

# Evaluation of the Precision of SARAL/AltiKa and Sentinel-3A Satellite Altimetry Data Over the Vietnam Sea and Its Surroundings



Do Van Mong , Nguyen Van Sang , Khuong Van Long , and Luyen K. Bui 

**Abstract** Satellite altimetry has proven to be a useful tool to measure sea surface height, which is of diverse applications in oceanography, geodesy, among others. However, the precision of satellite altimetry data is different between missions and areas. This article evaluates the precision of observed data received by two satellite altimeters of SARAL/AltiKa and Sentinel-3A in the Exact Repeat Mission mode over the Vietnam Sea and its surroundings. The precision of the data is assessed based on height differences at intersection points between ascending and descending tracks. First, the positions of each intersection point between the ascending and descending tracks are interpolated from measure points with the second-order polynomial model. Then, the standard deviation of the height difference is estimated from all intersection points for each of 34 repeat cycles (SARAL/AltiKa) and 28 repeat cycles (Sentinel-3A) over the study area. The results show that the standard deviations of the SARAL/AltiKa data are between  $\pm 4.5$  cm and  $\pm 7.5$  cm, with an average of  $\pm 5.9$  cm, while those of Sentinel-3A range from  $\pm 4.4$  cm to  $\pm 7.7$  cm, with an average of  $\pm 5.9$  cm. Of both datasets, the height differences are greater at points located close to the coastlines and islands.

**Keywords** Satellite altimetry · SARAL · AltiKa · Sentinel-3A · Vietnam Sea

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D. Van Mong · K. Van Long  
Vietnam's People Naval Hydrographic and Oceanographic Department, Hai Phong 04000, Vietnam

N. Van Sang (✉) · L. K. Bui  
Faculty of Geomatics and Land Administration, Hanoi University of Mining and Geology, Hanoi 100000, Vietnam  
e-mail: [nguyenvangsang@humg.edu.vn](mailto:nguyenvangsang@humg.edu.vn)

L. K. Bui  
e-mail: [buikhacluyen@humg.edu.vn](mailto:buikhacluyen@humg.edu.vn)

## 1 Introduction

Starting from the 1980s, satellite altimeter has been developed rapidly and become a useful tool for marine research. Since the first satellite platform Geodetic/Geophysical Satellite (Geosat) was launched in 1985, there have been many satellite missions working on their orbits; 10 inactive satellite missions are Geosat, the European Remote Sensing satellite (ERS-1/2), TOPEX/Poseidon (T/P), the US navy Geosat Follow On (GFO), Jason-1/2, Environmental Satellite (Envisat), Hai Yang 2A (HY-2A), Satellite pour l'Observation de la Terre (SPOT), and 9 active satellite missions being CryoSat, SARAL/AltiKa, Jason-3, Sentinel-3A/B, Chinese-French Oceanography Satellite (CFOSAT), HY-2B/2C, Jason-CS. The Surface Water and Ocean Topography (SWOT) satellite mission was scheduled to be launched in 2022. The satellites have created a rich database that has been applied in various fields, such as oceanography, hydrology, land and coastal studies, ice and cryosphere, climate, atmosphere, wind and waves, geodesy, and geophysics [1]. Satellite altimeters data are available in the exact repeat mission (ERM) or geodetic mission (GM) mode. In the ERM mode, the observations are made repeatedly at a regular time interval but with a low spatial resolution. This kind of data is useful for oceanography and climate sciences, but not applicable for the determination of high-resolution gravity field modeling. The data received from the geodetic mission (GM) can be used for various applications in geodesy. In this mode, the satellite flies in a non-repeated orbit where the observations are taken once only at each location, but with a much higher spatial density [2].

In the Vietnam Sea and the surrounding area, bounded by [5°N, 25°N] in latitude and [105°E, 120°E] in longitude, there have been several studies applying satellite altimeter data. For example, in 2000, Hwang et al. [3] used the Topex/Poseidon satellite altimeter data to determine surface currents in the East Sea. In 2012, marine gravity anomalies were determined from the ENVISAT data combined with *in-situ* gravity data measured at the coast and islands in the East Sea, in which an accuracy of about  $\pm 6$  mGal was obtained [4]. In 2019, Tran et al. improved the accuracy of marine gravity anomalies derived from satellite altimetry by fitting with the ship-derived gravity anomaly in the East Sea. The results showed the accuracy of the gravity anomaly from  $\pm 1.21$  to  $\pm 9.36$  mGal [5]. In 2020, the accuracies of the global gravity anomaly models DTU10GRAV, DTU13GRAV, DTU15GRAV were evaluated in the Vietnam Sea by comparing with ship-derived gravity anomaly data, which were found to be  $\pm 5.80$ ,  $\pm 5.73$ , and  $\pm 5.63$  mGal, respectively [6]. Also in 2020, the marine gravity anomaly over the Gulf of Tonkin was determined from the CryoSat-2 and SARAL/AltiKa satellite altimeter data with the accuracies achieved before and after fitting with shipborne gravity data being  $\pm 3.36$  and  $\pm 2.63$  mGal, respectively [7]. These studies indicated that satellite altimeter data are of great interest in the study area.

