# **Chapter 3 Multi-Phase Shear Thickening Fluid**



**Mohammad Rauf Sheikhi and Mahdi Hasanzadeh**

## **Nomenclature**



M. R. Sheikhi  $(\boxtimes)$ 

M. Hasanzadeh

Department of Textile Engineering, Yazd University, Yazd, Iran

State Key Laboratory for Strength and Vibration of Mechanical Structures, Shaanxi ERC of NDT and Structural Integrity Evaluation, School of Aerospace Engineering, Xi'an Jiaotong University, Xi'an, China

Key Laboratory of Traffic Safety on Track of Ministry of Education, School of Traffic & Transportation Engineering, Central South University, Changsha, Hunan, China e-mail: [4121999205@stu.xjtu.edu.cn](mailto:4121999205@stu.xjtu.edu.cn)

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### **3.1 Introduction**

Shear thickening fuid (STF) is a type of non-Newtonian fuid whose viscosity increases as shear rate increases. In other words, at high shear rates, the viscosity of STF rises dramatically, and it behaves like a solid. However, once the impact stress is removed, STF reverts to a liquid-like state as soon as shear is removed. The reversible process is considered as the main favorable feature of STF. This phenomenon is of special interest for both scientifc and technological issues in developing engineering applications [\[1](#page-15-0), [2](#page-15-1)]. Notably, this phenomenon was initially defned as a problem in many industrial processes such as coating and mixing. For instance, shear thickening leads to the failure of mixer motors due to overloading. However, the unique characteristics of the STF have been used in developing smart materials and structures more recently. For instance, STF has been combined with high performance fabrics to provide a uniquely thin, fexible, cost-effective material that is comparable to or even better than the present protective materials in terms of ballistic, stab, and puncture protection. The idea of impregnating fabric with STF to increase the impact resistance of textile structures has recently attracted a lot of attention [\[3](#page-15-2)[–8](#page-15-3)]. The absorption of the shock waves from the earthquake or severe wind conditions and the integration of STF within the damper systems are other applications of STF that have been recently investigated [[9\]](#page-15-4). STF is recommended for structural components to increase the vibratory and damage resistance of systems and to avoid unexpected accelerations; it should also limit the range of motion in the shoulders, knees, elbows, ankles, and hips [[10\]](#page-15-5). Figure [3.1](#page-2-0) depicts the rise of STF-related publications over the past ten years based on the Scopus database.

STF is a suspension of nano- or micro-particles like silica or silicon dioxide in a Newtonian fuid-like water or polyethylene glycol (PEG). This combination produces a material with extraordinary properties. Common types of STF are silica suspended in ethylene glycol (EG) [[6\]](#page-15-6), polyvinylchloride in dioctyl phthalate [[11\]](#page-15-7), kaolin clay in glycerol [[12\]](#page-15-8), poly(methyl methacrylate) (PMMA) in PEG [[13\]](#page-15-9), fumed silica in propylene glycol [\[14](#page-15-10), [15](#page-16-0)], and silica suspended in PEG [\[16](#page-16-1)]. Among these, the suspension of silica particles in PEG has been extensively investigated and frequently reported in STF literature (Table [3.1](#page-3-0)).

Multi-phase STF suspensions with particle additives have recently been fabricated to beneft from additives. In this chapter, the literature on the rheological characteristics of multi-phase STF is thoroughly reviewed. We discuss the shear thickening mechanism in concentrated colloidal suspension and the crucial factors affecting the rheological characteristics of multi-phase STF. We also explain

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**Fig. 3.1** The number of publications related to STF and multi-phase STF

how additional particles like carbon nanotubes, graphene, and nanoparticles affect the rheology of multi-phase STF systems. It is persuaded that a thorough analysis of the rheological characteristics of multi-phase STF is a crucial frst step in comprehending the function of multi-phase STFs in the creation of engineering structures.

#### **3.2 Shear Thickening Mechanism**

STF, as a non-Newtonian fuid, is usually identifed by a drastic increase in viscosity as the applied shear rate reaches a critical value. Figure [3.2](#page-4-0) shows a schematic representation of shear thickening behavior. In the equilibrium state, the particles are well dispersed in the medium. STF exhibits reduced viscosities at lower shear rates before the critical point. The chaotic nature of the particles under the applied stress leads to the formation of particle layers as shear rate increases. When shear rate increases to further levels, hydroclusters are formed, thereby causing the particles to agglomerate. After the stress is removed from the medium, the suspension reverts into an easy-fowing state and resumes fowing like any other liquid. The shear thickening phenomenon is fully reversible.

