# **Signal Processing for Cryptography and Security Applications**

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**Abstract** Embedded devices need both an efficient and a secure implementation of cryptographic primitives. In this chapter we show how common signal processing techniques are used in order to achieve both objectives. Regarding efficiency, we first give an example of accelerating hash function primitives using the retiming transformation, a well known technique to improve signal processing applications. Second, we outline the use of some special features of DSP processors and techniques earlier developed for efficient implementations of public-key algorithms. Regarding the secure implementations we outline the concept of side channel attacks

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and show how a multitude of techniques for preprocessing the data are used in such scenarios. Finally, we talk about fuzzy secrets and point out the use of DSP techniques for an important role in cryptography—a key derivation.

### **1 Introduction**

The implementation of cryptographic and security applications has adapted techniques more than expected from the architectures, design methods and tools of signal processing systems. When implementing cryptographic applications on embedded devices, in hardware, software or a combination of both, there are two optimization goals. The first request is one of efficiency: the implementations should be efficient in area, time, power consumption etc. This is very similar to the implementation of signal processing applications. The other requirement is one of a secure implementation. Implementations should not leak information. Signal processing techniques are used for both. As research progresses, signal processing and cryptography find more overlaps.

In this chapter, an overview is given of the use of signal processing techniques as they are used for efficient implementations as well as used for the analysis of secure implementations. The techniques that are used for efficient implementations in particular, are discussed in more detail in [\[62\]](#page-18-0) and [\[35\]](#page-16-0).

Section [2](#page-1-0) gives an overview of efficient implementations for both secret-key and public-key. It describes techniques borrowed from fast filter implementations to optimize the implementation of hash functions. It also describes implementations of public-key on DSP processors. Section [3](#page-10-0) focuses on secure implementations and the signal processing techniques used in analysis. Section [4](#page-12-0) discusses the usage of signal processing techniques for fuzzy secrets. Section [5](#page-14-0) gives the conclusion and describes some new trends.

### <span id="page-1-0"></span>**2 Efficient Implementation**

### *2.1 Secret-Key Algorithms and Implementations*

#### **2.1.1 Cryptographic Hash Functions and Implementations**

A cryptographic hash function is a deterministic algorithm that takes input strings— M of arbitrary length and returns short fixed-length strings, so called message digests—Hash(M), and it is required to satisfy the following cryptographic properties:

1. *Preimage resistance*: It must be infeasible to find any preimage, M, for a given hash output, H, such that H= *Hash*(M).



<span id="page-2-1"></span>**Fig. 1** MD6 DFG—critical path

- 2. *Second preimage resistance*: It must be infeasible to find another preimage, M1, for a given input,  $M_0$ , such that  $Hash(M_0) = Hash(M_1)$ .
- 3. *Collision resistance*: It must be infeasible to find two different inputs of the same hash output,  $M_0$  and  $M_1$ , such that  $Hash(M_0) = Hash(M_1)$ .

To be useful in applications such as Digital Signature Algorithm and message authentications, the performance becomes an important factor since inputs are easily large. To obtain architectures with a better performance, a design methodology is developed in [\[47\]](#page-17-0) based on theoretically proven signal processing techniques [\[61\]](#page-18-1). Here we illustrate this methodology with the example of MD6, which was one of the SHA-3 candidates<sup>1</sup> [\[16\]](#page-15-0). Parhi and Chen [\[62\]](#page-18-0) provide more detailed analysis of the common DSP techniques used in this example.

First, we derive a DFG (Data Flow Graph) of MD6 as shown in Fig. [1.](#page-2-1) This DFG represents one iteration of the algorithm, where the square nodes are registers and each register is paired with an *algorithmic delay* (*D*) so that the register values can be updated on each cycle. The circle nodes are functional nodes where ∧ denotes the bitwise "AND" operator,  $\oplus$ : the bitwise "XOR" operator,  $\ll b$ : left-shifted by *b* bits (zero shifting in), and  $\gg b$ : right-shifted by *b* bits (zero shifting in).  $S_i$  is constant, but changes from round to round. Each round is composed of 13 iterations and the number of rounds depends on the algorithm parameters.

