Describing Data

In this chapter, we tackle our first marketing analytics problem: summarizing and exploring a data set with descriptive statistics (mean, standard deviation, and so forth) and visualization methods. Such investigation is the simplest analysis one can do yet also the most crucial. It is important to describe and explore any data set before moving on to more complex analysis. This chapter will build your R skills and provide a set of tools for exploring your own data.

3.1 Simulating Data

We start by creating data to be analyzed in later parts of the chapter. Why simulate data and not work entirely with real data sets? There are several reasons. The process of creating data lets us practice and deepen R skills from Chap. 2. It makes the book less dependent on vagaries of finding and downloading online data sets. And it lets you manipulate the synthetic data, run analyses again, and examine how the results change.

Perhaps most importantly, data simulation highlights a strength of R: because it is easy to simulate data, R analysts often use simulated data to prove that their methods are working as expected. When we know what the data *should* say (because we created it), we can test our analyses to make sure they are working correctly before applying them to real data. If you have real data sets that you work with regularly, we encourage you to use those for the same analyses alongside our simulated data examples. (See Sect. 2.6 for more information on how to load data files.)

We encourage you to create data in this section step-by-step because we teach R along the way. However, if you are in a hurry to learn how to compute means, standard deviations, and other summary statistics, you could quickly run the commands in this section to generate the simulated data. Alternatively, the following will load the data from the book's website, and you can then go to Sect. 3.2:

> store.df <- read.csv("http://goo.gl/QPDdMl")</pre>

But if you're new to R, don't do that! Instead, work through the following section to create the data from scratch. If you accidentally ran the command above, you can use rm(store.df) to remove the data before proceeding.

3.1.1 Store Data: Setting the Structure

Our first data set represents observations of total sales by week for two products at a chain of stores. We begin by creating a data structure that will hold the data, a simulation of sales for the two products in 20 stores over 2 years, with price and promotion status. We remove most of the R output here to focus on the input commands. Type the following lines, but feel free to omit the comments (following "#"):

We see the simplest summary of the data frame using dim():

```
> dim(store.df)
[1] 2080 10
```

As expected, store.df has 2,080 rows and 10 columns. We create two vectors that will represent the store number and country for each observation:

```
> store.num <- 101:(100+k.stores)
> (store.cty <- c(rep("US", 3), rep("DE", 5), rep("GB", 3), rep("BR", 2),
+ rep("JP", 4), rep("AU", 1), rep("CN", 2)))
[1] "US" "US" "US" "DE" "DE" "DE" "DE" "GB" "GB" "GB" "BR" "BR" "JP" ...
> length(store.cty)  # make sure the country list is the right length
[1] 20
```

Now we replace the appropriate columns in the data frame with those values, using rep() to expand the vectors to match the number of stores and weeks:

```
> store.df$storeNum <- rep(store.num, each=k.weeks)
> store.df$country <- rep(store.cty, each=k.weeks)
> rm(store.num, store.cty)  # clean up
```

Next we do the same for the Week and Year columns:

We check the overall data structure with str():

. . . .

> :	str(store.dl)														
'da	ata.frame	'	2080) ob	s.	of	10	va	riab	les:					
\$	storeNum	ı:	int	101	10	1 1(01 3	101	101	101	101	101	101	101	
\$	Year	:	int	1 1	1	1 1	1 3	1 1	1 1						
\$	Week	:	int	1 2	3	45	6 '	78	9 1	0	•				
\$	plsales	:	logi	NA	NA	NA	NA	NA	NA						
\$	p2sales	:	logi	NA	NA	NA	NA	NA	NA						
\$	plprice	:	logi	NA	NA	NA	NA	NA	NA						
\$	p2price	:	logi	NA	NA	NA	NA	NA	NA						
\$	plprom	:	logi	NA	NA	NA	NA	NA	NA						
\$	p2prom	:	logi	NA	NA	NA	NA	NA	NA						
\$	country	:	chr	"US	" "	US"	"U	S" '	"US"						

The data frame has the right number of observations and variables, and proper column names.

R chose types for all of the variables in our data frame. For example, store.df \$country is of type chr (character) because we assigned a vector of strings to it. However, country labels are actually discrete values and not just arbitrary text. So it is better to represent country explicitly as a categorical variable, known in R as a *factor*. Similarly, storeNum is a label, not a number as such. By converting those variables to factors, R knows to treat them as a categorical in subsequent analyses such as regression models. It is good practice to set variable types correctly as they are created; this will help you to avoid errors later.

We redefine store.df\$storeNum and store.df\$country as categorical using factor():

```
> store.df$storeNum <- factor(store.df$storeNum)
> store.df$country <- factor(store.df$country)
> str(store.df)
'data.frame': 2080 obs. of 10 variables:
  $ storeNum: Factor w/ 20 levels "101","102","103",..: 1 1 1 1 1 1 1 1 1 1 ...
  ... [rows omitted] ...
  $ country : Factor w/ 7 levels "AU","BR","CN",..: 7 7 7 7 7 7 7 7 7 7 ...
```

storeNum and country are now defined as factors with 20 and 7 levels, respectively.

It is a good idea to inspect data frames in the first and last rows because mistakes often surface there. You can use head (x=DATA, n=NUMROWS) and tail() commands to inspect the beginning and end of the data frame (we omit long output from the last two commands):

>	head(stor	ce.df)	#	defaults	s to 6 rd	ows				
	storeNum	Year	Week	plsales	p2sales	plprice	p2price	plprom	p2prom	country
1	101	1	1	NA	NA	NA	NA	NA	NA	US
2	101	1	2	NA	NA	NA	NA	NA	NA	US
3	101	1	3	NA	NA	NA	NA	NA	NA	US
>	head(stor	.df,	120)	# 120	rows is	enough a	to check	2 store	s; not	shown
>	tail(stor	.df,	120)	# make	e sure ei	nd looks	OK too;	not sho	wn	

All of the specific measures (sales, price, promotion) are shown as missing values (indicated by NA) because we haven't assigned other values to them yet, while the store numbers, year counters, week counters, and country assignments look good. It's always useful to debug small steps like this as you go.

3.1.2 Store Data: Simulating Data Points

We complete store.df with random data for *store-by-week* observations of the sales, price, and promotional status of 2 products.