Based on the literature, researchers have brought forth some theories to account for the fundamental reasons behind the shear thickening behavior. The "orderdisorder transition" (ODT) [[30–](#page-16-2)[34\]](#page-17-0) and the "hydrocluster" mechanism [[35,](#page-17-1) [36](#page-17-2)]

	Particle	Weight fraction		Molecular		
Particles	$size$ (nm)	$(\%)$	Liquid medium	weight (g/ mol)	Application	Ref.
Colloidal silica	N/A	40	EG	N/A	<b>Ballistic</b> protection with STF-impregnated textiles	[6]
Spherical silica	15	40	<b>PEG</b>	200	Stab protection with STF-impregnated textiles	$\lceil 7 \rceil$
Nanosilica	500	$34 - 38$	EG	N/A	Stab protection with STF-impregnated textiles	$\lceil 8 \rceil$
Silica and <b>PMMA</b>	N/A	N/A	<b>PEG</b>	200	Puncture protection with STF-impregnated textiles	$\lceil 13 \rceil$
Spherical silica	650	$75 - 88$	<b>PEG</b>	N/A	Rheological properties of STF	$[17]$
Fumed silica	12	$4 - 9$	PEG	200 and 400	Rheological properties of STF	$[18]$
Fumed silica	14	20, 30, and 40	EG	N/A	Vibration damping with STF	$[19]$
Spherical silica and fumed silica	120 300-400	$5 - 65$	EG and <b>PEG</b>	200	Stab and ballistic protection with STF-impregnated textiles	$[20]$
Silica and <b>PMMA</b>	500	$0.64$ and 0.51	<b>PEG</b>	200	Impact protection with STF-impregnated textiles	$[21]$
Spherical silica	100, 300, 500	65	<b>PEG</b>	200	<b>Ballistic</b> protection with STF-impregnated textiles	$[22]$
Silica in aqueous dispersion	100	50, 60, and 70	<b>PEG</b>	200	<b>Ballistic</b> protection with STF-impregnated textiles	$\lceil 23 \rceil$
Colloidal silica	450	67	<b>PEG</b>	200	Puncture protection with STF-impregnated textiles	$\lceil 24 \rceil$
Silica	450	$35 - 40$	EG	N/A	Rheological properties of STF	$[25]$
Clay	30	N/A	PEO	400,000	Microstructural properties of STF	$[26]$
$ZIF-8$	240-400	$51 - 56$	EG	N/A	Rheological properties of STF	$\left[27\right]$
Core-shell structured silica@PDA	360	58-64	<b>PEG</b>	200	Rheological properties of STF	$[28]$
$PS-AA$ nanospheres	330	$50 - 56$	EG	N/A	Rheological properties of STF	$[29]$

<span id="page-3-0"></span>**Table 3.1** Single-phase STFs prepared by different particles and liquid mediums

<span id="page-4-0"></span>

**Fig. 3.2** Standard STF viscosity graph illustrating colloidal suspensions' shear thinning and thickening behavior

provide a more comprehensive explanation of this behavior than the other ideas. The ODT explains how the application of shear rate causes the particle arrangements to break down in the suspension, increasing the drag forces between the particles. Hoffman [[37\]](#page-17-3), one of the pioneers to research shear thickening in depth, created a micromechanical model of shear thickening as a fow-induced ODT based on this information. He suggested that the shear thickening tendency was the result of a change from a layer-ordered easy-fowing state to a disordered state. He claimed that the van der Walls-London, electric double layer, and shear stress forces acting on a collection of particles are responsible for this transformation. Additionally, it was proposed that the particles within the moving layers undergo hydrodynamically induced forces, which will cause the particles to be pushed out of their layer and disturb the orderly fow. When shear rate reaches a critical point, this transition shows a sharp increase in viscosity. Particle interactions in a liquid medium are the generation of the hydrocluster mechanism. Based on this, it can be stated that hydrodynamic lubricating forces between particles are the source of shear thickening behavior in concentrated colloidal suspensions. Hydrodynamic pressure increases when particles suspended in a fuid collide upon applying shear stress. Due to the formation of clusters under shear force, the drag forces between the particles grow stronger. Rheological, rheo-optic, and fow-SANS studies, as well as computer simulations, are used to experimentally support the hydrocluster mechanism [[38\]](#page-17-4). Although the microscopic mechanisms have been proposed to explain the shear thinning phenomenon, the "hydrocluster" mechanism is more accurate and generalized.

