

# Maximizing the amount of data collected from WSN based on solar-powered UAV in urban environment

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#### Abstract

Unmanned Aerial Vehicle (UAV) plays an increasingly role in data collection from Wireless Sensor Networks (WSNs) with the advantages of its high mobility and flexibility. However, the energy limitation of UAV restricts its application for data collection tasks. To solve the problem, we install solar panel on UAV to acquire energy from sunlight. This paper studies Data Collection Maximization based on Solar-powered UAV (DCMS) problem in urban environment with lots of obstacles, where one UAV equipped with solar panel is used to collect data from WSN. The problem aims at optimizing the flight trajectory of UAV such that the amount of data collected from WSN is maximized. We prove that the problem is NP-hard. To solve the DCMS problem, we first propose three algorithms: Bypass Obstacles during Flight Algorithm (BOFA), Auxiliary Graph Flight Path (AGFP), Construct Flight Plan in data collection Area (CFPA). Their objectives are to bypass the obstacles, to obtain the flight path connecting all data collection areas in WSN, to optimize the flight trajectories of UAV in the data collection areas, respectively. Afterwards, we propose an approximation algorithm called DCMSA to solve the DCMS problem based on BOFA, AGFP, CFPA algorithms. Finally, the proposed algorithm is verified by extensive simulations.

Keywords Wireless Sensor Networks  $\cdot$  Solar-powered UAV  $\cdot$  Data collection  $\cdot$  Trajectory optimization

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# 1 Introduction

Wireless Sensor Networks(WSNs) are self-organizing, multi-hops distributed networks, where sensors are deployed in the detection area to sense the environment information (Luo et al. 2021b). They have a large of applications, such as environment monitoring, disaster monitoring, intelligent transportation and so on. In traditional WSNs, the data stored in the sensors are transmitted back to the base station through multi-hop routing, which depends on the battery energy carried by sensors. However, since WSNs produce a amount of data as they are widely used in production and life, the traditional way of collecting data will greatly consume the energy of WSNs and reduce their service life. To overcome the above shortcomings, that Unmanned Aerial Vehicles (UAVs) are used as data collectors to collect massive data in WSNs can not be restricted by various ground conditions with the advantages of fast flight speed, flexible flight routes and strong transportation capabilities.

Although UAVs have many advantages for data gathering in WSNs, their battery capacity limitation are considered as the crucial technical challenges for UAVs, and which may make them unable to complete the data collection tasks in many applications. In order to extend the working time of UAVs, many wireless charging technologies are applied to replenish energy for UAVs in much literature, such as solar charging (Thipyopas et al. 2019; Alsharoa et al. 2019), radio frequency (RF) technology (Li et al. 2017), laser charging technology (L. Company 2012; Lahmeri et al. 2020) and so on. However, since laser transmitters and RF chargers are needed to deploy at specific locations in advance, UAVs need to fly at these locations for replenishing energy, which will reduce the efficiency of UAVs and consume a large amount of electric energy. Solar power as nature source can replenish energy for UAVs without energy supply equipment and does not require additional energy and human and material resources. Therefore, in this paper, we consider to use solar power to replenish energy for UAVs when the UAVs are used to collect data from WSN.

However, since the charging efficiency of solar energy is low and the energy limitation initially carried by UAV, we can not gather all data from WSN with the given solar-powered UAV. Specifically, there are many obstacles to present obstructing the communication between the UAV and sensors in urban environment. Therefore, in this paper, we study the Data Collection Maximization based on Solar-powered UAV(DCMS) problem, where the solar-powered UAV is used to collect data from WSN deployed urban environment. In the problem, we not only consider the situation that solar power is used to supplement energy for UAV, but also consider to avoid obstacles when the UAV collects data from sensors during flight. The objective of the problem aims at optimizing the flight trajectory of the solar-powered UAV to maximize the amount of data from sensors in urban environment before the energy of the UAV is exhausted. The contribution of this paper can be summarized as below.

(1) We identify a data collection model of WSN based on solar-powered UAV by considering avoiding obstacles in urban environment, which is called Data Collection Maximization based on Solar-powered UAV(DCMS) problem. Then we prove the problem is NP-hard.

- (2) To solve the DCMS problem, we first prove that the optimal horizontal flight speed is a function with respect to the flight altitude to minimize the net energy consumption of UAV by considering solar charging. Then we propose three algorithms: Bypass Obstacles during Flight Algorithm(BOFA), Auxiliary Graph Flight Path (AGFP), Construct Flight Plan in data collection Area (CFPA) to bypass the obstacles, to obtain the flight path connecting all data collection areas in WSN, to optimize the flight trajectories of UAV in the data collection areas, respectively. Afterwards, we propose an approximation algorithm to solve the DCMS problem based on the above algorithms.
- (3) The extensive simulations are presented to illustrate the effectiveness of the proposed algorithm for the DCMS problem.

The remainder of this paper is organized as follows. Section 2 introduces related works. Section 3 introduces models and the problem definition. In Sect. 4, we propose an approximation algorithm to solve the DCMS problem. Simulations are shown in Sect. 5. Section 6 concludes this paper.

# 2 Related works

This section will introduce the relevant research status and put forward the differences of the problems studied in this paper. We classify the study problems into three different types: data collection based on UAV, researches on solar-powered UAV, obstacle avoidance of UAV.

## 2.1 Data collection based on UAV

In Gong et al. (2018), Gong et al. studied the time minimization problem of UAV by considering both flying and communication of UAV. However, they only investigated the scenario that the UAV collects data from the sensors on a stright line, which is rare in reality and has many limitations. In Liu et al. (2018), the authors designed the flight paths for single UAV and multiple UAVs to maximize the capacity of sensors, but they assumed that the flight paths are fixed. However, in the actual scenario, the UAVs with variable paths will play a higher efficiency in communication in the WSN. In Luo et al. (2020), Luo et al. investigated the maximizing data collection proportion problem to find the trajectory of UAV such that the minimum data collection proportion of collected data to the stored data among all sensors is maximized. In Luo et al. (2021a), Luo et al. designed detailed flight and hover plans for multiple UAVs for data gathering from the WSN. They minimized the maximum flight time of UAVs such that all data in the WSN is collected by the UAVs and transported to the base station. In Sun et al. (2022), Sun et al. presented a new solar-powered fixed-wing UAV-assisted data collection technique, where a fixed-wing UAV harvests solar energy to fly and collect data from smart devices. They optimized the UAV's three-dimensional trajectory to maxmize the minimum of the data upload-ed from any of the smart devices.

# 2.2 Researches on solar-powered UAV

In Kingry et al. (2018), Kingry et al. presented a prototype quadcopter UAV, which carries a PV cell array. And they reported that the UAV can stay airborne for one to 2 h by harvesting solar power. In Thipyopas et al. (2019), the authors developed a mall solar-powered Unmanned Aerial Vehicle for environmental monitoring application and aimed to achieve continuous flight endurance of 6 h. The results showed that hybrid solar powered UAV weight of 5.5 kg is predicted for 6-h non-stop flight operation from 9AM to 3PM under Thailand weather condition. In Fu et al. (2021), Fu et al. investigated a solar-powered Unmanned Aerial Vehicle system, where UAV collects data from Internet of Things Devices (IoTDs) on the ground and the three-dimensional trajectory is optimized to maximize the total residual energy of the UAV. In Cong et al. (2021), Cong et al. considered a general UAV-enabled wireless communication system, where the fixed-wing UAV with thin-film solar cells is deployed to provide continuous communication services for the ground users.

# 2.3 Obstacles avoidance of UAV

In Li et al. (2022), Li et al. proposed a dynamic obstacle avoidance path planning strategy for UAV. They optimized the obstacle avoidance effect of the UAV by by changing the UAV turning radius, changing the UAV heading, solving the UAV minimum deviation distance, reducing the UAV obstacle avoidance space. In Zhou et al. (2022), Zhou et al. proposed a trajectory planning scheme and realized the unity of obstacle avoidance and trajectory planning, where the UAV does not deviate from the route after obstacle avoidance, and returns to the scheduled route nearby.

It is clear from previous discussions that there are many researches on UAV-based data collection in WSN and solar-powered UAV and UAV flying in some environment with obstacles. However, few people consider data collection based on solar-powered UAV in WSN in urban environment with obstacles. Inspired by above literatures, in this paper, we study the the data collection maximization problem based on solar-powered UAV by considering obstacles in urban environment, in which we aim to maximize the data collection volume and enable the solar-powered UAV to return to the base station before it runs out of energy. We not only consider the obstacle avoidence method, but also optimize the trajectory of UAV for data gathering from WSN.

# 3 Models and definition

In this section, we give the models and definition for the problem.

# 3.1 Network model

In this paper, we consider a WSN deployed at urban environment where many obstacles are located in. For simplicity, we assume that *n* sensors and *m* obstacles with known location and size are deployed at a two-dimensional plane area  $\mathcal{A} \subseteq \Re^2$ . Let S =

 $\{s_1, s_2, \dots, s_n\}$  denote the set of sensors, where each sensor  $s_i \in S$  stores  $V_i$  units of data. We use  $O = \{o_1, o_2, \dots, o_m\}$  to denote the set of the *m* obstacles in which each obstacle is shaped as a cube. We use a solar-powered UAV *u* with source node  $s_0$ , initial energy *E*, vertical flight speed  $v_l$ , horizontal flying speed  $v_f$  and minimum flying altitude *H* to serve as a mobile collector for gathering data from sensors in WSN, where *E* is also the energy capacity of UAV.

We use  $(x_i^s, y_i^s)$  to represent the coordinates for any  $s_i \in S \cup \{s_0\}$ . For arbitrary  $o_j \in O$ , let  $p_j^o = (x_j^o, y_j^o, z_j^o)$  denote its centre point and  $(l_j^o, w_j^o, h_j^o)$  represent the size of  $o_j$ , where  $l_j^o$  represents the length of  $o_j$ ,  $w_j^o$  denotes the width of  $o_j$  and  $h_j^o$  is the height of  $o_j$ . As we all known, the UAV can't fly close to the boundary of the obstacle. Therefore, we set a fixed buffer distance  $d_j^o$  between UAV and  $o_j$  when the UAV meets any  $o_j \in O$ .