Before simulating random data, it is important to set the random number generation *seed* to make the process replicable. After setting a seed, when you draw random samples in the same sequence again, you get exactly the same (*pseudo*-)random numbers. Pseudorandom number generators (PRNGs) are a complex topic whose issues are out of scope here. If you are using PRNGs for something important, you should review the literature; it has been said that whole shelves of journals could be thrown away due to poor usage of random numbers. (R has support for a wide array of pseudorandom sequences; see ?set.seed for details. A starting point to learn more abut PRNGs is Knuth [93].)

If you don't set a PRNG seed, R will select one for you, but you will get different random numbers each time you repeat the process. If you set the seed and execute commands in the order shown in this book, you will get the results that we show.

> set.seed(98250) # a favorite US postal code

Now we can draw the random data. In each row of data—that is, one week of 1 year, for one store—we set the status of whether each product was promoted (value 1) by drawing from the *binomial distribution* that counts the number of "heads" in a collection of coin tosses (where the coin can have any proportion of heads, not just 50%).

To detail that process: we use the rbinom(n, size, p) (decoded as "random *binom*ial") function to draw from the binomial distribution. For every row of the store data, as noted by n=nrow(store.df), we draw from a distribution representing the number of heads in a single coin toss (size=1) with a coin that has probability p=0.1 for product 1 and p=0.15 for product 2. In other words, we arbitrarily assign a 10% likelihood of promotion for product 1, and 15% likelihood for product 2 and then randomly determine which weeks have promotions.

```
> store.df$plprom <- rbinom(n=nrow(store.df), size=1, p=0.1) # 10% promoted
> store.df$p2prom <- rbinom(n=nrow(store.df), size=1, p=0.15) # 15% promoted
> head(store.df) # how does it look so far? (not shown)
```

Next we set a price for each product in each row of the data. We suppose that each product is sold at one of five distinct price points ranging from \$2.19 to \$3.19 overall. We randomly draw a price for each week by defining a vector with the five price points and using sample(x, size, replace) to draw from it as many times as we have rows of data (size=nrow(store.df)). The five prices are sampled many times, so we sample with replacement (replace=TRUE):

```
> store.df$p1price <- sample(x=c(2.19, 2.29, 2.49, 2.79, 2.99),</pre>
                      size=nrow(store.df), replace=TRUE)
+
> store.df$p2price <- sample(x=c(2.29, 2.49, 2.59, 2.99, 3.19),
                      size=nrow(store.df), replace=TRUE)
> head(store.df) # now how does it look?
storeNum Year Week plsales p2sales p1price p2price p1prom p2prom country
1
    101 1 1 NA NA 2.29 2.29 0 0 US
2
    101 1 2 NA NA 2.49 2.49
                                            0 0
                                                       US
    101 1 3 NA NA 2.99 2.99 1 0 US
3
. . .
```

Question: if *price* occurs at five discrete levels, does that make it a factor variable? That depends on the analytic question, but in general probably not. We often perform math on price, such as subtracting cost in order to find gross margin, multiplying by units to find total sales, and so forth. Thus, even though it may have only a few unique values, price is a number, not a factor.

Our last step is to simulate the sales figures for each week. We calculate sales as a function of the relative prices of the two products along with the promotional status of each.

Item sales are in unit counts, so we use the Poisson distribution to generate count data: rpois(n, lambda), where n is the number of draws and lambda is the mean value of units per week. We draw a random Poisson count for each row (nrow(store.df), and set the mean sales (lambda) of Product 1 to be higher than that of Product 2:

```
# sales data, using poisson (counts) distribution, rpois()
# first, the default sales in the absence of promotion
> tmp.sales1 <- rpois(nrow(store.df), lambda=120)
> tmp.sales2 <- rpois(nrow(store.df), lambda=100)</pre>
```

Now we scale those counts up or down according to the relative prices. Price effects often follow a logarithmic function rather than a linear function, so we use log(price) here:

```
# scale sales according to the ratio of log(price)
> tmp.sales1 <- tmp.sales1 * log(store.df$p2price) / log(store.df$p1price)
> tmp.sales2 <- tmp.sales2 * log(store.df$p1price) / log(store.df$p2price)</pre>
```

We have assumed that sales vary as the *inverse* ratio of prices. That is, sales of Product 1 go up to the degree that the log(price) of Product 1 is lower than the log(price) of Product 2.

Finally, we assume that sales get a 30 % or 40 % lift when each product is promoted in store. We simply multiply the promotional status vector (which comprises all $\{0, 1\}$ values) by 0.3 or 0.4, respectively, and then multiply the sales vector by that. We use the floor() function to drop fractional values and ensure integer counts for weekly unit sales, and put those values into the data frame:

```
# final sales get a 30% or 40% lift when promoted
> store.df$plsales <- floor(tmp.sales1 * (1 + store.df$plprom*0.3))
> store.df$p2sales <- floor(tmp.sales2 * (1 + store.df$p2prom*0.4))</pre>
```

Inspecting the data frame, we see that the data look plausible on the surface:

>	> head(store.df)											
	storeNum	Year	Week	p1sales	p2sales	plprice	p2price	plprom	p2prom	country		
1	101	1	1	127	106	2.29	2.29	0	0	US		
2	101	1	2	137	105	2.49	2.49	0	0	US		
3	101	1	3	156	97	2.99	2.99	1	0	US		

A final command is useful to inspect data because it selects rows at random and thus may find problems buried inside a data frame away from the head or tail: some() from the car package [51]:

```
> install.packages("car")  # if needed
> library(car)
> some(store.df, 10)
    storeNum Year Week plsales plsales plprice plprom p2prom country
27     101  1  27  135  99  2.29  2.49     0     0     US
144     102  1  40  123  113  2.79  2.59     0     0     US
473     105  2  5  127  96  2.99  3.19     0     0     DE
```

Thanks to the power of R, we have created a simulated data set with 20,800 values (2,080 rows \times 10 columns) using a total of 22 assignment commands. In the next section we explore the data that we created.

3.2 Functions to Summarize a Variable

Observations may comprise either *discrete* data that occurs at specific levels or *continuous* data with many possible values. We look at each type in turn.

