



Chapter 1

A Step Towards Testing of Foot Prostheses Using Real-Time Substructuring (RTS)

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Abstract Despite extensive research in prostheses development, amputees still have to cope with severe limits. Tasks, such as climbing stairs and running or walking on soft ground are demanding and represent obstacles in everyday life. Design verification of new devices helps to accelerate the development. However, current test procedures do not include the dynamic interaction between a prosthesis and the human. Real-time Substructuring (RTS) enables investigation of the dynamic behavior of a system, here human and prosthesis, by splitting it into numerically simulated components and one physical component. As this test imitates real dynamic conditions, foot prostheses can be improved during the development stage. In this preliminary study, a one-dimensional mass-spring-mass system is investigated. The upper mass, representing the human being, is simulated numerically on the computer. It is coupled virtually to a prosthesis, represented here as a spring-mass system, which is mounted on a Stewart Platform. Both systems exchange displacement and force information. The upper mass tries to follow a periodic desired trajectory, which is influenced by the coupling. This paper describes the experimental setup and the effect of delay compensation. In addition, it is shown how the accuracy and stability of the RTS simulation depends on the problem description, i.e. how much the system is governed by the mechanical properties of the numerical part. Although we are specifically considering the application of RTS to prosthetics, the current research tackles generic problems that will also help to enhance other applications involving contact, e.g. the docking of satellites.

Keywords Real-time substructuring · Testing of prosthetic feet · Stewart platform · Real-time hybrid testing with contact · Force compensation

1.1 Introduction

Testing of foot prostheses is an expedient step in the development of foot prostheses. The aim of prostheses is, in general, to emulate the behavior of the missing body part. Despite great advances in the design of foot prostheses, they need to be improved further to enable amputees to resume a normal everyday life. Walking on uneven and soft ground is one of the challenging situations for patients because a healthy human foot can balance actively in this situation. Testing procedures during the early development stage help to accelerate prosthesis development and improvement [1]. Currently, there are different methods for testing foot prostheses: one approach is that the force and position data are taken from gait analysis laboratories and incorporated on test benches [2]. Another method for validating the newly developed design is via finite element modeling [1]. Moreover, prostheses are also evaluated via in-vivo testing. Patients are asked to wear the device and give feedback. The results from these tests are important, as they give a response on how well the amputees cope with the prosthesis in everyday life. However, even though this represents valuable feedback for prostheses developers, it is not without difficulties as it is not reproducible and unsafe for the amputees [1, 2]. The main advantage of robot-driven test benches is that they can also mimic potentially dangerous situations, such as tripping, in a safe and reproducible environment. Therefore, it would be advantageous to combine the advantages of all mentioned methods; a promising approach is the use of Real-Time Substructuring.

Real-Time Substructuring (RTS) or Real-Time Hybrid Testing is a method for investigating the dynamic behavior of complex mechanical systems. The mechanical system is split into two parts (or substructures) and each of the parts is analyzed—one is analyzed in a numerical simulation, the other is investigated on the test bench which is driven by an actuator. Both simulations are coupled in real-time in order to assess the dynamic behavior of the whole system [3, 4].

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Fig. 1.1 Stewart Platform used for the RTS simulation



This method was established and extensively used for earthquake engineering [5] but is nowadays also used in diverse fields, e.g. for the simulation of wind turbine blades [6] or spacecraft parachute deployment [7]. The applicability of the RTS method in biomechanics has also been proven by Herrmann et al. [8]. They tested the dislocation of artificial hip and knee joints under physiological conditions.

The idea of testing foot prostheses using the RTS method was also proposed in [9]. The human is modeled in a multibody simulation which is solved numerically. The prosthesis is mounted on the test bench and force as well as displacement values are exchanged in real-time between the two systems. In [9] it is assumed that stability problems occur due to the highly nonlinear system properties and the discontinuity due to contact. Extensive research on stability problems due to delay and unknown dynamics of the transfer system (actuator and controller, force sensor) have been conducted over the last decades, e.g. by Horiuchi et al. [10], Darby et al. [11], Bonnet [12], and Bartl et al. [13]. Furthermore, Boge and Ma [14] addressed contact issues for their application satellite docking. In general, time delay of the transfer system brings negative damping into the simulated system. Therefore, they actively balance the energy input and output so that the total energy does not increase and the system remains stable.

