Chapter 1 History of Cryptography to the 1800s

Introduction

Cryptography is not a new endeavor. Certainly, the way in which we accomplish cryptography is different in the computer age than it was in the past. However, the essential goal of cryptography is the same. The desire to send and receive secure communications is almost as old as written communication itself. For centuries, it almost exclusively involved military secrets or political intrigue. Generals needed to communicate about troop movements to ensure that if a message was intercepted it wouldn't be intelligible to the enemy. Political intrigue, such as a palace coup, required clandestine communications. Prior to the advent of the computer age, there was little need for cryptography outside of military and political applications. There were, of course, hobbyists who used cryptography for their own intellectual edifcation. We will encounter some of those hobbyists in this and the next chapter.

Modern cryptography certainly still includes military communications as well as political communications, but it has expanded into more mundane areas as well. Online banking and shopping, for example, have made cryptography a part of most people's daily lives, whether they are aware of it or not. Many people also choose to encrypt their computer hard drives or fles. Others encrypt their email transmissions. Today, cryptography permeates our lives. Most people use cryptography with little or no awareness of how it works. And for many people that lack of detailed knowledge is sufficient. But many professionals require a deeper understanding of cryptography. Cybersecurity professionals, network administrators, and cybersecurity personnel would beneft from a better understanding. For these professionals, knowing more about cryptography will at least allow them to make better decisions regarding the implementation of cryptography. Deciding which symmetric algorithm to utilize for encrypting sensitive information, or which key exchange algorithm is most resistant to man-in-the middle attacks, requires a bit more knowledge of cryptography.

In This Chapter We Will Cover the Following

- Single-substitution ciphers
- Multi-alphabet substitution
- Devices
- Transposition ciphers

Why Study Cryptography?

It is an unfortunate fact that most people have almost no knowledge of cryptography. Even within the discipline of computer science, and more specifcally the profession of cybersecurity, a lack of cryptographic understanding plagues the industry. Most cybersecurity professionals have only the most basic understanding of cryptography. For many in cybersecurity, their knowledge of cryptography does not extend beyond the few basic concepts that appear on common cybersecurity certifcation tests such as CompTIA Security+ or ISC2 CISSP. Many feel that this level of knowledge makes them well informed about cryptography and are not even aware of how much they do not know. Some would even argue that a deeper knowledge of cryptography is unnecessary. It can be assumed that since you are reading this book, you feel a need to deepen and broaden your knowledge of cryptography, and there are clearly practical reasons to do so, particularly for those in the cybersecurity profession.

By understanding cryptology, you can select the most appropriate cryptographic implementations to suit your needs. Even if you have no desire to be a cryptographer, you still have to choose which tool to use to encrypt a hard drive, for example. Should you use the Data Encryption Standard (DES)? Triple DES (3DES)? Blowfsh? The Advanced Encryption Standard (AES)? If you use AES, then what key size do you use, and why? Why is CBC mode preferable to ECB mode? If you are interested in message integrity for email, should you use the Secure Hash Algorithm (SHA-2)? Perhaps a message authentication code (MAC) or hash message authentication code (HMAC)? Which will provide the most appropriate solution to your particular problem, and why? Many people are not even aware of the differences in algorithms.

In addition, knowing about cryptology helps you understand issues that occur when cryptographic incidents broadly impact cybersecurity. A good example occurred in 2013, when *The New York Times* reported that among the documents released by the National Security Agency, subcontractor Edward Snowden was evidence that the NSA had placed a cryptographic backdoor in the random number generator known as *Dual_EC_DRBG (Dual Elliptic Curve Deterministic Random Bit Generator*). This news story generated a flood of activity in the cybersecurity community. But what is a cryptographic backdoor? What does this mean for privacy and security? Does this mean that the NSA could read anyone's email as if it were published on a billboard? And more importantly, why did this surprise the cybersecurity community, when the cryptography community had been speculating about this possibility since 2005? This story illustrates a substantial gap between the cryptography community and the cybersecurity community.

We will be exploring all of these issues as well as random number generators and even quantum computing later in this book. For the time being, it is sufficient for you to realize that you cannot answer any questions about this particular news story without having some knowledge of cryptography. This story, in fact, was not news to the cryptographic community. As early as 2005, papers had been published that suggested the possibility of a backdoor in this random number generator. Wellknown and respected cryptographer Bruce Schneier, for example, blogged about this issue in 2006. Had the security community possessed a deeper knowledge of cryptography, this backdoor would have been a non-story.

Another example comes from the aforementioned cybersecurity certifcations. Many such certifcation exams ask about wireless security. Particularly about WPA2, and now WPA3. Many of you reading this text have undoubtedly passed such certifcations. Based on that you may well be able to assert that WPA2 utilizes the Advanced Encryption Standard (AES) using the Counter Mode Cipher Block Chaining (CBC) Message Authentication Code (MAC) Protocol (CCMP). But do you know what CBC is, or why it is so useful. In this book, you will learn about these issues and many more.

I could continue with other reasons—very practical reasons—why learning cryptography is essential, and you will see some of those reasons in later chapters. Cryptography is not merely a mathematical endeavor to be engaged in by a select few mathematicians and cryptologists. In this chapter, you will begin your journey into the world of cryptography by learning some essential terms and then exploring some historical ciphers. It must be clear, however, that this book will not make you a cryptographer. That does require much more extensive mathematical knowledge. However, it will provide you with sufficient understanding to make good cryptographic choices and to ask effective questions about cryptographic solutions.

What Is Cryptography?

Before you can begin studying cryptography, you need to know what exactly cryptography is. A number of people seem to have some misconceptions about what *cryptography* and related terms actually mean. The Merriam-Webster online dictionary defnes cryptography as follows: "(1) secret writing (2) the enciphering and deciphering of messages in secret code or cipher; also: the computerized encoding and decoding of information." This defnition does not seem overly helpful and may not provide you with much insight into the topic. Columbia University provides a slightly better defnition in its "Introduction to Cryptography" course: to "process data into unintelligible form, reversibly, without data loss—typically digitally."

The Columbia University defnition adds the important element of not losing information, certainly a critical component in secure communications. However, I cannot help but think that the defnition could be a bit clearer on the issue of exactly what cryptography is. So, allow me to try my hand at defining cryptography:

Cryptography is the study of how to alter a message so that someone intercepting it cannot read it without the appropriate algorithm and key.

