# **Image Classification Using Spatial Difference Descriptor Under Spatial Pyramid Matching Framework**

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**Abstract.** Spatial pyramid matching (SPM) model is an extension of the bagof-visual words (BoW) model for local feature encoding. It firstly partitions the image into increasingly fine sub-regions, and then concatenates the histograms within each sub-region. However, the SPM model does not consider the spatial information differences between sub-regions explicitly. To make use of this information, we exploit a novel descriptor called spatial difference. In the process of promoting the performance of image classification, this descriptor is mainly used to concatenate the histograms of bag-of-visual words model under spatial pyramid matching framework. Finally, we conduct image classification experi‐ ments on several public datasets to demonstrate the effectiveness of the proposed scheme.

**Keywords:** Image classification · Spatial difference descriptor · Spatial pyramid matching · Bag-of-visual words · Sparse coding

### **1 Introduction**

In recent years, the bag-of-visual words (BoW) model [\[1](#page-12-0)] has been very popular in various image applications, especially for image classification. Codebook generation and histogram representation are two important components for generating bag-ofvisual words representation. Bag-of-visual words model has been demonstrated that combining codebook and histogram representation together can achieve good performance after being trained to predict the classes of images.

Though bag-of-visual words model has achieved good performance, there exist obvious drawbacks: both the spatial information and correlations among visual contents are neglected. Later, a spatial pyramid matching (SPM) model [[2](#page-12-0)] was proposed to deal

with this problem by dividing the whole image into hierarchical sub-regions and concatenating the appropriately weighted histograms of each region. Extensive experimental results have shown that spatial pyramid matching model achieved a remarkable success on a wide range of image classification benchmarks as a fundamental model. However, spatial pyramid matching model has its own weaknesses: the finer the division, the more sensitive it is to location and orientation of visual content, as described in [[3\]](#page-12-0). In view of this, many works focused on improving SPM to overcome these weaknesses, such as researchers [\[3–6](#page-12-0)] tried to improve the coding procedure to minimize the representation information loss. Teng et al. [\[3](#page-12-0)] explored a weakly spatial symmetry descriptor to boost the performance of bag-of-visual words model by combining weakly spatial symmetry (WSS) and BoW together. Despite its success in the scene image classification domain, WSS model has its own limitations. For example, after dividing the image into many sub-regions and generating histograms of bag-of-visual words model, WSS only computes spatial symmetry information inside each sub-region, rather than considering the spatial difference information between sub-regions. While spatial difference infor‐ mation between sub-regions is much more important than inside spatial symmetry information when dividing images into increasingly fine sub-regions.

Hence we propose a novel approach to relieve the above problems under spatial pyramid matching framework. Firstly, we compute spatial difference information in four kinds of orientations. Secondly, we combine the spatial difference descriptors with histograms of bag-of-visual words model together. Finally, experiments are conducted on several datasets, which mainly include estimating different distance measurements, evaluating the performance with different codebook sizes and comparing with other methods to prove the effectiveness of our approach.

### **2 Related Work**

The bag-of-visual words (BoW) [\[1\]](#page-12-0) model has been widely used for visual applications. Traditional BoW model uses the *k*-means clustering algorithm and considers the cluster centers as visual words. Local features are then quantized to the nearest visual word. However, this solution leads to severe information loss, which limits its discriminative power. In order to reduce the information loss in the local feature encoding process, many works [\[6–8](#page-12-0)] have been proposed. For instance, as a classical and typical one, Yang et al. in [[6\]](#page-12-0) proposed one scheme to sparse coding with spatial pyramid matching for codebook generation, and trained linear classifier to save computational cost, which was much more effective than non-linear classifier.

Further more, the traditional BoW model lacks the spatial information. Inspired by the work done by Grauman and Darre1l [\[4](#page-12-0)], Lazebnik et al. [[2](#page-12-0)] proposed the spatial pyramid matching (SPM) algorithm which was widely used by many researchers. Later, a lot of works  $[9-13]$  have been done to combine the spatial information of local features, which are motivated by the SPM algorithm. A hierarchical matching method with side information was proposed by Chen et al. [[9\]](#page-12-0) and it was used for image classification. A weighting scheme was used to select discriminative visual words. Randomization and discrimination was combined into a unified frame work by Yao et al. [[10](#page-12-0)], which was used for fine grained