3.2.1 Discrete Variables

A basic way to describe discrete data is with frequency counts. The table() function will count the observed prevalence of each value that occurs in a variable

(i.e., a vector or a column in a data frame). In store.df, we may count how many times Product 1 was observed to be on sale at each price point:

```
> table(store.df$p1price)
2.19 2.29 2.49 2.79 2.99
395 444 423 443 375
```

If your counts vary from those above, that may be due to running commands in a different order or setting a different random number seed. The counts shown here assume that the commands have been run in the exact sequence shown in this chapter. There is no problem if your data is modestly different; just remember that it won't match the output here, or try Sect. 3.1.1 again.

One of the most useful features of R is that most functions produce an object that you can save and use for further commands. So, for example, if you want to save the table that was created by table(), you can just assign the same command to a named object:

```
> p1.table <- table(store.df$p1price)
> p1.table
2.19 2.29 2.49 2.79 2.99
395 444 423 443 375
> str(p1.table)
'table' int [1:5(1d)] 395 444 423 443 375
...
```

The str() command shows us that the object produced by table() is a special type called table. You will find many functions in R produce objects of special types. We can also easily pass pl.table to the plot() function to produce a quick plot.

> plot(p1.table)

You can see from the resulting bar plot in Fig. 3.1 that the product was on sale at each price point roughly the same number of times. R chose a type of plot suitable for our table object, but it is fairly ugly and the labels could be clearer. Later in this chapter we show how to modify a plot to get better results.

An analyst might want to know how often each product was promoted at each price point. The table() command produces two-way *cross tabs* when a second variable is included:



Fig. 3.1. A simple bar plot produced by passing a table object to plot(). Default charts are sometimes unattractive, but there are many options to make them more attractive and useful.

At each price level, Product 1 is observed to have been promoted approximately 10% of the time (as expected, given how we created the data in Sect. 3.1.1). In fact, we can compute the exact fraction of times product 1 is on promotion at each price point, if we assign the table to a variable and then divide the second column of the table by the sum of the first and second columns:

The second command takes the second column of table pl.table—the column with counts of how often the product is promoted—and divides by the total count to get the proportion of times the product was promoted at each price point. R automatically applies math operators + and / across the entire columns.

By combining results in this way, you can easily produce exactly the results you want along with code that can repeat the analysis on demand. This is very helpful to marketing analysts who produce weekly or monthly reports for sales, web traffic, and the like.

3.2.2 Continuous Variables

Counts are useful when we have a small number of categories, but with continuous data it is more helpful to summarize the data in terms of its distribution. The most common way to do that is with mathematical functions that describe the range of the data, its center, the degree to which it is concentrated or dispersed, and specific points that may be of interest (such as the 90th percentile). Table 3.1 lists some R functions to calculate statistics for numeric vector data, such as numeric columns in a data frame.

Describe	Function	Value
Extramas	min(x)	Minimum value
Extremes	max(x)	Maximum value
Central tendency	mean(x)	Arithmetic mean
Central tendency	median(x)	Median
	var(x)	Variance around the mean
Dispersion	sd(x)	Standard deviation
Dispersion		(sqrt(var(x)))
	IQR(x)	Interquartile range, 75th-25th per-
		centile
	mad(x)	Median absolute deviation (a ro-
		bust variance estimator)
Points	<pre>quantile(x, probs=c())</pre>	Percentiles

Table 3.1. Distribution functions that operate on a numeric vector

Following are examples of those common functions:

```
> min(store.df$p1sales)
[1] 73
> max(store.df$p2sales)
[1] 225
> mean(store.df$p1prom)
[1] 0.1
> median(store.df$p2sales)
[1] 96
> var(store.df$p1sales)
[1] 805.0044
> sd(store.df$p1sales)
[1] 28.3726
> IQR(store.df$p1sales)
[1] 37
> mad(store.df$p1sales)
[1] 26.6868
> quantile(store.df$p1sales, probs=c(0.25, 0.5, 0.75))
25% 50% 75%
113 129 150
```

In the case of quantile() we have asked for the 25th, 50th, and 75th percentiles using the argument probs=c(0.25, 0.5, 0.75), which are also known as the *median* (50th percentile, same as the median() function) and the edges of the *interquartile range*, the 25th and 75th percentiles.

For skewed and asymmetric distributions that are common in marketing, such as unit sales or household income, the arithmetic mean() and standard deviation sd() may be misleading; in those cases, the median() and interquartile range (IQR(), the range of the middle 50% of data) are often more useful to summarize a distribution.

Change the probs = argument in quantile() to find other quantiles:

The second example here shows that we may use sequences in many places in R; in this case, we find every 10th percentile by creating a simple sequence of 0:10 and dividing by 10 to yield the vector 0, 0.1, 0.2 ... 1.0. You could also do this using the sequence function (seq(from=0, to=1, by=0.1)), but 0:10/10 is shorter and more commonly used.

Suppose we wanted a summary of the sales for product 1 and product 2 based on their median and interquartile range. We might assemble these summary statistics into a data frame that is easer to read than the one-line-at-a-time output above. We create a data frame to hold our summary statistics and then populate it using functions from Table 3.1. We name the columns and rows, and fill in the cells with function values:

With this custom summary we can easily see that median sales are higher for product 1 (129 versus 96) and that the variation in sales of product 1 (the IQR across observations by week) is also higher. Once we have this code, we can easily run it the next time we have new sales data to produce a revised version of our table of summary statistics. Such code might be a good candidate for a custom function you can reuse (see Sects. 2.7 and 11.3.1.1). We'll see a shorter way to create this summary in Sect. 3.3.4.

3.3 Summarizing Data Frames

As useful as functions such as mean() and quantile() are, it is tedious to apply them one at a time to columns of a large data frame, as we did with the summary table above. R provides a variety of ways to summarize data frames without writing extensive code. We describe three approaches: the basic summary() command, the describe() command from the psych package, and the R approach to iterating over variables with apply().