This defnition is certainly not radically different from that of either Merriam-Webster or Columbia University. However, I think it is a good, concise defnition, and one we will use throughout this book.

Note that *cryptography* and *cryptology* are not synonyms, though many people mistakenly use the terms as if they were. In fact, many textbooks utilize the terms interchangeably. However, I will defne and differentiate these two terms, as well as some other common terms you will need throughout your study of cryptography. These terms are used in both ancient and modern cryptography.

- *Cipher* A synonym for the algorithm used in transforming plain text to cipher text.
- *Cipher text* The coded or encrypted message. If your encryption is sufficiently strong, your cipher text should be secure.
- *Cryptanalysis* Also known as code breaking; the study of principles and methods of deciphering cipher text without knowing the key. This is more diffcult than movies or television would indicate, as you will see in Chap. [17.](https://doi.org/10.1007/978-3-031-12304-7_17)
- *Cryptography* The study of how to alter a message so that someone intercepting it cannot read it without the appropriate algorithm and key.
- *Cryptology* Although some people, including more than a few cybersecurity books, use the terms *cryptography* and *cryptology* interchangeably, that is inaccurate. Cryptology is more comprehensive and includes both cryptography and cryptanalysis.
- *Decipher* (*decrypt*) *Decipher* and *decrypt* are synonyms. Both terms mean to convert the cipher text to plain text.
- *Encipher* (*encrypt*) *Encipher* and *encrypt* are synonyms. Both words mean to convert the plain text into cipher text.
- *Key* The information, usually some sort of number, used with the algorithm to encrypt or decrypt the message. Think of the key as the fuel the algorithm requires in order to function.
- *Key space* The total number of possible keys that could be used. For example, DES uses a 56-bit key; thus, the total number of possible keys, or the key space, is 2^{56} .
- *Plain text* The original message—the information you want to secure.

These are some of the most basic terms that permeate the study of cryptology and cryptography. In any discipline, it is important that you know, understand, and use the correct vocabulary of that feld of study. These terms are essential for your understanding.

If you suppose that you cannot study cryptography without a good understanding of mathematics, to some extent you are correct. Modern methods of cryptography, particularly asymmetric cryptography, depend on mathematics. We will examine those algorithms later in this book, along with the mathematics you need to understand modern cryptography. It is often easier for students frst to grasp the concepts of cryptography within the context of simpler historical ciphers, however. These ciphers don't require any substantive mathematics at all, but they do use the same concepts you will encounter later in this book. It is also good to have an historical perspective on any topic before you delve deeper into it. In this chapter we will examine a history of cryptography, looking at specifc ciphers that have been used from the earliest days of cryptography to the 1800s.

Let us begin our study of historical cryptography by examining the most common historical ciphers. These are fascinating to study and illustrate the fundamental concepts you need in order to understand cryptography. Each one will demonstrate an algorithm, plain text, cipher text, and a key. The implementations, however, are far simpler than those of modern methods and make it relatively easy for you to master these ancient methods. Keep in mind that these ciphers are totally inadequate for modern security methods. They would be cracked extremely quickly with a modern computer, and many can be analyzed and cracked with a pen, paper, and the application of relatively simple cryptanalysis legerdemain.

Substitution Ciphers

The frst ciphers in recorded history are *substitution ciphers*. With this method, each letter of plain text is substituted for some letter of cipher text according to some algorithm. There are two types of substitution ciphers: single-alphabet (or monoalphabet) and multi-alphabet (or poly-alphabet). In a single-alphabet substitution cipher, a given letter of plain text is always substituted for the corresponding letter of cipher text. For example, an *a* in the plain text would always be a *k* in the cipher text. Multi-alphabet substitution uses multiple substitutions, so that, for example, an *a* in the plain text is sometimes a *k* and sometimes a *j* in the cipher text. You will see examples of both in this section.

The Caesar Cipher

One of the most widely known historical encryption methods is the *Caesar cipher*. According to the Roman historian Gaius Suetonius Tranquillus (c. 70–130 CE), Julius Caesar used this cipher to encrypt military messages, shifting all letters of the plain text three places to the right (d'Agapeyeff [2016](#page-26-0)). So, for example, the message Attack at dawn

becomes

Dwwdfn dw gdzq

As you can see, the *a* in the plain text is shifted to the right three letters to become a *d* in the cipher text. Then the *t* in the plain text is shifted three letters to the right to become a *w* in the cipher text. This process continues for all the letters in the plain text. In our example, none of the shifts went beyond the letter *z*. What would happen if we shifted the letter *y* to the right three? The process would wrap around the alphabet, starting back at letter *a*. Thus, the letter *y* would be shifted to a letter *b* in the cipher text.

Although Caesar was reputed to have used a shift of three to the right, any shifting pattern will work with this method, shifting either to the right or to the left by any number of spaces. Because this is a quite simple method to understand, it is an appropriate place to begin our study of encryption. It is, however, extremely easy to crack. You see, any language has a certain letter and word *frequency*, meaning that some letters are used more frequently than others. In the English language, the most common single-letter word is *a*, followed closely by the word *I*. The most common three-letter word is *the*, followed closely by the word *and*. Those two facts alone could help you decrypt a Caesar cipher. However, you can apply additional rules. For example, in the English language, the most common two letter sequences are *oo* and *ee*. Examining the frequency of letter and letter combination occurrences is called *frequency analysis*.

It is claimed that other Caesars, such as Augustus, used variations of the Caesar cipher, such as 1 shift to the right. It should be obvious that any shift, left or right, of more than 26 (at least in English) would simply loop around the alphabet. So, a shift to the right of 27 is really just a shift of 1.

Although the Caesar cipher is certainly not appropriate for modern cryptographic needs, it does contain all the fundamental concepts needed for a cryptography algorithm. First, we have the plain text message—in our current example, *Attack at dawn*. Then we have an algorithm—shift every letter. And then a key, in this case *+3*, or three to the right (*–3* would be three to the left). And fnally, we have cipher text, *Dwwdfn dw gdzq*. This is, essentially, the same structure used by all modern symmetric algorithms. The only differences between the Caesar cipher and modern symmetric ciphers are the complexity of the algorithm and the size of the key.