The critical path delay can be measured as the maximum delay among any two consecutive algorithmic delays (*D*'s), which for MD6 consists of 6 XOR delays as shown in Fig. [1](#page-2-1) (indicated by an arrow with a dotted line). Before applying some techniques to minimize the critical path delay, we first need to know how much we can achieve. This can be done by analyzing the iteration bound of a DFG, which defines a theoretical lower bound of the achievable critical path delay as defined by the following equation:

$$
T_{\infty} = \max_{l \in L} \left\{ \frac{t_l}{w_l} \right\} = \frac{4 \times Delay(\bigoplus) + Delay(\wedge)}{18} \tag{1}
$$

<span id="page-2-0"></span><sup>&</sup>lt;sup>1</sup>SHA-3 competition, organized by the National Institute of Standards and Technology (NIST), is a worldwide competition for the development of a new hash standard.



<span id="page-3-0"></span>**Fig. 2** MD6 DFG—retiming transformation

where  $t_l$  is the loop calculation time,  $w_l$  is the number of algorithmic delays in the  $l$ th loop, and *L* is the set of all possible loops. The iteration bound of MD6 is defined with the loop indicated by a thick dotted line in Fig. [1.](#page-2-1)

In order to achieve a critical path delay as the iteration bound, it requires the unfolding transformation with the factor of the un-canceled denominator, which is 18 in this case. This introduces an overhead by duplicating the functional nodes (18 times duplication). Therefore, we choose not to perform the unfolding transformation but perform retiming transformation only. The achievable critical path delay only with the retiming transformation can be defined as follows:

$$
\lceil T_{\infty} \rceil = \left\lceil \frac{4 \times Delay(\bigoplus) + Delay(\wedge)}{18} \right\rceil = Prop(\bigoplus) \tag{2}
$$

 $\lceil \cdot \rceil$  is the maximum part when  $4 \times Delay(\oplus) + Delay(\wedge)$  is evenly distributed into 18 parts. Since it is assumed that a functional node can not be split into multiple parts in the iteration bound analysis,  $\oplus$  cannot be further split. By retiming transformations, we replace the algorithmic delays (*D*'s) in order to reduce the critical path delay. Some of the algorithmic delays between registers (including those in the abbreviated area) can be moved to proper positions as shown in Fig. [2](#page-3-0) where the new critical path delay is  $Prop(\oplus)$ . The details about retiming transformations and implementation issues can be found in [\[47,](#page-17-0) [61\]](#page-18-1). It shows that techniques which were originally developed for improving the throughput of digital filters with feedback can be also applied to hash function implementations. For more information about hardware design for cryptographic hash function we refer the reader to [\[48\]](#page-17-1).

In the light of the running SHA-3 competition, an extensive hardware evaluation of the competing algorithms has been performed by the research community. One of the examples is the work of Sharif et al. [\[68\]](#page-18-2), which specifically explores the influence of the embedded FPGA resources (such as DSP units) on hardware performance of the five SHA-3 finalists. Due to the presence of addition operation in their compression functions, two out of five candidates as well as the current SHA-2 standard benefit from using the DSP units. Since addition is a relatively simple operation, the benefit is more reflected in reducing the usage of other resources rather than increasing the overall throughput.

### *2.2 Public-Key Algorithms and Implementations*

#### **2.2.1 Efficient Modular Multiplication**

Public-key cryptography (PKC), a concept introduced by Diffie and Hellman [\[18\]](#page-15-1) in the mid 1970s, has gained its popularity together with the rapid evolution of today's digital communication systems. The best-known public-key cryptosystems are based on factoring i.e. RSA [\[66\]](#page-18-3) and on the discrete logarithm problem in a large prime field (Diffie-Hellman, ElGamal, Schnorr, DSA) [\[53\]](#page-17-2) or on an elliptic/hyperelliptic curve (ECC/HECC) [\[42,](#page-17-3) [43,](#page-17-4) [56\]](#page-17-5). Based on the hardness of the underlying mathematical problem, PKC usually deals with large numbers ranging from a few hundreds to a few thousands of bits in size. Consequently, the efficient implementations of the PKC primitives has always been a challenge.

An efficient implementation of the mentioned cryptosystems highly depends on the efficient implementation of modular arithmetic. Namely, modular multiplication forms the basis of modular exponentiation which is the core operation of the RSA cryptosystem. It is also present in many other cryptographic algorithms including those based on ECC and HECC. In particular, if one uses projective coordinates for ECC/HECC, modular multiplication remains the most time consuming operation for ECC. Hence, an efficient implementation of PKC relies on efficient modular multiplication.

