

Bitsliced Implementations of the PRINCE, LED and RECTANGLE Block Ciphers on AVR 8-Bit Microcontrollers

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Abstract. Due to the demand for low-cost cryptosystems from industry, there spring up a lot of lightweight block ciphers which are excellent for some different implementation features. An innovative design is the block cipher PRINCE. To meet the requirement for low-latency and instantaneously encryption, NXP Semiconductors and its academic partners cooperate and design the low-latency block cipher PRINCE. Another good example is the block cipher LED which is very compact in hardware, and whose designers also aim to maintain a reasonable software performance. In this paper, we demonstrate how to achieve high software performance of these two ciphers on the AVR 8-bit microcontrollers using bitslice technique. Our bitsliced implementations speed up the execution of these two ciphers several times with less memory usage than previous work. In addition to these two nibble-oriented ciphers, we also evaluate the software performance of a newly proposed lightweight block cipher RECTANGLE, whose design takes bitslicing into consider. Our results show that RECTANGLE has very high ranks among the existing block ciphers on 8-bit microcontrollers in the real-world usage scenarios.

Keywords: PRINCE · LED · RECTANGLE · Bitslice · Block cipher · Lightweight · Cryptography · Microcontroller · Wireless sensor · AVR · ATtiny · Implementation

1 Introduction

In several emerging areas and in the Internet of Things (IoT) era, where hundreds billion of highly constrained devices are interconnected, working together and typically communicating wirelessly, security and privacy can be very important. Cryptographic techniques will be required for those devices and will be implemented on more devices at present and in the future. For different application scenarios, there are different efficiency measures to evaluate whether a cryptographic technique can be applied to the scenarios. For hardware implementation, dominant metric are gate count (power, cost), energy, latency etc. The

corresponding application examples are RFID and low-cost sensors, healthcare devices and battery-powered devices, memory encryption, in-vehicle devices and industrial control systems. For software implementation, memory (ROM/RAM) and execution time are important measures. Again, application examples are in-vehicle devices, sensors and consumer electronics.

Compare with general purpose cryptographic algorithms, lightweight cryptographic primitives which relax implementation requirements have more advantages in those scenarios. In this paper, we mainly talk about block ciphers which are the most versatile of the symmetric ciphers. Lightweight block ciphers can overcome limitations of gate count in small chips, for examples a state of the art AES-128 [1] hardware implementation uses 2400 GE (Gate Equivalent) [7], while PRESENT-128 [5], LED-128 [3,4] and SIMON-128 [6] can respectively offer a 1391 GE [8], a 1265 GE [4] and a 1234 GE [6] implementation. As the gate count is small, energy consumption is small. In applications where instantaneous response is highly desired, lightweight primitives such as PRINCE [2] and SIMON can achieve same or less latency of AES with respectively 1/40 and 1/52 gate counts at 130 nm low-leakage Faraday libraries. In other applications, such as sensor nodes or RFID tags, the equipped inexpensive microprocessor and microcontroller typically have a limited power budget and severely constrained memory (RAM and flash). For example, the ATtiny45 [11] has just 4 KBytes of flash, 256 bytes of RAM. There are lightweight ciphers, such as PRIDE [9] that can use no RAM and achieve similar throughput of AES with 1/2 flash bytes.

Over the last decade, cryptographic community has made significant efforts in the development of lightweight block ciphers. Following as a result, there are now more than a dozen of lightweight block ciphers for industry to choose from, including PRESENT [5] and CLEFIA [12], which have become ISO/IEC lightweight block cipher standards, and many other lightweight block ciphers, such as HIGHT [13], KATAN/KATANTAN [14], KLEIN [15], LBlock [16], LED [3], TWINE [17], PRINCE [2], SIMON and SPECK [6], PRIDE [9], RECTANGLE [18] etc. They are all excellent with respect to certain features. We refer to a web page [19] for a complement lightweight block cipher list. Consequences are the work and projects to improve and evaluated the performance of those lightweight block ciphers. With respect to software implementation on microcontrollers, there are several survey papers and open projects provide benchmarking results and reports on the performance of lightweight block ciphers [20–33].

On [25], a web page of ECRYPT II project, compact implementation and performance evaluation of 12 low-cost block ciphers on AVR ATtiny45 8-bit microcontroller are presented. The set of analyzed ciphers includes the low-cost ciphers designed until the corresponding paper [24] publication and thus it does not contain recent designs. The authors introduce a comparison metric that takes into account both the code size (ROM and RAM), the cycle count and the energy consumption. Implementation of the 12 ciphers comes from 12 different designers and codes are written in assembly. Both encryption, decryption and key management routines have to be implemented, and there is no usage scenarios (message length and mode of operation) involved. The authors of [29]

implemented 21 low-cost (5 classical and 16 lightweight) block ciphers on the WSN430 sensor which is based on 16-bit TI MSP430 microcontroller. This is the biggest collection of low-cost ciphers implementations available on 16-bit microcontroller. However, as [32] points out, some of the implemented ciphers do not verify the test vectors. Both of the two above projects are not active for a long time.