The precision of satellite altimetry data is different between missions and study areas [2], depending on the characteristics of the sea, the corrections to the satellite altimeter data according to the global correction models, which may not be accurate

enough for regional areas. Therefore, it is necessary to evaluate the precision of satellite altimeter data at the regional scale before applying them. As a result, several studies have been conducted to evaluate the precision of satellite altimeter data. For instance, in 2012, altimetric sea levels in coastal areas were validated using available tide gage records in the Nordic, Barents, and Kara seas [8]. The comparison results showed that, at most locations in the Nordic Sea, the satellite altimeter data are in good agreement with the tide gage data, but the agreement is low at the shallows of the Barents and Kara Seas due to the seasonal presence of sea ice [8]. In 2017, the main range and geophysical corrections of TOPEX/Poseidon, Jason-1, and Jason-2 satellite altimetry data were evaluated over the Indonesian Sea, in which the distances from the coast at altimeter crossovers were used to assess the quality of the various corrections and mean sea surface models [9]. Also in 2017, the precision of CryoSat-2 satellite altimeter data was evaluated in the waters around the Spratly Islands, Vietnam, in which the results showed that the precision of CryoSat-2 satellite altimeter data from periods 31 to 43 is  $\pm 3.5$  cm [10]. Location and height difference at crossover points in satellite altimetry data processing were determined using a direct method in 2017 [11]. In 2020, Sentinel-3A and Jason-3 satellite data in the coastal area of the European Sea were evaluated by comparison with tide gage measurements, with the results showing that the root mean square deviation (RMSD) of Sentinel-3A is 13% lower than that of the Jason-3 [12].

Sentinel-3A was launched on February 16, 2016, and is now working in the ERM mode. As a result, its measurements are suitable for studying ocean currents. The mission measurements have been collected since March 12, 2016, with a repeated cycle of 27 days [13]. The SARAL/AltiKa satellite, a product made under the cooperation between the Indian Space Research Organization (ISRO) and Centre national d'études spatiales (CNES), was launched on February 25, 2013. The SARAL/AltiKa satellite collected the measurements in the ERM mode from March 14, 2013, to July 4, 2016, with a repeated cycle of 35 days, which is suitable for studying ocean currents. It then changed into the GM mode from July 4, 2016 onward, which is suitable for gravity field research [14].

Up to now, there have no studies on the assessment of the precision of the SARAL/AltiKa or Sentinel-3A data over the Vietnam Sea and its surroundings. This paper conducts an evaluation of the precision of their data based on height differences at intersection points between the ascending and descending tracks and experimentally evaluates the precision of the SARAL/AltiKa and Sentinel-3A data in the ERM mode. The research is a preliminary step in a further planned project to apply the SARAL/AltiKa and Sentinel-3A satellite altimeter data in studying the ocean current over the Vietnam Sea and its surroundings.

## 2 Research Area and Data

### 2.1 Research Area

The study area is the Vietnam Sea and the surrounding area, bounded by [5°N, 25°N] in latitude and [105°E, 120°E] in longitude (Fig. 1). In this area, tides, waves, and currents vary significantly, which affect the precision of the corrections in the satellite altimeter data. The sea of Vietnam and the surrounding area is an area with different tidal regimes; in the North, the tidal regime is the regular diurnal tide. In the Central region, there is an irregular diurnal tide. In the South, the tidal regime is quite complicated from semi-diurnal to diurnal tide with large tidal amplitudes [15].

The surface current in the East Sea area is clearly shown by the seasonal regime and two large-scale vortices. The winter current system is dominated by the prevailing wind field in the area and partly influenced by the geomorphic current system caused by temperature fields and sea salinity. In addition, the most prominent feature of the surface current in this period is the presence of a large cyclone over the entire sea [16]. For the surface laminar current system, which is formed mainly by the southwest wind field, with the characteristics of being strongly differentiated by the impact of the tropical convergence band. In addition, with the intensification of warm waters according to the deep sea off the Southeast, anti-vortexes which counterbalance with winter vortexes have been formed [17].