Assume that all sensors have the same communication radius R. For any  $s_i \in S$ , we let  $\Omega(s_i)$  denote the communication area of  $s_i$ . The sensor  $s_i$  can transmit data to UAV if and only if the UAV is in  $\Omega(s_i)$ . The data collection area of UAV is a circular area  $C(s'_i)$  whose radius and center are respectively  $R_c = \sqrt{R^2 - H^2}$  and  $s'_i$  when u flies at the altitude H. Let  $C = \{C(s'_1), C(s'_2), \dots, C(s'_n)\}$ . The UAV can collect data from sensors if and only if there does not exist obstacle between them. If  $H \le h_j^o + d_j^o$ , then the UAV must bypass  $o_j$  from other three directions: right side, left side and upward side. For simplicity, we assume that the UAV only can fly horizontally and vertically. For any pair of  $s_i \in S$  and  $s_j \in S$ ,  $\Omega(s_i)$  and  $\Omega(s_j)$  are disjoint with each other.

#### 3.2 Communication model

Only when the UAV is located in  $\Omega(s_i)$  and there is no obstacles between the UAV and  $s_i$  can the UAV collect data from  $s_i$ . Therefore, in this paper, we adopt the Free Space Path Loss (FSPL) model between UAV and sensors. Based on Gong et al. (2018) Luo et al. (2021a), the data transmission rate from  $s_i$  to u can be described as

$$C_u(s_i) = \begin{cases} \frac{1}{2}W \log_2(1 + \frac{\gamma_0 P_w}{d^{\alpha}(s_i, u)}), & \text{LoS} \\ 0, & \text{NLoS} \end{cases}$$
(1)

where *W* denotes the channel bandwidth,  $d(s_i, u)$  denotes the Euclidean distance between  $s_i$  and u,  $\alpha$  is the path loss exponent and  $2 \le \alpha < 4$ ,  $P_w$  represents the data transmission power of  $s_i$ ,  $\gamma_0 = \frac{\beta_0}{\sigma^2}$  denotes the reference signal-to-noise ratio in which  $\beta_0$  represents the channel gain at a reference distance  $d_0 = 1m$  and  $\sigma^2$  is the noise variance.

#### 3.3 Solar energy harvesting model

In this paper, we adopt the solar energy harvesting model in Fu et al. (2021). Ignoring the influence of atmosphere, the power of UAV collected from sunlight when it flies at altitude h can be expressed as

$$P_c(h) = \eta_s A_s G_s(\alpha_s - \beta_s e^{\frac{-h}{\delta_s}}), \qquad (2)$$

where  $\eta_s$  represents the energy conversion efficiency,  $A_s$  denotes the area of the solar panel,  $G_s$  is the average solar radiation,  $\alpha_s$  denotes the maximum value of atmospheric transmittance,  $\beta_s$  denotes the atmospheric extinction coefficient, and  $\delta_s$  is the scale height of the earth.

According to the Eq.(2), we can obtain that the higher the UAV flies, the more power it can charge from the sunlight.

#### 3.4 Propulsion power consumption model

According to the propulsion power consumption model for rotating wing UAV proposed in Wang et al. (2019), we can obtain the consumption power of UAV is a function of flight speed v, and it can be expressed as

$$P(v) = P_0 \left( 1 + \frac{3v^2}{v_r^2} \right) + P_1 \left( \sqrt{1 + \frac{v^4}{4v_0^4}} - \frac{v^2}{2v_0^2} \right)^{\frac{1}{2}} + \frac{d_0 \rho s A v^3}{2}, \quad (3)$$

where  $P_0$  and  $P_1$  are two constants representing the blade profile power and induced power in hovering status,  $v_r$  denotes the tip speed of the rotor,  $v_0$  is the mean rotor induced velocity in hover,  $d_0$  represents the fuselage drag ratio, s is the rotor robustness, and  $\rho$  denotes the air density in units of  $k_g/m^3$ , A is rotor disk area.

Based on proof in Wu et al. (2020), we have the equation (3) is convex, i.e., there exists an optimal speed  $v^*$  to minimize the value of P(v). And the value of  $v^*$  is given as

$$v^* = \arg\min_{v\ge 0} P(v),\tag{4}$$

#### 3.5 Definition for the problem

In this subsection, we give the detailed definition of the Data Collection Maximization based on Solar-powered UAV (DCMS) problem as shown in Definition 1, whose objective is to maximize the amount of data collected from WSN by solar-powered UAV with limited initial energy.

In the Definition 1, we use  $\Phi(U, Q, T, D_f)$  to denote the feasible flight plan of UAV such that a part of data in WSN are collected and transported to the data center, where U represents the flight tour of UAV, Q denotes the set of hovering points of UAV to collect data from sensors, T is the set of hovering time of UAV at the hovering points in Q, and  $D_f$  is the amount of data collected from sensors when the UAV is flying on U.

**Definition 1** (**DCMS**) Given a set  $S = \{s_1, s_2, ..., s_n\}$  of *n* sensors in which each  $s_i$  stores  $V_i$  units of data, a base station  $s_0$ , a set  $O = \{o_1, o_2 ..., o_m\}$  of *m* obstacles with known location and size, a solar-powered UAV *u* with initial energy *E*, horizontal

flight speed  $v_f$  that varies with flight altitude *h*, vertical flight speed  $v_l$ , minimum flight

altitude *H* for horizontal flying, the Data Collection Maximization based on Solarpowered UAV (DCMS) problem aims at finding a flight plan  $\Phi(U, Q, T, D_f)$  such that

- (1) U starts from and ends at  $s_0$ ,
- (2) the UAV can collect data from  $s_i$  when it is within  $\Omega(s_i)$  and there is no obstacles between it and  $s_i$ ,
- (3) at any given moment, the energy of the UAV is greater than 0 and less than or equal to E,
- (4) for any o<sub>j</sub> ∈ O, if o<sub>j</sub> is taller than H, then the UAV will by pass it from above or left or right,
- (5) for any hovering point  $hp_i \in Q$ , the UAV collects data from  $s_i$  with  $t_i^h \in T$  time,
- (6) the amount of data collected by the UAV,  $D = \Sigma_{hp_i \in Q} t_i^h \cdot C_u(s_i) + D_f$  is maximized.

Formally, problem DCMS can be formulated as

$$\max \ \Sigma_{hp_i \in Q} \frac{1}{2} t_i^h W \log_2 \left( 1 + \frac{\gamma_0 P_w}{d^\alpha(s_i, hp_i)} \right) + D_f$$
(5)

s.t

$$0 \le E_{\rho}^r \le E \tag{6}$$

**Theorem 1** The DCMS problem is NP-hard.

**Proof** If we set R = 0,  $E = +\infty$ ,  $V_i = 0$  for each sensor  $s_i \in S$ , H = 0 and  $h_j^o = 0$  for any  $o_j \in O$ , then the DCMS problem can be reduced to the the well-known Traveling Salesman Problem (TSP) since the UAV only needs to visit all sensors for collecting data. Since the TSP problem is a special case of the DCMS problem and the TSP problem has been shown to be NP-hard (?), the DCMS problem is also NP-hard.

**Theorem 2** Let L and  $E_{net}^L$  represent the horizontal flight distance and the net energy consumption flying on L of UAV, respectively. There exists an optimal horizontal flight speed  $v_f^*$  to minimize  $E_{net}^L$  which is a function with respect to the flight altitude h, i.e.,  $v_f^* = \varphi(h)$ .

**Proof** According to the definition, we can obtain

$$E_{net}^{L} = P(v_f) \frac{L}{v_f} - P_c(h) \frac{L}{v_f},$$
(7)

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By substituting  $P(v_f)$  and  $P_c(h)$  into equation (7), we have

$$E_{net}^{L} = \left( P_0 \left( 1 + \frac{3v_f^2}{v_r^2} \right) + P_1 \left( \sqrt{1 + \frac{v_f^4}{4v_0^4}} - \frac{v_f^2}{2v_0^2} \right)^{\frac{1}{2}} + \frac{d_0 \rho s A v_f^3}{2} - \eta_s A_s G_s \left( \alpha_s - \beta_s e^{\frac{-h}{\delta_s}} \right) \right) \frac{L}{v_f},$$
(8)

Based on Wu et al. (2020), the Eq. (8) can be reduced to

$$E_{net}^{L} = \left(P_0\left(1 + \frac{3v_f^2}{v_r^2}\right) + P_1\frac{v_0}{v_f} + \frac{d_0\rho sAv_f^3}{2} -\eta_s A_s G_s\left(\alpha_s - \beta_s e^{\frac{-h}{\delta_s}}\right)\right)\frac{L}{v_f},$$
(9)

The first derivative of  $E_{net}^L$  with respect to  $v_f$  is

$$(E_{net}^{L})' = \frac{L}{v_{f}^{2}} \left( \frac{3P_{0}v_{f}^{2}}{v_{r}^{2}} - \frac{2P_{1}v_{0}}{v_{f}} + Ad_{0}\rho s v_{f}^{3} - P_{0} + \eta_{s}A_{s}G_{s} \left( \alpha_{s} - \beta_{s}e^{\frac{-h}{\delta_{s}}} \right) \right),$$
(10)

Let  $g(v_f) = \frac{3P_0v_f^2}{v_r^2} - \frac{2P_1v_0}{v_f} + Ad_0\rho sv_f^3 - P_0 + \eta_s A_s G_s(\alpha_s - \beta_s e^{\frac{-h}{\delta_s}})$ , the first derivative of  $g(v_f)$  with respect to  $v_f$  is

$$g'(v_f) = \frac{6P_0v_f}{v_r^2} + \frac{2P_1v_0}{v_f^2} + 3Ad_0\rho sv_f^2,$$
(11)