In this paper, we present the experimental setup for testing foot prostheses using RTS. The presented experimental setup is tested in an RTS simulation, where a mass-spring-mass system that can move in vertical direction serves as the mechanical system being tested. The effects of delay compensation using polynomial extrapolation [10] are investigated.

Section 1.2 introduces the test bench and the coupling problem. The mechanical system as well as the required force compensation are presented and derived in Sect. 1.3. Section 1.4 presents the results of the experiments. It also highlights issues regarding contact problems for the stability and accuracy of RTS simulations. Finally, a brief summary and outlook are given in Sect. 1.5.

1.2 Experimental Setup

A Stewart Platform, shown in Fig. 1.1, is used as an actuator for the RTS simulations. Stewart Platforms are six DOFs manipulators with parallel kinematics. Therefore, they offer the benefits of high stiffness and accuracy making them suitable for use, for example, in milling machines and driving simulators [15]. The Stewart Platform used in this investigation, is driven by six electric motors and is position-controlled by a decentralized cascade controller (PPI) [15]. For parallel robots, the inverse kinematics can be directly calculated using kinematic relationships in contrast to serial robots, where Newton-Raphson iterations or similar methods need to be used. Thus, the desired displacement command for the Tool Center Point

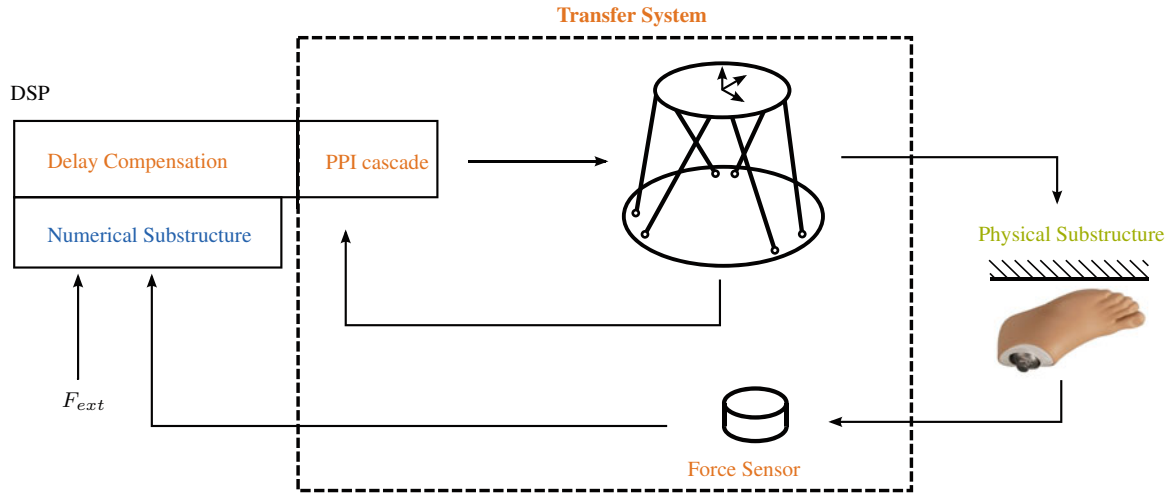


Fig. 1.2 Control loop for RTS testing using a Stewart Platform [16]

(center of upper platform) can be converted to a displacement command of each leg. Additionally, there is a velocity feed-forward in the control loop of the position-control that improves the controlled behavior of the Stewart Platform. The sample time of the controller is set to 1 ms.