The size of the key brings us to one signifcant problem with the Caesar cipher its small key space. Recall that key space is the total number of possible keys. Because there are only 26 letters in the English alphabet, the key space is *26* (i.e., *+–26*). It would be relatively easy for a person working with pen and paper to check all possible keys, and it would be ridiculously trivial for a computer to do so. In the cybersecurity world, a malicious person who checks all possible keys to decipher an

encrypted message is conducting what it called a *brute-force attack*. The smaller the key space, the easier a brute-force attack will be. Compare the Caesar cipher, with a key space of 26, to AES 128-bit, with a key space of 2^{128} , or about 3.4×10^{38} . Clearly, the larger key space makes a cipher more resistant to brute-force attacks. Note, however, that simply having a long key is not sufficient for security. You will learn more about this when we discuss cryptanalysis in Chap. [17](https://doi.org/10.1007/978-3-031-12304-7_17).

Mathematical Notation of the Caesar Cipher

With the various ancient ciphers, we will be using, the math is trivial. However, it is a good idea for you to become accustomed to mathematical notation, at least with those algorithms where such notation is appropriate. It is common to use a capital letter *P* to represent plain text and a capital letter *C* to represent cipher text. We can also use a capital letter *K* to represent the key. This gives us the following mathematical description of a Caesar cipher:

$$
C \equiv P + K \pmod{26}
$$

Here we see a symbol some readers may not be acquainted with, the \equiv . This is not a misprint of the = sign; rather, it is the symbol for congruence. Do not be overly concerned about the $\equiv 26$. We will explore modulus operations and congruence in detail in Chap. [4](https://doi.org/10.1007/978-3-031-12304-7_4). For now, I just use the modulus operation to denote dividing by a given number (in this case, 26, because there are 26 letters in the alphabet) and listing only the remainder. That is not a rigorous mathematical explanation, but it will suffice for now.

Decryption can also be represented via mathematical symbols:

$$
P \equiv C - K \pmod{26}
$$

The mathematical representation of Caesar's method of shifting three to the right is

$$
C \equiv P + 3 \pmod{26}
$$

According to the book *The Lives of the Caesars*, written by Suetonius, Julius Caesar used this cipher extensively:

There are also the letters of his to Cicero, as well as to his intimates on private affairs, and in the latter, if he had anything confdential to say, he wrote it in cipher, that is by so changing the order of the letters of the alphabet, that not a word could be made out. If anyone wishes to decipher these, and get at their meaning, he must substitute the fourth letter of the alphabet, namely D, for A, and so with the others.

If the plain text is the 24th letter of the alphabet (which is the letter *X*), then the cipher text is $(24 + 3)/26$, listing only the remainder. Thus, $27/26 = 1$, or the letter *A*.

We cannot know how effective the Caesar cipher was at concealing messages. However, at the time of Julius Caesar, illiteracy was common, and cryptography was not widely known. So, what may seem a trivial, even frivolous, cipher today may well have been effective enough more than 2000 years ago.

The Caesar cipher is probably the most widely known substitution cipher, but it is not the only one. All substitution ciphers operate in a similar fashion: by substituting each letter in the plain text for some letter in the cipher text, with a one-to-one relationship between the plain text and cipher text. Let's look at a few other substitution ciphers.

Atbash Cipher

Hebrew scribes copying the biblical book of Jeremiah used the *Atbash substitution cipher*. Applying the Atbash cipher is fairly simple: just reverse the order of the letters of the alphabet. This is, by modern standards, a very primitive cipher that is easy to break. For example, in English, *a* becomes *z*, *b* becomes *y*, *c* becomes *x*, and so on. Of course, the Hebrews used the Hebrew alphabet, with *aleph* being the frst letter and *tav* the last letter. However, I will use English examples to demonstrate the cipher:

Attack at dawn

becomes

Zggzxp zg wzdm

As you can see, the *A* (the frst letter in the alphabet) is switched with *Z* (the last letter), and the *t* is the 19th letter (or 7th from the end) and gets swapped with *g*, the 7th letter from the beginning. This process is continued until the entire message is enciphered.

To decrypt the message, you simply reverse the process so that *z* becomes *a*, *b* becomes *y*, and so on. This is obviously a simple cipher and is not used in modern times. However, like the Caesar cipher example, it illustrates the basic concept of cryptography—to perform some permutation on the plain text to render it diffcult to read by those who don't have the key to "unscramble" the cipher text. The Atbash cipher, like the Caesar cipher, is a single-substitution cipher (each letter in the plain text has a direct, one-to-one relationship with each letter in the cipher text). The same letter and word frequency issues that can be used to crack the Caesar cipher can be used to crack the Atbash cipher.

Affne Ciphers

Affne ciphers are any single-substitution alphabet ciphers (also called *monoalphabet substitution*) in which each letter in the alphabet is mapped to some numeric value, permuted with some relatively simple mathematical function, and then converted back to a letter. For example, using the Caesar cipher, each letter is converted to a number, shifted by some amount, and then converted back to a letter.

The basic formula for any affne cipher is

$$
ax + b \pmod{m}
$$

M is the size of the alphabet—so in English that would be 26. The *x* represents the plain text letter's numeric equivalent, and the *b* is the amount to shift. The letter *a* is some multiple—in the case of the Caesar cipher, *a* is 1. So, the Caesar cipher would be

$$
1x + 3 \pmod{26}
$$

What has been presented thus far is rather simplifed. To use an affne cipher, you need to pick the value a so that it is coprime with m. We will explore coprime in more detail later in this book. However, for now simply understand that two numbers are coprime if they have no common factors. For example, the number 8 has the factors 2 and 4. The number 9 has the factor 3. Thus, 8 and 9 have no common factors and are coprime. If you don't select a and m that are coprime, it may not be possible to decrypt the message.

Continuing with a simplifed example (ignoring the need for coprime a and m), you could obviously use any shift amount you want, as well as any multiplier. The *ax* value could be 1*x*, as with Caesar, or it could be 2*x*, 3*x*, or any other value. For example, let's create a simple Affne cipher:

$$
2x + 4 \pmod{26}
$$

To encrypt the phrase *Attack at dawn*, we frst convert each letter to a number and then multiply that number by 2 and calculate that result $\equiv 6$. So, *A* is *1*, 2 multiplied by 1 is still 2, add 54, gives us 6 mod 26 yielding 6, or *F*.

Then we have *t*, which is 20, and 2 multiplied by 20 is 40, add 4, which gives us 44, and 44 mod 26 yields 18, or *r*. Ultimately, we get this:

Attack at dawn Frrfj0 fr lfxf

Notice that the letter *k* did not convert to a letter; instead, a 0 (zero) appears. *K* is the 11th letter of the alphabet, and $2x + 4$, where $x = 11$, equals 26. And 26 mod 26 is 0.