Two algorithms for modular multiplication, namely Barrett [\[8\]](#page-15-2) and Montgomery [\[57\]](#page-17-6) algorithms are widely used today. Both algorithms avoid multiple-precision divisions, the operation that is considered to be expensive, especially in hardware. Implemented on a first generation of DSP produced by Texas Instruments (TMS 32010), the Barrett's algorithm is one of the famous examples in the area of signal processing for cryptography. The properties of a DSP such as fast multiply and accumulate (MAC) operation and a fast microprocessor on a single chip seemed to be an ideal combination for the proposed algorithm. Furthermore, additional speedups were obtained by taking advantage of a feature of the TMS320 DSP which allowed auto increment and decrement of data pointers during MAC operations. This ensured the data fetching for free. The original Barrett reduction algorithms is given in Algorithm [1.](#page-4-0)

#### <span id="page-4-0"></span>**Algorithm 1** Barrett modular reduction

**Input:**  $A = (A_{2n-1} \ldots A_0)_2$ ,  $M = (M_{n-1} \ldots M_0)_2$  where  $M_{n-1} \neq 0$ ,  $\mu = \lfloor 2^{2n}/M \rfloor$ . **Output:**  $R = A \text{ mod } M$ .  $\hat{Q} \Leftarrow \left| \frac{\left\lfloor \frac{A}{2^{n-1}} \right\rfloor \mu}{2^{n+1}} \right|$  $R \Leftarrow A \mod 2^{n+1} - \hat{Q}M \mod 2^{n+1}$ **while**  $R > M$  **do**  $R \Leftarrow R - M$ **end while** return *R*.

<span id="page-5-0"></span>

**Input:**  $A = (A_{2n-1} \ldots A_0)_2$ ,  $M = (M_{n-1} \ldots M_0)_2$ ,  $r = 2^n$  where  $gcd(M, 2) = 1$ ,  $M' = -M^{-1}$  mod *r*. **Output:**  $T = Ar^{-1} \mod M$ .  $S \leftarrow (A \mod r)M' \mod r$  $T \leftarrow (A + SM)/r$ **if**  $T > M$  **then**  $T \leftarrow T - M$ **end if** return *T*.

Montgomery's algorithm is the most commonly used reduction algorithm, nowadays. It is widely used to speed up the modular multiplications and squarings required during the exponentiation process. The Montgomery reduction algorithm computes  $T = A \cdot r^{-1}$  mod *M*, given  $A \lt M^2$  and *r* such that  $gcd(r, M) = 1$ . Even though the algorithm works with any  $r$ , relatively prime to  $M$ ,  $r$  is very often chosen to be a power of 2. In that case, the Montgomery algorithm performs integer divisions by a power of 2, which is an intrinsically fast operation on both generalpurpose and specialized processors. The algorithm is given in Algorithm [2.](#page-5-0)

There is a number of publications reporting the implementations of Montgomery's algorithm on a DSP. One of the first reported results was a work of Michael Wiener who had developed a general software implementation of RSA on the Motorola DSP56000 that achieved 10.2 Kbps for 512-bit modular exponentiation with the Chinese remainder theorem (CRT) [\[11\]](#page-15-3). Dusse and Kaliski have published an RSA implementation on the same chip achieving 11.6 Kbps for 512-bit modular exponentiation with the CRT [\[20\]](#page-16-1). They adopted the Montgomery's algorithm by reducing the number of shift operations. Since on many processors the "high part" and the "low part" of accumulators are separately addressable, the shift operations have to be performed with move instructions. This was also true for the DSP56000 and the idea of reducing the number of shifts turned out to be a very good approach. Itoh et al. proposed a fast implementation method of Montgomery multiplication on a DSP TMS320C6201 [\[38\]](#page-16-2). This DSP operates eight function units in parallel achieving a performance of 11.7 ms for 1024-bit RSA signing (87.5 Kbps). In 2004, Großschädl et al. [[30\]](#page-16-3) analyzed the performance of Montgomery multiplication on the MIPS32 4Km and the ARM 946E-S processors. In particular, they explored the suitability of the DSP architectural enhancements to speed up multiple-precision modular multiplication. Recently, Gastaldo et al. [\[25\]](#page-16-4) have published an enhanced Montgomery multiplication algorithm, a variant of the finely integrated product scanning (FIPS) algorithm, that is targeted to digital signal processors. More about various approaches for implementing Montgomery's algorithm on a DSP can be found in [\[44\]](#page-17-7).

