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# Seismic resilience assessment of corroded reinforced concrete structures designed to the Chinese codes

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**Abstract:** The natural landscape in China exposes many existing RC buildings to aggressive environments. Such exposure can lead to deterioration in structural performance with regard to resisting events such as earthquakes. Corrosion of embedded reinforcement is one of the most common mechanisms by which such structural degradation occurs. There has been increasing attention in recent years toward seismic resilience in communities and their constituent construction; however, to date, studies have neglected the effect of natural aging. This study aims to examine the effect of reinforcement corrosion on the seismic resilience of RC frames that are designed according to Chinese seismic design codes. A total of twenty RC frames are used to represent design and construction that is typical of coastal China, with consideration given to various seismic fortification levels and elevation arrangements. Seismic fragility relationships are developed for case frames under varying levels of uncorroded and corroded RC frames are compared using a normalized loss factor. It was found that the loss of resilience of the corrosion induced increase in loss of resilience can be more than 200%, showing the significant effect of reinforcement corrosion on structural resilience under the influence of earthquakes.

Keywords: seismic resilience; seismic fragility; corrosion; Chinese seismic design codes; RC frames

# **1** Introduction

Many parts of China are exposed to weather elements that would constitute an aggressive environment. This offers durability problems due to the degradation of material performance. Such an aggressive environment can cause significant corrosion in reinforcement (Enright and Frangopol, 1998), leading to the deterioration of the mechanical properties of reinforcing bars (Du *et al.*, 2005), the cracking of cover concrete (Zhao *et al.*, 2015), and a reduction in bar-concrete bond strength (Lundgren, 2007; Bhargava *et al.*, 2007). These deterioration mechanisms that are caused by corrosion could significantly affect structural resistance against earthquakes (Yalciner *et al.*, 2015; Liu *et al.*, 2017; Dai *et al.*, 2020a). Therefore, it is necessary to investigate

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the seismic performance of aging RC structures that exhibit corroded reinforcement.

In recent years, the concept of seismic resilience has attracted worldwide attention. Bruneau et al. (2003) proposed a conceptual framework for quantifying the seismic resilience of communities, which includes four dimensions: robustness, redundancy, resourcefulness and rapidity. This conceptual framework was extended by Cimellaro et al. (2010) to define the resilience of disasters. Moreover, Miles and Chang (2006) developed a conceptual model of community recovery by using Markov chains to simulate the recovery trajectory. All previous studies focused on seismic resilience from a regional-scale viewpoint. These studies demonstrated the consequences for and the recovery of the concerned region due to the effects of earthquakes. Unlike regional seismic resilience, numerous studies have also been conducted to improve structure-specific resilience with respect to earthquakes. For example, new types of building systems (Deierlein et al., 2011; Sabbagh et al., 2012) or structural elements (Wilkinson et al., 2006; Liu and Jiang, 2017) have been proposed. From a structurespecific resilience perspective, the enhancement of structural resilience is equal to the reduction of structural damage caused by earthquakes.

Through an overview of available studies, it is found that regional resilience and structure-specific

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resilience are not quantified in a consistent way. This is inconvenient for the extension of the resilience of individual structures in the context of a community. The regional resilience result also cannot be directly used to guild the design or retrofitting of individual structures. As noted by Cimellaro et al. (2010), the seismic resilience of individual structures should incorporate the interaction between the individual structures and the community. Based on this idea, it is important to evaluate structurespecific resilience as compatible with the strategy that was used in the regional resilience assessment (Wen et al., 2019). In recent years, several studies have focused on structural resilience by considering the effect of reinforcement corrosion. For example, Biondini et al. (2015) proposed a probabilistic lifetime assessment approach for quantifying the seismic resilience of concrete structures by considering corrosion-induced deterioration. This approach was then applied to a three-story concrete frame building and a four-span continuous concrete bridge. This approach showed the combined effects of corrosion and earthquakes on the time-varying performance of the system. Motlagh et al. (2020) evaluated seismic resilience for existing and corroded buildings by considering near-fault pulse-type ground motion. China has a long coastline with numerous RC structures located in a chloride environment. Therefore, the problem of reinforcement corrosion is severe in existing RC structures, which could cause a significant deterioration in the structural capacity to resist earthquakes. However, the seismic resilience of the corroded RC structures in China is not well documented.

To bridge this knowledge gap, this study aims to conduct a comprehensive investigation of the seismic resilience of aging RC frames that have been designed according to Chinese seismic design codes (GB50011-2010, 2010). To do this, a total of twenty RC frames have been designed with varying earthquake fortification levels and structural heights. The designed RC frames are used to represent typical designs and constructions of the RC frame in coastal areas of China. Fragility relationships are developed for case frames that are uncorroded and have experienced growing corrosion rates of 5%, 10%, and 15%. Subsequently, a normalized loss factor of resilience proposed by Wen et al. (2019) is used to quantify the resilience for uncorroded and corroded RC frames. Through comparisons, the effect of reinforcement corrosion on structural resilience is extracted.

# 2 Structural design and modeling

#### 2.1 Structural design

The RC frames were designed by assuming they are located in the eastern coastal regions of China. Sixtysix cities in the target regions were considered. Design requirements corresponding to the cities in the study were collected from GB50010-2010 (2010) and GB50011-2010 (2010) with regard to seismic fortification levels, wind loads, and snow loads. To make the structural designs representative, the method used in the global earthquake model (GEM) (D'Ayala D et al., 2014) was adopted to determine design variables, with high, medium and low levels. In this study, four important design variables were considered, which included the number of stories, bay width, the axial loading ratio of columns, and the period reduction factor, taking into account the contribution of infill walls to structural stiffness. Therefore, a total of four groups of RC frames were designed with varying story numbers, bay widths, axial force ratios, and period reduction factors. In the building group with varying story numbers, six and nine stories were chosen to represent the low-to-medium height of RC frames. Three types of bay widths, 6.0 m, 7.2 m, and 8.4 m, were considered. Two commonly used axial force ratios, 0.65 and 0.73, were selected as the basic ratios for nine- and six-story RC frames. For the high and low level of axial force ratio, the basic ratios should be increased or decreased by 0.1, respectively. As for the period reduction factors, they were considered to be varied as 0.85 and 0.7, corresponding to the low and high contributions of infill walls to the structural stiffness. Table 1 summarizes the designed frames and the corresponding design variables. Figure 1 shows the plan and elevation views of the designed frames. All the frames were designed with the same plan arrangement. The reinforcement details and the geometric sizes of columns and beams are provided in Fig. 2 and Table 2.

