

Restricted Path Consistency Revisited

Kostas Stergiou^(✉)

Department of Informatics and Telecommunications Engineering,
University of Western Macedonia, Kozani, Greece
kstergiou@uowm.gr

Abstract. Restricted path consistency (RPC) is a strong local consistency for binary constraints that was proposed 20 years ago and was identified as a promising alternative to arc consistency (AC) in an early experimental study of local consistencies for binary constraints. However, and in contrast to other strong local consistencies such as SAC and maxRPC, it has been neglected since then. In this paper we revisit RPC. First, we propose RPC3, a new lightweight RPC algorithm that is very easy to implement and can be efficiently applied throughout search. Then we perform a wide experimental study of RPC3 and a light version that achieves an approximation of RPC, comparing them to state-of-the-art AC and maxRPC algorithms. Experimental results clearly show that restricted RPC is by far more efficient than both AC and maxRPC when applied throughout search. These results strongly suggest that it is time to reconsider the established perception that MAC is the best general purpose method for solving binary CSPs.

1 Introduction

Restricted path consistency (RPC) is a local consistency for binary constraints that is stronger than arc consistency (AC). RPC was introduced by Berlandier [4] and was further studied by Debruyne and Bessiere [7, 8]. An RPC algorithm removes all arc inconsistent values from a domain $D(x)$, and in addition, for any pair of values (a, b) , with $a \in D(x)$ and $b \in D(y)$ s.t. b is the only support for a in a $D(y)$, it checks if (a, b) is path consistent. If it is not then a is removed from $D(x)$. In this way some of the benefits of path consistency are retained while avoiding its high cost.

Although RPC was identified as a promising alternative to AC as far back as 2001 [8], it has been neglected by the CP community since then. In contrast, stronger local consistencies such as max restricted path consistency (maxRPC) [7] and singleton arc consistency (SAC) [8] have received considerable attention in the past decade or so [1–3, 5, 9, 11, 13, 14]. However, despite the algorithmic developments on maxRPC and SAC, none of the two outperforms AC when maintained during search, except for specific classes of problems. Therefore, MAC remains the predominant generic algorithm for solving binary CSPs.

In this paper we revisit RPC and make two contributions compared to previous works that bring the state-of-the-art regarding RPC up to date. The first is algorithmic and the second experimental.

The two algorithms that have been proposed for RPC, called RPC1 [4] and RPC2 [7], are based on the AC algorithms AC4 and AC6 respectively. As a result they suffer from the same drawbacks as their AC counterparts. Namely, they use heavy data structures that are too expensive to maintain during search. In recent years it has been shown that in the case of AC lighter algorithms which sacrifice optimality display a better performance when used inside MAC compared to optimal but heavier algorithms such as AC4, AC6, AC7, and AC2001/3.1. Hence, the development of the residue-based version of AC3 known as AC3^r [10, 12]. A similar observation has been made with respect to maxRPC [1]. Also, it has been noted that cheap approximations of local consistencies such as maxRPC and SAC are more cost-effective than the full versions. In the case of maxRPC, the residue-based algorithm lmaxRPC3^r, which achieves an approximation of maxRPC, is the best choice when applying maxRPC [1].

Following these trends, we propose RPC3, an RPC algorithm that makes use of residues in the spirit of AC^r and lmaxRPC^r and is very easy to implement. As we will explain, for each constraint (x, y) and each value $a \in D(x)$, RPC3 stores two residues that correspond to the two most recently discovered supports for a in $D(y)$. This enables the algorithm to avoid many redundant constraint checks. We also consider a restricted version of the algorithm (simply called rRPC3) that achieves a local consistency property weaker than RPC, but still stronger than AC, and is considerably faster in practice.

Our second and most important contribution concerns experiments. Given that the few works on RPC date from the 90s, the experimental evaluations of the proposed algorithms were carried out on limited sets of, mainly random, problems. Equally importantly, there was no evaluation of the algorithms when used during search to maintain RPC. We carry out a wide evaluation on benchmark problems from numerous classes that have been used in CSP solver competitions. Surprisingly, results demonstrate that an algorithm that applies rRPC3 throughout search is not only competitive with MAC, but it clearly outperforms it on the overwhelming majority of tested instances, especially on structured problems. Also, it clearly outperforms lmaxRPC3^r. This is because RPC, and especially its restricted version, achieves a very good balance between the pruning power of maxRPC and the low cost of AC.