Even though shear thinning is thought to be more common than shear thickening, it has been proposed that shear thickening can occur in all dense mixtures under certain conditions [\[15](#page-16-0)]. However, one of the major challenges is determining why

not all dense mixtures show shear thickening properties. One of the more perplexing questions is why mixtures with soft particles, which can easily deform, do not exhibit shear thickening behavior, whereas densely packed mixtures with hard particles do. A recent research has shown that nanoparticle behavior varies signifcantly for hard spheres due to strong electrostatic, charge-dipole, dipole-dipole, and van der Waals interactions. In particular, the interactions between the nanoparticles as well as those between the nanoparticle and liquid medium in such systems infuence the state of the nanoparticles. The literature indicates that lubricating forces and frictional forces play a substantial role in the shear thickening process. To determine the hydrodynamic and contact force contributions to the shear thickening process, Lin et al. [[39\]](#page-17-5) investigated the shear thickening behavior in the interaction of micron-sized silica and latex particles. They found that as the suspension gets thickened, increasing the shear rate causes the contact contribution to growing while the hydrodynamic contribution stays the same. This phenomenon shows how contact forces have a signifcant impact on the shear thickening of dense colloidal suspensions. Based on the contact rheology models [\[39](#page-17-5), [40](#page-17-6)], hydrodynamic lubrication forces produce a Newtonian behavior or shear thinning at low shear rates (Zone I) as a result of the insignifcant interactions between particles. Lubrication breaks down when the shear rate (Zone II) is increased. As a result, frictional forces result in force chains, which cause discontinuous shear thickening [\[41](#page-17-7)]. The force network becomes tighter as shear rate increases (Zone III), eventually reaching a fully shear jammed state. Large clusters are produced when shear rearranges the particles into anisotropic formations. While frictionless contact results in a smooth and reversible viscosity increase associated with continuous shear thickening, frictional hydrodynamic interactions between suspended particles produce large jumps while rapid increase in viscosity associated with strong and discontinuous shear thickening [[37\]](#page-17-3).

#### **3.3 STF Rheology**

Up till now, several investigations on the rheological characteristics of STF under steady-state and dynamic conditions have been conducted [\[18](#page-16-4), [20\]](#page-16-6). It has been observed that some infuencing elements including particles, fow feld, suspending medium, additives, and the interaction between particles and additives affect the STF rheology [[15,](#page-16-0) [21,](#page-16-7) [42\]](#page-17-8). Table [3.2](#page-6-0) summarizes the key factors infuencing the rheological properties. Particle properties (shape, solid volume fraction, size distribution, and interaction with other particles), suspending phase properties (viscosity and molecular weight of carrier liquid), and STF properties are the main factors infuencing the rheological properties.

Barnes [[15\]](#page-16-0) suggested that above the particle volume fraction of 0.5, the fuid's behavior changes dramatically with shear rate. The critical shear rate (the shear rate at which shear thickening begins) decreases as the volume fraction of the particle increases. Similarly, Kang et al. [\[20](#page-16-6)] investigated the effect of silica loading on the

Parameter	Description	Effects on the rheology of STF		
Particles	Shape	Decreasing the critical shear rate by increasing the aspect ratio of particles		
	<b>Size</b>	Decreasing the critical shear rate with increasing the particle size		
	Size distribution	Decreasing the critical shear rate with narrow particle size distribution		
	Solid volume fraction	Decreasing the critical shear rate by increasing the solid volume fraction		
	Particle-particle interaction	Deflocculated suspensions exhibit shear thickening at a high shear rate		
	Hardness	Better shear thickening behavior for silica particles with higher hardness		
Suspending phase	Molecular weight and viscosity	Decreasing the critical shear rate by increasing the molecular weight of suspending phase		
STF properties	Temperature	Decreasing the critical shear rate with decreasing STF temperature		
	pН	Increasing the critical shear rate with increasing the pH of STF		