Obviously, when  $v_f > 0$ ,  $g'(v_f) > 0$ . Therefore,  $g(v_f)$  increases strictly monotonically over the interval  $(0, +\infty)$ . As  $v_f$  goes to 0,  $g(v_f)$  goes to  $-\infty$ , and as  $v_f$  goes to  $+\infty$ ,  $g(v_f)$  goes to  $+\infty$ . Thus,  $g(v_f)$  has a unique zero-point  $v_f^*$  on the interval  $(0, +\infty)$  that makes  $g(v_f)$  minimum. Therefore,  $E_{net}^L$  is minimum when  $v_f = v_f^*$ . Therefore, we can obtain the following function

$$h = \psi(v_f^*) = -\delta_s \ln\left(\frac{\alpha_s}{\beta_s} + \frac{1}{\eta_s A_s G_s \beta_s} \left(\frac{3P_0(v_f^*)^2}{v_r^2} - \frac{2P_1 v_0}{(v_f^*)} + Ad_0 \rho s(v_f^*)^3 - P_0\right)\right),\tag{12}$$

Let  $\chi(v_f) = \frac{3P_0v_f^2}{v_r^2} - \frac{2P_1v_0}{v_f} + Ad_0\rho sv_f^3 - P_0$ , then  $\chi(v_f)$  and  $g(v_f)$  have the same monotonicity, and we can rewrite Eq. (12) as



(a) Bypass  $o_j$  on the left (b) Bypass  $o_j$  on the right (c) Bypass  $o_j$  on the upward Fig. 1 Schematic diagram of obstacle  $o_j$  bypassing methods of UAV

$$h = \psi(v_f^*) = -\delta_s \ln\left(\frac{\alpha_s}{\beta_s} + \frac{\chi(v_f)}{\eta_s A_s G_s \beta_s}\right),\tag{13}$$

It is easy to observe that the Eq. (13) is strictly monotonically decreasing in the interval  $(0, +\infty)$ . According to the existence theorem of the inverse function, we have

$$v_f^* = \varphi(h) = \psi^{-1}(h).$$
 (14)

Therefore, in the following proposed algorithm, we let  $v_f = v_f^*$  to minimize the net energy consumption of UAV when the UAV flies at a fixed altitude.

## 4 Research methods

In this section, we propose an approximation algorithm to solve the DCMS problem. The algorithm consists of four phases.

The first phase to design a algorithm to bypass obstacles. The second phase is first to construct the auxiliary graph based on the given network model. Then we compute an flight path  $U_c$  of UAV based on the auxiliary graph to connect all data collection areas in WSN when its energy is enough. Afterwards, for any  $s_i \in S$ , we compute the two interconnect points  $st_i$  and  $ed_i$  between  $U_c$  and  $\Omega(s_i)$ . In the third phase, we design the flight trajectory  $\Upsilon(U_i, hp_i, t_i^h)$  of UAV in  $\Omega(s_i)$  for any  $s_i \in S$  such that all data of  $s_i$  is collected, where  $U_i$  is a path from  $st_i$  to  $ed_i$ . Based on the first three phases, we can obtain initial flight plan  $\Phi(U, Q, T, D_f)$  when the energy of UAV is enough, where  $U = \bigcup_{s_i \in S} U_i \cup U_c$ .

In the fourth phase, we first compute the energy consumption  $E_{net}$  of UAV when the UAV execute the flight plan  $\Phi(U, Q, T, D_f)$ . Then we compare  $E_{net}$  with E. If  $E_{net} \leq E$ , then the algorithm is exit and return the flight plan  $\Phi(U, Q, T, D_f)$  and D. Otherwise, the algorithm delete the visited data collection areas on  $\Phi(U, Q, T, D_f)$ whose the amount of data collected per unit energy consumption is minimum (Fig. 1).

#### Algorithm 1 BOFA

**Input:** UAV *u* with flight height *H*, horizontal flight speed  $v_f^*$  and vertical flight speed  $v^*$ ,  $p_j^o = (x_j^o, y_j^o, z_j^o), (l_j^o, w_j^o, h_j^o)$ ; **Output:**  $P_j^o, E_{net}^{bj}$ ; **1:** Compute the coordinates of corner points  $e_{sc}^{lj}, e_{ec}^{rj}, e_{sc}^{rj}, e_{sc}^{sj}$  and  $e_{ec}^{uj}$ ; **2:**  $P_j^{lo} = sp_j \rightarrow e_{sc}^{lj} \rightarrow e_{ec}^{lj} \rightarrow ep_j$ ; **3:**  $P_j^{ro} = sp_j \rightarrow e_{sc}^{rj} \rightarrow e_{ec}^{rj} \rightarrow ep_j$ ; **4:**  $P_j^{uo} = sp_j \rightarrow e_{sc}^{sj} \rightarrow e_{ec}^{uj} \rightarrow ep_j$ ; **5:**  $E_{net}^{lbj} = \frac{L(P_j^{lo})}{v_f^*} P(v_f^*) - \frac{L(P_j^{lo})}{v_f^*} P_c(H)$ ; **6:**  $E_{net}^{rbj} = \frac{L(P_j^{ro})}{v_f^*} P(v_f^*) - \frac{L(P_j^{ro})}{v_f^*} P_c(H)$ ; **7:**  $E_{net}^{ubj} = \frac{2d(sp_j, e_{sc}^{uj})}{v^*} P(v^*) + \frac{d(sp_j, ep_j)}{v_f^*} (P(v_f^*) - P_c(h_j^o + d_j^o)) - 2\int_0^{\frac{d(sp_j, e_{sc}^{uj})}{v^*}} P_c(H + v^*t) dt$ ; **8:**  $E_{net}^{bj} = min\{E_{net}^{lbj}, E_{net}^{rbj}, E_{net}^{ubj}\}$  and  $P_j^o = arc(E_{net}^{bj})$ ;

#### 4.1 Algorithm to bypass obstacles

In this subsection, we propose an algorithm to bypass obstacles, which is called Bypass Obstacles during Flight Algorithm (BOFA). For any  $o_j \in O$ , we use  $sp_j$  and  $ep_j$  to represent the positions where the UAV arrives and leaves  $o_j$ , respectively. The BOFA is used to design a path  $P_j^o$  to bypass  $o_j \in O$ , where  $P_j^o$  starts from  $sp_j$  to  $ep_j$ . Let  $L(P_j^o)$  be the length of  $P_j^o$ . We use  $E_{net}^{bj}$  to denote the net energy consumption of UAV flying on  $P_j^o$ .

Let  $e_{sc}^{lj}$  and  $e_{ec}^{lj}$  denote the two corner points on the left of  $o_j$  considering buffer distance, respectively. We use  $e_{sc}^{rj}$  and  $e_{ec}^{rj}$  to represent the two corner points on the right of  $o_j$  considering buffer distance, respectively. Let  $e_{sc}^{uj}$  and  $e_{ec}^{uj}$  denote the two corner points right above  $sp_j$  and  $ep_j$ , respectively.

**Input**: UAV *u* with flight height *H*, horizontal flight speed  $v_f^*$ , vertical flight speed  $v^*$ ,  $s_0 \cup S$ , *O*, and number  $\mu$ , pheromone importance factor  $\zeta$ , total pheromone  $\overline{\omega}$ , heuristic importance factor  $\rho$ , pheromone volatile factor  $\xi$ , maximum number of iterations  $\epsilon$ ; **Output**:  $U_c$ ,  $L(U_c)$ , G'(SC, EC, WC); **1:** For any pair  $s_i, s_j \in S$ , compute  $ip_i^j$  and  $ip_i^i$ ; **2:** Compute  $SC = \{sc_0, sc_1, ..., sc_n\}$ ; **3:** Compute  $EC = \{(sc_0, sc_1), (sc_0, sc_2), (sc_0, sc_3), ..., (sc_{n-1}, sc_n)\}$ 4:  $IO_i^J = \emptyset;$ **5:** for any  $(sc_i, sc_j) \in EC$  do 6: for q from 1 to m do 7: if the edge  $(ip_i^J, ip_i^i)$  bypasses  $o_q$ , then  $IO_i^j = IO_i^j \cup o_q$ , obtain  $E_{net}^{bq}$  by executing the Algorithm BOFA; end 8: 9: 10: end 11: if  $IO_i^j = \emptyset$  then  $E_{net}^{i,j} = \frac{d(ip_i^{j}, ip_j^{i})}{v_{\epsilon}^{*}} (P(v_f^{*}) - P_c(H)), WC = WC \cup \{E_{net}^{i,j}\};$ 12: 13: else Let  $k = |IO_i^j|$  and obtain  $IO_i^{\prime j} = \{o_{l_1}, o_{l_2}, ..., o_{l_k}\};$ 14:  $E_{net}^{i,j} = (\frac{d(ip_i^j, sp_{l_1})}{v_f^*} + \frac{d(ep_{l_k}, ip_j^i)}{v_f^*} + \Sigma_{q=1}^{k-1} \frac{d(ep_{l_q}, sp_{l_q+1})}{v_f^*})(P(v_f^*) - P_c(H)) + \Sigma_{q=1}^k E_{net}^{bq};$ 15:  $WC = WC \cup \{E_{not}^{i,j}\};$ 16: 17: end 18: end **19:**  $L(U_c) = +\infty$ , for each edge  $\in EC$ , set the common initial pheromone value  $t_0$ ; **20:** for *count* from 1 to  $\epsilon$  do **21:** for  $\ell$  from 1 to  $\mu$  do 22: Randomly initialize the starting position of the  $\ell$ -th ant which is located at one of node  $sc_p \in SC$ ; 23: The set of nodes on G'(SC, EC, WC) that hasn't been visited by  $\ell$ -th ant is  $NV_{\ell} = SC$ ; for  $\tau$  from 1 to |SC| do 24: 25:  $NV_{\ell} = NV_{\ell} \setminus \{sc_p\};$ 26: Calculate the transition probability *Pro* on  $NV_{\ell}$  based on  $\varsigma$ ,  $\varrho$ ; 27: Update the location  $sc_p$  of  $\ell$ -th ant based on *Pro*; 28: end 29: end 30: for  $\ell$  from 1 to  $\mu$  do Compute the circuit  $C_{\ell}$  and its length  $L(C_{\ell})$  of the  $\ell$ -th ant; 31: 32: if  $L(C_\ell) < L(U_c)$  do 33:  $U_c = C_\ell, L(U_c) = L(C_\ell);$ 34: end 35: end 36: for each edge  $e_i \in EC$  do 37: Update pheromone value based on  $\varpi_i$  and  $\xi_i$ ; 38: end 39: end

The BOFA algorithm consists of three steps. In the first step, we compute the coordinates of corner points  $e_{sc}^{lj}$ ,  $e_{ec}^{rj}$ ,  $e_{sc}^{rj}$ ,  $e_{sc}^{uj}$  and  $e_{ec}^{uj}$  based on  $p_j^o$ ,  $sp_j$  and  $ep_j$ ; In the second step, we obtain the flight paths  $P_j^{lo}$ ,  $P_j^{ro}$  and  $P_j^{uo}$  of UAV, where  $P_j^{lo} = sp_j \rightarrow e_{sc}^{lj} \rightarrow e_{ec}^{lj} \rightarrow ep_j$ ,  $P_j^{ro} = sp_j \rightarrow e_{sc}^{rj} \rightarrow ep_j$  and  $P_j^{uo} = sp_j$ .