<span id="page-2-0"></span>image categorization. Zhang et al. [\[11\]](#page-12-0) proposed a pose pooling kernel to recognize subcategory birds. Representing images with components and a bilinear model for object recognition was used in [\[12\]](#page-12-0) proposed by Zhang et al., Bao and He [[13](#page-12-0)] proposed an improved sparse coding model based on linear spatial pyramid matching (SPM) and scale invariant feature transform (SIFT) descriptors. Teng et al. [[3\]](#page-12-0) explored a weakly spatial symmetry descriptor to boost the performance of bag-of-visual words model by combining WSS and BoW together. Authors in [\[14,](#page-12-0) [15](#page-12-0)] explored methods of combining spectral and spatial information directly to boost the final performance. Zhu et al. [\[16\]](#page-12-0) presented a robust semi-supervised kernel-FCM algorithm incorporating local spatial information to solve the original problem of image classification. In another way, Zhang et al. [[17](#page-12-0)] proposed a novel object categorization method by using the sub-semantic space based image representation. Most of the previous works have their own superiority on some datasets. However, none of them consider the spatial difference information between sub regions. To make use of this lost information, we propose a novel descriptor named spatial difference to improve the performance for image classification.



**Fig. 1.** Flow chart of spatial difference descriptor computation

## **3 Proposed Framework**

Our image classification solution is derived from spatial pyramid matching model [[6\]](#page-12-0), which mainly includes five modules: feature extraction, sparse coding, spatial pooling, spatial difference descriptor computation, and finally linear classifier. Firstly, feature extraction accomplishes obtaining the original image representation vectors. Then sparse coding and spatial pooling are used to learn dictionary and encode the local features respectively. After this, the spatial difference descriptor is computed to complete the gist of obtaining discriminative image representation vectors by going one more step, as shown in Fig. [1.](#page-2-0) In the last module, we use linear SVM classifier to do image clas‐ sification by training and testing the obtained discriminative feature the same as other common benchmarks.

### **3.1 Feature Extraction**

Local features play a very important role for effective image representation. Choosing the proper local features is helpful to improve the final image classification performance substantially. For better discriminative power, we utilize higher-dimensional "strong features", which are SIFT descriptors of  $16 \times 16$  pixel patches computed over a grid with 8-pixel spacing. Before extracting features, the image should be all processed into gray scale. At last, These extracted features are then normalized with  $L_2$  norm.

### **3.2 Sparse Coding**

Sparse coding has been widely used for codebook generation in the BoW model. Let  $X = [x_1, x_2, ..., x_N]$  ( $x_i \in \mathbb{R}^{D \times 1}$ ) be a set of *N* local image descriptors of each *D* dimension. Given a codebook with *K* entries to be learned,  $V = [v_1, v_2, ..., v_K]$  ( $v_i \in \mathbb{R}^{D \times 1}$ ), each descriptor can be converted into a *K*-dimensional code to generate the final image repre‐ sentation. Let  $U = [u_1, u_2, ..., u_N]$  is the set of codes for *X*. Typically the sparse coding method solves the following optimization problem as:

$$
\min_{U,V} \sum_{n=1}^{N} ||x_n - u_n V||^2 + \lambda ||u_n||_1
$$
  
s.t.  $||v_k||^2 \le 1, \forall k$ 

where  $\lambda$  is the regularization parameter. Considering the large amount of local features, we only sample a subset of features to learn the codebook. With the codebook in place, the local features of each image can be encoded.

Yang et al. [[6\]](#page-12-0) developed an extension of the SPM method [[2\]](#page-12-0) by generating vector quantization to sparse coding followed by multi-scale spatial max pooling, and proposed a linear SPM kernel based on SIFT sparse codes. Their approach, called ScSPM, is naturally derived by relaxing the restrictive cardinality constraint of VQ.

#### <span id="page-4-0"></span>**3.3 Spatial Pooling**

In the "SPM" layer, we partition an image into  $2^l \times 2^l$  spatial sub-regions, where  $l = 0$ , 1, 2 stands for different scales. The codes of the descriptors are pooled together to get the corresponding pooled features. These pooled features from each sub-region are concatenated and normalized to form the image feature representation. The pooling method used in this paper is max pooling:

$$
z_i = \max(u_{ii})
$$
  $i = 1, 2, ..., N, j = K$ 

In our framework, "max pooling" combined with  $L_2$  normalization is used. Max pooling can produce better performance than other pooling methods (i.e. *Sqrt* and *Abs*), as demonstrated by Yang et al. [\[6](#page-12-0)], probably due to its robustness to local spatial trans‐ lation and biological plausibility.