This is one example of an affne cipher, and there are quite a few others. As you have just seen, you can easily create one of your own. You would want to limit your selection of *a* to values that produce only integer results, rather than decimals. A value of 1.3*x*, for example, would lead to decimal values, which could not easily be converted to letters. We know that *1* is *a* and *2* is *b*, but what letter is *1.3*?

All affne ciphers have the same weaknesses as any single-substitution cipher. They all preserve the letter and word frequencies found in the underlying language and are thus susceptible to frequency analysis. In fact, no matter how complex you make the permutation, any single-substitution cipher is going to be vulnerable to frequency analysis.

ROT 13

ROT 13 is a trivial single-substitution cipher that also happens to be an affine cipher. *ROT* is short for *rotate*: each letter is rotated to the right by 13. So, the affine representation of the ROT 13 (in English) is

 $1x + 13 \pmod{26}$

Since the Latin alphabet has 26 letters, simply applying ROT 13 a second time will decrypt the message. As you can probably guess, this is not at all secure by modern standards. However, it is actually used in some situations. For example, some of the keys in the Microsoft Windows Registry are encrypted using ROT 13. In this case, the reasoning is likely to be that frst and foremost, you need access to the system before you can explore the Windows Registry, and second, most people are not well versed in the Windows Registry and would have diffculty fnding specifc items there even if they were not encrypted at all, so ROT 13 may be secure enough for this scenario. I am not necessarily in agreement with that outlook, but it is a fact that the Windows Registry uses ROT 13.

It has also been reported that in the late 1990s Netscape Communicator used ROT 13 to store email passwords. ROT 13 has actually become somewhat of a joke in the cryptology community. For example, cryptologists will jokingly refer to "ROT 26," which would effectively be no encryption at all. Another common joke is to refer to "triple ROT 13." Just a brief refection should demonstrate to you that the second application of ROT 13 returns to the original plain text, and the third application of ROT 13 is just the same as the frst.

Homophonic Substitution

Over time, the faws in single-substitution ciphers became more apparent. *Homophonic substitution* was one of the earlier attempts to make substitution ciphers more robust by masking the letter frequencies, as plain text letters were mapped to more than one cipher text symbol, and usually the higher frequency plain text letters were given more cipher text equivalents. For example, *a* might map either to *x* or *y*. This had the effect of disrupting frequencies, making analysis more diffcult. It was also possible to use invented symbols in the cipher text and to have a variety of mappings. For example, *a* maps to *x*, but *z* maps to *¥*. The symbol *¥* is one I simply created for this example.

There are variations of this cipher, and one of the most notable versions is called the *nomenclator cipher*, which used a codebook with a table of homophonic substitutions. Originally the codebook used only the names of people, thus the term nomenclator. So, for example, Mr. Smith might be *XX* and Mr. Jones would be *XYZ*. Eventually, nomenclators were created that used a variety of words rather than just names. The codes could be random letters, such as those already described, or code words. Thus, Mr. Jones might be enciphered as *poodle* and Mr. Smith enciphered as *catfsh*. Such codebooks with nomenclator substitutions were quite popular in espionage for a number of years. The advantage of a nomenclator is that it does not provide any frequencies to analyze. However, should the codebook become compromised, all messages encoded with it will also be compromised.

The Great Cipher

The *Great Cipher* is one famous nomenclator used by the French government until the early 1800s. This cipher was invented by the Rossignol family, a French family with several generations of cryptographers, all of whom served the French court. The frst, a 26-year-old Rossignol mathematician, served under Louis XIII, creating secure codes.

The Great Cipher used 587 different numbers that stood for syllables (note that there where variations on this theme, some with a different number of codes). To help prevent frequency analysis, the cipher text would include nulls, or numbers that meant nothing. There were also traps, or codes that indicated the recipient should ignore the previous coded message.

Copiale Cipher

This is an interesting homophonic cipher. It was a 105-page, 75,000-character, handwritten manuscript that went unbroken for many years. The Copiale cipher used a complex substitution code that used symbols and letters for both texts and spaces. The document is believed to date from the 1700s from a secret society named the "high enlightened occultist order of Wolfenbüttel." The cipher included abstract symbols, Greek letters, and Roman letters. It was fnally cracked in 2011 with the help of computers.

Polybius Cipher

The *Polybius cipher* (also known as the Polybius square) was invented by the Greek historian Polybius (c. 200–118 BCE). Obviously, his work used the Greek alphabet, but we will use it with English here. As shown in the following grid, in the Polybius cipher, each letter is represented by two numbers (Mollin [2000](#page-26-1)). Those two numbers being the x and y coordinates of that letter on the grid. For example, *A* is 1 1, *T* is 4 4, *C* is 1 3, and *K* is 2 5. Thus, to encrypt the word *attack*, you would use 114444111325. You can see this in Fig. [1.1](#page-11-0).

Despite the use of two numbers to represent a single letter, this is a substitution cipher and still maintains the letter and word frequencies found in the underlying language of the plain text. If you used the standard Polybius square, which is a widely known cipher, it would be easily cracked, even without any frequency analysis. If you wanted to use a different encoding for letters in the square, that would require that the sending and receiving parties share the particular Polybius square in advance, so that they could send and read messages.

It is interesting to note that the historian Polybius actually established this cipher as a means of sending codes via torches. Messengers standing on hilltops could hold up torches to represent letters and thus send messages. Establishing a series of such messengers on hilltops, each relaying the message to the next, allowed communications over a signifcant distance, much faster than any messenger on foot or horseback could travel.

Fig. 1.1 Polybius square

Ancient Cryptography in Modern Wars

Here is a very interesting story that does not necessarily ft with the timeline of this chapter (pre-twentieth century), but it does concern the Polybius square. The Polybius square was used by prisoners of war in Vietnam, who communicated via tapping on a wall to signal letters. Therefore, for example, four taps, a pause, and then two taps would be the letter *R*. When used in this fashion, it is referred to as a *tap code*. This cipher was introduced into the POW camps in 1965 by Captain Carlyle Harris, Lieutenant Phillip Butler, Lieutenant Robert Peel, and Lieutenant Commander Robert Shumaker, all imprisoned at the Hoa Lo prisoner of war camp. It is reported that Harris recalled being introduced to the Polybius square by an instructor during his training. He then applied the Polybius square to a tap code so that he and his fellow prisoners could communicate. This technique was taught to new prisoners and became widespread in the POW camp. Vice Admiral James Stockdale wrote about using the tap code, stating, "Our tapping ceased to be just an exchange of letters and words; it became conversation. Elation, sadness, humor, sarcasm, excitement, depression—all came through." This is a poignant example of cryptography being applied to very practical purposes.