The wave height properties of this area are also extremely diverse. The smallest wave height is less than 3 m and located in the western part of the Gulf of Thailand. The area with the highest wave height of more than 12 m can be found in the northeast area of the East Sea due to frequent storm and strong northeast wind activities. The central area of the Gulf of Tonkin has the highest wave height of about 9–10 m. The central area of the East Sea has the highest wave height of about 11 m [18].

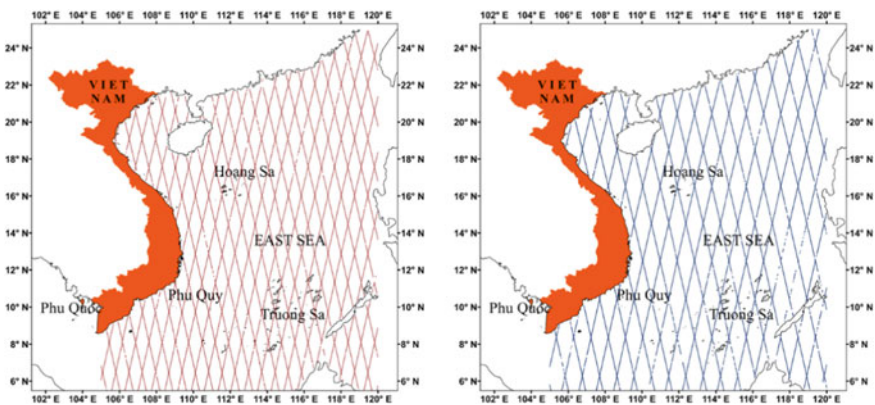


Fig. 1 Track distribution of SARAL/AltiKa (left) and Sentinel-3A (right) satellites

The composition of marine life in this area is of the tropical nature that mainly consists of tropical species distributed in the Western Indo-Pacific region. In addition, in the northern border region of Vietnam, where the tropical monsoon climate is cold, there are also a number of subtropical species distributed from the subtropical China Sea. In terms of ecology, the East Sea is also extremely diverse, with typical ecosystems such as submerged forests, coral reefs, and seagrasses [18].

## 2.2 Research Data

The data used in this study are obtained from two satellite altimeter systems of SARAL/AltiKa and Sentinel-3A in the ERM measurement mode, within the spatial limit from 5 to 25°N in latitude and from 105 to 120°E in longitude. These data are provided by the Radar Altimeter Database System [19]. The SARAL/AltiKa data were collected and aggregated over 34 cycles (from 1st cycle to 34th cycle), corresponding to a measurement period of over 3 years (from March 14, 2013, to June 16, 2016) with a total of 306,223 measurement points. Figure 1 (left) shows the track distribution of the SARAL/AltiKa satellite.

The Sentinel-3A data were collected and aggregated over 28 cycles (from 48th cycle to 75th cycle) in the ERM mode, corresponding to a time span of over 2 years (from August 7, 2019, to September 2, 2021) with a total of 306,223 measurement points. Figure 1 (right) shows the track distribution of the Sentinel-3A satellite. The information regarding the used data is summarized in Table 1. The corrections used in calculating sea surface height (SSH) include orbit, dry and wet tropospheric, ionospheric, solid earth tide, ocean tide, load tide, pole tide, and sea state bias [19].

**Table 1** Summary of collected satellite altimeter data

Data	Repeat cycle (day)	Number of cycles	Measurement time	Measurement points
SARAL/AltiKa	35	34	from March 14, 2013, to June 16, 2016	306,223
Sentinel-3A	27	28	from August 7, 2019, to September 2, 2021	210,375
Total		62		516,598

### 3 Precision Evaluation

#### 3.1 Locating and Computing the Height Difference at the Intersection

According to the operating principle of satellite altimeter systems, when encountering sea water, the wave beams from the satellite reflect back to the receivers on the satellites. The tracks can be classified into ascending and descending tracks. The intersection of the ascending and descending tracks forms the intersection points. The analysis of data sources received from the SARAL/AltiKa and Sentinel altimeter satellites shows that the position of the intersection point between the arcs formed from the dataset often does not coincide with the location of the received data points. Therefore, in order to evaluate the accuracy of satellite altimeter data, the research task requires determining the exact positions of the intersection points and computing the differences in sea level in these positions [20]. In the research content, we use the second-order polynomial simulation method to solve the above two problems [21]. Suppose on a data track, the point has coordinates of  $(\phi_i, \lambda_i)$ . This track will be simulated by a quadratic polynomial [21]:

$$\lambda = a\varphi^2 + b\varphi + c \quad (1)$$

where  $a, b, c$  are the parameters to be determined, in which at least three known coordinate points (i.e., the data points from the altimeter satellites over the track) are required. If there are more than three points, then the parameters are determined according to the principle of least squares.