Our experimental results provide strong evidence of a local consistency that is clearly preferable to AC when maintained during search. Hence, perhaps it is time to reconsider the common perception that MAC is the best general purpose solver for binary problems.

2 Background

A *Constraint Satisfaction Problem* (CSP) is defined as a triplet $(\mathcal{X}, \mathcal{D}, \mathcal{C})$ where: $\mathcal{X} = \{x_1, \dots, x_n\}$ is a set of n variables, $\mathcal{D} = \{D(x_1), \dots, D(x_n)\}$ is a set of domains, one for each variable, with maximum cardinality d , and $\mathcal{C} = \{c_1, \dots, c_e\}$ is a set of e constraints. In this paper we are concerned with binary CSPs. A binary constraint c_{ij} involves variables x_i and x_j .

At any time during the solving process if a value a_i has not been removed from the domain $D(x_i)$, we say that the value is *valid*. A value $a_i \in D(x_i)$ is *arc consistent* (AC) iff for every constraint c_{ij} there exists a value $a_j \in D(x_j)$ s.t. the pair of values (a_i, a_j) satisfies c_{ij} . In this case a_j is called an *support* of a_i . A variable is AC iff all its values are AC. A problem is AC iff there is no empty domain in D and all the variables in X are AC.

A pair of values (a_i, a_j) , with $a_i \in D(x_i)$ and $a_j \in D(x_j)$, is *path consistent* PC iff for any third variable x_k constrained with x_i and x_j there exists a value $a_k \in D(x_k)$ s.t. a_k is a support of both a_i and a_j . In this case a_j is a *PC-support* of a_i in $D(x_j)$ and a_k is a *PC-witness* for the pair (a_i, a_j) in $D(x_k)$.

A value $a_i \in D(x_i)$ is *restricted path consistent* (RPC) iff it is AC and for each constraint c_{ij} s.t. a_i has a single support $a_j \in D(x_j)$, the pair of values (a_i, a_j) is *path consistent* (PC) [4]. A value $a_i \in D(x_i)$ is *max restricted path consistent* (maxRPC) iff it is AC and for each constraint c_{ij} there exists a support a_j for a_i in $D(x_j)$ s.t. the pair of values (a_i, a_j) is *path consistent* (PC) [7]. A variable is RPC (resp. maxRPC) iff all its values are RPC (resp. maxRPC). A problem is RPC (resp. maxRPC) iff there is no empty domain and all variables are RPC (resp. maxRPC).

3 The RPC3 Algorithm

The RPC3 algorithm is based on the idea of seeking two supports for a value, which was first introduced in RPC2 [7]. But in contrast to RPC2 which is based on AC6, it follows an AC3-like structure, resulting in lighter use of data structures, albeit with a loss of optimality. As explained below, we can easily obtain a restricted but more efficient version of the algorithm that only approximates the RPC property. Crucially, the lack of heavy data structures allows for the use of the new algorithms during search without having to perform expensive restorations of data structures after failures.

In the spirit of AC^r , RPC3 utilizes two data structures, R^1 and R^2 , which hold residual data used to avoid redundant operations. Specifically, for each constraint c_{ij} and each value $a_i \in D(x_i)$, $R^1_{x_i, a_i, x_j}$ and $R^2_{x_i, a_i, x_j}$ hold the two most recently discovered supports of a_i in $D(x_j)$. Initially, all residues are set to a special value NIL, considered to precede all values in any domain.

The pseudocode of RPC3 is given in Algorithm 1 and Function 2. Being coarse-grained like AC3, Algorithm 1 uses a propagation list Q , typically implemented as a fifo queue. We use a constraint-oriented description, meaning that Q handles pairs of variables involved in constraints. A variable-based one requires minor modifications.