#### **2.2.2 Implementations of Public-Key Algorithms**

There are several implementations reported in the literature describing efficient PK cryptosystems on DSP architectures, mainly relying on the algorithm of Montgomery. For RSA cryptosystems, modular multiplication is practically the only required operation. As it is commonly implemented as a sequence of repeated squarings and multiplications, some authors explored possible speed-ups that can be achieved for a dedicated squaring. Krishnamurthy et al. proposed a new method for the Montgomery squaring reduction especially suited for DSP processors. The new method restructures the loop in the squaring reduction and when implemented on the TI TMS320C6201 DSP platform results in speed-ups of 10–15 % compared to the previous work in [\[38\]](#page-16-2). The results are obtained by removing the redundancy of previous proposals and by maximizing the feature of pipelining as much as the platform permits.

Guajardo et al. [\[31\]](#page-16-5) described a strategy for an efficient implementation of ECC over  $GF(p)$  on the 16-bit TI MSP430x33x family. This family of devices is commonly used for ultra-low power applications such as electronic meters for gas, water and electricity and also for sensor systems that collect analogue signals. The signal are converted to digital ones before being transmitted to a host. The properties make the platform very suitable for embedded security applications.

The authors use a Generalized-Merssenne prime to facilitate the underlying field arithmetic. The operations i.e. multiplication, squaring and modular reduction are adapted to explore the specifics of the architecture. For example, multiplications with small constants were traded for additions as the ratio of multiplication and addition is around 10 on this processor. Also, squaring was found to be much faster when implemented as a special routine because the communication with data memory was reduced (requiring only one input in this case). The use of a special prime, as suggested by standards, was additionally tailored to the 16-bit architecture. However, all the tricks used were not enough to meet the requirements for the 160-bit security level (as required minimum for ECC key lengths). Therefore, they propose to use 128-bit EC implementations as sufficient for the targeted applications.

We note here that implementing squaring in a different manner from general multiplication is found to be sensitive to side-channel attacks (see Sect. [3\)](#page-10-0). Therefore, the ideas of dedicated squaring are abandoned for embedded applications.

By extensive use of the DSP blocks on Xilinx's Virtex-4 SX55 FPGA board, Güneysu and Paar [\[34\]](#page-16-6) report the fastest point multiplication on commercially available FPGA platforms. Their implementation performs more than 24,000 and 37,000 point multiplications per second for ECC over the NIST P-256 and P-224 fields, respectively.

Morozov et al. [\[58\]](#page-17-8) investigate the design space of ECC implementation on Texas Instruments' OMAP 3530 platform (accommodating the ARM Cortex A8 core), specifically considering its DSP core for accelerating the underlying modular arithmetic. A speedup of more than 9 times is achieved, compared to the implementation executing on the ARM Cortex processor only.

#### **2.2.3 Other Ideas for Arithmetic Borrowed from Signal Processing**

Cryptographic application as well as signal processing require arithmetic-intensive operations, hence there are several ideas that were applied in both. Examples include Residue Number System (RNS) arithmetic [\[69\]](#page-18-4), signed-digit arithmetic, computation in frequency domain etc.

Nowadays ever faster arithmetic is demanded e.g. for RSA cryptosystems due to the constant improvements in factoring and the resulting requirements for even longer key sizes. In order to achieve that, the Residue Number System is an alternative to the common radix representation. RNS arithmetic is a very old idea which relies on the Chinese Remainder Theorem (CRT) and it provides a good means for very long integer arithmetic.

Let  $\langle x \rangle_a$  denote an RNS representation of *x*, then:

$$
\langle x \rangle_a = (x[a_1], x[a_2], \dots, x[a_n]) \tag{3}
$$

where,  $x[a_i] = x \mod a_i$ . The set  $a = \{a_1, a_2, \ldots, a_n\}$  is called a base (of size *n*). It is required that  $gcd(a_i, a_j) = 1$  for  $i \neq j$ . CRT implies that the integer *x* which satisfies  $0 \le x < \prod_{i=1}^{n} a_i$  is uniquely represented by  $\langle x \rangle_a$ .

A well known advantage of RNS is that to add, subtract and multiply such numbers we only need to compute the addition, subtraction and multiplication of their components, of size much smaller than the original modulus. Also carry-free arithmetic makes parallelization possible. The final result is obtained by means of the CRT. The disadvantage of an RNS representation is the overhead introduced by the input and output conversions from binary to RNS and vice versa. It is also difficult to perform division. To overcome this disadvantage, a combination with Montgomery multiplication was proposed [\[64\]](#page-18-5). Recent results show that RNS Montgomery brings a higher speed for both ECC and Pairing implementations on FPGAs [\[15,](#page-15-4) [33\]](#page-16-7).