Recently, a new benchmarking framework [32] was presented at the NIST Lightweight Cryptography Workshop 2015 [36]. Learn from the strengths and weakness of those previous benchmarking frameworks, the authors manage to design a more flexible and powerful framework for evaluation of lightweight ciphers on different embedded devices commonly used in the IoT context. By the publication, they have studied software performance of 13 lightweight block ciphers on three different devices, 8-bit AVR, 16-bit MSP and 32-bit ARM. Their evaluation consideration involves two most typical usage scenarios that resemble security-related operations commonly performed by real-world IoT devices. They also maintain a web page [34] with the most recent results. Triathlon challenge [33] are announced to improve those results and collect more implementations and more performance evaluations of more newer designs. They introduce a “Figure of Merit” (FOM) according to which an overall ranking of ciphers can be assembled.

Based on their current results in [32], the NSA designs Simon and Speck, AES and LS-designs are among the smallest and fastest ciphers on all platforms. Unfortunately, PRINCE which is superior as for low-latency and LED which is very compact as for hardware implementation get the lowest rank. Some newly proposed designs are also not included in their list, such as RECTANGLE [18] which is published in 2014 and presented at the NIST Lightweight Cryptography Workshop 2015 [36].

In this paper, we aim to contribute to the performance benchmarks of PRINCE, LED and RECTANGLE on 8-bit microcontrollers. Generally speaking, we expect to improve the performance of those ciphers on 8-, 16- and 32-bit microcontrollers. While, it seems reasonable to begin with 8-bit microcontroller, since the performance of those ciphers on 16- and 32-bit microcontrollers will be much better than that they can achieve on the 8-bit, and 8- and 16-bit microcontrollers constituted an overwhelming part of the total microcontroller market [35]. Moreover, optimizations on the 8-bit microcontrollers can have strong reference meanings for that on the 16- and the 32-bit.

1.1 Related Work

For nibble-oriented and byte-oriented ciphers, people usually use look up tables (LUTs), which may need large memory to achieve high throughput. Both of PRINCE and LED can be seen as nibble-oriented. Specifically, the original components of the ciphers can be described as operations on nibbles (intra-nibbles and inter-nibbles). For PRINCE, there are two related efforts which aim to improve the software performance on 8-bit AVR microcontrollers. In the first work [37], two implementations of PRINCE are presented. The first is T-table implementation which combines different operations within a round into a single

table lookup operation. The second is block-parallel implementation which stores two nibbles in one register and processes them in parallel wherever possible. The S-boxes are stored as two 256-byte tables. In these two implementations, LUTs are too large to store in RAM. Thus they are coded in the programmable flash memory to which each access takes 1 more clock than that takes to the RAM.

The second work [38] presents a nibble-sliced implementation which stemming from bitslicing. Nibble-slicing is custom-made for nibble-oriented permutation layers. Similar to the block-parallel implementation in the first work, two nibbles are stored in one register. However, there is a difference between the two work: the block-parallel implementation processes nibbles within one block in parallel, while the nibble-sliced implementation processes two blocks in parallel, specifically, two nibbles in the same position of two blocks are stored in one register. Thus, it needs 16 registers to store states of two blocks. As in the first work, the second work also uses byte-oriented LUTs, which are 256-byte tables stored in flash memory for the S-boxes computation. Due to the nibble-slicing manner, the S-boxes computation and the SR operations can be merged together, which helps to reduce execution time. In the second work, cycle count and memory consumption are derived using AVR Studio simulations. Code in both of the two work was implemented in assembly. Performance evaluation in the first work involved cycles and code for nibble reordering, while it is unclear whether cycles and code for the nibble slicing are taken into account in the second work. Usage scenarios are not considered in both of the two work.

Work to improve the performance of LED on 8-bit AVR microcontrollers is quite rare. We can only refer to [34] for open source software implementation of LED on 8-bit microcontrollers. Unfortunately, the performance achieved by those C implementations in [32,34] are quite unsatisfactory.

1.2 Our Contributions

This work aims to improve the software performance of PRINCE and LED on 8-bit microcontrollers in two usage scenarios. By using bitslice technique instead of LUTs, we can minimize the requirement for memory and at the same time keep high throughput. In our implementations, by inventively rearrange the state bits, each message block can be processed in fine granularity parallel. By minimizing the number of instructions needed by each operation (S-boxes, MixColumns, ShiftRows etc.) of these ciphers, high throughput and low memory usage are achieved at the same time. Thus, these implementations can be used in serial message processing scenarios (corresponds to Scenario 1 in Section 2) in which the work [38] is hard to be used. It is quite natural to processing two blocks in parallel using our bitslice methods. Thus, in scenarios where message blocks can be processed simultaneously (corresponds to Scenario 2 in Section 2), our implementations also reduce the memory usage and execution time.

With respect to PRINCE, in Scenario 1, we achieve **2.88** \times boost in throughput with **1/1.23** RAM and **1/2.18** flash memory comparing with [32], achieve **1.28** \times boost in throughput comparing with [37]. In Scenario 2, we achieve **4.67** \times boost in throughput with the same RAM and **1/2.09** flash comparing

with [32], achieve similar throughput with **1/9.17** RAM and similar flash comparing with [38]. For LED, comparing with [32], our implementation achieves **6.12** \times boost in throughput with **1/2.09** RAM and **1/2.17** flash in Scenario 1, and **11.27** \times boost in throughput with the same RAM and **1/2.72** flash in Scenario 2. As shown in this work, PRINCE which gets a low rank in [32] is actually very efficient on 8-bit AVR devices.