3.3.1 summary()

As we saw in Sect. 2.5, summary() is a good way to do a preliminary inspection of a data frame or other object. When you use summary() on a data frame, it reports a few descriptive statistics for every variable:

>	 summar 	у(store.	.df)									
	stor	eN	Jum	Ye	ar	We	ek	plsa	les		p2sa	les	
	101	:	104	Min.	:1.0	Min.	: 1.00	Min.	: 73	Min		: 51.	0
	102	:	104	1st Qu.	:1.0	1st Qu.	:13.75	1st Qu.	:113	1st	Qu.	: 84.	0
	103	:	104	Median	:1.5	Median	:26.50	Median	:129	Med	lian	: 96.	0
	104	:	104	Mean	:1.5	Mean	:26.50	Mean	:133	Mea	n	:100.	2
	105	:	104	3rd Qu.	:2.0	3rd Qu.	:39.25	3rd Qu.	:150	3rd	Qu.	:113.	0
	106	:	104	Max.	:2.0	Max.	:52.00	Max.	:263	Max		:225.	0
	(Other)	:1	456										
	plpr	ic	e	p2p	rice	p	lprom	p2p	rom		coun	try	
	Min.	:2	2.190	Min.	:2.29	Min.	:0.0	Min.	:0.000)	AU:1	.04	
	1st Qu.	:2	2.290	1st Qu	.:2.49	1st Ç	2u.:0.0	lst Qu.	:0.000)	BR:2	08	
	Median	:2	2.490	Median	:2.59	Media	ın :0.0	Median	:0.000)	CN:2	08	
	Mean	:2	2.544	Mean	:2.70	Mean	:0.1	Mean	:0.1385	5	DE:5	20	
	3rd Qu.	:2	2.790	3rd Qu	.:2.99	3rd Q	0.:00	3rd Qu.	:0.0000)	GB:3	12	
	Max.	:2	2.990	Max.	:3.19	Max.	:1.0	Max.	:1.0000)	JP:4	16	
											US:3	12	

summary() works similarly for single vectors, with a horizontal rather than vertical display:

```
> summary(store.df$Year)
Min. 1st Qu. Median Mean 3rd Qu. Max.
1.0 1.0 1.5 1.5 2.0 2.0
```

The digits = argument is helpful if you wish to change the precision of the display:

> summa	ary(sto:	re.df, di	.gits=2)						
st	oreNum	Y	ear	1	Week	p1	sales	p2sa	ales	
101	: 104	Min.	:1.0	Min.	: 1	Min.	: 73	Min.	: 51	
102	: 104	1st Qu	1.:1.0	1st Q	u.:14	1st Q	u.:113	1st Qu	.: 84	
p1price		p2pr	ice	p1	prom	p	2prom	country		
Min.	:2.2	Min.	:2.3	Min.	:0.0	Min.	:0.00	AU:104	1	
lst Q	u.:2.3	1st Qu.	:2.5	1st Qu	.:0.0	lst Q	u.:0.00	BR:20	3	

R generally uses *digits* to mean *significant digits* regardless of absolute magnitude or the decimal position. Thus, digits=3 does not mean "three decimal places" but instead "three significant positions." Output conforming to digits= is not guaranteed; the format may be different in various cases such as reporting integer values and for factors.

Perhaps the most important use for summary() is this: *after importing data, use* summary() to do a quick quality check. Check the min and max for outliers or miskeyed data, and check to see that the mean and median are reasonable and similar to one another (if you expect them to be similar, of course). This simple inspection often turns up errors in the data!

3.3.2 describe()

Another useful command is describe() from the psych package [132]. To use describe(), install the psych package if you haven't done so already and make it available with library():

```
> install.packages("psych")
Installing package ...
> library(psych)
```

describe() reports a variety of statistics for each variable in a data set, including *n*, the count of observations; *trimmed mean*, the mean after dropping a small proportion of extreme values; and statistics such as *skew* and *kurtosis* that are useful when interpreting data with regard to normal distributions.

> describe	describe(store.df)										
	vars	n	mean	sd	median	trimmed	mad	min	max	range	skew
storeNum*	1	2080	10.50	5.77	10.50	10.50	7.41	1.00	20.00	19.0	0.00
Year	2	2080	1.50	0.50	1.50	1.50	0.74	1.00	2.00	1.0	0.00
Week	3	2080	26.50	15.01	26.50	26.50	19.27	1.00	52.00	51.0	0.00
p1sales 	4	2080	133.05	28.37	129.00	131.08	26.69	73.00	263.00	190.0	0.74
country*	10	2080	4.55	1.72	4.50	4.62	2.22	1.00	7.00	6.0	-0.29
	kurto	osis	se								
storeNum*	- 1	1.21	0.13								
Year	- 2	2.00	0.01								
Week	- 1	1.20	0.33								
p1sales	(0.66	0.62								
country*	- (0.81	0.04								

By comparing the trimmed mean to the overall mean, one might discover when outliers are skewing the mean with extreme values. describe() is especially recommended for summarizing survey data with discrete values such as 1–7 Likert scale items from surveys (items that use a scale with ordered values such as "Strongly disagree (1)" to "Strongly agree (7)" or similar).

Note that there is an * next to the labels for storeNum and country in the output above. This is a warning; storeNum and country are factors and these summary statistics may not make sense for them. describe() treats each store number as an integer and computes statistics based on those integers. This may be useful when your factors are in a meaningful order. When data include character strings or other non-numeric data, describe() gives an error, "non-numeric argument." These problems may be solved by selecting only the variables (columns) that are numeric with matrix indices. For example, if we wished to describe only columns 2 and 4 through 9, then we could use the following:

<pre>> describe(store.df[, c(2, 4:9)])</pre>												
	vars	n	mean	sd	median	trimmed	mad	min	max	range	skew	
Year	1	2080	1.50	0.50	1.50	1.50	0.74	1.00	2.00	1.0	0.00	
plsales	2	2080	133.05	28.37	129.00	131.08	26.69	73.00	263.00	190.0	0.74	
p2sales	3	2080	100.16	24.42	96.00	98.05	22.24	51.00	225.00	174.0	0.99	

 plprice
 4
 2080
 2.54
 0.29
 2.49
 2.53
 0.44
 2.19
 2.99
 0.8
 0.28

 p2price
 5
 2080
 2.70
 0.33
 2.59
 2.69
 0.44
 2.29
 3.19
 0.9
 0.32

3.3.3 Recommended Approach to Inspecting Data

We can now recommend a general approach to inspecting a data set after compiling or importing it; replace "my.data" and "DATA" with the names of your objects:

- 1. Import your data with read.csv() or another appropriate function and check that the importation process gives no errors.
- 2. Convert it to a data frame if needed (my.data <- data.frame(DATA) and set column names (names (my.data) <- c(...)) if needed.
- 3. Examine dim() to check that the data frame has the expected number of rows and columns.
- 4. Use head() and tail(my.data) to check the first few and last few rows; make sure that header rows at the beginning and blank rows at the end were not included accidentally. Also check that no good rows were skipped at the beginning.
- 5. Use some () from the car package to examine a few sets of random rows.
- 6. Check the data frame structure with str() to ensure that variable types and values are appropriate. Change the type of variables—especially to factor types—as necessary.
- 7. Run summary() and look for unexpected values, especially min and max that are unexpected.
- Load the psych library and examine basic descriptives with describe(). Reconfirm the observation counts by checking that n is the same for each variable, and check trimmed mean and skew (if relevant).