The whole RTS simulation consists of a virtual and an experimental part as well as of a transfer system that imposes the desired displacement command. If the transfer system was ideal, i.e. it did not have any time delay or its own dynamics, the coupling of the virtual and experimental part would be perfect and the RTS simulation could perfectly imitate the dynamic behavior of the mechanical system [4]. The control loop for the RTS simulation is depicted in Fig. 1.2. The numerical model of the virtual part (blue), which is needed for the RTS simulation, is implemented in a Simulink Model. The real-time execution is done using a dSpace MicroLabBox as a Digital Signal Processor (DSP). The behavior of the numerical substructure is solved using a time integration scheme. The behavior depends on the current state as well as the loading and possible external forces F_{ext} . The calculated displacement at the interface between the virtual and physical substructure is sent to the transfer system (orange). The transfer system includes the Stewart Platform as an actuator with its inner control loop (position control) and a potential outer control loop for delay compensation. The Stewart Platform executes the desired displacement originating from the numerical substructure. The physical substructure (green), which is connected to a force sensor and mounted on the actuator, is being moved by this displacement. The force at the interface of the physical substructure is measured by a six DOFs force-torque sensor and fed back to the DSP. The next numerical simulation is performed on the numerical substructure and, depending on the new loading, updates the displacement command for the Stewart Platform.

1.3 Problem Description

In order to test foot prostheses with the experimental setup described in Sect. 1.2, the feasibility of the proposed idea must be validated. In addition, there are several research questions that must be solved to obtain a running and reliable RTS simulation. Therefore, the first simulations are done with the simple mechanical system described in Sect. 1.3.1. In Sect. 1.3.2, the force compensation of gravitational forces is derived. Finally, this section summarizes the delay compensation technique of [10] in Sect. 1.3.3.

1.3.1 Mechanical System

The system that we investigate is a mass-spring-mass system as depicted in Fig. 1.3a. The system consists of two masses, the upper mass m_V and the lower mass m_E . Following the later application $m_V \gg m_E$ is set. The spring stiffness of the massless spring is set to be k_E . Indices V and E imply the substructure to which the part belongs; mass m_V is simulated

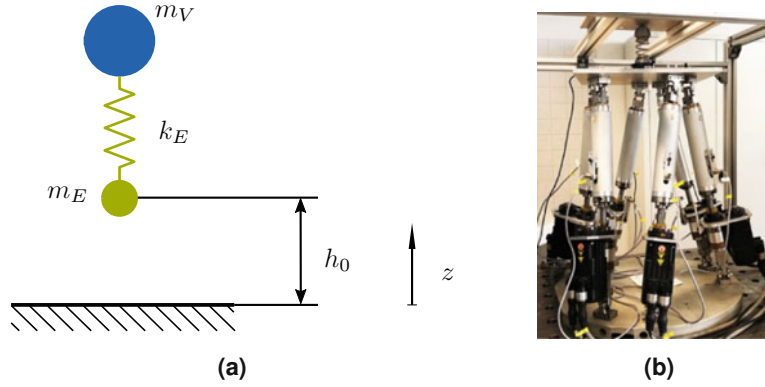


Fig. 1.3 Description and realization of the mechanical system. (a) Overall system for RTS simulation. (b) Experimental setup with mass m_E and spring (stiffness k_E)

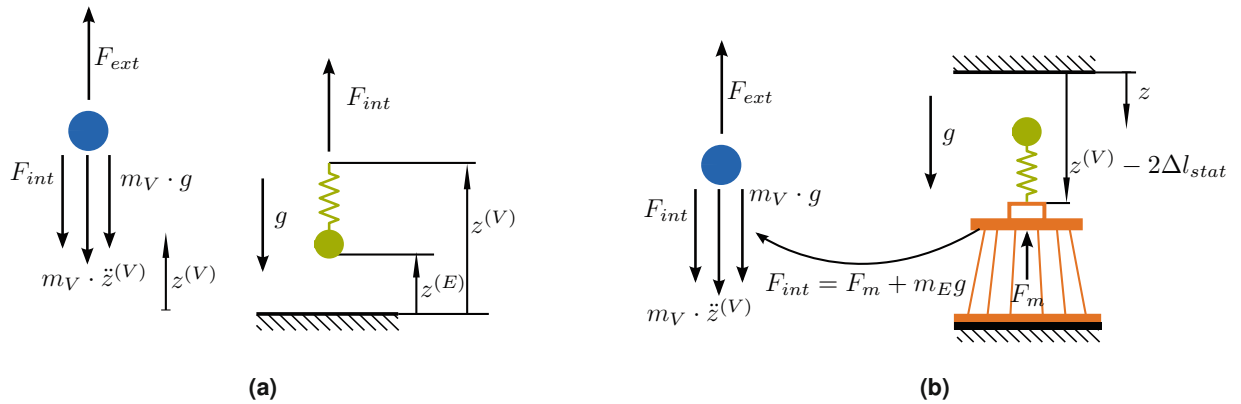


Fig. 1.4 Comparison of the dynamic behavior between validation simulation and measurement in the experimental setup. The RTS simulation consists of the numerical substructure (blue), the physical substructure (green) and the transfer system (orange). (a) Forces and displacements in the reference system. (b) Forces and displacements in the experimental setup

