further changes after 30 min at 75  $\degree$ C. As time increases, the original smooth edges of the islands observed at 5 min start reshaping into well-defined straight contours. Also, in some cases it is possible to see the appearance of needle-like features inside the nanoparticles. This fact is enhanced at the longest annealing time (1200 min).

Figure [6.10](#page-184-0) shows a  $(1 \times 1)$  μm AFM topography image of the PDLLA nanoparticles annealed at 75 °C for 1200 min. In this case, a smaller scan was used (in comparison to images in Fig. 6.9), which allowed getting more insight into the details of the nanocrystals. As stated before, the original spherical nanoparticles present now well-defined edges, as expected for crystalline structures. These crystalline structures seem to be formed by the agglomeration of several nanoparticles, since at the chosen annealing temperature PDLLA is expected to have mobility. Two different structures are observed in the AFM image of Fig. [6.10](#page-184-0). First, needle-like crystals (red arrow) resemble the edge-on crystalline structures in

<span id="page-184-0"></span>

polymer thin films. On the other hand, the green arrow highlights the structures resembling flat-on crystals, compared to thin polymer films (Wang et al. [2008;](#page-188-0) Xu et al. [2005](#page-188-0)).

The needle-like crystals prepared from the PDLLA nanoparticles show widths between 15 and 25 nm, heights between 15 and 40 nm and lengths between 100 and 300 nm. On the other hand, flat-on like crystals show sides between 50 and 150 nm and heights in the 15–60 nm range. Based on the geometrical sizes of the crystals obtained from the PDLLA nanoparticles, it is possible to consider them as nanocrystals. In principle, these nanocrystals could be recovered from the silicon waffers by washing it in distilled water. Afterwards, they could be used as additives in composites and/or polymer blends. Also, the heights of these nanostructures are comparable to the ones obtained for ultra-thin films of PLLA (Maillard and Prud'homme [2008\)](#page-186-0). This allows thinking in possible comparisons in the crystallization between the two confined geometries.

# 6.4 Summary

We have shown that by various physicochemical methods it is possible to nanostructure bulk polymers in the shape of nanoparticles, that in the case of amorphous polymers, have spherical shape. If the original bulk polymer is able to crystallize, the shape of the nanoparticle is modified by the process of crystallization. However, it is possible to limit the size of the crystal due to the confinement imposed by the nanoparticle shape.

# 6.5 Methods

Atomic Force Microscopy (AFM). Size and shape of the polymer nanoparticles were characterized by atomic force microscopy (AFM). Samples were drop casted on (100) Si wafers. A Multimode 8 AFM with a Nanoscope V controller (Bruker) was used under tapping mode with NCHV probes (Bruker). Square images with  $512 \times 512$  pixels resolution were taken. Analysis of size and shape of nanoparticles was performed with the Nanoscope Analysis 1.50 software (Bruker).

Wide Angle X-ray Scattering (WAXS). 2D-WAXS investigations were carried out in transmission geometry using a Bruker AXS Nanostar X-ray scattering instrument. The instrument uses CuK $\alpha$  radiation (1.54 Å) produced in a sealed tube. The sample chamber was under vacuum and controlled temperature. For WAXS experiments, we used lyophilized nanoparticles packed in aluminum sheets. Bulk sample was measured as received also packed in aluminum sheets. The scattered X-rays were detected on a two-dimensional multiwire area detector (Bruker Hi-Star) and converted to one-dimensional scattering by radial averaging and represented as a function of the momentum transfer vector  $q = 4\pi/\lambda \sin \theta$  in which  $\theta$  is half the scattering angle and  $\lambda$  the wavelength of the incident X-ray beam. The sample-to-detector distance was 10 cm. Patterns were collected during 5 min at each temperature.

Differential Scanning Calorimetry (DSC). Calorimetric measurements were carried out by means of a Perkin-Elmer DSC8500 instrument equipped with an Intracooler 2 sub-ambient device and calibrated with purity indium standards. In order to measure the transitions of the nanoparticles, the external block temperature was set at  $-100^{\circ}$ C. A lyophilized solid powder of nanoparticles was used as sample with weight c.a. 2 mg. The powder was enclosed in aluminum pans and heated from  $-20$  to 200 °C at a rate of 20 °C/min. Bulk sample was measured as received, enclosed in aluminum pans.

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# Chapter 7 Controlling Morphology in 3D Printing

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## 7.1 Introduction

3D printing is a term widely used to refer to Additive Manufacturing (AM) or Direct Digital Manufacturing (DDM), which is a technology used to fabricate objects based on a layer-by-layer process. This technology has been revolutionising manufacturing industry by overcoming some of the limitations of traditional manufacturing processes. The concept of additive manufacturing first appeared in the mid 1980s with the first stereolithography and Selective Laser Sintering machines. In the following decade, other innovative additive processes were developed, responding positively to other challenges which had been identified, significantly impacting on both commercial and academic accomplishments (Bourel et al. [2014](#page-214-0)).

Even though 3D printing has been subject to intense development, there remains a doubt regarding its suitability and the value added to industries like biomedical, tools and plastics. Traditional and mass production companies may not directly benefit compared with industries of high value/low volume productions, but they can profit from additive technologies when associated with Rapid Tooling (Conner et al. [2014](#page-214-0)). There are several pre-production steps required before an object can be manufactured (Fig. [7.1\)](#page-191-0). These dictate the quality and functionality of the final product.

Generically, additive manufacturing begins with a conceptual digital design which is converted into a parametric design using computer-aided design (CAD) software. This initial model can be analysed and optimised through computer-aided

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Fig. 7.1 Fused deposition modelling process (adapted from Gibson et al. [2010a\)](#page-214-0)

engineering (CAE) software which mathematically predicts the properties of the part and facilitates the redesign of the part (Wong and Hernadez [2012\)](#page-216-0). The next step involves the conversion of the digital design to an STL file format (ASCII or binary) which consists of a model of the part generated by a combination of the vertices and the normals of triangles defining the boundaries of the part.

Subsequently, the STL file is imported in a pre-processing software package such as Magic  $RP^{\mathcal{B}}$ , Viscam $^{\mathcal{B}}$  and Netfabb $^{\mathcal{B}}$  to define the orientation of the part on the build platform, the support structures and the layer densities. The slice thicknesses and tool path are both defined and saved in an SLI file (slice). Finally, the file is sent digitally to the selected printer for construction (Petrovic et al. [2011\)](#page-215-0). The manufacture of 3D printed parts is often followed by operations such as removal of the support structures (simple hand separation or dissolution baths), clean-up and post-processing. The latter is designed to reduce surface roughness (see Sect. [7.3.1\)](#page-197-0).

Developments in additive technologies provide a number of advantages including (Petrovic et al. [2011\)](#page-215-0):

- Product customisation with very low constraints in the geometric complexity of the part (freedom of design)
- Capability of print on demand due to high speed of small series of parts
- There is no need for extra tools or moulds (any support necessary to production will be created in each slice)
- Parts with variety of density can be manufactured (depending on the layers fill settings)
- Possibility of usage of recyclable materials
- Near to zero material waste

However, 3D printing technology still presents some challenges to overcome:

- There is increased production costs for larger series
- Lower mechanical and thermal performance of printed parts compared to conventional manufacturing techniques
- Limited choice of materials for additive technologies
- The staircase effect due to layered construction which impacts the surface finish and dimensional accuracy
- No recovery of support materials

### 7.1.1 Light-Based Technologies

The earliest AM systems employed high intensity laser light beams to process resins or powders.

The laser curing process causes the liquid resin to solidify using frequencyspecific light that moves point-by-point or layer-by-layer across the part area. Stereolithography (SLA) was first introduced to the market in 1986 by the 3D Systems<sup>®</sup> company and has been continuously used since then due to its accuracy and resolution of  $\sim 20$  µm (Melchels et al. [2010](#page-215-0)). At the present time, stereolithographic technologies use either UV or infra-red lights or a combination of both (Bártolo and Mitchell [2003\)](#page-213-0). Some examples of SLA-based 3D printers are detailed in Table 7.1.

In Selective Laser Sintering (SLS) technology, the light causes powder to controllably melt and fuse with neighbouring particles. Upon removal of the laser, the molten powder rapidly solidifies producing a consistent layer (Gibson et al. [2010b](#page-214-0)). This technology was originally developed at the University of Texas and commercialised by the DTM Corporation (Beaman et al. [1997](#page-214-0); Hon and Gill [2003\)](#page-214-0). Table 7.2 shows the most recent commercial SLS 3D printers.

	Print	Laser	Layer			
3D printer	volume $\text{cm}^3$ )	wavelength (Nm)	thickness $(\mu m)$	References		
Form $1+$	~2580	405	25, 50, 100	Formlabs $(2014)$		
Titan 1	$~10-5040$	400		Kudo 3D (2014)		
Pegasus touch	$\sim 7145$	405	$25 - 100$	Kickstarter, Inc. (2014)		

Table 7.1 Stereolithography-based 3D printers

	Print	Laser	Layer	
3D printer	volume $\text{cm}^3$ )	power $(W)$	thicknesses (mm)	References
Ice 1	10,000	10	$0.1 - 0.15$	Norge Ltd $(2014a)$
Ice 9	40,500	40		Norge Ltd (2014b)
Sintratec	~2200	2.3		Sintratec $(2015)$
<b>FORMIGA P 110</b>	16,500	30	$0.06 - 0.12$	EOS (2015)
Elite P3200	61,440	60	$0.13 - 0.18$	3D Printing
Elite P3600	77,760	80	$0.13 - 0.18$	Systems $(2014)$
Elite P5500	181,500	100	$0.15 - 0.1$	

Table 7.2 Selective laser sintering-based 3D printers

### 7.1.2 Print-Based Technologies

Printing-based additive technologies can be divided in two categories: tri-dimensional printing (3DP) and Inkjet technology. The former is the most primitive printing-based technology, first reported in 1989 by Sachs and co-workers. As the construction of the part proceeds, the system deposits successive individual powder layers that are bonded with a binding liquid which is selectively delivered by an inkjet print head, forming a pattern. The excess non-bonded powder is removed by an air jet and used on the subsequent layers (Pfister et al. [2004](#page-215-0); Butscher et al. [2011](#page-214-0)).

As an alternative to the powder-based technologies, Inkjet Printing has been developed as a versatile process using liquid viscous materials. Inkjet printers can be further subdivided accordingly to the method of the delivering the material onto a moving build platform: drop-on-demand and continuous jet.

#### 7.1.3 Extrusion-Based Technologies: Melt or Solution

Melt-based techniques are associated with high temperature material processes such as Fused Deposition Modelling (FDM), Fused Filament Fabrication (FFF), 3D fibre deposition, Precise Extrusion Manufacturing (PEM) and Multiphase Jet Solidification (MJS) which deposits a molten material onto the build platform. In the case of natural-derived materials, high temperatures compromise the product integrity, and it is necessary to resort to solution-based room temperature technologies. Regarding each type of extrusion system, four types of nozzles have been used in several studies: pressure-actuated, solenoid-actuated, piezoelectric and volume-actuated nozzles (Giannatsis and Dedoussis [2009\)](#page-214-0).

#### 7.1.3.1 Fused Deposition Modelling/Fused Filament Fabrication

Fused deposition modelling (FDM), first developed by Stratasys<sup>®</sup> and commercialised in 1992, uses a thermoplastic filament and a filament support material that are heated above their melting temperature in the nozzle where it is further extruded forming again a filament in a predefined position on the platform. The first layer, the so-called raft, is deposited onto a descending platform to form the compact and even base for the construction of the part. The molten material quickly solidifies and provides enough mechanical support to the part during printing. After each layer is built, the platform is lowered to enable a new layer deposition with user-defined build parameters such as writing speed, layer density and temperature, until the part is completed. The system is shown schematically in Fig. [7.2](#page-194-0) (Chang and Huang [2011\)](#page-214-0).

<span id="page-194-0"></span>



## 7.2 FDM/FFF Feedstock Materials

Fused deposition modelling and fused filament fabrication, as outlined above, is a melt-based process which uses heat to transform the material in to a more pliable manner. Tri-dimensional constructs require both building and support materials generally made from acrylonitrile-butadiene-styrene (ABS), polycarbonate (PC), blends of PC/ABS or polyphenylenesulfone (PPSU) (Wendel et al. [2008](#page-216-0)).

As the end use of AM parts has evolved from prototypes to marketable and functional components, developments have focused efforts on application-specific demands. Recent studies have reported usage of other thermoplastics and thermoplastic-based composites to obtain components with improved thermal or mechanical properties or even enhanced biodegradability (Table [7.3\)](#page-195-0).

Polymer–metal compounds have been developed specifically for direct rapidtooling applications as proposed by Masood and Song [\(2004](#page-214-0)). In that study, the composite filament was prepared by adding iron powder to a polyamide thermoplastic (P301) in order to increase the strength, the toughness and the conductivity of 3D printed injection moulding inserts. It was observed that the use of the FDM polymer/metal inserts reduced the injection cycle time and pressure of ABS parts compared to the accurate clear epoxy solid (ACES) injection moulding obtained from SLA.

Shofner et al. [\(2003](#page-215-0)) studied the effect of dispersion of vapour-grown carbon fibres (VGCF) in an ABS copolymer matrix on the mechanical properties of specimens printed in a Stratasys FDM 1600 Modeler. They observed good dispersion and alignment of the fillers and a lower porosity.

3D printing has also been used to produce medical implants and tissue engineering constructs involving biocompatible and bioresorbable scaffolds. Skowyra

<span id="page-195-0"></span>



et al. [\(2015](#page-215-0)) reported on a study involved patient-personalised extended-release prednisolone tablets fabricated via FDM. In that study, polyvinyl alcohol (PVA) tablets were prepared in a modified MakerBot Replicator 3D Printer in order to control drug dose via printed volume. In a similar study, Teo et al. [\(2011](#page-215-0)) used FDM technology to fabricate poly(caprolactone)-based scaffolds for delivery of gentamicin sulphate that acts as an antibacterial agent.

# 7.3 Parameters in FDM/FFF 3D Printers

A number of reports show how each parameter in the FDM process contributes to the quality (less distortion) and functionality of printed parts. The complexity of the 3D printing process arises from the number of variables which are used to define the operation of the 3D printer machine and the material. Bearing in mind the possibility of producing solid or shell objects, the correct selection of the manufacturing parameters contributes to the improvement of the properties, such as density, porosity, layer thickness, and material properties (Villalpando et al. [2014](#page-216-0)). The intrinsic layer parameters such as printing and feed roller speeds and, extrusion temperature should not be ignored in any optimisation process (Fig. 7.3).



Fig. 7.3 3D printing process parameters

# <span id="page-197-0"></span>7.3.1 Surface

Central to AM processes is the layer-by-layer construction which produces parts with a variety of surface roughness. 3D printers based on FDM/FFF technologies operate accordingly to the STL derived from the CAD model. Galantucci et al. ([2009\)](#page-214-0) pointed out the importance of the STL refinement in order to obtain smooth and model-like surfaces. The staircase-like effect is inevitable and results in angled surfaces (Ahn et al. [2009a](#page-213-0), [b;](#page-213-0) Pandey et al. [2003\)](#page-215-0).

#### 7.3.1.1 Layer Thickness

It is generally understood that thinner layers lead to smoother surfaces and more dimensionally accurate parts. The thickness of each layer is defined in the third step (slicing) of 3D printing process when the construction paths are established. Therefore, the slice thickness determines the Z-axis displacement relative to the subsequent layer during production. The definition of this parameter is considered one of the most important parameters that determines surface quality (Fig. 7.4).

Bakar et al. [\(2010\)](#page-213-0) investigated the effect of layer thickness on the surface roughness of cylindrical parts using a surface tester. From this study, they determined that horizontal surfaces were smoother compared to vertical ones (Fig. [7.5\)](#page-198-0).

#### 7.3.1.2 Part Orientation

In the FDM manufacturing process, an important factor for the quality of printed objects is how the part is orientated on the build platform. It has been established that this is often incorrectly chosen by the user. Not only does the orientation of the part affects the mechanical properties but may also contribute to extended production times, excessive support structures, decreased dimensional accuracy, increased surface roughness and higher cost of the production (Thrimurthulu et al. [2004](#page-215-0)). Lee et al. ([2007\)](#page-214-0) demonstrated the impact of axial and transversal build directions of



Fig. 7.4 (a) CAD model, (b) thick layers (rough surface) and (c) thin layers (smoother surface)

<span id="page-198-0"></span>

Fig. 7.5 Staircase effect (left) Reprinted from International Journal of Machine Tools and Manufacture, Vol. 44, K. Thrimurthulu, Pulak M. Pandey, N. Venkata Reddy, Optimum part deposition orientation in fused deposition modelling, 585–594, Copyright (2004) with permission from Elsevier; and micrograph of 3D printed part with layer thickness of 0.25 mm (right) Reprinted from Computer-Aided Design, Vol. 34, R. I. Campbell, M. Martorelli, H.S. Lee, Surface roughness visualisation for rapid prototyping models, 717–725, Copyright (2002) with permission from Elsevier

FDM parts on mechanical properties. Samples with 25.4 mm in length and 12.7 mm in diameter were made from ABS with a filling pattern of  $45^{\circ}/45^{\circ}$  angles. From this, it was concluded that the axial samples presented 11.6 % more compressive strength compared to the transversal samples.

### 7.3.2 Layer and Cross-Section

Depending on the function of the 3D printed parts, the operator may define a different fraction of the layer infill with variable raster gaps and different orientation of the filaments which produces parts with different densities and localised mechanical properties.

#### 7.3.2.1 Gap Between Filaments

The density and mechanical behaviour of FDM parts are greatly affected by the contour and the filling defined during the process. Depending on the final application of the part, the layer density can be tuned by optimisation of the distance between two neighbouring filaments. Low density parts may be produced with larger gaps without requiring supports. Figure [7.6](#page-199-0) demonstrates ABS parts in the software package uPrint<sup>®</sup> with different layer patterns printed.

Smaller or no gaps generate solid layers in which filaments are thermally bonded together. Bond formation is solely driven by thermal energy of the molten material. The heat transfer necessary to join two adjacent filaments is influenced by thermal properties of the material as well as the liquefier and envelope temperatures, nozzle

<span id="page-199-0"></span>

Fig. 7.6 uPrint ABS parts with different infill patterns: (a) solid and (b) sparse



Fig. 7.7 Neck growth between adjacent filament at 200  $\degree$ C (Reprinted from Journal of Manufacturing Processes, Vol. 6, Céline Bellehumeur, Longmei Li, Qian Sun, Peihua Gu, Modeling of Bond Formation Between Polymer Filaments in the Fused Deposition Modeling Process, 170–178, Copyright (2004), with permission from Elsevier

diameter and the flow and cooling rates. The bonding process occurs into three different stages: interfacial contact, neck formation and growth and molecular diffusion where polymer chains migrate across the interfacial zone.

Bellehumeur et al. ([2004\)](#page-214-0) studied the bonding quality of ABS P400 filaments. Figure 7.7 demonstrates the neck growth between adjacent filaments with no gap at a high envelope temperature with time. In a similar study, Reddy et al. [\(2007](#page-215-0)) reported the effect of small gaps on the inter-filament bond strength.

Too et al. ([2002](#page-216-0)) conducted a study relating the layer microstructure obtained from gaps between the filaments ranging from 0 to 0.5 mm. This study allowed the development of an understanding of the versatility of the FDM process to obtain matrix-like structures with a consistent pore distribution. Compressive tests were performed to determine how the gap between the filaments affects the mechanical behaviour of ABS P400 printed parts. It was found that by setting the gap to 0.2 mm which yielded a measured porosity of  $\sim$ 59% caused a decrease of the compressive strength by half compared with no gap samples.

#### 7.3.2.2 Layer Patterning

An important operation parameter which directly affects the layer anisotropy is the raster angle that is defined by the direction of the deposited filaments on the plane of construction.

Ziemian et al. ([2012\)](#page-216-0) studied the impact of four different raster angles on the mechanical properties of ABS printed specimens:  $0^{\circ}$  (aligned with the longitudinal axis of the part),  $45^{\circ}$  (diagonal),  $90^{\circ}$  (transversal) and  $+45^{\circ}/-45^{\circ}$ . In order to validate the 3D printed parts, identical mechanical tests were conducted on the injected parts. From the results, they concluded that tensile properties were higher with the raster angle set at  $0^{\circ}$  and weaker with a raster angle of  $90^{\circ}$ .

Failure profiles were analysed, leading to the conclusion that the  $0^{\circ}$  raster angle causes localised delamination at the primary stages which develop in to monofilament deformations whereas  $90^\circ$  raster angles demonstrates a failure due to a weak filament bonding leading to instantaneous delamination. In contrast, the transversal orientation demonstrated higher compressive strength.

#### 7.3.2.3 Materials Properties

In melt-based 3D printing, amorphous and semi-crystalline materials have been studied and optimised in order to obtain high quality parts. Ippolito et al. [\(1995](#page-214-0)) conducted a comparative study of SLA, SLS and FDM technologies and materials, where for the melt-based printing, polyolefin and polyamide resins were used. Through micrographs taken of the surface of the printed parts, they observed significant differences between the layer morphologies (Fig. [7.8](#page-201-0)) and the mechanical properties.

More recently, reinforced feedstock materials have been studied and are now commercially available to fabricate application specific parts involving mechanical, thermal, physical and biological properties.

An example of the development of materials used in FDM/FFF technologies is that conducted by Tekinalp et al. [\(2014](#page-215-0)) where they studied the benefits of short carbon fibre reinforcement on ABS load-bearing 3D printed parts. As observed in Fig. [7.9](#page-201-0), carbon fibres were found to exhibit near-perfect alignment with the writing

<span id="page-201-0"></span>

Fig. 7.8 Layer micrographs of 3D printed parts using P300 resin (left) and P200 resin (right)<br>(Reprinted from CIRP Annals–Manufacturing Technology, Vol. 44, R. Ippolito, L. Iuliano, A. Gatto, Benchmarking of Rapid Prototyping Techniques in Terms of Dimensional Accuracy and Surface Finish, 157–160, Copyright (1995), with permission from Elsevier)



Fig. 7.9 Cross-sectional SEM micrographs: (a, b) neat ABS, and (c) ABS/10 wt% carbon fibre 3D printed parts; and (d) compression-moulded ABS/10 wt% carbon fibre (Reprinted from Composites Science and Technology, Vol. 105, Halil L. Tekinalp, Vlastimil Kunc, Gregorio M. Velez-Garcia, Chad E. Duty, Lonnie J. Love, Amit K. Naskar, Craig A. Blue, Soydan Ozcan, Highly oriented carbon-fiber-polymer composites via additive manufacturing, 144–150, Copyright (2014), with permission from Elsevier

direction and well dispersed within the polymer matrix. Furthermore, they demonstrated an upwards trend of the modulus and the tensile strength with the content of reinforcing agent.

# 7.3.3 Filaments

Several operating parameters affect the morphology of printed objects as they determine how the filaments solidify and subsequently respond to mechanical load. Aside from the geometrical parameters of printed parts, the microstructure obtained during material deposition is expected to be affected by the materials properties such as thermal expansion and viscosity and possibly by operational parameters such as deposition speed, feed roller velocity and extrusion temperature.

The authors of this work have undertaken a series of small angle X-ray scattering experiments (Fig. 7.10) in order to determine how each operating variable impacts the individual filament morphology. Individual strands, prepared using either poly (acid lactic) (PLA) or poly(ε-caprolactone) (PCL), were extruded under different conditions of deposition speed, feed roller velocity and temperature. The PLA samples were prepared using two different 3D commercial printers: 3D Touch<sup>®</sup> of 3D Systems, Inc. and BOX Basic® from AMcubed, Ltd.

Filaments patterns were collected using a SAXS Quantum 210r CCD detector from ADSC at the Non Crystalline Diffraction beamline at the ALBA Synchrotron with a sample-to-detector distance of  $\sim 6.1$  m and a wavelength of  $\sim 1$  Å. Silver behenate sample was used for calibration.



Fig. 7.10 Scattering experiments on 3D printed filaments, where  $r_1$ ,  $r_2$  and  $r_3$  are the crosssectional planes of the filament,  $\Phi$  is the azimuthal angle, sl and s3 are the momentum transfer in equatorial and meridional directions ( $s = 4\pi \sin(\theta)/\lambda$ , where  $2\theta$  is the angle between the incident and scattered beam and  $\lambda$  is the X-ray wavelength) and s2 is the intensity of the scattering

# 7.4 Case Study 1: Feedstock Material

Typically, crystallisation from a quiescent melt tends to form a spherulitic morphology. A spherulite is a spherical organisation of the chain folded lamella crystals. However, during 3D printing, the flow stress applied to the liquefied polymer as it passes through the nozzle induces oriented crystallisation due to the formation of row nuclei (Tojeira et al. [2014](#page-215-0)). The addition of a small fraction of nucleating agents, in this case, graphene nanoflakes, alters the crystallisation mechanism and consequently the morphology of semi-crystalline filaments.

2D SAXS patterns were taken from vertically aligned PCL and PCL/grapheneprinted filaments. The addition of different contents of filler induced significant modification in the PCL scattering pattern in the equatorial axis. The scattering patterns shown as inserts in Fig. 7.11 are typical of scattering patterns from semicrystalline polymers which contain chain folded lamellar crystals. Azimuthal integration of the scattering pattern leads to the calculation of the orientation parameters which described the level of preferred orientation of the crystals with respect to the filament axis. Figure 7.11, demonstrates the variation of the orientation parameter  $\langle P_2 \rangle$  determined based on the method described in Chap. [2,](http://dx.doi.org/10.1007/978-3-319-39322-3_2) Sect. [2.4.1.2](http://dx.doi.org/10.1007/978-3-319-39322-3_4).  $\langle P_2 \rangle$  values of PCL/graphene filaments indicate a preferential orientation of the crystals c-axis parallel with the filament axis. However, by doubling the amount of the filler no significant alteration was registered.

Analysis of the intensity profiles along the equatorial direction (Fig. [7.12a](#page-204-0)) shown an obvious peak at approximately 0.047  $\AA^{-1}$  which relates to a two-phase



Fig. 7.11 2D SAXS pattern and orientation parameter  $(\langle P_2 \rangle)$  of vertically positioned PCL filaments with different contents on graphene nanoflakes: 0 wt%, 0.25 wt% and 0.50 wt%

<span id="page-204-0"></span>

Fig. 7.12 (a) Scattering curves of 2D SAXS patterns of neat PCL filaments and graphene nanoflakes reinforced PCL filaments at different percentages and (b) correlation function obtained from scattering curves

structure (stacks of lamellae). The peaks position remains unchanged with the addition of graphene nanoflakes.

The long period, the crystalline and amorphous layer thicknesses and the bulk volume crystallinity were obtained from an analysis of the correlation functions, an example is shown in Fig. 7.12b. The correlation function is defined as:

$$
\gamma(R) = \frac{1}{Q_s} \int_0^\infty I(q) q^2 \cos(qR) \mathrm{d}q \tag{7.1}
$$

where  $Q_s$  represents the relative invariant and which is defined by  $(7.2)$ :

$$
Q_{s}(t) = \int_{0}^{\infty} q^{2} I(q) dq \approx \int_{q_{1}}^{q_{2}} q^{2} I(q) dq
$$
 (7.2)

For correlation function calculation, data were smoothed using Hermite splines and extrapolated to low  $q$  values by fitting a linear combination of Gaussian and Cauchy distribution. Extrapolation to high  $q$  values was performed using the function in  $(7.3)$  considering constant level of background  $(B)$  throughout all the experiments (Rabiej and Rabiej [2011](#page-215-0)).

$$
I(s) = \frac{K}{s^4} \cdot e^{-(2\pi\sigma s)^2} + B
$$
 (7.3)

Figure [7.13](#page-205-0) shows the variation of long period and crystalline/amorphous layer thicknesses with increase content of graphene nanoflakes. From this, is it possible to observe that the graphene induces a thickening of the soft layer (Ab), leading to an increase of the long period,  $L_p$  and a reduction of bulk crystallinity.

<span id="page-205-0"></span>

Fig. 7.13 A plot of the variation in the values of long period  $(L_p)$ , crystalline  $(C_p)$  and amorphous layer  $(A_h)$  thicknesses and bulk crystallinity (BC) extracted from correlation functions with graphene nanoflake content

## 7.5 Case Study 2: Deposition Speed

Deposition velocities define how fast the filaments are drawn onto the platform. Very few studies have addressed how this parameter impacts the overall quality of the parts, but Anitha et al.  $(2001)$  $(2001)$  determined that this variable can contribute ~15 % to the surface roughness of the part. However, within the microstructure of the printed parts, it is possible to observe the effect of varying such parameter and how it modifies mechanical properties.

Glassy polymer filaments do not exhibit hard segments as consequence of the thermal history or randomness along the polymer chains (Tojeira et al. [2014\)](#page-215-0). Figure [7.14](#page-206-0) shows radially integrated scattering curves of PLA filaments drawn at different deposition speeds using two different printers. We attribute the increase of the intensity of the scattering pattern at a smaller  $q$  to the increase of nanovoids in the PLA filaments.

Although there is no other visible changes on the filament structure, nanovoids formation generally leads to lower mechanical properties due to inter-lamellar slip, as verified in Fig. [7.15.](#page-206-0)

Semi-crystalline samples, on the other hand, deposited at high speeds produce thinner filaments due to the inherent stretching of the crystallising polymer at the tip of the nozzle. However, in this case study (Fig. [7.16](#page-207-0)), where the variation of speed was relatively low, there were no significant variations in the crystals orientation

<span id="page-206-0"></span>

Fig. 7.14 Scattering curves of vertically positioned PLA filaments printed in: (a) 3D Touch<sup>®</sup> and (b) BOX Basic®, varying the deposition speed



Fig. 7.15 Tensile properties of PLA filaments drawn at different speeds

Similarly to case study 1, PCL filaments drawn at different speeds did not exhibit a variation of the peaks position indicating a very minor impact in this range of velocities (Fig. [7.17a\)](#page-207-0).

From an analysis of the correlation functions of the equatorial scattering curves (Fig. [7.17b](#page-207-0)), largely constant values regarding the bulk crystallinity and the amorphous and crystalline phases under these processing conditions were observed as shown in Fig. [7.18](#page-208-0).

<span id="page-207-0"></span>

Fig. 7.16 2D SAXS patterns and orientation parameter  $(\langle P_2 \rangle)$  of vertically positioned PCL filaments drawn at different deposition speeds: 10 mm/s, 20 mm/s and 30 mm/s



Fig. 7.17 (a) Scattering curves of 2D SAXS patterns of neat PCL filaments drawn at different deposition speed and (b) correlation function obtained from scattering curves

# 7.6 Case Study 3: Feed Roller Velocity/Screw Rotation **Velocity**

Extrusion-based 3D printers are generally efficient with feed roller mechanisms that push the feedstock wire downwards in to the heating chamber. Although smaller in number, pelleted-base printers use a screw-type mechanism to delivery molten material to the nozzle. The most recent example is the David 3D Printing by Sculptify (from Kickstarter<sup>®</sup>).

<span id="page-208-0"></span>

Fig. 7.18 Long period  $(L_p)$ , crystalline  $(C_b)$  and amorphous layer  $(A_b)$  thicknesses and bulk crystallinity (BC) extracted from the correlation functions



Fig. 7.19 (a) Scattering curves of PLA filaments printed in 3D Touch<sup>®</sup> varying feed roller speed and (b) their impact in mechanical properties

The former mechanism feeds the wire into the heated extrusion head using a pinch rollers connected to stepper motors (Turner et al. [2014\)](#page-216-0).

In both printers, the PLA feedstock is compressed between the rollers and pushed against the aperture of the nozzle causing a critical increase of pressure at the tip of the nozzle.

2D SAXS patterns were taken from filaments extruded at different roller angular velocities (Fig. 7.19a). Significant differences in modulus and yield stress were observed between two feed roller speeds in the same 3D printer, as shown in Fig. 7.19b.



Fig. 7.20 2D scattering patterns and orientation parameter  $(\langle P_2 \rangle)$  of vertically positioned PCL filaments prepared using different screw rotation velocities: (a) 40 rpm, (b) 50 rpm and (c) 70 rpm



Fig. 7.21 (a) Scattering curves of 2D SAXS patterns of PCL filaments drawn at different screw rotation velocities and (b) correlation function obtained from the scattering curves

Semi-crystalline filaments, produced in the Bioextruder equipped with a screwtype feeding mechanism, demonstrated a minor increase of preferred orientation of the crystals under the same range of screw rotation velocity (Fig. 7.20).

Further analysis of the scattering curves shown in Fig. 7.21a, b revealed that the feed velocity did affect the thicknesses of the crystalline and amorphous blocks (Fig. [7.22](#page-210-0)).

<span id="page-210-0"></span>

Fig. 7.22 Long period (Lp), crystalline (C<sub>b</sub>) and amorphous layer  $(A_b)$  thicknesses and bulk crystallinity (BC) extracted from correlation functions

### 7.7 Case Study 4: Extrusion Temperature

The dynamics of the molten material in the extrusion head is a quite complex process involving the melting point of the materials coupled with flow processes and stresses which are in part related to the viscosity and surface energy as well as the design of the extruder. Most 3D printers use shear thinning materials that follow power-law viscosity models (7.4):

$$
\eta = K(\dot{\gamma})^{n-1} \tag{7.4}
$$

where,  $\eta$  is the viscosity,  $\dot{\gamma}$  is the shear rate and K and n are power-law fit<br>parameters. It is important to consider that viscosity varies due to the parameters. It is important to consider that viscosity varies due to the non-isothermal flow of material across the extrusion head (Turner et al. [2014](#page-216-0)).

Similarly to case study 2, Fig. [7.23](#page-211-0) demonstrates shows the variations of the elastics modulus and yield stress of PLA filaments produced using different temperatures in the extruder using different 3D printers. By fixing the extrusion parameters such as deposition velocity and screw rotation velocity, it is possible to observe that the different temperatures of the extruder nozzle produce strands with different mechanical properties.

We expect that the flow stresses on the liquid polymer in the extruder result in some deformation of the polymer chains in the melt. Before solidification, relaxation may take place on a timescale which is exponentially related to the temperature of the melt. At higher temperatures, relaxation will take place more quickly than at lower temperatures. Clearly, relaxation processes will cease on crystallisation in the case of crystallisable polymers. In this case study, the increase

<span id="page-211-0"></span>

Fig. 7.23 Tensile properties of PLA filaments obtained from two different 3D printers and at varying the nozzle temperature



Fig. 7.24 2D scattering patterns and orientation parameter  $(\langle P_2 \rangle)$  of vertically positioned PCL filaments drawn at different extrusion temperatures: 80 °C, 100 °C and 120 °C

of the extrusion temperature leads to a decrease in the level of preferred orientation of the crystals as  $\langle P_2 \rangle$  changed from 0.043 to 0.017 from 80 to 120 °C. The SAXS<br>patterns show a change from anisotropic pattern to an almost isotropic pattern patterns show a change from anisotropic pattern to an almost isotropic pattern (Fig. 7.24).