If the ascending track is simulated by a polynomial model by:

$$\lambda = a_a\varphi^2 + b_a\varphi + c_a \quad (2)$$

And the descending track is simulated by a polynomial model by:

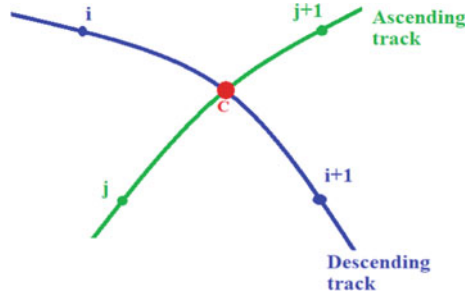
$$\lambda = a_d\varphi^2 + b_d\varphi + c_d \quad (3)$$

Then, the position of the intersection point is the solution of the system of equations:

$$\begin{cases} \lambda = a_a\varphi^2 + b_a\varphi + c_a \\ \lambda = a_d\varphi^2 + b_d\varphi + c_d \end{cases} \quad (4)$$

The system of Eqs. (4) has two solutions, that is, there will be two intersection points located in the two halves of the parabolic graph of the quadratic polynomial. The intersection point is detected based on the beginning and the ending points of the track. Comparing these two points with the beginning and the end points of the track

**Fig. 2** Exact intersection location



helps to find a suitable intersection. The position of the found intersection point is not an exact location, but an approximate location. After determining an approximate intersection point, four neighborhood points of the intersection  $i$ ,  $i + 1$ ,  $j$ , and  $j + 1$  from the ascending and descending tracks are determined (Fig. 2). From these 4 points, we will determine the position of the intersection point (C) more accurately.

After the position of the intersection is determined, the SSH at the intersection point according to the ascending track ( $SSH_{C,a}$ ) and the descending track ( $SSH_{C,d}$ ) will be interpolated from neighboring measurement points  $i$ ,  $i + 1$ ,  $j$ , and  $j + 1$ . The height difference at the intersection point is computed by:

$$dH = SSH_{C,a} - SSH_{C,d} \tag{5}$$

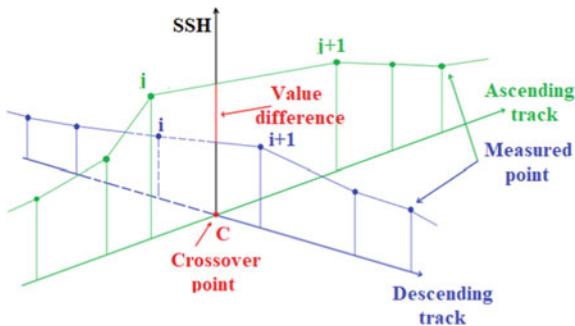
### 3.2 *Evaluating the Precision of Satellite Altimeter Data Based on the Height Differences at the Intersection Points*

$SSH_{C,a}$  and  $SSH_{C,d}$  are the SSHs at the intersection point C computed according to the two ascending and descending tracks. If there is no error, then the two values are identical (i.e.,  $dH = 0$ ). In fact, the value of  $dH \neq 0$  is due to measurement errors (Fig. 3). Therefore, based on the  $dH$  value at the intersection point, we can evaluate the altimeter satellite measurement accuracy.

Let  $dH_i$  be the measured value at the  $i$ -th intersection. Over the entire study area, we have a series of measurement values ( $dH_1, dH_2, \dots, dH_m$ ). The true values of these measurements are all zero. The mathematical expectation of this range of values is calculated by:

$$E(dH) = \overline{dH} = \frac{[dH]}{m} \tag{6}$$

**Fig. 3** Height difference at the intersection



+If the mathematical expectation  $E(dH) = 0$ , then there is no systematic error in the measurements, then the precision of the measured values is determined by:

$$RMS_{dH} = \pm \sqrt{\frac{[dH \cdot dH]}{m}} \tag{7}$$

According to the principle of equal influence, from Eq. (5), we have:

$$RMS_{dH}^2 = RMS_a^2 + RMS_d^2 = 2RMS_{SSH}^2 \tag{8}$$

Substituting to Eq. (7), we have:

$$RMS_{SSH} = \frac{RMS_{dH}}{\sqrt{2}} = \pm \sqrt{\frac{[dHdH]}{2m}} \tag{9}$$

+If the mathematical expectation  $E(dH) \neq 0$ , then there is systematic error in the measurements, and the precision of the measured values is determined according to the standard deviation by the Bessel equation:

$$STD_{dH} = \pm \sqrt{\frac{[vv]}{m - 1}} \tag{10}$$

where given is the calculated correction:

$$v = dH - \overline{dH}$$

Then, the precision of the SSH is determined by:

$$STD_{SSH} = \frac{STD_{dH}}{\sqrt{2}} = \pm \sqrt{\frac{[vv]}{2(m - 1)}} \tag{11}$$



## **4 Results of Precision Evaluation of SARAL/AltiKa and Sentinel-3A Data in the Waters of Vietnam and Surrounding Areas**

### ***4.1 Results of Precision Evaluation of the SARAL/AltiKa Satellite Altimeter Data***

In this section, we evaluate the precision of the SARAL/AltiKa satellite altimeter data for 34 cycles with the results shown in Table 2, Figs. 4 and 5.