#### 2.2 Structural modeling and validation

OpenSees was used to develop analytical models and simulate the inelastic behavior of structures experiencing the effects of an earthquake (Mckenna, 2011; Yu et al., 2018). A two-dimensional model was used for the case RC frames owing to the limited torsional effects. Beams and columns were modeled using nonlinear force-based beam-column elements, with plasticity concentrating over a specified hinge length at element ends (Scott and Fenves, 2006). In the plastic concentrating regions, the fiber-type sections were used and discretized into fibers as reinforcement bars and confined (core) and unconfined (cover) concrete. The fiber section did not consider the shear-critical failure model of RC elements (Ning et al., 2019). For unconfined concrete, its inelastic behavior was represented by a nonlinear constitutive model with degraded linear unloading/reloading stiffness, and tensile strength is not given (Kent and Park, 1971). Regarding confined concrete, the model proposed by Mander et al. (1988) was used to account for the confinement effect offered by the stirrup. The reinforcement bars were represented by a uniaxial tri-linear hysteretic material model with a pinching effect and degradation of stiffness and strength due to damage. Aside from the above, a zerolength element was defined at the ends of columns and

Table 1 Structul	Table 1 Structural designs and the varying design variables						
Building group	Number	Story number	Bay width	Axial force ratio	Period reduction factor		
Varying of story number	S61	6	7.2	0.79	0.70		
	S62	6	7.2	0.73	0.70		
	S63	6	7.2	0.73	0.70		
	S64	6	7.2	0.64	0.70		
	S65	6	7.2	0.41	0.85		
	S91	9	7.2	0.75	0.70		
	S92	9	7.2	0.65	0.70		
	S93	9	7.2	0.65	0.70		
	S94	9	7.2	0.59	0.70		
	S95	9	7.2	0.47	0.85		
Varying of bay width	SA62	6	8.4	0.76	0.70		
	SA92	9	8.4	0.64	0.70		
	SR62	6	6.0	0.71	0.70		
	SR92	9	6.0	0.62	0.70		
Varying of axial force ratio	SW62	6	7.2	0.84	0.70		
	SW92	9	7.2	0.75	0.70		
	SS62	6	7.2	0.63	0.70		
	SS92	9	7.2	0.56	0.70		
Varying of the period reduction factor	SP65	6	7.2	0.37	0.70		
	SP95	9	7.2	0.50	0.70		

 Table 1
 Structural designs and the varying design variables



Fig. 1 Plan and elevation views of case RC frames (unit: mm)

beams between two nodes at the same location. A single fiber section was used to represent the force-deformation relationship for the zero-length element. Unlike the fiber section outside the zero-length element, the fiber section in the zero-length element adopted a uniaxial material model for reinforcement bars by considering bond-slip due to strain penetration (Zhao and Sritharan, 2007). Figure 3 summarizes the overall structural modeling details.