numerically (blue), whereas mass m_E and the spring (stiffness k_E) are tested on the test bench (green). Gravity acts in the negative z -direction and the height of mass m_E at time zero, i.e. when the simulation begins, is h_0 . The behavior of the spring is linear over the range used in the experiments. The spring has an undeformed spring length of l_0 . Furthermore, it is assumed, that the real system does not include any damping. The test bench realization is shown in Fig. 1.3b. The experimental substructure is connected to the Tool Center Point of the Stewart Platform by a force sensor and can be brought into contact by the actuator.

1.3.2 Compensation of Gravity Effects

The test setup is shown in Fig. 1.3b. The device under test that is mounted on its platform can be brought into contact with a ceiling but not with the ground. We could have inverted the Stewart Platform, however, the construction effort that would have been required prevented us from doing so. Consequently, the dynamic behavior of the system changes because the effect of gravity differs in the experimental setup and in the reference model, which must be included and compensated for in the RTS simulation.

The considerations are visualized in Fig. 1.4, where Fig. 1.4a shows the reference model and Fig. 1.4b shows the experimental realization. The position $z^{(V)}$ stands for the position of mass m_V and hence the position of the interface. Likewise, the position of mass m_E is denoted by $z^{(E)}$. The numerical simulation consists of the mass m_V (blue) which is under the following loads: the inertia force $m_V \cdot \ddot{z}^{(V)}$, the gravitational force $m_V \cdot g$, the force at the interface F_{int} and a (time-dependent) external force F_{ext} . As the mass m_E and its corresponding accelerations $\ddot{z}^{(E)}$ are in the same range as the noise of the force sensor, the inertia forces of mass m_E are henceforth assumed to be negligible. In addition, it is assumed that

there is no delay in the transfer system (orange). In the real-time experiments, the force offset is set when the experimental part is already mounted on the test bench. Hence, the measured force is $F_m = 0 \text{ N}$ if the mass m_E is not in contact. However, the force that acts at the interface of the reference system is $F_{int} = m_E \cdot g$. Since the interface force F_{int} acts on the numerical part and is thus required for a correct RTS simulation, the measured force must be corrected by

$$F_{int} = F_m + m_E \cdot g. \quad (1.1)$$

In other words, the difference between the measured forces and the interface forces in the reference system is $2m_E g$, which results from the different orientation of the gravitational force. However, due to setting the offset of the force sensor when the mass m_E is already mounted, we only have to compensate $m_E g$ according to Eq. (1.1).

1.3.3 Delay Compensation

The delay and dynamics of the transfer system can lead to instability and inaccuracy of the RTS simulation, as they bring negative damping into the system. To compensate, there are a lot of different delay compensation techniques. For the experiments presented in Sect. 1.4, we used a polynomial extrapolation as published in [10]. The formulation is

$$z'(t) = \sum_{i=0}^2 a_i \cdot z(t - i \cdot \tau) \quad \text{with } a_0 = 3, \quad a_1 = -1 \quad \text{and } a_2 = 3,$$

if a polynomial of degree $n = 2$ is used and the time delay of the transfer system is τ . Here, the position value that is calculated by the numerical simulation at the current time t is z and the command that is sent to the actuator is z' . z' is an extrapolated value that depends on the value of z in the past.

1.4 Experiment

This section presents the experiments performed and results obtained with the mechanical system presented in Sect. 1.3. Firstly, the load case is described with the corresponding simulation parameters in Sect. 1.4.1 and then the results are shown in Sect. 1.4.2.