#### **3.4 Spatial Difference Descriptor Computation**

After image representation being generated by sparse coding and spatial pooling hier‐ archically, spatial difference descriptors are computed according to four kinds of spatial difference information. For example, the sub-figure (a) in Fig. 2 describes left to right difference, and the sub-figure (b) describes top to down difference. As for the diagonal differences, we compare two different schemes, as shown in Fig. [1](#page-2-0).



**Fig. 2.** Four kinds of spatial difference information

In the first scheme, diagonal spatial difference information is extracted by computing distances between sub-regions which may not be contiguous. In the second scheme, diagonal spatial difference information is extracted by computing distances between sub-regions which are all contiguous. Both of the two schemes compute spatial differ‐ ence information between sub-regions rather than in each sub-region.

Because the two sub-regions to be calculated for diagonal spatial difference information may be not contiguous, their correlation is denoted by dotted line, as shown in sub-figure (c) and sub-figure (d) of Fig. 2. Especially, Fig. [1](#page-2-0) describes the flow chart of the spatial difference descriptor computation process in the whole image level. In order to differentiate the two computing schemes, we denote the first scheme as spatial differ‐ ence 1  $(SD<sup>1</sup>)$  and the second one as spatial difference 2  $(SD<sup>2</sup>)$ . It is important to note that, in Figs. [1](#page-2-0) and 2, the blocks in which the head and tail of the arrow line locate are the sub-regions we choose to compute difference descriptor.

For two computing sub-regions of the segmented image, two vectors  $h_1$  and  $h_2$  are built based on the size of codebook:

$$
h_1 = [h_{11}, h_{12}, \dots, h_{1K}]
$$
  

$$
h_2 = [h_{21}, h_{22}, \dots, h_{2K}]
$$

where *K* is the size of codebook.

If these two sub-regions are strictly the same, the distance between them would be near 0. Obviously, different distance measurements may lead to different results, and then we can use different methods to compute the distance. Finally, we will adopt *euclidean* distance measurement as the most proper one to calculate the spatial difference information between two vectors. Now we can obtain a feature vector to describe the spatial difference descriptor for the whole image:

$$
D_{SD} = [d_1, d_2, \dots, d_P]
$$

where  $P$  is the number of sub-region pairs to compute according to Figs. [1](#page-2-0) and [2](#page-4-0).

To combine histograms of bag-of-visual words model and spatial difference infor‐ mation, we utilize the method as described in [\[3](#page-12-0)] by Teng et al. and obtain the final discriminative feature representation:

$$
W_{ScSPM+SD} = [H, D_{SD}]
$$
  
= [h<sub>1</sub>, h<sub>2</sub>, ..., d<sub>m</sub>, d<sub>1</sub>, d<sub>2</sub>, ..., d<sub>p</sub>]

where *H* is the histograms of bag-of-visual words, and *m* is the size of *H*.

### **4 Experiments and Results**

To evaluate the effectiveness of the proposed method in this paper, we choose to conduct image classification experiments on several public datasets. The datasets are Scene 15 dataset, Caltech 101 dataset and Caltech 256 dataset.

Our approach uses the popular SIFT descriptors. The same as other common benchmarks, we randomly select the training images and use the rest images for testing. This process is repeated for ten times to get reliable results. Mean of per-class classification rates for performance measurement is used and we report the final results by mean and standard deviation of the classification rates. SPM with three pyramid and  $SD<sup>1</sup>$  (or  $SD<sup>2</sup>$ ) in which spatial difference information is extracted are used to combine the hierarchical histograms and correlations between sub-regions together. Hence, each image is represented by a vector of  $21 \times K$  (size of codebook) + 40 (or 48) for all datasets.

Our experiments mainly include three parts: firstly, fixing the codebook size with 1024, and for Scene 15 dataset and Caltech 101 dataset, we evaluate the performance of different distance measurements. Measuring distance includes six methods, which are *chebychev, jaccard, hamming, cosine, cityblcok* and *euclidean*. Secondly, fixing the distance measurement, we evaluate the performance by changing the codebook size. Finally, we choose to compare with other methods which are closely related with the proposed method by their reported results instead of re-implementing them and test on every datasets for fair comparison mostly.

#### <span id="page-6-0"></span>**4.1 Scene 15 Dataset**

We firstly try our method on the Scene 15 dataset. There are 4485 images of 15 classes (bedroom, coast, forest, highway, industrial, insidecity, kitchen, living room, mountain, office, opencountry, store, suburb and tallbuiding) in this dataset. Each class has 200 to 400 images. We follow the same experiment setup as Yang et al. [\[6](#page-12-0)] did and randomly select 100 images per class for classifier training.