Null Cipher

The *null cipher* is a very old cipher—in fact, by today's standards, it might be considered more steganography than cipher (you'll read about steganography in Chap. [16\)](https://doi.org/10.1007/978-3-031-12304-7_16). Essentially, the message is hidden in unrelated text. So, in a message such as

We *a*re having breakfas*t* a*t* noon *a*t the *c*afe, would that be o*k*ay?

the sender and recipient have prearranged to use some pattern, taking certain letters from the message. So, for example, the numbers

3 20 22 27 32 48

would signify the letters in the sentence and provide the message

attack

The pattern can be complex or simple—such as always using the second letter of each word or any other pattern. In addition, punctuation and spaces could be counted as characters (our example ignored punctuation and spaces).

Multi-alphabet Substitution

As you know, any single-alphabet substitution cipher is susceptible to frequency analysis. The most obvious way to improve such ciphers would be to fnd some mechanism whereby the frequency of letters and words could be disrupted. Eventually, a slight improvement on the single-substitution cipher was developed, called *multialphabet substitution*. In this scheme, you select multiple numbers by which to shift letters (i.e., multiple substitution alphabets). For example, if you select three substitution alphabets $(+1, +2,$ and $+3)$, then

Attack at dawn

becomes

Bvwben bv gbxo

In this example, the frst letter was shifted forward by one, so *A* became *B*; the second letter was shifted forward by two, so t became v ; and the third letter was shifted forward by three, so in this case *t* became *w*. Then you start over with one shift forward. It should be abundantly clear that the use of multiple alphabets changes letter and word frequency. The frst letter *t* became *v*, but the second letter *t* became *w*. This disrupts the letter and word frequency of the underlying plain text. The more substitution alphabets that are utilized, the more disruption there will be to the letter and word frequency of the plain text. This disruption of the letter and word frequency overcomes the weaknesses of traditional single-substitution ciphers. There are a variety of methods for making a multi-alphabet substitution cipher. We will examine a few of the most common multi-alphabet ciphers in the following sections.

Tabula Recta

Tabula recta is one of the earliest major multi-alphabet substitution ciphers. It was invented in the sixteenth century by Johannes Trithemius. A tabula recta is a square table of alphabets made by shifting the previous alphabet to the right, as shown in Fig. [1.2.](#page-14-0)

This essentially creates 26 different Caesar ciphers. Trithemius described this in his book *Polygraphia*, which is presumed to be the frst published book on cryptology. To encrypt a message using this cipher, you substitute the plain text letter for the letter that appears beneath it in the table. Basically, the frst letter of the plain text (denoting the row) is matched with the frst letter of the keyword (denoting the column), and the intersection of the two forms the cipher text. This is repeated with each letter. When the end of the keyword is reached, you start over at the beginning

	A	в	С	D	Ε	F	G	н	I.	J	κ	L	м	N		O P		Q R	S	T	U	ν	w	х	Y	z
А	А	в	С	D	E	F	G	н	Î.	J	к	L	м	N	O	P	Q	R	S	Т	U	v	w	x		7
в	в	C	D	F	F	G	н		J	κ		M	N	O	P	Q	R	s	т	U	v	w			7	А
с	С	D	E	F	G	н		J.	к		M	N	Ο	P	Q	R	S	т	U	v	w	x	Y	Z	А	B
D	D	E	F	G	н		J.	κ		M	N	O	P	Q	R	S	т	U	ν	w	x	Y	7	А	B	C
Ε	Ε	F	G	н			κ		м	N	Ο	P	Q	R	s	т	U	ν	w	x	Y	Z	А	в	C	D
F	F	G	н			κ		м	N	O	P	Q	R	s	т	U	v	w	x	Y	7	А	в	С	D	Ε
G	G	н		J	к		м	N	O	P	Q	R	s	т	U	v	w	x	Y	Z	А	в	С	D	E	F
н	н			ĸ		м	N	Ο	P	Q	R	s	т	U	ν	w	X	Y	Z	A	B	C	D	E	F	G
		J.	ĸ			Ν	Ω	P	Ω	R	S	т	U	v	w	X	Y	Z	А	B	c	D	F	F	G	н
J		к		м	N	O	P	Q	R	S	т	U	ν	w	х	Y	Z	А	в	C	D	E	F	G	н	
κ	κ		м	N	O	P	Ω	R	s	т	U	v	w	x	Y	Z	А	в	C	D	Ε	F	G	н		
			N	Ο	P	Q	R	S	т	U	v	w	x	Y	Z	А	B	C	D	E		G				к
м	M	N	Ω	P	Ω	R	S	т	U	v	w	X	Y	Z	A	в	C	D	F	F	G	н		J.	ĸ	
N	ΙN		P	Ω	R	S	т	U	v	w	x	Y	7	А	в	C	D	F	F	G	н			ĸ		M
Ο	O	P	Q	R	S	т	U	v	w	x	Y	Z	A	в	с	D	Ε	F	G	н		J	κ		м	N
P	P	Q	R	S	т	U	v	w	X	Y	Z	А	B	с	D	Ε	F	G	н		J	ĸ		м	N	Ω
Q	Q		S	т	U	v	w	x	Y	Z	А	в	C	D	E	F	G	н		J	к		м	N	O	P
R	R	S	т	U	ν	w	x	Y	Z	А	B	C	D	E	F	G	н		J.	к		м	N	Ω	P	Q
S	S	т	U	ν	w	x	Y	7	A	B	С	D	Ε	F	G	н		J	κ		M	N	Ο	P	Ω	R
Т		U	ν		x	Y	Z	А	B	C	D	E	F	G	н		J	к		M	N	O	P	Q	R	S
U	U	v	w	x		Z	A	B	C	D	E	F	G	н	L	J	к		м	N	Ο	P	Ω	R	S	т
		w	x Υ	Y 7	Z A	А	B	C D	D	Ε F	F	G	н		J	κ		м	N	O P	P	Ω	R	S т	т U	U
w	w	X	7			в	С	E	Ε F		G	н	ı	J	к		М	N	Ω		O	R	s	U		
х	Χ	Y z		А B	в	С	D E	F		G	н	ı	J	κ	L	М	N	O P	P	Q	R S	s т	т U			X
Z			А		D	D E	F		G	н	1 J	J. K	κ		М	N	Ο P		Q R	R S	т	U	v	w x		
		А	в	С				G	Н	ı			L	M N		\circ		Q								

Fig. 1.2 Tabula recta

of the keyword. Trithemius used a fxed keyword, so although this did change the frequency distributions found in single-substitution ciphers, it still had a signifcant flaw when compared to later developments such as Vigenère.