The results in Table 2 show that, over the study area, the standard deviations of the SARAL/AltiKa data are between  $\pm 4.5$  cm and  $\pm 7.5$  cm, with an average of  $\pm 5.9$  cm. The average deviation at the intersections is small, ranging from  $-0.033$  m to  $0.004$  m. This indicates that the systematic error in the SARAL/AltiKa satellite altimeter data over study area is small.

### ***4.2 Results of Precision Evaluation of Sentinel-3A Satellite Altimeter Data***

The results of precision evaluation of Sentinel-3A satellite altimeter data are shown in Table 3, Figs. 6 and 7.

Maximum, minimum, and average values of precision of the Sentinel-3A satellite altimeter data are  $\pm 4.4$  cm,  $\pm 7.7$  cm, and  $\pm 5.9$  cm, respectively. The average deviation at the intersection is small, ranging from  $-0.022$  m to  $0.023$  m. This proves that the systematic error in the Sentinel-3A satellite altimeter data is small over the study area.

In order to identify the areas with large height differences at the intersections (dH), we show the average height difference of all cycles of the SARAL/AltiKa satellite in Fig. 8 and the Sentinel-3A satellite in Fig. 9. The results for both data show that the height differences are larger at points located close to the coastlines and islands. Additionally, Fig. 9 shows that not only in the coastal zones, large SSH differences at the intersections can also be found in the area between the Hoang Sa and Truong Sa Islands. This is likely that, in this area, the corrections to the satellite altimeter data according to the global correction models are not very appropriate. It is necessary to study and correct local factors to improve the precision of satellite altimeter data in these areas.

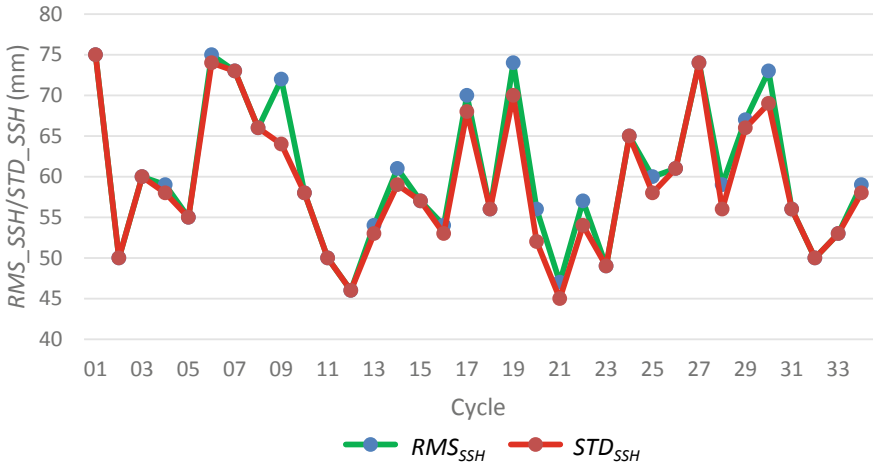
**Table 2** Results of evaluating of the precision of the SARAL/AltiKa satellite altimeter data