Exponent recoding techniques for modular exponentiation (as used for RSA) replace the binary representation of an exponent with a representation which has fewer non-zero terms (see Gollmann et al. [\[29\]](#page-16-8)). Many techniques for exponent recoding have been proposed in the literature. Here we mention the signed-digit representation. Consider an integer representation of the form  $k = \sum_{i=0}^{l} s_i 2^i$ , where  $s_i \in \{-1,0,1\}$ . This is called the (binary) signed digit (SD) representation (see Menezes et al. [\[53\]](#page-17-2)). The representation is redundant. For example, the integer 3 can be represented as  $(011)_2$  or  $(10\bar{1})_2$ , where  $\bar{1} = -1$ . It is said that an SD representation is *sparse* if it has no adjacent non-zero digits. A sparse SD representation is also called a *non-adjacent form* (NAF). Every integer *k* has a unique NAF which has the minimum weight of any signed digit representation of *k*.

For RSA, the NAF techniques are not beneficial because they assume performing the division operation, which should be avoided due to the complexity of the operation. However, for ECC it is considered advantageous because the Hamming weight of the scalar is minimal. Also in this case "−1" means point subtraction instead of addition, which is an addition of the inverse point. More precisely, the

scalar is decomposed as a NAF and the scalar multiplication is done with a series of addition/subtractions of elliptic curve points.

Other redundancy-based techniques include on-line arithmetic as proposed by Ercegovac [\[21\]](#page-16-9). In particular on-line arithmetic for DSP applications can be found in [\[22\]](#page-16-10).

ECC implementation in the frequency domain is given by Baktir et al. [\[6\]](#page-15-5). The work is based on Discrete Fourier transform (DFT) modular multiplication and ECC processor architecture using the multiplier is presented. In this way multiplication in  $GF(q^m)$  is achieved by only a linear number of base field  $GF(q)$ multiplications in addition to a quadratic number of simpler base field operations such as additions/subtractions and bitwise rotations.

An idea for implementation of large integer multiplication in the discrete Fourier domain originates from Kalach and David [\[40\]](#page-17-9).

### *2.3 Architecture*

The architecture design of cryptographic systems requires special considerations on performance, cost and security. Many cryptographic systems, especially public-key cryptosystems, involve complex operations with large integers or long polynomials. Thus, cryptographic co-processors, just like accelerators for multimedia, communication or image processing, are introduced to offload the heavy processes from CPU. As a result, a Hardware/Software (HW/SW) co-design approach is usually used. Both the co-processor and the interface need to be carefully designed such that the co-processor can efficiently offload the work from CPU while security and flexibility are maintained. We illustrate the idea with an Elliptic Curve Processor.

#### **2.3.1 Datapath**

Datapath normally accounts for a large percentage of the total area and is a determinative factor of the performance. Taking ECC over GF(p) as an example, each scalar point multiplication involves hundreds of modular multiplications. As a result, speeding up the modular multiplication is the key to improve the overall performance. The multiplier can be implemented in a bit-parallel, digit-parallel or digit-serial way. When using digit-serial multiplier, the area of the datapath can be by adjusted by changing the digit-size. On some FPGA platforms, we can also use the dedicated multipliers or MACs (e.g. 25-bit MAC on Virtex-5) as building blocks of a modular multiplier [\[34,](#page-16-6) [54\]](#page-17-10).

When targeting high speed applications, an implementation can use multiple datapaths to run several modular multiplications in parallel [\[23,](#page-16-11) [67\]](#page-18-6). The basic idea is similar to a classical superscalar processor that explores the instruction level parallelism. However, such kind of architecture normally requires aggressive memory accesses, which requires a high throughput memory.

<span id="page-9-0"></span>



#### **2.3.2 Interface**

The interface between the co-processor and CPU is of vital importance, as the HW/SW partitioning has a large impact on the performance and flexibility. Take ECC as an example, one can immediately see the following three choices, as shown in Fig. [3.](#page-9-0)

When choosing *PL* as the partitioning point, the co-processor performs the modular arithmetic while the CPU generates instruction sequences for point addition/doubling and all functions above. This choice is offers a very good flexibility. On the other side, the CPU has to frequently transfer data and instructions to the co-processor, which may become a bottleneck. If we choose  $P_H$  as the partitioning point, then the CPU only needs to send the data at the very beginning of a scalar multiplication, and substantially reduces the communication overhead. However, it is difficult to update the scalar multiplication algorithm since it is now implemented in hardware.