1.4.1 Loading Condition and Simulation Parameters

The aim of our research is to carry out a RTS simulation of a human walking with a prosthesis. A major question is how a human being stabilizes its body so that it does not fall, even if there are disturbances. One approach used in robotics for stabilizing bipeds is to use a planned trajectory and track this trajectory with a controller [17]. Using this approach, we prescribed a desired trajectory z_d (and \dot{z}_d) for the mass m_V in the numerical substructure. A PD controller (parameters K_p and K_d) attempts to follow this trajectory by adding an external force, if the desired motion is not tracked:

$$F_{ext} = (m_V + m_E) \cdot g + K_p \cdot (z_d - z^{(V)}) + K_d \cdot (\dot{z}_d - \dot{z}^{(V)}).$$

The first term corresponds to the static external force for holding the system in the air. Hence, the external force F_{ext} that acts on the system as displayed in Fig. 1.4 is the force that is required to keep mass m_V on the desired trajectory z_d . The higher the values K_p and K_d , the faster the controller that tries to hold mass m_V on the desired trajectory z_d . Even small deviations from the trajectory are adjusted in a short period. If the parameters of the PD controller are reduced, the ability of the mass to follow its desired trajectory is reduced as well. Returning to the aim of testing a prosthesis using the RTS approach, this is similar to the case where the forces coming from a badly designed prosthesis are so large compared to the equilibrating forces, that the patient needs for example to tension a muscle much more than usual or tilt the hip. The dynamic behavior of the mechanical system is more relevant in this case and not dominated by the properties of the PD controller.

Table 1.1 Simulation parameters

Parameter	Value	Parameter	Value
m_V	9.62 kg	f_d	0.25 Hz and 1 Hz
m_E	0.38 kg	Δz_{max}	0.005 m
k_E	10,000 N/m	K_p	$2 \cdot 10^6$ kg/s ² and 10^4 kg/s ²
h_0	0.01 m	K_d	500 kg/s and 50 kg/s
τ	10 ms		

The trajectory is chosen to be of sinusoidal shape

$$\begin{aligned} z_d(t) &= h_0 + l_0 + \Delta l_{stat} - \frac{h_0 + \Delta z_{max}}{2} + \frac{h_0 + \Delta z_{max}}{2} \cdot \cos(2\pi f_d t) \\ &= z_0^{(V)} - \frac{h_0 + \Delta z_{max}}{2} + \frac{h_0 + \Delta z_{max}}{2} \cos(2\pi f_d t), \end{aligned}$$

starting at the initial position $z^{(V)}(t = 0) = z_0^{(V)}$ and using $\Delta l_{stat} = \frac{m_E \cdot g}{k_E}$. Here, the initial height of mass m_E is $z^{(E)}(t = 0) = h_0$, the frequency of the cosine is f_d and the maximum deflection of the spring is Δz_{max} (neglecting the static sag Δl_{stat} due to the weight $m_E \cdot g$). The velocity at time zero is $\dot{z}_{d,0}^{(V)} = 0$.

In the numerical simulation, Heun's method (*ode2* in Simulink) was used as a time integration scheme and the sample time was taken to be 1 ms. The properties of the mechanical system and the parameters for the RTS simulation were chosen as follows:

All results were compared to the validation simulation, where the reference mass-spring-mass system was simulated fully numerical by solving the differential equation with Simulink and an explicit Runge-Kutta time integration scheme (*ode45*). The contact was considered according to the penalization method, i.e. a spring acts as the mass m_E penetrates the ground. The spring constant was defined as $k = 10^9$ N/m. The solver returned the positions and velocities of both masses, i.e. $z^{(V)}$, $z^{(E)}$, $\dot{z}^{(V)}$ and respectively $\dot{z}^{(E)}$. Consequently, the interface force F_{int} can be calculated using the spring constant k_E ,