We also aim to contribute performance benchmarks in the real-world usage scenarios of a newly proposed cipher RECTANGLE. Our results show that RECTANGLE gets very high ranks in those scenarios and can parallel SIMON in performance, see Table 3.

Table 1. Results for Scenario 1 (encryption of 128 bytes of data using CBC mode)

Cipher	Implementation	Code [Bytes]	RAM [Bytes]	Time [Cycles]
I: Encryption + Decryption (including key schedule)				
PRINCE	Triathlon [32]	5358	^c (374 – 70) 304	243396
	This work^a	2454	248	84656
LED	Triathlon [32]	5156	^c (574 – 88) 486	2221555
	This work^a	2374	232	362889
RECTANGLE	This work	682	310	60298
II: Encryption (without key schedule)				
PRINCE	Triathlon [32]	4210	^c (174 – 46) 128	121137
	Block-Parallel [37]	^b 1574	^b 24	^b 52048
	This work^a	1746	0	40736
LED	Triathlon [32]	2600	^c (242 – 66) 176	1074961
	This work^a	1412	0	180384
RECTANGLE	This work	250	0	29148
III: Decryption (without key schedule)				
PRINCE	Triathlon [32]	4352	^c (198 – 70) 128	122082
	This work^a	1746	0	40976
LED	Triathlon [32]	3068	^c (280 – 88) 192	1146226
	This work^a	1414	0	182128
RECTANGLE	This work	252	0	29788

^aState rearrangement operations on plaintext, ciphertext and round-keys are all included.

^b[37] evaluates the encryption of one block (3253 cycles), and the cost of dealing with the encryption mode is not included. We use $3253 \times 16 = 52048$ to estimate the cycles count.

^cIn this table and in Tables 2 and 3, we subtract the stack consumption from the RAM usage of implementation in [32,34] to make a comparison considering the problem explained in Sect. 6.

Table 2. Results for Scenario 2 (encryption of 128 bits of data using CTR mode)

Cipher	Implementation	Code [Bytes]	RAM [Bytes]	Time [Cycles]
PRINCE	Triathlon [32]	4420	(68 – 44) 24	17271
	Nibble-Slice [38]	^a 2382	^a 220	^a 3606
	This work (FixOrder)	2118	24	3696
	This work (ReOrder)	2642	24	4236
LED	Triathlon [32]	2602	(91 – 67) 24	143317
	This work (FixOrder)	956	24	12714
	This work (ReOrder)	1480	24	13254
RECTANGLE	This work (LessTime)	582	24	3405
	This work (LowFlash)	428	24	3995

^aIn [38] (processing two blocks in parallel in nibble-slicing), it is unclear whether cost of reordering the nibbles and dealing with the encryption mode are considered.

Table 3. Updated results for ciphers performance in Scenario 1 and Scenario 2

Scenario 1 (encryption of 128 bytes of data using CBC mode)					Scenario 2 (encryption of 128 bits of data using CTR mode)				
Cipher	Code [Bytes]	RAM [Bytes]	Time [Cycles]	p_i	Cipher	Code [Bytes]	RAM [Bytes]	Time [Cycles]	p_i
Speck ^b	560	280	44264	3.21	Speck ^b	294	24	2563	3.00
Simon ^b	566	320	64884	3.86	Simon ^b	364	24	4181	3.87
REC ^b	682	310	60298	3.92	REC ^b	428	24	3995	4.01
PRIN ^b	2454	248	84656	7.36	AES ^a	1246	(81 – 49) 32	3408	6.90
AES ^a	3010	(408 – 70) 338	58246	8.15	LED ^b	956	24	12714	9.21
PRES ^a	2160	(448 – 46) 402	245232	11.13	PRIN ^b	2118	24	3696	9.65
LED ^b	2374	232	362889	13.44	PRES ^a	1294	(56 – 32) 24	16849	11.97

$p_i = \sum_{m \in M} (w_m \times \frac{v_{i,m}}{\min_i(v_{i,m})})$, where $M = \{\text{the code, the RAM, the cycles}\}$, $w_m = 1$ [32].

^aResults for assembly implementations in [34]. ^bResults for assembly implementations by this work.

Tables 1 and 2 summarize our results on the performance of PRINCE, LED and RECTANGLE in Scenario 1 and Scenario 2, in which we also include the results of previous work to make comparisons.

The rest of the paper is organized as follows. Section 2 clarifies our target device, considering scenarios and performance measurement metrics. Sections 3, 4 and 5 respectively demonstrate how to achieve high software performance of PRINCE, LED and RECTANGLE on the AVR 8-bit microcontrollers using bit-slice technique. For each cipher, after a brief description, we exhibit how to rearrange the state bits, and how to implement its main operations in bitslicing with minimal number of instructions in two usage scenarios. Section 6 summarizes the results of this work.