Being able to update the functionality of an cryptographic implementation is very important as standards may change or the old algorithm is no longer safe due to the discovery of new attacks. For example, when new side-channel attacks are founded, corresponding countermeasures need to be added. Thus, the co-processor should have a certain degree of programmability. One method to achieve low communication overhead and high flexibility is to introduce control hierarchy. Instead of fixed state machine (FSM), a programmable micro-controller can be used in the co-processor.

#### **2.3.3 Low Power Architecture**

When using cryptography in constrained devices, i.e. passive RFID tags and wireless sensor nodes, power consumption becomes a big challenge. Several low power architectures [\[36,](#page-16-12) [49\]](#page-17-11) for ECC have been proposed. Traditional techniques such as reducing the hardware size, lowering the clock frequency and using clockgating are helpful. For ECC implementations, registers account for more than 60% of the area and most of the dynamic power. Thus, reducing the size of register file and register flipping can significantly reduce the power consumption.

### <span id="page-10-0"></span>**3 Secure Implementations: Side Channel Attacks**

Cryptographic algorithms, i.e. mathematical objects describing the input–output behavior of a black box, have to go through a thorough process of cryptanalysis before they are widely accepted as secure and possibly standardized. Implementations of cryptographic algorithms essentially instantiate these black boxes.

An implementation of an algorithm does however not automatically inherit the algorithm's security. The fact that the abstract black box is implemented in software, hardware, or a combination of both gives rise to new security risks. Indeed, measurable physical properties of an implementation become an additional, unintended source of information, giving away knowledge about the secrets involved in cryptographic implementations. Those sources are called side channels. While the execution time of an implementation can be measured even from a distance, e.g. over a network, the physical accessibility of embedded devices in particular gives rise to even more side channels such as the power consumption, electromagnetic radiation, acoustics, heat dissipation, light emission, etc.

Cryptanalytical methods exploiting such information leakage to extract secret data are called side channel attacks. Side channel attacks are a serious concern as they allow to extract secret information from unprotected implementations of black box secure algorithms with moderate effort. With the ever increasing availability and ubiquity of embedded devices, side channel attacks are a realistic threat nowadays.

One type of side channel attacks, a differential side channel attack, sequences several steps to extract the secret information. In a first stage the attacker collects measurements of the side channel, e.g. power consumption, as a function of the time. Each measurement is the physical representation of the execution of the cryptographic algorithm with a different message but a fixed key. In a second stage, the attacker preprocesses the data, chooses a hypothetical power leakage model and calculates the hypothetical leakage using this model for each message and for every possible key guess. An example of one such model is the hamming weight of the processed data at a certain time instant. In this case an adversary assumes that the amplitude of the side channel measurement is related to the amount of binary ones in the data. The validity of this model in certain cases is demonstrated in Fig. [4.](#page-11-0) In the last phase of the attack, the attacker uses a statistical test to quantify the similarity between the hypothetical leakage and the real side channel leakage for every key guess. The key that reveals the strongest relation is the adversary's best guess.

### *3.1 DSP Techniques Used in Side Channel Analysis*

The side channel analysis research domain has become a mature research area over the last decade, hence a multitude of techniques for preprocessing the data and quantifying the relation between the real and hypothetical leakage have been proposed.



<span id="page-11-0"></span>**Fig. 4** Measurements of supply current over time. Data dependent operations in clock cycles three and four leak information about the operand(s)

The measurements of the side channel are susceptible to external and internal noise contamination. Therefore, a first group of preprocessing techniques aims at reducing the amplitude noise. The easiest preprocessing technique is averaging the measurements. This was first pointed out by Kocher et al. in [\[45\]](#page-17-12). More noise reduction can be achieved through filtering the data [\[7\]](#page-15-6). Results have been published for the power side channel [\[55\]](#page-17-13) as well as for the electromagnetic side channel [\[5\]](#page-15-7). Another, more recently proposed technique is calculating the fourth-order cumulant [\[46\]](#page-17-14). In some cases, the useful information is modulated onto a carrier. For this type of data extraction, demodulation techniques are appropriate [\[5,](#page-15-7) [41,](#page-17-15) [60\]](#page-17-16).

Due to clock jitter, absence of a suitable trigger or simply due to countermeasures, measurements can suffer from temporal misalignment. Some publications deal with this problem and try to remove the temporal misalignment. Homma et al. explain the phase-based waveform matching procedure [\[37\]](#page-16-13) and Gebotys and White introduce the phase replacement technique [\[27\]](#page-16-14). Pelletier and Charvet use wavelets to get rid of misalignment [\[63\]](#page-18-7). The rapid alignment method [\[59\]](#page-17-17) of Muijrers et al. also builds on wavelets. Woudenberg et al. propose to use dynamic time warping [\[70\]](#page-18-8).