$$F_{int} = k_E \cdot \left(z^{(V)} - z^{(E)} - l_0 \right). \quad (1.2)$$

1.4.2 Results

The first experiments included a sinusoidal trajectory with $f_d = 0.25$ Hz and $f_d = 1$ Hz. Preliminary experiments revealed that the delay of the Stewart Platform is $\tau \approx 10$ ms for this kind and amplitude of excitation. K_p and K_d were chosen to be $K_p = 2 \cdot 10^6$ kg/s² and $K_d = 500$ kg/s, respectively, which means that the controller that keeps the upper mass on the desired trajectory z_d has a strong influence. All other parameters were taken from Table 1.1. The results are shown in Fig. 1.5. Each figure includes the validation simulation of the reference system (dashed line) and the measured solution from our RTS simulation (solid line). Figure 1.5a and b shows the displacement of mass m_V for an excitation of $f_d = 0.25$ Hz and $f_d = 1$ Hz. Figure 1.5c and d shows the interface force that was measured and adjusted as given in Eq. (1.1) compared to the interface force from the validation simulation, see Eq. (1.2). Due to numerical oscillation and rounding errors, the interface force of the validation simulation oscillates when there is no contact between m_E and the ground.

The results in Fig. 1.5 show that the results from the RTS experiment closely correspond to the results from the validation simulation. As the parameters K_p and K_d are quite high, the system dynamics are dominated by this controller that keeps m_V on the desired trajectory. Nevertheless, these first results show that our implementation is correct and that the experimental setup (introduced in Sect. 1.2) can be used for RTS simulations. Similar experiments were also conducted using a delay compensation. Nevertheless, the results are not improved because the results without delay compensation already sufficiently emulate the system dynamics.

So far, we have analyzed the feasibility of RTS experiments with the experimental setup. However, in the case of prostheses testing, we assume that the human will not control its desired trajectory as closely as the controller in the first experiments. Rather it will behave like a floating system. Hence, we have reduced the parameters to $K_p = 10^4$ kg/s² and $K_d = 50$ kg/s, respectively and performed similar tests. The prescribed trajectory had a frequency of $f_d = 0.25$ Hz. The