3.3.4 apply() *

An advanced and powerful tool in R is the apply() command. apply (x=DATA, MARGIN=MARGIN, FUN=FUNCTION) runs any function that you specify on each of the rows and/or columns of an object. If that sounds cryptic, well...it is. In R the term *margin* is a two-dimensional metaphor that denotes which "direction" you want to do something: either along the rows (MARGIN=1) or columns (MARGIN=2), or both simultaneously (MARGIN=c(1, 2)).

Here's an example: suppose we want to find the mean of every column of store.df, except for store.df\$Store, which isn't a number and so doesn't

have a mean. We can apply() the mean() function to the *column* margin of the data like this:

```
> apply(store.df[,2:9], MARGIN=2, FUN=mean)
        Year Week plsales p2sales p1price p2price
    1.5000000 26.5000000 133.0485577 100.1567308 2.5443750 2.6995192
        p1prom p2prom
    0.1000000 0.1384615
```

As it happens, colMeans() does the same thing as the command above, but apply gives you the flexibility to apply any function you like. If we want the *row* means instead, we simply change the margin to 1:

```
> apply(store.df[,2:9], 1, mean)
[1] 29.9475 31.2475 32.9975 29.2725 31.2600 31.7850 27.5225 30.7850 28.0725
[10] 31.5600 30.5975 32.5850 25.6350 29.3225 27.9225 30.5350 31.4475 ...
```

Although row means make little sense for this data set, they can be useful for other kinds of data.

Similarly, we might find the sum() or sd() for multiple columns with margin=2:

```
> apply(store.df[,2:9], 2, sum)
Year Week plsales p2sales p1price p2price p1prom p2prom
3120.0 55120.0 276741.0 208326.0 5292.3 5615.0 208.0 288.0
> apply(store.df[,2:9], 2, sd)
Year Week p1sales p2sales p1price p2price ...
0.5001202 15.0119401 28.3725990 24.4241905 0.2948819 0.3292181 ...
```

What if we want to know something more complex? In our discussion of functions in Sect. 2.7, we noted the ability to define an ad hoc *anonymous function*. Imagine that we are checking data and wish to know the difference between the mean and median of each variable, perhaps to flag skew in the data. Anonymous function to the rescue! We can apply that calculation to multiple columns using an anonymous function:

```
> apply(store.df[,2:9], 2, function(x) { mean(x) - median(x) } )
Year Week plsales p2sales plprice p2price p1prom p2prom
0.0000000 0.0000000 4.0485577 4.1567308 0.0543750 0.1095192 0.1000000 0.1384615
```

This analysis shows that the mean of plsales and the mean of plsales are larger than the median by about four sales per week, which suggests there is a righthand tail to the distribution. That is, there are some weeks with very high sales that pull the mean up. (Note that we only use this to illustrate an anonymous function; there are better, more specialized tests of skew, such as those in the psych package.)

Experienced programmers: your first instinct, based on experience with procedural programming languages, might be to solve the preceding problem with a for() loop that iterates the calculation across columns. That is possible in R but less efficient and less "R-like". Instead, try to think in terms of functions that are applied across data as we do here.

There are specialized versions of apply() that work similarly with lists and other object types besides data frames. If interested, check ?tapply and ?lapply.

All of these functions, including apply(), summary(), and describe() return values that can be assigned to an object. For example, using apply, we can produce our customized summary data frame from Sect. 3.2.2 in five lines of code rather than seven:

```
> mysummary2.df <- data.frame(matrix(NA, nrow=2, ncol=2))
> names(mysummary2.df) <- c("Median Sales", "IQR")
> rownames(mysummary2.df) <- names(store.df)[4:5] # names from the data frame
> mysummary2.df[, "Median Sales"] <- apply(store.df[, 4:5], 2, median)
> mysummary2.df[, "IQR"] <- apply(store.df[, 4:5], 2, IQR)
> mysummary2.df
Median Sales IQR
plsales 129 37
p2sales 96 29
```

If there were many products instead of just two, the code would still work if we changed the number of allocated rows, and apply() would run automatically across all of them.

Now that we know how to summarize data with statistics, it is time to visualize it.

3.4 Single Variable Visualization

We start by examining plots that are part of the base R system. We examine histograms, density plots, and box plots, and take an initial look at more complex graphics including maps. Later chapters build on these foundational plots and introduce more that are available in other packages. R has many options for graphics including dedicated plotting packages such as ggplot2 and lattice, and specialized plots that are optimized for particular data such as correlation analysis.

3.4.1 Histograms

A fundamental plot for a single continuous variable is the *histogram*. Such a plot can be produced in R with the hist() function:

> hist(store.df\$p1sales)

The result, which will appear in the graphical display of base R or RStudio, is shown in Fig. 3.2. It is not a bad start. We see that the weekly sales for product 1 range from a little less than 100 to a bit more than 250. Because axes should always be labeled, R tried to provide reasonable labels based on the variables we passed to hist().

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That plot was easy to make but the visual elements are less than pleasing, so we will improve it. For future charts, we will show either the basic chart or the final one, and will not demonstrate the successive steps to build one up. However, we go through the intermediate steps here so you can see the process of how to evolve a graphic in R.

As you work through these steps, there are four things you should understand about graphics in R:

- R graphics are produced through commands that often seem tedious and require trial and iteration.
- Always use a text editor when working on plot commands; they rapidly become too long to type, and you will often want to try slight variants and to copy and paste them for reuse.
- Despite the difficulties, R graphics can be very high quality, portable in format, and even beautiful.
- Once you have code for a useful graphic, you can reuse it with new data. It is often helpful to tinker with previous plotting code when building a new plot, rather than recreating it.