 $sp_j \rightarrow e_{sc}^{uj} \rightarrow e_{ec}^{uj} \rightarrow ep_j$ . In the third step, we compute the net energy consumption,  $E_{net}^{lbj}$ ,  $E_{net}^{rbj}$  and  $E_{net}^{ubj}$  of UAV when the UAV flies on  $P_j^{lo}$ ,  $P_j^{ro}$  and  $P_j^{uo}$ , respectively. Finally, we let  $E_{net}^{bj} = min\{E_{net}^{lbj}, E_{net}^{rbj}, E_{net}^{ubj}\}$  and  $P_j^o = arc(E_{net}^{bj})$ .

# 4.2 Construct flight path U<sub>c</sub>

In this subsection, we propose an algorithm to construct the auxiliary graph G'(SC, EC, WC) and obtain flight path  $U_c$  and its length  $L(U_c)$  based on G', where SC denotes the node set, EC denotes the edge set and WC represents the set of weight of edges in EC. The algorithm is called Auxiliary Graph Flight Path (AGFP), which consists of the following three steps.

In the first step, we compute the intersection point  $ip_i^j$  between  $C(s_i')$  and edge  $(s_i', s_j')$  and the intersection point  $ip_i^j$  between  $C(s_j')$  and edge  $(s_i', s_j')$ .

In the second step, we construct the auxiliary graph G'(SC, EC, WC). We first compute the set  $SC = \{sc_0, sc_1, \ldots, sc_n\}$  of points, where each  $sc_i$  is a virtual point shrunk from  $C(s'_i)$  and obtain the set EC that is set of edges made up of any two points in SC, i.e.,  $EC = \{(sc_0, sc_1), (sc_0, sc_2), \ldots, (sc_{n-1}, sc_n)\}$ . Then, for any edge  $(sc_i, sc_j) \in EC$ , we compute the set  $IO_i^j$  of all obstacles passed by the edge  $(ip_i^j, ip_j^i)$  and the ordered set  $IO_i'^j$  in which all obstacles in  $IO_i^j$  are ordered from  $ip_i^j$  to  $ip_j^i$ . Afterwards, for arbitrary  $(sc_i, sc_j) \in EC$ , we compute the net energy consumption  $E_{net}^{i,j}$  of UAV flying from  $ip_i^j$  to  $ip_j^i$  based on  $IO_i'^j$ , and we use  $E_{net}^{i,j}$  to denote the weight of the edge  $(sc_i, sc_j)$  and  $WC = WC \cup \{E_{net}^{i,j}\}$ .

In the third step, we use Ant Colony Algorithm(ACA) to construct a hamiltonian circuit  $U_c$  on G'(SC, EC, WC). Let  $\epsilon$  be the number of iterations of the algorithm ACA. We initialize  $L(U_c) = +\infty$  and set the common initial pheromone value  $t_0$  for each edge of EC. For any *count* from 1 to  $\epsilon$ , we repeat executing the following steps. Firstly, we randomly place  $\mu$  ants on some nodes in SC ( $\mu < |SC|$ ), and let these nodes be the starting positions of ants. Secondly, each ant selects the next node from SC until all ants have visited all nodes on SC. We can obtain an initial hamiltonian circuit  $C_\ell$  and its length  $L(C_\ell)$  for the  $\ell$ -th ant. Thirdly, we update pheromone value based on  $\varpi_i$  and  $\xi_i$ , where  $\varpi_i$  and  $\xi_i$  are total pheromone and pheromone volatile factor, respectively. Finally, for any  $\ell$  from 1 to  $\mu$ , we compare  $L(C_\ell)$  with  $L(U_c)$ , if  $L(C_\ell) < L(U_c)$ , then we set  $U_c = C_\ell$  and  $L(U_c) = L(C_\ell)$ .

#### Algorithm 3 CFPU

**Input**:  $v_f^*$ ,  $v^*$ , H, O, R,  $s_i$ ,  $st_i$ ,  $ed_i$ ,  $\Gamma$ ; **Output:**  $\Upsilon(U_i, hp_i, t_i^h), E_{net}^i;$ **1:**Divide  $\Omega(s_i)$  into  $\Gamma$  parts based on R, and obtain  $\Delta_i = \{\Delta_i^1, \Delta_i^2, ..., \Delta_i^{\Gamma}\}$ ; **2:**Compute the ordered sets  $O_i^{sx} = \{o_{j_1}, o_{j_2}, ..., o_{j_{k_1}}\}, O_i^{xe'} = \{o_{\aleph_1}, o_{\aleph_2}, ..., o_{\aleph_{k_2}}\}, O_i^{se'} = \{o_{i_1}, o_{i_2}, ..., o_{i_{k_3}}\}$ , and let  $X_i = s'_i, st'_i = st_i, ed'_i = ed_i$ . **3:if**  $s'_i \in o_{\aleph_1}$  then 4: if  $(l_{\aleph_1}^o + d_{\aleph_1}^o)/2 - |x_i - x_{\aleph_1}^o| \le (w_{\aleph_1}^o + d_{\aleph_1}^o)/2 - |y_i - y_{\aleph_1}^o|$  then if  $x_i \le x_{\aleph_1}$ , then  $X_i = (x_{\aleph_1} - (l_{\aleph_1}^{\circ} + d_{\aleph_1}^{\circ})/2, y_i, H);$ if  $x_i > x_{\aleph_1}$ , then  $X_i = (x_{\aleph_1} + (l_{\aleph_1}^{\circ} + d_{\aleph_1}^{\circ})/2, y_i, H);$ 5: 6: 7: else if  $y_i \le y_{\aleph_1}$ , then  $X_i = (x_i, y_{\aleph_1} - (w_{\aleph_1}^o + d_{\aleph_1}^o)/2, H);$ if  $y_i > y_{\aleph_1}$ , then  $X_i = (x_i, y_{\aleph_1} + (w_{\aleph_1}^o + d_{\aleph_1}^o)/2, H);$ 8: 9: 10: end 11:end **12:** If  $st_i \in o_{j_1}$ , then obtain  $P_{j_1}^o$  by executing the BOFA algorithm,  $st'_i = P_{j_1}^o \cap \Delta_i^{\Gamma}$ ; **13:** If  $ed_i \in o_{\aleph_{k_2}}$  then obtain  $P^o_{\aleph_{k_2}}$  by executing the BOFA algorithm,  $ed'_i = P^o_{\aleph_{k_2}} \cap \Delta^{\Gamma}_i$ ; **14:** Compute the paths  $P_{st'_i}^{X_i}$ ,  $P_{X_i}^{ed'_i}$  and  $P_{st'_i}^{ed'_i}$  based on  $st'_i$ ,  $ed'_i$ ,  $X_i$ ,  $O_i^{sx}$ ,  $O_i^{xe}$  and  $O_i^{se}$ ; **15:** Compute the amount of data  $V_{st'_i}^{X_i}$ ,  $V_{X_i}^{ed'_i}$  and  $V_{st'_i}^{ed'_i}$  collected on  $P_{st'_i}^{X_i}$ ,  $P_{X_i}^{ed'_i}$  and  $P_{st'_i}^{ed'_i}$ ; **16:if**  $V_{st'_i}^{ed'_i} < V_i$  then **17:**  $\Theta_i = X_i, \ O_i^{s\theta} = O_i^{sx}, \ O_i^{\theta e} = O_i^{xe}, \ P_{st'}^{\Theta_i} = P_{st'}^{X_i}, \ P_{\Theta_i}^{ed'_i} = P_{X_i}^{ed'_i}, \ V_{st'}^{\Theta_i} = V_{st'_i}^{X_i}, \ V_{\Theta_i}^{ed'_i} = V_{x_i}^{ed'_i};$ **18:** for k from 1 to  $\Gamma$  do  $g_k = (X_i, ed_i) \cap \Delta_i^k;$ 19: if  $g_k \notin O_i^{xe}$  then 20: Compute  $O_i^{sg}$ ,  $O_i^{ge}$ ,  $P_{st'}^{gk}$ ,  $P_{gk}^{ed'}$ ,  $V_{st'}^{gk}$ ,  $V_{gk}^{ed'}$ ; 21: If  $V_{st'_i}^{g_k} + V_{g_k}^{ed'_i} \ge V_i$ , then  $\Theta_i = g_k$ ,  $O_i^{s\theta} = O_i^{sg}$ ,  $O_i^{\theta e} = O_i^{ge}$ ,  $P_{st'_i}^{\Theta_i} = P_{st'_i}^{g_k}$ ,  $P_{\Theta_i}^{ed'_i} = P_{g_k}^{ed'_i}$ 22:  $V_{st_{i}'}^{\Theta_{i}} = V_{st_{i}'}^{g_{k}}, V_{\Theta_{i}}^{ed_{i}'} = V_{g_{k}}^{ed_{i}'};$ 23: 24: end **25:** Let  $O_i^{s\theta} = \{o_{h_1}, o_{h_2}, ..., o_{h_{k_4}}\}, O_i^{\theta e} = \{o_{\theta_1}, o_{\theta_2}, ..., o_{\theta_{k_5}}\};$  **26:**  $NE_{st'_i}^{\Theta_i} = (L(P_{st'_i}^{\Theta_i}) - \sum_{q=1}^{k_4} L(P_{h_q}^o) / v_f^* \cdot (P(v_f^*) - P_c(H)) + \sum_{q=1}^{k_4} E_{net}^{bh_q};$ **27:**  $NE_{\Theta_i}^{ed'_i} = (L(P_{\Theta_i}^{ed'_i}) - \sum_{q=1}^{k_5} L(P_{\partial_q}^o))/v_f^*(P(v_f^*) - P_c(H)) + \sum_{q=1}^{k_5} E_{net}^{b\partial_q}$  **28:** if  $\Theta_i = X_i$  then  $hp_{i} = X_{i}, t_{i}^{h} = \frac{V_{i} - (V_{s_{i}}^{X_{i}} + V_{X_{i}}^{ed_{i}})}{C_{u}(s_{i})}, E_{net}^{i} = NE_{st'}^{X_{i}} + NE_{X_{i}}^{ed_{i}'} + t_{i}^{h}(P(0) - P_{c}(H));$ 29: 30: else  $hp_i = \emptyset, t_i^h = 0, E_{net}^i = N E_{st'}^{\Theta_i} + N E_{\Theta_i}^{ed'_i};$ 31: 32: end **33:**  $U_i = P_{st'_i}^{\Theta_i} \cup P_{\Theta_i}^{ed'_i};$ 34:else **35:**  $U_i = P_{st'}^{ed'_i}, hp_i = \emptyset, t_i^h = 0;$ **36:**  $E_{net}^i = (L(P_{st'}^{ed'_i}) - \sum_{q=1}^{k_3} L(P_{i_q}^o)) / v_f^* \cdot (P(v_f^*) - P_c(H)) + \sum_{q=1}^{k_3} E_{net}^{bi_q}$ 37: end