Due to the limitation of experimental conditions,

Columns Pooms												
Frames	Story	Bay	Geometry	Longitud	inal reinf	orcement	Transverse	Geometry	Longitudin	al reinford	rement	Transverse
1 funites	number	width	size	Part A	Part B	Part C	reinforcement	size	Part D	Part E	Part F	reinforcement
S61	6	7.2	600×600	4×18	4×18	4×18	8@100/200	300×600	4×25	4×22	4×12	8@100/200
S62	6	7.2	600×650	4×18	4×18	6×18	8@100/200	300×600	4×25	4×22	4×12	8@100/200
S63	6	7.2	600×650	5×18	5×18	6×18	8@100/200	300×600	$2 \times 25 + 2 \times 22$	4×22	4×12	8@100/200
200	Ū	,	000 000	0 10	0 10	0 10	001001200	200 000	/2.×2.2			00100.200
S64	6	72	600×650	6×25	6×25	8×25	8@100	300×700	4×22/	2×25+	4×12	8@100/150
501	Ū	,	000 020	0 23	0 20	0 20	000100	500 700	4×22	2×22	1 12	000100/100
\$65	6	72	Story 1-2.	9×25	9×25	14×25	8@100/150	400×700	6×22/	$4 \times 25 +$	4×12	8@100/200
505	0	/.2	750×750	<i>)</i> ~23	J. 23	11-20	0@100/150	100**700	5×22	1×22	112	000100/200
			Story 3_6:						5722	1722		
			$700 \times 700$									
S01	0	7 2	/00×/00	5~10	5~10	6~10	10@100/200	200~600	4~22/	2~25	4~12	8@100/200
591	9	1.2	030~030	3~18	3~18	0^18	10@100/200	300^000	4^22/	3~23	4^12	8@100/200
503	0	7.2	C4 1 -	6,10	6,10	0,10	10@100/150	200,400	2~22 4×22/	2.25	4,12	8@100/200
592	9	1.2	Story 1:	0×18	0×18	8×18	10@100/150	300×600	4×22/	3×23	4×12	8@100/200
			/00×/00						2×22			
			Story 2-9:									
~~~	0		650×650	- 10	- 10	0.10	400400/4 =0					0.0100/1.50
\$93	9	7.2	Story 1:	7×18	7×18	8×18	10@100/150	300×600	4×22/	4×22	4×12	8@100/150
			700×700						4×22			
			Story 2-9:									
			650×650									
S94	9	7.2	Story 1:	8×25	8×25	10×25	10@100/200	400×700	6×22/	5×22	4×12	10@100/200
			700×700						3×22			
			Story 2-9:									
			650×650									
S95	9	7.2	Story 1-3:	11×25	11×25	16×25	10@100/200	400×750	6×22/	2×25+	4×14	10@100/200
			850×850						5×22	4×22		
			Story 4-6:									
			750×750									
			Story 7-9:									
			650×650									
SA62	6	8.4	650×650	5×18	5×18	6×18	8@100/200	300×700	4×22/	2×22/	4×12	8@100/150
							0		4×22	5×22		0
SA92	9	8.4	Story 1-2:	7×18	7×18	10×18	10@100	300×700	4×25/	4×25	4×12	8@100/200
			800×800				U		2×22			0
			Story 3-9:									
			700×700									
SR62	6	6	500×550	4×18	4×18	4×18	8@100/200	300×500	4×22	3×22	4×12	8@100/200
SR92	9	6	600×600	5×18	5×18	6×18	10@100/150	300×500	4×25	3×22	4×12	8@100/200
SW62	6	7.2	500×500	4×18	4×18	4×18	8@100/200	300×600	2×22+2×25	3×25	4×12	8@100/200
SW92	9	7.2	650×650	5×18	5×18	6×18	10@100/150	300×600	4×22/	3×25	4×12	8@100/200
							Q		2×22			0
SS62	6	7.2	600×650	4×18	4×18	4×18	8@100/200	300×600	4×25	4×22	4×12	8@100/200
SS92	9	7.2	Story 1:	6×18	6×18	8×18	10@100/150	300×600	4×22/	3×25	4×12	8@100/200
			700×700				0		2×22			0
			Story 2-9:									
			650×650									
SP65	6	7.2	Story 1-2:	10×25/	10×25/	16×25	10@100	400×800	6×22/	5×25+	6×12	8@100/200
51 00	Ū	,	750×750	4×25	4×25	10 20	1000100	100 000	6×22	2×22	0 12	001001200
			Story 3-6	. 20	. 20				~			
			$700 \times 700$									
SP05	0	72	Story 1-3.	11×25+	20×25	$11 \times 25 +$	10@100	400×800	6×22/	4×25+	6×12	10@100/200
51 75	)	1.2	850×850	5×25	20~23	5×25	10/0/100	100/000	6×22/	3×22	0.12	10/0/200
			Stor 1 4	5~25		5~25			0~22	3~22		
			510Fy 4-0:									
			/ 30×/30									
			Story /-9:									
			630×650									

 Table 2 Geometry sizes and reinforcement details of the case RC frames

Note: Longitudinal reinforcement is represented by the number of reinforcing bars times the corresponding diameter (mm). For example, 4×18 means 4 bars with a diameter of 18 mm. Two layers of longitudinal reinforcing bars are represented by the first reinforcement layer/the second reinforcement layer. For example, 4×22/2×22 means the first reinforcement layer has 4 bars with a diameter of 22 mm, and the second reinforcement layer has 2 bars with a diameter of 22 mm. The transverse reinforcement is arranged in a smaller spacing at the plastic hinge areas of columns and beams, while it is arranged with a larger spacing outside the plastic hinge areas.

experimental studies have rarely been conducted to investigate the seismic performance of corroded RC frames. Therefore, the modeling strategy used in this study is validated through simulating the hysteretic behaviors of two corroded column specimens that were tested by Dai et al. (2020b). The details of the tests are not provided herein but may be referred to elsewhere (Dai *et al.*, 2020b). The two test specimens are designed with the same geometric size and reinforcement details. They are labeled C-E5-0.1, and C-E10-0.1 (Dai et al., 2020b), corresponding to the low to medium corrosion rates of reinforcement of 5% and 10%, respectively. Figure 4 compares the simulated and experimental data for the three specimens. It is clear that the adopted structural modeling strategy effectively simulates the test data of uncorroded and corroded columns, showing the reliability of the adopted structural model. A reliable structural model is beneficial for the following assessment of seismic resilience for corroded RC frames.

# 2.3 Modelling consideration for reinforcement corrosion

In this study, reinforcement corrosion caused by the penetration of chloride ions was considered, which can lead to four types of deterioration mechanisms, including

Distributed

Concentrated