<span id="page-6-0"></span>**Table 3.2** Key factors on STF rheology

shear thickening properties. They stated that critical shear rate develops at lower shear rates as silica particle concentration increases. Moreover, with increasing the silica particle concentration, the shear thickening phenomenon realizes sharply. Wetzel et al. [[43\]](#page-17-9) found that when the aspect ratio of the particles grows, lower volume percentages of particles are sufficient to trigger the shear thickening behavior. According to Maranzano et al. [\[42](#page-17-8)] particle size signifcantly affects the transition from reversible shear thickening to dense colloidal suspensions. They also noted that the fow curves systematically change to decrease shear stresses as particle size increases. Lee et al. [[22\]](#page-16-8) also observed a similar pattern of behavior. Kang et al. [\[20](#page-16-6)] reported the temperature effect on the critical shear rate and STF viscosity. From this work, as temperature increases, hydrodynamic interactions grow stronger due to the increased Brownian motion with the colloidal particles and, thus, critical shear rate slightly moves toward higher shear rates.

Is there a regulating factor, such as a range above or below which the critical shear rates appear to be lower? As was already mentioned, the solid volume percentage affects how colloidal suspensions thicken under shear. However, due to variations in form, size, size distribution, and interaction with other particles, distinct nanoparticles display different shear thickening rheology. The solid particle amount cannot, therefore, be the only determining factor. Another diffculty is knowing how to change STF characteristics. Creating a straightforward and organized way of showing the interrelated effects of elements is another challenge. There has not been any publication on comprehensive quantitative analysis of effective parameters yet in the literature.

#### **3.4 Rheology of Multi-phase STF**

Several studies on the rheological behavior of STF have been conducted up to now. Integrating particle additives into STF and studying the rheological behavior of multi-phase STF have recently received much attention. As mixtures of singlephase STF and different additives, multi-phase STF offers the opportunity to tune the rheological behavior of suspension concerning the application feld. For example, Hasanzadeh and Mottaghitalab [\[44](#page-17-10)] investigated the use of multi-walled carbon nanotubes (MWCNTs) as an additive to tune the rheological properties of a fumed silica/PEG-based STF. Rheological measurements revealed that MWCNTs have a signifcant impact on the rheology of STF. Even at low concentrations of MWCNTs  $(0.4 \text{ wt.}\%)$ , the critical viscosity of the STF decreases with the addition. Furthermore, shear thickening appears at higher shear rates in the multi-phase STF system. In other words, the MWCNTs interfere with the shear thickening behavior. The proposed mechanism of MWCNT incorporation and shear thickening behavior of a multi-phase STF system is depicted in Fig. [3.3.](#page-7-0) According to this mechanism, the increased interactions between the fumed silica nanoparticles, PEG as a carrier fuid, and MWCNTs are responsible for affecting the shear thickening properties. The silanol groups on the surface of fumed silica nanoparticles form hydrogen bonds with the PEG hydroxyl groups and the internal oxygen atoms. When MWCNTs are added to the STF, the hydroxyl/carboxyl groups on the MWCNT surfaces can form hydrogen bonding with silica particles and PEG. However, hydrogen bonds are more likely to be formed with PEG than with silica particles. Fourier transform infrared spectroscopy (FTIR) confrms that the hydrogen bonding in the MWCNT-silica-PEG suspension enhances. As a result of the strong interactions between MWCNTs and PEG, higher shear force is needed to withstand the strong interactions, and the thickening in the mixture is postponed to higher critical shear rates. Finally, the presence of MWCNTs in the STF reduces the thickening ratio so that the shear thickening properties.

<span id="page-7-0"></span>

**Fig. 3.3** The mechanism of incorporation of MWCNTs additive on the rheological behavior of multi-phase STFs

<span id="page-8-0"></span>

increase in the "particle clustering" spacing, and the shear thickening effect is destroyed.





(b) Interaction between MWNT and silica nanoparticles in 0.8%MWNT/SiO<sub>2</sub>-STF

**Fig. 3.4** The schematic of the mechanism of interaction between silica and MWCNTs in multiphase STF [[45](#page-17-11)]. Reprinted by permission from Springer