Once a pair of variables (x_i, x_j) is removed from Q , the algorithm iterates over $D(x_i)$ and for each value a_i first checks the residues $R^1_{x_i, a_i, x_j}$ and $R^2_{x_i, a_i, x_j}$ (line 5). If both are valid then a_i has at least two supports in $D(x_j)$. Hence, the algorithm moves to process the next value in $D(x_i)$. Otherwise, function *findTwoSupports* is called. This function will try to find two supports for a_i in $D(x_j)$. In case it finds none then a_i is not AC and will thus be deleted (line 13).

Algorithm 1. RPC3:boolean

```

1: while  $Q \neq \emptyset$  do
2:    $Q \leftarrow Q - \{(x_i, x_j)\}$ ;
3:   Deletion  $\leftarrow$  FALSE;
4:   for each  $a_i \in D(x_i)$  do
5:     if both  $R_{x_i, a_i, x_j}^1$  and  $R_{x_i, a_i, x_j}^2$  are valid then
6:       continue;
7:     else
8:       if only one of  $R_{x_i, a_i, x_j}^1$  and  $R_{x_i, a_i, x_j}^2$  is valid then
9:          $R \leftarrow$  the valid residue;
10:      else
11:         $R \leftarrow$  NIL;
12:      if  $\text{findTwoSupports}(x_i, a_i, x_j, R) = \text{FALSE}$  then
13:        remove  $a_i$  from  $D(x_i)$ ;
14:        Deletion  $\leftarrow$  TRUE;
15:   if  $D(x_i) = \emptyset$  then
16:     return FALSE;
17:   if Deletion = TRUE then
18:     for each  $(x_k, x_i) \in C$  s.t.  $(x_k, x_i) \notin Q$  do
19:        $Q \leftarrow Q \cup \{(x_k, x_i)\}$ ;
20:     for each  $(x_l, x_k) \in C$  s.t.  $x_l \neq x_i$  and  $(x_l, x_i) \in C$  and  $(x_l, x_k) \notin Q$  do
21:        $Q \leftarrow Q \cup \{(x_l, x_k)\}$ ;
22:   return TRUE;

```

In case it finds only one then it will check if a_i is RPC. If it is not then it will be deleted. Function *findTwoSupports* takes as arguments the variables x_i and x_j , the value a_i , and a parameter R , which is set to the single valid residue of a_i in $D(x_j)$ (line 9) or to NIL if none of the two residues is valid.

Function *findTwoSupports* iterates over the values in $D(x_j)$ (line 3). For each value $a_j \in D(x_j)$ it checks if the pair (a_i, a_j) satisfies constraint c_{ij} (this is what function *isConsistent* does). If both residues of a_i in $D(x_j)$ are not valid then after a support is found, the algorithm continues to search for another one. Otherwise, as soon as a support is found that is different than R , the function returns having located two supports (lines 9-11).

If only one support a_j is located for a_i then the algorithm checks if the pair (a_i, a_j) is path consistent. During this process it exploits the residues to save redundant work, if possible. Specifically, for any third variable x_k that is constrained with both x_i and x_j , we first check if one of the two residues of a_i is valid and if a_j is consistent with that residue (line 16). If this is the case then we know that there is a PC-witness for the pair (a_i, a_j) in $D(x_k)$ without having to iterate over $D(x_k)$. If it is not the case then the check is repeated for the residues of a_j in $D(x_k)$. If we fail to verify the existense of a PC-witness in this way then we iterate over $D(x_k)$ checking if any value a_k is consistent with both a_i and a_j . If a PC-witness is found, we proceed with the next variable that is constrained with both x_i and x_j . Otherwise, the function returns false, signaling that a_i is not RPC.