Equatorial scattering curves were extracted from the 2D SAXS patterns and the correlation functions were obtained, as displayed in Fig. [7.25.](#page-212-0) Clearly the processing of PCL at higher extruder temperatures did not induce significant changes in the crystalline and amorphous layer thicknesses, as shown in Fig. [7.26.](#page-212-0) We attribute this to the fact that the crystallisation takes place at a

<span id="page-212-0"></span>

Fig. 7.25 (a) Scattering curves of 2D SAXS patterns of PCL filaments deposited at different temperatures and (b) correlation function of the scattering curves



Fig. 7.26 Long period (Lp), crystalline  $(C_b)$  and amorphous layer  $(A_b)$  thicknesses and bulk crystallinity (BC) extracted from correlation functions

more or less constant temperature defined by the environment in the printer and the build platform. The changes observed in Fig. [7.24](#page-211-0) are related to the rate of cooling of the molten filament. If crystallisation takes place from an unrelaxed and deformed melt any extended chains will direct the crystallisation as discussed in Chap. [3](http://dx.doi.org/10.1007/978-3-319-39322-3_3). The ability to fine tune the level of anisotropy of the crystalline morphology provides an opportunity to optimise the mechanical properties of the printed objects, particularly important in the field of scaffolds for tissue engineering.

# <span id="page-213-0"></span>7.8 Summary

In this chapter, we show that additive manufacturing and 3D printing in particular is a multi-step process where each step significantly affects the properties of the object being manufactured. We have found that as with more traditionally polymer processing procedures discussed in other chapters that the precise details of the 3D printing parameters have an impact on the internal morphology of the filaments as well as the external finish quality. In particular, the preferred alignment of the crystals and thicknesses of the amorphous and crystalline layers are effected by the composition of the feedstock and the extruder jet temperature. Clearly, these results highlight the possibilities to use the 3D printing process to fine tune the properties of application-specific components and to estimate how each parameter will affect the final properties.

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# Chapter 8 Electrically Conductive Polymer **Nanocomposites**

Thomas Gkourmpis

# 8.1 Introduction

Polymer nanocomposites combine the properties of the matrix with those of the filler additive, thus allowing for the creation of totally new classes of materials with improved mechanical, electrical, optical and thermal properties. This combination of properties offers immense versatility and design capabilities and as consequence research in nanocomposites has been ever-growing. Traditionally carbon black has been the filler of choice for applications where electrical conductivity was required. This was done mainly due to the simplicity and versatility of the carbon black particles in combination with the relatively low cost preparation methods available (Kuhner and Voll [1993](#page-243-0)). Over the years other conductive fillers of anisotropic dimensions (high aspect ratio) like metal nanowires, graphene and carbon nanotubes (CNTs) have been introduced leading to a revolution in polymer nanocomposites. The potential of these fillers to achieve high conductivity due to their unique geometry at low or very low concentrations has attracted enormous scientific and commercial attention.

In order for this potential to be realised the possibility of producing and controlling well-defined systems is dependent on the detailed understanding of the structure–property relations of these nanocomposites. In this section we will review systems where the filler introduced creates a level of electrical conductivity in the resulting composition, and we will discuss how different classes of fillers affect the overall properties of the polymer. Furthermore, we will discuss the key structure– property relationships highlighting the underlying mechanisms that give rise to them. Of course such a wide topic cannot be treated within the limitations of this work, so the interested reader is encouraged to explore a number of comprehensive

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studies on polymer nanocomposites available (Bauhofer and Kovacs [2009;](#page-241-0) Moniruzzaman and Winey [2006](#page-243-0); Winey and Vaia [2007](#page-244-0); Winey et al. [2007;](#page-244-0) Byrne and Gunko [2010](#page-241-0); Mutiso and Winey [2012;](#page-243-0) Gkourmpis [2014\)](#page-242-0).

# 8.2 Percolation Theory

The connectivity and spatial arrangement of objects within a network structure and the resulting macroscopic effects can be described by the percolation theory. In all its variations the percolation theory focuses on critical phenomena that originate from the spatial formation of a network and result in sharp transitions in the behaviour of the system of interest (Kirkpatrick [1973](#page-243-0)). Percolation models have been applied with various degrees of success to the description of the electrical behaviour of polymer nanocomposites. In these systems the insulating polymer matrix is loaded with conductive filler whose network formation leads to a sharp insulation-conductor transition (Lux [1993\)](#page-243-0). Experimental work and theoretical predictions have established that the system's conductivity σ follows a power-law dependence in accordance with percolation theory

$$
\sigma \approx \sigma_{\rm o}(\phi-\phi_{\rm C})^t
$$

with  $\sigma_0$  a pre-exponential factor that is dependent on the conductivity of the filler, the network topology and the types of contact resistance. The terms  $\phi$  and  $\phi_C$ correspond to the filler concentration and the critical concentration at the transition (also known as percolation threshold) (Foygel et al.  $2005$ ). The critical exponent t is also conductivity-dependant with universal values of  $t \approx 1.33$  and  $t \approx 2$  for two and three dimensions, respectively (Stauffer and Aharony [1987;](#page-244-0) Sahimi [1994\)](#page-244-0). It must be noted however that a wide range of values as high as  $t \approx 10$  for the critical exponent have been reported (Bauhofer and Kovacs [2009](#page-241-0); Gkourmpis [2014](#page-242-0)). The reason for this deviation from universality is still not well understood with complex tunnelling transport phenomena (Balberg [1987,](#page-241-0) [2009;](#page-241-0) Grimaldi and Balberg [2006;](#page-242-0) Johner et al. [2008\)](#page-242-0) and filler variability in terms of production, entanglement, interconnections and surface chemistry being suggested as possible culprits (Mutiso and Winey [2012\)](#page-243-0). In Fig. [8.1,](#page-219-0) the percolative behaviour of a system of polycarbonate with single-walled carbon nanotubes can be seen (Ramasubramaniam et al. [2003](#page-244-0)). This behaviour of sharp conductivity increase at a specific filler concentration is typical of all polymer nanocomposites and can be understood within the framework of the percolation theory.

As discussed previously, there are a number of percolation models dealing with electrical conductivity. Initial approaches were treated with systems where the particles were confined in well-defined periodic positions (lattice models). For such systems analytical solutions can be used in the case of one and two dimensions (Fisher and Essam [1961\)](#page-242-0) and numerical solutions based on Monte Carlo methods for three dimensions (Kirkpatrick [1973\)](#page-243-0). Obviously such models despite their

<span id="page-219-0"></span>

Fig. 8.1 (a) Electrical conductivity of polycarbonate/SWCNT composites as a function of the filler mass fraction. Different commercial applications are also noted in the graph. (b) Power-law application to experimental data for the calculation of the percolation threshold. Reprinted with permission from Ramasubramaniam et al. [\(2003](#page-244-0))

usefulness are very poor representations of real systems, something that has led to the development of continuum (off-lattice) models that allow more realistic placement of the particles in space. The main types of continuum models can be classified as follows:

Soft-core systems: In this class of models the particles are assumed to be fully interpenetrating and are considered bonded when they overlap.

- Hard-core systems: In this approach the particles are allowed to touch each other but not overlap.
- Hard-core with soft shell: In this approach the electrical percolation depends not only on the geometry of the particles but on the tunnelling distance between them. In other words the particles are considered to have a hard non-penetrating core and a penetrable shell around the hard core.

For high aspect ratio systems the study gets computationally expensive due to the spatial orientation of the particles. One of the most common approaches to avoid complexity is to treat the particles with respect to their excluded volume (Hard-core) that can be significantly different from their true volume (Balberg et al. [1984](#page-241-0)). In such a representation the critical number of particles required for percolation  $N_{\rm C}$  is inversely proportional to the excluded volume ( $V_{\rm excl}$ )

$$
N_{\rm C} \propto \frac{1}{V_{\rm excl}}
$$

In a similar manner, the percolation threshold  $\phi_C$  can be expressed as the ratio of the true volume of the particle  $(V)$  over the excluded volume

$$
\phi_{\rm C} \propto \frac{V}{V_{\rm excl}}
$$

In the case of a cylinder the average excluded volume per rod can be written as (Balberg et al. [1984](#page-241-0))

$$
V_{\text{excl}} = \frac{32\pi}{3} R^3 \left[ 1 + \frac{3}{4} \left( \frac{L}{R} \right) + \frac{3}{8\pi} \langle \sin \theta \rangle \left( \frac{L}{R} \right)^2 \right]
$$

with L and R the length and radius of the cylinder and  $\theta$  the angle between two random rods. In a similar manner, the percolation threshold can be expressed as (White et al. [2009](#page-244-0))

$$
\phi_{\rm C} = \frac{\frac{4}{3}\pi R^3 + \pi R^2 L}{\frac{32}{2}\pi R^3 + 8\pi R^2 L + \pi R L^2}
$$

From these relations we can clearly see that the aspect ratio  $(L/R)$  will dominate the percolation threshold, and although in the limit  $L/R \rightarrow \infty$  the above-mentioned equations require some alterations (Balberg et al. [1984;](#page-241-0) Berhan and Sastry [2007\)](#page-241-0), the basic assumptions are still valid (Mutiso and Winey [2012](#page-243-0)). In the case of the hard-core with soft shell cylinders the equivalent relationship can be expressed as (Berhan and Sastry [2007;](#page-241-0) Wang and Ogale [1993](#page-244-0))



$$
V_{\text{excl}} = \frac{32\pi}{3} R^3 \left[ \left( 1 - \kappa^3 \right) + \frac{3}{4} \left( \frac{L}{R} \right) \left( 1 - \kappa^2 \right) + \frac{3}{32} \left( \frac{L}{R} \right)^2 \left( 1 - \kappa \right) \right]
$$

with  $\kappa = r/s$  being the core–shell ratio (see Fig. 8.2).

Most percolation studies rely on Monte Carlo simulations, whose properties of interest are critical cluster size, bond densities (i.e. number of bonds that lead to network per site), particle volume in the matrix, particle orientation and network geometry at the threshold. In most cases simulations treat the percolation in a statistical manner which means that the particles are randomly distributed in the matrix and network pathways are formed simply by increasing the particle volume fraction in the composite. Although such an approach has merit and provides valuable insight on the network formation, it is far away from reality, especially when polymers are concerned. Addition of particles in a polymer matrix is mainly performed via solution or melt mixing, which means that both particles and polymer chains are in motion and interact with each other. More advanced theoretical approaches do take into consideration the thermodynamic interactions between the composite constituents (particle–particle, particle–polymer and polymer–polymer) as well as any external stimulus such as shear forces. The need to account for the particle mobility and interactions manifests itself in cases where strongly interacting particles with a tendency to cluster after mixing is considered. A typical example of such system is epoxy/CNT composites whose very low reported and experimentally observed percolation  $(\phi_c \ll 0.1 \text{ wt})$  is attributed to the strong attractive interactions between the carbon nanotubes (Bauhofer and Kovacs [2009;](#page-241-0) Mutiso and Winey [2012;](#page-243-0) Gkourmpis [2014](#page-242-0); Bryning et al. [2005\)](#page-241-0).

# 8.2.1 Electrical Conductivity Mechanisms

Macroscopic conductivity is achieved by addition of conductive particles in an insulating polymer matrix and is controlled by percolative behaviour. The conductivity-filler dependence is typically governed by an s-shape curve with three distinct regimes: (1) at very low loadings the filler amount in the matrix is low and the individual particle density is not enough to create an adequate network for current flow. In this regime the macroscopic (observed) conductivity is dominated by the matrix, (2) close to the percolation threshold the filler concentration is such that an adequate network capable of facilitating current flow is created, and this is followed by a sharp increase in the observed conductivity value and, (3) above the threshold the particle network becomes extensive, thus capable to facilitate current flow through multiple channels, and this is manifested by a high observed conductivity value. Within the framework of the percolation theory the electrical conductivity of a polymer nanocomposite is treated in geometrical terms in each of the three distinct regimes. In other words in order to have current flow through the matrix, the particles must be in contact in such numbers as to have a clear intact pathway (network) whose number or density determines the overall value of the conductivity. In the case where the particles are far apart with enough polymers occupying the space between them, no current flow is possible and the system is not conductive. A schematic representation of these ideas can be seen in Fig. [8.3.](#page-223-0)

Here we must note that even in the insulating region there is a certain level of conductivity despite the lack of adequate conductive network. The conductivity in this region is dominated by trapped charge carriers and polarisation effects and is mainly influenced by the morphology, polarity and electronic band structure of the polymer. Furthermore due to the frequency dependence of conductivity and permittivity of the matrix, the dielectric response of the system will be different for direct and alternating current. Nevertheless, this type of conductivity of essentially insulating materials is beyond the scope of this work but the interested reader is encouraged to consult recently published reviews and the references wherein (Glowacki et al. [2012](#page-242-0)).

It has been reported that filler particles can be separated by polymer at the high conductive region as well as in the insulating region (Balberg [2009\)](#page-241-0). For electrical conductivity to exist in this case it has been suggested that the electric transport between the conductive particles is facilitated by quantum tunnelling and electronic

<span id="page-223-0"></span>

Filler Amount in the composite

Fig. 8.3 Schematic representation of the percolative behaviour of a nanocomposite, indicating the different regions as a function of the electrical conductivity and the total amount of filler present. A schematic representation of the network creation for artificial spherical particles can also be seen for the different conductivity regions

hoping mechanisms (Balberg [1987,](#page-241-0) [2009,](#page-241-0) [2012;](#page-241-0) Glowacki et al. [2012](#page-242-0); Strumpler and Glatz-Reichenbach [1999](#page-244-0); Balberg et al. [2004;](#page-241-0) Sherman et al. [1983](#page-244-0)). Here we must note that while the percolation theory requires a sharp cut-off as onset to conductivity (i.e. the particles will either touch and conduct or be apart and not conduct) the tunnelling approximation is a continuous function of the interparticle distances (Stauffer and Aharony [1987;](#page-244-0) Sahimi [1994\)](#page-244-0). Consequently, the tunnelling conductance decays exponentially with the interparticle distance, thus leading to a non-sharp cut-off (Balberg [2009](#page-241-0)). According to this we can express the interparticle conductance g between two particles i and i as (Balberg [2012;](#page-241-0) Ambrosetti et al. [2010](#page-241-0))

$$
g_{ij} = g_o \exp\left(-\frac{2\delta_{ij}}{\xi}\right)
$$

with  $\xi$  the wavefunction decay length of the electron outside the particle to which it belongs and  $\delta_{ii}$  the minimal distance between two particles. In the case of spheres of diameter D the minimal distance can be written as  $\delta_{ij} = r_{ij} - D$  with  $r_{ij}$  the distance between the two centres. In this case we have two extremes that will lead to qualitatively different conductivity behaviours. In the case of large particles  $\xi/D$  $\rightarrow$  0 it becomes obvious from the above relationship that non-zero conductance is possible only when the particles touch each other. Therefore removing particles from the random closed packed limit will be equivalent of removing tunnelling bonds in a similar manner to a standard percolation lattice system (Sahimi [1994;](#page-244-0) Balberg [2012](#page-241-0)). In such a case the system will exhibit conductivity that follows percolation-type behaviour with critical exponent  $t \approx 2$  and  $\varphi_C$  that correspond to the appropriate system-dependant percolation threshold (Johner et al. [2008\)](#page-242-0). In the other extreme case  $D/\xi \rightarrow 0$  the sites are randomly distributed in the system and site density  $\rho$  variations have no effect on the particle connectivity, but affect the distance  $\delta_{ii} = r_{ii}$  between sites (Balberg [2009](#page-241-0)). In such case it has been seen that the conductivity behaviour in the context of hoping approximation in amorphous semiconductors can be expressed as (Balberg [2012;](#page-241-0) Ambrosetti et al. [2010\)](#page-241-0)

$$
\sigma \propto \exp\left[-\frac{1.75}{\left(\xi \rho\right)^{1/3}}\right]
$$

which is the low density limit of the first extreme case.

The conductivity behaviour as a function of the percolation threshold and the aspect ratio for spheres, oblate (sheet-like) and prolate (rod-like) spheroids has been calculated using random sequential addition (RSA) and Monte Carlo techniques (Mutiso and Winey [2012](#page-243-0); Balberg [2012;](#page-241-0) Shklovskii and Efros [1984;](#page-244-0) Tye and Halperin [1989;](#page-244-0) Berman et al. [1986](#page-241-0); Shante and Kirckpatrick [1971](#page-244-0); Balberg and Binenbaum [1987](#page-241-0); Hunt and Ewing [2009;](#page-242-0) Ambrosetti et al. [2010\)](#page-241-0). In Fig. [8.4](#page-225-0) the distributions of impenetrable spheres and spheroids of different aspect ratio  $a/b$ (with  $a$  and  $b$  the polar and equatorial semi-axes, respectively) can be seen. In this framework the conductivity has been seen to reduce strongly with decreasing volume fraction of the particles (see Fig. [8.5](#page-226-0)), something attributed to the increasing interparticle distances that lead to a reduction of the local tunnelling conductances (Ambrosetti et al. [2010](#page-241-0)). This reduction depends strongly on the shape of the filler particles, and with increased anisotropy the overall conductivity onset decreases for a fixed  $\xi$  (Fig. [8.5b](#page-226-0)). Analytical relations for the tunnelling conductivity of randomly distributed prolate, oblate and spherical particles, respectively, can be expressed as (Ambrosetti et al. [2010\)](#page-241-0)

$$
\sigma \approx \sigma_0 \exp\left[-\frac{2D\gamma(b/a)^2}{\xi} \right]
$$

$$
\sigma \approx \sigma_0 \exp\left\{-\frac{2D}{\xi} \left[\frac{0.15(a/b)}{\phi}\right]^{4/3}\right\}
$$

$$
\sigma \approx \sigma_0 \exp\left[-\frac{2D}{\xi} \frac{1.65(1-\phi)^3}{12\phi(2-\phi)}\right]
$$

In the previous discussion we have seen that the hoping and tunnelling conductivity models are extreme cases of the same problem. Therefore for a system with

<span id="page-225-0"></span>

Fig. 8.4 Examples of distributions of impenetrable oblate and prolate spheroids of different aspect ratio  $\left(\alpha/b\right)$  and volume fraction  $\left(\varphi\right)$  generated from computational techniques. Reprinted with permission from Ambrosetti et al.  $(2010)$  $(2010)$ 

interparticle conduction by tunnelling there must be a "well-defined" threshold. According to this and by assuming that the critical behaviour will depend on the distribution of conductance along the average local resistance of the system we can express the critical exponent as (Balberg [2012\)](#page-241-0)

$$
t - t_{\rm un} = \frac{4(a-b)}{\xi} - 1
$$

Although more accurate expressions of  $t$  are available (Johner et al. [2008](#page-242-0)), the above relationship is sufficient for this discussion. So far we have seen that both conductivity (under the hoping model) and the critical exponent (under the

<span id="page-226-0"></span>

Fig. 8.5 Computational predictions indicating electrical conductivity dependence as a function of volume fraction on (a) tunnelling conductivity for hard prolate spheroids of aspect ratio  $\alpha/b = 10$ with different characteristic tunnelling distances and (b) tunnelling conductivity in a system of hard spheroids of different aspect ratios. The dotted lines are predictions based on the critical path approximation method. Reproduced with permission from Ambrosetti et al. ([2010\)](#page-241-0)

tunnelling model) are dependent on the interparticle distances in the system. Therefore we can see that when conductivity varies with the concentration of particles, the effect that will dominate is the variation of the local conductance instead of the connectivity of the system. This is obviously valid only in areas where an appropriate interparticle distance distribution exists. In this description, when tunnelling is considered as the mechanism of interparticle conduction, the conductivity function  $\sigma(\varphi)$  leads to two distinct results for the critical exponent (Johner et al. [2008;](#page-242-0) Balberg [2012](#page-241-0)). Based on the previous discussion we can see that the two expressions of the critical exponent behaviour are equivalent (the physics is essentially the same in both approaches) and will merge in the  $(2a - 2b)/\zeta \gg 1$ limit. It is also possible to estimate the percolation threshold value for prolate

$$
\phi_{\rm C} \approx \frac{2D}{\xi} \frac{\gamma (b/a)^2}{\ln(\sigma_{\rm o}/\sigma_{\rm m})}
$$

and oblate particles as a function of the matrix conductivity  $\sigma_{\rm m}$ 

$$
\phi_{\rm C} \approx 0.15 \left(\frac{a}{b}\right) \left[\frac{2D}{\xi} \frac{1}{\ln(\sigma_{\rm o}/\sigma_{\rm m})}\right]^{3/4}
$$

The critical path approximation and the critical path distance  $\delta_C$  are a very effective way of describing the tunnelling conductivity of polymer composites, since the geometrical connectivity problem of semi-penetrable particles in the continuum is of fundamental importance for the understanding of the filler dependencies  $(\varphi, \varphi)$ D and  $\alpha/b$ ) on conductivity. From the above expressions for the percolation threshold  $(\varphi_C)$  we can see that it corresponds to the critical concentration required



Fig. 8.6 Schematic representation of the electrical conductivity dependence on the site occupation probability when tunnelling is the main conduction mechanism. The dotted lines indicate the local percolation thresholds when all corresponding near neighbours are considered. The overall conductivity behaviour appears to have a staircase dependence of the occupation probability leading to a system of multiple thresholds (refer to the text for more details)

for percolation (onset of conductivity) by an ensemble of equal (or nearly equal) resistors (Balberg [2009](#page-241-0), [2012](#page-241-0); Balberg et al. [2004\)](#page-241-0). Therefore in the tunnelling model more than just one onsets (percolations) are possible in a sequential manner, thus leading to a series of "steps" that are representative of the local conductances in the system (see Fig. 8.6). Thus in the case of a single or multiple mixed but not well-separated steps the data will be fitted with a single  $t$  in a manner similar to the standard percolation theory. In the case where multiple clearly defined steps are available multiple fits are required, leading to a larger value of  $t$  and a lower percolation threshold. In the latter case we must stress that the value of the percolation threshold does not have an intrinsic meaning.

We will close this discussion on conduction mechanisms by stressing that the tunnelling percolation model is in good agreement with experimental data and the geometrical percolation model. This is quite striking especially if we consider all the different factors that affect filler dispersion in a polymer matrix in comparison with the idealised models discussed previously. In reality fillers have non-uniform size, shape, aspect ratio and geometry distributions, and they are subject to orientation, entanglements, agglomeration and interaction with the polymer matrix. Furthermore, different mixing methods can have a huge impact on the dispersion level and structural integrity of the filler particles, especially in cases where high sheer and elongational forces are present (Gkourmpis [2014](#page-242-0); Oxfall et al. [2015;](#page-243-0) Pötschke et al. [2004](#page-244-0)).

# <span id="page-228-0"></span>8.3 Filler Effects on Polymer Nanocomposites

In this section we are going to discuss the effect high aspect ratio fillers have in the polymer matrix and subsequent properties. We will discuss the effect the filler shape, size, distribution and orientation have on the polymer matrix focusing especially in the resulting morphology.

### 8.3.1 Aspect Ratio

High aspect ratio fillers percolate at low loadings in comparison with spherical or other low aspect ratio objects. This has been attributed to the efficiency of the network formation by large objects, due to the limited number of contacts required for the creation of a conductive cluster. This has resulted in percolation thresholds of the order of 0.1 wt% for CNT and graphene-based nanocomposites (Gkourmpis [2014;](#page-242-0) Stankovich et al. [2006;](#page-244-0) Ramasubramaniam et al. [2003](#page-244-0); Kim and Macosko [2008;](#page-242-0) Kim et al. [2010\)](#page-243-0). The theoretical percolation threshold of soft- and hard-core spheres in three dimensions is 0.29 and 0.16, respectively (Balberg [1986](#page-241-0); Pike and Seager [1974](#page-243-0)). In the case of conventional fillers like carbon black the percolation threshold varies between 3 and 20 wt%, but these values are heavily dependent on the carbon black type, structure, surface purity and preparation method (Gkourmpis [2014\)](#page-242-0). Recently, conducted theoretical studies on finite aspect ratio nanowires (Gelves et al. [2006](#page-242-0), White et al. [2009](#page-244-0)) and randomly distributed graphite nanoplatelets (Li and Kim [2007\)](#page-243-0) have highlighted the role of the aspect ratio in the percolation threshold. In both studies the filler diameter and thickness has been seen to have a direct impact on the predicted percolation threshold, and the overall aspect ratio increase leads to lower thresholds (see Fig. 8.7).



Fig. 8.7 Computational prediction on the effect of the diameter (left) and thickness (right) of randomly distributed graphene nanoplatelets of different aspect ratio  $(D/t)$  on the percolation threshold. Adopted from Li and Kim [\(2007](#page-243-0))

	D	$\boldsymbol{t}$		Percolation	
Polymer matrix	$(\mu m)$	(nm)	$dl$ t	threshold $(\%$ vol)	Reference
High density polyethylene	6	10	600	4.46	Weng et al. $(2004)$
Epoxy	15	9.5	1579	1.13	Li and Kim $(2007)$
Poly(styrene-methyl methacrylate)	100	30	3333	0.878	Chen et al. $(2001)$
Polymethylmethacrylate	100	22	4545	0.529	Zheng and Wong (2003)
Polyisopropylene	50	10	5000	0.67	Chen et al. (2002)
Epoxy	46	4.5	10,222	0.5	Li et al. $(2007)$
Poly(ethylene vinyl-acetate)	25	6	4000	2.5	Gkourmpis (2014)
Poly(ethylene butyl- acrylate)	25	6	4000	6.9	Oxfall et al. $(2015)$

Table 8.1 Effect of geometric shape factors and aspect ratio on the percolation threshold for graphene nanoplatelets with different matrix polymers

Here we must note that reported experimental results vary widely due to the different preparation methods that have a direct impact on the level of dispersion of the filler in the polymer matrix. All theoretical predictions are made assuming perfect or near-perfect dispersion, so a level of discrepancy between the theoretical and experimental threshold values is to be expected. These discrepancies become significant when melt mixing methods are employed. In Table 8.1 a small collection of experimental data for graphite platelets can be seen for a number of different polymers. These values are higher than the theoretical predictions seen in Fig. [8.7](#page-228-0) indicating how important the filler geometry and preparation method is. A more comprehensive discussion on the different preparation methods and their effect on the nanocomposite properties has been presented elsewhere (Moniruzzaman and Winey [2006](#page-243-0); Gkourmpis [2014;](#page-242-0) Kim and Macosko [2008](#page-242-0); Kim et al. [2010](#page-243-0)).

#### 8.3.2 Polydispersity

So far in the discussion we have assumed that all fillers introduced in the matrix are of the exact same size and shape. Such assumptions do not hold for real systems where the preparation methods of the filler and the nanocomposite have an effect on the geometry of the individual filler particle (Moniruzzaman and Winey [2006;](#page-243-0) Gkourmpis [2014;](#page-242-0) Kim and Macosko [2008](#page-242-0); Kim et al. [2010](#page-243-0)). Carbon nanotubes especially are known to be very sensitive to their preparation methods that can have significant effects on their diameter, length and chirality. The latter is of particular importance since it has a direct influence on the electrical conductivity, resulting to metallic and semiconductive tubes (Moniruzzaman and Winey [2006\)](#page-243-0). As discussed previously the aspect ratio has a strong influence on the percolation phenomena, therefore it is expected that any changes in the distribution of aspect ratio, length, thickness (or diameter) of the filler particles will have an effect on the overall electrical conductivity of the nanocomposite.

It has been reported that the percolation threshold exhibits an inversely proportional relationship to the weight average of the length distribution in the case of rods, an effect that is getting more pronounced with increasing width of the length distribution (Kyrylyuk and van der Schoot [2008](#page-243-0)). Analytical studies predict that the incorporation of small amounts of longer rods significantly reduces the percolation threshold. This effect is also more pronounced with increasing amounts of longer rods in the system (Otten and van der Schoot [2009\)](#page-243-0). The inverse relation between percolation and amount of conductive filler indicates that the electrical conductivity of the nanocomposite is governed solely by the existence of conductive particles and not the polymer matrix. Although this appears self-evident in real nanocomposites, the situation is not exactly like that. In a real system the distribution of conductivities from the high aspect ratio fillers varies in an almost continuous manner taking into consideration the morphology and the possible defects, leading to a less profound effect on the percolation than predicted theoretically. An example of this is the case of CNT-based systems, where the individual conductivity of SWCNT varies significantly, sometimes to levels of several orders of magnitude (Ebbesen et al. [1996](#page-242-0)). The contact resistance between CNTs also differs with metallic–semiconducting junctions exhibiting significantly higher values than metallic–metallic or semiconducting–semiconducting, something that has been attributed to the Schottky and tunnelling barrier between different tubes (Fuhrer et al. [2000](#page-242-0)).

The addition of low aspect ratio particles in the high aspect ratio conductive network creates a hybrid mixture of particles of different sizes. This is a common practice in both research and industrial materials as it allows for unique versatility and balancing of the overall conductivity with other desired properties of interest (e.g. viscosity, mechanical reinforcement, crystallinity). For example it has been reported that the addition of (relatively) more expensive CNTs or GNPs in standard polymer/carbon black compositions offers significant improvements in conductivity and other properties of interest (Oxfall et al. [2015;](#page-243-0) Ma et al. [2009](#page-243-0); Sun et al. [2009;](#page-244-0) Brigandi et al. [2014;](#page-241-0) Fan et al. [2009](#page-242-0); Wei et al. [2010;](#page-244-0) Kostagiannakopoulou et al. [2012](#page-243-0)). For epoxy and poly(ethylene butyl acrylate) copolymers it has been reported that by substituting just 10 wt% of the high aspect ratio filler (graphene nanoplatelets in this case) with carbon black a reduction of the percolation threshold from 0.75 to 0.5 wt% and 6.9 to 4.6 vol.% was achieved for the two systems, respectively (Oxfall et al. [2015](#page-243-0); Fan et al. [2009\)](#page-242-0). In a similar manner the creation of hybrid blends of graphene, nanotubes and carbon black has been seen to offer improvements in mechanical properties (Wei et al. [2010](#page-244-0); Kostagiannakopoulou et al. [2012\)](#page-243-0). The reason for the improved conductivity of hybrids has been attributed to synergistic effects between the structural arrangements of the two particle networks. Due to thermodynamic reasons it is expected that each conductive particle type will create a network structure in the matrix. This structure will have active pathways capable of enhancing conductivity and the so-called dead ends which are parts of the network that do not contribute in the overall



Fig. 8.8 (Left) Electrical conductivity as a function of filler content for EBA with carbon black, graphene platelets, and hybrid systems of mixtures between carbon black and graphene platelets. Adopted from Oxfall et al. ([2015\)](#page-243-0). (Right) schematic representation of a CB/CNT hybrid indicating the preferential localisation of the filler particles, the existence of active (conductive) and dead (non-conductive) network branches and the conductive bridges between the two filler networks existing in the matrix

conductivity. Due to size the network structure of high aspect ratio filler will be fairly extended, whereas the network of the low aspect ratio carbon black is expected to be fairly compact. Therefore, the low aspect ratio filler network can localise partially between branches of the extended high aspect ratio network creating conductive bridges (see schematic in Fig. 8.8b). By doing so the percolative behaviour of the overall composition changes, leading to a lower threshold while at the same time the overall conductivity follows a more complex expression than the traditional power law we discussed earlier. This can be seen in Fig. 8.8 where the percolative behaviour of a system of poly(ethylene butylacrylate) with carbon black and graphene nanoplatelets is presented. Both systems containing a single filler type exhibit the traditional power-law percolative behaviour, whereas the different hybrids (systems of graphene with carbon black added) deviate from it while at the same time exhibit lower percolation threshold values (Oxfall et al. [2015](#page-243-0)).

### 8.3.3 Orientation

All fillers are capable of orienting with external stimulus in the melt, a situation that is common in most polymer-based processes. High aspect ratio filler orientation has a far greater impact on conductivity, mainly due to the reduction of contact points between the individual particles. This contact reduction destroys the integrity of the filler network, leading to a substantial decrease in conductivity. The extent of the orientation can be described through the orientation distribution function  $n(\theta, \varphi)$ and by assuming that the polar and azimuthal angles  $\theta$  and  $\phi$  are independent the axial and planar orientation parameters for the case of rods can be expressed as (Munson-McGee [1991](#page-243-0))

$$
f_p = 2\langle \cos^2 \varphi \rangle - 1
$$

$$
f_a = \frac{1}{3} (3\langle \cos^2 \theta \rangle - 1)
$$

These parameters can have values between 0 and 1 that correspond to random and axial spatial arrangement, respectively, in a matter similar to the nematic order parameter in liquid crystal polymers (both expressed in the literature as S) (Mitchell et al. [1987](#page-243-0); Pople and Mitchell [1997](#page-244-0); Lacey et al. [1998](#page-243-0); Andersen and Mitchell [2013\)](#page-241-0). Theoretical predictions and experimental work on nanorods in two and three dimensions have indicated that the electrical percolation takes its lowest value in the case of isotropic  $(S = 0)$  or slightly isotropic  $(S \sim 0.1{\text -}0.2)$  system. As the level of anisotropy increases the percolation threshold takes ever higher values that are correlated with the level of alignment of the filler in the system (large values of S) (Mutiso and Winey [2012](#page-243-0); White et al. [2009;](#page-244-0) Behnam et al. [2007\)](#page-241-0).

Filler orientation has a significant effect on the overall electrical conductivity especially in melt-mixing methods. This is the result of the disruption of the filler network integrity due to the shear and elongational forces during mixing. In almost all cases where the system (matrix and filler) flows the polymer chains will align along the flow direction creating extended chain conformations. This chain alignment leads to further alignment of the filler particles along the flow direction. Obviously the alignment level of the polymer is strongly dependant to the chain conformation, but in principle all polymers do exhibit a level of orientation along the flow direction. As soon as the external stimulus stops the polymer chains revert to the "natural" random coil conformations, but the filler particles due to their size cannot do the same in a very short period of time. If now we consider that in most cases when the external stimulus ends the system undergoes a certain level of cooling (e.g. injection moulding, film blowing, fibre spinning) then we can see that the crystallisation process in the matrix makes the filler movement even more difficult. Large fillers like graphene and nanotubes tend to suffer from this effect more than more traditional ones like carbon black, although this depends heavily on the shear forces and the polymer/filler composition.

#### 8.3.4 Dispersion and Filler Localisation

Filler incorporation in a polymer matrix is achieved by a number of different methods, but all generally fall under three main categories, solution, melt and in-situ polymerisation mixing. In solution mixing, both polymer and filler dispersion is facilitated by solvents that are removed after mixing. Melt mixing is by far the most common method used commercially and in this case the filler is added to the polymer melt and dispersion is facilitated by an external stimulus, usually in the form of a compounding or extruding machine. In the case of in-situ polymerisation mixing, the filler is added during the growth phase of the polymer. Each of the mixing methods has advantages and disadvantages, that have been discussed elsewhere (Gkourmpis  $2014$ ), but in the context of this work is sufficient to say that the level of dispersion is strongly influenced by the way the filler is incorporated in the matrix.