Then we evaluate the performance by using different distance measurements. For fair comparison, we extract WSS descriptor proposed by Teng et al. [[3](#page-12-0)] and use them under the same framework with us. When, taking WSS,  $SD^2$  and  $SD^1$  into consideration, as shown in Fig. 3, we can see that  $SD<sup>1</sup>$  can achieve better performance than the other two methods, and the distance measurement of *euclidean* is the best selection to get amazing performance.

We also conduct experiments on different size of codebook to observe the effect for classification on the Scene 15 dataset. As shown in Fig. 4, when the codebook size is 2048, we can achieve the best performance on Scene 15 dataset.



**Fig. 3.** Performance under different distance measurements on Scene 15



**Fig. 4.** Performance of codebook size on Scene 15

<span id="page-7-0"></span>

**Fig. 5.** Example images from classes with classification accuracy comparison on Scene 15

| Methods             | Performance      |
|---------------------|------------------|
| KSPM <sub>[2]</sub> | $81.40 \pm 0.50$ |
| $WSS + SPM [3]$     | $81.51 + 0.00$   |
| KCSPM [5]           | $76.70 \pm 0.40$ |
| LSPM [6]            | $65.32 + 1.02$   |
| $ScSPM$ [6]         | $80.28 + 0.93$   |
|                     |                  |
| LScSPM [7]          | $89.75 + 0.50$   |
| NNScSPM [13]        | $81.92 \pm 0.42$ |
| $S^3R$ [17]         | $83.72 \pm 0.78$ |
| $WSS + ScSPM$       | $81.46 \pm 0.00$ |
| $SD^2 + SCSPM$      | $82.80 \pm 0.00$ |

Table 1. Image classification results on Scene 15

Finally, we give the performance of the proposed method and compare with methods proposed by [[2](#page-12-0), [3,](#page-12-0) [5–7](#page-12-0), [13](#page-12-0), [17](#page-12-0)] in Table [1.](#page-6-0) As shown in Table [1,](#page-6-0) LScSPM can achieve high performance on scene classification. The problem reason is that scene images contain plentiful textures in each patch, which results in the unstableness for sparse coding process. By adding Laplacian term, similar patches will be encoded into similar codes, thus the image can be accurately represented [[7\]](#page-12-0). Except LScSPM, we can see that our method  $SD<sup>1</sup>$  descriptor under SPM framework achieves comparable results. Figure [5](#page-7-0) shows some example images from Scene 15 dataset classes with classification accuracy in brackets. The first number in the bracket is the accuracy obtained by using  $SD<sup>1</sup>$  descriptor under spatial pyramid matching framework, and the second number in the bracket is the accuracy obtained by using the classic method proposed by Yang et al. in  $[6]$  $[6]$ .

#### **4.2 Caltech 101 Dataset**

The Caltech 101 dataset contains 8144 images falling in 101 classes including animals, vehicles, flowers, etc., with significant variance in shape. The number of images per class varies from 31 to 800. Most images are medium resolution, i.e. about  $300 \times 300$ pixel. We follow the common experiment setup as Yang et al. [[6\]](#page-12-0) did and randomly select 15 and 30 images per class for classifier training and use the rest images for testing.

On one hand, for fair comparison, as did on Scene 15 dataset, we conduct experi‐ ments to evaluate the performance of different distance measurements by taking WSS,  $SD<sup>2</sup>$  and  $SD<sup>1</sup>$  into consideration under spatial pyramid matching framework. On the other hand, we test the performance with different codebook sizes. We can see from Fig. 6, the method of *euclidean* outperforms the others. When the codebook size is 2048, we can achieve the best performance, as shown in Fig. [7](#page-9-0).



**Fig. 6.** Performance under different distance measurements on Caltech 101

<span id="page-9-0"></span>

**Fig. 7.** Performance of codebook size on Caltech 101

At last we give the performance of the proposed method and compare with other methods described [\[2](#page-12-0), [3](#page-12-0), [5,](#page-12-0) [6\]](#page-12-0) in Table 2. Figure [8](#page-10-0) shows some typical images owning the top 18th classification accuracy in brackets. The first number in the bracket is the accuracy obtained by using  $\mathrm{SD}^1$  descriptors under spatial pyramid matching framework, the second one is the accuracy by using the method proposed by Yang et al. in [[6\]](#page-12-0). From Table 2 and Fig. [8,](#page-10-0) we can see our method outperforms the other related methods, mainly due to the contribution of spatial difference descriptors.