Function 2. *findTwoSupports*(x_i, a_i, x_j, R):**Boolean**

```

1: if  $R = \text{NIL}$  then oneSupport  $\leftarrow$  FALSE;
2: else oneSupport  $\leftarrow$  TRUE;
3: for each  $a_j \in D(x_j)$  do
4:   if isConsistent( $a_i, a_j$ ) then
5:     if oneSupport = FALSE then
6:       oneSupport  $\leftarrow$  TRUE;
7:        $R_{x_i, a_i, x_j}^1 \leftarrow a_j$ ;
8:     else
9:       if  $a_j \neq R$  then
10:         $R_{x_i, a_i, x_j}^2 \leftarrow a_j$ ;
11:        return TRUE;
12: if oneSupport = FALSE then
13:   return FALSE
14: else
15:   for each  $x_k \in X, x_k \neq x_i$  and  $x_k \neq x_j$ , s.t.  $(x_k, x_i) \in C$  and  $(x_k, x_j) \in C$  do
16:     if there is a valid residue  $R_{x_i, a_i, x_k}^*$  and isConsistent( $R_{x_i, a_i, x_k}^*, a_j$ ) or if there
17:     is a valid residue  $R_{x_j, a_j, x_k}^*$  and isConsistent( $R_{x_j, a_j, x_k}^*, a_i$ )
18:     then continue;
19:     PCwitness  $\leftarrow$  FALSE;
20:     for each  $a_k \in D(x_k)$  do
21:       if isConsistent( $a_i, a_k$ ) and isConsistent( $a_j, a_k$ ) then
22:         PCwitness  $\leftarrow$  TRUE;
23:         break;
24:     if PCwitness = FALSE then
25:       return FALSE;
26: return TRUE;

```

Moving back to Algorithm 1, if at least one value is deleted from a domain $D(x_i)$, some pairs of variables must be enqueued so that the deletions are propagated. Lines 18-19 enqueue all pairs of the form (x_k, x_i) . This ensures that if a value in a domain $D(x_k)$ has lost its last support in $D(x_i)$, it will be processed by the algorithm when the pair (x_k, x_i) is dequeued, and it will be removed. In addition, it ensures that if a value in $D(x_k)$ has been left with only one support in $D(x_i)$, that is not a PC-support, it will be processed and deleted once (x_k, x_i) is dequeued. This means that if we only enqueue pairs of the form (x_k, x_i) , we can achieve stronger pruning than AC. However, this is not enough to achieve RPC. We call the version of RPC3 that only enqueues such pairs *restricted RPC3* (rRPC3).

To achieve RPC, for each pair (x_k, x_i) that is enqueued, we also enqueue all pairs of the form (x_l, x_k) s.t. x_l is constrained with x_i . This is because after the deletions from $D(x_i)$ the last PC-witness in $D(x_i)$ for some pair of values for variables x_k and x_l may have been deleted. This may cause further deletions from $D(x_l)$.

The worst-case time complexity of RPC3, and rRPC3, is $O(ned^3)$ ¹. The space complexity is determined by the space required to store the residues, which is $O(ed)$. The time complexities of algorithms RPC1 and RPC2 are $O(ned^3)$ and $O(ned^2)$ respectively, while their space complexities, for stand-alone use, are $O(ed^2)$ and $O(end)$. RPC3 has a higher time complexity than RPC2, and a lower space complexity than both RPC1 and RPC2. But most importantly, RPC3 does not require the typically quite expensive restoration of data structures after failures when used inside search. In addition, this means that its space complexity remains $O(ed)$ when used inside search, while the space complexities of RPC1 and RPC2 will be even higher than $O(ed^2)$ and $O(end)$.

4 Experiments

We have experimented with 17 classes of binary CSPs taken from C.Lecoutre's XCSP repository: *rlfap*, *graph coloring*, *qcp*, *qwh*, *bqwh*, *driver*, *job shop*, *haystacks*, *hanoi*, *pigeons*, *black hole*, *ehi*, *queens*, *geometric*, *composed*, *forced random*, *model B random*. A total of 1142 instances were tested. Details about these classes of problems can be found in C.Lecoutre's homepage. All algorithms used the dom/wdeg heuristic for variable ordering [6] and lexicographic value ordering. The experiments were performed on a FUJITSU Server PRIMERGY RX200 S7 R2 with Intel(R) Xeon(R) CPU E5-2667 clocked at 2.90GHz, with 48 GB of ECC RAM and 16MB cache.

We have compared search algorithms that apply rRPC3 (resp. RPC3) during search to a baseline algorithm that applies AC (i.e. MAC) and also to an algorithm that applies lmaxRPC. AC and lmaxRPC were enforced using the AC^r and lmaxRPC3 algorithms respectively. For simplicity, the four search algorithms will be denoted by AC, rRPC, RPC, and maxRPC hereafter. Note that a MAC algorithm with AC^r and dom/wdeg for variable ordering is considered as the best general purpose solver for binary CSPs.