1) the loss of a longitudinal reinforcement section, 2) the reduction of reinforcement strength and ductility, 3) the degradation of compressive strength of concrete cover, and 4) the deterioration of bond-slip performance. Table 3 summarizes the mathematical models adopted to represent the above-stated deterioration mechanisms due to reinforcement corrosion. The mathematical modeling details of the first three deterioration mechanisms can be found in Yu *et al.* (2017a). With regard to bond-slip deterioration, a reduction ratio  $R_c$  of the bond strength  $\tau_{c,orr}$  at any corrosion level to the original bond strength  $\tau_{c,0}$  is used herein according to Chung *et al.* (2004), which is expressed by

$$R_{\rm c} = \frac{\tau_{\rm c,corr}}{\tau_{\rm c,0}} \tag{1}$$

In this study, the empirical equations proposed by Xu (2003) are used to relate  $R_c$  to the corrosion rate  $\eta_s$ , as

$$R_{\rm c} = 1 + 0.5625\eta_{\rm s} - 0.3375\eta_{\rm s}^2 + 0.055625\eta_{\rm s}^3 - 0.003\eta_{\rm s}^4$$
  
for  $0 < \eta_{\rm s} < 7\%$  (2)

$$R_{\rm c} = 2.0786 \eta_{\rm s}^{-1.0369} \quad \text{for} \ 7\% < \eta_{\rm s} \tag{3}$$



Fig. 2 Typical reinforcement details of the columns and beams



Fig. 3 Illustration of the structural modeling strategy

# **3** Seismic fragility assessment of RC frames under corrosion

### 3.1 Seismic fragility function

Seismic fragility is described by the probability of structural demand reaching or exceeding stipulated limit

states (LSs) as a function of a ground motion intensity measure. The seismic fragility function is termed  $f_{LS}(S_a = x)$ , where spectral acceleration,  $S_a$ , in the fundamental period of a structure with a 5% damping ratio was adopted to represent the intensity of ground motion acceleration. A widely accepted lognormal distribution function was adopted herein for fragility assessment (Wen *et al.*, 2004), which is expressed by



Fig. 4 Simulated and tested hysteretic curves for Specimens C-E5-0.1 and C-E10-0.1 in Dai et al. (2020b)

Table 3	Mathematical models	dented to represent	t deterioration ma	hanisms due to	aannosian
Table 5	Wrathematical models	adopted to represent	t deterioration med	chamsms due to	corrosion

Deterioration mechanisms	Numerical models	Important parameters	Reference
Loss of longitudinal reinforcement section	$A_{\rm s}'=\frac{\pi D^2}{4}(1-\eta_{\rm s})$	$A'_{s}$ : cross-section area of the corroded reinforcing bars; D: diameter of the uncorroded reinforcement.	Ghosh and Padgett (2010)
Reduction of reinforcement strength	$f'_{y} = (1 - 0.5 \times \eta_{s}) \times f_{y}$ $f'_{u} = (1 - 0.5 \times \eta_{s}) \times f_{u}$	$f'_{y}$ and $f_{y}$ : yield strengths of the corroded and uncorroded reinforcing bars, respectively; $f'_{u}$ and $f_{u}$ : ultimate strength of the corroded and uncorroded reinforcing bars, respectively.	Du (2005)
Reduction of reinforcement ductility	$\varepsilon'_{\mathrm{u}} = (1 - 3 \times \eta_{\mathrm{s}}) \times \varepsilon_{\mathrm{u}}$	$\varepsilon'_{u}$ and $\varepsilon_{u}$ : ultimate elongation of the corroded and uncorroded reinforcing bars, respectively.	Cairns (2005)
Degradation of compressive strength of concrete cover	$f_{\rm c}' = \frac{f_{\rm c}}{1 + K\varepsilon_1 / \varepsilon_{\rm c0}}$ $\varepsilon_1 = (b_{\rm f} - b_0) / b_0$ $b_{\rm f} - b_0 = n_{\rm c} \times \omega_{\rm cr}$ $\omega_{\rm cr} = 2\pi (v_{\rm rs} - 1) X$	$f'_{e}$ and $f'_{e}$ : compressive strengths of concreter cover after and before cracking led by reinforcement corrosion; K: coefficient related to reinforcement roughness and diameter, where $K = 0.1$ is taken herein for medium- diameter ribbed reinforcement; $\varepsilon_{e0}$ : strain at the peak compressive stress of concrete cover; $\varepsilon_{1}$ : average tensile strain of the cracked concrete; $b_{0}$ and $b_{r}$ : cross-section widths of the concrete cover before and after cracking, respectively; $n_{e}$ : number of reinforcements in the compression area; $\omega_{cr}$ : width of concrete cracking; $v_{rs}$ is the volume expansion ratio of corrosion products; X: depth of the corrosion attack equal to the reduction of in reinforcement radius.	Coronelli and Gambarova (2004)
Reduction of bond-slip		Eqs. (1)–(3)	Chung <i>et al.</i> (2004); Xu (2003)

$$f_{LS}\left(S_{a}=x\right) = P\left(LS \mid S_{a}\right) =$$

$$1 - \varPhi\left(\frac{\ln m_{C} - \ln m_{D \mid S_{a}}}{\sqrt{\beta_{C}^{2} + \beta_{D \mid S_{a}}^{2} + \beta_{M}^{2}}}\right) = \varPhi\left(\frac{\ln m_{C} - \ln m_{D \mid S_{a}}}{\sqrt{\beta_{C}^{2} + \beta_{D \mid S_{a}}^{2} + \beta_{M}^{2}}}\right)$$

$$(4)$$

where  $P(LS | S_a)$  denotes the exceeding probability of a predefined LS conditioned on  $S_a = x$ ;  $\phi(\cdot)$  represents the standard normal probability integral;  $m_{D|S_a}$  and  $\beta_{D|S_a}$ are median and the standard deviation of the natural logarithm of the structural demand D on the condition of  $S_a = x$ , respectively; and  $m_c$  and  $\beta_c$  are median and the standard deviation of the natural logarithm of limit state capacity C, respectively; and  $\beta_{\rm M}$  is used to denote uncertainty due to the imperfection of analytical modeling. The value of  $\beta_{\rm M}$  is taken as 0.2 based on the assumption that the modeling process yields a response that is within  $\pm 30\%$  of the actual value, with 90% confidence (Wen *et al.*, 2004).