2 Our AVR Implementations, Considering Scenarios and Performance Measurement

The specific target device in this work is the AVR ATmega128 8-bit microcontroller, which has 128 KBytes of flash, 4 KBytes of RAM and 32 8-bit general purpose registers. The ATmega128 uses an 8-bit RISC microprocessor. The arithmetic and logical instructions are usually destructive source operand, i.e. destination register is one of the source registers. And most of the numeric processing instructions take one clock cycle. Instructions which load data from and store data to RAM take 2 clock cycles and that access to flash memory take 3 clock cycles. Opcode of most instructions uses 2 bytes, some special types uses 4 bytes. For a detailed introduction of 8-bit AVR instructions, please refer to [10,32]. To achieve optimal performance, we code the ciphers in assembly and the assembly code was written in and compiled using Atmel Studio 6.2. Cycle counts, code sizes and RAM usage are also determined using this tool.

For each cipher, we have implementations targeting to two scenarios which are introduced in [32].

Scenario 1 - Communication Protocol [32]. This scenario covers the need for secure communication in sensor networks and between IoT devices. Sensitive data is encrypted and decrypted using a lightweight block cipher in CBC mode of operation. Data length exchanged in a single transmission is fixed to 128 bytes. The master key is stored in the device’s RAM, from which, round keys are computed using the key schedule and then stored in RAM for later use. The key schedule does not modify the master key. The data that have to be sent as well as the initialization vector are also stored in RAM. Encryption is performed in place to reduce the RAM consumption.

Scenario 2 - Challenge-Handshake Authentication Protocol [32]. This scenario covers the need of authentication in the IoT. In the authentication protocol, the block cipher is used in CTR mode to encrypt 128 bits of data. The device has the cipher round keys stored in Flash memory and there is no master key stored in the device and consequently no key schedule is required. The data that has to be encrypted is stored in RAM, as well as the counter value. To reduce the RAM usage, the encryption process is done in place.

We consider the same three metrics of ciphers performance as considered in [32], including code size, RAM and execution time. Code sizes include the value of the Code and Data sections. Code section contains the bytes used by the binary code, Data section contains global initialized variables (such as the flash used by round constants etc.). The measurements do not consider the main function’s code size, where all the cipher operations are put together. RAM usage includes scenario specific RAM data, such as data to encrypt, master keys, round keys and initialization vectors. The execution time is expressed in number of processor cycles spent executing those procedures, such as encryption, key schedule or decryption. In addition, our measurement includes the cost taken by rearrangement operations on the plaintexts, ciphertexts and round keys.

3 PRINCE AVR Implementations

In this section, we present the first (to our knowledge) bitsliced implementation of the PRINCE cipher on 8-bit AVR microcontroller.

3.1 The PRINCE Cipher

PRINCE operates on 64-bit blocks and uses a 128-bit key k which composed of two 64-bits elements, k_0 and k_1 . It is based on the so-called FX-construction. The 128-bit key is extended to 192 bits by the mapping: $(k_0||k_1) \rightarrow (k_0||k'_0||k_1) = (k_0||(k_0 \ggg 1) \oplus (k_0 \ggg 63))||k_1$. k_0 and k'_0 are used as whitening keys, while k_1 is the 64-bit key used without updates by the 12-round block cipher refer to as PRINCE_{core}. PRINCE has an α -reflection property. Decryption can reuse the exact same procedure of encryption by simply XOR a constant α to the third element k_1 of the extended key and exchange the used order between k_0 and k'_0 . While, both procedures use the inverse round function as well as the round function.

The round function of PRINCE is AES-like, operates on a 4×4 state matrix of nibbles, which can be seen as composed of the following operations: KeyXor (correspond to k_i -add in the cipher specification) and RCXor (corresponds to RC_i -add), S-box (corresponds to S-Layer), MixColumns (corresponds to The Matrices M' -layer) and ShiftRows (corresponds to SR , and $SR \circ M' = M$ which is called the Linear Layer), among which only MixColumns is an involution. Thus, the implementations of the PRINCE have to instantiate the following operations: the KeyXor and RCXor, the S-box and inverse S-box, the MixColumns, the ShiftRows and Inverse ShiftRows. For more details about PRINCE please refer to [2].

We implement all of those operations in bitslicing, while all previous work is nibble-oriented and based on LUTs. Before the demonstration of those bitsliced implementations of each operation, we show how we slice the state.

3.2 PRINCE AVR Implementations

State Bits Rearrangement. The original arrangement of the state can be seen in Fig. 1. In this arrangement, successive four bits from right to left is called a *nibble*, successive four nibbles from right to left is a *row*. Successive four bits from top to bottom is a *slice*, successive four nibbles from top to bottom is a *column* [40]. Bits are indexed in the form of xyz , where x is the column index (0 to 3 right-to-left), y is the row index (0 to 3 top-to-bottom) and z is the slice index (0 to 3 right-to-left) within a column. Then the right up corner can be seen as the origin of the state.

To bitsliced implement the operations, we gather the bits with index $*yz$, i.e. bits with same row index and same slice index are gathered together. We call the resulted bit set a *lane*¹, in which all bits will be settled in the same register in our implementations. And we rearrange the state in a way as depicted in Fig. 2a.

¹ This name is borrowed from names of KECCAK-f state parts [42].