When filler is incorporated in a matrix, a wide range of interactions is available in the system that can have a direct link in the overall morphology, topology and properties of the nanocomposite. Polymer–filler interactions can extend over a range of distances and length-scales and can be weak or strong (Kyrylyuk and van der Schoot [2008\)](#page-243-0). The interfacial energy between polymer and filler has been seen to affect the compatibility and efficiency of mixing, although this is strongly related to the chain conformation and filler structure (Alig et al. [2012](#page-241-0)). This property has been exploited in immiscible polymer blends where preferential localisation along the interface (Filippone et al. [2014;](#page-242-0) Huang et al. [2014;](#page-242-0) Gubbels et al. [1998](#page-242-0)) or in one of the phases allows for reduced percolation threshold (Gubbels et al. [1994,](#page-242-0) [1995;](#page-242-0) Gkourmpis et al. [2013\)](#page-242-0). This preferential localisation enhances conductivity only in the host phase leaving part of the matrix insulating and filler free. Consequently, the overall conductivity of the nanocomposite will be determined by the conductivity of the phase that hosts the filler in a manner similar to the single polymer cases discussed previously. Obviously for the entire nanocomposite to be conductive a network is required, which means that the two polymer phases must be co-continuous. Depending on the polymers immiscible blends tend to form co-continuous phases at ranges of 30–70 %, but addition of fillers can lead to phase swelling, thus creating systems where phase continuity can be achieved at far lower amounts. An example of this is an immiscible blend of polyethylene (PE) and polystyrene (PS) that reaches co-continuity at a range of 30–45 wt% PE. The amount of PE required to create a co-continuous phase can drop to 5 wt% by addition of small amounts of carbon black (Gubbels et al. [1995\)](#page-242-0). This effect is a simple manifestation of polymer thermodynamics, since the filler particle occupies a larger volume it means that the polymer phase containing it needs to take into consideration the volume increase. In terms of thermodynamics the criterion of the filler localisation and phase behaviour is the minimisation of the free energy of the system. Therefore if the free energy criterion is satisfied by the filler located in the polymer phase, then that phase will have to adjust to the volume change by swelling in a manner similar to block copolymers (Matsen [2002\)](#page-243-0). If this is not possible, then the filler will localise to the larger phase that is capable of adjusting to the subsequent volume changes.

For the understanding of the percolative behaviour of conductive fillers in immiscible polymer blends, the details of the filler distribution in the different phases are important. The critical condition for achieving the all-important co-continuity of the conductive filler-rich phase has been suggested to be determined by the viscosity of the phases as (Paul and Barlow [1980\)](#page-243-0)

$$
\frac{\phi_{\rm A}}{\phi_{\rm B}} \times \frac{\eta_{\rm B}}{\eta_{\rm A}} = X
$$

with  $\varphi$  and  $\eta$  the volume fraction and melt viscosity of the two phases (noted as A and B), respectively. For  $X > 1$  phase A is continuous,  $X \approx 1$  both phases are co-continuous and for  $X < 1$  phase B is continuous (Jordhamo et al. [1986](#page-242-0)). Interfacial tension and wetting coefficient of the different mixture components have also been identified to influence the filler distribution and subsequent morphology of the blend. For carbon black particles in an immiscible blend it has been suggested that their distribution can be qualitatively predicted by the wetting coefficient ω. The interfacial free energy minimisation can lead to Young's equation (Sumita et al. [1991](#page-244-0))

$$
\omega_{AB} = \frac{\gamma_{CB-B} - \gamma_{CB-A}}{\gamma_{AB}}
$$

with  $\gamma_{AB}$ ,  $\gamma_{CB-A}$  and  $\gamma_{CB-B}$  the interfacial tension between polymer A and B, CB and polymer A and CB and polymer B, respectively. According to this the distribution of carbon black particles can be classified as: for  $\omega_{AB} > 1$  the particles localise in phase A, for  $-1 < \omega_{AB} < 1$  the particles localise along the interface and for  $\omega_{AB}$  < -1 the particles localise in phase B. The interfacial tension between the phases can be estimated by Wu's harmonic mean average (Wu [1982](#page-244-0))

$$
\gamma_{AB}=\gamma_A+\gamma_B-4\bigg(\frac{\gamma_A^d\gamma_B^d}{\gamma_A^d+\gamma_B^d}+\frac{\gamma_A^p\gamma_B^p}{\gamma_A^p+\gamma_B^p}\bigg)
$$

with  $\gamma_A$  and  $\gamma_B$  the interfacial tension between polymers A and B,  $\gamma_A^d$  and  $\gamma_B^d$  the dispersive components of the surface tensions  $\gamma_A$  and  $\gamma_B$  and  $\gamma_B^p$  and  $\gamma_B^p$  the equivalent polar components. According to this three spreading coefficients  $\lambda$  can be defined for a ternary blend (Hobbs et al. [1988\)](#page-242-0)

$$
\lambda_{ikj}=\gamma_{ij}-(\gamma_{ik}+\gamma_{jk})
$$

Except for these thermodynamic considerations, kinetic factors, such as viscosity, chain conformation, mixing procedures (time, speed, sequence of incorporation, shear forces etc.) and possible affinity or reaction of the polymer to the filler have been seen to play a vital role in the particle localisation. Mixing in particular has been seen to have a big effect on the overall morphology of the system, as shear forces have a tendency to break large agglomerates into smaller aggregates. These smaller filler clusters can in turn erode into even smaller aggregates given enough mixing time, thus leading into a system with increased filler dispersion. Obviously such concepts are fairly simple in terms of small conductive fillers like carbon black, but the situation becomes more complicated in the case of larger nanosize and high aspect ratio fillers like graphene or nanotubes. In the latter case dispersion



Fig. 8.9 Electrical conductivity as a function of filler loading for a system of EVA/CB and an immiscible blend of EVA/EPP/CB, indicating the effects of selective localisation. Adopted from Gkourmpis et al. [\(2013](#page-242-0))

is even more difficult due to the filler size and the breakdown of the large agglomerates into smaller aggregates is truly challenging (Gkourmpis [2014](#page-242-0)).

The almost exclusive localisation of the filler in one phase of the blend has another very important effect as far as conductivity is concerned. Since the filler is the sole conductivity medium in the system (we can ignore the matrix conductivity for this discussion), its network formation will determine the amount of current flowing in the nanocomposite. As discussed previously if the system is co-continuous then the entire nanocomposite will be conductive, but its conductivity will arise only from the phase that contains the conductive filler. This concept is illustrated in Fig. 8.9 where the conductivity of a system of poly(ethylene vinylacetate)/poly(ethylene-co-propylene)/carbon black (EVA/EPP/CB) appears almost constant regardless of the filler loading (Gkourmpis et al. [2013\)](#page-242-0), something that is achieved by keeping the ratio of the filler with respect to the EVA phase (where it localises) constant. In other words the percolative behaviour of the filler in the EVA phase is similar to the percolative behaviour of the same filler in the EVA phase in a single-component system.

## 8.3.5 Rheology and Mechanical Properties

The introduction of large conductive fillers into a polymer matrix has been seen to influence the mechanical and flow characteristics of the system. In almost all cases this addition leads to increase in storage modulus  $(G')$  and complex viscosity with increasing filling amounts (Brigandi et al. [2014\)](#page-241-0). Storage modulus has been seen to increase sharply with adding filler amounts, leading to a situation where the system crosses over from a liquid-like response to a solid-like response. This transition is usually referred to as mechanical or rheological percolation (Penu et al. [2012\)](#page-243-0) and a power-law relationship can be used to determine its threshold

$$
G^{'} \propto (m-m_{\rm C})^t
$$

with m the mass fraction of the filler,  $m<sub>C</sub>$  the threshold for percolation and t the critical exponent (Du et al. [2004\)](#page-242-0).

Systems containing carbon black have been seen to exhibit significant shear thinning in comparison with single polymers or binary blends. This has been utilised in the case of poly(ethylene acrylic acid) (EAA) and polypropylene (PP) blends where by adding carbon black the rheological percolation has been reported to increase with increasing EAA content. This behaviour suggested that the rheological percolation was tightly coupled with the electrical percolation by forming network structures in both PP/CB and EAA/PP/CB composites (Chen et al. [2009](#page-241-0)).

The incorporation of conductive fillers has been reported to increase the strength and stiffness of the host matrix (Gkourmpis [2014\)](#page-242-0). One of the most important factors affecting the overall mechanical properties of a nanocomposite is the interfacial interaction between filler particles and polymer. This interaction is of great importance as the level of adhesion of the filler particle to the polymer will affect the efficiency of the energy transfer between them under load. In cases where the adhesion is high the stress transfer between the filler particles and the host matrix will be efficient, thus leading to an overall reinforcement of the nanocomposite. Parameters like yield, strain and tensile strength can be modelled for different adhesion levels with relatively good comparison to experimental results (Yan et al. [2006](#page-244-0)).

The reinforcement effects, as seen through the tensile strength, discussed previously are large with the incorporation of small amount of carbonaceous fillers into the polymer matrix. In the case of high aspect ratio fillers these effects are even more pronounced. The reason for this behaviour can be traced in the level of dispersion of the filler particles in the polymer matrix. In Fig. [8.10](#page-237-0), we can see that for a system of poly(vinyl alcohol) (PVA) with graphene nanosheets introducing 0.06 vol.% of graphene into the PVA matrix the tensile strength increases by 73 % whereas by increasing the filler level from 1.8 to 3 vol.% the tensile strength increase is negligible (from 42 to 43 MPa) with the elongation at break having similar decreasing behaviour (Zhao et al. [2010](#page-244-0)). This effect has been attributed to the rearrangement and further aggregation of graphene sheets as the overall amount increases due to van der Waals interactions. When this is happening the slippage of the aggregated sheets and energy transfer to the matrix will be less efficient in comparison with the case of single sheets during a tensile measurement. In Fig. [8.10](#page-237-0), we can see a schematic representation of this with respect to the different dispersion and aggregation levels of the filler in the matrix. Case (1) is the initial

<span id="page-237-0"></span>

Fig. 8.10 Mechanical properties (tensile strength and elongation at break) of PVA/graphene nanocomposites as a function of graphene loading (top left). Comparison between experimental data of the Young's Modulus of PVA/graphene nanocomposites with theoretical predictions using the Halpin-Tsai models. Two cases of unidirectional and random distribution of the graphene in the PVA were considered for the theoretical estimations (top right). Schematic representation of the various levels of dispersion of graphene in the PVA. Refer to the text for a more detailed discussion of the different dispersion possibilities (bottom). Adopted and reprinted with permission from Zhao et al. [\(2010](#page-244-0))

low loading situation where each filler particle is individually placed in the matrix, as more filler particles are introduced the spaces between the particles are filled and a network structure where the particles are in physical contact is created (case 2). Case (3) is an intermediate case where the particles are properly dispersed but a certain level of lose aggregation exists. In case (4) the individual particles are heavily aggregated creating larger structures that are detrimental to the efficiency of the reinforcement of the matrix. In a real system the spatial arrangement will move from case (1) to case (3) with increasing filler loading. A critical level of filler content called rheological (or mechanical) percolation exists on the interplay between the amount of filler and the efficiency of the mechanical reinforcement on the nanocomposite (Zhang et al.  $2008$ ). Below this content the filler particles are well dispersed and by increasing the loading a significant improvement on the mechanical performance can be realised. Above the percolation the filler particles tend to aggregate leading to inefficient structures that cannot transfer energy in an optimal manner leading to moderate mechanical improvement.

As discussed previously, a number of mathematical models for prediction of the mechanical reinforcement in polymer matrices exist. Halpin-Tsai (Halpin and Kardos [1976;](#page-242-0) Cadek et al. [2002\)](#page-241-0) and Lewis-Nielsen (Lewis and Nielsen [1970](#page-243-0)) equations are based on simple approximations and provide reliable predictions of the modulus of reinforced matrices where the filler is unidirectional or randomly distributed. Therefore one can utilise these predictions to quantify the level of dispersion and the possible orientation of the filler particles in the matrix (see Fig. [8.10\)](#page-237-0).

# 8.3.6 Crystallisation and Morphology

The introduction of conductive fillers in a polymer matrix except for the obvious effect on electrical conductivity which was discussed previously, has the possibility to affect the overall morphology of the nanocomposite. Here though we must note that the changes or their absence in the overall morphology are heavily dependent on the polymer, the type, regularity and size of the filler, the preparation methods as they affect the level of dispersion and the crystallisation conditions (Gkourmpis [2014\)](#page-242-0).

For systems containing simple fillers like carbon black one expects a decrease in overall crystallinity, in comparison with the pure polymer, that is linked to the overall filler content (Gubbels et al. [1994,](#page-242-0) [1995](#page-242-0), [1998;](#page-242-0) Gkourmpis et al. [2013\)](#page-242-0). Crystallisation kinetics as seen through the melting and crystallisation temperatures are affected, something that can be attributed to the partial immobilisation of the macromolecular chains in the vicinity of the filler particles. In the case of binary blends where the filler localises in one of the two phases it is not uncommon to see morphological changes in both phases. This has been seen for a system of EVA/EPP where despite the apparent immiscibility of the two components mutual interactions between the two phases lead to the EPP phase to exhibit a split in its crystallisation peak and adopt two distinct phases. The introduction of carbon black in the system localises the particles in the EVA phase, further limiting the crystallisation of the host phase due to the reduced mobility of the polymer chains in the vicinity of the carbon black particles (Gkourmpis et al. [2013](#page-242-0)).

In the case where high aspect ratio fillers like graphene or nanotubes are introduced in the matrix the shape and geometry of the particles has been seen to have an even more direct effect on the overall crystallisation behaviour of the nanocomposite. Due to their sheer size and geometrical regularity these fillers can be very efficient nucleating agents, promoting or hindering crystallisation and leading to morphological changes (Gkourmpis [2014](#page-242-0)). CNTs have been reported to induce nanohybrid shish-kebab (NHSK) crystals for a number of polymers like PE (Laird and Li [n.d.](#page-243-0)), PP (Xu et al. [2010](#page-244-0)) and poly(L-lactide) (PLLA) (Xu et al. [2011](#page-244-0)). The molecular origin of NHSK periodicity has been suggested to be closely related to the concentration gradient and the heat dissipation of the growth front of the lamellar structure. Once nucleation is initiated, the polymer concentration gradient at the crystal growth front adopts a periodic profile along the



Fig. 8.11 NHSK structure of PE/MWCNT as seen by SEM (a), TEM (b) and a schematic representation indicating how lamellas grow from the CNT surface (c). Reprinted with permission from Li et al. ([2005\)](#page-243-0)

nanotube axis. This combined with the fact that most of the heat generated by the crystallisation process can be dissipated along the nanotube, leads to a further temperature gradient along the axis of the nanotube. Parameters like the crystal periodicity, the CNT diameter, the lamellar thickness and the nanotube chirality have been suggested to affect the NHSK formation and growth (Laird and Li [n.d.;](#page-243-0) Li et al. [2009](#page-243-0)).

Control of the NHSK growth has been attributed to two factors, namely the epitaxial growth of the polymer on the CNT surface and the geometric confinement. Due to the small CNT dimensions the polymer chains exhibit preferential alignment along the tube axis regardless of the lattice matching between polymer and graphitic surface, leading to a soft epitaxy mechanism (Laird and Li [n.d.\)](#page-243-0). In the case of polyethylene the polymer behaves as being on a flat surface due to the significantly larger size of the nanotube, thus epitaxy is the main mechanism for crystal growth. As the chain begins crystallising on the surface geometric confinement, elements become important due to the comparable size of the crystal lamellar and the nanotube. Therefore the crystallisation will be preferential parallel to the nanotube axis without any regard for its chirality, leading to a situation where the orthogonal orientation of the lamellar is obtained (see Fig.  $8.11$ ) (Li et al. [2005](#page-243-0)). Computer simulations have suggested that CNT chirality is strongly influencing molecular crystallisation, something that has not so far been verified experimentally (Laird and Li [n.d.\)](#page-243-0).

As a final note we can say that the addition of CNTs in a semicrystalline polymer has the potential to impede, promote or have no effect on the nanocomposite crystallisation behaviour. This of course will be heavily dependent on the preparation method, the level of dispersion and the chemical configuration of both polymer and filler. It has also been suggested that the amount of CNTs in the system might

have an effect of the overall crystallisation behaviour. Low levels of CNTs might promote crystallisation while higher loadings can actually impede the whole process (Laird and Li [n.d.](#page-243-0)).

In the case of graphene the two-dimensional arrangement of the filler makes lattice matching the dominant form in the crystallisation process. This can be attributed to the sequential absorption of polymer chains on the graphitic surface that leads the polymer to undergo structural rearrangements in order to adopt the lowest energy. Therefore crystallisation will take longer time something also seen experimentally in the case of polypropylene (Xu et al. [2010](#page-244-0)). The flat graphitic surface can also allow the polymer crystals to grow into multiple nucleation points and orientations. It has been suggested that the multiple spatial opportunities for crystal growth might create interference from adjacent crystals leading to an overall suppression of the crystallisation kinetics process (Xu et al. [2010\)](#page-244-0). Again as in the case of nanotubes the nanocomposite preparation method, the level of filler dispersion, the amount of filler, the polymer architecture and the filler's surface characterisation are critical on the overall crystallisation process. A good example of this are two independent studies on poly(ethylene vinyl acetate) filled with graphene nanoplatelets, that indicate a totally different behaviour with respect to the crystallisation process. In the case of a melt-mixed system the existence of the filler has been seen to reduce slightly the overall crystallinity, while crystallisation takes place away from the filler that has a minimal impact on the overall morphology of the system (Stalmann [2012](#page-244-0)) in a manner similar to the one expected from traditional fillers like carbon black (Gkourmpis et al. [2013](#page-242-0)). In the case of solutionbased similar systems the existence of the filler has been reported to facilitate and promote crystallisation due to the high nucleating activity of the nanoplatelets (He et al. [2011](#page-242-0); Pang et al. [2012](#page-243-0)).

# 8.4 Summary

Electrically conductive polymer nanocomposites are widely used especially due to their superior properties and competitive prices. It is expected that as the level of control of the overall morphology and associated properties increases we will see an even wider commercialisation on traditional and totally novel applications. In this section we have discussed the basic principles of the percolation theory and the different types of conduction mechanisms, outlined some of the critical parameters of controlling primarily the electrical performance and we have provided some indications on the effect such conductive fillers have on the overall morphology and crystallisation of the nanocomposite. The latter becomes even more critical if we take into consideration that modern nanosized fillers offer unique potential for superior properties at low loadings (low percolation thresholds) but have a more direct impact on the morphology of the system. Furthermore we have indicated that similar systems can have totally different behaviour as the preparation methods, the chain conformation and the surface chemistry of the fillers will have a massive

<span id="page-241-0"></span>impact on the resulting nanocomposite. Obviously such wide topic cannot be exhausted in a small chapter but we hope we have provided enough information to intrigue and assist the interested reader to explore this unique class of materials even further.

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# Chapter 9 Nanodielectrics: The Role of Structure in Determining Electrical Properties

Alun S. Vaughan

# 9.1 Introduction

One of the most pressing challenges faced by the current generation is how to meet the ever-increasing global demand for energy without suffering the consequences of major climate change. The situation in developed economies is exemplified by that in the UK where, in November 2012, the Department of Energy and Climate Change (DECC) published the UK's Energy Security Strategy document. While highlighting the generalities of energy security and climate change as two critical societal issues, it also illustrated the scale of the problem. In the UK:

- Electricity usage is predicted to increase by at least 30% and potentially by 100 % by 2050, as heating and transportation become increasingly electrified.
- Massive investment will consequently be required in electricity infrastructure.
- Future electricity systems will take a very different form from the proven systems of the past, as decarbonisation targets will drive an ever greater reliance on renewable generation, coupled with interconnection of neighbouring power systems to increase resilience against the intermittent nature of many renewable energy sources.

Such changes will involve a paradigm shift in the ways in which we generate and transmit electricity.

A central element of all power systems is insulation and, consequently, the development and deployment of advanced material solutions that are capable of supporting the above plans is critical. In Western Europe, for example, a total of 1.5 Mton per annum of polymeric materials are currently used for electrical insulation, with an estimated value of ~£2bn; the 2013 UK Renewable Energy Roadmap

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indicates that between January 2010 and September 2013, DECC recorded announcements worth £31bn of private sector investment in renewable electricity generation in the UK; globally, the 2014 IEA Renewables Report indicates that global investment in new renewable power capacity was around \$250bn in 2014 alone. The technological potential and economic value of novel, high performance insulation systems are therefore enormous.

# 9.1.1 Nanotechnology

Although largely unnoticed at the time, the lecture There's Plenty of Room at the Bottom given in December 1959 at Caltech by Richard Feynman is now often cited as the birth of nanotechnology. However, in reality, mankind has unwittingly been exploiting nanostructured materials for very much longer, with notable examples being the Lycurgus Cup (~400 AD), Damascus steel and, perhaps rather more prosaically, carbon black as an additive in automotive tyres. Nevertheless, credit for the current interest in nanostructured polymer-based material systems containing nanoscale inclusions is often traced back to work conducted by Toyota in the late 1980s, which led to the concept of nanocomposites (Kojima et al. [1993\)](#page-269-0).

Many different standards and regulatory bodies have sought to define a nanomaterial, but a convenient definition derived from the 2010 European Commission Joint Research Centre report, Considerations on a Definition of Nanomaterial for Regulatory Purposes, is as follows: An intentionally manufactured material with one or more external dimensions, or an internal structure, on a scale from 1 to 100 nm, which exhibits novel properties not observed for coarser structures. This definition is informative in that it specifies a size range, considers the necessary dimensionality and introduces the concept that nanomaterials behave in unique ways which, in the case of nanocomposites, is generally associated with their enormous specific internal surface area. Consider, for example, the case of spherical metal oxide particles; if the diameter is 20  $\mu$ m, then the consequent specific surface area is about 1.2  $m^2$  g<sup>-1</sup> while, for 20 nm nanoparticles, this figure increases to  $\sim$ 1200 m<sup>2</sup> g<sup>-1</sup>. Practically, when considering nanoparticles, it is useful to consider both the quoted size and the specific surface area of the system; in the case of the MKnano silica nanopowder MKN-SiO<sub>2</sub>-015P, the average particle size and specific surface area are specified as 15 nm and 650  $m<sup>2</sup>$  $g^{-1}$ , respectively. In this case, both figures are broadly consistent but, where this is not the case, it is likely that the system contains primary nanoparticles that are agglomerated into larger structures, which can have adverse consequences.

The current interest in nanostructured dielectrics is generally attributed to John Lewis' 1994 paper, Nanometric Dielectrics (Lewis [1994](#page-269-0)), which considers dimensional effects in a dielectric that is formulated from two distinct components. For illustration, in the case of a composite containing a 10 % volume fraction of spherical particles 20 nm in diameter, the interfacial area will be  $\sim 3 \times 10^7$  m<sup>-1</sup> and the typical separation between nearest neighbour nanoparticles will be

<span id="page-247-0"></span>comparable to the nanoparticle diameter. Lewis discusses the consequences of this (Lewis [2004,](#page-269-0) Lewis [2005\)](#page-269-0), where it is suggested that interfacial effects can be considered in terms of local interactions that determine the intensity, I, of any property, such that the "extent of the interface is then defined by the change in I and will depend on the property of interest". That is, the region(s) immediately adjacent to the nanoparticle surface—so-called interphase(s)—will differ from both the matrix and nanoparticle when these are evaluated in the form of the relevant bulk material. Considering again the case of a system composed of 10 % by volume of isolated spherical nanoparticles 20 nm in diameter embedded within a continuous matrix, assuming an interphase thickness of just 5 nm, this will equate to nearly 25 % of the volume of the complete system, whereupon, the overall macroscopic properties will be reflective of this.

## 9.1.2 Nanocomposites: Scales of Structure

As in the case of other material systems, the macroscopic properties of nanocomposites are driven by their micro-/nanoscopic structure. From an electrical insulation perspective, polyethylene (PE) and epoxy resins constitute two technologically important material systems, each of which embodies in very different ways, a great deal of structural complexity. In the case of PE, the constituent molecules are the result of the inherently statistical polymerisation process, which can ultimately result in the formation of a hierarchical morphology in which different molecular fractions become segregated to specific morphological locations. In an epoxy resin, the epoxy monomer chemistry, the hardener and the stoichiometry can all be varied, to affect the network structure that evolves. In the case of nanocomposites, another layer of structural hierarchy is then overlaid upon and interacts with the inherent characteristics of the host matrix.

Figure 9.1 represents schematically the structural complexity of a nanocomposite. First, at the level of the primary nanoparticle (Fig. 9.1b), relevant



Fig. 9.1 Schematic representation of the range of structuring that may influence the behaviour of a nanodielectric: (a) aggregation; (b) nanoparticle parameters; (c) interfacial factors

structural characteristics include particle size, aspect ratio, crystallinity, bulk chemistry, defect structures, surface chemistry, surface structure and, in the case of its electrical behaviour, the density of electronic states in the interior and at the surface. Second, as introduced above, interactions between the nanoparticles and their environment may lead to a perturbation of the local structure or composition of the surrounding matrix material (Fig. [9.1c\)](#page-247-0). Finally, the range of aggregation states of the primary nanoparticles needs to be considered, together with their distribution throughout the bulk (Fig. [9.1a](#page-247-0)).

### 9.2 Nanodielectric Properties

The previous section has introduced in a general way the means by which the introduction of a filler with dimensions in the nanometric range can affect structure and, thereby, lead to novel materials with combinations of properties that are exhibited by neither of the constituents in isolation. In power engineering applications, the technological objective of this is to produce materials with, in addition to improved electrical characteristics, improved mechanical performance, increased thermal conductivity, enhanced thermal endurance, etc. In general, the technological motivation behind nanodielectrics research is to facilitate the design of power plant with reduced footprints, which can operate at higher power densities. The relative importance of these various electrical, mechanical and thermal factors will depend upon the particular application, but improving electrical characteristics alone is rarely sufficient.

As far as dielectrics are concerned, electrical behaviour can be grossly divided into surface properties and bulk properties and these two areas will be briefly discussed in the following sections. While nanodielectrics have exhibited clear promise in both of these domains, our understanding of the fundamental physics and chemistry that underlie the effects that have been reported is, however, often poor.

# 9.2.1 Surface Electrical Properties of Nanodielectrics

#### 9.2.1.1 Resistance to Corona and Surface Discharges

An increasingly common application area for polymeric dielectrics is as outdoor insulation; that is, on overhead lines or as outdoor bushings. In such circumstances, corona activity and surface discharges can occur, which will progressively degrade the material. Similar processes also occur in large electrical machines. As such, the ability of a dielectric to withstand surface discharge activity is technologically important and considerable efforts have been devoted to formulating materials with improved characteristics. Although corona and surface discharge effects have been evaluated in nanocomposites based upon a range of different base polymers, the technological importance of epoxy resins and silicones has meant that these systems have attracted particular attention.

The effect of nano-alumina on the ability of an epoxy resin to resist surface discharge activity was reported by Anglhuber and Kindersberger [\(2012](#page-268-0)). In this study, the nanofiller loading level was varied and the material damage was evaluated by surface profiling. Although damage was found to be substantially reduced by adding 1.5 % of the nanofiller, no further improvements were seen on increasing the amount of nano-alumina present. This work highlights a common theme in nanodielectrics, namely, that while the addition of a small quantity of nanofiller can be beneficial, in general, increasing this beyond a critical level either leads to no further benefits or, as described below, can have detrimental consequences.

From a practical viewpoint, it is not possible to optimise the performance of a material system with respect to just its electrical performance—other factors also need to be considered. In the case of high voltage bushings, for example, the coefficient of thermal expansion (CTE) is of critical importance and, ideally, the insulation and the conductor materials would exhibit the same CTE. To approach this position, significant quantities of an appropriate inorganic filler (e.g. silica) are commonly added to epoxy resins, which has led to the concept of nano/microcomposites. In one study (Iyer et al. [2012\)](#page-269-0), the corona resistance of an epoxy resin containing 65 % microsilica plus 2.5–5 % nano-silica was compared with the same base resin containing either 2.5 % nano-silica or 65 % micrometric silica alone; the nano/micro-composite was found to out-perform both of the other systems. Elsewhere, the beneficial effects of adding  $\sim$  1 % of an organically modified nanoclay to an epoxy resin heavily filled with silica have been reported, where it was concluded that the nanofiller "substantially improved the surface performance and was capable of resisting the degrading effects associated with partial discharges" (Fréchette et al. [2008](#page-268-0)). The beneficial consequence of adding nanofillers are not limited to epoxies, similar effects have been reported in silicones. In one study by Raetzke and Kindersberger [\(2010](#page-270-0)), a range of silicone rubbers containing a hydrophilic precipitated nano-silica (nominal particle size 20 nm) was subjected to a number of different surface arcing and erosion protocols. In this study, optimal performance was seen in systems containing 2–5 % of nano-silica.

#### 9.2.1.2 Degradation of Nanocomposites: Mechanisms

The empirical evidence demonstrating that surface erosion by electrical activity is reduced when a very small volume fraction of a nanofiller is present seems clear. However, understanding of the underlying mechanisms is less secure and suggestions include changes in the structure of the matrix polymer (Kozako et al. [2004\)](#page-269-0), the existence of interphases that are in some way inherently resistant (Raetzke and Kindersberger [2010\)](#page-270-0), barrier effects resulting from the close proximity of neighbouring nanoparticles in well-dispersed systems (Venkatesulu and Thomas [2010\)](#page-270-0) and increased bulk thermal conductivity (Ramirez et al. [2010](#page-270-0)).

Electrical activity adjacent at a polymer/gas interface can affect the solid through a multitude of different processes but, essentially, these will either be thermally driven or a consequence of aggressive chemical species generated in electrically active regions. As such, the mechanisms will have much in common with thermal degradation, thermo-oxidative degradation and chemical degradation. A topic where the chemistry of polymer degradation and the effect on this of included nanoparticles has been studied extensively is in connection with flammability and this would seem to have some parallels with the evidence presented above. While numerous factors have been found to influence the thermal stability and flammability of nanocomposites, in general, the beneficial consequences of adding a nanofiller to a polymer are ascribed to two different processes, one physical and one chemical.

The physical effect is related to the formation of a surface barrier layer due to local accumulation of the nanofiller as a consequence of ablation of the polymer. This layer will be rich in the inorganic components of the system, will consequently be thermally stable and will also act to reduce heat transfer into the underlying material. In the case of combustion, its presence will also limit diffusion of degradation products from the polymer to feed the flame. The chemical effect is ascribed to the nanofiller acting to promote the formation of solid rather than gaseous decomposition products (the so-called char), which will then act in the same way as the physical barrier described above. In this latter case, impurity atoms are believed to play an important role (Kashiwagi et al. [2002](#page-269-0)).

Many experimental studies of the influence of nanofillers on degradation have been conducted, which support these concepts. Saccani et al. [\(2007](#page-270-0)) investigated the degradation of polypropylene (PP) containing an organically modified layered silicate by Thermogravimetric Analysis (TGA) and showed that nanocomposites exhibited superior performance. Elsewhere, an increase in thermal stability of more than  $50^{\circ}$ C was reported for PP containing an organically modified montmorillonite (MMT) compared with the unfilled polymer (Zanetti et al. [2001](#page-270-0)); this study is also significant in that it highlights the importance of competing reactions relating to chain scission and cross-linking, where the latter leads to char formation. Indeed, Drozdov ([2007\)](#page-268-0) described a combined experimental and theoretical analysis of the degradation of PP/carbon nanotube (CNT) nanocomposites, which indicated that the inclusion of the nanofiller led to the following: an increase in the activation energy for thermal degradation; a reduction in the rate of chain scission due to reduced permeation of oxygen into the system; a reduction in the rate of detachment of side-groups as a consequence of reduced mobility of chain segments in the vicinity of CNTs and reduced mass transport of decomposition products out of the system. Elsewhere (Ramirez-Vargas et al. [2012\)](#page-270-0), a study of the effects of both aluminium hydroxide (ATH) and MMT on the flammability of systems based upon blends of a low density polyethylene (LDPE) and an ethylene-(vinyl acetate) copolymer (EVA) concluded that the enhanced performance of systems containing increased MMT contents should be attributed to the MMT promoting the formation of inorganic residues.

It is reasonable to state that, where surface electrical properties are concerned, the vast bulk of the published literature is consistent and indicates that the addition of even a very small quantity  $(\sim 1\%)$  of a nanofiller can significantly improve the performance of polymers. Although different authors have ascribed these effects to different mechanisms, examination of the broader literature provides credible mechanisms, which have a structural origin and are largely associated with a good dispersion of the nanofiller combined with the consequent close proximity of the nanoparticles and the polymer.

# 9.2.2 Bulk Electrical Properties of Nanodielectrics

The complete topic of the bulk electrical performance of nanodielectrics includes a very wide range of phenomena and properties and, consequently, a comprehensive discussion of this is not possible here. Rather, just two areas are considered below, since these well illustrate the major issues associated with the bulk characteristics of nanocomposites in dielectric applications.

#### 9.2.2.1 Breakdown Strength

A fundamental requirement of electrical insulation is an ability to withstand the applied electric field and a number of different approaches can be used to evaluate this. From a practical perspective, the important criterion is that the material system is able to withstand the applied electric field for the lifetime of the item concerned, but a comprehensive evaluation of this is time consuming, particularly in view of the statistical nature of breakdown. Consequently, a commonly used alternative is to measure the breakdown strength of a material by progressively increasing the applied field until breakdown occurs, repeating this a number of times (10–20 repeats would be typical) and, then, by assuming an appropriate statistical distribution, deriving the required quantities. Conventionally, the statistical analysis of breakdown data assumes a two parameter Weibull distribution (Weibull [1951\)](#page-270-0), whereupon, the parameters of interest are the scale parameter (comparable to the mean in the normal distribution), the shape parameter (conveys information about the spread of the data and, hence, serves a similar function to the normal distribution's standard deviation) plus associated confidence bounds. However, the data that are generated are highly dependent on the chosen experimental protocol and are affected by the rate of increase of the applied field, the sample thickness, the immersion medium, the electrode geometry, etc. Consequently, while the approach is useful in providing relative performance metrics for different material formulations when tested under strictly identical conditions, it is not possible to compare absolute values reported by different authors.