In the final phase of a side channel attack, the attacker uses a statistical tool to find the correct key by analyzing the relation between the hypothetical leakage and the measured leakage. The difference of means test was proposed by Kocher et al. in their seminal paper [\[45\]](#page-17-12). Later, more advanced techniques were put forward: the Ttest [\[17\]](#page-15-8), the Pearson correlation coefficient [\[12\]](#page-15-9), Spearman rank correlation [\[9\]](#page-15-10), mutual information [\[28\]](#page-16-15), and maximum likelihood [\[14\]](#page-15-11). While all the previous techniques are applied in the time domain, the differential frequency analysis exploits the frequency information [\[26\]](#page-16-16).

Advanced signal processing techniques strengthen the adversary's capabilities and raise the need for proper and better countermeasures against side channel attacks.

### <span id="page-12-0"></span>**4 Working with** *Fuzzy Secrets*

# *4.1* **Fuzzy Secrets***: Properties and Applications in Cryptography*

Secrets play an important role in cryptography, since the alleged security of many cryptographic schemes is solely based on the assumed confidentiality of certain data, mostly called a *key*. In order for a secret key to be secure, it needs to be hard for an adversary to guess its value. Keys are mostly represented as digital *n* bit strings and when they are sampled uniformly at random from  $\{0,1\}^n$ , an adversary can only guess their value with probability  $2^{-n}$ , which becomes negligibly small when *n* is chosen large enough. Also, a cryptographic algorithm should only succeed when the correct key is applied, and fail when even the slightest bit is changed, in order to prevent an adversary from guessing *close* keys, which is easier than 2−*n*. This means that secret keys cannot be subject to any kind of noise or distortion.

In a number of security applications, secret data is present, but not in the form of a uniformly distributed and noise-free binary key string. This is often the case when the secret stems from a physical phenomenon which is mostly analogue in nature, not uniformly distributed and subject to random noise. Such data is called a *fuzzy secret*. Some examples of cryptographic settings involving fuzzy secrets are listed below:

- Biometric readings such as fingerprints, iris scans, face structure and voice patterns are believed to be unique to each human being and can hence serve as a unique, and possible secret, identifier. To obtain digital data from these readings, a feature extraction process is necessary. However, the extracted features are most likely not uniformly distributed and some features are measured differently at consecutive readings, i.e. they are subject to measurement noise. Extracted biometrical features can hence not be directly used as a cryptographic key.
- Physically unclonable functions [\[52\]](#page-17-18) or PUFs are cryptographic hardware primitives that fulfill a function similar to biometrics, i.e. they measure unique physical properties of their embedding device. Interesting constructions of PUFs are those that are embedded into integrated circuits, since they allow to generate device-unique and highly protected chip identifiers [\[24,](#page-16-17) [32\]](#page-16-18). The uniqueness of every chip stems from uncontrollable nano-scale manufacturing variability in the production process of the circuits. Like biometrics, PUF responses suffer from a non-uniform distribution and unreliability due to measurement inaccuracy and random thermal noise in the electrical measurement circuits.

More settings involving fuzzy secrets exist, e.g. in authentication with long passphrases and in quantum key agreement.

The non-uniformity and the noise of a fuzzy secret can be quantified. Information entropy is commonly used to describe the uncertainty about a random variable.

A special case of entropy called *min-entropy* describes the worst case uncertainty, i.e. it evaluates the best chances an adversary has in guessing a secret value chosen from a known distribution. The min-entropy of a random variable *X* is denoted as  $H_{\infty}(X)$  and defined as  $H_{\infty}(X) \stackrel{def}{=} -\log_2 \max_x \Pr[X = x]$ . A uniformly distributed *n*-bit variable has maximal min-entropy equal to *n*, while a deterministic value has min-entropy zero. To describe the noise, it is assumed that the measured fuzzy secret *X* is a bit vector of length *n*. Two distinct observations of the fuzzy secret possibly differ in a number of bit locations due to noise. The *amplitude* of the noise affecting *X* can be quantified by the maximum number  $\delta(X)$  of differing bits between two measurements.