Our first improvement to Fig. 3.2 is to change the title and axis labels. We do that by adding arguments to the hist() command:

main="..." : sets the main title
xlab="..." : sets the X axis label
ylab="..." : sets the Y axis label

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We add the title and axis labels to our plot command:

```
> hist(store.df$p1sales,
+ main="Product 1 Weekly Sales Frequencies, All Stores",
+ xlab="Product 1 Sales (Units)",
+ ylab="Count" )
```

Product 1 Weekly Sales Frequencies, All Stores





The result is shown in Fig. 3.3 and is improved but not perfect; it would be nice to have more granularity (more bars) in the histogram. While we're at it, let's add a bit of color. We adjust the graphic by asking for more bins (*breaks*) and color the histogram bars light blue. Here are the arguments involved:

breaks=NUM : suggest NUM bars in the result

col="..." : color the bars

When specifying colors, R knows many by name, including the most common ones in English ("red", "blue", "green", etc.) and less common (such as "coral" and "burlywood"). Many of these can be modified by adding the prefix "light" or "dark" (thus "lightgray", "darkred", and so forth). For a list of built-in color names, run the colors () command.

We add breaks= and col= arguments to our code, with the result shown in Fig. 3.4:

```
> hist(store.df$p1sales,
+ main="Product 1 Weekly Sales Frequencies, All Stores",
+ xlab="Product 1 Sales (Units)",
+ ylab="Count",
+ breaks=30,  # more columns
+ col="lightblue") # color the bars
```

Product 1 Weekly Sales Frequencies, All Stores





Comparing Figs. 3.4 with 3.3 we notice a new problem: the y-axis value for the height of the bars changes according to count. The count depends on the number of bins and on the sample size. We can make it absolute by using *relative frequencies* (technically, the *density* estimate) instead of counts for each point. This makes the Y axis comparable across different sized samples.

Figure 3.4 also has ugly and oddly centered numbering on the X axis. Instead of using hist()'s default *tick marks* (axis numbers), we remove the axis in order to replace it with one more to our liking. The arguments for relative frequency and removing the X axis are:

```
freq=FALSE : use density instead of counts on Y axis
```

xaxt="n" : X axis text is set to "none"

Now we need to create the replacement axis. This can be done with axis(side= MARGIN, at=VECTOR). Note that axis() is a second command and not an argument to hist(); hist() creates the plot and then axis() modifies it.

Here is the amended code. First we call hist() to create a new plot without an X axis :

With axis (), we specify which axis to change using an argument: side=1 alters the X axis, while side=2 alters the Y axis (the top and right axes are side=3 and side=4, respectively). We have to tell it where to put the labels, and the argument

at=VECTOR specifies the new tick marks for the axis. These are easily made with the seq() function to generate a sequence of numbers:

> axis(side=1, at=seq(60, 300, by=20)) # add "60", "80", ...

The updated histogram is shown in Fig. 3.5. It is looking good now!





Finally, we add a smoothed estimation line. To do this, we use the density() function to estimate density values for the plsales vector, and add those to the chart with the lines() command. The lines() command adds elements to the current plot in the same way we saw above for the axis command.

```
> lines(density(store.df$plsales, bw=10),  # "bw= ..." adjusts the smoothing
+ type="l", col="darkred", lwd=2)  # lwd = line width
```

Figure 3.6 is now very informative. Even someone who is unfamiliar with the data can easily tell that this plot describes weekly sales for product 1 and that the typical sales range from about 80 to 200.

The process we have shown to produce this graphic is representative of how analysts use R for visualization. You start with a default plot, change some of the options, and use functions like axis() and density() to alter features of the plot with complete control. Although at first this will seem cumbersome compared to the drag-and-drop methods of other visualization tools, it really isn't much more time consuming if you use a code editor and become familiar with the plotting functions' examples and help files. It has the great advantage that once you've written the code, you can reuse it with different data.

Exercise: modify the code to create the same histogram for product 2. It requires only minor change to the code whereas with a drag-and-drop tool, you would start all over. If you produce a plot often, you could even write it as a custom function.

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Fig. 3.6. Final histogram with density curve.

3.4.2 Boxplots

Boxplots are a compact way to represent a distribution. The R boxplot() command is straightforward; we add labels and use the option horizontal=TRUE to rotate the plot 90° to look better:

Figure 3.7 shows the resulting graphic. The boxplot presents the distribution more compactly than a histogram. The median is the center line while the 25th and 75th percentiles define the *box*. The outer lines are *whiskers* at the points of the most extreme values that are no more than 1.5 times the width of the box away from the box. Points beyond the whiskers are outliers drawn as individual circles. This is also known as a *Tukey boxplot* (after the statistician, Tukey) or as a *box-and-whiskers* plot.





Boxplots are even more useful when you compare distributions by some other factor. How do different stores compare on sales of product 2? The boxplot() command makes it easy to compare these by specifying a response *formula* using *tilde notation*, where the tilde ("~") separates the *response variable* (sometimes called a *dependent* variable) from the *explanatory variable* (sometimes rather misleadingly

called an *independent variable*). In this case, our response variable is p2sales and we want to plot it with regard to the explanatory variable storeNum. This may be easiest to understand with the R code:

```
> boxplot(store.df$p2sales ~ store.df$storeNum, horizontal=TRUE,
+ ylab="Store", xlab="Weekly unit sales", las=1,
+ main="Weekly Sales of P2 by Store")
```

The first portion of the command may be read as "boxplot p2sales by Store." Formulas like this are pervasive in R and are used both for plotting and for estimating models. We discuss formulas in detail in Sect. 5.2.1 and Chap. 7.

We added one other argument to the plot: las=1. That forces the axes to have text in the horizontal direction, making the store numbers more readable. The result is Fig. 3.8, where stores are roughly similar in sales of product 2 (this is not a statistical test of difference, just a visualization).



Fig. 3.8. boxplot() of sales by store.

We see in Fig. 3.8 that the stores are similar in unit sales of P2, but do P2 sales differ in relation to in-store *promotion*? In this case, our explanatory variable would be the promotion variable for P2, so we use <code>boxplot()</code> with the response formula again, replacing <code>storeNum</code> with the promotion variable <code>p2prom</code>.