Figure [9.2](#page-252-0) presents DC breakdown data (Andritsch [2010\)](#page-268-0) that clearly demonstrate the reason for the current interest in using nanocomposites as high




performance dielectric materials. These data were derived from epoxy-based systems containing  $10\%$  of boron nitride (BN), where the size of the BN particles was varied as shown. In this study, all the systems containing BN exhibited increased breakdown strength compared with the unfilled resin and, the smaller the particle size, the greater the increase. Numerous other examples can be found in the literature for the beneficial consequences of adding nanofillers. For example, Okuzumi et al. [\(2008\)](#page-270-0) considered the effect of nano-magnesium oxide (MgO) on the breakdown strength of PP and reported an increase in DC breakdown strength of about one-third. Elsewhere, the addition of  $5\%$  hydrophobic fumed nano-silica to PP was reported to increase the DC breakdown strength from 511 to 778 kV mm<sup> $-1$ </sup> (Takala et al. [2010\)](#page-270-0).

The relationships between nanofiller/polymer compatibility and breakdown strength have been studied extensively in connection with many particulate filled systems, where silane chemistry can be used to substitute hydroxyl functionality with other moieties that would be expected to interact more favourably with the matrix material. In an early study of this type, the electrical response of a range of cross-linked polyethylene (XLPE) systems containing  $5\%$  silica (SiO<sub>2</sub>) was com-pared (Roy et al. [2005\)](#page-270-0). As is commonly reported, the inclusion of  $5\%$  of micronsized filler markedly reduced the breakdown strength relative to that of the unfilled XLPE. The performance of the unfilled XLPE and the XLPE containing untreated nano-silica was, however, equivalent, while the inclusion of 5 % of nano-silica in which the surface chemistry had been modified through treatment with a vinylsilane resulted in increased strength compared with the unfilled polymer. In a subsequent study by the same group (Roy et al. [2007](#page-270-0)), the effect of different silanes on the DC breakdown behaviour of a range of different nanocomposites containing 5 %

nano-silica was reported. While, simplistically, it is not unreasonable to suppose that replacing hydroxyl surface groups with moieties such as alkyl chains could lead to improved compatibility between the nanofiller and PE, in this later study, enhanced performance was seen in a system containing a nano-silica that had been functionalised with N-(2-aminoethyl) 3-aminopropyl-trimethoxysilane (AEAPS), a relatively polar species. This point is discussed further in Sect. [9.3.2](#page-261-0) below.

As discussed in the review by Li et al.  $(2010)$  $(2010)$ , if the addition of a small fraction of nanofiller leads to an increase in breakdown strength then, beyond a certain point, this trend is reversed, presumably, as a consequence of increased nanofiller aggregation, which dominates any other factors. Then, the agglomerated nanoparticles behave, effectively, as micron-sized inclusions, the presence of which leads to a reduction in breakdown strength (Roy et al. [2005;](#page-270-0) Vaughan et al. [2006\)](#page-270-0). This result is consistent with studies in which inclusion of various types were added to polymers (Morshuis et al. [1988\)](#page-269-0), which showed empirically that the presence of sizeable particles degrades breakdown performance.

The studies considered above show that adding a small volume faction of nanoparticles to a polymer can lead to improved breakdown performance. This conclusion is, however, not universal. Hong et al. [\(2003](#page-269-0)), for example, reported on the effect of zinc oxide (ZnO) on the DC breakdown strength of LDPE. This work considered a wide range of different loading levels and compared both microscopic and nanoscopic ZnO. A monotonic decrease in strength with increasing filler loading was reported in both cases. Ma et al.  $(2005)$  $(2005)$  reported a decrease of DC breakdown strength approaching  $40\%$  when titania (TiO<sub>2</sub>) nanoparticles were added to LDPE. This reduction in strength could, however, be reduced to about 10 % by drying the  $TiO<sub>2</sub>$  nanoparticles. Nevertheless, reacting the nano-TiO<sub>2</sub> with AEAPS—the very same silane that was reported to lead to beneficial effects elsewhere (Roy et al. [2007\)](#page-270-0)—resulted in a decrease in breakdown strength compared with the dried, but unfunctionalised nanofiller.

From the brief account given above, it is clear that published reports on the effect of nanoparticles on the breakdown strength of polymers differ widely. This diversity in behaviour, which is in marked contrast to the consistent picture described in Sect. [9.2.1](#page-248-0) in connection with surface electrical performance, suggests that the linkages between material formulation, material structure and breakdown performance are complex and are reliant on factors that are not routinely considered, or at least, not routinely reported.

#### 9.2.2.2 Permittivity

The dielectric response of a material can be represented in terms of the frequency dependence of the permittivity. Permittivity is the macroscopic manifestation of the polarisability of the material constituents, as exemplified by the Claussius–Mossotti equation:

$$
\alpha = \frac{3\varepsilon_0 M}{N_A \rho} \cdot \frac{(\varepsilon_r - 1)}{(\varepsilon_r + 2)}
$$

In this, M is the molecular mass,  $\rho$  is density,  $N_A$  is Avogadro's number,  $\varepsilon_0$  is the permittivity of free space,  $\varepsilon_r$  is the relative permittivity/dielectric constant and  $\alpha$  is the molecular polarisability. For a full discussion of the dielectric behaviour of polymer-based materials, reference to the excellent works by Kremer [\(2003](#page-269-0)) and Jonscher [\(1983](#page-269-0)) is highly recommended. Nevertheless, simplistically, permittivity can be thought of in terms of the number and nature of the polarisable species present in the system, plus their dynamics. Since the dielectric response of a given moiety is affected by its environment, dielectric spectroscopy can provide local structural information. In practice, the relative permittivity of a material is a complex quantity:

$$
\varepsilon_{\rm r}=\varepsilon_{\rm r}^{'}+i\varepsilon_{\rm r}^{''}
$$

where  $\epsilon_{\rm r}$  is the real part of the relative permittivity, which is related to the energy stored in the system,  $\varepsilon_{\rm r}^{''}$  is the imaginary part of the relative permittivity, which is related to the energy dissipated by the material, and the loss angle,  $\delta$ , is expressed:

$$
\tan \delta = \frac{\varepsilon_{\rm r}^{\prime\prime}}{\varepsilon_{\rm r}^{\prime}}
$$

For the sake of brevity, henceforth,  $\vec{e_r}, \vec{e_r}$  and tan  $\delta$  will, in general, be referred to as the real permittivity, the imaginary permittivity and the loss, respectively. In the following discussion, the real permittivity will first be considered, before moving on to consider the imaginary permittivity/dielectric loss.

In the case of a multi-component system such as a nanodielectric, an effective medium approach can be used to define the real permittivity of the whole based upon the composition and the properties of the individual components; Myroshnychenko and Brosseau [\(2005](#page-270-0)) provide a good overview of the topic, as applied to binary systems. The Lichtenecker–Rother equation is an example of such a relationship:

$$
\log \epsilon_{\rm c}^{'} = \phi_{\rm p} \log \epsilon_{\rm p}^{'} + \phi_{\rm m} \log \epsilon_{\rm m}^{'}
$$

where  $\varepsilon_{\rm c}'$ ,  $\varepsilon_{\rm p}'$  and  $\varepsilon_{\rm m}'$  represent the real permittivity of the composite, particles and matrix and  $\phi_p$  and  $\phi_m$  represent the volume fraction of particles and matrix, respectively. While the underlying physical models may vary, the resultant mathematics all share the common feature that the range of possible values is bounded by the real permittivity of each of the two components. Nevertheless, in the case of nanodielectrics, many experimental studies have reported a form of behaviour that differs markedly for this.

Kochetov et al. [\(2012](#page-269-0)) described the dielectric response of a range of nanodielectrics based upon particulate nanofillers dispersed within an epoxy matrix. In all cases, with the exception of nano-silica, the inclusion of a low volume fraction  $\langle 5\% \rangle$  of nanofiller resulted in a reduction in the measured real permittivity, below that of the host matrix, despite  $\epsilon_p > \epsilon_m$ . In another epoxy-based system, the addition of  $5\%$  of MMT led to a reduction in the real permittivity from ~4.6 to a value around 4.3 (Tagam et al. [2008\)](#page-270-0). In thermoplastics, a study of the dielectric response of LDPE-based nanocomposites containing  $5\%$  SiO<sub>2</sub> revealed evidence of a reduction in the permittivity of the nanocomposite to a value lower than that of the base polymer (Roy et al. [2005\)](#page-270-0). Hui et al. [\(2010](#page-269-0)) also considered nanocomposites based upon nano-silica but, in this case, in an EVA matrix; a reduction in permittivity from 3.27 to 3.09 on adding of 5 % of the filler was reported. Elsewhere, a reduction in permittivity from 3.27 to 2.26 was seen in a series of polyimide/silica systems on increasing the percentage of nanofiller from 0.06 to 5.58 % (Srisuwan et al. [2010](#page-270-0)). Representative data of this form are shown in Fig. 9.3.

Imaginary permittivity data provide a complementary picture of the processes that occur in nanodielectrics and can be particularly informative in probing local interactions; epoxy resins constitute ideal systems for study by dielectric spectroscopy, because of the presence of polar groups that can couple with the applied field. Figure [9.4](#page-256-0) shows imaginary permittivity data obtained from a range of epoxy/nanosilica systems. The data shown in Fig. [9.4a](#page-256-0) were obtained at different temperatures from a single system, in which the nano-silica was thoroughly dried but, otherwise, used as supplied. In this figure, a number of distinct processes can be seen. At low



<span id="page-256-0"></span>



temperatures and high frequencies (arrow at  $~5 \times 10^4$  Hz), the β-relaxation can be seen, which is associated with the hydroxyether groups in the polymer backbone (Kosmidou et al. [2012](#page-269-0)). Two other processes are evident, which are most easily seen in the data obtained at 100 °C. These are related to the  $\alpha$ -relaxation (i.e. the glass transition—arrow at  $\sim 2 \times 10^3$  Hz) and, at low frequencies, a progressive increase in  $\varepsilon$ <sup>*u*</sup> with decreasing frequency, which is primarily associated with electrical conduction as a result of residual chloride ions in the resin (Hammerton [1997\)](#page-268-0). In Fig. 9.4b, all data were obtained at a fixed temperature (60  $\degree$ C), but in this case, the surface chemistry of the nano-silica was varied by treating it with different quantities of 3-glycidyloxypropyl)trimethoxysilane (GLYMO). From these data sets, it is evident that surface functionalisation has a marked effect on the α-relaxation. While a detailed interpretation of this is complicated by differences in behaviour between the DSC glass transition and the dielectric α-relaxation, these

results nevertheless indicate that changes in nanoparticle surface chemistry do affect local interactions and local structure and that these effects can manifest themselves as changes in bulk properties.

In the case of polymers such as PE and PP, the non-polar nature of the molecule implies that any observed dielectric relaxation effects are either associated with the nano-filler itself, or else, the polymer/nano-filler interface/interphase. In one study of PP containing nano-silica, an invariant dielectric loss was reported at intermediate frequencies, together a marked increase in loss at low frequencies in the nanocomposite containing unfunctionalised nano-silica. This behaviour was interpreted in terms of some quasi-DC conduction process. Zhang and Stevens [\(2008](#page-270-0)) contrasted the dielectric response of nanocomposites  $(0-10\% \text{ nano-Al}_2\text{O}_3)$ based upon linear low density polyethylene- (LLDPE) and an epoxy resin. Although a complete analysis is not presented, the paper does nevertheless highlight the potential impact of absorbed water at nanoparticle interfaces on the dielectric spectrum. While absorbed water generally has unwanted consequences, it can however be used as a sensitive dielectric probe of nanoparticle interface structures. Indeed, Lau et al. ([2013\)](#page-269-0), compared the dielectric response of a range of systems based upon blends of high density polyethylene (HDPE) and LDPE, containing nano-silicas with different surface chemistries, as a function of their exposure time to water. This work showed that the quantity of water accumulated at the nano-silica/polymer interface and its dynamics were both markedly affected by substitution of surface hydroxyl groups with propyl moieties. The implication of this is that changes in the nanoparticle surface chemistry affect the interfacial structure which, in this case, manifests itself in its ability to accommodate water molecules.

#### 9.2.3 Nanoparticles as Structural Modifiers

The primary aim of the preceding sections has been to illustrate the impact that introducing nanoparticles can have on properties. Effective medium theories, of the type described above, are widely used in materials science to estimate a given property,  $P$ , of a composite system C composed of materials  $A$  and  $B$ ; in general, limiting values are given as follows:

$$
\left(\frac{\phi_A}{P_A} + \frac{\phi_B}{P_B}\right)^{-1} < P_C < \phi_A P_A + \phi_B P_B
$$

Applying such concepts to the real permittivity data described above, it is evident that this inequality does not hold. This suggests that the situation in nanodielectrics is more complex, which implies that the presence of the nanoparticles is affecting the overall performance of the system in a much more subtle and complex way.

In the case of breakdown, an immediate issue that needs to be addressed is the potential effect of the nanoparticles on the structure of the matrix polymer, as highlighted by Hoyos et al. ([2008\)](#page-269-0), who concluded that, in systems based upon LDPE containing silicate fillers, the final dielectric performance is determined by both the inorganic particles and the semi-crystalline morphology. In PP, in particular, increasing the nucleation density will reduce the spherulite size which, in itself, can lead to markedly increased breakdown strength (Kolesov [1980](#page-269-0)). This could explain the dramatic beneficial effects reported by some workers on adding nanofillers to PP (Okuzumi et al. [2008;](#page-270-0) Takala et al. [2010\)](#page-270-0). Although most studies of nanodielectrics have not sought to consider morphological effects in detail, the influence of the added nanofiller on both matrix morphology and breakdown was studied explicitly by Vaughan and co-workers (Vaughan et al. [2006;](#page-270-0) Green et al. [2008\)](#page-268-0) in systems based upon a polyethylene blend containing organically modified MMT. In the case of systems containing MMT derived from the pre-compounded masterbatch Nanoblend 2101 (PolyOne Corporation), the addition of the MMT was found to have little effect on the morphology of the matrix but to lead to an increase in breakdown strength from 143 to 171 kV  $mm^{-1}$  on adding 10 % of the MMT. However, when the same experiments were undertaken using a different masterbatch (Nanocor C30PE), the MMT was found to nucleate the polymer strongly and to impede crystallite evolution, such that reduced overall levels of matrix crystallinity resulted. Although reduced spherulite size would normally be expected to increase the breakdown strength as a consequence of reduced segregation of low molar mass and defective species to spherulite boundaries coupled with reduced specific volume effects, in this case, no improvement in breakdown strength was seen, even when the MMT was well dispersed (see Fig. 9.5). The difference between Nanoblend 2101 and Nanocor C30PE concerns that organic compatibiliser used in the two systems; in the former case it is dimethyl-di(hydrogenated tallow) quaternary amine while the latter contains octadecyl ammonium cations. Elsewhere (Lau et al. [2013](#page-269-0)), the addition of nanosilica to an HDPE/LDPE blend was also shown to have a strong nucleating effect on

Fig. 9.5 Scanning electron micrograph showing the disordered, highly nucleated structure of a polyethylene blend containing  $\sim$  5% of MMT modified using octadecyl ammonium cations. Scale bar: 2 μm



the polymer but, in this case, the presence of the nanofiller did not appear to affect crystal growth and its nucleating ability appeared largely independent of surface chemistry. Evidently, nanofillers can have a major effect on both the matrix morphology and the electrical properties of the resulting nanocomposites, but these factors are not simply linked.

In terms of the real permittivity, the anomalous reduction in this parameter on addition of a low volume fraction  $\langle \langle 5\% \rangle$  of a high permittivity nanofiller can be interpreted in terms of local interactions between the nanofiller and the epoxy serving to immobilise a region of the matrix immediately adjacent to the nanoparticle surface. In such circumstances, the presence of a third component (i.e. an interphase region where the nanoparticles serve to modify the structure and/or dynamics of the matrix) is commonly invoked, such that the Lichtenecker–Rother equation given above should be rewritten.

$$
\log \vec{e_c} = \phi_p \log \vec{e_p} + \phi_i \log \vec{e_i} + \phi_m \log \vec{e_m}
$$

Here, the additional term involves the real permittivity  $(\epsilon_i)$  and volume fraction  $(\phi_i)$ of the interphase. Although this provides a qualitative structural interpretation of the data, it is not without its problems, as illustrated by the finite element simulation work of Maity et al. ([2010\)](#page-269-0), where it is necessary to assume an unrealistically large interphase thickness of about 200 nm in order quantitatively to reproduce the experimental data. Studies of nitroxide spin-labelled poly(methyl acrylate) containing a synthetic fluoromica suggested a rigid interface region that is just 5–15 nm in thickness (Miwa et al. [2008\)](#page-269-0).

#### 9.3 Theories and Models

A number of different hypotheses have been proposed to account for the structure and consequent properties of nanocomposites, but the dominant concept relates to nanoparticle/matrix interactions. This topic is briefly reviewed below in connection with two issues: nanoparticle dispersion; the formation of structurally distinct interphase regions near nanoparticle surfaces.

#### 9.3.1 Miscibility and Dispersion

Nanocomposites equate to a distribution of nanoparticles within a continuous phase and, consequently, share certain features with colloids, where a range of factors influence the structure of the system. These include: excluded volume effects that are related to the direct interactions between hard particles; where particle surfaces are covered with long chain molecules, additional steric repulsive forces will also

exist that are related to local molecular conformations; thermodynamic interactions between the discrete particles and the continuous phase. Finally, in colloids, the particles will generally be charged, which results in the attraction of oppositely charged ions to form an electric double layer, in which the charge density diminishes to zero far from the interface and where the system as a whole is not charged. This structure is termed the Helmholtz–Stern–Gouy–Chapman double layer and is often discussed in terms of the associated zeta potential, which corresponds to the potential at the hydrodynamic slip plane surrounding the charged particle. The zeta potential is an important parameter, since it is often related to the stability of the system. Indeed, a common assumption is that if the zeta potential exceeds about 25 mV, then flocculation is suppressed. However, in view of the range of different interactions that will exist between nanoparticles and their environment, a more generally valid equivalent is to consider the potential energy of particles as a function of their separation. For example, in the case of lyophobic particles, adsorption of lyophilic polymer can act to promote or suppress flocculation, depending on the degree of surface coating. If this is low, then it is possible for a single chain to become adsorbed onto adjacent particles, thereby inducing aggregation. Conversely, if the degree of surface coverage is high, then steric interchain effects will dominate, such that, as neighbouring particles approach, molecular conformations will be perturbed and the particles will be repelled. The concepts of lyophilic and lyophobic are related to enthalpic interactions between the particles and their environment and, as such, this involves comparable physics to that which governs polymer solubility.

In discussing the concept of miscibility of a binary system in the most general terms, for the two components to mix intimately:

$$
G_{12} < G_1 + G_2
$$

where  $G_{12}$  is the Gibbs free energy of the mixed system and  $G_1$  and  $G_2$  represent the Gibbs free energies of the individual components. Alternatively, at a given temperature, T, this can be expressed:

$$
\Delta G_{\rm m}=G_{12}-(G_1+G_2)=\Delta H_{\rm m}-T\Delta S_{\rm m}
$$

where  $\Delta H_{\text{m}}$  is the enthalpy of mixing and  $\Delta S_{\text{m}}$  is the entropy of mixing; provided  $\Delta G_{\rm m}$  < 0, mixing/dissolution will be favoured thermodynamically. In the case of polymer solutions, enthalpic effects are known to dominate and comparable effects are likely to pertain in nanocomposites. Consequently, the topic of surface interaction and nanoparticle dispersion has been considered by a number of workers. Xue et al.  $(2015)$  $(2015)$ , applied coarse grained molecular dynamics (MD) techniques to study molecular conformations in systems based upon polydisperse polymer chains grafted onto nanoparticles. This work adjusted a number of system variables including grafted chain length, grafted chain polydispersity, graft density and nanoparticle size and computed the effect of such parameters on the average radius of gyration of the grafted chains, the average thickness of the film of grafted chains,

<span id="page-261-0"></span>etc. From this, the authors concluded that enhanced excluded volume interactions occur for larger nanoparticles (reduced curvature) under conditions when the grafted chain polydispersity is low and the grafting density is high. Liu et al. ([2011\)](#page-269-0), considered aggregation effects in a non-specific polymer-based nanocomposite and, initially, focused on the effect of varying the nanoparticle/ matrix interactions on the nanoparticle dispersion, as defined by the radial distribution function (RDF). Unsurprisingly, when the nanoparticle/polymer interactions were low ( $\varepsilon_{\rm np}$  < 1), the simulation led to a peak in the RDF corresponding to direct contact of filler particles while, for  $\varepsilon_{np} > 2$ , specific peaks in the RDF were reported which suggested a morphology based upon agglomerates in which the nanoparticles were separated from one another by intervening layers of polymer. Interestingly, in a system corresponding to intermediate nanoparticle/matrix interactions ( $\varepsilon_{np}$  = 2), no strong peaks were observed in the RDF, suggesting a high degree of nanoparticle dispersion. The investigation then examined the effect of grafted chains on the behaviour of the system and showed that, even in the absence of favourable nanoparticle/matrix interactions, this strategy could prevent direct contact aggregation.

#### 9.3.2 Interfaces and Interphases

It is generally accepted that Lewis ([1994\)](#page-269-0) first discussed the concept of nanometric dielectrics and introduced the notion of interphases whereby, as filler particle decreases in size, so the specific surface area increases and the total interphase volume progressively increases, as discussed in Sect. [9.1.1.](#page-246-0)

The most detailed hypothesis of this type is the so-called multi-core model, proposed by Tanaka et al. ([2005\)](#page-270-0), which explicitly proposes four local factors. In this, a thin layer of material of the order of 1 nm in thickness immediately adjacent to the nanoparticle surface is thought to be tightly bonded to both the inorganic and organic components, as a consequence of the presence of a suitable coupling agent. Adjacent to the bonded layer is a so-called bound layer (thickness <10 nm), which is composed of a region consisting of polymer chains that are strongly bound and/or strongly interacting with the first layer and/or the surface of the nanoparticle. In this region, chain mobility may be restricted. Also, if the interactions that occur in the bonded and bound layers result in the nanoparticle surface acting to nucleate a semi-crystalline polymer, the overall morphology of the matrix will be altered while, in the case of thermosetting polymers, the presence of reactive moieties will affect the local stoichiometry and, consequently, the network architecture. The final structural element is seen as a region of material that is loosely coupled to the bound, second layer, in which the chain conformations, chain mobility, free volume, crystallinity, stoichiometry, etc., may all differ from that in the unperturbed matrix. Finally, superimposed upon these structurally distinct regions, it is argued that an electric double layer may exist, as in the colloid case described above. A necessary requirement for this is that the nanoparticles are charged, which seems

very reasonable, but also that the polymer contains sufficient mobile charge carriers to form an equivalent of the Helmholtz–Stern–Gouy–Chapman double layer.

While the existence of interphases as a consequence of nanoparticle/matrix interactions is eminently reasonable, compelling experimental evidence for these equating to a significant volume fraction of the system remains scarce. As such, it is worth considering other ways in which the presence of interfaces can directly affect the properties of a system. The concept of effective medium theories has been discussed above in Sects. [9.2.2](#page-249-0) and [9.2.3,](#page-251-0) primarily, in connection with the dielectric response of a system. Progelhof et al. [\(1976](#page-270-0)), however, have described a multitude of such approaches in connection with the thermal conductivity of mixed systems. Since the dissipation of heat is important in many applications, it is tempting to suggest that the thermal conduction of a polymer can be improved simply by introducing a filler with a high thermal conductivity. However, heat transfer in a disordered dielectric should be considered in terms of phonons that move through the system and undergo frequent scattering, whereupon, the phonon mean free path between scattering events is affected by a combination of phonon/ phonon scattering and geometrical scattering from structural irregularities in the material (Berman [1976](#page-268-0)). As such, internal boundaries within a system can have a major effect on thermal conductivity and can be represented in terms of an interfacial thermal resistance, such that heat transfer through a multicomponent system can be very much less efficient than effective medium theories would suggest.

Electrically, the effect of micro-particles, nanoparticles and nanoparticle surface chemistry on the electrical characteristics of systems based upon XLPE and silica has been reported by Roy et al. [\(2007](#page-270-0)). In the systems considered here, it is noteworthy that the nanocomposite containing nano-silica functionalised with AEAPS was characterised by a breakdown strength that was significantly higher than that of the unfilled polymer (see Sect. [9.2.2\)](#page-249-0), despite the fact that is difficult to see how the introduction of polar functionality could lead to enhanced dispersion. However, by conducting an Arrhenius analysis of thermally stimulated current (TSC) data, these workers were able to estimate the depth of the charge carrier traps in their various systems and, from this, they showed the nanocomposite containing the AEAPS-functionalised nano-silica exhibited evidence for the formation of novel trap sites, which the authors ascribed to the polar nature of the surface moieties. That is, the electrical behaviour of nanocomposites may not only be affected by interphases and dispersion effects, but that the local density of interfacial states and the effect of these on charge transport dynamics may also be of great importance.

#### 9.3.3 From Composition to Properties

The preceding sections have considered a wide range of processes by which the addition of nanoparticles to a polymer matrix can affect the structure and, consequently, the properties of the resulting material. In the case of flammability, for example, the mechanisms appear relatively well understood but, in the case of the bulk dielectric response, this is not the case. Evidently, nanoparticles may change the local structure of the polymer or, where they act as nucleation sites, the morphology of the whole system. There is an undoubted need for new dielectric materials to underpin new electrical technologies but, at present, the linkages between the composition, processing, structure and many electrical properties of particulate-filled nanocomposites remain unclear. This lack of certainty and reproducibility currently constitute major impediments to the technological deployment of nanostructured systems based upon inorganic nanoparticles distributed within a polymeric host. Consequently, the following section presents an alternative and less conventional approach to the design of a nanostructured dielectric, where the underlying processes are better understood.

#### 9.4 Advanced Dielectrics Through Morphological Design

It can be argued that the lamellar nature of semi-crystalline polymers means that all such systems contain at least two phases in which at least one characteristic dimension falls into the nanometric range. This section will therefore take a less conventional approach to the topic of nanodielectrics where, here, the concept is broadened to include blend systems that have been intentionally manufactured to exhibit internal structure that are  $\lt 100$  nm in size and which, consequently, exhibit novel properties.

The influence of polymer morphology on the electrical properties of polymers has been studied for many decades. In 1980, Kolesov published a key paper on the effect of spherulite size on the breakdown strength of PE and PP. This work showed that as the spherulite size increased, so the breakdown strength decreased, until the spherulite size became commensurate with the specimen thickness, at which point, it thereafter remained constant. The implications of this are twofold: first, that breakdown is intimately linked with structural defects (spherulite boundaries in this case); second, that optimum performance would be obtained from a material containing no large scale morphological features. Figure [9.6](#page-264-0) shows a TEM micrograph of a sample of XLPE, which exhibits a morphology composed of small crystalline units that, even in their lateral extend, appear to be  $\sim$ 100 nm in size.

The weakness of spherulite boundaries in semi-crystalline polymers can be attributed to two effects. First, as spherulites evolve, the lowest molar mass fractions in the system will be rejected from the crystal melt interface and will diffuse away, such that they become concentrated where neighbouring spherulites impinge. Second, the density of crystalline structures is necessarily greater than that of the melt from which they form such that, when crystalline structures form under constant volume conditions, the last regions to solidify will tend to contain increased free volume and inbuilt mechanical stresses. Both of these factors mean that spherulite boundaries are mechanically and electrically weak.

<span id="page-264-0"></span>

Fig. 9.6 Transmission electron micrograph showing the morphology of a high voltage XLPE cable insulation system (scale bar 200 nm)

#### 9.4.1 Polyethylene Blends

By judiciously blending together different polymers and appropriately controlling subsequent morphological evolution it is, however, possible to engineer out the weakness of spherulitic boundaries; the process is shown conceptually in Fig. [9.7](#page-265-0), which is well demonstrated in the case of blends of linear (LPE) and branched (BPE) polyethylenes, where the LPE is the minority component. In PE, the crystalline unit cell means that bulky defects such as branches cannot be incorporated into crystalline structures and, therefore, these are excluded. As a consequence of this, BPE is not able to form lamellae that are as thick as in LPE and, consequently, LPE is able to crystallise at a high temperature than BPE. In the melt, the LPE and the BPE are miscible but, if the temperature is then reduced into the approximate range  $110-130$  °C, the LPE will begin to crystallise but the BPE will remain in the melt phase. Depending upon the chosen LPE crystallisation temperature, either relatively compact semi-crystalline inclusions of the linear polymer will form within the BPE melt, or else, an array of LPE lamellae will evolve to fill space. This skeleton of LPE crystals are then separated from one another by molten BPE, which acts to solvate and disperse the defective low molar mass fractions which, in a single component system, would become concentrated at spherulite boundaries. In addition, when the BPE subsequently crystallises, associated specific volume effects are also distributed throughout the bulk, with no adverse consequences.

In the above case, control of morphology depends upon three factors: the branch density in the BPE; the temperature at which the LPE component of the blend is crystallised and the fraction of LPE present in the system. Experimentally, it has been found that provided the branch density is not too high, the key features of morphological evolution are insensitive to the nature of the BPE; LDPE, Ziegler Natta LLDPE and metallocene LLDPE behave similarly (Hosier et al. [2000\)](#page-269-0).

<span id="page-265-0"></span>

Fig. 9.7 Schematic representation showing how isothermal crystallisation at an appropriate, intermediate temperature can be used to instigate a two stage crystallisation process in polyethylene blends, together with two scanning electron micrographs showing the morphology of PE blends crystallised at 124 °C (high temperature) and 115 °C (intermediate temperature)

Figure [9.8](#page-266-0) shows the effect of blend composition and crystallisation temperature on breakdown strength (Hosier et al. [1997](#page-269-0)). From this, it is evident that in the case of quenching, the composition of the blend has little effect on breakdown; within the parameter space considered here, all quenched systems exhibit the same morphology. For both isothermal data sets, the breakdown strength first drops before progressively increasing as the proportion of LPE present in the blend increases. The differences in the behaviour of the three differently crystallised sets of samples clearly demonstrates that the variations in breakdown strength shown are due to morphological effects and that by appropriately controlling morphological evolution, materials with enhanced properties can be generated. Elsewhere, alternative aspects of structure/property relationships in such blends related to their long term breakdown behaviour, mechanical properties and processing have been discussed (Dodd et al. [2003;](#page-268-0) Green et al. [2013](#page-268-0)).

<span id="page-266-0"></span>

## 9.4.2 Polypropylene Blends

An attractive extension to the above concept concerns the substitution of LPE and BPE with appropriate propylene-based grades. While this idea has a long history, as judged by the patent literature, control of morphology and hence properties, is very much more difficult in PP-blends. In such systems, the analogue of LPE is an isotactic polypropylene (iPP) homopolymer and the analogue of BPE is a propylene-based copolymer. However, molecular packing in the PP unit cell means that inclusion of defects occurs much more readily than in PE and, consequently, it is much more difficult to control morphological evolution in such systems, such that the desired combination of properties ultimately results. The effect of molecular architecture and composition on the morphology and electrical and mechanical properties of binary blends derived from six propylene-based systems was reported by Hosier et al. ([2011\)](#page-269-0). This work set out to develop materials systems that would be characterised by high breakdown strength, low temperature flexibility and good high temperature mechanical integrity. Mechanically, effective medium mixing rules suggest that the required temperature dependence of the modulus can be obtained by combining a relatively stiff iPP homopolymer with a low crystallinity, and therefore softer, copolymer. Then, the copolymer provides the low temperature flexibility while the isotactic homopolymer provides the required high temperature mechanical integrity. However, to achieve desirable electrical performance it is necessary to eliminate distinct spherulite boundaries and to limit phase separation in order to prevent the formation of distinct inclusions rich in the low crystallinity copolymer. Figure 9.9 shows two examples of propylene-based blend morphologies; in Fig. 9.9a, the homopolymer and copolymer undergo neither liquid/liquid nor liquid/solid phase separation such that, even though the majority propyleneethylene copolymer is unable to crystallise at the chosen crystallisation temperature (130 °C), a fine scale space-filling spherulitic morphology results. In Fig. 9.9b, the appearance is totally dominated by phase separation effects that result in distinct inclusions rich in the propylene-ethylene copolymer  $\sim$ 10  $\mu$ m in size. It is noteworthy that, in these examples, the system that phase separates contains a copolymer with a very much lower ethylene content than the system that exhibits the

Fig. 9.9 Scanning electron micrographs showing two very different morphologies in homopolymer/copolymer blends: (a) pronounced spherulites are evident (scale bar 50  $\mu$ m); (b) the morphology is dominated by phase separation (scale bar 50 μm)



<span id="page-268-0"></span>continuous, non-phase separated morphology, which suggests that it is not the gross composition of the copolymer that is important in morphological evolution but, rather, the precise sequences of co-monomers within the backbone.

#### 9.5 Summary

Nanodielectrics undoubtedly remain one of the "hot topics" in dielectrics research. However, despite the  $20+$  years that have passed since the concept was first introduced, they still remain an enigmatic concept, with many inconsistent and contradictory results being derived from different studies that, apparently, involve very similar systems. Consequently, at present, our understanding of why property enhancements come about and how to achieve them reliably and reproducibly is poor. As such, if these materials are ever to migrate from the research laboratory into our electrical infrastructure, then there is a clear need to develop a better understanding of the key structure/property relationships, suitable techniques for material characterisation and reliable bulk processing routes that will guarantee reliably products. The alternative is to design new materials through polymer blending and, while this strategy is far from simple, the underlying principles appear, at present, to be far better understood.

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# Chapter 10 Block Copolymers and Photonic Band Gap **Materials**

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#### 10.1 Introduction

As discussed in Chap. [1,](http://dx.doi.org/10.1007/978-3-319-39322-3_1) in general, chemically different polymers do not mix well, particularly as the molecular length of chains is increased. This is largely as a consequence of the unfavourable entropy of mixing. Block copolymers are materials which consist of two or more polymer chains covalently bonded together in a single chain. In a similar way to polymer blends the two blocks may phase separate but the process is substantially different from the phase separation of polymer blends both in terms of the nature of the transitions involved (Liebler [1980\)](#page-292-0) but largely because, by virtue of their chemical connectivity, the macroscopic separation of the blocks is not possible and structures are developed on length scales between 5 and 500 nm; furthermore, the phase separation of the blocks gives rise to periodic structures with arrangements which depend on the nature of the polymer and the size of the blocks (Hamley [2004\)](#page-291-0). Thus such materials offer the potential for a "bottom up" approach to the construction of structures on sub-micrometre scales. Block copolymers have a wide range of uses, and some examples are shown in Table [10.1](#page-272-0). However, the ability to produce repeating structure on these length scales has particularly attracted interest in their use as photonic band gap materials (Urbas et al. [1999;](#page-293-0) Fink et al. [1999\)](#page-291-0) (and more recently phononic band gap materials (Lee et al. [2014\)](#page-292-0)), and it is this area that forms the basis of this contribution. In this chapter we discuss the origin of photonic band gaps, the synthesis of block copolymers, the connections between chemical structure and the large scale

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Properties	Applications	Examples
Dimensional stability, recovery compres- sion set, and utility at high and low temperatures	Mechanical goods like flexible couplings, O-rings, seals, gas- kets, and extruded hydraulic and industrial hoses	<b>Brenner</b> et al. (1972)
Low dielectric constants and dissipation factor levels	Electrical and electronic goods like wire and cable insulation and transformer encapsulation	Djiauw and Icenogle (1986)
These materials can be applied either via solution or melt and subsequently develop high strength and recovery characteristics	Sealants, caulks, and adhesives	Crossland and Harlan (1975)
Melt processability, good elastomeric properties, high dynamic coefficient of friction, and excellent abrasion resistance	Footwear industry	Kraton Perfor- mance and Inc. (2015)
Block copolymers can contain a high vol- ume fraction of a hard block and a minor concentration of a soft block	Toughened thermoplastic resins	Statz et al. $(2004)$
Block copolymers having one hydropho- bic and one hydrophilic segment can be used as surfactants	Emulsification of aqueous and non-aqueous components, wet- ting of substrate surfaces and foam stabilisation	Riess (1999)

<span id="page-272-0"></span>Table 10.1 Exemplar properties and commercial applications of some block copolymers

structures, and the limitations and alternatives to these materials particularly with regard to their interactions with different wavelengths of light.