| Methods         | 15 training      | 30 training      |  |
|-----------------|------------------|------------------|--|
| KSPM [2]        | $56.40 \pm 0.00$ | $64.60 \pm 0.80$ |  |
| $WSS + SPM [3]$ |                  | $67.57 + 0.00$   |  |
| KCSPM [5]       |                  | $64.14 + 0.18$   |  |
| $LSPM$ [6]      | $67.00 + 0.45$   | $58.81 \pm 1.51$ |  |
| ScSPM [6]       | $67.00 + 0.45$   | $73.20 \pm 0.54$ |  |
| $WSS + ScSPM$   | $66.94 + 0.01$   | $73.39 + 0.14$   |  |
| $SD^2 + SCSPM$  | $67.60 \pm 0.00$ | $73.15 \pm 0.01$ |  |
| $SD1 + ScSPM$   | $70.01 \pm 0.00$ | $74.26 + 0.01$   |  |

**Table 2.** Image classification results on Caltech 101

<span id="page-10-0"></span>

**Fig. 8.** Example images from classes with the top 18th classification accuracy on the Caltech 101 when using  $SD<sup>1</sup>$  descriptor under spatial pyramid matching framework

| Methods        | 15 training      | 30 training      | 45 training      | 60 training      |
|----------------|------------------|------------------|------------------|------------------|
| KCSPM [5]      |                  | $27.17 + 0.46$   |                  |                  |
| $LSPM$ [6]     | $13.20 \pm 0.62$ | $15.45 + 0.37$   | $16.37 + 0.47$   | $16.57 \pm 1.01$ |
| ScSPM [6]      | $27.73 \pm 0.51$ | $34.02 \pm 0.35$ | $37.46 \pm 0.55$ | $40.14 \pm 0.91$ |
| LScSPM [7]     | $30.00 \pm 0.14$ | $35.74 \pm 0.10$ | $38.54 + 0.36$   | $40.43 \pm 0.38$ |
| $S^3R$ [17]    | $37.85 + 0.48$   | $43.52 \pm 0.44$ | $46.86 + 0.63$   |                  |
| KSPM $[18]$    |                  | $34.10 + 0.00$   |                  |                  |
| $WSS + ScSPM$  | $30.98 + 0.00$   | $36.90 + 0.00$   | $39.79 + 0.00$   | $41.63 \pm 0.00$ |
| $SD^2 + SCSPM$ | $31.25 \pm 0.00$ | $36.84 \pm 0.00$ | $39.67 \pm 0.00$ | $41.63 \pm 0.00$ |
| $SD^1 + SCSPM$ | $31.60 \pm 0.00$ | $37.04 \pm 0.00$ | $40.25 + 0.00$   | $42.66 + 0.00$   |

**Table 3.** Image classification results on Caltech 256

### **4.3 Caltech 256 Dataset**

The Caltech 256 dataset has 256 classes of 29,780 images. Each class contains at least 80 images. Compared with the Caltech 101 dataset, images within the Caltech 256 dataset are more larger intra-class variant. We test our method on 15, 30, 45 and 60 training images randomly chosen in per class respectively. As shown in Table  $3$ ,  $S<sup>3</sup>R$ performs better than our method. This is because it combines the visual similarity and weak semantic similarity of the training images. Furthermore it is time-costing because of learning extra classifier and space-consuming because of requiring more space for extra sub-semantic feature. Except  $S^3R$ , we can see that our approach outperforms all the other related methods, mainly due to the addition of spatial descriptors under spatial pyramid framework. Figure 9 shows some typical images owning the top 18th classification accuracy in brackets. The first number in the bracket is the accuracy obtained by using  $\mathrm{SD}^1$  descriptors under spatial pyramid matching framework, the second one is the accuracy by using the method proposed by Yang et al. in [\[6\]](#page-12-0).



**Fig. 9.** Example images from classes with the top 18th classification accuracy on the Caltech 256 dataset when using  $SD<sup>1</sup>$  descriptors under spatial pyramid matching framework

# **5 Conclusion**

This article focuses on boosting the performance of image classification with spatial difference information. A novel descriptor named spatial difference is proposed to describe the spatial information of differences. And this descriptor is mainly used in the combination with histograms of bag-of-visual words model under spatial pyramid matching framework, which can boost the final performance of image classification. The experimental results on the three public image datasets of the Scene 15 dataset, the Caltech 101 dataset and the Caltech 256 set demonstrate the effectiveness of the proposed method.

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