<i>row</i>	303'302'301'300	203'202'201'200	103'102'101'100	003'002'001'000
	313'312'311'310	213'212'211'210	113'112'111'110	013'012'011'010
	323'322'321'320	223'222'221'220	123'122'121'120	023'022'021'020
	333'332'331'330	233'232'231'230	133'132'131'130	033'032'031'030
	<i>nibble</i>	<i>column</i>	<i>bit</i>	<i>slice</i>

Fig. 1. The original arrangement of the state of bits for PRINCE

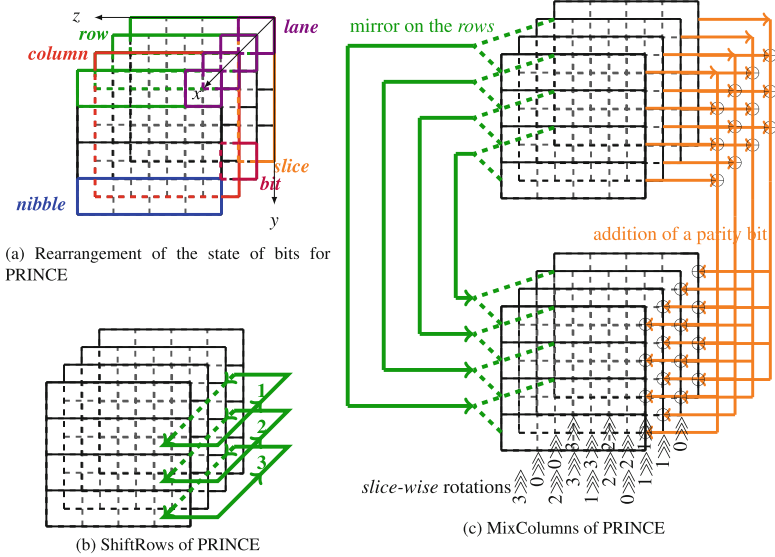


Fig. 2. Rearrangement of the state of bits, ShiftRows and MixColumns of PRINCE

We then use the following conventions. Let \mathbf{S} denotes the complete state, then $\mathbf{S}[* , y , z]$ denotes a particular lane. In implementations for Scenario 1, two lanes of one state $\mathbf{S}[* , y , z]$ and $\mathbf{S}[* , y + 2 , z]$ ($y \in \{0, 1\}$, $z \in \{0, \dots, 3\}$) are stored in one register, in the lower half and the high half respectively. In Scenario 2, two lanes of two states $\mathbf{S}[* , y , z]$ and $\mathbf{S}'[* , y , z]$ ($y \in \{0, \dots, 3\}$, $z \in \{0, \dots, 3\}$) are stored in one register to process two blocks in parallel.

The rearrangement of the state takes 2 clocks per bit using rotate through carry instructions (ROL and ROR). Thus, rearranging the input state and back rearranging the output state take 4 clocks per bits.

Bitsliced Implementation of the KeyXor and RCXor. Since we have rearranged the encryption state, we should also rearrange the key and the round constant state in the same way. The KeyXor and RCXor operations can be merged together. In Scenario 1, during the key schedule procedure, the master

key is extended and the resulted 3 sub-keys are rearranged and XORed to the pre-rearranged round constants to generate round-key-constant materials. The resulted round-key-constant materials are then stored in RAM. In Scenario 2, the resulted round-key-constant materials is extended (to encrypt two blocks in parallel) and coded in flash memory.

Bitsliced Implementation of the S-Box and the Inverse S-Box. By rearranging the state bits, we can implement the S-box and inverse S-box using logical operations instead of LUTs. In our rearrangement, 4 lanes within one row respectively correspond to the 4 input-outputs of S-boxes, thus 8 S-boxes can be computed in parallel using a logical instruction sequence operating on 8-bit registers, since 2 lanes share one register.

We firstly managed to find the bitsliced implementation of the 4×4 S-box (resp. inverse S-box) of PRINCE using an automatic search tool [41]. Operations in the resulted bitsliced implementations use the ‘*operator destination, source₁, source₂*’ instruction format. While in AVR ATtiny, instructions destination register is one of the source register, i.e. it uses ‘*operator destination, source*’ instruction format. Thus, we translate the primary instruction sequences into two-operator instruction sequences manually. In our translation, we try to minimum the required clock cycles and realize in place process, i.e. the outputs are in the same registers as the inputs.

The primary bitsliced implementation of the S-box (resp. inverse S-box) of PRINCE need 17 (resp. 16) terms. Translating into AVR instructions, it turns to be an instruction sequence with length of $17 + 4 = 21$ (resp. $16 + 6 = 22$) with 4 (resp. 6) additional copy register (MOV) instructions. Taking advantage of the copy register pair (MOVW) instruction, and processing 16 S-boxes together instead of 8 S-boxes, the S-layer (inverse S-layer) of PRINCE needs $17 \times 2 + 4 = 38$ (resp. $16 \times 2 + 6 = 38$) instructions, instead of $21 \times 2 = 42$ (resp. $22 \times 2 = 44$).

Bitsliced Implementation of the MixColumns. According to observations on the linear layer of PRINCE in [39, 40], MixColumns of PRINCE can be seen as being composed of three compositions: mirror on the *rows*, addition of a parity bit, *slice-wise* rotations by 0,1,2 or 3 positions. Thus, it can be expressed as the parallel application of 16 independent transformations operating on one *slice* of the internal state. Figure 2c explains those transformations in a 3-dimensional way.

In our way of state bits rearrangement, 4 bits in same position within 4 different *slices* are stored in same register. Thus, parity bits of 8 *slices* can be computed in parallel. Mirror on the *rows* and *slice-wise* rotations can be combined to be a bits exchanging among different *lanes*.