A timeout of 3600 seconds was imposed on all four algorithms for all the tested instances. Importantly, **rRPC only timed out on instances where AC and maxRPC also timed out**. On the other hand, there were several cases where rRPC finished search within the time limit but one (or both) of AC and maxRPC timed out. There were a few instances where RPC timed out while rRPC did not, but the opposite never occurred.

Table 1 summarizes the results of the experimental evaluation for specific classes of problems. For each class we give the following information:

- The mean node visits and run times from non-trivial instances that were solved by all algorithms within the time limit. We consider as trivial any instance that was solved by all algorithms in less than a second.
- Node visits and run time from the single instance where AC displayed its best performance compared to rRPC.

¹ The proof is quite simple but it is omitted for space reasons.

- Node visits and run time from the single instance where maxRPC displayed its best performance compared to rRPC.
- Node visits and run time from a representative instance where rRPC displayed good performance compared to AC, excluding instances where AC timed out.
- The number of instances where AC, RPC, maxRPC timed out while rRPC did not. This information is given only for classes where at least one such instance occurred.
- The number of instances where AC, rRPC, RPC, or maxRPC was the winning algorithm, excluding trivial instances.

Comparing AC to rRPC we can note the following. rRPC is more efficient in terms of mean run time performance on all classes of structured problems with the exception of *queens*. The difference in favor of rRPC can be quite stunning, as in the case of *qwh* and *qcp*. The numbers of node visits in these classes suggest that rRPC is able to achieve considerable extra pruning, and this is then reflected on cpu times.

Importantly, in all instances of 16 classes (i.e. all classes apart from *queens*) AC was at most 1.7 times faster than rRPC. In contrast, there were 7 instances from *rlfap* and 12 from *graph coloring* where AC timed out while rRPC finished within the time limit. The mean cpu time of rRPC on these *rlfap* instances was 110 seconds while on the 12 *graph coloring* instances the cpu time of rRPC ranged from 1.8 to 1798 seconds. In addition, there were numerous instances where rRPC was orders of magnitude faster than AC. This is quite common in *qcp* and *qwh*, as the mean cpu times demonstrate, but such instances also occur in *graph coloring*, *bqwh*, *haystacks* and *ehi*.

Regarding random problems, rRPC achieves similar performance to AC on *geometric* (which is a class with some structure) and is slower on *forced random* and *model B random*. However, the differences in these two classes are not significant. The only class where there are significant differences in favour of AC is *queens*. Specifically, AC can be up to 5 times faster than rRPC on some instances, and orders of magnitude faster than both RPC and maxRPC. This is because all algorithms spend a lot of time on propagation but evidently the strong local consistencies achieve little extra pruning. Importantly, the low cost of rRPC makes its performance reasonable compared to the huge run times of RPC and maxRPC.

The comparison between RPC and AC follows the same trend as that of rRPC and AC, but importantly the differences in favour of RPC are not as large on structured problems where AC is inefficient, while AC is clearly faster on random problems, and by far superior on dense structured problems like *queens* and *pigeons*.

Comparing the mean performance of rRPC to RPC and maxRPC we can note that rRPC is more efficient on all classes. There are some instances where RPC or/and maxRPC outperform rRPC due to their stronger pruning, but the differences in favour of RPC and maxRPC are rarely significant. In contrast, rRPC can often be orders of magnitude faster. An interesting observation that

Table 1. Node visits (n), run times in secs (t), number of timeouts (#TO) (if applicable), and number of wins (winner) in summary. The number in brackets after the name of each class gives the number of instances tested.