For the seismic demand parameters, i.e.,  $m_{D|S_a}$  and  $\beta_{D|S_a}$ , they are quantified from the statistics of the inelastic structural response under earthquakes. The maximum drift ratio,  $\theta_{\max}$ , is taken herein as the engineering demand parameter to quantify D and C. A cloud method is used to generate a linear relationship between  $\theta_{\max}$  and  $S_a$  at a log-log space, yielding (Shome *et al.*, 1998; Miano *et al.*, 2018)

$$\ln m_{D|S_a} = a + b \ln S_a \tag{5}$$

$$\beta_{D|S_a} = \sqrt{\frac{\sum_{i=1}^{N} \left( \ln D_i - \ln m_{D|S_a} \right)}{N-2}} \tag{6}$$

where a and b are coefficients determined by regression; N is the number of input ground motion records; and  $D_i$  is the drift response caused by the *i*th ground motion record.

Three limit states expressed as immediate occupancy (IO), life safety (LS), and collapse prevention (CP) are considered herein. Their median drift capacities  $m_C$  are defined as  $\theta_{max} = 1\%$ , 2% and 4%, respectively (FEMA 273, 1997). Similar definitions have also been adopted in other studies (Ramamoorthy *et al.*, 2006; Ellingwood *et al.*, 2007; Howary and Mehanny, 2011) to quantify  $m_C$ . According to Wen *et al.* (2004), the variation in drift capacities is assumed to be  $\beta_C = 0.3$  for all limit states, a figure also used in Ramamoorthy *et al.* (2006) and Hueste and Bai (2007).

Substituting Eq. (5) into Eq. (4), the five-parameter fragility function shown in Eq. (4) can be transformed into a function with only two parameters, yielding (Lu *et al.*, 2014; Yu *et al.*, 2017b)

$$f_{LS}\left(S_{a}=x\right) = \boldsymbol{\Phi}\left[\frac{\ln m_{D|IM} - \ln m_{C}}{\sqrt{\beta_{D|IM}^{2} + \beta_{C}^{2} + \beta_{M}^{2}}}\right] = \boldsymbol{\Phi}\left[\frac{a+b\ln S_{a} - \ln m_{C}}{\sqrt{\beta_{D|IM}^{2} + \beta_{C}^{2} + \beta_{M}^{2}}}\right] = \boldsymbol{\Phi}\left[\frac{\ln\left(S_{a} / m_{R}\right)}{\beta_{R}}\right]$$
(7)

where  $m_{\rm R}$  denotes the fragility median corresponding to a failure probability of 50%, and  $\beta_{\rm R}$  denotes fragility dispersion, showing the total variation of fragility. The values of  $m_{\rm R}$  and  $\beta_{\rm R}$  can be calculated by the following equations, respectively, as

$$m_{\rm R} = \left[ m_C / \exp(a) \right]^{1/b} \tag{8}$$

$$\beta_{\rm R} = \frac{1}{b} \sqrt{\beta_{D|IM}^2 + \beta_C^2 + \beta_{\rm M}^2}$$
(9)

Figure 5 shows the effect of  $m_{\rm R}$  and  $\beta_{\rm R}$  on the shape of a fragility curve. It was found that  $m_{\rm R}$  dominates the global location of the fragility curve and its variation can lead to a global shift in the curve. The value of  $\beta_{\rm R}$  controls the slope of the fragility curve. The fragility curve is growing steeply when  $\beta_{\rm R}$  is decreased. The transformed fragility function in Eq. (7) was used to extract the effect of reinforcement corrosion in the following sections.

#### 3.2 Ground motion records

A total of 100 ground motion records was selected from the PEER Ground Motion Database (Ancheta *et al.*, 2013). The detailed information in these ground motion records can be found in Lu *et al.* (2014) and Yu *et al.* (2017b). Figure 6 shows the distribution of the selected ground motions in the space of earthquake magnitude  $(M_w)$  and distance (*R*). It is clear that the selected ground motions cover a wide  $M_w$ –*R* range. In a region with a low



Fig. 5 Effect of  $m_{\rm R}$  and  $\beta_{\rm R}$  on a fragility curve

 $M_{\rm w}$  and a small *R*, the largest number of ground motion records was selected since it is the most unfavorable measure among the four that were considered four  $M_{\rm w}$ -*R* regions. As for the  $M_{\rm w}$ -*R* region with a small  $M_{\rm w}$  and a large *R*, the fewest ground motion records were selected due to their insignificant damage potential for structures. The directivity pulse-type effects of near-fault ground motions were not considered and the *R* values of the selected ground motion records are greater than 10 km. Besides, all the ground motions were recorded on NEHRP soil types C or D (stiff soil or soft rock) sites. These soil types are similar to the soil condition found at the target building site.

#### 3.3 Fragility curves of corroded RC frames

Three corrosion rates of reinforcing bars,  $\eta_s = 5\%$ , 10% and 15%, were considered in i.e., correspondence to the low, medium, and high corrosion levels of structures, respectively. The intact frames without corroded reinforcement were also examined for comparison. A total of  $4 \times 20 = 80$  frame cases were considered to develop their fragility curves. The numerical models for the corroded RC frames were developed according to Section 2.2 by considering deterioration mechanisms due to reinforcement corrosion (see Section 2.3). The uncorroded and corroded RC frames were subjected to 100 selected ground motion records. Through nonlinear time-history analyses, the structural responses in terms of  $\theta_{\max}$  were obtained. Next, the seismic demand model parameters, i.e.,  $m_{D|S_a}$  and  $\beta_{D|S_a}$ , were calculated through regressions between  $\ln S_a$  and  $\ln m_{D|S_a}$  (see Eq. (5) and Eq. (6)). The seismic demand parameters  $(m_{D|S_a} \text{ and } \beta_{D|S_a})$ and the limit state capacity parameters  $(m_c \text{ and } \beta_c)$ were substituted into Eq. (4). Finally, the seismic fragility curves of corroded and uncorroded RC frames were generated. At a given limit state, the fragility curves of the uncorroded and corroded structures were compared to investigate the effect of reinforcement corrosion on seismic performance.