# 4.3 Construct fight plan $\Upsilon(U_i, hp_i, t_i^h)$ of UAV in $\Omega(s_i)$

In this subsection, we propose an algorithm to construct the flight plan  $\Upsilon(U_i, hp_i, t_i^h)$  and compute the net energy consumption  $E_{net}^i$  of UAV in  $\Omega(s_i)$ , which is called Construct Flight Plan in data collection Area (CFPA). The algorithm consists of the following five steps.

In the first step, we divide  $\Omega(s_i)$  into  $\Gamma$  parts based on R, and let  $\Delta_i = \{\Delta_i^1, \Delta_i^2, \ldots, \Delta_i^{\Gamma}\}$  denote the set of all hemispherical shells, where for any  $\Delta_i^{\vartheta} \in \Delta_i$ , the spherical equation is  $(x - x_i)^2 + (y - y_i)^2 + z^2 = (\vartheta \frac{R}{\Gamma})^2 (z \ge 0)$ .

In the second step, we compute the ordered sets  $O_i^{sx} = \{o_{j_1}, o_{j_2}, \dots, o_{j_{k_1}}\}, O_i^{xe} = \{o_{\aleph_1}, o_{\aleph_2}, \dots, o_{\aleph_{k_2}}\}, \text{ and } O_i^{se} = \{o_{i_1}, o_{i_2}, \dots, o_{i_{k_3}}\}, \text{ where } O_i^{sx}, O_i^{xe} \text{ and } O_i^{se} \text{ represent all obstacles passed by the edge } (st_i, s'_i) \text{ from } st_i \text{ to } s'_i, \text{ edge } (s'_i, ed_i) \text{ from } st_i \text{ to } ed_i \text{ and edge } (st_i, ed_i) \text{ from } st_i \text{ to } ed_i, \text{ respectively.}$ 

In the third step, we initially set  $X_i = s'_i$ ,  $st'_i = st_i$ ,  $ed'_i = ed_i$ . We judge whether the point  $s'_i$  is located in the first obstacle  $o_{\aleph_1} \in O_i^{xe}$ . If  $s'_i \in o_{\aleph_1}$ , then we update the coordinates of  $X_i$  based on the following situations.

(1) 
$$\frac{l_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2} - |x_{i} - x_{\aleph_{1}}^{o}|| \leq \frac{w_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2} - |y_{i} - y_{\aleph_{1}}^{o}||. \text{ If } x_{i} \leq x_{\aleph_{1}}, \text{ then } X_{i} = (x_{\aleph_{1}} - \frac{l_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2}, y_{i}, H), \text{ otherwise, } X_{i} = (x_{\aleph_{1}} + \frac{l_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2}, y_{i}, H).$$
  
(2) 
$$\frac{l_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2} - |x_{i} - x_{\aleph_{1}}^{o}|| > \frac{w_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2} - |y_{i} - y_{\aleph_{1}}^{o}||. \text{ If } y_{i} \leq y_{\aleph_{1}}, \text{ then } X_{i} = (x_{i}, y_{\aleph_{1}} - \frac{w_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2}, H), \text{ otherwise, } X_{i} = (x_{i}, y_{\aleph_{1}} + \frac{w_{\aleph_{1}}^{o}+d_{\aleph_{1}}^{o}}{2}, H).$$

Afterwards, we update the coordinates of  $st'_i$  by determining whether the  $st_i$  belongs to  $o_{J_1} \in O_i^{sx}$ . If  $st_i \in o_{J_1}$ , then we compute  $P_{J_1}^o$  by executing the BOFA algorithm, and obtain  $st'_i = P_{J_1}^o \cap \Delta_i^{\Gamma}$ . Finally, we update the coordinates of  $ed'_i$  by determining whether the  $ed_i$  belongs to  $o_{\aleph_{k_2}} \in O_i^{xe}$ . If  $ed_i \in o_{\aleph_{k_2}}$  then we compute  $P_{\aleph_{k_2}}^o$  by executing the BOFA algorithm, and obtain  $ed'_i = P_{\aleph_{k_2}}^o \cap \Delta_i^{\Gamma}$ .

In the fourth step, we compute the paths  $P_{st'_i}^{X_i}$ ,  $P_{X_i}^{ed'_i}$  and  $P_{st'_i}^{ed'_i}$  based on  $st'_i$ ,  $ed'_i$ ,  $X_i$ ,  $O_i^{sx}$ ,  $O_i^{xe}$  and  $O_i^{se}$ , and compute the amount of data  $V_{st'_i}^{X_i}$ ,  $V_{X_i}^{ed'_i}$  and  $V_{st'_i}^{ed'_i}$  collected by UAV during flying on  $P_{st'_i}^{X_i}$ ,  $P_{X_i}^{ed'_i}$  and  $P_{st'_i}^{ed'_i}$ , respectively. Firstly, we compute the avoid obstacle path  $P_{i_j}^o$  for any  $o_{i_j} \in O_i^{se}$  by executing the Algorithm BOFA. Then we compute the actual flight path  $P_{st'_i}^{ed'_i}$  of UAV from  $st'_i$  to  $ed'_i$  by considering obstacles in  $O_i^{se}$  based on the following four cases.

(1) 
$$st_i = st'_i$$
 and  $ed_i = ed'_i$ . Let  $P_{st'_i}^{ed'_i} = st_i \rightarrow P_{i_1}^o \rightarrow P_{i_2}^o \rightarrow \dots \rightarrow P_{i_{k_3}}^o \rightarrow X_i$ .  
(2)  $st_i = st'_i$  and  $ed_i \neq ed'_i$ . Let  $P_{st'_i}^{ed'_i} = st_i \rightarrow P_{i_1}^o \rightarrow \dots \rightarrow sp_{i_{k_3}} \rightarrow ed'_i$ .  
(3)  $st_i \neq st'_i$  and  $ed_i = ed'_i$ . Let  $P_{st'_i}^{ed'_i} = st_i \rightarrow ep_{i_1} \rightarrow \dots \rightarrow P_{i_{k_3}}^o \rightarrow ed_i$ .  
(4)  $st_i \neq st'_i$  and  $ed_i \neq ed'_i$ . Let  $P_{st'_i}^{ed'_i} = st_i \rightarrow ep_{i_1} \rightarrow \dots \rightarrow P_{i_{k_3-1}}^o \rightarrow sp_{i_{k_3}} \rightarrow ed'_i$ .

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Secondly, we compute the avoid obstacle path  $P_{J_j}^o$  for any  $o_{J_j} \in O_i^{sx}$  by executing the Algorithm BOFA. Then we compute the actual flight path  $P_{st'_i}^{X_i}$  of UAV from  $st'_i$  to  $X_i$  by passing obstacles in  $O_i^{sx}$  based on the following four cases.

(1)  $st_i = st'_i$  and  $X_i = s'_i$ . Let  $P^{X_i}_{st'_i} = st_i \rightarrow P^o_{J_1} \rightarrow P^o_{J_2} \rightarrow \ldots \rightarrow P^o_{J_{k_1}} \rightarrow X_i$ . (2)  $st_i = st'_i$  and  $X_i \neq s'_i$ . Let  $P^{X_i}_{st'_i} = st_i \rightarrow P^o_{J_2} \rightarrow P^o_{J_2} \rightarrow \ldots \rightarrow P^o_{J_{k_1}}$ . (3)  $st_i \neq st'_i$  and  $X_i = s'_i$ . Let  $P^{X_i}_{st'_i} = st'_i \rightarrow ep_{J_1} \rightarrow P^o_{J_2} \rightarrow \ldots \rightarrow P^o_{J_{k_1}} \rightarrow X_i$ . (4)  $st_i \neq st'_i$  and  $X_i \neq s'_i$ . Let  $P^{X_i}_{st'_i} = st'_i \rightarrow ep_{J_1} \rightarrow P^o_{J_2} \rightarrow P^o_{J_3} \rightarrow \ldots \rightarrow P^o_{J_{k_1}}$ .

Thirdly, we compute the avoid obstacle path  $P_{\aleph_j}^o$  for any  $o_{\aleph_j} \in O_i^{xe}$  by executing the Algorithm BOFA. Then we compute the actual flight path  $P_{X_i}^{ed'_i}$  of UAV from  $X_i$  to  $ed'_i$  by passing obstacles in  $O_i^{xe}$  based on the following four cases.

(1)  $X_i = s'_i$  and  $ed_i = ed'_i$ . We have  $P_{X_i}^{ed'_i} = X_i \to P_{\aleph_1}^o \to \ldots \to P_{\aleph_{k_2}}^o \to ed_i$ .