Cycle	Number of intersection	$dH_{\max}$ (m)	$dH_{\min}$ (m)	$dH_{\text{mean}}$ (m)	$RMS_{SSH}$ (m)	$STD_{SSH}$ (m)
CK01	169	0.393	- 0.949	- 0.001	0.075	0.075
CK02	149	0.217	- 0.311	0.000	0.050	0.050
CK03	129	0.482	- 0.225	- 0.007	0.060	0.060
CK04	153	0.225	- 0.331	- 0.011	0.059	0.058
CK05	156	0.204	- 0.314	- 0.003	0.055	0.055
CK06	155	0.542	- 0.377	- 0.016	0.075	0.074
CK07	172	0.374	- 0.301	0.004	0.073	0.073
CK08	165	0.428	- 0.22	- 0.007	0.066	0.066
CK09	174	0.471	- 0.347	- 0.033	0.072	0.064
CK10	170	0.281	- 0.259	- 0.004	0.058	0.058
CK11	178	0.208	- 0.236	- 0.006	0.050	0.050
CK12	140	0.199	- 0.214	0.003	0.046	0.046
CK13	136	0.258	- 0.273	- 0.013	0.054	0.053
CK14	161	0.367	- 0.282	- 0.013	0.061	0.059
CK15	164	0.319	- 0.189	0.004	0.057	0.057
CK16	142	0.244	- 0.251	- 0.006	0.054	0.053
CK17	108	0.287	- 0.266	- 0.014	0.070	0.068
CK18	170	0.322	- 0.220	0.002	0.056	0.056
CK19	171	0.483	- 0.325	- 0.024	0.074	0.070
CK20	179	0.186	- 0.284	- 0.021	0.056	0.052
CK21	169	0.165	- 0.193	- 0.012	0.047	0.045
CK22	172	0.413	- 0.280	- 0.017	0.057	0.054
CK23	146	0.196	- 0.264	- 0.006	0.049	0.049
CK24	138	0.355	- 0.301	0.001	0.065	0.065
CK25	135	0.287	- 0.385	- 0.015	0.060	0.058
CK26	149	0.278	- 0.349	- 0.011	0.061	0.061
CK27	146	0.468	- 0.324	- 0.005	0.074	0.074
CK28	162	0.349	- 0.269	- 0.018	0.059	0.056
CK29	165	0.273	- 0.450	- 0.001	0.067	0.066
CK30	178	0.304	- 0.408	- 0.024	0.073	0.069
CK31	177	0.309	- 0.295	- 0.009	0.056	0.056
CK32	171	0.292	- 0.232	- 0.007	0.050	0.050
CK33	154	0.220	- 0.282	- 0.005	0.053	0.053
CK34	153	0.343	- 0.381	- 0.010	0.059	0.058
Max	179	0.542	- 0.189	0.004	0.075	0.075
Min	108	0.165	- 0.949	- 0.033	0.046	0.045

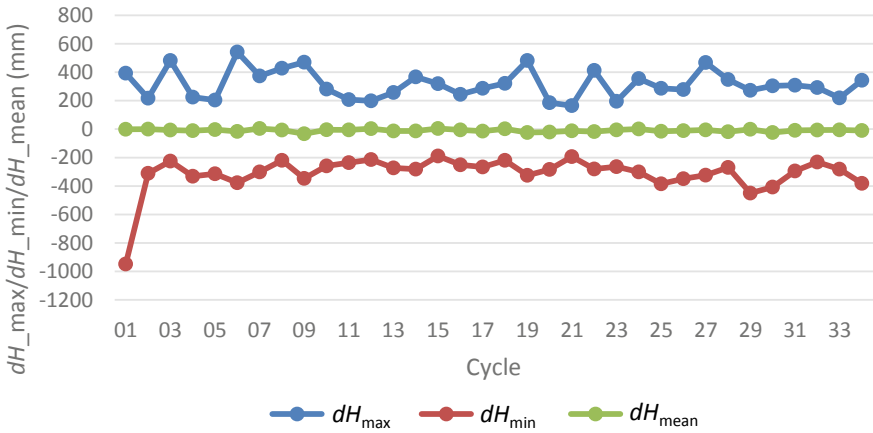
(continued)

**Table 2** (continued)

Cycle	Number of intersection	$dH_{max}$ (m)	$dH_{min}$ (m)	$dH_{mean}$ (m)	$RMS_{SSH}$ (m)	$STD_{SSH}$ (m)
Mean	157.5	0.316	-0.311	-0.009	0.060	0.059



**Fig. 4**  $RMS_{SSH}$  and  $STD_{SSH}$  of SARAL/AltiKa satellite data for 34 cycles



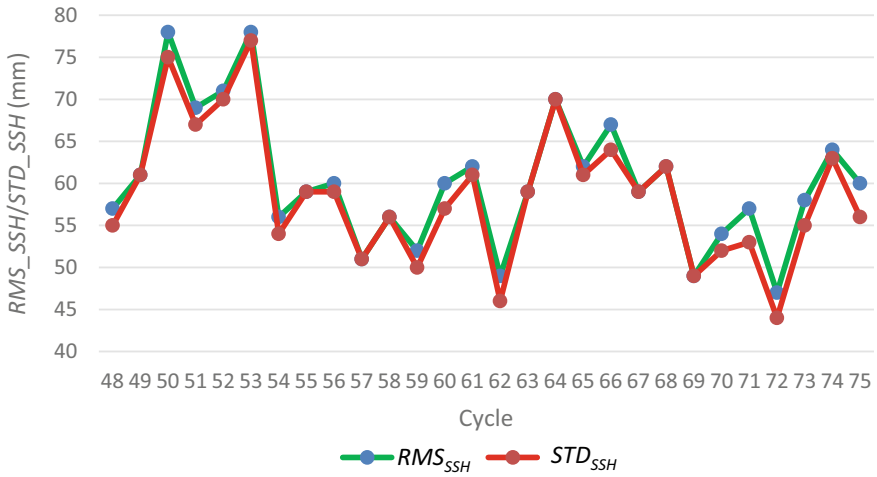
**Fig. 5**  $dH_{max}$ ,  $dH_{min}$ , and  $dH_{mean}$  of SARAL/AltiKa satellite data for 34 cycles