## *4.2 Generating Cryptographic Keys from* **Fuzzy Secrets** *by Means of Error Correction*

Mostly, a physical variable cannot be directly used. It should first be measured as accurately as possible and afterwards quantized into a discrete value which can be used by a digital algorithm. The quantization process translates physical noise into bit errors of a bit vector. Also, due to rounding, part of the information in the measured value is already lost. A careful choice for quantization should be made to optimize these parameters given the implementation constraints.

After measurement and quantization, one is left with a possibly non-uniform and unreliable bit string  $X \in \{0,1\}^n$ . By performing multiple measurements, the aforementioned parameters  $H_{\infty}(X)$  and  $\delta(X)$  can be estimated. The next step in the transformation is dealing with the noise which can introduce up to  $\delta(X)$  bit errors. Error correction techniques are frequently used in channel coding theory. A process known as the *code-offset construction* [\[19,](#page-15-12) [39,](#page-16-19) [50\]](#page-17-19) is an elegant way of using error correcting block codes in order to get rid of bit errors in a measurement of *X*. The technique works in two phases:

- 1. In the generation phase, *X* is measured and a codeword *C* is randomly selected from an  $[n, k, t]$ -block code, with *n* the code length, *k* the code dimension and *t* the error correcting capability. The binary offset between *X* and *C* ia calculated as  $W = X \oplus C$  and *W* is made publicly available, e.g. it is published in an online database.
- 2. In the reproduction phase,  $X'$  is measured which can differ from  $X$  in up to  $\delta(X)$  bit positions. Using the publicly available *W*, one can calculate  $C' =$  $X' \oplus W$ , which differs from *C* in at most  $\delta(X)$  bits. If the used code is chosen appropriately such that  $t > \delta(X)$ , the decoding algorithm will succeed to compute  $C = \text{Decode}(C')$ . In that case the same *X* as in the generation phase can be reconstructed as  $X = C \oplus W$ .

More elaborate error-correction techniques can be applied to transform a noisy measurement value into a reliable bit string. In the *syndrome construction* [\[19\]](#page-15-12) the syndrome, instead of the offset, of a linear block code is used, which reduces the communication overhead. In [\[51\]](#page-17-20), it is shown that certain fuzzy secrets produce *soft-decision information*, which allows the use of soft-decision error-correcting techniques. This allows to extract a longer and hence more secure key from the same fuzzy secret.

All these techniques uses a public communication to establish a noise-free secret from a noisy secret. The data that is passed through this channel, *W* is called *helper data*. It is clear that the publishing of *W* decreases the uncertainty an adversary may have about the value of *X*. In fact, for the code-offset construction it can be shown that the min-entropy of *X* is reduced from  $H_{\infty}(X)$  to  $H_{\infty}(X) - n + k$ , i.e. that the helper data induces a *min-entropy loss*.

To conclude, the now noise-free secret with limited min-entropy needs to be transformed into a uniformly distributed key *K*. In order to do this, *randomness extractors* are used. Randomness extractors succeed in extracting uniform randomness from non-uniformly distributed variables [\[10,](#page-15-13) [13\]](#page-15-14). It is obvious that the output domain of a randomness extractor is smaller than the input, hence they are compression functions. In fact, the min-entropy of a random variable *X* is a measure for the maximum number of uniform bits an ideal randomness extractor can extract from *X*. After error correction with the code-offset technique, the fuzzy secret *X* can hence contribute at most *H*∞(*X*)−*n*+*k* uniformly random bits. Generic randomness extractors can be constructed relatively easy by using so-called *universal hash functions*: if  $H$  is a universal hash family, the process that selects a random function  $h_{\sigma} \leftarrow \mathcal{H}$  and calculates  $K = h_{\sigma}(X)$  is a randomness extractor. The *seed*  $\sigma$  can again be published as helper data to allow reconstruction of *K* at later times, this time however without additional loss in min-entropy.

### <span id="page-14-0"></span>**5 Conclusion**

The purpose of this chapter is to illustrate the usage of signal processing techniques into the design and implementation of cryptographic and security applications. This is only the beginning and by no means complete. New directions are being explored. One example is the exploration of signal processing in the encrypted domain, which is the topic of the SPEED project [\[65\]](#page-18-9).

**Acknowledgements** This work is supported in part by the IAP Programme P6/26 BCRYPT of the Belgian State, by the European Commission under contract numbers ICT-2007-216676 ECRYPT NoE phase II and ICT-2007-238811 UNIQUE, and by the Research Council K.U.Leuven: GOA 11/007 TENSE. Benedikt Gierlichs is a Postdoctoral Fellow of the Fund for Scientific Research - Flanders (FWO).

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