In our implementation for Scenario 1, since the lower half and the high half of one register hold lanes in two rows (lane $\mathbf{S}[* , y, z]$ and lane $\mathbf{S}[* , y+2, z]$), addition of parity bit takes 7 instructions for 4 slices. Thus, addition of parity bit for the whole state takes 28 instructions per state. Since column $\mathbf{S}[0, *, *]$ and column $\mathbf{S}[3, *, *]$ in state \mathbf{S} of PRINCE go through same MixColumns operations M_0 ,

slice $\mathbf{S}[0, *, z]$ and slice $\mathbf{S}[3, *, z]$ within column $\mathbf{S}[0, *, *]$ and column $\mathbf{S}[3, *, *]$ go through same mirror and rotation operations for $z \in \{0, \dots, 3\}$. Thus, bit 0 and bit 3 in a register, and bit 4 and bit 7 in a register go through same operations. Likewise, since column $\mathbf{S}[1, *, *]$ and column $\mathbf{S}[2, *, *]$ in state \mathbf{S} go through same MixColumns operations M_1 , bit 1 and bit 2 in a register, and bit 5 and bit 6 in a register go through same operations. Finally, we achieve a 4-way parallel implementation for the combination between mirror on the *rows* and *slice-wise* rotations. That takes $2 \times 9 + 2 \times 8 = 34$ instructions per state.

In our implementation for Scenario 2, since the lower half and the high half of one register hold some lanes in two states (lane $\mathbf{S}[* , y, z]$ and lane $\mathbf{S}'[* , y, z]$), addition of the parity bit takes 8 instructions for 8 slices. Thus, addition of parity bit for the whole state takes 32 instructions for two states (thus 16 instructions per state). Similar to the implementation for Scenario 1, the 0, 3rd, 4th and 7th bit in a register go through same operations, and the 1st, 2nd, 5th and 6th bit in a register go through another set of operations. We also achieve 4-way and 8-way parallel implementations for the combination between mirror on the *rows* and *slice-wise* rotations. That takes $4 \times 16 = 64$ instructions for 2 states (thus 32 instructions per state).

On the whole, in respect of Scenario 1, the MixColumns takes $28 + 34 = 62$ instructions per state. And in respect of Scenario 2, the MixColumns takes $16 + 32 = 48$ instructions per state.

Bitsliced Implementation of the ShiftRows and the Inverse ShiftRows.

In our way of state bits rearrangement, ShiftRows and Inverse ShiftRows correspond to rotate bits in *lanes*, which are depicted in Fig. 2b. Thus that needs to rotate high the half and the lower half of 8-bit registers separately in our implementation. We implement this by logical AND (AND), logical shift left and right (LSL and LSR), bit load from the T flag in SREG to a bit in register (BLD) and bit store from bit in register to T flag in SREG (BST) instructions.

With respect to Scenario 1, it takes $4 \times 19 = 76$ instructions to implement ShiftRows (or Inverse ShiftRows) per state. With respect to Scenario 2, it takes $4 \times 19 + 2 = 78$ instructions to implement ShiftRows (or Inverse ShiftRows) per 2 states (thus 39 instructions per state).

4 LED AVR Implementations

In this section, we present the first (to our knowledge) bitsliced implementation of the LED cipher on 8-bit AVR microcontroller.

4.1 The LED Cipher

LED is a 64-bit block cipher, uses a key size from 64 to 128 bits, bases on an substitution-permutation network (SPN). The two primary instances, 64-bit key LED (named LED-64) and 128-bit key LED (named LED-128), respectively has 32 rounds and 48 rounds. In this paper, we will focus on LED-128. The

key schedule of LED is very simple. In the case of LED-128, the master key k is composed of two 64-bit subparts, $k = k_1 || k_2$, alternatively XORed to the internal state every 4 rounds. The 4-round operation between two key addition is called a *step*. The whole encryption process of LED is described using key addition and *step* operation.

Similar to the round function of PRINCE, the round function of LED is also AES-like, which operates on a 4×4 state matrix of nibbles. It also uses the following operations AddConstants (round constant addition), SubNibbles (corresponds to SubCells in [4]), ShiftRows, and MixColumnsSerial. None of those operations is involution. Thus, we should also implement their inverse operations. For more details about LED, please refer to [4].

4.2 LED AVR Implementations

State Bits Rearrangement. We follow the same naming convention for PRINCE state mentioned above in Fig. 2a to define the names of parts of LED state. Our rearrangement of LED state is quite similar to that of PRINCE state. A difference is that, in Scenario 1, each lane of LED state is stored in a whole 8-bit register, i.e. only the high half of the 8-bit register holds meaningful bits. Thus, 16 lanes $S[*, y, z]$ are respectively stored in 16 8-bit registers, leaving the lower half part of register empty. In Scenario 2, the lower half part of those 16 registers hold 16 lanes in another block state.