**Table 3** Results of evaluating the precision of Sentinel-3A satellite altimeter data

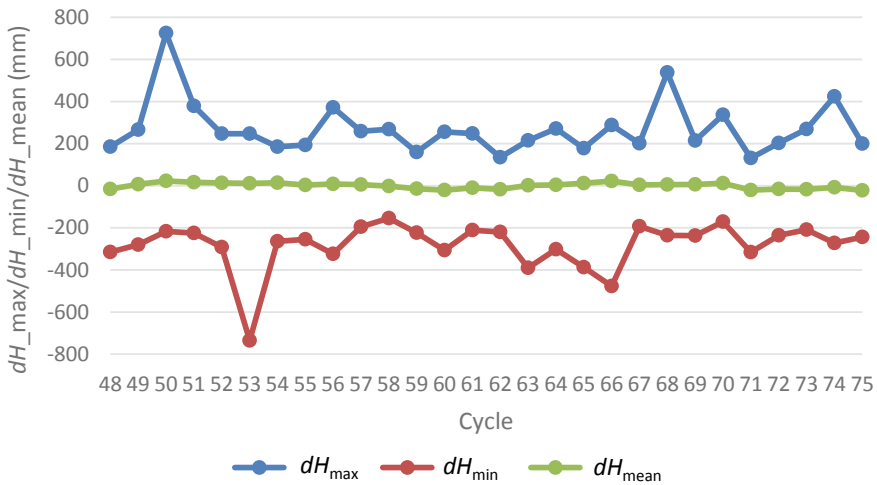
Cycle	Number of intersection	$dH_{\max}$ (m)	$dH_{\min}$ (m)	$dH_{\text{mean}}$ (m)	$RMS_{SSH}$ (m)	$STD_{SSH}$ (m)
CK48	110	0.185	- 0.315	- 0.016	0.057	0.055
CK49	111	0.266	- 0.280	0.007	0.061	0.061
CK50	108	0.725	- 0.217	0.023	0.078	0.075
CK51	113	0.379	- 0.225	0.016	0.069	0.067
CK52	108	0.247	- 0.292	0.013	0.071	0.070
CK53	110	0.247	- 0.735	0.011	0.078	0.077
CK54	114	0.185	- 0.264	0.014	0.056	0.054
CK55	114	0.193	- 0.255	0.003	0.059	0.059
CK56	114	0.372	- 0.324	0.008	0.060	0.059
CK57	113	0.259	- 0.195	0.005	0.051	0.051
CK58	107	0.268	- 0.154	- 0.002	0.056	0.056
CK59	102	0.160	- 0.223	- 0.014	0.052	0.050
CK60	106	0.256	- 0.306	- 0.021	0.060	0.057
CK61	103	0.248	- 0.211	- 0.010	0.062	0.061
CK62	101	0.135	- 0.220	- 0.017	0.049	0.046
CK63	100	0.215	- 0.390	0.002	0.059	0.059
CK64	107	0.271	- 0.302	0.004	0.070	0.070
CK65	110	0.178	- 0.387	0.012	0.062	0.061
CK66	108	0.288	- 0.477	0.022	0.067	0.064
CK67	111	0.201	- 0.193	0.004	0.059	0.059
CK68	112	0.538	- 0.236	0.005	0.062	0.062
CK69	110	0.214	- 0.237	0.006	0.049	0.049
CK70	109	0.337	- 0.171	0.012	0.054	0.052
CK71	108	0.131	- 0.316	- 0.021	0.057	0.053
CK72	104	0.203	- 0.236	- 0.016	0.047	0.044
CK73	108	0.269	- 0.209	- 0.017	0.058	0.055
CK74	109	0.424	- 0.272	- 0.008	0.064	0.063
CK75	104	0.200	- 0.244	- 0.022	0.060	0.056
Max	114	0.725	- 0.154	0.023	0.078	0.077
Min	100	0.131	- 0.735	- 0.022	0.047	0.044
Mean	108.4	0.271	- 0.282	0.000	0.060	0.059