A similar study on the rheological behavior of multi-phase STF with MWCNTs additive was carried out by Wei et al. [[45\]](#page-17-11). They found that the peak viscosity of the multi-phase STF with 1 wt.% MWCNTs increases about 360% and the critical shear rate decreases about 70%. Investigation of the variation of the mass fraction of MWCNT additives shows the irregular change in the viscosity of multi-phase STF. For instance, the multi-phase STF with 0.2 wt.% MWCNTs does not show shear thickening behavior, which is likely due to the hindering of the fow by focculent structure and the large aspect ratio of MWCNT. Figure [3.4](#page-8-0) shows the schematic of the interaction mechanism between silica and MWCNTs. In multi-phase STF with a low mass fraction of MWCNT, a large amount of silica nanoparticles adsorbs on a small amount of MWCNT and forms a larger new particle group containing MWCNT. Due to the no "particle clustering" mechanism, the multi-phase STF (2 wt.% MWCNT) has no obvious shear thickening effect. However, when the mass fraction of MWCNTs increases, the "particle clustering" mechanism

develops. The reason is that increasing the mass fraction of MWCNT leads to an increase in the interaction forces between the particles as well as the number of new particles, which decreases the inter-particle distances and thereby hinders their fow. Hence, a signifcant shear thickening phenomenon occurs. Wei et al. [\[45](#page-17-11)] also studied the thermal effect on the rheology of multi-phase STF and found a signifcant effect of temperature on the shear thickening behavior. The temperature sensitivity of multi-phase STF is similar to that of single-phase STF and dominates by silica nanoparticles. The MWCNT can signifcantly enhance the shear thickening effect without infuencing the temperature sensitivity. At higher temperatures, the shear thickening properties of multi-phase STF weaken due to the poor hydrogen bonds. This phenomenon may be due to the good thermodynamic properties and high thermal conductivity of MWCNTs. Hence, the temperature of each component in the STF is similar and the particle distribution is uniform due to the effective heat transfer at an elevated temperature environment.

Li et al. [\[46](#page-17-12)] studied the shear thickening rheology of a silica and PEG-based STF using oxygen-plasma-modifed MWCNTs for improving the quasi-static stab resistance of textiles. They modifed the MWCNTs with plasma treatment, due to the van der Waals interactions and the hydrophobicity of MWCNTs, which led to the agglomeration in STF. The rheology of multi-phase STF was investigated in different mass friction of modifed-MWCNTs (0.02–0.06 wt.%). The results showed that the multi-phase STF with 0.06 wt.% of modifed MWCNTs exhibits an enhanced peak viscosity of about 120%. Similarly, the critical shear rate reduces by 80%. The multi-phase STF displays higher yield stress in comparison with the single-phase STF. The stronger network formed by the modifed-MWCNTs enhances the interaction between the M-MWCNTs and silica particles. This is likely due to the presence of oxygen-containing functional groups, such as hydroxyl and carboxyl groups, on the surface of the modifed-MWCNTs, which facilitate the formation of hydrogen bonds with silanol groups on the surface of silica. Hence, more interaction between silica particles and modifed-MWCNTs leads to the easy formation of "hydrocluster" and consequently shear thickening at a lower shear rate.

In another study by Gürgen et al. [[47,](#page-17-13) [48\]](#page-17-14), various ceramic particles have been used in a silica-based STF. They found that the incorporation of ceramic particles into STF disrupts the thickening behavior. Moreover, the thickening behavior is dependent on the parameters, including the amount and particle size of additives. For example, at higher loadings of ceramic particles, the volume fraction of silica falls below the effective limit and the shear thickening behavior of suspension fades away. They suggested that the incorporation of additive particles to STF may disrupt the thickening behavior in two ways: (i) lowering the silica percentage of particles by adding additives and (ii) shortening the hydrocluster networks along suspensions due to interstitial additive particles. According to the hydrocluster thickening mechanism, the more the extended hydroclusters, the more the powerful shear thickening behavior. The ceramic micro-particles in suspension occupy the large volume in silica nanoparticles medium and thereby hinders the extension of hydroclusters. Hence, in the multi-phase STFs, the contact networks of silica particles are less likely to form than in the single-phase STF. Moreover, the coarser particles have

signifcant effects on the weakening of shear thickening behavior in comparison to fner particles. This is likely attributed to the larger distance between silica particles in the fow induced by the coarser particles. The ceramic particles with smaller sizes have less effect on the hydroclusters and thickening behavior. The results show that the coarser ceramic particles lead to a decrease in the critical shear rate and the thickening properties of the suspension.