Vigenère

Perhaps the most widely known multi-alphabet cipher is the *Vigenère cipher*. This cipher was frst described in 1553 by Giovan Battista Bellaso, though it is misattributed to nineteenth-century cryptographer Blaise de Vigenère (Singh [2000\)](#page-26-2). It is a method of encrypting alphabetic text by using a series of different mono-alphabet ciphers selected based on the letters of a keyword. Bellaso also added the concept of using any keyword, thereby making the choice of substitution alphabets diffcult to calculate. Essentially, the Vigenère cipher uses the tabula recta with a keyword. So, let us assume you have the word *book*, and you wish to encrypt it. You have a keyword for encryption, that keyword is *dog*. You would like up the frst letter of your plaintext, *b* on the left-hand side of the tabula recta, with the frst letter or your keyword *d* on the top. The frst letter of your cipher text is then *e*. Then you take the second letter of your plaintext, *o*, and line it up with the second letter of the keyword, also *o*, producing the second letter of your cipher text, *c*. The next o in book will line up with the g in dog, producing u. Now that you have reached the end of your keyword, you start over at d. So, the *k* in book is lined up with the *d* in dog, producing the last letter of your cipher text, which is *n*. Thus, using Vigenère, with the keyword dog, the plaintext book becomes the cipher text *ecun*.

For many years, Vigenère was considered very strong—even unbreakable. However, in the nineteenth century, Friedrich Kasiski published a technique for breaking the Vigenère cipher. We will revisit that when we discuss cryptanalysis later in this book. It is important that you get accustomed to mathematical notation. Here, using *P* for plain text, *C* for cipher text, and *K* for key, we can view Vigenère very similarly to Caesar, with one important difference: the value *K* changes.

$$
Ci = Pi + Ki \left(\bmod{26} \right)
$$

The *i* denotes the current key with the current letter of plain text and the current letter of cipher text. Note that many sources use *M* (for message) rather than *P* (for plain text) in this notation. Let us assume the word you wish to:

A variation of the Vigenère, the *running key cipher*, simply uses a long string of random characters as the key, which makes it even more difficult to decipher.

The Beaufort Cipher

The *Beaufort cipher* also uses a tabula recta to encipher the plain text. A keyword is preselected by the involved parties. This cipher was created by Sir Francis Beaufort (1774–1857) and is very similar to the Vigenère cipher. A typical tabula recta was shown earlier in this chapter in Fig. [1.1.](#page-11-0)

When using the Beaufort cipher, you select a keyword, except unlike Vigenère, you locate the plain text in the top row, you move down until you fnd the matching letter of the keyword, and then you choose the letter farthest to the left in the row as the cipher text.

For example, using the tabula recta in Fig. [1.1](#page-11-0), and the keyword *falcon*, you would encrypt the message *Attack at dawn* in the following manner:

- 1. Find the letter *A* on the top row.
- 2. Go straight down that column until you fnd the letter *F* (the frst letter of the keyword).
- 3. Use the letter in the far-left column as the cipher text letter. In this case, which would be *F*.
- 4. Repeat this, except this time use the next letter of the keyword, *a*. Locate the second letter of the plain text *t* in the top row.
- 5. Move down that column until you fnd an *a*, and then we select the letter on the far left of that row, which would be *h*.
- 6. When you reach the last letter of the keyword, you start over at the frst letter of the keyword, so that

Substitution Ciphers

Attack at dawn

becomes

Fhscmdfhicsa

Devices

In modern times, devices are almost always used with cryptography. For example, computers are used to encrypt email, web traffc, and so on. In ancient times, there were also ciphers based on the use of specifc devices to encrypt and decrypt messages.

Scytale Cipher

The *Scytale cipher* is one such ancient cypher. Often mispronounced (it actually rhymes with "Italy"), this cipher used a cylinder with a strip of parchment wrapped around it. If you had the correct diameter cylinder, then when the parchment was wrapped around it, the message could be read (Dooley [2018\)](#page-26-3). You can see the concept shown in Fig. [1.3](#page-16-0).

If you did not have the correct size of cylinder, however, or if you simply found the parchment and no cylinder, the message would appear to be a random string of letters. This method was frst used by the Spartans and later throughout Greece. The earliest mention of Scytale was by the Greek poet Archilochus in the seventh century BC. However, the frst mention of how it actually worked was by Plutarch in the frst century BCE, in his work *The Parallel Lives*:

The dispatch-scroll is of the following character. When the ephors send out an admiral or a general, they make two round pieces of wood exactly alike in length and thickness, so that each corresponds to the other in its dimensions, and keep one themselves, while they give the other to their envoy. These pieces of wood they call "scytalae." Whenever, then, they wish to send some secret and important message, they make a scroll of parchment long and narrow, like a leather strap, and wind it round their "scytale," leaving no vacant space

Fig. 1.3 Scytale

thereon, but covering its surface all round with the parchment. After doing this, they write what they wish on the parchment, just as it lies wrapped about the "scytale"; and when they have written their message, they take the parchment off, and send it, without the piece of wood, to the commander. He, when he has received it, cannot other get any meaning of it—since the letters have no connection, but are disarranged—unless he takes his own "scytale" and winds the strip of parchment about it, so that, when its spiral course is restored perfectly, and that which follows is joined to that which precedes, he reads around the staff, and so discovers the continuity of the message. And the parchment, like the staff, is called "scytale," as the thing measured bears the name of the measure.

Alberti Cipher Disk

The Alberti *cipher disk*, created by Leon Battista Alberti, is an example of a multialphabet substitution. Alberti wrote about this cipher in 1467 in his book *De Cifris*. It consists of two disks attached in the center with a common pin. Each disk had 24 equal cells. The larger, outer disk, called the *stabilis*, displayed an uppercase Latin alphabet used for the plain text. The smaller, inner disk, called the *mobilis*, displayed a lowercase alphabet for the cipher text.