Bitsliced Implementation of the MixColumnsSerial. In MixColumnsSerial, each column of the internal LED state is transformed by multiplying it once with MDS matrix M , where $M = A^4$. It can also be viewed as four serial applications of a hardware-friendly matrix A , which can be implemented using XOR and bit-permutation. Bit-permutation is free in hardware, but usually not free in software implementations. However, by observing the iterative processing procedure of $M = A^4$, which is depicted in Fig. 3, we find that after 4 times of matrix multiplication, the four bits in each nibble switched from the order (3,2,1,0) to the order (1,0,3,2). Since each register in our implementation stores bits at same position within different nibbles, this switching operation corresponds to an exchanging operation between registers. Since bits needed to be exchanged are located in same nibble, this switching operation can be combined with the S-box operation, thus there is no need to exchange registers in real. Thus, we can implement the MixColumnsSerial using sequential XOR instructions, and implement a bit-permutation variant of the original S-box. In addition, because of the four columns of the LED state go through same MixColumnsSerial operation, and due to our rearrangement of the state of bits, MixColumnsSerial operations on four columns are done in parallel. In Scenario 1, we achieve a 4-way parallel implementation which needs 64 instructions per state, and in Scenario 2, we achieve an 8-way parallel implementation using 64 instructions for two states.

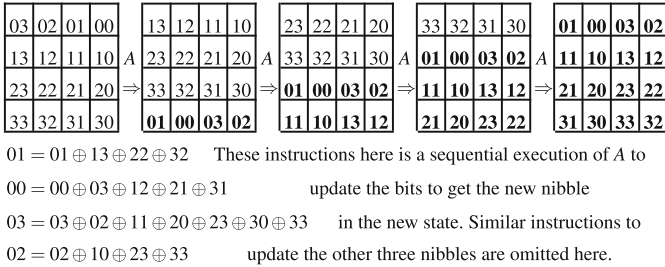


Fig. 3. MixColumnsSerial of LED operate on one column

Bitsliced Implementation of the S-Box and the Inverse S-Box. LED uses the PRESENT Sbox. There are previous work in which bitsliced implementation of PRESENT Sbox is studied. In [38], the authors aim to improve the throughput of PRESENT using bitslice technique. Their 19-instruction AVR implementation of the PRESENT S-box based on the 14 terms representation found by Courtois in [43]. Using the automatic search tool [41], we try to find optimal bitsliced implementations of both PRESENT S-box and the inverse S-box. The best solutions also need 14 terms for PRESENT S-box and it needs 15 terms for the inverse S-box.

Similar to our work on PRINCE S-box, we also try to find the best translation from those general solutions to instruction sequences in AVR instruction set. Through our manual optimization, there are 4 additional instructions (mov) penalty to implement the S-box on AVR based on the 14 terms (resp. 15 terms) sequences. When take advantage of the MOVW instruction, and deal with two sets of 8-bit registers together, 32 instructions (resp. 34 instructions) are needed to finish 16 S-boxes (in Scenario 1, since the lower part of a register is left empty, it takes 64 instructions to execute 16 S-boxes).

As mentioned above, our implementation of MixColumnsSerial for LED does not execute the last switching operation, instead, we combine this switching operation with the S-box operation. To encrypt, the input of S-boxes are switched between bit 0 and bit 2, and between bit 1 and bit 3. To decrypt, the output of inverse S-boxes are switched similarly. Thus, in our implementation, we actually implement a bit-permutation version of the S-box and the inverse S-box, and the final instruction number is 33 for the 16 input-switched S-boxes and 34 for the 16 output-switched inverse S-boxes.

Bitsliced Implementation of the ShiftRows and the Inverse ShiftRows. ShiftRows and the Inverse ShiftRows of LED are same with that of PRINCE. The difference between the implementations of the two ciphers is caused by the difference in the arrangement of the state bits in Scenario 1. $4 \times 12 = 48$ instructions are needed in Scenario 1 to rotate 16 lanes in one state and $4 \times 19 = 76$ instructions are needed in Scenario 2 to rotate 32 lanes in two states (thus 38 instructions to rotate 16 lanes in average).

5 RECTANGLE AVR Implementations

Presented at [36], RECTANGLE [18] is the most recent cipher discussed here, which is not involved in the analyzed cipher list in [32]. Thus, in this paper, we aim to provide a software performance benchmark for this cipher to [34].

5.1 The RECTANGLE Cipher

RECTANGLE operates on 64-bit cipher state. The key length can be 80 or 128 bits. In this paper, we mainly focus on the 128-bit key version (named RECTANGLE-128). The encryption is also based on an SP network. The substitution layer consists of 16 4×4 S-boxes in parallel, which is called SubColumn. The permutation layer is composed of 3 rotations, which is called ShiftRows. For more details about RECTANGLE, please refer to [18].

5.2 RECTANGLE AVR Implementations

State Bits Arrangement. Since the main idea of the design of RECTANGLE is to allow fast implementations using bitslicing techniques, the state arrangement in the bitsliced implementation is quite straightforward. Each 16-bit row of the cipher state is held by 2 registers, thus 8 registers are needed to hold the cipher state.

Bitsliced Implementation of the S-Box and the Inverse S-Box (SubColumns). Similar to our work on PRINCE and LED S-box, we first find the optimal general bitsliced implementations of the S-box and the inverse S-box, both of which requires 12 terms. Then we try to get the best translation from those general solutions to instruction sequences in AVR instruction set. Our manual optimization needs 2 (resp. 3) additional instructions (mov) penalty to implement the S-box (resp. inverse S-box) on AVR. When take advantage of the MOVW instruction, and deal with two sets of 8-bit registers together, $26 = 12 \times 2 + 2$ (resp. $27 = 12 \times 2 + 3$) instructions are needed to finish 16 S-boxes.