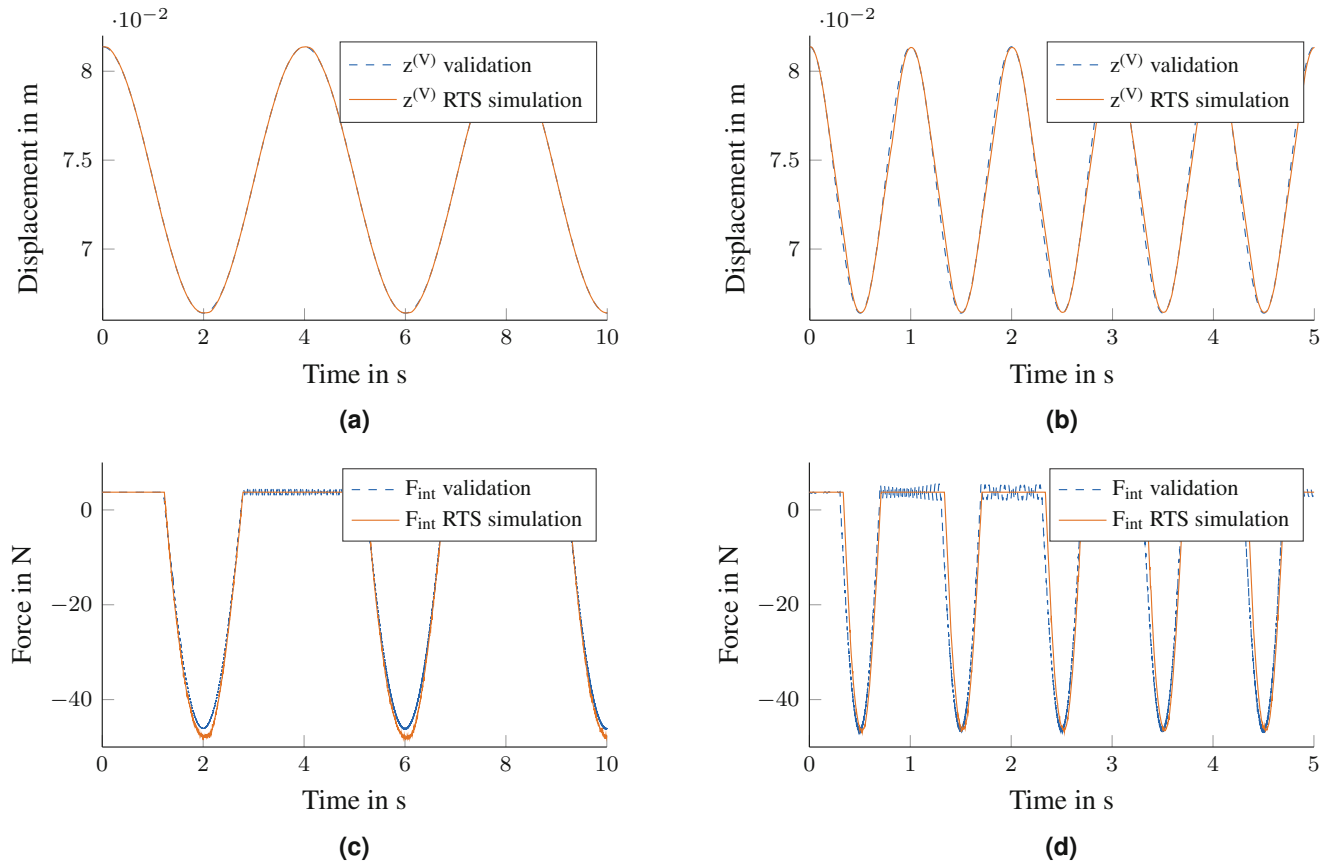


Fig. 1.5 Comparison of displacements and forces at the interface between validation simulation (dashed line) and real-time hybrid test (solid line). Experiments were conducted without delay compensation at 0.25 Hz and 1 Hz. (a) Displacement 0.25 Hz. (b) Displacement 1 Hz. (c) Interface force 0.25 Hz. (d) Interface force 1 Hz

experiments were conducted without and with a delay compensation as introduced in Sect. 1.3.3 with a polynomial of degree $n = 2$. The system dynamics are now much more influenced by contact problems and delay of the transfer system, as can be seen in Fig. 1.6. Figure 1.6a and b shows the displacement at the interface ($z^{(V)}$) without and respectively with delay compensation. Figure 1.6c and d shows the corresponding forces at the interface F_{int} .

Previously, the PD controller had higher values for K_p and K_d . This helped to stabilize the whole mechanical system, as the dynamics that are taken into account through the transfer system and the contact forces were suppressed. Now, the results show that coupling during contact makes the RTS simulation unstable. The displacement at the interface oscillates around the desired position with increasing amplitude. This effect is smaller, if we use the polynomial extrapolation as delay compensation (Fig. 1.6b and d). As the influence of the transfer system and the contact is increased (parameters K_p and K_d reduced), stability problems that can occur during RTS simulation with contact become clearly apparent. Furthermore, the accuracy of the dynamic analysis is reduced.

1.5 Conclusions

We have presented the experimental setup for RTS tests using a Stewart Platform. Ongoing research aims to test foot prostheses using this approach. First experiments show the applicability of this kind of actuator for real-time tests. The experimental setup differs from the reference model in respect of its orientation to external forces. This paper describes the relation between measured forces and interface forces that are required for a correct RTS simulation. As a first step towards testing of foot prostheses, we assume a simplified system for RTS simulations. The mechanical system investigated in this paper, is a mass-spring-mass system that moves in the vertical direction and is brought into contact with the ground. The upper mass is controlled by a PD controller (parameters K_p and K_d) so that it follows a desired, defined trajectory.