## 5 Conclusion

This paper has presented the evaluation of the precision of SARAL/AltiKa and Sentinel-3A satellite altimeter data over the Vietnam Sea and surroundings based on height differences at the intersection points. The evaluation was conducted with



**Fig. 6**  $RMS_{SSH}$  and  $STD_{SSH}$  values of Sentinel-3A satellite data for 28 cycles



**Fig. 7**  $dH_{max}$ ,  $dH_{min}$ , and  $dH_{mean}$  values of Sentinel-3A satellite data for 28 cycles

34 cycles of the SARAL/AltiKa satellite data (from 1st to 34th cycle), corresponding to an over 3-year period, and the Sentinel-3A satellite data at 28 cycles (from 48 to 74th cycle), corresponding to a more than 2-year time span. Both evaluations were performed with data in the ERM mode.

The standard deviations of the SARAL/AltiKa data are between  $\pm 4.5$  cm and  $\pm 7.5$  cm, with an average of  $\pm 5.9$  cm, while that of the Sentinel-3A satellite altimeter data was found between  $\pm 4.4$  and  $\pm 7.7$  cm, with a mean value of  $\pm 5.9$  cm. The mean height difference at the intersection points is small indicating a

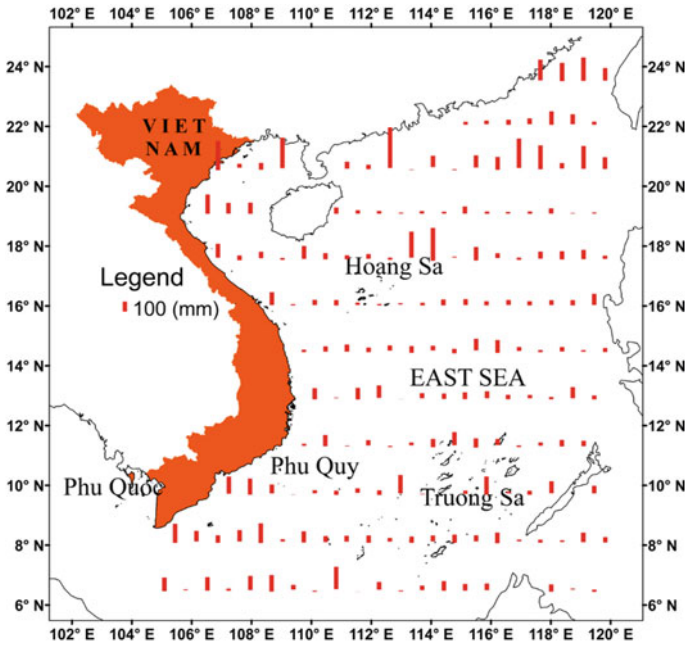


Fig. 8 Height difference (dh) at the intersection points of SARAL/AltiKa satellite

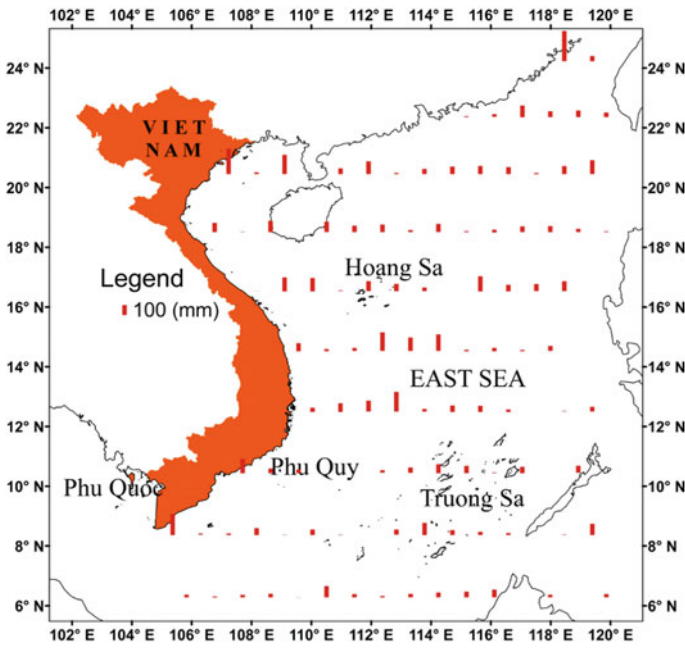


Fig. 9 Height difference (dh) at the intersection points of Sentinel-3A satellite

small systematic error in satellite altimeter data over the study area. Additionally, the height differences at intersection points are found higher in coastal areas and the areas near the archipelagos than those in offshore areas. This difference is also large with Sentinel-3A satellite data in the area between the Hoang Sa and Truong Sa Islands.

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