(2) 
$$X_i \neq s'_i$$
 and  $ed_i = ed'_i$ . We have  $P_{X_i}^{ed_i} = X_i \rightarrow P_{\aleph_2}^o \rightarrow \ldots \rightarrow P_{\aleph_{k_2}}^o \rightarrow ed_i$ 

- (3)  $X_i = s'_i$  and  $ed_i \neq ed'_i$ . We have  $P_{X_i}^{ed'_i} = X_i \rightarrow P_{\aleph_1}^o \rightarrow \ldots \rightarrow P_{\aleph_{k_2-1}}^o \rightarrow sp_{\aleph_{k_2}} \rightarrow ed'_i$ .
- (4)  $X_i \neq s'_i$  and  $ed_i \neq ed'_i$ . Obtain  $P_{X_i}^{ed'_i} = X_i \rightarrow P_{\aleph_2}^o \rightarrow \ldots \rightarrow P_{\aleph_{k_2-1}}^o \rightarrow sp_{\aleph_{k_2}} \rightarrow ed'_i$ .

Afterwards, we compute the amount of data  $V_{st_i}^{X_i}$ ,  $V_{X_i}^{ed_i'}$  and  $V_{st_i'}^{ed_i'}$  collected by UAV during flying on  $P_{st_i'}^{X_i}$ ,  $P_{X_i}^{ed_i'}$  and  $P_{st_i'}^{ed_i'}$ , respectively. For any  $\Delta_i^{\vartheta} \in \Delta_i$ , we compute the intersection points  $P_{st_i'}^{X_i} \cap \Delta_i^{\vartheta}$  between  $\Delta_i^{\vartheta}$  and  $P_{st_i'}^{X_i}$ . Let  $IS_{st_i'}^{X_i} = \bigcup_{\Delta_i^{\vartheta} \in \Delta_i} (P_{st_i'}^{X_i} \cap \Delta_i^{\vartheta})$ . For arbitrary  $\Delta_i^{\vartheta} \in \Delta_i$ , we compute the intersection points  $P_{X_i}^{ed_i'} \cap \Delta_i^{\vartheta}$  between  $\Delta_i^{\vartheta}$  and  $P_{X_i}^{ed_i'}$ . Let  $IS_{X_i}^{ed_i'} = \bigcup_{\Delta_i^{\vartheta} \in \Delta_i} (P_{X_i}^{ed_i'} \cap \Delta_i^{\vartheta})$ . For any  $\Delta_i^{\vartheta} \in \Delta_i$ , we compute the intersection points  $P_{st_i'}^{ed_i'} \cap \Delta_i^{\vartheta}$  between  $\Delta_i^{\vartheta}$  and  $P_{st_i'}^{ed_i'}$ . Let  $IS_{st_i'}^{ed_i'} = \bigcup_{\Delta_i^{\vartheta} \in \Delta_i} (P_{st_i'}^{ed_i'} \cap \Delta_i^{\vartheta})$ . After that, we obtain the ordered sets  $IS_{st_i'}^{X_i}$ ,  $IS_{X_i}^{Yed_i'}$  and  $IS_{st_i'}^{Yed_i'}$  by sorting  $IS_{st_i'}^{X_i}$  from  $st_i'$  to  $X_i$ ,  $IS_{X_i}^{ed_i'}$  from  $X_i$  to  $ed_i'$  and  $IS_{st_i'}^{ed_i'}$  from  $st_i'$  to  $ed_i'$ , respectively.

Finally, for any pair of points  $is_g$ ,  $is_{g+1} \in IS'_{st'_i}^{X_i}$ , we compute the flight time  $t_g^{sx} = \frac{\sqrt{(x_{is_g} - x_{is_{g+1}})^2 + (y_{is_g} - y_{is_{g+1}})^2}}{v_f^*} + \frac{|z_{is_{g+1}} - z_{is_g}|}{v^*}$  of UAV during from  $is_g$  to  $is_{g+1}$ . Let  $V_{st'_i}^{X_i} = \sum_{g=1}^{|IS'_{st'_i}|-1} t_g^{sx} C_u(s_i)$ . We compute the flight time  $t_g^{xe} = \frac{\sqrt{(x_{is_g} - x_{is_{g+1}})^2 + (y_{is_g} - y_{is_{g+1}})^2}}{v_f^*} + \frac{|z_{is_{g+1}} - z_{is_g}|}{v^*}$  of UAV for any pair of points  $is_g$ ,  $is_{g+1} \in IS'_{X_i}^{ed'_i}$ , during from  $is_g$  to  $is_{g+1}$ . Let  $V_{X_i}^{ed'_i} = \sum_{g=1}^{|IS'_{X_i}^{ed'_i}|-1} t_g^{xe} C_u(s_i)$ . For any pair of points  $is_g$ ,  $is_{g+1} \in IS'_{st'_i}^{ed'_i}$ ,

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**Fig. 2** Schematic diagram of UAV flight trajectory optimization: **a**  $V_i > V_{st_i'}^{X_i} + V_{X_i}^{ed_i'}$ , UAV flies from  $st_i$  to  $X_i$  and from  $X_i$  to  $ed_i$ , and hovers on  $X_i$ ; **b**  $V_{st_i'}^{ed_i'} < V_i \le V_{st_i'}^{X_i} + V_{X_i}^{ed_i'}$ , UAV flies from  $st_i$  to  $\Theta_i$ , and from  $\Theta_i$  to  $ed_i'$ ; **c**  $V_i \le V_{st_i'}^{ed_i'}$ , UAV flies from  $st_i'$  to  $ed_i$  directly

we compute the flight time 
$$t_g^{se} = \frac{\sqrt{(x_{isg} - x_{isg+1})^2 + (y_{isg} - y_{isg+1})^2}}{v_f^*} + \frac{|z_{isg+1} - z_{isg}|}{v^*}$$
 of UAV during from  $is_g$  to  $is_{g+1}$ . Let  $V_{st_i'}^{ed_i'} = \Sigma_{g=1}^{|IS_{st_i'}^{ed_i'}| - 1} t_g^{se} C_u(s_i)$ .

In the fifth step, we compute  $\Upsilon(U_i, hp_i, t_i^h)$  and  $E_{net}^i$  by considering the following two scenarios. The optimization result of UAV flight trajectory is shown in Fig. 2.

- (1)  $V_{st'_i}^{ed'_i} < V_i$ . We initially set  $\Theta_i = X_i$ ,  $O_i^{s\theta} = O_i^{sx}$ ,  $O_i^{\theta e} = O_i^{xe}$ ,  $P_{st'_i}^{\Theta_i} = P_{st'_i}^{X_i}$ ,  $P_{\Theta_i}^{ed'_i} = P_{X_i}^{ed'_i}$ ,  $V_{\sigma_i}^{\Theta_i} = V_{st'_i}^{X_i}$ ,  $V_{\Theta_i}^{ed'_i} = V_{X_i}^{ed'_i}$ . For any k from 1 to  $\Gamma$ , we repeat executing the following steps.
  - 1) Let  $g_k = (X_i, ed_i) \cap \Delta_i^k$ . If  $g_k \notin O_i^{xe}$ , then we compute the obstacles set  $O_i^{sg}$  and  $O_i^{ge}$  passed by the edge  $(st'_i, g_k)$  from  $st'_i$  to  $g_k$  and edge  $(g_k, ed'_i)$  from  $g_k$  to  $ed'_i$ , respectively, compute the flight paths  $P_{st'_i}^{gk}$  and  $P_{gk}^{ed'_i}$  of UAV from  $st'_i$  to  $g_k$  and from  $g_k$  to  $ed'_i$ , respectively, and compute the amount of data  $V_{st'_i}^{gk}$  and  $V_{gk}^{ed'_i}$  collected by UAV during flying on  $P_{st'_i}^{gk}$  and  $P_{gk}^{ed'_i}$ , respectively.
  - 2) If  $V_{st'_{i}}^{g_{k}} + V_{g_{k}}^{ed'_{i}} \ge V_{i}$ , then we set  $\Theta_{i} = g_{k}, O_{i}^{s\theta} = O_{i}^{sg}, O_{i}^{\theta e} = O_{i}^{ge}, P_{st'_{i}}^{\Theta_{i}} = P_{st'_{i}}^{g_{k}}, P_{\Theta_{i}}^{ed'_{i}} = P_{g_{k}}^{g_{k}}, V_{st'_{i}}^{\Theta_{i}} = V_{st'_{i}}^{g_{k}}, V_{\Theta_{i}}^{ed'_{i}} = V_{g_{k}}^{gd'_{i}}.$

Afterwards, we let  $O_i^{s\theta} = \{o_{\hbar_1}, o_{\hbar_2}, \dots, o_{\hbar_{k_4}}\}$  and  $O_i^{\theta e} = \{o_{\partial_1}, o_{\partial_2}, \dots, o_{\partial_{k_5}}\}$ denote the ordered set of obstacles. Then, we compute the net energy consumption  $NE_{st'_i}^{\Theta_i} = \frac{L(P_{st'_i}^{\Theta_i}) - \sum_{q=1}^{k_4} L(P_{\hbar_q}^{\circ})}{v_f^*} (P(v_f^*) - P_c(H)) + \sum_{q=1}^{k_4} E_{net}^{b\hbar_q}$  and  $NE_{\Theta_i}^{ed'_i} = \frac{L(P_{\Theta_i}^{ed'_i}) - \sum_{q=1}^{k_5} L(P_{\partial_q}^{\circ})}{v_f^*} (P(v_f^*) - P_c(H)) + \sum_{q=1}^{k_5} E_{net}^{b\partial_q}$ . Finally, we can obtain  $U_i = P_{st_i'}^{\Theta_i} \cup P_{\Theta_i}^{ed_i'}$ . If  $\Theta_i = X_i$ , then  $hp_i = X_i$ ,  $t_i^h = \frac{V_i - (V_{st_i'}^{X_i} + V_{x_i}^{ed_i'})}{C_u(s_i)}$ ,  $E_{net}^i = NE_{st_i'}^{X_i} + NE_{X_i}^{ed_i'} + t_i^h(P(0) - P_c(H))$  and  $U_i$  is shown in Fig. 2a, otherwise,  $hp_i = \emptyset$ ,  $t_i^h = 0$ ,  $E_{net}^i = NE_{st_i'}^{\Theta_i} + NE_{\Theta_i}^{ed_i'}$  and  $U_i$  is shown in Fig. 2b. (2)  $V_i \leq V_{st_i'}^{ed_i'}$ . We set  $E_{net}^i = \frac{L(P_{st_i'}^{ed_i'}) - \sum_{q=1}^{k_3} L(P_{t_q}^o)}{v_f^*} (P(v_f^*) - P_c(H)) + \sum_{q=1}^{k_3} E_{net}^{bt_q}$ ,  $U_i = P_{st_i'}^{ed_i'}$ ,  $hp_i = \emptyset$ , and  $t_i^h = 0$ , where  $U_i$  is shown in Fig. 2c.