To encrypt a message, a letter on the inner disk was lined up with a letter on the outer disk as a key. If you knew what letter to line up with, you would know which key to use. This has the effect of offering multiple substitution alphabets. You can see an example of the cipher disk, with the English alphabet, in Fig. [1.4](#page-17-0).

In Alberti's original cipher disk, he used the Latin alphabet. So, the outer disk had the Latin alphabet minus a few English letters, as well as numbers 1 through 4 for use with a codebook that had phrases and words assigned four-digit values.

Fig. 1.4 Cipher disk

Fig. 1.5 Jefferson disk

The Jefferson Disk

The *c*, which was called a "wheel cipher" by its inventor, Thomas Jefferson, is a rather complex device, at least for its time. Invented in 1795, the disk is a set of wheels or disks, each displaying the 26 letters of the English alphabet. The disks are all on a central axle and can be rotated about the axle. The order of the disks is the key, and both sender and receiver had to order their disks according to the key. An example of the Jefferson disk is shown in Fig. [1.5](#page-18-0).

When using the Jefferson disk, the sender would rotate the letters on the disks until the message was spelled out in a single row. The sender would then copy down any row of text on the disks other than the one that contained the plain text message. That enciphered message would then be sent to the recipient. The recipient then arranged the disk letters according to the predefned order and then rotated the disk until the message was displayed.

It should be noted that this device was independently invented by Étienne Bazeries (1846–1931), a French cryptographer, although Jefferson improved on the disk in his version. Bazeries was known for being a very skilled cryptographer and cryptanalysis. After he broke several transposition systems used by the French military, the French government hired him to work for the Ministry of Foreign Affairs. During World War I, he worked on breaking German ciphers.

Stories such as this are not uncommon in cryptography. Two different parties may independently invent the same or remarkably similar ciphers. This often occurs from time to time in modern times, when at least some work in cryptography is classifed by various governments. You will see other examples of this in later chapters on modern ciphers.

Phaistos Disc

This is a clay disk from the Minoan palace of Phaistos on the island of Crete. It is believed to date from sometime between 1850 BCE and 1600 BCE (i.e., the Bronze Age). This disk has 45 distinct signs. However, unlike the other devices we have discussed, this one has never been deciphered. Archeologists do not know the key for this and don't know precisely how it was used.

Phryctoriae

It may seem like a stretch to call this a cipher, but it was an integral part of secure communications in ancient Greece. This was a set of towers positioned on mountain tops. Fire beacons were used to send messages. Greek letters were represented by a given number of torches shown. The following table illustrates this:

So, to represent M, one would do frst two torches on the right and three torches on the left. This illustrates that the need to encode messages for transmission is nothing new. Human beings have been using such systems for millennia. The systems we have now are more complex, but the same essential concepts.

Book Ciphers

Book ciphers have probably been around for as long as books have been available. Essentially, the sender and receiver agree to use a particular book as its basis. The simplest implementation is to send coordinates for words. So, for example, *3 3 10* means "go to page 3, line 3, tenth word." In this way, the sender can specify words with coordinates and write out entire sentences. There are numerous variations of this cipher. For example, you could combine book ciphers with Vigenère and use the book coordinates to denote the keyword for Vigenère.

Beale Ciphers

In 1885, a pamphlet was published describing treasure buried in the 1820s by one Thomas J. Beale in Virginia. The *Beale ciphers* are three cipher texts that allegedly give the location, contents, and names of the owners of the buried treasure. The frst Beale cipher, which has not been solved, provides the location. The second cipher provides details of the contents of the treasure and has been solved. The second cipher was a book cipher that used the US Declaration of Independence as the book. Each number in the cipher represents a word in the document. There is a great deal of controversy regarding the Beal ciphers, which we will explore in more detail in Chap. [2.](https://doi.org/10.1007/978-3-031-12304-7_2) They are presented here simply as an example of a book cipher.

Dorabella Cipher

The Dorabella cipher is not a book, but rather a letter. It was composed by Edward Elgar to Dora Penny and sent in July of 1897. Ms. Penny never delivered the message, and it remains an unexplained cipher. It consists of 87 characters spread over 3 lines. There have been proposed solutions, but no one has been able to verify their proposed solution.

Babington Plot Ciphers

In 1586 there was a plot to assassinate Queen Elizabeth I. The reason for the plot was to depose Queen Elizabeth who was a protestant and replace her with Mary Queen of Scots who was Roman Catholic. Queen Mary was currently imprisoned. Anthony Babington was one of the conspirators and communicated with encrypted messages with Queen Mary. The details of the ciphers are less important than the illustration of the role of ciphers in political intrigue.

Transposition Ciphers

So far, we have looked at ciphers in which some sort of substitution is performed. However, this is not the only way to encrypt a message. It is also possible to transpose parts of a message. Transposition ciphers provide yet another avenue for encryption.

Reverse Order

The simplest implementation of a transposition cipher is to reverse the plain text. In this way

Attack at dawn

becomes

Nwadtakcatta

Obviously, this is not a particularly diffcult cipher to break, but it demonstrates a simple transposition.

Rail Fence Cipher

The *rail fence cipher* may be the most widely known transposition cipher. You encrypt the message by alternating each letter on a different row. So

Attack at dawn

is written like this:

A t c a d w t a k t a n

Next you write down the text on both lines, reading from left to right, as you normally would, thus producing

Atcadwtaktan

To decrypt the message, the recipient must write it out on rows:

A t c a d w t a k t a n

Then the recipient reconstructs the original message. Most texts use two rows as examples, but any number of rows can be used.

Geometric Shape Cipher

In the *geometric shape cipher*, the sender writes out the plain text in rows and then maps a path (i.e., a shape) through it to create the cipher text. So, if the plain text is

Attack the beach at sunrise

this message would be written in rows like this:

A t t a c k t h e b e a c h a t s u n r i s e

Then the sender chooses some path through the message to create the cipher text. Perhaps start at bottom right and go up and down the columns as shown in Fig. [1.6](#page-22-0).

Using the path depicted in Fig. [1.6](#page-22-0), the cipher text reads

```
esihtkcrnacaeusottetaha
```
For this example, I used a very simple geometric path through the plain text, but you could use other, more complex patterns as well. This method is sometimes called a route cipher, as it is encrypted using a specifc route through the plain text.