Fig. 6 Distribution of the selected ground motion records in  $M_{w}$ -R bins

The frame labeled S61 was taken alone as an example for illustration. Figure 7 shows the fragility curves of this structure, subjected to different levels of corrosion. It was observed that the difference of fragility curves corresponding to the cases with  $\eta_s = 10\%$  and  $\eta_s = 15\%$  are limited compared to those corresponding to the cases with  $\eta_s = 5\%$  and  $\eta_s = 10\%$ , as well as the cases with uncorroded reinforcement and  $\eta_c = 5\%$ . In particular, at the IO limit state, the fragility curves of the corroded structures with  $\eta_s = 10\%$  and  $\eta_s = 15\%$  are almost identical to each other. Besides that, the fragility curves of the uncorroded structures are significantly different from those of the slightly corroded structure with  $\eta_{\rm c} = 5\%$ . This phenomenon was also observed in Afsar et al. (2018), which shows that the occurrence of reinforcement corrosion leads to a clear reduction of structural performance. Besides, at the CP limit state, there is an intersection between the fragility curve of the uncorroded structure and that of the corroded structure with  $\eta_{c} = 5\%$  since reinforcement corrosion leads to a clear effect on fragility dispersion  $\beta_{\rm R}$  ( $\beta_{\rm R}$  controls the slope of the fragility curve, as shown in Fig. 5). It is noteworthy that the effect of the corrosion rate on fragility is complex since it is related to the numerical modeling approach of uncorroded and corroded structures, in addition to the adopted mathematical models of deterioration mechanisms due to reinforcement corrosion. Therefore, there is a considerable model error in the evaluation of fragility for corroded structures.

# 3.4 Effect of reinforcement corrosion on fragility parameters

The effect of reinforcement corrosion on the fragility median  $m_{\rm R}$  and dispersion  $\beta_{\rm R}$  is examined in this section. A ratio  $\alpha_m$  between the fragility median for the corroded frame and that of the intact frame is defined, which is expressed by

$$\alpha_m = \frac{m_{\rm R, \, corr}}{m_{\rm R, \, int}} \tag{10}$$

where  $m_{R, corr}$  and  $m_{R, int}$  denote the fragility medians for the corroded and uncorroded frames, respectively.

Figure 8 shows the relationship between  $\alpha_m$  and  $\eta_{s^3}$ which was generated using the analysis data for the S61 frame at the IO limit state. An exponent-form function was used to represent the changing law of  $\alpha_m$  on  $\eta_{s^3}$  as

$$\alpha_m = A e^{\left(-B\eta_s\right)} + \left(1 - A\right) \tag{11}$$

where A and B are the coefficients determined through regression.

Table 4 shows the obtained A and B values for different RC frame cases and the corresponding coefficient of determination  $R^2$ . It is clear that Eq. (10)







Fig. 8 Regressed relationship between  $\alpha_m$  and  $\eta_s$ 

can well fit the relationship between  $\alpha_m$  and  $\eta_s$ . To summarize the results in Table 4, the *A* and *B* values corresponding to different limit states are recommended to be in the scopes listed in Table 5. Figure 9 shows the obtained  $\beta_R$  values for different case frames at the limit states of IO, LS, and CP. Nevertheless, no clear trend was observed between  $\beta_R$  and  $\eta_s$ . Therefore, the median values of  $\beta_R$  corresponding to different limit states and different corrosion levels are calculated in Table 6.

#### 4 Seismic resilience of corroded RC frames

#### 4.1 The loss factor of resilience

The normalized loss factor of resilience,  $L_{\rm R}$ , proposed by Wen *et al.* (2019) was adopted herein to measure the resilience of structures subjected to the effects of earthquakes, which is expressed by

$$R_{\text{Loss}} = \frac{1}{\left[\mathcal{Q}\left(t < t_0\right)\right] \cdot \left(t_1 - t_0\right)} \int_{t_0}^{t_1} \left[\mathcal{Q}\left(t < t_0\right) - \mathcal{Q}\left(t\right)\right] \mathrm{d}t$$
(12)



Fig. 9  $\beta_R$  values for different case frames at the limit states of IO, LS, and CP

where Q(t) is the functionality of the structure, with its value varying from 0 to 1.0;  $t_0$  is the time at which an earthquake occurs; and  $t_1$  denotes the time at which structural functionality is recovered to target functionality  $Q_{\text{target}}$  at the end of the recovery process. It is noteworthy that  $Q_{\text{target}}$  should not be less than  $Q(t < t_0)$  (i.e.,  $Q_{\text{target}} \ge Q(t < t_0)$ ). Moreover,  $Q(t < t_0)$  is less than 1.0 for aging structures due to functionality degradation. Figure 10 illustrates the concept of the loss factor of resilience defined by Eq. (11).

As noted by Cimellaro *et al.* (2010), Q(t) is a function related to earthquake intensity, economic loss,