## 10.1.1 Phase Behaviour of Block Copolymers

Block copolymers (BCPs) are defined as a class of macromolecules that are produced by joining two or more chemically distinct polymer blocks containing a series of identical monomer units, which may be thermodynamically incompatible. Well-defined block copolymers will have impeccable block integrity and near perfect sequential architecture. These properties are a direct consequence of the limited number of intersegment linkage sites allowed in the block copolymers synthesised. As a result it is possible to predict the properties of the material precisely and use it with greater confidence. Block copolymers with many different molecular architectures have been prepared and some common examples are shown in Fig. [10.1.](#page-273-0)

The sequential arrangement of polymers can vary from the simplest AB structures, containing two segments only, to ABA block copolymers with three segments, ABC, with three different blocks through to multi-block  $(AB)$ <sub>n</sub> systems possessing many segments such as those found in some polyurethane block copolymers (Davis and Mitchell [2008](#page-291-0)). Various chemical coupling strategies permit the synthesis of branched architectures such as those shown in Fig. [10.1](#page-273-0); a more detailed description of some of the synthetic routes to such materials is given below in Sect. [10.3.](#page-279-0)

<span id="page-273-0"></span>

Fig. 10.1 Nomenclature for linear and branched block copolymer architectures of diblock and triblock systems

AB and ABA copolymers typically give rise to four different microphase structures, namely lamellae, double gyroid, cylinders, and spheres and, as described in Chap. [1](http://dx.doi.org/10.1007/978-3-319-39322-3_1), these phases are relatively well understood and their presence are predicted by self-consistent mean field theory (Matsen [1994,](#page-292-0) [1996\)](#page-292-0). The introduction of an additional block as in an ABC type systems opens up the possibility of many more phase structures by self-assembly (segregation) of the blocks (Bates and Fredrickson [1999\)](#page-291-0). The number of structures observed is further increased by the presence of non-equilibrium metastable states which can be formed in conditions of rapid solidification, by, for example, thermal quenching, precipitation, or solvent casting; but therein lies a problem, in that the formation of these states (though potentially of interest) cannot be predicted and may depend on preparation conditions. Furthermore, the presence of such states may compete with the formation of the more predictable equilibrium states. In addition high viscosities are not particularly helpful in terms of the development of equilibrium structures and this is particularly a problem where the formation of photonic band gaps of longer wavelengths is desired, since this requires the formation of rather high molecular weight polymers (*vide infra*) and the development of particular structure is likely to be extremely slow.

In the absence of kinetic effects the variability of phase structure provides a promising route to the control of self-assembly. The main factors that control the phase behaviour have been described by a number of authors (for example, Bates

et al. [2012](#page-291-0); Stefik et al. [2015](#page-293-0); Yoon et al. [2005\)](#page-293-0) and in principle the phase behaviour can be related to the fractions of the various blocks and the interaction parameters between the chemically dissimilar blocks. For an AB diblock system, for example, the entropy of mixing the two different polymer blocks is small (and decreases with increasing molecular weight) and the interaction parameter  $\gamma_{AB}$  which describes the (generally unfavourable) energy differences which arise as a result of mixing of even only slightly dissimilar blocks determines the phase behaviour.<sup>1</sup> Positive values for  $\chi_{AB}$  indicate a drive towards phase separation, while a negative value suggests a drive towards mixing the two components. Typical values are positive and less than unity. As the contribution to the free energy of mixing is largely enthalpic (vide supra), the value for  $\chi_{AB}$  should decrease with temperature; however, this is not always the case, for example, polystyrene and poly(methyl methacrylate) have an interaction parameter that is largely independent of temperature suggesting a substantial entropic contribution to the parameter (Russell et al. [1990\)](#page-292-0).

The properties of block copolymers are unique in that some of their properties resemble those of homogeneous random copolymers and others of simple physical blends. Block copolymers display multiple thermal transitions, such as glass transitions  $(T_{\sigma})$  and/or crystalline melting points  $(T_{\rm m})$  characteristic of each of the components. This behaviour resembles that of physical blends; however, they also show a high degree of transparency and good balance of mechanical properties, which are typical of homogeneous random polymers. This versatility renders block copolymers suitable for many diverse applications. Aside from photonic band gap materials (*vide infra*) block copolymers are particularly well known as thermoplastic elastomers. Such materials have hard/rigid blocks separated by soft flexible blocks, which phase separated and behave as a cross-linked material, with the rigid phase acting as the cross-link points. These materials behave as typical elastomers in that they can be stretched, and will return to their original shape when the stress is released; however, unlike simple elastomers such as vulcanised rubber they can be processed, for example, as a melt at elevated temperature, when the rigid part is heated above the glass transition temperature or melting point. The most common of these include styrene block copolymers and polyurethanes. Styrenic block copolymers include the well-known Kraton<sup>®</sup> family, initially developed by Shell in the 1950s; these are generally triblock copolymers with styrene blocks surrounding a soft central block formed from butadiene, isoprene, or related materials. Polyurethane thermoplastic elastomers include the ubiquitous Spandex® (also known as Lycra® or Elastane®) originally developed by Du Pont in the 1950s. This consists of a segmented polymer containing a soft block consisting of a polyol [such as poly(tetrahydrofuran)] and a hard block from MDI  $(4,4'-diisocyanatophenylmethane)$  [I] and an amine such as ethylenediamine.

Table [10.1](#page-272-0) summarises some common applications of block copolymers along with the properties which make them suitable for that particular application

 $1$  Interestingly even protonated and deuterated polystyrene has been found to be incompatible at sufficiently high molecular weights (Bates et al. [1985](#page-291-0)).



#### 10.2 Photonic Band Gap Materials

The concept of the Photonic Band Gap (PBG) was proposed independently by Yablonovitch ([1987\)](#page-293-0) and John [\(1987](#page-292-0)). A Photonic Crystal (PC) is any material which exhibits a photonic band gap (vide infra) and is therefore able to reflect certain wavelengths of electromagnetic radiation as propagation through it is prohibited.<sup>2</sup>

The structure of any photonic crystal is based upon a regular arrangement of materials of alternating dielectric constant. Any incident waves are reflected by the periodic structure and a band gap will arise if these reflected waves, working in phase with one another, cancel with the incident wave and thus do not allow its propagation through the crystal (Yablonovitch [2001](#page-293-0)). In many respects, photonic crystal investigations are biomimetic in that they copy well-known phenomena found in nature and scale it to serve the application required (Saito et al. [2006;](#page-293-0) Starkey [2005](#page-293-0)). Thus, photonic crystals are often characterised by strong colours and there are numerous examples in nature. A spectacular example of this phenomenon is provided by the wings of certain butterflies (Christensen [2002](#page-291-0); Vukisic et al. [1999](#page-293-0), [2000\)](#page-293-0) in particular those of the genus morpho (Fig. 10.2). Here the distinct colours of the butterfly are probably used as a defence mechanism against predatory attack or as an intraspecies method of communication (Forsman and Merilaita [2003\)](#page-291-0). Unfortunately (for the butterfly) the beautiful iridescence has made this particular genus historically extremely attractive to lepidopterists.

Fig. 10.2 Example of a morpho butterfly; the blue colour arises from the regular arrangement of scales on the wing



<sup>&</sup>lt;sup>2</sup> This differs from the reflections observed from a standard mirror which relates to conductivity of the mirror's tain (highly polished, reflective metal coating) and the abundance of mobile electrons; the electrons respond to an applied electromagnetic field by generating an equal and opposite electromagnetic field of their own, hence reflection is observed.

The interest in photonic crystals has grown significantly since Yablonovitch built the first photonic crystal structure which operated in the microwave regime and, because of the long wavelength, could be built by conventional machining. The action of electromagnetic repulsion/reflection, independent of the frequency at which it occurs, is due to the dielectric materials that make up the crystal and the periodicity (the regular arrangement of materials of alternating dielectric constant). It is these factors that result in the formation of a useful band gap. The width of this band gap [usually expressed either in hertz (Hz) or in electron volts (eV)] depends on the geometry, feature size, spacing, and the materials that make up the crystal.

A photonic band gap covers a range of frequencies where any photon incident on the crystal will be reflected rather than transmitted. The simplest analogy is that of a mirror, as a mirror reflects light that is incident on it. However, while a mirror demonstrates the concept of reflection perfectly, the microscopic behaviour inside a photonic crystal is somewhat more complicated and is described in more detail later in this section.

Just as any periodic structure has dimensionality, so do photonic crystals. Thus, photonic crystals can be 1, 2, or 3-dimensional in terms of their mode of operation. This dimensionality reflects the periodicity which is relevant to the desired optical properties, thus a simple layered structure will show properties in one dimension only (i.e. if light is perpendicular to the surface) whereas a regular 3-dimensional lattice will be dependent on the lattice parameters.

A photonic crystal may consist of a simple square lattice of dielectric cylinders (Fig. 10.3a) but equally, it is also possible to have a square lattice with cylinders consisting of air in a medium of dielectric material (Fig. 10.3b). Both lattices will display a photonic band gap but all other factors being equal, these will not be centred at the same frequency, or as wide as each other. Lattices that make up photonic crystals may be square, cubic, hexagonal, or tetragonal to name a few. Equally the features within the lattices may be cylinders, squares, rectangles, hexagons, or more complex arrays (Liguda et al. [2001](#page-292-0); Xia et al. [1999;](#page-293-0) Yang [2000;](#page-293-0) Ozin [2001\)](#page-292-0).



Fig. 10.3 An example of the periodic structure that may be seen in 2-dimensional photonic crystals



Fig. 10.4 Schematic diagram for determining Bragg's Law

The interaction of electromagnetic radiation with a photonic crystal can be explained in part as a problem in diffraction using Bragg's Law, as seen in Fig. 10.4. Figure 10.4 illustrates schematically the interference observed between waves scattering from adjacent rows of atoms in a crystal lattice. The overall effect of scattering from a row is akin to partial reflection from a mirror aligned with the row, and hence the angle of reflection is equal to the angle of incidence for each row. Interference then occurs between the waves reflecting from different rows of atoms in the crystal. For the two adjacent rows shown in Fig. 10.4, simple geometry determines that the path difference between beams is  $2d \sin \theta$  which is in turn twice the distance  $h$ . For constructive interference  $h$  must be an integer number of wavelengths (where the integer is called the order of interference); from this, simple trigonometry gives Bragg's Law of Diffraction (10.1).

$$
n\lambda = 2d \sin \theta \quad \text{where} \quad n = 1, 2, 3 \dots \quad \text{(Bragg's Law)} \tag{10.1}
$$

The principles for reflection from two layers can be extended to a plane wave incident on a periodic structure such as the first row of cylinders in a 2-dimensional photonic crystal as shown in Fig. [10.5a.](#page-278-0) As a normal wave is incident on the structure it may diffract and scatter, but it will also split into forward and reflected waves. As the forward wave continues into the crystal it encounters more obstacles (i.e. periods of alternating dielectric constant) that cause more diffraction, scattering, and forward and reflected waves. Thus as a consequence of the periodic spacing of the cylinders there may be destructive interference between the reflected waves inside the crystal and the incident wave; this occurs if the reflected waves are in phase with each other. The net result is a photonic band gap, ensuring that the

<span id="page-278-0"></span>

Fig. 10.5 (a) A wave incident on a photonic band gap material partially reflects off each layer of the structure. The reflected waves are in phase with each other and destructively interfere with the incident wave to produce a standing wave that does not propagate through the material. Where there is no destructive interference  $(b)$  the wave is propagated (Yablonovitch  $2001$ )

incident wave cannot propagate through the crystal. This does not occur if the wavelength is not in the band gap (Fig. 10.5b).

A crucial factor in the development of photonic band gap materials is the contrast between the two media in terms of their refractive indices. Ideally there should be a large difference in refractive index as the contrast controls reflection through a variety of mechanisms, e.g. total internal reflection and birefringence; without this contrast there will be nothing to distinguish the two layers and the interface would be invisible (refractive index matching). The wavelength of the band gap is then determined by the spacing and refractive indices of the structure (Zhao et al. [2009\)](#page-293-0). In general the wavelength of the band gap is determined by the size of the blocks which should be  $\lambda/4n$  where n is the refractive index of the block material (Yoon et al. [2005](#page-293-0)). The refractive index difference will affect the width of the gap, and will determine the number of layers required to reduce transmission to zero and greater contrast will increase the width of the band gap. This is particularly important when considering applications involving organic polymer systems, as refractive index differences tend to be rather small (Stefik et al. [2015](#page-293-0)), though this difference may be enhanced by the incorporation of inorganic materials (Bockstaller et al. [2001](#page-291-0)).

Photonic crystals have considerable potential for applications (Stefik et al. [2015](#page-293-0)) and have been used widely as the active components in many commercial devices such as optical notch filters (Dowling [1998](#page-291-0)), dielectric mirrors/optical resonance cavities (Painter et al. [1999\)](#page-292-0), and Bragg gratings (on optical fibres) (Vengsarkar [1996\)](#page-293-0). Photonic crystal fibres provide a route to fibre optic materials and contrast with Bragg filters in terms of the directionality of the periodicity (Russell [2003\)](#page-292-0). Photonic crystals are designed and fabricated to work at a certain frequency, namely the central or mid-band frequency. The range of frequencies around the central frequency over which the crystal is able to operate defines the operational bandwidth of the crystal. Once outside this operation range the photonic band gap nature is no longer seen for that particular photonic crystal.

<span id="page-279-0"></span>The means of fabrication of photonic crystals are linked directly to the operational band gap sought. Synthetic photonic crystals may be fabricated by many varied methods. Saado et al. ([2001\)](#page-293-0) has demonstrated an array of magnetic particles which are able to self-assemble to form ordered 2D and 3D structures, whereby the lattice parameter may be controlled by an external magnetic field, which exhibit tuneable and non-tuneable microwave and millimetre-wave photonic band gaps. Busch and John [\(1999](#page-291-0)) have also demonstrated a tuneable photonic band gap material using liquid crystals. An inverse opal structure is generated by the infiltration of silicon into the air voids of an artificial opal and the template opal structure is etched away to reveal the inverse-opal. An optically birefringent nematic liquid is infiltrated into the voids of the inverse-opal photonic crystal and the tuneable light localisation effects are realised by controlling the orientational disorder in the nematic. Similarly Zhou et al. [\(2001](#page-293-0)) prepared a thermally tuneable photonic crystal from a  $SiO<sub>2</sub>$  colloid crystal prepared by self-assembly and in filled with BaTiO<sub>3</sub>. The bare silica colloid crystal shows a dip in transmittance at approximately 570 nm but an in-filled colloid crystal at 400 and 600  $^{\circ}\mathrm{C}$  shows broadening of the dip and also a shift to longer wavelength. Metallic crystals also present a novel route to photonic band gap structures as they can possess a large band gap whilst new electromagnetic phenomena and high temperature applications may be explored. An all metallic three-dimensional photonic crystal featuring a large infrared band gap has been prepared by using chemical vapour deposited (CVD) tungsten to back-fill a polysilicon/ $SiO<sub>2</sub>$  structure from which the silicon has been selectively removed (Flemming et al. [2002\)](#page-291-0).

## 10.3 Synthesis of Block Copolymers

Block copolymers may be synthesised by various methods but two of the common techniques are anionic polymerisation and atom transfer radical polymerisation (ATRP). Living anionic polymerisation, a technique which has been used widely since the 1950s, is now a well-established way of making block copolymers for photonic band gap applications. The first publication and introduction of the term "living polymer" was in 1956 (Szwarc et al. 1956). The work described the making of block copolymers, based on the fact that aromatic hydrocarbons reacted with metallic sodium in suitable solvents yielding coloured and soluble complexes with a composition 1 Na to 1 hydrocarbon which in turn initiated polymerisation of conjugated olefinic hydrocarbons. Paul et al. ([1956\)](#page-292-0) showed them to be composed of negative aromatic hydrocarbon ions and Na ions and that they acted as electron transfer agents as shown in Scheme [10.1](#page-280-0).

Szwarc et al. postulated that the same type of electron-transfer process was responsible for the initiation of polymerisation by a sodium–naphthalene complex. The monomer anions formed may be represented by (Ia) and (Ib) in Scheme [10.2](#page-280-0), and if an excess of monomer is present, polymerisation will proceed with one end growing as a radical and the other as a carbanion. After the addition of the first

<span id="page-280-0"></span>

Scheme 10.2 Initial observed reactions of

naphthalene complex



monomer unit to either (Ia) or (Ib) a true separation of electrons takes place and species such as  $(II)$  in Scheme 10.2 are formed; however, the radical ends have a short lifetime even at low temperature, and they dimerise to form dianions [species (III) in Scheme 10.2]. The experimental details given showed that the characteristic green colour of the sodium–naphthalene complex was immediately replaced by a deep red colour on addition of styrene, due to the styrene ends. At the end of the reaction the red colour persisted indicating that termination had not occurred. Thus, if an additional amount of styrene was added after the initial monomer was converted entirely to polymer, a further increase in molecular weight was observed. If, however, a different monomer was added in place of the second portion of styrene, the living polymerisation still proceed, but in this case, yielding block copolymers of various compositions.

Significant studies have been carried out in the field of living anionic polymerisation over the last 50 years (Uhrig and Mays [2005](#page-293-0); Franta et al. [2007;](#page-291-0) Baskaran and Müller [2007\)](#page-291-0). The "living" anionic polymerisation technique employs anions rather than radicals to propagate the reaction. Alkyllithiums are the initiator used most commonly for this technique. The reaction proceeds in homogeneous solutions in hydrocarbon solvents but it is essential that all active hydrogen impurities (water, alcohols, etc.) be excluded in order to obtain a termination free system. The anionic active chain ends exist primarily in the form of ion pairs when hydrocarbons are used as polymerisation solvents. Polar solvents, such as ethers, result in the appearance of free ion species and reaction rates increase greatly. As there is no



Scheme 10.4 Living anionic polymerisation of styrene and isoprene

unintentional termination, block length, which is dependent only upon the monomer/initiator ratio, is easily controllable and the absence of termination affords an extremely monodisperse polymer sample. A general reaction mechanism is given in Scheme 10.3.

One of the first block copolymer to exhibit a photonic band gap was a styrene isoprene block copolymer. This was prepared by anionic polymerisation using butyllithium as an initiator; the mechanistic details for the copolymerisation of styrene and isoprene are given in Scheme 10.4. Some anionic polymerisations can be undertaken with basic laboratory equipment provided sufficient care is taken (Aragrag et al. [2004](#page-291-0)). For the formation of photonic band gap materials however, the molecular weights for each block need to be of the order of 200,000; as the number average degree of polymerisation  $(X_n)$  is given by the ratio of monomer  $(M)$ to initiator  $(I)$  concentrations  $(10.2)$  $(10.2)$  $(10.2)$  the production of the required molecular weight will only be possible with very low initiator concentrations. This places particularly high demands on technique as it will be particularly susceptible to termination of the propagating polymer chain or initiator (Hadjichristidis et al. [2000\)](#page-291-0). For this reason the reactants require extensive purification to remove all traces of water and any other impurities; additionally traces of oxygen must be removed. The preparation requires the highly competent use of well-established

<span id="page-282-0"></span>vacuum line techniques (Morton [1983](#page-292-0)) utilising an ultra-high vacuum line, breakseal technology and advanced glassblowing techniques, thus this polymerisation requires a vacuum line equipped with dual pumps; a roughing pump able to evacuate the system to between  $1 \times 10^{-2}$  and  $1 \times 10^{-3}$  Torr and typically a water-cooled silicone oil diffusion pump, which when connected sequentially with the first pump evacuates the system to  $1 \times 10^{-6}$  Torr.

$$
X_n = [M]/[I] \tag{10.2}
$$

Using the conditions described above it is possible to produce high molecular block copolymers containing styrene and isoprene. In a typical procedure, degassed styrene was purified by distillation from CaH2 across a vacuum line into a graduated measuring cylinder containing dibutyl magnesium (DBuMg) and the styrene/ DBuMg solution was stirred at room temperature for approximately 1 h until a pale straw colour had developed. The correct volume of styrene required for the reaction was distilled from DBuMg solution into the reactor directly. After ensuring that the reactor was frozen in liquid nitrogen, approximately 500 mL of pre-dried benzene was distilled into the reactor. The mixture was thawed and polymerisation initiated by rupturing the break-seal of an ampoule of sec-butyllithium attached directly to the reactor vessel. An instantaneous colour change from colourless to a light yellow colour was observed. After 24 h isoprene was added to the system through a reactor sidearm. The reaction was allowed to proceed for a further 24 h to ensure complete reaction of the monomer although a noticeable change in viscosity was evident after only 3 h. The reaction was terminated using degassed methanol. The polymer was precipitated directly into cold methanol containing 2,6-di-tertbutylated-methylphenol (butylated hydroxytoluene, BHT). The precipitated polymer was dried under vacuum for 48 h. The <sup>1</sup>H NMR spectrum of this polymer is shown in Fig. [10.6](#page-283-0); this reveals the composition of the block copolymer to be 40.59 mol% polystyrene to 59.41 mol% polyisoprene (cf. 39.56 mol% styrene to 60.44 mol% isoprene monomer feed ratio). The isoprene polymerised by 1,4-, and 1,2- addition in the ratio; 1,4-, 92.64 %: 1,2-, 7.36 %. In the example shown the molecular weight of the polymer was found to be 750,000 with a polydispersity of 1.21. The polymer was found to be a white solid, but when in solution in toluene showed a vivid blue iridescence indicative of its photonic band gap properties as shown in Fig. [10.7](#page-283-0) (Castiglione [2008\)](#page-291-0).

Although anionic polymerisation remains an important technique today for the preparation of block copolymers and other controlled polymer architecture, recent developments in controlled free-radical polymerisation has presented an alternative approach which may complement this methodology.

Atom radical transfer polymerisation (ATRP) has its roots in atom transfer radical addition (ATRA), which involves the formation of 1:1 adducts of alkyl halides and alkenes, and is also catalysed by transition metal complexes. ATRP is a modification of the Kharasch addition reaction (Kharasch et al. [1945](#page-292-0)) although there may be some differences (Minisci [1975\)](#page-292-0). A general mechanism for ATRP is shown in Scheme [10.5](#page-284-0). In ATRP the radicals or the active species are generated through a reversible redox process catalysed by a transition metal complex (Mtn-L/

<span id="page-283-0"></span>

Fig. 10.6 NMR spectrum of a high molecular weight block copolymer of styrene and isoprene produced by anionic polymerisation



Fig. 10.7 High molecular weight styrene-b-isoprene copolymer (a) as a solid (b) swollen in toluene

Ligand, where L may be another ligand or the counter ion) which undergoes a one-electron oxidation with abstraction of a (pseudo) halogen atom, X, from a dormant species, P-X. This process occurs in a manner similar to a conventional radical polymerisation.

Termination reactions also occur in ATRP, mainly through radical coupling and disproportionation, however, unlike free-radical processes, in a well-controlled ATRP, less than a few percent of the polymer chains undergo termination.

<span id="page-284-0"></span>

Scheme 10.5 General mechanism for ATRP

Although other side reactions may additionally limit molecular weights yields and the homogeneity of the products (Fischer [1999](#page-291-0)), typically no more than  $5\%$  of the total growing polymer chains terminate during the initial, short, non-stationary stage of the polymerisation. A successful ATRP requires both a small contribution of terminated chains and uniform growth of all chains. This is a result of fast initiation and rapid reversible deactivation. Polymers obtained by ATRP have a narrow molecular weight distribution and the degree of polymerisation can be controlled accurately (Hayes and Rannard [2004](#page-292-0)).

Using ATRP block copolymers can be prepared fairly readily and with some degree of complexity. For example, a commercially available difunctional initiator, dimethyl 2,6-dibromoheptanedioate (DMDBHD [II]), has been used to initiate ATRP of *tert*-butyl acrylate and styrene; in this case the presence of two bromines allows the formation of a tri-block copolymer, with either styrene or tert-butyl acrylate units acting as the central block, depending on the order of addition of the monomers. Figure [10.8](#page-285-0) shows the NMR spectrum of a styrene-b-tert-butyl acylateb-styrene triblock copolymer. In this case freshly distilled from calcium hydride and deoxygenated, *tert*-butylacrylate was added to degassed CuBr with DMDBHD being the initiator. After the addition of *tert*-butylacrylate, the ligand PMDETA was added to the mixture and the solution was stirred at 60  $^{\circ} \mathrm{C}$  for a further 6 h. After 3 h the green solution started becoming viscous. The polymer was dissolved in acetone and flushed through a layer of neutral aluminium oxide. Precipitation produced the desired difunctionalised poly(tert-butylacrylate) as a white solid. This difunctionalised polymer was then further polymerised with styrene in a similar matter to produce the desired triblock copolymer (Aragrag 2010).



As inspection of Fig. [10.8](#page-285-0) shows the polymer produced is relatively pure, there is a small peak at 3.6 ppm which may reflect the presence of the initiator residue in the central block. The detection of this in the NMR is testament to a lower molecular weight than the anionic polymer described above and GPC measurements showed a

<span id="page-285-0"></span>

Fig. 10.8 NMR spectrum of a medium molecular weight copolymer of styrene and tert-butyl acrylate produced by ATRP

molecular weight of ca. 11,000 with a polydispersity of 1.55. In general this reflects a problem with atom transfer processes in terms of producing very high molecular weight materials. Thus although Matyjaszewski has been able to produce a very high molecular weight polystyrene under certain conditions (Mueller et al. [2011;](#page-292-0) Jakubowski et al. [2008\)](#page-292-0), in general such polymerisations are subject to a number of problems, in the case of styrene the initiation rate is too low and there may be thermal self-initiation (Mueller et al. [2011\)](#page-292-0); more generally there is a problem with termination by combination/disproportionation or chain transfer to solvent as with conventional free-radical polymerisations (Simms and Cunningham [2008](#page-293-0)). To date this limitation has restricted the use of this technique in terms of producing photonic band gap materials with gaps in the visible part of the spectrum, but recent advances by Haddleton et al. has shown the potential of using Cu(0) mediated living radical polymerisation to produce high molecular weight block copolymers (Anastasaki et al.  $2013$ ). The use of the related technique RAFT (reversible addition  $-$  fragmentation chain transfer) polymerisation is also being developed to produce high molecular weight materials (Gody et al. [2014\)](#page-291-0), however, it is fair to say that in terms of organic polymer systems their potential as photonic band gap materials have been largely explored using anionic polymers.



Fig. 10.9 Reflectance (blue) and transmission (yellow) measurements of poly(styrene-b-isoprene) block copolymer with molecular weights as shown

#### 10.3.1 Characterisation of Photonic Band Gap Materials

The crucial test of a photonic band gap material is the existence of the band gap. For a material with a band gap in the visible range this can be qualitatively gauged by observation of the sample. Quantitative assessment requires the use of UV visible spectroscopy, both in transmittance and reflectance such that any components arising from electronic absorptions can be isolated. For example, Fig. 10.9 shows two poly(styrene-b-isoprene) block copolymers of differing molecular weight, the transmission spectrum of the higher molecular weight exhibited a strong trough (300–450 nm) which was also related to the observed reflection of the sample. The difference in appearance between transmission and reflection below 300 nm is due to the absorption of the polymer by virtue of the presence of the styrene chromophores.

To further establish the presence of phase separation, the polymer domains should be analysed by microscopy. In view of the sizes of the domains, this usually means electron microscopy (see Chap. [2](http://dx.doi.org/10.1007/978-3-319-39322-3_2), Sect. [2.4\)](http://dx.doi.org/10.1007/978-3-319-39322-3_2), and, Fig. [10.10](#page-287-0) shows TEM micrographs of the high molecular weight poly(styrene-b-isoprene) block copolymer described earlier. The dark areas relate to the stained polyisoprene and the light areas to the unstained polystyrene (Bockstaller et al. [2001](#page-291-0)). The polyisoprene domains range from 50 to 80 nm and the polystyrene domains range from 78 to 129 nm. The white spots (24–71 nm) which appear on the dark areas are

<span id="page-287-0"></span>

Fig. 10.10 TEM micrograph of poly(styrene-b-isoprene) cast from a 1% solution in dichloromethane. The *red scale bars* indicate  $2 \mu m$  (*left*) and  $0.5 \mu m$  (*right*)

conceivably polystyrene which phase separated quickly. It is possible that annealing the sample would enable the structure to phase separate further and become better defined (Albalak and Thomas [1993\)](#page-290-0).

#### 10.3.2 Extending to Longer Wavelengths

There is a significant desire to increase the range of photonic band gap polymers to the near infrared region, this is prompted particularly by the use of infrared light (of wavelengths around  $1.55 \mu m$ ) in optical communications, which minimises attenuation (crucial over long distances). In addition options for blocking infrared light selectively are limited. A large number of infrared reflecting pigments such as titanium dioxide are available (Bendiganavale and Malshe [2008](#page-291-0)); such materials presumably block infrared by virtue of their high refractive index rather than through absorption due to an electronic transition. Unfortunately these materials (and metallic films) tend to reflect the visible light also. Highly conjugated organic molecules that show electronic transitions in the infrared are available, some of which may show absorptions above 1000 nm (Fabian et al. [1992\)](#page-291-0); however, in most cases these show additional bands which make them highly coloured and thus partially block visible light.

Infrared reflection is an important consideration in building design. Around 45 % of the sunlight at the earth's surface is in the near infrared (NIR). This can be responsible for considerable build-up of heat within glazed structures; thus removal of infrared is an important consideration. Interestingly one of the best NIR blocking


structures in nature is provided by foliage. The cool shade of a tree is due in part to the leaves reducing the amount of NIR reaching the ground. This is not due to the pigments in the leaves, chlorophyll absorption tails off at 700 nm, but rather is due to the leaf structure as illustrated in Fig. 10.11. Thus, a typical leaf structure consists of four layers (Wuyts et al. [2010](#page-293-0)), the first layers are the epidermis (which is the layer of cells that make up the surface of the leaf) and the palisade parenchyma (which consists of a regular arrangement of elongated cells) and this is where the leaf pigments such as chlorophyll and anthocyanins are to be found. The third layer is known as the spongy parenchyma, and here irregularly shaped cells separated by air spaces are to be found. It is the third layer which is largely responsible for the scattering of infrared light and ray-tracing models have shown how this can result in reflection of a substantial amount of the light passing through the system, depending on the position of the incident light (and hence the time of day) (Jacquemoud et al. [1997](#page-292-0)). Commercial infrared reflecting films applied to windows to minimise heat build-up are generally rather more efficient (and of course allow the passage of visible light). These tend to be made up from multilayered films, which act by reflecting infrared light but not visible light. An interesting alternative has recently been described by Khandelwal et al. ([2014\)](#page-292-0) who use a cholesteric liquid crystal polymer bilayer film to produce an infrared reflective material suitable for building applications.

As the discussion above suggests, at the NIR length, scale top-down fabrication currently may be more effective than self-assembly, in many applications. However the development of larger dimension photonic band gap polymers remains an area of considerable interest. The principle challenges remain the synthetic demands of producing extremely high molecular weight polymers, the poor refractive index contrast generally available between different types of polymer block and thus increased length of the blocks required. There may be some degree of tunability, thus Fig. [10.12](#page-289-0) shows significant changes in colour from the high molecular weight

<span id="page-289-0"></span>

 $10 \text{ mg} \text{ mL}^{-1}$  $DCB*$ 



 $mL^{-1}$ 20 mg **DCB** 



 $24$  mg mL $^{-1}$ DCB



 $30 \text{ mg} \text{ mL}^{-1} \text{DCB}$ 



 $20 \text{ mg} \text{ mL}^{-1}$ **THF** 



 $10 \text{ mg } \text{mL}^{-1}$ Toluene



 $20 \text{ mg} \text{ mL}^{-1}$ Toluene



 $40 \text{ mg} \text{ mL}^{-1}$ Toluene

Fig. 10.12 High molecular weight styrene-b-isoprene copolymer (from Fig. [10.7](#page-283-0)) in different solvents at different concentrations. DCB dichlorobenzene

styrene-b-isoprene copolymer described earlier arising as a result of swelling in different solvent; in addition the polymer colour is not homogeneous and clearly this is not ideal in terms of processing for applications. However, a number of alternative approaches have been used to utilise phase separation in block copolymers to produce infrared reflecting materials; two examples are given below.

The swollen polymers in Fig. 10.12 show a level of inhomogeneity; this raises another issue with very high molecular weight polymers, namely their high viscosity arising from chain entanglements is likely to slow down the formation of equilibrium structures. Recently a team at Caltech has described block copolymer made of two similar brush copolymer segments, the only difference being a phenyl substituent on one of the brushes (Miyake et al. [2012\)](#page-292-0) as shown in Fig. [10.13.](#page-290-0) The brush configuration allows the high molecular weight required to form large domains to be achieved without significant entanglement such that NIR reflecting films can be cast directly from solution.

An alternative method to avoid the problems associated with high molecular weight materials has been described by Li et al.  $(2004)$  $(2004)$ . They used an approach where the periodicity was introduced using monodisperse silica microspheres (in this example with a diameter of 700 nm); these spheres were sintered at 950 °C. This process introduces connections between the beads and this provides channels for subsequent removal of the silica by etching. The array thus produced was used as a template and a solution of a thermoplastic elastomer in

<span id="page-290-0"></span>

Fig. 10.13 Brush copolymer system to produce NIR reflecting photonic band gap materials

dichloromethane was allowed to fill the voided space. The silica was then removed by etching with HF. This arrangement not only allows for the convenient production of larger photonic band gap wavelengths (in this case in the near infra-red), without the intrinsic time problems resulting from the viscosity of extremely high molecular weight materials, but is also tuneable, as the shape of the pores produced in the structure can be altered by stretching.