Columnar Cipher

The *columnar cipher* is an intriguing type of transposition cipher. In this cipher, the text you want to encrypt is written in rows usually of a specifc length and determined by some keyword. For example, if the keyword is *falcon*, which is six characters long, you would write out your messages in rows of six characters each. So, you would write out

```
A t t a c k
t h e b e a
c h a t s u
n r i s e q
```
Notice the added q at the end. That was added because the last row is only five characters long. In a regular columnar cipher, you pad the last row so that all rows are of equal length.

Fig. 1.6 Geometric shape cipher

If you leave the blank spaces intact, this would be an irregular columnar cipher, and the order of columns would be based on the letters in the keyword as they appear in the alphabet. So, if the keyword is *falcon*, the order is 3 1 4 2 6 5 as *f* is the third lowest letter in the alphabet, *a* is the lowest, *l* is the fourth lowest, and so on. So, if we apply 3 1 4 2 6 5 to encrypt the message, we frst write out the letters down column 3, then column 1, then column 4, then column 2, then column 6, and then column 5. So, the message

a t t a c k t h e b e a c h a t s u n r i s e q

is encrypted like so:

teaiatcnabtskauqcese

Many variations of the columnar cipher, such as the Myskowski variation, have been created over the years, each adding some subtle twist to the concept.

Myskowski Variation

When using a columnar cipher, what happens if the keyword includes the same letter twice? Normally, you treat the second occurrence as if it were the next letter. For example, if *babe* is the keyword, the second *b* is treated as if it were a *c*, so the order would be 2 1 3 4.

In 1902, Emile Myskowski proposed a variation that did something different. The repeated letters were numbered identically, so *babe* would be 2 1 2 3. Any plain text columns that had unique numbers (in this case 1 and 3) would be transcribed downward as usual. However, the recurring numbers (in this case 2) would be transcribed left to right.

Combinations

One of the frst thoughts that may occur when you're frst learning cryptography is to combine two or more of the classic ciphers, such as those covered in this chapter. For example, you might use a Vigenère cipher frst and then put the message through a columnar transposition or a rail fence cipher. Combining some substitution cipher with a transposition cipher would increase the diffculty a human would have in

breaking the cipher. You can think of this in mathematical terms as a function of a function:

$$
f(g(x))
$$

where g is the first cipher, x is the plain text, and f is the second cipher. And you could apply them in any order—frst a substitution and then a transposition, or vice versa.

When you're exploring this train of thought, be aware that if you simply apply two mono-alphabet substitution ciphers, you have not improved secrecy at all. The cipher text will still preserve the same letter and word frequencies. In fact, the best improvement will come from combining transposition and substitution ciphers. As you will see beginning in Chap. [6,](https://doi.org/10.1007/978-3-031-12304-7_6) modern block ciphers combine substitution and transposition, albeit in a more complex fashion. Don't think, however, that such innovations will lead to ciphers that are sufficient for modern security needs. Performing such combinations is an intriguing intellectual exercise and will hone your cryptography knowledge, but these methods would not provide much security against modern computerized cryptanalysis.

D'Agapeyeff Cipher

For the more adventuresome reader, this cipher may capture your attention. It is, as of yet unbroken. So, I cannot tell you specifcally how it works. I can only give you a bit of history and then present to you the unbroken cipher text, should you choose to undertake this rather herculean challenge.

In 1939 cryptography Alexander D'Agapeyeff authored the frst edition of the book *Codes and Ciphers*. In that book he offered the following cipher text, shown in Fig. [1.7,](#page-24-0) as a challenge. In later editions of the book, this challenge was omitted.

```
75628 28591 62916 48164 91748 58464 74748 28483 81638 18174
74826 26475 83828 49175 74658 37575 75936 36565 81638 17585
75756 46282 92857 46382 75748 38165 81848 56485 64858 56382
72628 36281 81728 16463 75828 16483 63828 58163 63630 47481
91918 46385 84656 48565 62946 26285 91859 17491 72756 46575
71658 36264 74818 28462 82649 18193 65626 48484 91838 57491
81657 27483 83858 28364 62726 26562 83759 27263 82827 27283
82858 47582 81837 28462 82837 58164 75748 58162 92000
```
Fig. 1.7 D'Agapeyeff cipher

Conclusions

In this chapter, you have been exposed to a variety of historical ciphers. You were shown single-substitution ciphers such as Caesar and Atbash and multi-alphabet ciphers such as Vigenère. You learned about the weaknesses of mono-alphabet substitution ciphers and how multi-alphabet methods attempt to overcome those issues. You were introduced to a variety of transposition ciphers, including the rail fence and columnar ciphers. This chapter also introduced you to devices such as Scytale and the Jefferson disk. It is important that you get very comfortable with these ciphers before proceeding on.

You were also introduced to some basic mathematical notation to symbolize some of the ciphers in this chapter as well as some general cryptographic terminology such as *cipher text* and *key space*. That notation and those terms should be very familiar to you because they will help form the basis for modern symmetric ciphers you'll read about, beginning in Chap. [4.](https://doi.org/10.1007/978-3-031-12304-7_4)

Test Your Knowledge

A few questions are provided here to aid you in testing your knowledge before you proceed.

- 1. What is the most obvious weakness in a mono-alphabet cipher?
	- A. They preserve word frequency.
	- B. They can be cracked with modern computers.
	- C. They are actually quite strong.
	- D. They don't use complex mathematics.
- 2. The total number of possible keys for a given cipher is referred to as the
	- A. Key group

_______________.

- B. Key domain
- C. Key space
- D. Key range
- 3. Which of the following methods used a cylinder with text wrapped around it?
	- A. Vigenère cipher
	- B. Jefferson disk
	- C. Cipher disk
	- D. Scytale
- 4. What is an affne cipher?
	- A. Any cipher of the form $ax + b \ (\equiv m)$
	- B. Only single-substitution ciphers
	- C. Any single-substitution cipher
	- D. A multi-alphabet cipher
- 5. What are the key features of homophonic substitution?
	- A. Multiple substitution alphabets are used.
	- B. A single plain text letter may have several cipher text representations.
	- C. The cipher text is phonically similar to the plain text.
	- D. It combines substitution with transposition.

References

d'Agapeyeff, A. (2016). Codes and ciphers-A history of cryptography. Read Books Ltd.

Dooley, J. F. (2018). History of cryptography and cryptanalysis: Codes, Ciphers, and their algorithms. Springer.

Mollin, R. A. (2000). An introduction to cryptography. CRC Press.

Singh, S. (2000). The code book: the science of secrecy from ancient Egypt to quantum cryptography. Anchor.