#### 4.4 Algorithm for the DCMS problem

In this subsection, we propose an approximation algorithm to solve the DCMS problem, which is called DCMSA. The algorithm consists of the following two steps.

#### Algorithm 4 DCMSA

**Input**:  $E, s_0 \cup S, v_f^*, v^*, H, O, R;$ **Output**:  $\Phi(U, Q, \mathring{T}, D_f), D;$ 1: Use the AGFP algorithm to obtain virtual graph G'(SC, EC, WC) and  $U_c$  based on  $s_0 \cup S$  and O and let  $U_c = sc_{\rho_0} \rightarrow sc_{\rho_1} \rightarrow ... \rightarrow sc_{\rho_n} \rightarrow sc_{\rho_0};$ 2: Use the CFPU algorithm to obtain  $\Upsilon(U_i, hp_i, t_i^h)$  and  $E_{net}^i$  for any  $s_i \in S$ ; **3:**  $U = \bigcup_{s_i \in S} U_i \cup U_c, Q = \bigcup_{s_i \in S} hp_i, T = \bigcup_{s_i \in S} t_i^h$ ; 4:  $E_{net} = \sum_{i=1}^{n} E_{net}^{\rho_i} + \sum_{i=0}^{n-1} E_{net}^{\rho_i, \rho_{i+1}} + E_{net}^{\rho_n, \rho_0};$ **5:** Let  $S' = \{s_{\rho_0}, s_{\rho_1}, \dots, s_{\rho_n}\}$  be the ordered set of sensors visited by U from  $s_0$  to  $s_0$ ; **6:** while  $E_{net} > E$  do 7: for each  $s_{\rho_i} \in S' \setminus \{s_{\rho_0}\}$  do 8:  $\Lambda_{\rho_i} = \frac{V_{\rho_i}}{E_{net}^{\rho_i - 1, \rho_i} + E_{net}^{\rho_i, \rho_i + 1} + E_{net}^{\rho_i} - E_{net}^{\rho_i - 1, \rho_{i+1}}};$ 9: end **10:**  $\Lambda_{\min} = \min\{\Lambda_{\rho_1}, \Lambda_{\rho_2}, ..., \Lambda_{\rho_{|S'|-1}}\}, s_{\rho_x} = arc(\Lambda_{\min}), S' = S' \setminus \{s_{\rho_x}\};$ **11:**  $U_c = U_c \setminus \{(sc_{\rho_{i-1}}, sc_{\rho_i}), (sc_{\rho_i}, sc_{\rho_{i+1}})\}, U_c = U_c \cup \{(sc_{\rho_{i-1}}, sc_{\rho_{i+1}})\}; u_c = U_c \cup \{(sc_{\rho_{i+1}}, sc_{\rho_{i$ 12: Use the CFPU algorithm to obtain  $\Upsilon(U_{\rho_{i-1}}, hp_{\rho_{i-1}}, t^h_{\rho_{i-1}}), \Upsilon(U_{\rho_{i+1}}, hp_{\rho_{i+1}}, t^h_{\rho_{i+1}}), E^{\rho_{i-1}}_{net}$  $E_{net}^{\rho_{i+1}};$ **13:**  $U = \bigcup_{s_i \in S' \setminus \{s_{\rho_0}\}} U_i \cup U_c, Q = \bigcup_{s_i \in S' \setminus \{s_{\rho_0}\}} hp_i, T = \bigcup_{s_i \in S' \setminus \{s_{\rho_0}\}} t_i^h;$ **14:** Let  $S' = \{s_{\rho_0}, s_{\rho_1}, \dots, s_{\rho_{|S'|-1}}\}$  be the ordered set of sensors visited by U from  $s_0$  to  $s_0, U_c = sc_{\rho_0} \rightarrow sc_{\rho_1} \rightarrow \dots \rightarrow sc_{\rho_{|S'|-1}} \rightarrow sc_{\rho_0};$  **15:**  $E_{net} = \sum_{i=1}^{|S'|-1} E_{net}^{\rho_i} + \sum_{i=0}^{|S'|-2} E_{net}^{\rho_i, \rho_{i+1}} + E_{net}^{\rho_{|S'|-1}, \rho_0};$ 16: end 17:  $D = \Sigma_{s_i \in S' \setminus \{s_{oo}\}} V_i;$ **18:**  $D_f = D - \Sigma_{hp_i \in \mathcal{Q}} \frac{1}{2} t_i^h W \log_2(1 + \frac{\gamma_0 P_w}{d^{\alpha}(\varsigma, hp_i)});$ 

In the first step, we compute initial U, Q, T and  $E_{net}$ . First of all, we use the AGFP algorithm to obtain a virtual graph G'(SC, EC, WC) and  $U_c$  based on  $s_0 \cup S$  and O, and let  $U_c = sc_{\rho_0} \rightarrow sc_{\rho_1} \rightarrow \ldots \rightarrow sc_{\rho_n} \rightarrow sc_{\rho_0}$ . Then, for any  $s_i \in S$ , we use the CFPU

algorithm to obtain  $\Upsilon(U_i, hp_i, t_i^h)$  and  $E_{net}^i$ . Finally, we obtain  $U = \bigcup_{s_i \in S} U_i \cup U_c$ ,  $Q = \bigcup_{s_i \in S} hp_i, T = \bigcup_{s_i \in S} t_i^h \text{ and } E_{net} = \sum_{i=1}^n E_{net}^{\rho_i} + \sum_{i=0}^{n-1} E_{net}^{\rho_i, \rho_{i+1}} + E_{net}^{\rho_n, \rho_0};$ In the second step, we update U, Q, T and  $E_{net}$  to obtain the flight plan

 $\Phi(U, Q, T, D_f)$  and D. Firstly, we let  $S' = \{s_{\rho_0}, s_{\rho_1}, \cdots, s_{\rho_n}\}$  be the ordered set of sensors visited by U from  $s_0$  to  $s_0$ . Secondly, we repeat executing the following steps when  $E_{net} > E$ .

- 1) For each  $s_{\rho_i} \in S' \setminus \{s_{\rho_0}\}$ , we compute  $\Lambda_{\rho_i} = \frac{V_{\rho_i}}{E_{net}^{\rho_i 1, \rho_i} + E_{net}^{\rho_i, \rho_i + 1} + E_{net}^{\rho_i} E_{net}^{\rho_i 1, \rho_{i+1}}}$ . 2) Let  $\Lambda_{\min} = \min\{\Lambda_{\rho_1}, \Lambda_{\rho_2}, \dots, \Lambda_{\rho_{|S'|-1}}\}$ ,  $s_{\rho_X} = arc(\Lambda_{\min})$ ,  $S' = S' \setminus \{s_{\rho_X}\}$ .
- 3) Set  $U_c = U_c \setminus \{(sc_{\rho_{i-1}}, sc_{\rho_i}), (sc_{\rho_i}, sc_{\rho_{i+1}})\}, U_c = U_c \cup \{(sc_{\rho_{i-1}}, sc_{\rho_{i+1}})\}.$ 4) Use the CFPU algorithm to obtain  $E_{net}^{\rho_{i-1}}, E_{net}^{\rho_{i+1}}, \Upsilon(U_{\rho_{i-1}}, hp_{\rho_{i-1}}, t_{\rho_{i-1}}^h), \Upsilon(U_{\rho_{i+1}}, t_{\rho_{i-1}}^h)$
- $hp_{\rho_{i+1}}, t^h_{\rho_{i+1}}).$
- 5) Set  $U = \bigcup_{s_i \in S' \setminus \{s_{\rho_0}\}} U_i \cup U_c$ ,  $Q = \bigcup_{s_i \in S' \setminus \{s_{\rho_0}\}} hp_i$ ,  $T = \bigcup_{s_i \in S' \setminus \{s_{\rho_0}\}} t_i^h$ .
- 6) Let  $S' = \{s_{\rho_0}, s_{\rho_1}, \dots, s_{\rho_{|S'|-1}}\}$  be the ordered set of sensors visited by U from  $s_0$ to  $s_0, U_c = sc_{\rho_0} \to sc_{\rho_1} \to \dots \to sc_{\rho_{|S'|-1}} \to sc_{\rho_0}$  and  $E_{net} = \sum_{i=1}^{|S'|-1} E_{net}^{\rho_i} + \sum_{i=0}^{|S'|-2} E_{net}^{\rho_i,\rho_{i+1}} + E_{net}^{\rho_{|S'|-1},\rho_0}$ .

Finally, we can obtain  $D = \sum_{s_i \in S' \setminus \{s_{oo}\}} V_i$  and  $D_f = D - \sum_{h p_i \in Q} \frac{1}{2} t_i^h W \log_2(1 + C_i)$  $\frac{\gamma_0 P_w}{d^{\alpha}(s_i,hp_i)}).$ 

# 5 Simulation

In this section, we evaluate the performance of the DCMSA algorithm by extensive simulation experiments on several key performance metrics under different settings. We implement the code using MATLAB 2019b and Java programming.

All results are averaged over 100 random instances. Table 1 gives the values of some constant parameters used in every instance.