# 10.4 Conclusion

Block copolymers exhibit micro phase separation, which, in the absence of kinetic considerations, results in self-assembly to form a remarkable range of structures. Of particular interest is the potential for such structures to act as photonic band gap materials, where the passage of light is restricted by multiple reflections at the phase boundaries between the different blocks. The development of such materials has faced a number of challenges. The effectiveness of these materials relies on difference in refractive indices and these are often small for organic polymers; the preparation of high molecular weight materials can be synthetically challenging; the high molecular weights required may require significant annealing to form equilibrium phases due to the high viscosity typical of such polymers. That being said recent developments show that there is considerable potential that these materials could be developed into effective products.

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# Chapter 11 Relationship Between Molecular Configuration and Stress-Induced Phase **Transitions**

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# 11.1 Introduction

The physical and mechanical properties of semi-crystalline polymers depend on their molecular architecture, molecular mass and distribution of molecular mass which are fixed in the polymerization step (Heimenz and Lodge [2007](#page-331-0); Halary et al. [2011](#page-331-0); Billmeyer [1984](#page-330-0); Schultz [1984](#page-333-0)). Furthermore, for any molecular architecture the properties also depend on the processing conditions (Cowie and Arrighi [2008;](#page-330-0) Richardson and Lokensgard [1996;](#page-333-0) Bicerano [2002](#page-330-0)) (Fig. [11.1](#page-295-0)).

If we confine our attention to linear polymers, the molecular architecture addresses the constitution of the polymer chains, the configuration defined by the sequence of the monomeric units along the chains, presence of branches, and/or defects such as configurational defects, regio-irregularities and constitutional defects in the case of copolymers [\(IUPAC](#page-331-0) and Chap. [1](http://dx.doi.org/10.1007/978-3-319-39322-3_1)). Since the conformation and the intrinsic flexibility of the chains depend on the chain architecture, properties such as glass transition, mechanical strength and rigidity are intrinsically dependent on the chain architecture.

The crystallization properties and polymorphism are dependent on the chain architecture. In fact, chains with a regular constitution and configuration are generally able to adopt low energy conformations with a regular and periodic repetition of the monomeric units along the chain axis, and therefore, they are also more able to crystallize than less regular chains (De Rosa and Auriemma [2013\)](#page-331-0).

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Moreover, the presence of defects along the chains does not necessarily prevent crystallization, even though the degree of crystallinity, the melting temperature, the type and amount of disorder included in the crystals, crystallization kinetics and polymorphism may be strongly influenced by the defects (Wunderlich [1973\)](#page-334-0). Since the properties of a polymer depend on the kind of polymorph present in the material and the degree of disorder in the crystals, small changes in the chain microstructure produce change in the polymorphism and/or crystallization behaviour, resulting in gross changes in material properties and consequent possibility of fine tuning properties through the control of crystallization (De Rosa and Auriemma [2013](#page-331-0), Ch. 7).

On the other hand, for any given chain architecture, the final properties of a polymeric material may be also controlled by processing (Richardson and Lokensgard [1996;](#page-333-0) De Rosa et al. [2014](#page-331-0)). In fact, small variation in the variables associated with the process, including the maximum temperature achieved in the melt, application of shear forces to the melt (Ward [1997;](#page-334-0) Somani et al. [2005\)](#page-333-0), cooling rate (Zia et al. [2009;](#page-334-0) De Rosa et al. [2014;](#page-331-0) Sorrentino et al. [2007](#page-333-0)), presence of additives or nucleating agents (Menyha´rd et al. [2009](#page-332-0)), may produce large variations of the segmental dynamics, influence the polymorphism and crystallization ability, or drive a different morphology (Baird [1998\)](#page-330-0). Therefore, a tight control over the manufacturing conditions may allow tailoring the material properties directly in the processing plant, through development of the morphology (Bicerano [2002](#page-330-0)).

Polymorphic transitions between different crystalline forms can be triggered not only by thermal treatments but also by mechanical deformation (Hay and Keller [1970;](#page-331-0) Séguéla [2005;](#page-333-0) De Rosa and Auriemma [2007;](#page-330-0) Hughes et al. [1997\)](#page-331-0). In general, the deformation mechanism of semi-crystalline polymers involves complex phenomena, and the principal event consists in the transformation of an original isotropic lamellar (generally spherulitic) morphology into a fibrillar one, where polymeric chains become preferentially aligned along the drawing direction (Peterlin [1971](#page-333-0); Bowden and Young [1974](#page-330-0)). The mechanism is complex and involves a hierarchy of transformations, including block slippage within the crystalline lamellae that takes place at low deformations, followed by the stress-induced fragmentation of crystals and recrystallization into fibrils at high values of strain (Lin and Argon [1994](#page-332-0); Bowden and Young [1974;](#page-330-0) Schultz [1974\)](#page-333-0). The exact mechanism of deformation depends on the relative stability of crystals and the density of entanglements in the amorphous network (Men et al. [2003\)](#page-332-0). During the deformation, after yielding and concomitant with the breaking of lamellae, polymorphic transformations may also occur (Hay and Keller [1970](#page-331-0); Séguéla [2005](#page-333-0); De Rosa and Auriemma [2007;](#page-330-0) Hughes et al. [1997\)](#page-331-0). Transitions involving polymorphic modifications either characterized by a different conformation of the chains (conformational polymorphism) or a different packing mode, but identical chain conformation (packing polymorphism) may both be involved by effect of strain (De Rosa and Auriemma [2006,](#page-330-0) [2007,](#page-330-0) [2013](#page-331-0), Ch. 7; De Rosa et al. [2006](#page-331-0)). These phase transformations dissipate mechanical energy so that the sample breaking is prevented, and the mechanical toughness and ductility are enhanced (De Rosa and Auriemma [2012;](#page-330-0) De Rosa et al. [2013](#page-331-0), [2014\)](#page-331-0). Therefore, not only does the initial morphology of the sample play a key role in the mechanical properties, but also phase transitions are important.

In this chapter, we focus on the effect of the chain microstructure on the mechanical properties of polymers, illustrating how the presence of stereodefects in a stereoregular vinyl polymer may influence polymorphism, morphology, stressinduced phase transitions and mechanical properties in a cascade of events that reflect the hierarchy of structural organization of semi-crystalline polymers. Because of that, the transformations are also hierarchical. In particular, these effects are shown in the case of some selected samples of isotactic polypropylene (iPP) with a well-defined molecular structure that have been synthesized using single site metalorganic catalyst systems. All stretching experiments are performed at room temperature. Since the glass transition temperature of our samples is around  $-10^{\circ}$ C to  $0^{\circ}$ C (De Rosa et al. [2004,](#page-331-0) [2005;](#page-331-0) De Rosa and Auriemma [2007](#page-330-0)) the effect of the chain microstructure on the deformation behaviour at temperatures above glass transition is illustrated.

In Sect. [11.3](#page-298-0), [11.4,](#page-303-0) [11.5](#page-306-0) of this chapter we focus on the polymorphism, morphology and mechanical properties of iPP samples with different concentration of stereo-defects.

In Sect. [11.6](#page-311-0), [11.7](#page-317-0) and [11.8](#page-323-0), the results of X-ray scattering measurements at both wide and small angles recorded in situ during stretching are illustrated.

Therefore, the transformations are related to changes in the packing mode of the chains in the crystals, and those occurring at lamellar length scales. These changes are followed in real time using the high flux of X-rays available at a Synchrotron light source. It is shown how the differences in concentration of stereodefects in iPP samples may influence the critical values of strain at which a given crystalline polymorph starts or ends transforming into another crystalline form throughout the gradual destructions of the original lamellar morphology and transformation into a fibrillar morphology (De Rosa and Auriemma [2006,](#page-330-0) [2007;](#page-330-0) De Rosa et al. [2006](#page-331-0)). The effect of chain microstructure on the critical values of strain at which the original unoriented assembly of lamellae breaks and the chains become oriented in the stretching direction, up to transformation into fibrillae, is also studied. Numerical descriptors of the degree of preferred orientation at atomic and lamellar length scales are also identified. Correlations between mesoscopic phenomena such as buckling instabilities of lamellar stacks and cavitation and microscopic phenomena such as chain orientation and phase transitions are established. The critical value of strain at which changes at the atomic length scale (conformation/packing/polymorphism) occur are then correlated to those at which change at the nanometer length scale (lamellae/lamellar aggregates) occur. The aim is of establishing precise correlations on how stressinduced changes at different length scales are correlated as a function of chain microstructure.

# 11.2 Isotactic Polypropylene Samples

The development of single-centre metallocene catalysts for the polymerization of olefins has allowed to the synthesis of polyolefins in general and polypropylenes in particular with controlled chain microstructures (Resconi et al. [2000](#page-333-0)). Polypropylenes characterized by different kinds and amounts of regio- and stereoirregularities, different distributions of defects and different molecular masses can be prepared through the rational choice of the catalytic system (Resconi et al. [2000\)](#page-333-0). Exploiting the available large library of metallocene catalyst precursors, samples of iPP with different stereoregularity, characterized by only one kind of stereodefect (isolated  $rr$  triads), and containing no measurable amount of regio-errors, have been synthesized. The samples have been prepared with the complexes of Scheme [11.1](#page-298-0), activated with methylalumoxane (MAO) (Ewen [1997,](#page-331-0) [1998;](#page-331-0) Brintzinger et al. [1995](#page-330-0); Kaminsky [1996](#page-332-0), [1998](#page-332-0), [1999](#page-332-0)). The amount of rr defects depends on the structure of the catalyst, in particular the ligand substituents and the conditions of polymerization, and the amount of rr defects has been varied in the range between 0.5 and 11 mol% (Nifant'ev et al. [2004\)](#page-332-0). Correspondingly the samples show melting temperatures variable between 162 and 84  $^{\circ}$ C (Table [11.1](#page-298-0)) (De Rosa et al. [2004](#page-331-0), [2005\)](#page-331-0).

<span id="page-298-0"></span>

**Scheme 11.1** Structure of  $C_2$ -symmetric (1) and  $C_1$ -symmetric (2–5) pre-catalysts

**Table 11.1** Molecular mass  $(M_v)$ , melting temperature  $(T_m)$  and content of rr triad and mmmm pentad stereosequences of iPP samples prepared with the catalysts of Scheme 11.1<sup>a</sup>

Sample	Catalyst/ cocatalyst	$M_{\rm v}$ 10 <sup>5</sup> $(g/mol)^b$	$T_{\rm m}$ $(^{\circ}C)^{\circ}$	$\lceil mm \rceil$ mol%	$\lceil mr \rceil$ mol%	[rr] mol%	$\lceil mmm \rceil$ mol%	$x_c^{\rm d}$ $\mathscr{G}_o$	$f_{\gamma}^{\rm d}$ $(\%)$
iPP1	1/MAO	1.96	162	98.5	1.0	0.49	97.5	70	17
iPP <sub>2</sub>	2/MAO	1.06	140	92.4	5.1	2.54	87.6	66	60
iPP3	3/MAO	2.02	133	88.9	7.4	3.70	82.2	64	85
iPP4	4/MAO	2.11	114	82.2	11.8	5.92	72.2	55	96
iPP <sub>5</sub>	5/MAO	1.23	84	66.9	22.0	11.01	51.0	42	100

<sup>a</sup>No or negligible regioerrors (2,1 insertions) could be observed in the  $^{13}$ C NMR spectra of the samples (Fritze et al. [2003;](#page-331-0) Resconi et al. [2005](#page-333-0))

<sup>b</sup>From the intrinsic viscosities

<sup>c</sup>The melting temperatures were obtained with a differential scanning calorimeter Perkin Elmer DSC-7 performing scans in a flowing  $N_2$  atmosphere and heating rate of 10 °C/min (De Rosa et al.  $2005$ )

<sup>d</sup>Crystallinity index  $x_c$  and relative amount of  $\gamma$  form with respect to the  $\alpha$  form  $f_\gamma$  evaluated from X-ray diffraction profiles

# 11.3 Structural Analysis and Mechanical Properties

The X-ray powder diffraction profiles of melt-crystallized compression moulded specimens of the iPP samples of Table 11.1 are reported in Fig. [11.2a](#page-299-0). The samples crystallize from the melt as mixtures of  $\alpha$  and  $\gamma$  forms (Fig. [11.2b, c](#page-299-0), respectively),

<span id="page-299-0"></span>

Fig. 11.2 (a) X-ray powder diffraction profiles of iPP samples of Table [11.1](#page-298-0) crystallized from the melt by compression moulding and cooling the melt to room temperature at  $1 \degree C/\text{min}$  (De Rosa et al. [2004\)](#page-331-0). The  $(110)_{\alpha}$ ,  $(040)_{\alpha}$  and  $(130)_{\alpha}$  reflections of the  $\alpha$  form (Natta and Corradini [1960](#page-332-0)) at  $2\theta$  (CuK $\alpha$ ) = 14, 17 and 18.6° ( $d \approx 0.65, 0.52$  and 0.48 nm, respectively) and the (111)<sub>γ</sub>, (080)<sub>γ</sub> and (117)<sub>γ</sub> reflections of the γ form (Brückner and Meille [1989](#page-332-0)) at 2θ (CuKα) = 14, 17 and 20.1°  $(d \approx 0.65, 0.52$  and 0.44 nm) are indicated. (b, c) Limit ordered models of packing proposed for the  $\alpha$  (b) and  $\gamma$  (c) forms of iPP. The *dashed horizontal lines and dotted oblique lines* are the traces of  $(040)_{\alpha}$  and  $(110)_{\alpha}$  planes of  $\alpha$  form in (b), respectively, and  $(080)_{\gamma}$  and  $(111)_{\gamma}$ , planes of  $\gamma$  form in (c), respectively. Subscripts  $\alpha$  and  $\gamma$  identify unit cell parameters referred to the monoclinic (Natta and Corradini [1960](#page-332-0)) and orthorhombic (Brückner and Meille [1989](#page-332-0)) unit cells of  $\alpha$  and  $\gamma$ forms, respectively. ((a) redrawn from De Rosa and Auriemma [2007](#page-330-0) with permissions)

as indicated by the presence of both  $(130)_{\alpha}$  and  $(117)_{\gamma}$  reflections of  $\alpha$  (Natta and Corradini [1960\)](#page-332-0) and γ (Brückner and Meille [1989](#page-332-0)) forms, respectively, in the diffraction profiles of Fig. 11.2a. The intensity of the  $(117)$ <sub>γ</sub> reflection of the γ form at  $2\theta = 20.1^{\circ}$  increases with increasing the concentration of rr defects (De Rosa et al.  $2004$ ). The most isotactic sample crystallizes basically in the  $\alpha$ form (curve a of Fig. 11.2a), and the concentration of  $\gamma$  form of 17% is low (Table [11.1](#page-298-0)). The amount of  $\gamma$  form increases with increasing the content of rr defects up to 100 % for rr concentrations higher than 6 mol% (Table [11.1](#page-298-0)) (De Rosa et al. [2004,](#page-331-0) [2005;](#page-331-0) De Rosa and Auriemma [2007\)](#page-330-0). Finally, the crystallinity index (Table [11.1](#page-298-0)) decreases with increasing concentration of rr defects from  $\approx$  70 % for the stereoregular iPP1 sample with  $[rr] = 0.49$  mol% to  $\approx 42\%$  for the stereodefective iPP5 sample with  $[rr] = 11.0$  mol%.

The small angle X-ray scattering (SAXS) curves of the metallocene-made iPP samples are shown in Fig. [11.3a](#page-300-0). The samples have been isothermally crystallized at temperatures  $T_c$  lower than the melting temperature of Table [11.1](#page-298-0) by 40–50 °C. SAXS data were recorded at the crystallization temperature  $T_c$ , on samples first rapidly cooled to room temperature immediately after completion of crystallization process, and successive heating at  $T_c$ . The simultaneous recording of the X-ray

<span id="page-300-0"></span>

Fig. 11.3 (a) SAXS profiles of iPP samples of Table [11.1](#page-298-0) isothermally crystallized from the melt at the indicated values of temperature  $T_c$  (a) and corresponding normalized autocorrelation functions. SAXS data are recorded at  $T_c$ . Values of long spacing  $(L)$ , and thickness of crystalline  $(l_c)$  and amorphous  $(l_a = L - l_c)$  layers (c). They are evaluated from the autocorrelation function in (b) (full symbols) and also using the Bragg law for the calculation of L and successive multiplication of L times the crystallinity index (see the text) for  $l_c$  (*open symbols*)

scattering intensity in the wide angle (WAXS, data not reported) indicates that in the selected crystallization conditions the samples develop the same crystallinity index as the compression moulded films of Fig. [11.2](#page-299-0).

The Lorentz corrected SAXS profiles of all samples (Fig. 11.3a) show a single and broad correlation peak with maximum at  $q = q_{\text{peak}}$ , q being the magnitude of the scattering vector  $q = 4\pi \sin \theta/\lambda$  where  $\lambda$  is the wavelength of the incident X-ray beam and 2θ the angle between the incident and scattered beam. The broadness of the scattering peak indicates that all samples present a disordered lamellar morphology, where lamellar crystals (average thickness  $l_c$ ) alternate to amorphous layers (average thickness  $l_a$ ) with average periodicity (long spacing)  $L = l_c + l_a$ . Disorder is due to a broad distribution of both  $l_c$  and  $l_a$ .

The values of L,  $l_c$  and  $l_a$  have been evaluated either from the main-correlation triangle in the autocorrelation function (Fig. 11.3b) or with use of the Bragg law, that is  $L = 2\pi / q_{\text{peak}}$ ,  $l_c \approx L x_c$  and  $l_a = L - l_c$  where  $x_c$  is the crystallinity index obtained from WAXS analysis of Table [11.1.](#page-298-0) The values obtained are compared in Fig. 11.3c.

It is worth noting that whereas the values of the long spacing calculated with the two methods are in a good agreement within the experimental error (1–2 nm), the agreement for the values of  $l_c$  and  $l_a$  is less good. In fact the values of  $l_c$  and  $l_a$ obtained from the autocorrelation function (Fig. 11.3b) are higher and lower, respectively, than those obtained directly, especially for the less stereoregular samples iPP4 and iPP5 with rr content of 5.92 and 11.01 mol%, respectively. This is due to the fact that the correlation peak of SAXS profiles (Fig. 11.3a) is more weighted towards the well-organized stacks of lamellar crystals and the amorphous layers containing the less defective crystals. The amorphous phase located in the extralamellar regions and the defective lamellar crystals not participating in the regular stacks, instead,

<span id="page-301-0"></span>contribute to the SAXS intensity as diffuse scattering in the background and in the tail at low q values of the correlation peak. Therefore, the values of  $l_c$  extracted from the autocorrelation function correspond to the thickness of the less defective lamellar crystals in the sample forming regular (periodic) lamellar stacks, whereas the values of  $l_a$  correspond to the thickness of intralamellar amorphous layers. The direct method, instead, is based on the use of a value of the crystallinity index (amorphous fraction), that accounts for all kind of crystallites and amorphous phases, located both in the intralamellar and interlamellar regions. Therefore, the values of  $l_c$  (and  $l_a$ ) calculated by the direct method correspond to values that are averaged over both regular and irregular lamellar crystals (both intra- and inter-lamellar amorphous phase). For this reason, the largest difference in the values of  $l_c$  and  $l_a$  calculated with the two methods occur for the less stereoregular samples, the defective chains of which tend to form a major amount of defective crystals, and/or are rejected in the interlamellar amorphous regions.

The stress–strain curves of compression-moulded films of the iPP samples of Table [11.1](#page-298-0) are shown in Fig. 11.4a, b. The values of Young modulus decrease with



Fig. 11.4 (a, b) Stress–strain curves of unoriented compression moulded films of the samples in Table [11.1](#page-298-0) (De Rosa et al. [2004](#page-331-0), [2005](#page-331-0)); (c, d) Average values of Young Modulus as a function of crystallinity index (c) and relationship between the lamellar thickness  $l_c$  and the yield stress  $\sigma_y$  (d) of iPP samples with the indicated concentrations of  $rr$  stereo-defects  $((a, b)$  Reprinted from De Rosa et al. [2005](#page-331-0) with permissions)

increasing concentration of rr defects and decreasing the crystallinity (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007\)](#page-330-0) (Fig. [11.4c\)](#page-301-0). The strain at yield, instead, increases with increasing the concentration of defects from values close to 10 % deformation for the sample iPP1 with  $[rr] = 0.49$  mol%, to values close to 100% for the sample iPP5 with  $[rr] = 11.0$  mol% (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007\)](#page-330-0). Moreover, the values of yield stress tend to decrease with increasing concentration of defects (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007\)](#page-330-0), whereas they increase almost linearly with the values of the average lamellar thickness (Fig. [11.4d](#page-301-0)).

It is worth noting that a linear relationship between yield stress and lamellar thickness has been found also in other polymers as for instance in the case of isotactic polypropylene (O'Kane and Young [1995;](#page-333-0) O'Kane et al. [1995\)](#page-333-0), and random isotactic copolymers of propene with 1-hexene (De Rosa et al. [2009](#page-331-0)), polyethylene and random copolymer of polyethylene (Kennedy et al. [1994](#page-332-0), [1995;](#page-332-0) Popli and Mandelkern [1987;](#page-333-0) Crist 1989; Schrauwen et al. [2004\)](#page-333-0), and several different mechanisms have been suggested to explain such behaviour. The proportional relation of yield stress and lamellar thickness has been associated with the intrinsic complex molecular structure and morphology of semi-crystalline polymers and the most popular explanations include occurrence of partial melting and recrystallization (Kennedy et al. [1994](#page-332-0), [1995;](#page-332-0) Popli and Mandelkern [1987;](#page-333-0) Crist 1989), nucleation and propagation of screw dislocations (Young [1974](#page-334-0)), the role that thermally activated conformational (chain twist) defects play to overcome energy barriers for nucleation and propagation of dislocations (Séguéla  $2002$ ), and the intrinsic stability of the crystalline modifications that develop upon crystallization (De Rosa et al. [2009](#page-331-0)). It is clear that a definitive and general understanding of this proportionality and of the yield behaviour of semi-crystalline polymers in general has not yet been achieved (Schrauwen et al. [2004](#page-333-0)). In a recent study it has been pointed out that in order to reach such a more definitive understanding, in addition to the structural and morphological aspects, kinetic factors associated with the segmental relaxation dynamics of the polymer chains should also be included in the theory (Schrauwen et al. [2004\)](#page-333-0).

It is worth noting that in our case, the linear relationship (Fig. [11.4d\)](#page-301-0) holds only for the average values of lamellar thickness evaluated accounting for lamellar crystals included both in the well-developed and regular stacks and those embedded inside the inter-lamellar amorphous regions, and does not hold for the values of  $l_c$ deduced from the autocorrelation function (Fig. [11.3b](#page-300-0)) relative to the best developed lamellar crystals in a sample. Moreover, for the most stereo-regular samples  $iPP1$  and  $iPP2$  with rr content less than 3 mol%, presenting a more regular lamellar organization, the values of  $l_c$  present large deviations from the linear relationships holding for the less stereo-regular samples iPP3-iPP5 with rr content higher than 5 mol%. The stereo-irregular samples present a non-negligible population of irregular lamellar crystals not participating to lamellar stacks. This suggest that different mechanisms are involved at yielding in these samples, since different populations of lamellar crystals experience different stress level during the tensile deformation (Hiss et al. [1999](#page-331-0); Al-Hussein and Strobl [2002](#page-330-0); Men and Strobl [2001;](#page-332-0)

<span id="page-303-0"></span>Men et al. [2003;](#page-332-0) Hong et al. [2004a](#page-331-0), [b](#page-331-0)). In particular the presence of irregular crystals produce values of yield strength, which increase linearly with the average lamellar thickness. Instead, for samples characterized by a negligible population of irregular lamellae, the yield stress seems to level off with the lamellar thickness. In fact, since the most stereoregular samples form also ordered lamellar crystals, we argue that the relaxation mechanisms involving the chains stems in the crystals also play a role at the onset of plastic deformation (Schmidt-Rohr and Spiess [1991\)](#page-333-0). In the stereodefective samples, instead, stem relaxation in the crystals would be damped and/or prevented by a too high concentration of steric defects located at the fold-surface (De Rosa et al. [2009](#page-331-0)).

At large deformations the samples show cold drawing and values of deformation at break of  $\approx$  250–350%, for concentration of rr defects lower than 4 mol% (Fig. [11.4a\)](#page-301-0), and a strong increase of the ductility and toughness, for higher contents of rr defects (Fig. [11.4b](#page-301-0)). Therefore, samples of iPP containing low concentration of rr defects (up to  $[rr] = 3.7\%$ ) show high stiffness, coupled with relatively high ductility in spite of the high degree of crystallinity and melting temperature (Fig. [11.4a](#page-301-0)) (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007\)](#page-330-0). Samples with concentration of  $rr$  defects around 5–6 % present the behaviour typical of thermoplastic materials with a slightly lower strength but much higher deformation at break ( $\varepsilon_b \approx 1200\%$ , Fig. [11.4b\)](#page-301-0). Finally, the less crystalline and stereoregular samples, such as iPP5, with concentration of  $rr$  defects of 11 mol%, show a strong strain hardening at high deformation, and values of the tensile strength (32 MPa) (Fig. [11.4b\)](#page-301-0) higher than those of the more isotactic and crystalline samples (20–23 MPa, Fig. [11.4a](#page-301-0)) (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007\)](#page-330-0). The strain hardening of this sample may be somehow related to the fact that it presents uniform stretching behaviour, and involves crystals with low plastic resistance and therefore low cavitation (vide infra) (Pawlak and Galeski [2005\)](#page-333-0). Once crystals have experienced irreversible plastic deformations at low values of deformation, strain hardening is caused by the straightening of the entangled network (Pawlak and Galeski [2005\)](#page-333-0). It is worth to remark, that the sample iPP5 presents also large elastic recovery even at large deformations (vide infra) (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007](#page-330-0)). These elastic properties are associated with remarkable values of the modulus of nearly 20–30 MPa (Fig. [11.4c\)](#page-301-0), and also high values of tensile strength (Fig. [11.4b](#page-301-0)) (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007](#page-330-0)).

#### 11.4 Optical and Atomic Force Microscopy

Polymer films (with a thickness of 90–120 μm) have been prepared for Atomic Force Microscopy (AFM) and Optical Microscopy (OM) experiments by sandwiching a small amount of the samples in between glass cover slips, after melting at  $\approx$  200 °C and then crystallizing them at cooling rate of 10 °C/min up to room temperature. The samples crystallize in either the α or  $\gamma$  forms by slow

<span id="page-304-0"></span>

Fig. 11.5 Polarizing optical microscopy  $(a-c)$  and high resolution AFM phase  $(d-f)$  images of samples of iPP of different stereoregularity crystallized from the melt by slow cooling (10  $\degree$ C/min) to room temperature in  $\alpha$  or  $\gamma$  forms. Samples iPP1 with  $[rr] = 0.49$  mol% (a, d), iPP3 with  $[rr] =$ 3.7 mol% (b, e) and iPP5 with  $[rr] = 11$  mol% (c, f). The images (d, e) are on area of 50 μm  $\times$  50 μm, and that in (f) is 2 μm  $\times$  2 μm (Reprinted from De Rosa et al. [2014](#page-331-0) with permissions)

crystallization from the melt and develop different morphologies as shown by the POM and AFM phase images of Fig. 11.5. The different morphologies are variant of the basic lamellar morphology typical of melt crystallized iPP samples, and reflect the crystallization of different amounts of the  $\alpha$  and the  $\gamma$  forms (De Rosa et al. [2014\)](#page-331-0), as a result of the different concentration of rr defects. In particular, the micrographs of the highly isotactic sample iPP1 shows lamellae of the  $\alpha$  form and space filling spherulitic superstructure (Fig. 11.5a, d). The sample iPP3 with 3.7 mol% of  $rr$ defects crystallizes slowly from the melt mainly in the  $\gamma$  form with about 20% of crystals of  $\alpha$  form (WAXS curve c of Fig. [11.2a](#page-299-0)), and the crystalline supermolecular structure presents bundle-like entities, rather than spherulites, organized in a nearly 90 $\degree$  texture (Fig. 11.5b, e). The sample iPP5 with 11 mol % of rr defects crystallizes slowly from the melt completely in the  $\gamma$  form (WAXS curve e of Fig. [11.2a\)](#page-299-0) and the morphology has a superstructure characterized by single, elongated entities organized in a nearly  $90^\circ$  texture resulting in an interwoven morphology (Fig. 11.5c, f) (De Rosa et al. [2014](#page-331-0)). The appearance of the three different morphologies shown in Fig. 11.5 and in the corresponding X-ray diffraction profiles of Fig. [11.2](#page-299-0) indicates that, with increasing the content of the  $\gamma$  form, the morphology changes from spherulites to bundle-like and elongated entities.

These data are in agreement with early observations by Thomann et al. [\(1996](#page-334-0), [2001\)](#page-334-0) and Stocker et al. ([1993\)](#page-333-0) of the morphology of the  $\gamma$  form of iPP, and more recent TEM data by Cao et al. ([2009,](#page-330-0) [2011\)](#page-330-0), and homoepitaxial growth of lamellar branches in the  $\alpha$  and  $\gamma$  forms of iPP (Stocker et al. [1993;](#page-333-0) Compostella et al. [1962;](#page-330-0) Norton and Keller [1985;](#page-333-0) Sauer et al. [1965](#page-333-0); Khoury [1966](#page-332-0); Katayama et al. [1968;](#page-332-0) Andersen and Carr [1975](#page-330-0); Padden and Keith [1966](#page-333-0), [1973;](#page-333-0) Lovinger [1983](#page-332-0); Bassett and Olley [1984;](#page-330-0) Lotz and Wittmann [1986;](#page-332-0) Zhou et al. [2005\)](#page-334-0). In the case of the  $\alpha$  form, the homoepitaxial growth of lamellar branches corresponds to the unique crosshatched morphology of the  $\alpha$  form, which takes place upon crystallization from solution (Sauer et al. [1965](#page-333-0); Khoury [1966](#page-332-0)), melt (Norton and Keller [1985](#page-333-0)) and in fibres (Compostella et al. [1962](#page-330-0); Andersen and Carr [1975\)](#page-330-0). In particular, the crosshatched structures that develop upon crystallization from solution are so regular that they have been termed "quadrites" by Khoury (Khoury [1966\)](#page-332-0).

For the cross-hatched lamellar structure which develops in spherulites of iPP in the  $\alpha$  form (Compostella et al. [1962](#page-330-0); Norton and Keller [1985;](#page-333-0) Sauer et al. [1965;](#page-333-0) Khoury [1966](#page-332-0); Katayama et al. [1968;](#page-332-0) Andersen and Carr [1975;](#page-330-0) Padden and Keith [1966,](#page-333-0) [1973;](#page-333-0) Lovinger [1983;](#page-332-0) Bassett and Olley [1984](#page-330-0); Lotz and Wittmann [1986\)](#page-332-0), mother lamellae develop from the centre of spherulites according to the radial direction and show on the sides a dense overgrowth of daughter lamellae inclined with their long axis at an angle of  $\approx 80^\circ$  with respect to the long axis of parent lamellae, according to the self-epitaxial relationship  $c_{\alpha}$  (mother)// $a_{\alpha}$  (daughter) and  $a_{\alpha}$  (mother)//c<sub>α</sub> (daughter), with  $a_{\alpha} = 6.65$  Å and  $c_{\alpha} = 6.5$  Å the nearly identical unit cell parameters of  $\alpha$  form forming an angle of  $\beta_{\alpha} = 99.67^{\circ}$  (Scheme 11.2b) (Compostella et al. [1962](#page-330-0); Norton and Keller [1985](#page-333-0); Sauer et al. [1965;](#page-333-0) Khoury [1966;](#page-332-0) Katayama et al. [1968;](#page-332-0) Andersen and Carr [1975;](#page-330-0) Padden and Keith [1966](#page-333-0), [1973;](#page-333-0) Lovinger [1983;](#page-332-0) Bassett and Olley [1984](#page-330-0); Lotz and Wittmann [1986](#page-332-0)).

In the case of the sample iPP3 that crystallizes in mixture of  $\alpha$  and  $\gamma$  forms forming bundle-like entities (Fig.  $11.5b$ , e), the lateral structure of these entities is due to the lateral growth of the  $\gamma$  form on the mother  $\alpha$  form lamellae (Scheme 11.2c). In fact, the angle between the polymer chains in the  $\gamma$  form and

Scheme 11.2 Lamellar branching and epitaxial relationships in isotactic polypropylene (Reprinted from Auriemma and De Rosa [2006](#page-330-0) with permission)



<span id="page-306-0"></span>the angle of the daughter lamellae with respect to the mother-lamellae (homoepitaxial growth) in the  $\alpha$  form are similar ( $\approx 80^{\circ}$ ). Therefore, the key of the epitaxial growth of  $\gamma$  form on parent lamellae of  $\alpha$  form is of structural origin, and lies in the nonparallel arrangement of chain axes in crystals of the  $\gamma$  form at an angle of  $\approx 80^\circ$ , identical to the complement of angle  $\beta_\alpha$  of 99.67° of the monoclinic unit cell of iPP in the  $\alpha$  form. Even in the case of the sample iPP5 that crystallizes nearly completely in the γ form (curve e of Fig. [11.2a\)](#page-299-0), the typical lateral growth is visible, with formation of an interwoven morphology. Straight entities appear frequently arranged in an angle of about  $80^{\circ}$ -90 $^{\circ}$  to each other, that corresponds to the crosshatching in the  $\alpha$  form. This suggests that the interwoven morphology is formed by the γ form growth on crosshatched α form (Thomann et al. [1996,](#page-334-0) [2001\)](#page-334-0). Small amount of crystals of  $\alpha$  form are therefore present in the sample that show X-ray diffraction profile of the pure γ form (profile e of Fig. [11.2a\)](#page-299-0).

It is worth noting that spherulites, bundle-like and elongated needle-like crystals were obtained by Thomann et al. ([1996,](#page-334-0) [2001\)](#page-334-0) for the same sample of metallocene stereoirregular iPP by changing the temperature of isothermal crystallization from the melt and favouring the crystallization of the  $\alpha$  form (spherulites) and the  $\gamma$  form (bundle-like and elongated needle-like crystals) at low and high temperatures, respectively. In the case of Fig. [11.5](#page-304-0) these morphologies develop under the same crystallization conditions by changing the concentration of rr stereodefects, favouring the crystallization of the  $\alpha$  and the  $\gamma$  forms at low and high contents of rr defects, respectively (De Rosa et al. [2014](#page-331-0)).

These morphologies are in part responsible of the mechanical properties of iPP samples of different stereoregularity. In particular the morphology accounts for the gradual decrease of rigidity and plastic resistance of these samples with stereoirregularity, ranging from the space filling spherulitic morphology of the rigid sample iPP1 with 0.49 mol%  $rr$  defect, to the open (bundle like) spherulite morphology of the flexible sample iPP3 with 3.7 mol%  $rr$  content. Finally the outstanding mechanical properties of high ductility and flexibility of the sample iPP5 crystallized in the γ form (De Rosa et al. [2004](#page-331-0), [2005](#page-331-0); De Rosa and Auriemma [2006,](#page-330-0) [2007,](#page-330-0) [2012\)](#page-330-0) may be accounted for by the interwoven morphology created by small and elongated needle-like crystals of Fig. [11.5c](#page-304-0) that should be more easily deformable than the better developed lamellar morphology of the stereoregular samples (De Rosa et al. [2014](#page-331-0)).