class	AC		rRPC		RPC		maxRPC	
	(n)	(t)	(n)	(t)	(n)	(t)	(n)	(t)
rlfap (24)								
<i>mean</i>	29045	64.1	11234	32.3	10878	39.0	8757	134.0
<i>best AC</i>	12688	9.3	11813	14.5	10048	18.2	5548	33.2
<i>best maxRPC</i>	8405	10.1	3846	4.4	3218	6.86	1668	4.8
<i>good rRPC</i>	19590	28.8	5903	8.2	5197	10.4	8808	23.7
<i>#TO</i>	7				3		6	
<i>winner</i>	1		18		1		0	
qcp (60)								
<i>mean</i>	307416	345.4	37725	44.8	43068	167.1	49005	101.3
<i>best AC</i>	36498	63.5	36286	73.7	57405	354.3	63634	173.5
<i>best maxRPC</i>	20988	16.8	7743	7.6	4787	11.9	1723	1.8
<i>good rRPC</i>	1058477	761	65475	53.5	67935	162.9	54622	63.1
<i>winner</i>	2		8		0		4	
qwh (40)								
<i>mean</i>	205232	1348.2	20663	46.2	28694	177.9	24205	64.7
<i>best AC</i>	6987	4.5	3734	3.0	5387	11.9	3174	3.2
<i>best maxRPC</i>	231087	461.4	30926	72.3	30434	187.6	13497	35.8
<i>good rRPC</i>	445771	859.6	35923	79.5	56965	375.4	37582	103.9
<i>winner</i>	0		9		0		6	
bqwh (200)								
<i>mean</i>	28573	7.6	7041	2.4	5466	2.9	6136	2.7
<i>best AC</i>	5085	1.2	4573	1.4	4232	2.0	3375	1.3
<i>best maxRPC</i>	324349	85.3	122845	46.1	56020	33.8	64596	29.3
<i>good rRPC</i>	83996	22.5	7922	2.6	10858	5.6	9325	4.2
<i>winner</i>	2		36		13		20	
graph coloring (177)								
<i>mean</i>	322220	88.6	261882	60.4	192538	73.7	263227	138.79
<i>best AC</i>	1589650	442.5	1589650	743.8	1266416	930.8	1589650	1010.0
<i>best maxRPC</i>	1977536	647.9	1977536	762.4	1265930	613.7	1977536	759.8
<i>good rRPC</i>	31507	189.1	3911	15.6	2851	18.2	10477	62.7
<i>#TO</i>	12				1		5	
<i>winner</i>	8		35		17		0	
geometric (100)								
<i>mean</i>	111611	58.4	54721	58.6	52416	97.3	38227	190.9
<i>best AC</i>	331764	203.1	169871	218.1	160428	358.1	113878	696.2
<i>best maxRPC</i>	67526	28.1	31230	28.1	30229	53.5	20071	73.6
<i>good rRPC</i>	254304	123.3	119248	117.4	117665	203.0	84410	363.3
<i>winner</i>	12		11		1		0	
forced random (20)								
<i>mean</i>	348473	143.5	197994	177.2	191114	309.8	154903	455.4
<i>best AC</i>	1207920	491.5	677896	596.7	654862	1040.4	538317	1551.4
<i>best maxRPC</i>	26729	7.6	12986	9.0	12722	13.5	9372	22.4
<i>good rRPC</i>	455489	201.6	270345	258.5	262733	462.0	207267	651.2
<i>winner</i>	20		0		0		0	
model B random (40)								
<i>mean</i>	741124	194.3	383927	224.5	361926	346.5	28871	1044.9
<i>best AC</i>	2212444	669.8	1197369	805.7	1136257	1283.8	-	TO
<i>best maxRPC</i>	345980	81.2	181127	94.4	171527	142.7	130440	405.8
<i>good rRPC</i>	127567	32.4	43769	24.4	41328	39.1	51455	171.5
<i>#TO</i>	0				0		14	
<i>winner</i>	39		1		0		0	
queens (14)								
<i>mean</i>	2092	14.2	797	59.2	2476	1032.2	953	2025.2
<i>best AC</i>	150	9.2	149	43.0	149	499.1	149	3189.2
<i>best maxRPC</i>	7886	10.8	2719	11.5	9425	910.5	3341	367.9
<i>good rRPC</i>	7886	10.8	2719	11.5	9425	910.5	3341	367.9
<i>#TO</i>	0				0		1	
<i>winner</i>	4		0		0		0	

requires further investigation is that in some cases the node visits of rPRC are fewer than RPC and and/or maxRPC despite the weaker pruning. This usually occurs on soluble instances and suggests that the interaction with the dom/wdeg heuristic can guide search to solutions faster.