	0					· · · · · ·	<i>,</i>			
		IO			LS			СР		
Frame	A	В	$R^2$	A	В	$R^2$	A	В	$R^2$	
S61	0.32	0.2	0.99	0.35	0.25	0.99	0.26	0.12	0.75	
S62	0.30	0.25	0.98	0.3	0.12	0.95	0.19	0.20	0.99	
S63	0.29	0.09	0.95	0.31	0.16	0.99	0.4	0.11	0.99	
S64	0.25	0.08	0.95	0.5	0.05	0.99	0.36	0.09	0.99	
S65	0.29	0.19	0.95	0.41	0.07	0.99	0.31	0.30	0.71	
S91	0.20	0.08	0.98	0.24	0.13	0.97	0.19	0.09	0.83	
S92	0.42	0.05	0.83	0.42	0.08	0.95	0.17	0.07	0.92	
S93	0.38	0.24	0.99	0.34	0.15	0.96	0.25	0.07	0.95	
S94	0.34	0.09	0.99	0.31	0.12	0.99	0.43	0.07	0.99	
S95	0.32	0.15	0.99	0.34	0.15	0.98	0.38	0.10	0.94	
SA62	0.40	0.2	0.99	0.26	0.10	0.85	1.67	0.01	0.99	
SA92	0.34	0.04	0.99	0.28	0.10	0.88	0.32	0.04	0.91	
SR62	0.35	0.05	0.98	0.21	0.23	0.99	0.16	0.21	0.98	
SR92	0.41	0.06	0.95	0.36	0.11	0.99	0.41	0.03	0.98	
SW62	1.36	0.03	0.93	0.35	0.04	0.97	0.24	0.06	0.97	
SW92	0.27	0.11	0.99	0.22	0.19	1.00	0.66	0.02	0.95	
SS62	0.32	0.25	0.97	0.38	0.07	0.95	0.39	0.07	0.89	
SS92	0.28	0.21	0.99	0.26	0.29	0.96	0.67	0.02	0.88	
SP65	0.83	0.03	0.97	0.48	0.09	0.98	0.55	0.17	0.99	
SP95	0.39	0.09	0.96	0.48	0.19	0.99	0.53	0.24	0.95	

Table 4 Regressed coefficients A and B for different frames at IO, LS, and CP limit states

 Table 5 Ranges of the coefficients A and B at IO, LS, and CP limit states

Coefficients	ΙΟ	LS	СР
A	(0.25, 0.45)	(0.20, 0.50)	(0.15, 0.55)
В	(0.05, 0.25)	(0.05, 0.25)	(0.05, 0.25)

Table 6 Mean value of  $\beta_{\rm R}$  for limit states of IO, LS, and CP

	IO	LS	СР
Uncorroded	0.38	0.39	0.37
$\eta_{\rm s} = 5\%$	0.40	0.41	0.37
$\eta_{s} = 10\%$	0.40	0.40	0.38
$\eta_{\rm s} = 15\%$	0.38	0.41	0.37

and recovery function, associated with recovery time and recovery path. In this study, functionality Q(t) is defined by

$$Q(t) = Q(t < t_0) - L(S_a, T_r) \times [H(t - t_0) - H(t - t_1)] \times f_{rec}(t, t_0, T_r)$$
(13)

where  $T_r$  is the recovery time, determined by  $t_1 - t_0$ ;

 $L(S_a, T_r)$  is the loss function; H(t) is the Heaviside step function;  $f_{rec}(t, t_0, T_r)$  is the recovery function.

There are commonly three types of recovery functions, including the linear, exponential function and trigonometric (Cimellaro *et al.*, 2010). In this study, a linear functionality Q(t) was adopted herein as a preliminary trial, which is expressed by

$$f_{\rm rec}\left(t, T_{\rm r}\right) = \left(1 - \frac{t - t_0}{T_{\rm r}}\right) \tag{14}$$

#### 4.2 Seismic loss estimation

The seismic loss of structures can be generally categorized into direct and indirect varieties. For the purpose of simplicity, only direct loss was considered herein. However, the current study can be extended by including indirect loss. The direct loss of the aging frames due to earthquakes is computed by

$$L = \sum_{i=1}^{4} R_{DS_i} \times P(DS_i \mid S_a)$$
(15)

where  $R_{DS_i}$  is the loss ratio of the damaged structure in the *i*th damage state, i.e.,  $DS_i$ ;  $P(DS_i | S_a)$  is the failure probability of the structure at  $DS_i$ , which can be determined by the difference of failure probabilities of adjacent limit states, yielding

$$P(DS_i|S_a) = \begin{cases} P(LS_{i+1}|S_a) - P(LS_i|S_a) & i < 4\\ P(LS_4|S_a) & i = 4 \end{cases}$$
(16)

where the failure probabilities of  $P(LS_{i+1}|S_a)$  and  $P(LS_i | S_a)$  are determined from the fragility curves listed in Section 3.

Three limit states in terms of IO, LS, and CP divide structural performance into four states of damage, i.e.,  $DS_i$  (i = 1, 2, 3, 4) The loss ratio  $R_{DS_i}$  is determined between the direct loss and the replacement cost. Table 7 provides the  $R_{DS_i}$  values corresponding to  $DS_i$  (i = 1, 2, 3, 4), where  $R_{DS_i} = 10\%$ , 40%, 70%, 100% are defined to relate to  $DS_i$  (i = 1, 2, 3, 4), respectively.

#### 4.3 Seismic resilience assessment

Substituting Eq. (14) and Eq. (15) into Eq. (13), the values of  $R_{\text{Loss}}$  can be calculated by Eq. (12). Figure 11 shows the calculated  $R_{\text{Loss}}$  values of uncorroded and corroded frames, where the replacement treatment is adopted once the predefined replacement threshold is exceeded. In this study, the replacement threshold was determined once the repair cost exceeded 45% (Wen *et al.*, 2019). The replacement cost is defined by the initial cost times a factor of 1.25. Therefore, when the direct loss ratio reached beyond  $1.25 \times 45\% = 56\%$ , the repair of a structure is not necessary; rather, a replacement is required. As seen in Fig. 11, the calculated  $R_{\text{Loss}}$  values of the corroded frames are clearly greater than that of their uncorroded counterparts. Moreover, with growing corrosion levels, the corresponding  $R_{\text{Loss}}$  values are accordingly increased. The above observations show that reinforcement corrosion can lead to a promotion of the loss of resilience. To illustrate this promotion,



Fig. 10 Conceptual illustration for the loss factor of resilience

Table 7 Direct loss ratio considered in this study

$\theta_{_{ m max}}$	Damage state	Direct loss ratio
0–1%	$DS_1$	10%
1%-2%	$DS_2$	40%
2%-4%	$DS_3$	70%
>4%	$DS_4$	100%



Fig. 11 Calculated loss factors of resilience for the case RC frames

D '11'		$R_{\rm loss}$ (×10 <sup>-4</sup> ) conditioned on RE				
Building	$S_a$ values at RE	Uncorroded	$\eta_s = 5\%$	$\eta_{s} = 10\%$	$\eta_{s} = 15\%$	