Bitsliced Implementation of the ShiftRows. The 1-bit rotation of the 16-bit row can be carried out using AVR's logical shift left (LSL), rotate left through carry (ROL) and add with carry (ADC) instructions, together with an all 0 register. We mainly focus on implementing the 12-bit and 13-bit rotation of the 16-bit row with a minimized number of instructions. Thanks for our optimization on the 4-bit rotation (both left and right) of 16-bit row using swap nibbles (SWAP), copy register pair (MOVW), logical AND with immediate (ANDI) and exclusive OR (EOR) instructions and 2 temporary registers, it only needs 7 instructions to perform 12-bit rotation (both left and right) of the 16-bit row. Thus the total ShiftRows and the inverse ShiftRows only need 20 instructions per state.

Bitsliced Implementation of the Key Schedule and Adding Round Key. The 128-bit key state are arranged as a 4×32 matrix. The key schedule for RECTANGLE-128 consists of applying the 4×4 S-boxes to the 8 rightmost columns of the four 32-bit rows of the key state, 1-round generalized Feistel transformation on the 4 rows and 5-bit round constant XORing on a single row. The 64-bit round key rk consists of the 16 rightmost columns of the four 32-bit rows.

In our implementation, applying the 4×4 S-boxes to the 8 columns takes 14 logical instructions (28 bytes and 14 cycles), the 1-round generalized Feistel transformation takes 18 instructions (36 bytes and 18 cycles), the 5-bit round constant XORing takes 2 instructions (4 bytes and 4 cycles). There are two key bytes shared between every two successive round keys. According to this observation, we can use $8 + 25 \times 6$ bytes instead of 26×8 bytes to store 26 round keys. Meanwhile, by reordering the key bytes and using two additional registers, we can use 6 load instructions instead of 8 when adding the 8-byte round keys during encryption and decryption.

Our results are consistent with that shown in [18], while evaluation in this paper considers the two typical real-world usage scenarios. In addition, we develop a high throughput implementation (LessTime) and a low flash implementation (LowFlash) in Scenario 2. In the high throughput implementation, two blocks are processed simultaneously. Thus, it allows to load the subkeys one time every two blocks and reduce the cycles by sacrificing 146 bytes of flash than that in the low flash implementation which processes blocks one by one using a loop.

6 Results Summary and Comparisons

The vast majority of instructions used in our bitsliced implementations are types of instruction which takes one clock cycle and 2 bytes. And there is no memory access except for load inputs, load round keys, load round constants and store outputs. We write the whole program in assembly code. And executions of operations in our implementations are all in place in registers. Thus, there is no extra RAM used to store local variables during the whole executions of encryption, decryption and key schedule. While, that inevitably gives rise to difficulty when making a comparison with the inline assembly implementation in [32] or [34], in which stack RAM is needed and PUSH and POP instructions are used to store and restore all modified registers. Thus, in Tables 1, 2 and 3, we subtract the stack consumption from the RAM usage of implementation in [32] or [34] to make a comparison. Besides, it would be hard to process blocks in parallel if comply with the C interface provided in [31].

All of our implementations have verified the test vectors provided in the cipher specifications, and the source codes are available on a web site [45].

For Scenario 1, our implementations include the key schedule and encryption, inverse key schedule (when needed) and decryption procedures. State rearrangement operations on the plaintext, ciphertext and round-keys are all included

in our measurement. For Scenario 2, we only need to implement the encryption procedure, no decryption and no key schedule procedure are needed. Since encryption of 128-bit data using CTR mode, data is XORed with the output of the encryption procedure with counters as the input. There are two conventions on the usage of the two counters in our implementation for PRINCE and LED, because we rearrange the input of the encryptions. In the first convention, these two counters must be rearranged before going through the encryption procedure and must be back rearranged after the encryption procedure before XORed to the 128 bits message. We denoted this convention ReOrder. In the other convention, we encrypt the two counters directly and XOR the output with the 128-bit message without rearrangement of the state bits. We denoted this convention FixOrder. In our opinion, FixOrder convention does not relate to the security issues and is more efficient, thus it can be used as the final performance benchmark.

Our results on the performance of PRINCE, LED and RECTANGLE are summarized in Tables 1 and 2, in which we also include the results of previous work to make comparisons. In addition, we have also implemented Simon and Speck in assembly according to the method provided in [44]. If use our results to update the results in [34], we get Table 3. Since AES and PRESENT are coded in assembly, we only include this two ciphers to make comparisons. As shown in Table 3, RECTANGLE get a higher rank than AES and slightly lower rank than SIMON both in Scenario 1 and Scenario 2. PRINCE and LED respectively get a higher rank than AES in Scenario 1 and higher rank than PRESENT in Scenario 2. We believe that comparison in [34] is inevitable unfair since only AES, PRESENT, SIMON and SPECK are coded in assembly. Several other ciphers may also get a performance improvement if coded in assembly. And as pointed above, there is also unfairness when making a comparison between an implementation using pure assembly code and an implementation using inline assembly code. Besides, it is difficult to compare the performance between ciphers which supports parallelization and which does not. We remain the optimization work on other ciphers and a more fair comparison to the future.

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