Finally, the classes not shown in Table 1 mostly include instances that are either very easy or very hard (i.e. all algorithms time out). Specifically, instances in *composed* and *hanoi* are all trivial, and the ones in *black hole* and *job shop* are either trivial or very hard. Instances in *ehi* typically take a few seconds for AC and under a second for the other three algorithms. Instances in *haystacks* are very hard except for a few where AC is clearly outperformed by the other three algorithms. For example, in *haystacks-04* AC takes 8 seconds and the other three take 0.2 seconds. Instances in *pigeons* are either trivial or very hard except for a few instances where rRPC is the best algorithm followed by AC. For example on *pigeons-12* AC and rRPC take 709 and 550 seconds respectively, while RPC and maxRPC time out. Finally, *driver* includes only 7 instances. Among them, 3 are trivial, rRPC is the best algorithm on 3, and AC on 1.

5 Conclusion

RPC was recognized as a promising alternative to AC but has been neglected for the past 15 years or so. In this paper we have revisited RPC by proposing RPC3, a new algorithm that utilizes ideas, such as residues, that have become standard in recent years when implementing AC or maxRPC algorithms. Using RPC3 and a restricted variant we performed the first wide experimental study of RPC when used inside search. Perhaps surprisingly, results clearly demonstrate that rRPC3 is by far more efficient than state-of-the-art AC and maxRPC algorithms when applied during search. This challenges the common perception that MAC is the best general purpose solver for binary CSPs.

References

1. Balafoutis, T., Paparrizou, A., Stergiou, K., Walsh, T.: New algorithms for max restricted path consistency. *Constraints* **16**(4), 372–406 (2011)
2. Balafrej, A., Bessiere, C., Bouyakh, E., Trombettoni, G.: Adaptive singleton-based consistencies. In: *Proceedings of the Twenty-Eighth AAAI Conference on Artificial Intelligence*, pp. 2601–2607 (2014)
3. Barták, R., Erben, R.: A new algorithm for singleton arc consistency. In: *Proceedings of the Seventeenth International Florida Artificial Intelligence*, pp. 257–262 (2004)
4. Berlandier, P.: Improving domain filtering using restricted path consistency. In: *Proceedings of IEEE CAIA 1995*, pp. 32–37 (1995)
5. Bessiere, C., Cardon, S., Debruyne, R., Lecoutre, C.: Efficient Algorithms for Singleton Arc Consistency. *Constraints* **16**, 25–53 (2011)
6. Boussemart, F., Hemery, F., Lecoutre, C., Sais, L.: Boosting systematic search by weighting constraints. In: *Proceedings of ECAI 2004, Valencia, Spain (2004)*

7. Debruyne, R., Bessière, C.: From restricted path consistency to max-restricted path consistency. In: Smolka, G. (ed.) CP 1997. LNCS, vol. 1330, pp. 312–326. Springer, Heidelberg (1997)
8. Debruyne, R., Bessière, C.: Domain Filtering Consistencies. JAIR **14**, 205–230 (2001)
9. Grandoni, F., Italiano, G.F.: Improved algorithms for max-restricted path consistency. In: Rossi, F. (ed.) CP 2003. LNCS, vol. 2833, pp. 858–862. Springer, Heidelberg (2003)
10. Lecoutre, C., Hemery, F.: A study of residual supports in arc consistency. In: Proceedings of IJCAI 2007, pp. 125–130 (2007)
11. Lecoutre, C., Prosser, P.: Maintaining singleton arc consistency. In: 3rd International Workshop on Constraint Propagation and Implementation (CPAI 2006), pp. 47–61 (2006)
12. Likitvivanavong, C., Zhang, Y., Bowen, J., Shannon, S., Freuder, E.: Arc consistency during search. In: Proceedings of IJCAI 2007, pp. 137–142 (2007)
13. Prosser, P., Stergiou, K., Walsh, T.: Singleton consistencies. In: Dechter, R. (ed.) CP 2000. LNCS, vol. 1894, pp. 353–368. Springer, Heidelberg (2000)
14. Vion, J., Debruyne, R.: Light algorithms for maintaining max-RPC during search. In: Proceedings of SARA 2009 (2009)