# 11.5 Stress-Induced Phase Transitions in Unoriented Films

The changes in texture and structure occurring during stretching at room temperature in the iPP samples of Table [11.1](#page-298-0) are analysed by X-ray fibre diffraction. To this aim, rectangular specimens of initial gauge length  $l_0 = 3.0$  mm, initial width  $w_0 = 1.6$  mm and initial thickness  $t_0 = 0.25$  mm, cut from films prepared by compression moulding in a hot press using a low pressure, are stretched at different deformations. In a series of experiments, diffraction data have been collected while keeping the sample in tension, on samples stretched step by step (ex situ analysis or <span id="page-307-0"></span>stretch-and-hold experiments) (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2006](#page-330-0), [2007\)](#page-330-0). Two benchmarks are drawn in the central part of the specimens at distance  $l_0$  and the local deformation is measured for the region between the benchmarks as  $\varepsilon = 100 (l - l_0)/l_0$  with l the distance between the benchmarks after deformation. In all experiments, the X-ray beam was incident on the central region between the benchmarks. In this way, the structural changes occurring by effect of mere uniaxial deformation with negligible shear components may be probed, provided that the x-ray beam is focused in the center of the specimens and possibly in the central zone of necking regions in case of non homogeneous deformations. Diffraction data are collected 1 h after stretching for at least 40 min. Diffraction data are also collected continuously during stretching at controlled deformation rate of  $=$  2.36 mm/min (in situ measurements), using synchrotron radiation light at a time resolution of 1 frame every 5 s. Examples of in situ collected X-ray fibre diffraction patterns are reported in Fig. 11.6 (bi-dimensional diffraction patterns) and Fig. [11.7](#page-308-0) (equatorial sections).



Fig. 11.6 Bi-dimensional X-ray diffraction patterns of fibres of samples iPP3 with  $[rr] = 3.7$  mol % (a–d) iPP4 with  $[rr] = 5.9 \text{ mol\%}$  (e–i) and iPP5 with  $[rr] = 11.0 \text{ mol\%}$  (l–p), obtained by stretching at room temperature compression moulded films at the indicated values of the strain  $\varepsilon$ . Data are collected in situ, at the beam-line 16.1 of the Synchrotron Radiation Source in Daresbury (Cheshire, UK), 2.36 mm/min deformation rate, incident wavelength  $\lambda = 1.4 \text{ Å}$ , 1 frame/5 s. The stretching direction is vertical. The strong reflections of the unoriented film specimens of iPP are used to determine the correct beam centre coordinates and the sample to detector distance. Arrows in b, f, g, m and n indicate the polarization of the reflection  $(040)$ <sub>α</sub> of  $\alpha$  form,  $(008)$ <sub>γ</sub> of γ form along the meridian, due to the perpendicular chain-axis orientation (cross  $\beta$ , Scheme [11.3a](#page-313-0)') of crystals in  $\gamma$  form occurring at intermediate deformations, before transformation into the mesophase at the onset of the fibrillar morphology

<span id="page-308-0"></span>

Fig. 11.7 Equatorial section profiles extracted from the bi-dimensional X-ray diffraction patterns of fibres of the samples iPP3 with  $[rr] = 3.7 \text{ mol\%}$  (a), iPP4 with  $[rr] = 5.9 \text{ mol\%}$  (b), and iPP5 with  $[rr] = 11.0$  mol% (c), obtained by stretching at room temperature compression moulded films at the indicated values of the strain  $\varepsilon$ . The typical reflections of  $\alpha$  and  $\gamma$  forms are indicated. (c') Stress–strain hysteresis cycles of iPP5 ( $[rr] = 11 \text{ mol\%}$ ) recorded during consecutive steps of stretching and relaxation according to the direction of the *arrows* (2.36 mm/min deformation rate) while collecting the diffraction data. In the first cycle  $(a, b, solid lines)$  a compression-moulded film of initial length 3 mm is stretched up to 900 % deformation (final length  $L_f = 10 L_0$ ) and then it is relaxed. In the successive cycles  $(c, d, dashed lines)$  the so-obtained relaxed fibre is stretched up to the final length  $L_f = 10 L_0$  and then it is relaxed

The structural changes occurring upon stretching unoriented films of the most stereoregular samples of Table [11.1](#page-298-0) with rr content below 5 mol% are shown in Fig. [11.6a–d,](#page-307-0) in the case of the sample iPP3 with  $[rr] = 3.7$  mol%. Compressionmoulded films of the sample iPP3 crystallize as mixtures of the  $\alpha$  and the  $\gamma$  forms (WAXS curve c of Figs. [11.2a](#page-299-0), [11.6a](#page-307-0) and curve a of Fig. [11.7a\)](#page-308-0) (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007\)](#page-330-0). It is clear that the transformation to the mesomorphic form yields structures which have a very high level of preferred orientation with respect to the stretching direction. This sample behaves as a stiff plastic material even though it can be easily stretched up to 300–400 % deformation at room temperature (Fig. [11.4a\)](#page-301-0). The crystalline forms initially present in the sample starts transforming into the mesomorphic form at  $\approx$  170 % deformation (Fig. [11.6b](#page-307-0)) in agreement with the data collected ex situ (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007](#page-330-0)). The formation of the mesomorphic form is indicated in the X-ray fibre diffraction pattern of the iPP3 sample stretched at 173 % deformation, by the presence of a broad halo in the equatorial regions in the  $q$  range 9–14  $\text{nm}^{-1}$  (curve g of Fig. [11.7a\)](#page-308-0), typical of the mesomorphic form of iPP, subtending non-oriented reflections of the  $\alpha$  or  $\gamma$  forms (Fig. [11.6b\)](#page-307-0). At  $\approx$ 200 % deformation the sample transforms almost completely into the mesomorphic form, achieving a high degree of orientation of the crystals (Fig. [11.6c, d](#page-307-0) and curves h–m of Fig. [11.7a\)](#page-308-0).

Samples with higher  $rr$  content, in the range 4–6 mol%, are highly flexible materials that show high deformation at break (curve d of Fig. [11.4a](#page-301-0)). For these samples, the  $\gamma$  form, originally present in compression-moulded unstretched films (curve d of Fig. [11.2a](#page-299-0)), gradually transforms into the mesomorphic form by stretching. The gradual transformation of the  $\gamma$  form into the mesomorphic form at high draw ratios is shown in the case of sample iPP4 with  $[rr] = 5.9$  mol% in Figs. [11.6e–i](#page-307-0) and [11.7b](#page-308-0), as an example (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007\)](#page-330-0). The critical deformation at which the mesophase starts appearing is  $\approx$  200 % and at  $\approx$  400 % the initial  $\gamma$  form is completely transformed. Also in this case a high degree of orientation of the chain axes in the mesomorphic aggregates along the stretching direction is achieved, typical of fibrillary morphology.

Samples with concentration of  $rr$  defects in the range  $7-11\%$  are thermoplastic elastomers with high strength (Fig. [11.4](#page-301-0)). For these samples, diffraction data collected in stretch-and-hold experiments indicate that the γ form, which is present in unstretched films (Fig. [11.2e, f\)](#page-299-0), transforms by stretching into the  $\alpha$  form, up to transformation into the mesomorphic form at very high deformations (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007\)](#page-330-0). As an example, the diffraction data collected in situ during stretching for the sample iPP5 ( $[rr] = 11\%$ ) are shown in Figs. [11.6l–p](#page-307-0) and [11.7c.](#page-308-0) In particular, since this sample exhibits elastomeric behaviour, the structural transformations have been followed during mechanical test cycles consisting of consecutive stretching steps up to 900 % deformation, followed by relaxing steps at controlled deformation rate. The stress–strain curves recorded while collecting the bi-dimensional diffraction patterns of Fig. [11.6l–p](#page-307-0) are shown in Fig.  $11.7c'$  $11.7c'$ . It is apparent that unoriented samples of  $\gamma$  form (curve e Fig. [11.2a](#page-299-0)) experience irreversible plastic deformations upon stretching (curve a of

Fig.  $11.7c'$  $11.7c'$ ), and the strain is recovered only in part during the successive relaxing step (curve b of Fig. [11.7c](#page-308-0)) (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007](#page-330-0), [2011\)](#page-330-0). However, after the first mechanical cycle presenting large hysteresis, the sample exhibits elastic recovery in the successive cyclic stretching-relaxation steps (curves c, d of Fig.  $11.7c'$  $11.7c'$ ) (De Rosa et al.  $2005$ ; De Rosa and Auriemma  $2007$ ).

Diffraction data recorded in situ indicate that the initial  $\gamma$  form at 0% deformation (Fig. [11.6l](#page-307-0), and curve a of Fig. [11.7c\)](#page-308-0) starts transforming into the mesophase at deformations slightly higher than 200 % (Fig. [11.6n](#page-307-0) and curve e of Fig. [11.7c](#page-308-0)). In the deformation range 200–500 % (curves b–d of Fig. [11.7c](#page-308-0)) the diffraction peaks of the  $\gamma$  form become broader and broader and a large amount of diffuse scattering emerges behind the Bragg peaks. This indicates that at 200 % deformation the size of coherently scattering domains decreases, because the lamellar crystals of the initial  $\gamma$  form undergo break through different mechanisms such as lamellar slip, shear banding and/or twinning (Peterlin [1971;](#page-333-0) Lin and Argon [1994](#page-332-0)). The transformation into the mesophase is more gradual than in that occurring in iPP3 and iPP4. At  $\approx 400\%$  deformation a small amount of crystals of  $\gamma$  form is still present (Fig. [11.6n\)](#page-307-0) and only at  $\approx 900\%$  deformation the sample is almost completely transformed into the mesophase (Fig. [11.6o](#page-307-0) and curve f of Fig. [11.7c\)](#page-308-0). A highly oriented fibrillar morphology is achieved at this deformation.

Upon release of the tension, the mesophase gradually transforms into the  $\alpha$  form, and the high degree of orientation achieved during stretching is not lost (Fig. [11.6o](#page-307-0) and curves h–i of Fig.  $11.6c$ ). This transition is reversible (Fig.  $11.6o$ , p). In fact, during consecutive mechanical test cycles, the  $\alpha$  form transforms back into the mesophase during stretching (curves f-m of Fig.  $11.7c$ ) and the mesophase trans-forms again into the α form during release of the tension (curves m–o of Fig. [11.7c\)](#page-308-0), while elastic recovery occurs (curves c, d of Fig.  $11.7c'$  $11.7c'$ ). Therefore, whereas the development of the fibrillar morphology starting from unoriented specimens entails occurrence of large amount of irreversible plastic deformation coupled with the irreversible transformation of the initial  $\gamma$  form into the mesomorphic form, oriented fibres of the sample iPP5 show elastomeric properties and the reversible phase transition between the α form and the mesophase (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007](#page-330-0)).

It is worth noting that the diffraction data collected ex situ in a series of stretchand-hold experiments reveal that the onset of transformation  $\gamma$  form occurs at the same values of deformation identified from the diffraction data collected in situ (i.e.  $\varepsilon \approx 200\%$ ). However at variance with the data collected continuously during stretching, the stepwise diffraction experiments evidence that the  $\gamma$  form transforms first into the  $\alpha$  form and only at  $\approx$ 500 % deformation the mesomorphic form starts appearing (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2006,](#page-330-0) [2007\)](#page-330-0). The appearance of  $\alpha$  form at intermediate deformations is not evident in the stream of WAXS data collected in situ probably because no relaxation occurs. In the stretch-and-hold experiments, instead, relaxation of the samples takes place immediately after the stop of the elongation. Because of relaxation, the mesomorphic aggregates created by the mechanical melting of the  $\gamma$  form by effect of deformation "melt" and then recrystallize again into the α form. The melting/recrystallization of the chains is facilitated by the compliance of the amorphous phase surrounding the crystalline

<span id="page-311-0"></span>aggregates in the low stereoregular samples iPP4 and iPP5. Similar differences in between the data collected in continuum and ex situ during tensile tests have been evidenced and discussed by Stribeck in the case of commercial iPP samples (see for instance Stribeck et al. [2008\)](#page-333-0). In that case the differences have been attributed to some kind of relaxation effect in the segmental dynamics. In our case, the in situ experiments show that the stress-induced phase transitions of  $\gamma$  form are the results of competition between strain-rate and melting-recrystallization phenomena, and are facilitated by the fast segmental dynamics of the defective iPP chains.

Moreover, the data of Figs. [11.6](#page-307-0) and [11.7](#page-308-0) lead to the conclusion that the  $\gamma$  form of iPP is mechanically unstable, and gradually transforms into the mesophase (or  $\alpha$ form) by stretching through melting and recrystallization phenomena occurring at local scale. This phase transition is associated with the increase in the degree orientation of crystals with chain axes parallel to the stretching direction (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007\)](#page-330-0). In particular, the high degree of orientation achieved by mesophase at high deformation starting from unoriented α and/or γ forms may be taken as the hallmark of melting /recrystallization phenomena induced by stretching (Mitchell [1984](#page-332-0)).

#### 11.6 Structural Analysis at Microscopic Length Scale

The radial intensity distribution along the azimuthal angle  $\chi$  in the q regions around 10 and 12 nm<sup>-1</sup> is reported in Fig. [11.8a–c.](#page-312-0) The selected q regions correspond to the reflections (110)<sub>α</sub> of α form, (111)<sub>γ</sub> of γ form ( $d \approx 0.65$  Å nm), and (040)<sub>α</sub> of α form, (008)<sub>γ</sub> of γ form ( $d \approx 0.52$  nm) at low deformations (Scheme [11.3](#page-313-0)a), to the tails of the mesomorphic halo at high deformations (see Fig. [11.7a–c](#page-308-0) vertical dashed lines). The azimuthal angle  $\chi$  is defined by the angle that the q radial vector makes with the stretching direction (fibre axis) (Scheme [11.3a](#page-313-0)). Therefore, the meridian axis corresponds to  $\gamma = 0^{\circ}$  and 180° whereas the equator corresponds  $\gamma = 90^{\circ}$  and 270°.

In Fig. [11.8a–c](#page-312-0) the intensity distribution at zero deformation is essentially uniform. With increasing deformation, the intensity at  $q \approx 10 \text{ nm}^{-1}$  becomes more intense on the equator (curves a–e of Fig.  $11.8b$  and a–g of Fig. [11.8c\)](#page-312-0). In particular, the distribution of intensity at  $q \approx 10 \text{ nm}^{-1}$  shows a broad maximum on the equator up to deformations close to  $150-200\%$  (curves b, c of Fig.  $11.8b$ , c). At deformation higher than 200 % the maximum becomes narrow (curves d, e of Fig. [11.8b, d–h](#page-312-0) of Fig. [11.8c\)](#page-312-0) marking the development of the fibrillar morphology. In fact, since the normal to the  $(110)_{\alpha}$  planes of  $\alpha$  form,  $(111)_{\alpha}$  planes of  $\gamma$  form (poles) are perpendicular to the chain axes direction in  $\alpha$  form (Fig. [11.2b\)](#page-299-0) to the direction of one-half of chain axes in the  $\gamma$  form (Fig. [11.2c\)](#page-299-0) the polarization of the intensity at  $q \approx 10$  nm<sup>-1</sup> on the equator marks the tendency of chain-axes to orient parallel to the stretching direction (fibre axis).

This suggests that the development of the fibrillar morphology can be followed using the azimuthal spreading of the intensity at  $q \approx 10 \text{ nm}^{-1}$  (curves a–e of Fig. [11.8b](#page-312-0) and a–g of Fig. [11.8c](#page-312-0)) to obtain an order parameter  $\langle P_2(\cos \chi) \rangle$ defined as:

<span id="page-312-0"></span>

Fig. 11.8 Radial intensity distribution along the azimuthal angle  $\chi$  extracted from the bi-dimensional X-ray diffraction patterns of Fig. [11.6](#page-307-0) relative to the samples iPP3 with  $[rr]$  = 3.7 mol% (a), iPP4 with  $[rr] = 5.9$  mol% (b), and iPP5 with  $[rr] = 11.0$  mol% (c) in the q regions close to 10 (b, c) and 12  $\text{nm}^{-1}$  (a–c). The data are obtained by stretching at room temperature compression moulded films at the indicated values of the strain  $\varepsilon$ . Degree of alignment of chain axes with the stretching direction  $O$  (d, d') and total scattered intensity normalized for the integrated intensity of the unoriented sample  $\Gamma(\varepsilon)$  (e, e') as a function of strain. Insets **d'** and e' show the parameters O and  $\Gamma(\varepsilon)$  at low deformation on an enlarger y-scale. The parameter O is calculated from the radial intensity distribution at  $q \approx 10 \text{ nm}^{-1}$  (see the text)

# A

<span id="page-313-0"></span>

**Scheme 11.3** Definition of the azimuthal angle  $\chi$  and scheme of the perpendicular chain axis orientation  $(a, a')$  and the chevron-like texture  $(b, b')$  in the reciprocal  $(a, b)$  and direct space  $(\mathbf{a}', \mathbf{b}')$ 

$$
\langle P_2(\cos \chi) \rangle = \frac{1}{2} \left( 3 \langle \cos^2 \chi \rangle - 1 \right) \tag{11.1}
$$

In Eq. ([11.1](#page-311-0))  $\langle \cos \chi \rangle$  is the average cosine that the poles of a given family of planes make with the preferred (fibre axis) direction and  $\langle P_2(\cos \chi) \rangle$  the second order Legendre polynomial of argument  $\langle \cos \chi \rangle$ . Equation [\(11.1\)](#page-311-0) is also known as Herman's orientation parameter, where  $P_2(\cos \chi) = 1$  corresponds to an ideal case of perfect alignment of the poles toward a preferential direction,  $P_2(\cos \chi)$  $= 0$  corresponds to isotropic case and  $P_2(\cos \chi) = -0.5$  corresponds to an ideal case of perfect perpendicular orientation. The values of  $\langle \cos \chi \rangle$ , in turn, are calculated from the azimuthal intensity distribution at  $q \approx 10 \text{ nm}^{-1}$  as it follows:

$$
\langle \cos^2 \chi \rangle = \frac{\int_0^{\pi/2} I(q) \cos^2 \chi \sin \chi \, \mathrm{d}\chi}{\int_0^{\pi/2} I(q) \sin \chi \, \mathrm{d}\chi} \tag{11.2}
$$

Strictly precise determination of the degree orientation of the chain axis in the crystals along the stretching direction should be performed using the azimuthal intensity distribution of a 00l (meridional) reflection or using the azimuthal intensity distribution of three orthogonal reflections (Alexander, 1979). In our case, the chain axis orientation is inferred indirectly, measuring the degree of polarization of the intensity at  $q \approx 10 \text{ nm}^{-1}$  on the equator, with respect to the meridional axis. Because of the equatorial polarization of intensity at  $q \approx 10 \text{ nm}^{-1}$ , the development of the fibrillar morphology as a function of deformation would be indicated by the decrease of the experimental values of the order parameter  $\langle P_2(q)\rangle^{\text{exp}}$  from 0 at zero deformation (completely isotropic sample) to values less than zero with increasing the deformation, corresponding to the fibre morphology. Therefore, a measure of the degree of orientation  $O$  of the iPP samples as a function of deformation may be obtained by comparing the experimental values of  $\langle P_2(q) \rangle^{\text{exp}}$  at  $q \approx 10 \text{ nm}^{-1}$  with that of an ideal model characterized by an extremely narrow equatorial polarization of intensity at this q (that is  $\langle P_2 \rangle^{\text{Id}} = -0.5$ ) as:

$$
O = \frac{P_2(\cos \chi)^{\text{Exp}}}{P_2(\cos \chi)^{\text{Id}}}
$$
(11.3)

According to Eq. (11.3), the parallel chain axis orientation corresponds to values of  $0 > 0$ . Furthermore, the higher O, the higher the fraction of chain axes in the crystalline aggregates reaching a parallel alignment with the stretching direction during deformation. The values of the parameter  $O$  derived for the iPP samples are reported in Fig. [11.8d.](#page-312-0)

All samples follow a common scheme consisting of three steps. In the first step, for deformations  $\varepsilon$  lower than 100 %, a steep increment of the degree of orientation occurs, with the parameter O reaching values  $O = 0.30{\text{-}}0.4$  (Fig. [11.8d](#page-312-0)'). Therefore, at low deformations, but higher than yield strain (Fig. [11.4\)](#page-301-0), change in radial intensity distribution along  $\chi$  of (110)<sub>α</sub> of reflection of α form, (111)<sub>γ</sub> of reflection of  $\gamma$  form at  $q \approx 10 \text{ nm}^{-1}$  essentially probes small reorientation of lamellar crystals along the pathway toward the fibrillar morphology. Reorientation of crystals at low deformations is generally due to lamellar or lamellar stacks rotations, and it is associated with interlamellar shear movements (Bowden and Young [1974](#page-330-0); Lin and Argon [1994](#page-332-0); Humbert et al. [2010;](#page-331-0) Mourglia-Seignobos et al. [2014\)](#page-332-0).

In the second step, corresponding to the deformation range between 100 and  $\approx$ 150–200 % (Fig. [11.8d, d](#page-312-0)'), the orientation parameter O reaches a *quasi plateau*. We argue that the leading deformation mechanisms in this region correspond to interlamellar shear that is slip of the crystalline lamellae parallel to each other, and possibly interlamellar separation, both phenomena being assisted above glass transition temperature, by the shear deformation of the compliant interlamellar amorphous phase (Bowden and Young [1974;](#page-330-0) Schultz [1974;](#page-333-0) Lin and Argon [1994;](#page-332-0) Séguéla [2002](#page-333-0)).

In the third step, starting from deformations close to the critical strain at which stress-induced phase transitions start occurring ( $\varepsilon \approx 200\%$ , Figs. [11.6](#page-307-0) and [11.7](#page-308-0)), the orientation order O experiences a new increase up to reach a final plateau value at high deformations of  $0 \approx 0.9$  for the sample iPP3 with  $[rr] = 3.7$  mol%,  $0 \approx 0.8$  for the less stereoregular samples iPP4 and iPP5 (Fig. [11.8d\)](#page-312-0). In this high deformation range, the increase of deformation induces collective shear processes, up to reach the destruction of the pre-existing crystals (mechanical melting) and successive recrystallization with formation of fibrils (Schultz [1974](#page-333-0); Lin and Argon [1994\)](#page-332-0). Further increase of plastic strain in the successive steps entails disentanglement of the amorphous network or strain hardening due to the stretching of the amorphous entangled network at high deformations (Schultz [1974](#page-333-0); Peterlin [1971;](#page-333-0) Men et al. [2003\)](#page-332-0).

The analysis of the radial intensity distribution along the azimuthal angle  $\chi$  in the q region around 12 nm<sup>-1</sup> of Fig. [11.8a–c](#page-312-0) reveals that during the development of the fibrillar morphology, for deformations lower than the critical value at which transformation of  $\gamma$  form into mesophase is complete, there is a portion of the crystalline lamellae which tend to orient with the chain axes nearly perpendicular to the stretching direction instead than parallel, contrary to what expected in the standard fibre morphology.

This non-standard crystals orientation is observed in the case of the sample iPP3 up to 170 % deformation (curves b–f of Fig. [11.8a\)](#page-312-0), the sample iPP4 up to 300 % deformation (curves  $b'$ –d' of Fig.  $11.8b$ ) and the sample iPP5 up to 500 % defor-mation (curves b'-d' of Fig. [11.8c\)](#page-312-0) as indicated by the polarization of the  $(040)_{\alpha}$ reflection of the α form,  $(008)$ <sub>γ</sub> reflection of the γ form at  $d = 5.21 \text{ Å } (q \approx 12 \text{ nm}^{-1})$ , at oblique angles, and as indicated also in Fig.  $11.6b$ , f, g, m, n by arrows. At higher deformations, the diffraction maxima at oblique angles disappear or become very low (Fig. [11.8b, c\)](#page-312-0), and the radial intensity distribution at  $q \approx 12$  nm<sup>-1</sup> becomes peaked on the equator, according to the standard fibre morphology (Fig. [11.8a](#page-312-0) curves g, i, up to breaking, Fig.  $11.8b$  curves d', e', Fig.  $11.8c$  curves d'-h').

The nearly meridional polarization of the reflection at  $q \approx 12$  nm<sup>-1</sup> (reflections (040)<sub>α</sub> of α form, or (008)<sub>γ</sub> of γ form) in the patterns of Fig. [11.6](#page-307-0) and azimuthal profiles of Fig. [11.8a–c](#page-312-0) indicate that portion of the crystals of  $γ$  form, or in disordered modifications intermediate between the  $\gamma$  and  $\alpha$  forms more similar to the γ form, assume an orientation with the c<sub>γ</sub>-axis of γ form (b<sub>α</sub>-axis of  $\alpha$  form) nearly perpendicular to the stretching direction (Fig. [11.2b, c](#page-299-0)) (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007](#page-330-0); Auriemma and De Rosa [2006\)](#page-330-0). Since the  $c<sub>y</sub>$ -axis of γ form ( $b_{\alpha}$ -axis of  $\alpha$  form) are the axes of stacking of the layers of chains (Fig. [11.2b,](#page-299-0) [c](#page-299-0)) this non-standard mode of orientation of iPP crystals corresponds to lamellae oriented with chain axes nearly perpendicular to the fibre axis (Fig. [11.2b, c](#page-299-0), and Scheme  $11.3a'$  $11.3a'$ ).

A similar kind of orientation has been well known for many years in some naturally occurring fibrous proteins such as silks (Geddes et al. [1968](#page-331-0)). The perpendicular orientation of chain axes with respect to the fibre axis, described as cross-β, occurs at low draw ratio and has been explained by the fact that in these soft silks the small crystallites are elongated along the hydrogen bond directions, which run perpendicular to chain axes (Geddes et al. [1968\)](#page-331-0). The cross-β orientation in iPP may be attributed to the simultaneous occurrence of two kinds of slip processes at low

deformations, interlamellar and intralamellar (Men and Strobl [2001\)](#page-332-0). Whereas interlamellar shear leads to a location of the (008)<sub>γ</sub> reflection of γ form ((040)<sub>α</sub> reflection of α form) on the meridian, the intralamellar shear pushes the chain axes to align parallel with the stretching direction, and thus shifts the position of the reflection toward the equator (De Rosa et al. [2005;](#page-331-0) De Rosa and Auriemma [2007\)](#page-330-0).

The fact that the cross-β orientation is apparent up to high deformations indicates that not all the crystalline lamellae of  $\gamma$  form originally present in the sample experience simultaneously the uniaxial mechanical stress field. The non-standard mode of orientation of these crystals reflects crystallographic restraints on the slip processes, and topological constrains on the response of crystals to the tensile stress field. In the crystalline domains of  $\gamma$  form, indeed, the chains are oriented along two perpendicular directions, and the crystallites have the shape of elongated entities along the direction normal to the chain axes (De Rosa et al. [2005](#page-331-0); Auriemma and De Rosa [2006](#page-330-0)). Because of the intrinsic structural and morphological characteristics of  $\gamma$  form, at low deformations portion of  $\gamma$  lamellae remains frozen in strained positions of the polymer matrix with the chain axes oriented nearly perpendicular to the stretching direction. By stretching at higher deformations the  $\gamma$  form transforms into the mesophase. Since in the crystals of the mesophase the chains are all parallel, the deformation also induces orientation of crystals with the chain axes oriented along the stretching direction, as in a standard fibre morphology (De Rosa et al. [2005](#page-331-0); Auriemma and De Rosa [2006](#page-330-0)). This mechanism is confirmed by the fact that this non-standard mode of orientation of crystals has been observed only during stretching of iPP samples containing crystals of  $\gamma$  form and has never been observed for iPP samples crystallized in the pure  $\alpha$  form.

For samples exhibiting uniaxial symmetry (fibres), the WAXS intensity collected on a bi-dimensional detector (Fig. [11.6\)](#page-307-0) can be integrated over the whole sampled reciprocal space, that is between  $q_{\min} (=3 \text{ nm}^{-1})$  and  $q_{\max} (20 \text{ nm}^{-1})$ , obtaining the total scattered intensity in the WAXS region  $\Omega_{\text{waxs}}$ , using (11.4):

$$
\Omega_{\text{WAXS}}(\varepsilon) = \int_0^{2\pi} \int_{q_{\text{min}}}^{q_{\text{max}}} I(q, \chi) q^2 \sin \chi \, d\chi \, dq \tag{11.4}
$$

In Eq. (11.4), it is implicitly assumed a uniform distribution of intensity along circles of radius  $q \sin \chi$  because of the uniaxial symmetry of the fibres. The ratio of the total scattered intensity evaluated at deformation  $\varepsilon$  and the integrated intensity of the unoriented sample gives the normalized value of the total scattered intensity  $\Gamma(\varepsilon) = \Omega_{\text{waxs}}(\varepsilon)/\Omega_{\text{waxs}}(\varepsilon = 0)$ . The values of the parameter  $\Gamma(\varepsilon)$  of iPP samples are shown in Fig.  $11.8e$ ,  $e'$  as a function of deformation.

Also in this case the samples follow a common scheme regardless of stereoregularity. In particular, up to  $\approx$ 200 % deformation the values of  $\Gamma(\varepsilon)$  are coincident and decrease with increase of deformation (Fig.  $11.8e'$  $11.8e'$ ), whereas for deformations higher than 200 %, the values of the parameter  $\Gamma(\varepsilon)$  increase by 30–40 %, up to reach a quasi-plateau (Fig. [11.8e](#page-312-0)). Changes occur by effect of deformation because of decrease in thickness, consequent change of absorption factor, change in the relative amount of the phases, stress-induced phase transitions and/or

<span id="page-317-0"></span>crystallization, appearance of additional phases and consequent change in contrast. Additional effects can also arise from decrease (or increase) of the size of coherent crystalline domains embedded in the amorphous phase, due to lamellar fragmentation (coalescence) of the domains. Since the total scattering intensity is proportional to the squared volume of incoherently scattering objects  $V_{\text{obj}}^2$ , a decrease (increase) in volume of the scattering objects  $V_{\text{obj}}$  leads to a decrease (increase) in scattering intensity, even if the total degree of crystallinity, proportional to  $N_{\text{obj}}$   $V_{\text{obj}}$  with  $N_{\text{obj}}$ the number of scattering objects contributing additively to intensity, remains constant (Alexander [1979;](#page-330-0) Glatter and Kratky [1982\)](#page-331-0).

In general, the transverse strain of semi-crystalline polymers (perpendicular to the stretching direction under uniaxial elongation) decreases with deformation. For a uniform deformation, the thickness of the sample decreases. For rubbery materials, at low deformations, the thickness t decreases as  $t = t_0 (l_0/l)^{\nu}$ , where  $l_0$  and l are the initial gauge length and the gauge length in deformed state, and  $\nu$  is he Poisson's ratio equal to 0.4–0.5. However, for semi-crystalline polymers the Poisson's ratio changes during deformation, from the maximum value of 0.5 up to drop to values close to zero, by effect of volume expansion due to crazing, cracks and voids (Nitta and Yamana [2012](#page-333-0)). In the lack of direct measurements of the thickness values during deformation, data in Fig.  $11.8e$ ,  $e'$  have not been corrected by this factor. On the other hand, concerning the absorption correction, this factor would not greatly influence the values of  $\Gamma(\varepsilon)$ , and, at least to a first approximation may be neglected. In fact the linear absorption coefficient of iPP for X-ray wavelength  $\lambda = 0.14$  nm is  $\approx 3$  cm<sup>2</sup>/g (Maslen [2006\)](#page-332-0) and the absorption coefficient at 900 % deformation ( $l_0/l = 0.1$ ) would decrease by a factor less than 1.1 assuming a Poisson's ratio of 0.5.

Since in our samples the degree of crystallinity does not greatly change during deformation (De Rosa et al. [2005](#page-331-0); De Rosa and Auriemma [2007](#page-330-0)) the decrease in the normalized total scattering intensity value  $\Gamma(\varepsilon)$  of Fig. [11.8e, e](#page-312-0)' at deformation less than 200 % can be attributed to a decrease in thickness coupled to a lamellar fragmentation. The increase of the  $\Gamma(\varepsilon)$  parameter at deformations higher than 200 %, instead, may be ascribed to structural changes, including appearance of additional phases due to the gradual transformation of  $\gamma$  form, nucleation of voids (due to cavitation, vide infra), small increase in the degree of crystallinity, but also to coalescence of small crystalline mesomorphic aggregates embedded in the mobile amorphous phase into larger aggregates.

#### 11.7 Structural Analysis at Lamellar Length Scale

The structural transformations occurring at lamellar length scale during stretching have been followed by performing time-resolved SAXS measurements at the SRS synchrotron light source at Daresbury, UK. Rectangular specimens of initial gauge length  $l_0 = 3.0$  mm, initial width  $w_0 = 1.6$  mm and initial thickness  $t_0 = 0.25$  mm, prepared by compression moulding, are stretched at controlled deformation rate of 2.36 mm/min (1 frame/20 s, beam diameter 0.1 mm). Scattering data were collected

<span id="page-318-0"></span>

Fig. 11.9 Bi-dimensional X-ray diffraction patterns recorded at small angle (SAXS) of the samples iPP4 with  $[rr] = 5.9 \text{ mol\%}$  (a-d) and iPP5 with  $[rr] = 11.0 \text{ mol\%}$  (a'-f'). Data are collected in situ, at the beam-line 16.1 of the Synchrotron Radiation Source in Daresbury (Cheshire, UK), 2.36 mm/min deformation rate, incident wavelength  $\lambda = 1.4 \text{ Å}$ , 20 s/frame. The stretching direction is vertical. Arrows in (c) and (b') and (c') indicate the polarization of intensity off the equator and meridian due to the chevron-like texture (Scheme  $11.3<sup>b</sup>$ )

537%

900%

using the Rapid Area Detector system in the q range  $0.1-1$  nm<sup>-1</sup>. The scattering geometry was calibrated using a wet collagen fibre.

A selected sequence of the bi-dimensional SAXS patterns of the samples iPP4 and iPP5 ( $[rr] = 5.9$  and 11.0 mol%, respectively) taken during tensile stretching are shown in Fig. 11.9, whereas the corresponding radial distribution along the azimuthal angle  $\chi$  (Scheme [11.3](#page-313-0)b) is reported in Fig. [11.10a, b](#page-319-0). Both samples show a uniform distribution of intensity along rings centred in the q region 0.3–1 nm<sup>-1</sup> in the undeformed state (Fig.  $11.9a$ , a' and curves a of Fig.  $11.10a$ , b).