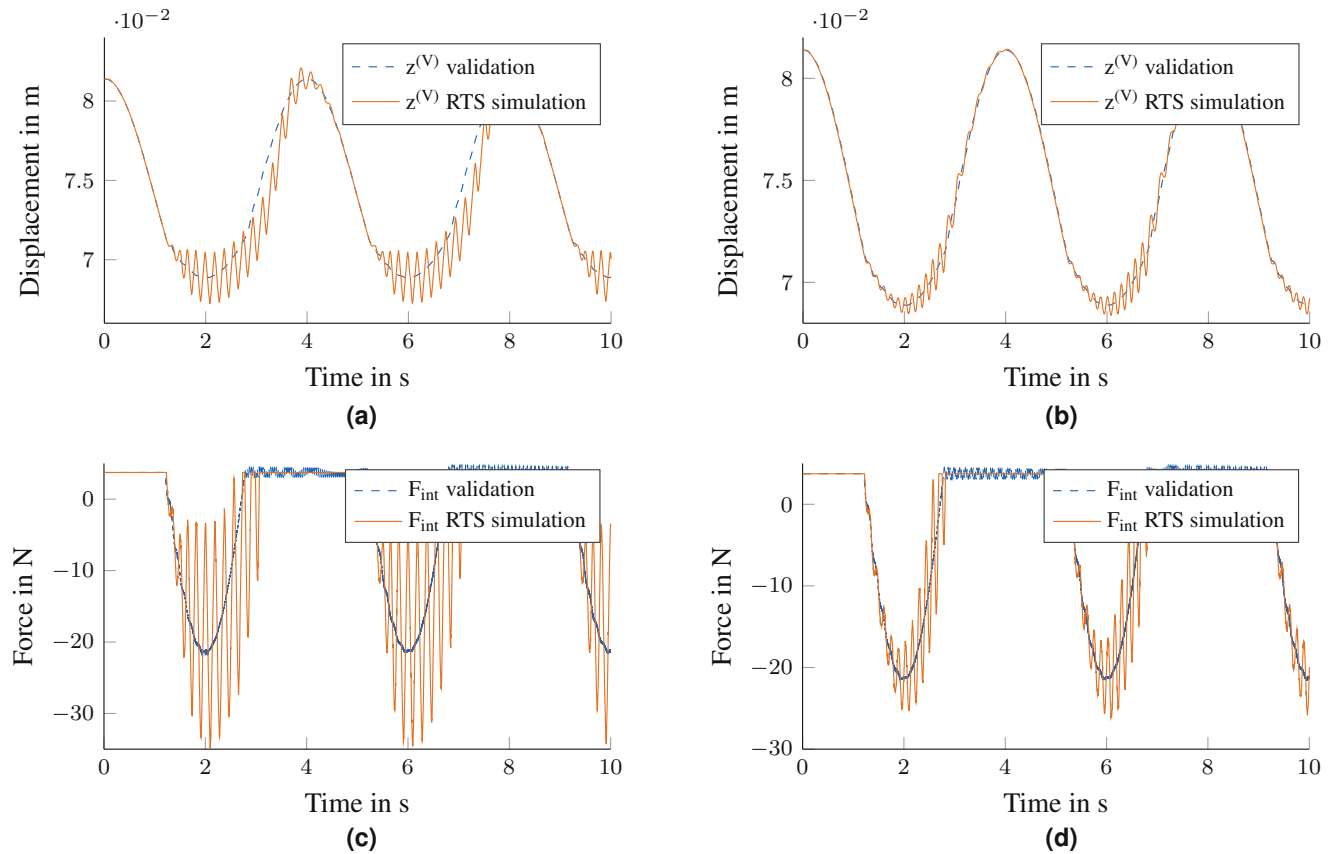


Fig. 1.6 Comparison of displacements and forces at the interface between validation simulation (dashed line) and real-time hybrid test (solid line) with smaller controller values for K_p and K_d . Experiments were conducted with a trajectory of frequency 0.25 Hz without and with delay compensation. (a) Displacement 0.25 Hz. (b) Displacement 0.25 Hz with delay compensation. (c) Interface Force 0.25 Hz. (d) Interface Force 0.25 Hz with delay compensation

Depending on the parameters of the PD controller, the dynamic behavior of the mechanical system is dominated by the PD controller or by the dynamics through coupling, i.e. the dynamics of the transfer system and forces when the device under test comes into contact. Experiments were conducted with different values for K_p and K_d as well as with delay compensation. The technique adopted for delay compensation is a polynomial extrapolation with degree $n = 2$. Results show that the influence of the coupling dynamics causes the RTS simulation to become unstable. The accuracy improves when using the delay compensation, although the system is still unstable in the RTS simulation. These preliminary results reveal the main obstacles that will also occur in the RTS simulation of a human walking with a prostheses. Hence, we need to improve the current test setup to obtain more accurate results even for those systems where the numerical part is floating.

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