## 5.1 An example for the DCMSA algorithm

As an example shown in Fig. 3, we set the configurations as n = 30, m = 40, R = 50m, H = 40 m, E = 200,000 J, W = 800 KB/s,  $100 \le V_i \le 200$  KB for any  $s_i \in S$ , and the other parameters are shown in Table 1. After executing the DCMSA algorithm for the instance, we can obtain the flight path U in the three dimensional space as shown in Fig. 3a and its top view is shown as Fig. 3b, where the purple zones denote the set of sensors, the cubes represent the set of obstacles, the red lines are the flight paths of UAV.

## 5.2 Simulations for the DCMSA algorithm

In the following, we evaluate the impact of the different parameter settings on the Data Collection Rate(DCR) that is the proportion of D obtained by DCMSA and  $\sum_{s \in S} V_i$ .

Notation	Physical meaning	Value
$d_i^o$	Buffer distance of $o_j$ in m	2
$l_i^o$	Length of $o_j$ in m	[50,100]
$w_i^o$	Width of $o_j$ in m	[50,100]
$h_i^o$	Height of $o_j$ in m	[30,150]
γο	Reference SNR at transmission distance 1 m in dB	80
$\eta_s$	Energy conversion efficiency	0.4
$A_s$	Solar panel area in m <sup>2</sup>	0.1
$G_s$	Average solar radiation	1367
$\alpha_s$	Maximum value of atmospheric transmittance	0.8978
$\beta_s$	Atmospheric extinction coefficient	0.2804
$\delta_s$	Scale height of the earth	8000
$P_0$	Blade power	14.7517
$P_1$	Induced power	41.5409
$v_r$	Tip speed of the rotor blade	80
$v_0$	The average rotor-induced velocity	5.0463
$d_0$	The fuselage drag ratio	0.5009
ρ	Air density in kg/m <sup>3</sup>	1.225
S	Rotor solidity	0.1248
Α	Rotor disc area in m <sup>2</sup>	0.1256

 Table 1
 Some constant parameters



Fig. 3 The flight of UAV for a given instance obtained by DCMA algorithm

In Fig. 4, we illustrate the performance of the DCMSA algorithm when we set the detection area as  $5000 \text{ m} \times 5000 \text{ m}$ , m = 40, R = 100 m, W = 800 KB/s,  $\alpha = 2$ ,  $P_w = 10 \text{ W}$ ,  $20 \le V_i \le 25 \text{ MB}$  for any  $s_i \in S$ , E = 700,000 J, n = 100, 150, 200, 250, 300 in Fig. 4a and change *H* from 10 to 100 m. Figure 4a measures the impact of *H* on the DCR, which shows that the DCR decreases with the increasing of the flight altitude *H* since the flight time of UAV in the data collection area of each sensor becomes shorter and the data transmission rate decreases as *H* increases.

At the same time, since the UAV doesn't have enough energy to collect all the data in the WSN, the DCR decreases with the increasing of the number of sensors n.



Fig. 4 Simulations by changing H from 10 to 100 m under different n



Fig. 5 Simulations by changing  $V_i$  from [5,10] to [45,50] MB under different W

In Fig. 4b, the DCR when the UAV is charged by solar is obviously better than that without charging, and the average DCR of charging is 9.525% higher than that of non-charging when n = 100, as shown in Fig. 4b.

In Fig. 5, we illustrate the performance of the DCMA algorithm when we set the detection area as  $5000 \text{ m} \times 5000 \text{ m}$ , n = 100, R = 50 m,  $P_w = 10 \text{ W}$ , m = 40, H = 40 m,  $\alpha = 2$ , E = 700,000 J, W = 200,400,600,800,1000 KB/s and change  $V_i$  from [5,10] to [45,50] MB for any  $s_i \in S$ . Figure 5a shows that the DCR decreases with the increasing of the data volume of sensors. This is because the UAV needs to consume more energy on hovering points to collect as the amount of data increases. We also observe that the DCR increases with the increasing of the value of the bandwidth. This is because the efficiency of the data collection is improved, and the flight paths within data collection area of sensors are optimized. The DCR when the UAV is charged by solar is obviously better than that without charging, and the average DCR of charging is 3.744% higher than that of non-charging when W = 200 KB/s, as shown in Fig. 5b.

In Fig. 6, we illustrate the performance of the DCMA algorithm as we set n = 100, m = 40, R = 50 m, H = 40 m, W = 1000 KB/s,  $P_w = 10$  W,  $20 \le V_i \le 25$  MB for any  $s_i \in S$ , E = 600,000 J,  $A = 2000 \times 2000$  m,  $3000 \times 3000$  m,  $4000 \times 4000$  m,  $5000 \times 5000$  m,  $6000 \times 6000$  m in Fig. 6a and change  $\alpha$  from 2.0 to 2.9. We can find that the DCR decreases with the increasing of  $\alpha$  in Fig. 6a since as the data transmission



**Fig. 6** Simulations by changing  $\alpha$  from 2.0 to 2.9 under different  $\mathcal{A}$ 

rate decreases, it needs more time on the hovering points to collect data, which will consume additional energy. At the same time, since the flight energy consumption of UAV increases as the size of the detection area increases, the DCR decreases with the increasing of the area  $\mathcal{A}$ . Figure 6b shows that the DCR when the UAV is charged by solar is obviously better than that without charging, and the average DCR of charging is 5.771% higher than that of non-charging when  $\mathcal{A} = 2000 \times 2000 \text{ m}$ .

#### 5.3 Performance comparison of different algorithms

In this subsection, we compare the performance of our algorithm DCMSA with other two algorithms MSTA and Greedy to verify the effective of the proposed algorithm.

The MSTA algorithm consists of the following steps: (1) construct a auxiliary graph G'(SC, EC, WC) as shown in Algorithm 2; (2) construct a minimum spanning tree  $T'_G$  from G'(SC, EC, WC); (3) obtain the hamiltonian circuit  $U_c$  by doubling all edges of  $T'_G$ ; (3) execute the Algorithms 3 and 4 successively to obtain the flight plan  $\Phi(U, Q, T, D_f)$  and D.

Initially, we set  $s_i = s_0$  and D = 0, where  $s_i$  represents the initial position of UAV. The Greedy algorithm repeats the following steps until the remaining energy of UAV can not arrive the next sensor and return to the base station:(1) compute the amount of data collected per unit of energy  $\Lambda_j = \frac{V_j}{E_{net}^{i,j} + E_{net}^{j} + E_{net}^{j,0}}$  for each  $s_j \in S$ ; (2)  $\Lambda_j = \max{\{\Lambda_k | s_k \in S\}}$  and  $s_j = arc(\Lambda_j)$ ; (3) update the energy of UAV as  $E = E - (E_{net}^{i,j} + E_{net}^{j}), D = D + V_j, s_i = s_j$ , and  $S = S \setminus \{s_j\}$ ;

In Fig. 7a, we compare the performance of three algorithms when we set the detection area as 4000 m × 4000 m, R = 50 m,  $P_w = 10$  W, m = 40, H = 40 m, W = 1000 KB/s,  $\alpha = 2$ ,  $100 \le V_i \le 200$  KB for any  $s_i \in S$ , E = 250,000 J and change *n* from 30 to 70. Figure 7a shows that the proposed algorithm outperforms the other two algorithms. We can find that the average performance of DCMSA algorithm is about 11.522% higher than MSTA algorithm, and about 7.915% higher than Greedy algorithm.





rithms by varying the number of sensors n. rithms as the bandwidth W grows.

(a) Performance comparison of three algo- (b) Performance comparison of three algo-



(c) Performance comparison of three algo-(d) Performance comparison of three algorithms by changing the data volume of sen- rithms with the different detection area  $\mathcal{A}$ . sors  $V_i$ .

**Fig. 7** Performance comparison of three algorithms by varying  $n, W, V_i, A$ 

In Fig. 7b, we compare the performance of three algorithms as we set the detection area as  $4000 \text{ m} \times 4000 \text{ m}$ , n = 50, R = 50 m,  $P_w = 10 \text{ W}$ , m = 40, H = 40 m,  $\alpha = 2, 25 \le V_i \le 30$  MB for any  $s_i \in S, E = 500,000$  J and change W from 100 to 1000 KB/s. Figure 7b shows that DCMSA algorithm is superior to the other two algorithms. The average performance of DCMSA algorithm is about 5.448% higher than MSTA algorithm, and about 8.006% higher than Greedy algorithm.

In Fig. 7c, we compare the performance of three algorithms when we set the detection area as  $4000 \text{ m} \times 4000 \text{ m}$ , n = 50, R = 50 m,  $P_w = 10 \text{ W}$ , m = 40, H = 40m, W = 500 KB/s,  $\alpha = 2$ , E = 350,000 J and change  $V_i$  from [5,10] to [45,50] MB for any  $s_i \in S$ . Figure 7c shows that DCMSA algorithm outperforms the MSTA and Greedy algorithms. We can observe that the average performance of DCMSA

algorithm is about 4.247% higher than MSTA algorithm, and about 4.083% higher than Greedy algorithm.

In Fig. 7d, we compare the performance of three algorithms as we set n = 50, R = 50 m,  $P_w = 10$  W, m = 40, H = 40 m, W = 800 KB/s,  $\alpha = 2,200 \le V_i \le 300$  KB for any  $s_i \in S$ , E = 300,000 J and change the detection area  $\mathcal{A}$  from 4000 m × 4000 m to 8000 m × 8000 m. Figure 7d shows that DCMSA algorithm outperforms the other two algorithms. The average performance of DCMSA algorithm is about 9.476% higher than MSTA algorithm, and about 4.352% higher than Greedy algorithm.

## 6 Conclusion

In this paper, we investigate the Data Collection Maximization based on Solar-powered UAV(DCMS) problem in a wireless sensor network with obstacles in urban environment, which focuses on finding an optimal flight plan to maximize the data collection volume of UAV from WSN and enable the UAV to return to the base station before running out its energy. Then we prove that the DCMS problem is NP-hard. To solve the DCMS problem, we propose the BOFA algorithm to bypass obstacles, the AGFP algorithm to compute the flight path connecting all data collection areas in WSN and the CFPU algorithm to optimize the flight trajectory of UAV in data collection area of each sensor. Finally, we propose an approximation algorithm DCMSA to solve the DCMS problem based on the above proposed three algorithms, and verify the effectiveness of the proposed algorithm with a large of simulations.

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# Declarations

**Conflict of interest** The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper

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