With increasing deformation the intensity distribution becomes anisotropic, marking the tendency of the lamellae to become oriented with their normal parallel to stretching direction as in fibre morphology.

At deformations lower than  $\approx$ 300–400 %, the SAXS patterns tend to assume an elliptical geometry characterized by a concentration of intensity above and below the equatorial region (Fig. 11.9b, c, b', c'). The corresponding azimuthal intensity profiles show broad maxima centred on the meridian ( $\chi = 0^{\circ}$  and 180<sup>o</sup>) for the

 $iPP4$  [ $rr$ ] = 5.9mol%

<span id="page-319-0"></span>

Fig. 11.10 (a, b) Radial intensity distribution along the azimuthal angle  $\chi$  extracted from the bi-dimensional SAXS patterns of Fig. [11.9](#page-318-0) relative to the samples, iPP4 with  $[rr] = 5.9 \text{ mol\%}$  (a), and iPP5 with  $[rr] = 11.0$  mol% (b). The profiles have been obtained by integrating the intensity in spherical shells of q with q comprised between 0.2 and 0.8 nm<sup>-1</sup>. (a', a'', b', b'') Amplitude of zero order spherical harmonics  $I_0(q)$  ([11.6](#page-321-0)) (a', b') and order parameter  $P_2(\cos \chi)_q$  ([11.7\)](#page-321-0) (a'', b'') obtained through interpolation of the bi-dimensional SAXS intensity of Fig. [11.9](#page-318-0) with the series expansion using spherical harmonics  $P_{2n}(\cos \chi)$  as basis set according to Eq. ([11.5](#page-321-0))

sample iPP4 at deformations lower than  $100\%$  (Fig. [11.9b](#page-318-0) and curves b, c of Fig. [11.10a\)](#page-319-0) or four weak maxima displaced by  $20^{\circ} - 30^{\circ}$  from meridian ( $\chi \approx 30^{\circ}$ , 150°, 210° and 330°) at deformations higher than 100 % for the sample iPP4 and in the deformation range 80–220 % for the sample iPP5 (Fig.  $11.9c$ , b', c', curves d, e of Fig. [11.10a](#page-319-0) and curves b, c of Fig. [11.10b](#page-319-0)). The four maxima off the equator and meridian (evidenced by arrows in Fig.  $11.9c$ , b', c') correspond to the buckling of the lamellar stacks according to a chevron-like (undulated) texture as depicted in the Scheme [11.3b](#page-313-0)'. These undulated textures take place in a large number of semicrystalline polymers such as polyethylene at low and intermediated deformations (before fibrillation) (Gerasimov et al. [1974;](#page-331-0) Read et al. [1999](#page-333-0); Krumova et al. [2006\)](#page-332-0). According to a general mechanism, lamellar stacks subjected to tensile deformation in the direction normal to their layers experience also compressive stress in the direction transverse to the tensile deformation axis. The crystalline (hard) layers sustain this transverse compression until buckling occurs with consequent formation of undulated structures (Scheme  $11.3b'$  $11.3b'$ ) (Makke et al. [2012\)](#page-332-0).

At deformation higher than the chevron texture (200 % for iPP4, 400 % for iPP5), the four-lobe pattern defined by the intensity distribution is replaced by a diamond-shaped diffuse scattering (Fig. [11.9d, d](#page-318-0)', e'). Diffuse scattering appears as streaks located on the equator (Fig.  $11.9d$ ,  $d'$ ,  $e'$ ), and marks formation of nanocavities in the interlamellar regions during deformation. With increasing deformation, the microcavities undergo elongation in the stretching direction, and the bi-dimensional SAXS patterns become entirely dominated by the equatorial streaks due to cavitation (Pawlak and Galeski [2005](#page-333-0)). This is evidenced by the azimuthal intensity profiles in Fig.  $11.10a$ , b showing maxima on the equator  $(\chi = 90^{\circ}$  and 270°) superimposed to a flat background (curves f-i of Fig. [11.10a,](#page-319-0) [d,](#page-319-0) e of Fig. [11.10b\)](#page-319-0). In these curves no meridional maxima are apparent up to very high deformations.

Therefore, the SAXS data evidence that with increasing the deformation the polarization of intensity shifts from positions in between the meridian and the equator, toward the equator, and no meridional maxima become apparent, as instead expected for a well oriented fibre morphology (Figs. [11.9a–d,](#page-318-0) a'–e' and [11.10a, b](#page-319-0)). The absence of meridional maxima in the SAXS intensity distribution at high deformations is in apparent contrast with WAXS results of Figs. [11.6](#page-307-0) and [11.7](#page-308-0). In fact, WAXS analysis indicate almost complete transformation of the initial  $\gamma$ form into well oriented mesomorphic aggregates already at deformations of  $\approx$  200% for the sample iPP4 and 400% for the sample iPP5. The absence of meridional maxima in the SAXS patterns of the samples iPP4 and iPP5 stretched at high deformations (Fig.  $11.9d$ ,  $d'$ ,  $e'$ ) is due to the too low contrast in electron density between the mesophase and amorphous components and cavitation. Upon cavitation, indeed, nanocavities act as a third phase with zero electron density, and the scattering intensity becomes entirely dominated, in the small angle, by the large contrast between nanocavities and the surrounding phases.

The damage effect due to cavitation in the elastomeric sample iPP5 stretched at 900 % deformation (Fig. [11.9e](#page-318-0) and profile f of Fig. [11.10b](#page-319-0)) is irreversible. In fact, in mechanical cycles of stretching and relaxing the tension no significant changes in <span id="page-321-0"></span>the SAXS intensity distribution occur (Fig. [11.9f](#page-318-0) and profile g–i of Fig. [11.10b\)](#page-319-0). This indicates that even though reversible structural changes occur between the mesophase and  $\alpha$  form (see Sect. 3.2), damages due to cavitation are not recovered, and the SAXS intensity distribution keeps dominated by the large contrast between the nanocavities and the surrounding phases (amorphous phase,  $\alpha$  or  $\gamma$  form and mesophase).

The SAXS intensity of Fig. [11.9](#page-318-0) has been analysed in the framework of series expansion of uniaxially symmetric samples in terms of spherical harmonics  $P_{2n}(\cos \chi)$  (Lovell and Mitchell [1981](#page-332-0); Mitchell and Windle [1982](#page-332-0)) as:

$$
I(q,\chi) = \sum_{2n=0,2,4,\dots}^{\infty} I_{2n}(q) P_{2n}(\cos \chi)
$$
 (11.5)

In Eq. (11.5), only the even terms are required due to the inversion centre intrinsic to X-ray scattering patterns for a non-absorbing sample of uniaxial symmetry. The amplitude of spherical harmonics components in the series expansion of Eq. (11.5) can be obtained by (Lovell and Mitchell [1981](#page-332-0); Mitchell and Windle [1982](#page-332-0)):

$$
I_{2n}(q) = (4n+1) \int_0^{\pi/2} I(q,\chi) P_{2n}(\cos \chi) \sin \chi \,d\chi \tag{11.6}
$$

where  $P_0(\cos \chi) = 1$ ,  $P_2(\cos \chi) = 1/2(3\cos^2 \chi - 1)$ ,  $P_4(\cos \chi) = 1/8(35 \cos^4 \chi)$  $\chi$  – 30 cos<sup>2</sup>  $\chi$  + 3), etc. In practice, the value of the intensity representation with Eq.  $(11.5)$  is that the effects of preferred orientation are separated from the dependence of the scattering on the spatial correlations. In particular, the amplitude of the zero order term  $I_0(q)$  gives for each q the integrated intensity scattered from an equivalent sample with complete random orientation. The amplitude of the second order spherical harmonics  $I_2(q)$  is also relevant. In fact the ratio between  $I_2(q)$  and  $I_0(q)$  (after normalization by the coefficient  $4n + 1$ ) corresponds to the order parameter  $P_2(\cos \chi)_{\rm q}$  as a function of q (11.6):

$$
P_2(\cos \chi)_q = \frac{I_2(q)}{5I_0(q)}\tag{11.7}
$$

At any given q, values of  $P_2(\cos \chi)$  close to 1 correspond to intensity distribution polarized on the meridian at that  $q$ , close to 0 correspond to isotropic distribution of intensity, less than 0 correspond to polarization on the equator.

We have used the amplitude of the zero order spherical harmonics  $I_0(q)$  in Eq. (11.6) and the value of  $P_2(\cos \chi)_q$  in Eq. (11.7) as descriptors for the structural and textural changes occurring in our samples by effect of deformation. Selected curves are reported in Fig.  $11.10a'$  $11.10a'$ , b',  $a''$ , b''.

The isotropic intensity component  $I_0(q)$  of undeformed samples ( $\varepsilon = 0\%$ ) presents a correlation peak at  $q_{\text{max},x} \approx 0.5 \text{ nm}^{-1}$  (Fig. [11.10a](#page-319-0)'[, b](#page-319-0)') and isotropic distri[b](#page-319-0)ution of intensity  $(P_2(\cos \chi)_a \approx 0)$  (Fig. [11.10a](#page-319-0)'', b''). The correlation peak is due to the lamellar stacking and corresponds to values of long period  $L \approx 12.6$  nm.

Upon stretching, for deformation lower than 203 % the correlation peak of the  $I_0(q)$  curves shifts to low q values  $(q_{\text{max}} \approx 0.45 \text{ nm}^{-1})$  indicating an increase of the long period to  $L \approx 14$  nm (Fig. [11.10a](#page-319-0)', [b](#page-319-0)') due to interlamellar separation (Bowden) and Young [1974;](#page-330-0) Peterlin [1971](#page-333-0); Lin and Argon [1994](#page-332-0)). The corresponding values of the order parameter are positive and achieve values close to  $P_2(\cos \chi)_a \approx 0.1$  for the sample iPP4 and  $\approx 0.06$  for the sample iPP5 (Fig. [11.10a](#page-319-0)'', [b](#page-319-0)'') in agreement with the four-lobe patterns observed in the bi-dimensional SAXS patterns (Fig. [11.9b, c,](#page-318-0) b',  $c'$ ) and the broad distribution of the SAXS intensity profile along the azimuthal angle  $\gamma$  with maxima centred around the meridian (curves b–e of Fig. [11.10a–c](#page-319-0) of Fig. [11.10b\)](#page-319-0). As discussed before, the four-lobe patterns originate from the formation of the chevron-like undulated structures (Scheme  $11.3b'$  $11.3b'$ ) and are formed by lamellar stacks oriented with their normal parallel to the stretching direction, experiencing compressive forces in the transverse direction. Therefore the present analysis evidences that in the deformation range  $0-200\%$  undulation and interlamellar separation take place simultaneously since they possibly involve the same population of lamellae and/or lamellar stacks, oriented with their layers normal parallel to the stretching direction (Bowden and Young [1974\)](#page-330-0).

At deformation higher than 200% the isotropic intensity component  $I_0(q)$ becomes featureless. No correlation peaks are apparent, but only a gradual decay of intensity from low to high q values occurs (Fig.  $11.10a'$  $11.10a'$ , [b](#page-319-0)'). The values of the order parameter  $P_2(\cos \chi)$ <sub>q</sub> become negative at all q. In particular the values of  $P_2(\cos \chi)_q$  are  $\approx -0.2$  to  $-0.25$  at  $q = 0.2$  nm<sup>-1</sup> and increase only slightly at higher q. This indicates that the polarization is localized on the equator, in agreement with the diamond-like pattern in the bi-dimensional SAXS patterns (Fig.  $11.9d, d'-e'$  $11.9d, d'-e'$ ) due to cavitation. This is also in agreement with the distribution of SAXS intensity along the azimuthal angle  $\chi$  presenting maxima on the equator and no maxima in the meridional regions (curves f-i of Fig. [11.10a, b\)](#page-319-0). The values of  $I_0(q)$  amplitude at these deformations decays according to a power law dependence of  $q$ , that is, according to  $q^{-D}$  with  $D \approx 2$ , indicating an ellipsoidal shape of the nanocavities along the stretching direction. Therefore, the analysis in terms of spherical harmonics  $P_{2n}(\cos \chi)$  according to [\(11.5\)](#page-321-0) confirms the formation of nanocavities at deformations higher than a threshold and provides a quantitative insight of the structural and textural evolutions occurring during the stretching of our materials.

In the case of the elastomeric sample iPP5 the values of the scattering  $I_0(q)$  and order parameter of  $P_2(\cos \chi)$  of the stress-relaxed specimens are also reported in Fig.  $11.10a'$  $11.10a'$ , [b](#page-319-0)', [a](#page-319-0)'', b''. They are similar to those of the fully stretched fibre at 900 % deformation, indicating that the damage effect caused by cavitation is irreversible.

# <span id="page-323-0"></span>11.8 Determination of Damage Effect

Quantitative information about damage caused by cavitation may be extracted from the SAXS data collected during stretching through calculation of the invariant (Alexander [1979\)](#page-330-0):

$$
Q_{\text{SAXS}}(\varepsilon) = \int_0^{q_{\text{max}}} \int_0^{2\pi} I(q, \chi) q^2 \sin \chi \, d\chi \, dq = \int_0^{q_{\text{max}}} I_0(q) q^2 dq \tag{11.8}
$$

The outer integral in (11.8) is performed after subtraction for the background to  $I_0(q)$ , and should be classically extended to the whole reciprocal space and not limited to the narrow  $q$  range sampled with our experimental set-up, that is  $q_{\text{min}}(=0.2 \text{ nm}^{-1}) < q < q_{\text{max}}(=1 \text{ nm}^{-1})$ . However, in our case, since the integrating function is already very low in the sampled region of q close to  $q_{\min}$  and  $q_{\max}$ , classic extrapolation methods to extend the inferior and superior integration limits were not applied.

From (11.8), the normalized scattering invariant has been calculated as the ratio between the invariant at a deformation ε to the value of the invariant in the undeformed state:

$$
R = \frac{Q_{\text{SANS}}(\varepsilon)}{Q_{\text{SANS}}(\varepsilon = 0)}\tag{11.9}
$$

The normalized values of the invariant R relative to the samples iPP4 and iPP5 are reported in Fig. [11.11](#page-324-0) as a function of deformation. Curves a and b are not corrected for the decrease in thickness of the specimen during stretching. Curves  $a'$  and  $b'$ , instead, have been corrected for this effect, in the limiting hypothesis that the thickness *t* decreases according to the power law  $t = t_0 (l_0/l)^{\nu}$ , with  $\nu = 0.5$ , in the whole deformation range, as expected for an ideal rubbery materials (Nitta and Yamana [2012\)](#page-333-0).

It is apparent that in the case of the sample iPP4 the normalized scattering invariant (curve a of Fig. [11.11](#page-324-0)) exhibits a sigmoidal shape. The parameter R decreases slightly from 0 to  $\approx$  200% deformation, at  $\approx$  200% deformation it decays steeply by  $\approx 80\%$ , and then, in the deformation range from  $\approx 400\%$  up to the breaking, it reaches a new quasi-plateau corresponding to  $R \approx 0.20$ . In the case of the sample iPP5, instead, (curve b of Fig. [11.11](#page-324-0)) the decrease of the normalized invariant follows a less pronounced sigmoidal shape. It starts decreasing immediately upon deformation. The rate of decrease becomes more pronounced in the deformation range 200–500%. Successively, the decrease of the R parameters becomes smooth again and reaches a quasi-plateau in the deformation range 800–900 %. The total decrease of the invariant for the sample iPP5 is similar ( $\approx 80\%$ ) to that of the sample iPP4 (final values of  $R \approx 0.20$ ). Considering the effect of thickness contraction according to the rubbery model, instead, (curves  $a'$ ,  $b'$  of Fig. [11.11\)](#page-324-0), the invariant would change according to a similar trend,
<span id="page-324-0"></span>

Fig. 11.11 Small angle scattering invariant of the samples iPP4 with  $[rr] = 5.9$  mol% (a, a) and iPP5 with  $[rr] = 11.0 \text{ mol\%}$  (**b**, **b**<sup> $\prime$ </sup>) normalized for the invariant of the unoriented sample ( $\varepsilon = 0$ ) as a function of strain  $(R, 11.9)$  $(R, 11.9)$ . Curves a' and b' are corrected for the decrease in thickness t by assuming that t decreases according to the power law  $t = t_0 (l_0/l)^{\nu}$ , with  $t_0$  the thickness of the undeformed specimen and  $\nu = 0.5$  as expected for an ideal rubbery material. The correction has been applied for deformations >200 %

corresponding to a total decrease of  $\approx 40\%$ , and leading to a final value of the R parameter close to 0.6 at high deformations.

The rate of decrease in the invariant changes at deformations of  $\approx$ 200 and  $\approx$ 400% for the sample iPP4 and  $\approx$ 200 and  $>$ 500% for the sample iPP5 and these deformations mark the critical values of strain at which the initial  $\gamma$  form starts and ends almost completely to transform into the mesophase (Figs. [11.6,](#page-307-0) [11.7](#page-308-0), and  $11.8$ ). In addition (Figs. [11.9](#page-318-0) and  $11.10$ ) at 200 % deformation, also cavitation starts occurring.

This indicates that the change of the invariant with deformation is not due to the mere effect of thickness contraction of the specimens. In fact, cavitation and transformation into mesophase also influence the invariant. In general, the invariant depends on the total sampled volume, the number and relative amount of the phases present in the sample, and on the contrast between the electron density of the phases.

More precisely, the scattering invariant  $Q_{\text{bin}}$  for an ideal binary phase system without nano-voids is expressed by Eq.  $(11.10)$  (Glatter and Kratky [1982\)](#page-331-0):

$$
Q_{\text{bin}} = k2\pi^2 V \varphi_1 \varphi_2 (\rho_1 - \rho_2)^2 \tag{11.10}
$$

<span id="page-325-0"></span>In Eq.  $(11.10)$  $(11.10)$  $(11.10)$ , k is a scaling parameter, V denotes the total sampled volume in the scattering experiment and  $\varphi_i$  and  $\rho_i$  denote the volume fraction and the electron density, respectively, of the phase  $i$ . The difference in electron density of the two phases define the contrast, the higher the contrast, the higher the invariant. The scaling parameter accounts for the conversion of the intensity to absolute units.

The density of  $\gamma$  form, mesophase and amorphous phase in isotactic polypropylene are 0.939, 0.91 and 0.854  $g/cm<sup>3</sup>$  at room temperature respectively (Brandrup and Immergut [1989](#page-330-0)), and the corresponding values of electron density are 323, 313 and 294 electrons/nm<sup>3</sup>, respectively. Therefore, in a hypothetical two phase model, with no change in the relative amount of the phases and constant thickness of the specimen, the value of invariant by effect of complete transformation of the initial  $\gamma$ form into the mesophase is expected to decrease, because of decrease in contrast. More precisely, using Eq.  $(11.10)$  $(11.10)$  $(11.10)$ , regardless of the relative amount of the two phases, the invariant would decrease by  $\approx 60\%$ , corresponding to a drop in the parameter R from 1 to  $\approx 0.4$ . This indicates that the transformation of  $\gamma$  form into the mesophase with no change in the degree of crystallinity and no cavitation leads always to a decrease of invariant.

However, in the stretching experiments, we have to consider also cavitation. Cavitation creates an additional phase, characterized by zero electron density. Therefore, in the deformation range between 200 % and 400–500 % our systems consist of four phases,  $\gamma$  form, mesophase, amorphous component and nanocavities. At strain higher than 400–500 % the  $\gamma$  form is almost completely transformed into mesophase, and only three phases (mesophase, amorphous component and nanocavities) should be considered. The scattering invariant for this three-phase system (that is, for deformations  $\varepsilon$  above the threshold limit at which transformation of γ form is almost complete)  $Q_{\epsilon}$  can be written as (Glatter and Kratky [1982\)](#page-331-0):

$$
Q_{\varepsilon} = k2\pi^2 V_{\varepsilon} \Big[ \varphi_{1\varepsilon} \varphi_{2\varepsilon} (\rho_{1\varepsilon} - \rho_{2\varepsilon})^2 + \varphi_{1\varepsilon} \varphi_{\text{voids}} \rho_{1\varepsilon}^2 + \varphi_{2\varepsilon} \varphi_{\text{voids}} \rho_{2\varepsilon}^2 \Big] \tag{11.11}
$$

In Eq. (11.11),  $\varphi_{ie}$  and  $\varphi_{\text{voids}}$  denote the volume fractions of the phases and  $\rho_{ie}$ the corresponding electron densities, whereas  $V_{\varepsilon}$  denotes the total sampled volume in the scattering experiment at deformation  $\varepsilon$ . This volume will change principally by effect of the thickness contraction on stretching and also through phase transitions, cavitation, etc. Therefore, Eq.  $(11.11)$  accounts for the change in the scattering invariant because of all effects, volume change, phase transitions and cavitation and it may be utilized to calculate the theoretical invariant at deformation higher than 400–500 % that is for a three-phase system. Equation  $(11.10)$  $(11.10)$  $(11.10)$  instead, accounts for the presence of only two phases and may be utilized to calculate the invariant at zero deformation that is for a two phase system. Equation  $(11.11)$ predicts that the main effect of cavitation results in an increase of the invariant already for low values of the volume fraction of voids  $\varphi_{\text{voids}}$  because of the increase in contrast.

We have utilized  $(11.9)$  $(11.9)$  $(11.9)$  and  $(11.11)$  to evaluate the volume fraction of voids at high deformations. Since the relative amount of amorphous and crystalline (γ form

or mesophase) components does not change by effect of stretching in our samples (De Rosa et al. [2005](#page-331-0), [2006](#page-331-0); De Rosa and Auriemma [2007\)](#page-330-0), we have assumed that at the maximum deformation the volume fractions of the mesophase and amorphous components ( $\varphi_{1\epsilon}$  and  $\varphi_{2\epsilon}$ , respectively) are approximately related to the volume fraction of the initial  $\gamma$  form and corresponding amorphous component ( $\varphi_{\gamma}$  and  $\varphi_{\alpha}$ , respectively) at zero deformation, by (11.12):

$$
\varphi_{1\varepsilon} \approx \varphi_{\gamma} (1 - \varphi_{\text{voids}}) \n\varphi_{2\varepsilon} \approx \varphi_{a} (1 - \varphi_{\text{voids}})
$$
\n(11.12)

Substituting (11.12) into ([11.11](#page-325-0)), and indicating with  $\rho_m$ ,  $\rho_\gamma$  and  $\rho_a$  the electron density of the mesophase,  $\gamma$  form and amorphous component, the theoretical value of the normalized invariant  $R<sub>e</sub>$  at deformation higher than a critical value results:

$$
R_{\varepsilon} = \frac{Q_{\varepsilon}}{Q(\varepsilon = 0)}
$$
  
=  $(1 - \varphi_{\text{voids}}) \frac{V_{\varepsilon} \left[ \varphi_{\gamma} \varphi_{a} (1 - \varphi_{\text{voids}}) (\rho_{m} - \rho_{a})^{2} + \varphi_{\gamma} \varphi_{\text{voids}} \rho_{m}^{2} + \varphi_{a} \varphi_{\text{voids}} \rho_{a}^{2} \right]}{V \varphi_{\gamma} \varphi_{a} (\rho_{\gamma} - \rho_{a})^{2}}$ (11.13)

In practice, considering that the experimental value of the normalized invariant [\(11.9\)](#page-323-0) at high deformation reaches a quasi-plateau value R of  $\approx 0.2$  with no correction (curves a' and b' of Fig. [11.11](#page-324-0)) and  $\approx 0.6$  after correction for the reduction in thickness (curves a' and b' of Fig. [11.11](#page-324-0)), by setting  $\varphi_{\gamma}(\varphi_{a})$  equal to 0.4–0.6 (0.6–0.4) (see Table [11.1](#page-298-0)) and  $V_{\epsilon} = V(l/l_0)^{-0.5}$  (as in rubbery materials) we have that in the deformation range 600–900 %,the calculated percentage of voids would reach values close to 1% of the total volume, for values of  $R$  in the range  $0.2 - 0.6$ .

The low value of the volume fraction for the nanocavities is in agreement with the low intensity of the diamond-like SAXS patterns of these samples (Fig. [11.9c, d](#page-318-0),  $c'$ – $e'$ ) compared with the high intensity in the corresponding WAXS patterns of γand mesomorphic forms (Fig.  $11.6g-i$ , m-p). In fact, although the presence of voids enhances the contrast with the surrounding environment  $(11.11)$ , the distribution of SAXS intensity in the bi-dimensional patterns is concentrated in a narrow region of reciprocal space close to the origin and produces only strong diffuse scattering (streaks) on the equator, and no additional significant enhancement. On the other hand, the presence of 1% of voids does not significantly alter the average electron density and the self-correlation function of fluctuation in electron density at length scale of atomic distances of the environment surrounding the nanocavities. Therefore the WAXS patterns are not affected.

Cavitation corresponds to formation of microvoids in the amorphous layers confined between crystalline lamellae. According to a general view (Pawlak and Galeski [2005](#page-333-0)), during stretching of semi-crystalline polymers there is a competition

between cavitation and activation of crystal plasticity: easiest phenomena occur first, that is cavitation in polymers with crystals of higher plastic resistance, and plastic deformation of crystals in polymers with crystals of lower plastic resistance. The stress level at yield point corresponds to the onset of cavitation and not necessarily to the onset of plastic deformation of crystals. Therefore, cavitation is negligible for polymers having crystals with low plastic resistance.

In our case, cavitation occurs for both samples at deformations higher than the yield point, concomitant with the onset of transformation of the  $\gamma$  form into the mesophase. At this deformation a high level of orientational order is achieved for the mesomorphic aggregates. Cavitation takes place either in the undulated chevron-like structures involving the residual lamellar crystal of  $\gamma$  form or within the amorphous regions of the fibrillar entities including the mesomorphic form. However, the SAXS intensity distribution keeps dominated by the large contrast between the nanocavities and the surrounding phases up to high deformations, and in the case of the sample iPP5 even in the fully relaxed fibre, characterized by presence of crystals of α form, that is at deformations at which the transformation of  $\gamma$  form is almost complete. This suggests that the fibrillar morphology of the mesophase is accomplished by formation of a low fraction of nanovoids, by effect of breaking of the undulated structures including the  $\gamma$  form.

## 11.9 Concluding Remarks

In this chapter, the complex transformations occurring at different length scales during tensile deformation of semi-crystalline polymers are illustrated in the case of some samples of isotactic polypropylene which present different microstructures of the chains. In particular, the structural, textural and morphological changes occurring at different length scales are studied, by performing time resolved measurements of X-ray intensity scattered at wide and small angle, during stretching. The data are analysed in the framework of our current understanding of the deformation mechanism of polymers at temperatures higher than the glass transition temperature. The main results of the present analysis are depicted in Fig. [11.12](#page-328-0).

In particular the WAXS analysis has shown that for all samples, regardless of stereoregularity, the initial crystalline form obtained from the melt, transforms by effect of tensile deformation into the mesomorphic form (Fig.  $11.12a-a''$ ). A high degree of orientational order of the mesomorphic aggregates is achieved in the final morphology, with the chain axes parallel to the stretching direction. The values of the critical strain marking the beginning of the polymorphic transitions  $\varepsilon$ (start) is close to 200 % for all samples, whereas the strain marking the complete transformation  $\varepsilon$ (end) increases with decreasing the stereoregularity. It has been also shown that at low deformation a non-negligible portion of the crystals in  $\gamma$  form tend to assume a perpendicular chain axis orientation (cross-β) instead then parallel to stretching direction (Fig. [11.12b](#page-328-0)). The gradual transformation of the initial crystalline form into the mesophase, associated with this non-standard mode of

<span id="page-328-0"></span>

Fig. 11.12 Stress-induced changes in the structure, texture and morphology in isotactic polypropylene samples (iPP) with different content of [rr] stereodefects. All changes occur at critical values of strain according to the general scheme  $c - c^{iv}$ . Also phase transitions follow a general scheme. The critical values of strain depend on the intrinsic stability of crystals and flexibility of amorphous chains. The latter factors are both dependent on the stereoregularity ( $(c-e^{iv})$  redrawn from Schultz [1974\)](#page-333-0)

orientation, indicates that the crystals do not experience simultaneously the phase transition during stretching. If we assume that in semi-crystalline polymers, the strain is homogeneously distributed, whereas the stress is not, the gradual transition entails that with increasing deformation, only the crystals that experience a stress higher than a critical value undergo re-orientation and/or transform into another polymorphic form.

In the present multiscale approach, SAXS data analysis reveals that already at low deformations (lower than  $\varepsilon$ (start)) the lamellar crystals oriented with their normal parallel to the tensile force, in order to alleviate compressive transversal stress, undergo buckling instability, with consequent formation of undulated chevron-like super-structures (Fig.  $11.12b'$ ). However, at deformations close to  $\varepsilon$ (end) up to the breaking the effect of lamellar stacking and parallel orientation of the lamellar normal to the stretching direction on the SAXS intensity becomes buried by the large diffuse scattering localized on the equator due to cavitation  $(Fig. 11.12c'')$ .

Therefore the values of  $\varepsilon$ (start) and  $\varepsilon$ (end) mark not only the deformations at the onset and at the end of phase transitions of  $\gamma$  form but also events involving change in texture and morphology and/or damage. The above cascade of events promoted by tensile strain fits quite well into the general scheme of the deformation mechanism of semi-crystalline polymers depicted in Fig.  $11.12c-c<sup>IV</sup>$ . According to this scheme, with increasing the deformation, typically involved processes are: orientation of intralamellar amorphous phase, isolated inter and intralamellar slip processes, at low deformation (Fig.  $11.12c'$  $11.12c'$ ); collective activity of slip motions of crystals, including re-orientation of lamellar stacks (Fig.  $11.12c''$  $11.12c''$ ), buckling instability leading to formation of undulated structures at intermediate deformations; collective intralamellar shear  $(Fig. 11.12c')$  $(Fig. 11.12c')$  $(Fig. 11.12c')$  followed by destruction of crystals (mechanical melting) and recrystallization with formation of fibrils (Fig.  $11.12c^{IV}$  $11.12c^{IV}$ ) at large deformations; the beginning of disentangling of the amorphous network or strain hardening due to the stretching of the amorphous entangled network at deformations close to breaking.

In other terms, the stress-induced phase transitions occurring by effect of plastic deformation are regulated by the same factors that govern the textural and morphological changes during transformation of the initial spherulitic morphology into fibrillar morphology, and reflects crystallographic restraints on the slip processes, and topological constrains on the response of crystals to the tensile stress field transmitted by the interconnected crystallites.

The above considerations support the hypothesis that when polymorphic transformations occur during plastic deformation, in iPP but also in many other polymers, the phase transitions are strain-controlled rather than stress-controlled (De Rosa et al. [2005](#page-331-0), [2006;](#page-331-0) De Rosa and Auriemma [2006](#page-330-0), [2007](#page-330-0), [2011\)](#page-330-0). As discussed above, the critical values of deformation at which the polymorphic transitions start always correspond to the destruction of a portion of original lamellae of a given crystalline form, and recrystallization with formation of fibrils in a new crystalline form. Moreover these critical values depend on the stereoregularity of the sample (Fig. [11.12](#page-328-0)). This suggests that the two factors that govern the location of the critical strain corresponding to the formation of fibrils, that is the modulus of the entangled amorphous (Ahmad et al. [2013\)](#page-330-0) and the stability of the crystals, depend on the stereoregularity. Chains of different stereoregularity possess, indeed, different flexibility. In fact, the relative configuration of consecutive stereoisomeric centres along the chain affects the space correlation among skeletal bonds and the rotational energy barriers around the C–C bonds (Flory [1969\)](#page-331-0). Since the dynamics of macromolecular chains is largely controlled by these parameters, which can be defined as "the internal viscosity" (Allegra [1974\)](#page-330-0) different degrees of stereoregularity produce a different entanglement density of the amorphous phase. Moreover, the stereoregularity also affects the stability of crystals, the degree of crystallinity, as well as the relative stability of the different polymorphic forms involved in the structural transformations (De Rosa and Auriemma [2006,](#page-330-0) [2007](#page-330-0), [2011,](#page-330-0) [2013](#page-331-0), Ch. 7; De Rosa et al. [2006\)](#page-331-0).

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# Chapter 12 Summary

Geoffrey R. Mitchell

As long-chain molecular materials, synthetic polymers naturally exhibit structure on a number of scales. We have seen in the earlier chapters, many examples of the consequences of small changes to the chemical configuration on larger scale structure.

This interplay between structural scales places great demands on both the designers of materials and on the development of processing routes to provide shaped objects for end users. This introduces the requirement to define what morphologies are required at different structural scales. This is an area where definitions and standardization have yet to appear.

Such a time lag is typical in technological development, and we can see this with the drive within the European Union for standardization of nanotechnology (EU [2011](#page-336-0)) and the challenges this presents (Rauscher and Roebben [2014\)](#page-336-0). A number of EU-wide programmes such as Nanodefine [\(2015](#page-336-0)) are seeking the development of methods that reliably identify, characterize, and quantify nanomaterials both as substance and in various products and matrices. The development of manufacturing processes to produce defined properties dependent on the control of morphology through the definition of the chemical configuration of the polymer has been a long-held ambition of many polymer scientists and engineers. From a 'design a polymer to deliver the properties' point of view that ambition remains some way in the future. The complications are the interplay between the different scales of structure.

Just as the discussion of the definition of a nanomaterial underlines, any specification must be accompanied by practical steps by which that specification can be verified. There has been a surge in the development of experimental techniques, and details of many of these have appeared in this book. The availability of calibrated

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<span id="page-336-0"></span>data over a number of structural scales (e.g., see NIMROD in Chap. [2\)](http://dx.doi.org/10.1007/978-3-319-39322-3_2) presents some considerable but interesting challenges in the use of that data to develop a robust understanding of the structure and morphology on the different scales. Clearly, a big computer is no longer sufficient and is unlikely to be sufficient in the foreseeable future. Rather than seeking an ever larger grid computing power, we need to identify how to coarse grain intelligently and effectively so that the interchange of information between the structural scales is effective and efficient. An FCT-funded project to achieve this is underway in the Author's Laboratory (Mitchell 2015).

We have also seen the mix of manufacturing processes, both traditional processes and the emerging area of Direct Digital Manufacturing (Chap. [7](http://dx.doi.org/10.1007/978-3-319-39322-3_7)) which has the possibility to create complex structures at the nano to macroscopic structural scales. Much of this is driven by applications in the medical field including regenerative medicine (Murphy and Atala 2014). The successes of the twentieth century in delivering mass production so that we could all benefit from the industrial revolution may be replaced by mass customization in this so-called Third Industrial Revolution.

"A once-shuttered warehouse is now a state-of-the art lab where new workers are mastering the 3-D printing that has the potential to revolutionize the way we make almost everything." Barack Obama during his state of the union address of 2013, Obama (2013).

What is in no doubt is the capacity of polymer-based materials to yield complex targeted structures with specific properties. To achieve this requires an understanding of the interplay between the different scales of structure. We hope that this book has moved that goal nearer to realization.

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