This is a good time to introduce two shortcut commands that make life easier. Many commands for statistics and plotting understand the data=DATAFRAME argument, and will use variables from data without specifying the full name of the data frame. This makes it easy to repeat analyses on different data sets that include the same variables. All you have to do is change the argument for data=.

```
> boxplot(p2sales ~ p2prom, data=store.df, horizontal=TRUE, yaxt="n",
+ ylab="P2 promoted in store?", xlab="Weekly sales",
+ main="Weekly sales of P2 with and without promotion")
> axis(side=2, at=c(1,2), labels=c("No", "Yes"))
```

In this plot we also used axis () to replace the default Y axis with one that is more informative. The result is shown in Fig. 3.9. There is a clear visual difference in sales on the basis of in-store promotion!

To wrap up: boxplots are powerful tools to visualize a distribution and make it easy to explore how an outcome variable is related to another factor. In Chaps. 4 and 5 we explore many more ways to examine data association and statistical tests of relationships.



Fig. 3.9. Boxplot of product sales by promotion status.

3.4.3 QQ Plot to Check Normality*

This is an optional section on a graphical method to evaluate a distribution more formally. You may wish to skip to Sect. 3.4.4 on cumulative distributions or Sect. 3.4.5 that describes how to compute aggregate values in R.

Quantile–quantile (QQ) plots are a good way to check one's data against a distribution that you think it should come from. Some common statistics such as the correlation coefficient r (to be precise, the *Pearson product-moment correlation coefficient*) are interpreted under an assumption that data are normally distributed. A QQ plot can confirm that the distribution is, in fact, normal by plotting the *observed* quantiles of your data against the quantiles that would be *expected* for a normal distribution.

To do this, the qqnorm() command compares data vs. a normal distribution; you can use qqline() to add a diagonal line for easier reading. We check plsales to see whether it is normally distributed:

```
> qqnorm(store.df$p1sales)
> qqline(store.df$p1sales)
```

The QQ plot is shown in Fig. 3.10. The distribution of plsales is far from the line at the ends, suggesting that the data is not normally distributed. The upward curving shape is typical of data with high positive skew.

What should you do in this case? If you are using models or statistical functions that assume normally distributed data, you might wish to transform your data. As we've already noted, a common pattern in marketing data is a logarithmic distribution. We examine whether plsales is more approximately normal after a log() transform:

```
> qqnorm(log(store.df$p1sales))
> qqline(log(store.df$p1sales))
```



Fig. 3.10. QQ plot to check distribution. The tails of the distribution bow away from the line that represents an exact normal distribution, showing that the distribution of plsales is skewed.

The QQ plot for $\log(plsales)$ is shown in Fig. 3.11. The points are much closer to the solid line, indicating that the distribution of $\log(store.df\plsales)$ is more consistent with the normal distribution than the untransformed variable.



Fig. 3.11. QQ plot for the data after log() transformation. The sales figures are now much better aligned with the *solid line* that represents an exact normal distribution.

We recommend that you use qqnorm() (and the more general qqplot() command) regularly to test assumptions about your data's distribution. Web search will reveal further examples of common patterns that appear in QQ plots and how to interpret them.

3.4.4 Cumulative Distribution*

This is another optional section, but one that can be quite useful. If you wish to skip ahead to cover just the fundamentals, you should continue with Sect. 3.4.5.

Another useful univariate plot involves the impressively named *empirical cumulative distribution function* (ECDF). It is less complex than it sounds and is simply a plot that shows the cumulative proportion of data values in your sample. This is an easy way to inspect a distribution and to read off percentile values.

Before that we should explain an important thing to know about the R plot() command: plot() can make only a few plot types on its own and otherwise must be given an *object* that includes more information such as X and Y values. Many R functions produce objects automatically that are suitable as input for plot(). A typical pattern looks like this:

```
> my.object <- FUNCTION(my.data)  # not real code
> plot(my.object)
```

... or combined into a single line as:

```
> plot(FUNCTION(my.data))  # not real code
```

We plot the ECDF of plsales by combining a few steps. First, we use the ecdf() function to find the ECDF of the data. Then we wrap plot() around that, adding options such as titles. Next we put some nicer-looking labels on the Y axis that relabel the proportions as percentiles. The paste() function combines a number vector (0, 10, 20, ...) with the "%" symbol to make each label.

Suppose we also want to know where we should expect 90% of sales figures to occur, i.e., the 90th percentile for weekly sales of P1. We can use the function abline() to add vertical and horizontal lines at the 90th percentile. We do not have to tell R the exact value at which to draw a line for the 90th percentile; instead, we use quantile(, pr=0.9) to find it:

```
> plot(ecdf(store.df$plsales),
+ main="Cumulative distribution of P1 Weekly Sales",
+ ylab="Cumulative Proportion",
+ xlab=c("P1 weekly sales, all stores", "90% of weeks sold <= 171 units"),
+ yaxt="n")
> axis(side=2, at=seq(0, 1, by=0.1), las=1,
+ labels=paste(seq(0,100,by=10), "%", sep=""))
> abline(h=0.9, lty=3)  # "h=" for horizontal line; "lty=3" for dotted
> abline(v=quantile(store.df$plsales, pr=0.9), lty=3)  # "v=" for vertical line
```

The resulting plot is shown in Fig. 3.12. We often use cumulative distribution plots both for data exploration and for presenting data to others. They are a good way to highlight data features such as discontinuities in the data, long tails, and specific points of interest.

3.4.5 Language Brief: by() and aggregate()

What should we do if we want to break out data by factors and summarize it, a process you might know as "cross-tabs" or "pivot tables"? For example, how can we compute the mean sales by store? We have voluminous data (every store by every week by each product) but many marketing purposes only need an aggregate figure such as a total or mean. We saw in Sect. 3.3.4 how to summarize data with



Fig. 3.12. Cumulative distribution plot with lines to emphasize the 90th percentile. The chart identifies that 90 % of weekly sales are lower than or equal to 171 units. Other values are easy to read off the chart. For instance, roughly 10 % of weeks sell less than 100 units, and fewer than 5 % sell more than 200 units.

various statistics and plots, and to summarize across columns with the apply() function. Now we will see how to summarize by a factor within the data itself using the commands by() and aggregate().