The rheological properties of multi-phase STF were also investigated by using graphene oxide (GO) as an additive. Huang et al. [\[49](#page-17-15)] prepared a multi-phase STF using fumed silica (15 wt.%) and PEG-based suspension. The multi-phase STFs with various amounts (from 0 to 0.3 wt.%) of GO additives were rheologically measured and compared with the single-phase STF. They found that the addition of GO particles leads to a remarkable increase in the viscosity and a decrease in the critical shear rate. Moreover, the thickening ratio gradually decreases with increasing GO content. These results are similar to the output of ceramic particles and MWCNTs investigated by Gürgen et al. [[47,](#page-17-13) [48](#page-17-14)] and Hasanzadeh and Mottaghitalab [\[44](#page-17-10)] respectively. Due to the sheet-like structure of GO, they have a stronger hydrodynamic feld effect than that of the silica particles. Hence, GO additives can cause a stronger congestion effect and, therefore, hydro-clusters can be formed at lower shear rates. Moreover, the strong interaction between the GO additives and silica particles leads to more aggregation of silica nanoparticles on the GO surfaces. However, the incorporation of GO into the STF prevents the hydrocluster elongations and consequently lowers the viscosity increase in the multi-phase STF.

Halloysite nanotubes as an additive (1 to 5 wt.%) in multi-phase STFs have been investigated by Passey [[50\]](#page-17-16). Fumed silica (7 nm) as a solid phase and PEG200 as a liquid medium were utilized for the preparation of the STF. The rheological studies revealed that the halloysite nanotubes disrupt the thickening mechanism of STF and reduce the viscosity of the suspension. They suggested the formation of strong hydrogen bonding between the fumed silica and halloysite nanotubes. The hydrodynamic forces progressively take control of the suspension as shear rate increases, and the nanotubes align themselves in a layered and parallel orientation. The extension of the clusters in the suspension is suppressed by the formation of hydroclusters around the halloysite nanotubes as shear rate is further increased. The inclusion of more halloysite nanotube additives leads to an increase in the critical shear rates. The addition of halloysite nanotubes enhances the surface area of the particles due to the cylindrical morphology and, consequently, more hydrodynamic forces are required for cluster formation. Similarly, Laha et al. [[51\]](#page-17-17) studied the multi-phase STF system using halloysite nanotubes in a spherical silica and PEG200-based STF. However, they discovered that adding more halloysite nanotubes to suspensions causes the critical shear rate to drop. The results demonstrated that the halloysite nanotubes enhance the shear thickening behavior. Although Passey [\[50](#page-17-16)] and Laha et al. [\[51](#page-17-17)] used the same type of additives, the rheology of the suspensions is completely different. Laha et al. [\[51](#page-17-17)] discovered that halloysite nanotubes act as bases for the hydroclusters in which the spherical silica particles are collected around the halloysite nanotubes. In the study by Passey [\[50](#page-17-16)], the halloysite nanotubes do not attract fumed silica while the additives prevent the hydrocluster formation by intercepting the growing of the silica chains. The interaction between the halloysite nanotubes and silica may differ depending on the shape of the silica particles as the spherical silica may be attractive while the fumed silica may be repulsive to the halloysite nanotubes. However, the particle morphology of silica may not be the only factor infuencing the interactions between the silica and additives. Fumed silica, for example, can exist in both hydrophobic and hydrophilic forms, which have a direct impact on the suspension rheology. Hydrophilic silica contains silanol groups, which exhibit enhanced thickening in low polarity media due to strong hydrogen bonds, whereas hydrophobic silica exhibits thickening in high polarity media due to weak hydrogen bonding [\[52](#page-18-0)].

Sha et al. [\[53](#page-18-1)] studied the rheology of a multi-phase STF using graphene nanoplatelets (GNs) and carbon nanotubes (CNTs). The rheology of the STF with spherical silica in a PEG was investigated as well as the effects of GNs and CNTs as additives. They discovered that the suspension viscosity increases as the additive concentration in the STF rises. Additionally, the viscosity of the multi-phase STF can be increased more effectively by CNTs in comparison to GNs. Because CNTs are shaped like long tubes and PEG has long chemical chains, their relative lubricating forces are stronger than those between GNs and PEG. The GNs play as bridges between the silica particles in a liquid, forming hydrogen bonds and thus connecting the aggregated silica groups. Consequently, shear thinning occurs at lower shear rates. PEG-CNTs have a much weaker internal force than PEG-GNs because GNs are sheet-like additives. As a result, phase separation occurs more easily in the CNT suspensions than in the GN suspensions. Furthermore, CNTs having rigid rod shapes in STF can withstand contact forces and, therefore, provide more advances for shear thickening, whereas GNs with two-dimensional soft structures can be easily deformed. Therefore, CNTs are better for shear thickening behavior than GNs. The coexistence of CNTs and GNs on STF further demonstrates that CNTs predominate over GNs concerning suspensions. The viscosity of suspension increases with an increase in the CNTs/GNs ratio in a multi-phase STF. The results demonstrated the enhanced shear thickening behavior by additive incorporation.