S61	0.1	1.48	18.26 (>200%)↑	51.57 (>200%)↑	52.33 (>200%)↑	
S62	0.2	292.78	744.59 (154.3%)↑	1001.04 (>200%)↑	927.62 (>200%)↑	
S63	0.3	913.06	1247.92 (36.7%)↑	1493.72 (63.6%)↑	1996.49 (118.6%)↑	
S64	0.4	1919.8	1451.15 (-24.4%)↓	1584.82 (-17.4%)↓	2098.93 (9.32%)↑	
S65	0.6	1435.86	2062.06 (43.6%)↑	2352.32 (63.8%)↑	2865.15 (99.5%)↑	
S91	0.1	42.25	130.48 (>200%)↑	169.38 (>200%)↑	196.19 (>200%)↑	
S92	0.2	1069.42	1112.28 (4.02%)↑	1701.95 (59.2%)↑	1760.55 (64.7%)↑	
S93	0.3	1821.46	2124.23 (16.6%)↑	2368.35 (30%)↑	2523.54 (38.6%)↑	
S94	0.4	2086.68	2617.3 (25.4%)↑	2514.24 (20.5%)↑	2819.59 (35.1%)↑	
S95	0.6	2165.56	2545.85 (17.5%)↑	2888.26 (33.3%)↑	3004.06 (38.7%)↑	
SA62	0.2	97.75	525.62 (>200%)↑	819.21 (>200%)↑	803.78 (>200%)↑	
SA92	0.2	770.91	866.86 (12.5%)↑	1025.11 (32.9%)↑	1270.58 (64.9%)↑	
SR62	0.2	811.01	275.79 (-66%)↓	1260.9 (55.5%)↑	1433.2 (76.7%)↑	
SR92	0.2	860.87	1334.94 (55.1%)↑	1559.04 (81.1%)↑	1797.12 (108.7%)↑	
SW62	0.6	156.14	130.37 (-16.7%)↓	1756.34 (>200%)↑	1960.16 (>200%)↑	
SW92	0.2	1199.81	1573.02 (31.1%)↑	1762.11 (46.8%)↑	1684.11 (40.3%)↑	
SS62	0.2	296.29	784.25 (164.9%)↑	615.62 (108.1%)↑	975.25 (>200%)↑	
SS92	0.2	888.3	1557.05 (75.3%)↑	1666.24 (87.6%)↑	1818.72 (104.8%)↑	
SP65	0.2	1098.3	1568.64 (42.9%)↑	2168.79 (97.5%)↑	2764.43 (151.7%)↑	
SP95	0.6	1895.28	3436.62 (81.4%)↑	3849.64 (103.2%)↑	3893.06 (105.4%)↑	

Table 8 Seismic resilience loss ratios conditioned on the RE hazard level

the  $R_{\text{Loss}}$  values conditioned on earthquake hazards at the rare earthquake (RE) were especially calculated for corroded and uncorroded RC frames, as shown in Table 8. It is noteworthy that the seismic performance of structures under three seismic hazards, i.e., frequent earthquake (FE), design basis earthquake (DBE), and RE, is concentrated in the Chinese seismic design code (GB50010-2010, 2010). At the FE and DBE hazard levels, the seismic damage to structures is commonly limited and therefore solely the RE hazard level was considered here for illustration. As seen from Table 8, reinforcement corrosion leads to significant growth of  $R_{\text{Loss}}$ . For the case frames, this growth can even exceed 200%, showing the huge effect of reinforcement corrosion on structural resilience.

# **5** Conclusions

This study conducted a comprehensive investigation on the seismic resilience of RC frame structures under corrosion. A total of twenty RC frames were designed according to Chinese seismic design codes for representing the typical construction in coastal China. In the structural designs, four important variables, the number of stories, bay width, axial loading ratio, and period reduction factor, were considered at low, medium, and high levels. A numerical finite element model was developed on the OpenSees platform to simulate the inelastic behaviors of corroded RC frames due to the effects of earthquakes, an approach verified by effectively simulating the cyclic loading test data of uncorroded and corroded RC columns. Reinforcement corrosion rates of 5%, 10%, and 15% were considered to represent low, medium, and high corrosion levels, respectively. The effect of reinforcement corrosion on structural performance was accounted for by degrading properties of reinforcement, concrete cover, and their bond-slip performance.

To quantify the seismic resilience of structures, a normalized loss factor of resilience was assessed for all the case frames by considering growing corrosion levels. As an important ingredient of resilience, the fragility relationships were first developed for the corroded and uncorroded case frames by considering three limit states: IO, CP, and LS. Compared to the uncorroded RC frame, the corroded frames showed larger failure probability at a specific limit state, illustrating the deterioration of the structural capacity due to the effects of earthquakes. Moreover, the effect of reinforcement corrosion on the corresponding fragility is limited at the IO limit state, whereas it is significant at the CP and LS limit states. It was found that the fragility medians of corroded RC frames were decreased with the corrosion rate of reinforcement. However, no clear trend was observed between fragility dispersions and corrosion rates.

The obtained loss of resilience for the corroded RC frames is significantly higher than that for their uncorroded counterparts. This reduction of resilience due to corrosion is aggregated with growing corrosion rates. At the Rare Earthquake hazard level, the corrosioninduced growth in the loss of resilience can even exceed 200%. This result reveals that reinforcement corrosion should not be neglected in the resilience assessment of structures. It is noteworthy that no clear trend was observed on the effect of the four important design variables that were considered-including the number of stories, bay width, axial loading ratio, and period reduction factor-on the fragility and resilience of corroded structures. This reflects the complexity of the effect of reinforcement corrosion on the seismic performance of RC structures. The above conclusions are limited to the cases in the current study. An additional study is being conducted to correlate structure-specific resilience with regional resilience, while incorporating the aging effect.

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