Let's look first at by (data=DATA, INDICES=INDICES, FUN=FUNCTION). by () uses INDICES as grouping factors to divide DATA into subgroups. Then it applies the function FUN to each subgroup.

This is easier to understand in the context of an example. Suppose we wish to find the average sales of P1 by store. The DATA would be the weekly sales for each store, store.df\$p1sales. We wish to split this by store, so the INDICES (actually, "index" in this case) would be store.df\$storeNum. Finally, we get the average of each of those groups by using the mean function. Here is the complete command to break out mean sales of P1 by store:

To group it by more than one factor, use a list() of factors. For instance, we can obtain the mean of plsales by store and by year:

: 1 [1] 129.7115

A limitation of by() is that the result is easy to read but not structured for reuse. How can we save the results as data to use for other purposes such as plotting?

The answer is aggregate() which operates almost identically to by() but returns a nicely formatted data frame. The following computes the total (sum()) sales of P1 by country:

```
> aggregate(store.df$plsales, by=list(country=store.df$country), sum)
 country
           x
1
  AU 14544
2
      BR 27836
3
      CN 27381
4
      DE 68876
5
     GB 40986
    JP 55381
6
7 US 41737
```

How does this work? Just as with by(), aggregate(x=DATA, by=BY, FUN=FUNCTION) applies a particular function (FUN) according to divisions of the data specified by a factor (by). We want to find the total sales by country, so we apply the mean function by store.df\$country.

If we want to save the result as a new data frame, we simply assign it somewhere as we do now because we will use it in Sect. 3.4.6 to make a map:

```
> plsales.sum <- aggregate(store.df$plsales,
+ by=list(country=store.df$country), sum)
> plsales.sum
country x
1 AU 14544
2 BR 27836
3 CN 27381
...
```

aggregate() gave us a nicely structured data frame with our summary. We will see further options for aggregate() in Sect. 5.2.1.

3.4.6 Maps

We often need to plot marketing data on a map. A common variety is a *choropleth* map, which uses graphics or color to indicate values of a variable such as income or sales. We consider how to do this for a world map using the rworldmap package [146].

Here is a routine example. Suppose that we want to chart the total sales by country. We use aggregate() as in Sect. 3.4.5 to find the total sales of P1 by country:

To make a map, we'll use the rworldmap package for plotting routines [146], plus the RColorBrewer package [121] to generate some better-looking colors.

```
> install.packages(c("rworldmap", "RColorBrewer")) # if needed
> library(rworldmap)
```

```
> library(RColorBrewer)
```

First, we have to associate the aggregated data with specific map regions using the country codes. This can be done with the joinCountryData2Map() function, which matches country locations (store.df\$country) for data points with the corresponding international standard names (*ISO* names) and returns a map object:

Let's inspect that command more closely. The data object that we wish to map is the plsales.sum aggregated data frame. We place that on a map according to the 2-letter country names (joinCode="ISO2") which are present in the data object as the "country" column.

Next we draw the resulting map object using mapCountryData(), selecting colors from the RColorBrewer package "Greens" palette. We plot the column named x because that is the default name that the aggregate() function gives in the aggregated data fame:

```
> mapCountryData(plsales.map, nameColumnToPlot="x",
+ mapTitle="Total Pl sales by Country",
+ colourPalette=brewer.pal(7, "Greens"),
+ catMethod="fixedWidth", addLegend=FALSE)
```

The result is shown in Fig. 3.13, known as a *choropleth* chart.

Although such maps are popular, they can be misleading. In *The Wall Street Journal Guide to Information Graphics*, Wong explains that choropleth charts are problematic because they confuse geographic area with scaled quantities [168, p. 90]. For instance, in Fig. 3.13, China is more prominent than Japan not because it has a higher value but because it is larger in size. We acknowledge the need for caution despite the popularity of such maps.

For more complex charts, there are options in ?rworldmap for drawing regional maps, more granular areas, setting color palettes, using locations other than country codes, and so forth. For other mapping options, see the suggestions in Sect. 3.5 below.



Fig. 3.13. World map for P1 sales by country, using rworldmap.

3.5 Learning More*

Plotting. We demonstrate plotting in R throughout this book. R has multiple, often disjoint solutions for plotting and in this text we use plots as appropriate without going deeply into their details. The *base* plotting system comes standard in R and appears in commands such as hist() and plot().

Two popular and powerful packages that produce more complex graphics are lattice [141] and ggplot2 [162]. The choice between lattice and ggplot2 is largely a matter of personal preference and style. We sometimes suspect that lattice appeals more to scientists and engineers while ggplot2 appeals to computer scientists and social scientists. Chang's *R Graphics Cookbook* [24] is a single volume overview of many kinds of plots available in R, focused on the ggplot2 package.

Wong's *The Wall Street Journal Guide to Information Graphics* [168] presents fundamentals of good style for effective graphics in any business context (not specific to R).

Maps. Producing maps in R is an especially complex topic. Maps require three essential components: *shape files* that define the borders of areas (such as country or city boundaries); *spatial translation* of one's data (for instance, a database to match Zip codes in your data to the relevant areas on a map); and *plotting software* to perform the actual plotting. R packages such as rworldmap usually provide access to all three of those elements.

As of this writing, the landscape of available packages and tools for mapping in R was changing rapidly. We use the rworldmap package here for its simplicity.

For more complex tasks, the ggplot2 package [162] serves as the basis for a sophisticated mapping tool, the ggmap package [90].

3.6 Key Points

The following guidelines and pointers will help you to describe data accurately and quickly:

- Consider simulating data before collecting it, in order to test your assumptions and develop initial analysis code (Sect. 3.1).
- Always check your data for proper structure and data quality using str(), head(), summary(), and other basic inspection commands (Sect. 3.3.3).
- Describe discrete (categorical) data with table() (Sect. 3.2.1) and inspect continuous data with describe() from the psych package (Sect. 3.3.2).
- Histograms (Sect. 3.4.1) and boxplots (Sect. 3.4.2) are good for initial data visualization.
- Use by() and aggregate() to break out your data by grouping variables (Sect. 3.4.5).
- Advanced visualization methods include cumulative distribution (Sect. 3.4.4), normality checks (Sect. 3.4.3), and mapping (Sect. 3.4.6).