The rheological behavior of a multi-phase STF with the incorporation of cellulose nanofbers (CNFs) was investigated by Ghosh et al. [[54\]](#page-18-2). Different concentrations (0.1–0.3 wt.%) of CNFs were used for the preparation of the multi-phase STFs. The rheological measurements showed that the addition of CNFs (0.3 wt.%) to the STF leads to a considerable increase in the viscosity. Moreover, the stronger shear thickening behavior occurs at a lower critical shear rate. This is likely attributed to the large number of hydroxyl groups on the CNFs, which contribute to the formation of hydrogen bonding between the CNFs and silica particles. Increasing the amount of CNFs in the multi-phase STF leads to a reduction in the critical shear rate due to the more interaction between the CNFs with high aspect ratio and silica particles, which induced shear thickening at a lower shear rate. Indeed, the number of available hydroxyl groups increases by increasing the CNFs content, implying stronger interaction and entanglement between the silica particles and CNFs through the formation of a greater number of hydrogen bonds. Figure [3.5](#page-12-0) shows the

<span id="page-12-0"></span>

**Fig. 3.5** Schematic representation of shear thickening behavior of (**a**) single-phase STF and (**b**) multi-phase STF before and after shear

schematic representation of shear thickening behavior in the multi-phase STF using CNFs as additives.

Sun et al. [\[55](#page-18-3)] investigated the rheological properties of a multi-phase STF based on zirconia nanoparticle additives. They found that the incorporation of zirconia nanoparticles into the STF (20% silica nanoparticles) leads to a growth in the shear thickening behavior while increasing the apparent viscosity level. The formation of a cluster of zirconia particles around the functional groups induces the shear thickening behavior and consequently increases the viscosity of the suspension. No regular changes are observed with increasing additive contents. In the multi-phase STF with zirconia content more than the cut-off point (12%), the initial viscosity and critical shear rate increase while the peak viscosity decreases. This is likely due to the hindering of the interaction of the silica nanoparticles by the excess amount of zirconia. Interestingly, the effect of temperature on the viscosity of the multi-phase STF becomes less pronounced when the content of zirconia increases. However, it still signifcantly infuences the critical shear rate and shear thickening behavior.

The rheological behavior of a multi-phase STF was investigated by Sun et al. [\[56](#page-18-4)]. Neodymium oxide  $(Nd_2O_3)$  nanoparticles were used as an additive in the suspensions. They prepared various suspensions with different concentrations (9–15 wt.%) and found that an appropriate amount of  $Nd_2O_3$  (12 wt.%) results in a signifcant increase in the peak viscosity by about 320%. The critical shear rate decreases by 75%. The investigation on the effect of temperature reveals a reduction

<span id="page-13-0"></span>

**Fig. 3.6** Schematic representation of shear thickening behavior of  $Nd_2O_3$ -based multi-phase STF [[56](#page-18-4)]. Reprinted by permission from Springer

in the peak viscosity with increasing temperature. Applying shear force to the multiphase STF containing  $Nd<sub>2</sub>O<sub>3</sub>$  particles with more mass fraction and larger size than silica particles results in the movement of  $Nd_2O_3$  particles and adherence of silica particles to the  $Nd_2O_3$  particles. By increasing shear force, the  $Nd_2O_3$  particles are well organized and distributed uniformly, which leads to the shear thinning behavior. Further increase in shear force leads to a destroying effect in the layered structure of  $Nd<sub>2</sub>O<sub>3</sub>$  particles. The silica particles form particle clusters by adhering to the  $Nd<sub>2</sub>O<sub>3</sub>$  particles, which leads to a sharp increase in the viscosity of the Nd<sub>2</sub>O<sub>3</sub>-based multi-phase STF. Figure [3.6](#page-13-0) shows the schematic illustration of the shear thickening mechanism. The results show that the incorporation of  $Nd_2O_3$  particles significantly enhances the shear thickening effect especially at higher weight fractions and lower temperatures.

Although several studies have been carried out on the rheology of different multi-phase STF systems, further investigations are needed using various types of additives for a comprehensive understanding of the role of additives in the multiphase STF. Table [3.3](#page-14-0) summarizes the most relevant research works on the rheology of multi-phase STF. The effect of additives on the shear thickening behavior does not have the same trend each other as the literature provides only case-dependent studies. Some additives disrupt the shear thickening mechanism and some improve this behavior. However, it can be concluded that the rheology of multi-phase STF is dependent on various factors such as chemistry, material, geometry, weight fraction, aspect ratio, temperature, and mechanical properties.

Single-phase STF		Multi-phase STF			
	Liquid medium		Weight		
	(molecular		fraction		
Particle (size)	weight)	Additive particles	$(\%)$	Focus of the research	Ref.
Fumed silica (12 nm)	PEG (200 g/mol)	<b>MWCNTs</b>	$0.4 - 1.2$	Tuning STF rheology	[44]
Fumed silica $(12 \text{ nm})$	PEG $(200 \text{ g/mol})$	<b>MWCNTs</b>	$0.2 - 1$	Tuning STF rheology	[45]
Fumed silica $(12 \text{ nm})$	PEG $(200 \text{ g/mol})$	Oxygen-plasma- modified <b>MWCNTs</b>	$0.02 - 0.06$	Enhancing impact resistance of STF treated textiles	[46]
Fumed silica (14 nm)	PEG $(200 \text{ g/mol})$	GO	$0 - 0.3$	Tuning STF rheology	[49]
Fumed silica $(12 \text{ nm})$	PEG $(200 \text{ g/mol})$	GO and MWCNTs	$0.002 -$ 0.02	Tuning STF rheology	$[57]$
Fumed silica (11 nm)	PEG $(200 \text{ g/mol})$	Halloysite nanotubes	$1 - 5$	Tuning STF rheology	[50]
Fumed silica $(20 \text{ nm})$	PEG $(400 \text{ g/mol})$	SiC particles	$5 - 45$	Tuning STF rheology	[47]
Spherical silica $(300 \text{ nm})$	PEG $(400 \text{ g/mol})$	SiC nanowires	$0 - 1.25$ (vol. %)	Tuning STF rheology	$[58]$
Spherical silica $(650 \text{ nm})$	PEG $(200 \text{ g/mol})$	GNs and CNTs	$1 - 3$	Tuning STF rheology	$\left[53\right]$
Spherical silica $(500 \text{ nm})$	PEG (200 g/mol)	<b>CNFs</b>	$0.1 - 0.3$	Tuning STF rheology	[54]
Spherical silica (12 nm)	PEG $(200 \text{ g/mol})$	$ZrO2$ nanoparticles	$9 - 20$	Tuning STF rheology	$\left[55\right]$
Fumed silica $(20 \text{ nm})$	PEG $(400 \text{ g/mol})$	$Al_2O_3$ nanoparticles	$5 - 45$	Tuning STF rheology	[9]
Fumed silica (12 nm)	PEG (200 g/mol)	Nd <sub>2</sub> O <sub>3</sub> nanoparticles	$9 - 15$	Tuning STF rheology	[56]

<span id="page-14-0"></span>**Table 3.3** Multi-phase STF prepared by different additive particles

## **3.5 Conclusions**

The unique rheological behavior of STF provides the opportunity for different various applications such as protective fabrics and mechanical dampers. Several attempts have been carried out to design multi-phase STF by adding particular additives. A detailed review of the rheological behavior of multi-phase STF is presented in this chapter. This chapter shows that there are many signifcant parameters infuencing the shear thickening properties of multi-phase STF such as the shape, size, and weight fraction of additives as well as their interactions with the base particles and carrier liquid in STF. There is an increasing attention and necessity to understand the rheological characteristic of multi-phase STF to fgure out and tune it according to their special applications. Several micro and nano additives have been utilized for tuning the STF rheology including carbon based structures, metal oxides, and inorganic materials. Although the effect of additives on the shear thickening behavior of multi-phase STF does not have the same trend, they often lead to enhanced rheological properties in the optimum conditions. Hence, the fabrication of multi-phase STF with unique structural and rheological characteristics provides new possibilities for the design and development of effcient STF-based systems for various applications.

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